

Compiler Design

Bottom-up Parser (I)

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Bottom-up parsing and reverse rightmost derivation

- A derivation consists of a series of rewrite steps
- A bottom-up parser builds a derivation by working from the input sentence back toward the start symbol S

$$S \Rightarrow \gamma_0 \Rightarrow \gamma_1 \Rightarrow \gamma_2 \Rightarrow ... \Rightarrow \gamma_{n-1} \Rightarrow \gamma_n \Rightarrow sentence$$
bottom-up

In terms of the parse tree, this is working from leaves to root

- Nodes with no parent in a partial tree form its upper fringe
- Since each replacement of β with A shrinks the upper fringe, we call it a *reduction*.

Finding Reductions

(handles)

* Parser must find a substring β of the tree's frontier

- Matches some production $A \to \beta$ that occurs as one step in the rightmost derivation
- Informally, we call this substring β a handle

Formally,

- A *handle* of a right-sentential form γ is a pair $\langle A \rightarrow \beta, k \rangle$
 - $A \rightarrow \beta \in P$
 - k is the position in γ of β 's rightmost symbol.
- If $\langle A \rightarrow \beta, k \rangle$ is a handle, then replace β at k with A

Handle pruning

- The process of discovering a handle & reducing it to the appropriate lefthand side (non-terminal) is called handle pruning
- Because γ is a right-sentential form, the substring to the right of a handle contains only terminal symbols

Bottom-Up Parser Example

Handles for rightmost derivation of x - 2 * y

The expression grammar

	The exp	ress	ion grammar	Prod'n.	Sentential Form	Handle
1	Goal	\rightarrow	Expr		Goal	_
2	Expr	\rightarrow	Expr + Term	1	Expr	1,1
3			Expr - Term	3	Expr - Term	3,3
4			Term	5	Expr-Term * Factor	5,5
5	Term	\rightarrow	Term * Factor	9	Expr - Term * <id,y></id,y>	9,5
6			Term / Factor	7	Expr - Factor * <id,y></id,y>	7,3
7			Factor	8	Expr - <num, 2=""> * <id, y=""></id,></num,>	8,3
8	Factor	\rightarrow	<u>number</u>	4	<i>Term</i> - <num,2> * <id,y></id,y></num,2>	4,1
9			<u>id</u> ,	7 7	Factor - <num,2> * <id,y></id,y></num,2>	7,1
10			<u>(Expr)</u>	9	<id,x> - <num,2> * <id,y></id,y></num,2></id,x>	9,1
				•		

Reverse rightmost derivation (RRD)

Handles are specified in blue

One of Bottom-up Parsers

Shift-reduce parser

```
push INVALID
token \leftarrow next\_token()
repeat until (top of stack = Goal and token = EOF)
   if the top of the stack can reduce using a handle \langle A \rightarrow \beta.k \rangle then
        // reduce \beta to A
          pop |\beta| (=k) symbols off the stack
          push A onto the stack
   else if (token != EOF) then
                                                               How do errors show up?
        // shift

    failure to find a handle

          push token
                                                               hitting EOF & needing to
          token \leftarrow next\_token()
   else // need to shift, but out of input
                                                                shift (final else clause)
          report an error
                                                               Either generates an error
```

Stack	Input	Handle	Action
\$ \$ <u>id</u>	<u>id – num * id</u>	none	shift
\$ <u>id</u>	<u> </u>		

- 1. Shift until the top of the stack is the right end of a handle
- 2. Find the left end of the handle & reduce

Stack	Input	Handle	Action
\$ \$ <u>id</u>	<u>id – num * id</u>	none	shift
\$ <u>id</u>	<u>– num * id</u>	9,1	red. 9
\$ Factor	<u>– num * id</u>	7,1	red. 7
\$ Term	<u>– num * id</u>	4,1	red. 4
\$ Expr	<u>– num * id</u>		

- 1. Shift until the top of the stack is the right end of a handle
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Stack	Input	Handle	Action
\$ \$ <mark>id</mark>	<u>id – num * id</u>	none	shift
^{ড়} । <u>u</u> \$ <i>Factor</i>	<u>– num * id</u> <u>– num * id</u>	9,1 7,1	red. 9 red. 7
\$ Term	<u>– num * id</u>	4,1	red. 4
\$ Expr	<u>– num * id</u>	none	shift
\$ Expr_	<u>num * id</u> * id	none	shift
\$ Expr_ num	<u>* id</u>		

- 1. Shift until the top of the stack is the right end of a handle
- 2. Find the left end of the handle & reduce

Stack	Input	Handle	Action
\$	<u>id – num * id</u>	none	shift
\$ <u>id</u>	<u>– num * id</u>	9,1	red. 9
\$ Factor	<u>– num * id</u>	7,1	red. 7
\$ Term	<u>– num * id</u>	4,1	red. 4
\$ Expr	<u>– num * id</u>	none	shift
\$ Expr_	<u>num * id</u>	none	shift
\$ Expr_ num	<u>*</u> <u>id</u>	8,3	red. 8
\$ Expr_ Factor	<u>* id</u>	7,3	red. 7
\$ Expr_ Term	<u>*</u> <u>id</u>		

- 1. Shift until the top of the stack is the right end of a handle
- 2. Find the left end of the handle & reduce

Stack	Input	Handle	Action
\$	<u>id – num * id</u>	none	shift
\$ <u>id</u>	<u>– num * id</u>	9,1	red. 9
\$ Factor	<u>– num * id</u>	7,1	red. 7
\$ Term	<u>– num * id</u>	4,1	red. 4
\$ Expr	<u>– num * id</u>	none	shift
\$ Expr_	<u>num * id</u>	none	shift
\$ Expr_ num	<u>* id</u>	8,3	red. 8
\$ Expr_ Factor	<u>* id</u>	7,3	red. 7
\$ Expr_ Term	<u>*</u> <u>id</u>	none	shift
\$ Expr <u>-</u> Term <mark>*</mark>	<u>id</u>	none	shift
\$ Expr_ Term * id			

- 1. Shift until the top of the stack is the right end of a handle
- 2. Find the left end of the handle & reduce

Stack	Input	Handle	Action
\$	<u>id – num * id</u>	none	shift
\$ <u>id</u>	<u>– num * id</u>	9,1	red. 9
\$ Factor	<u>– num * id</u>	7,1	red. 7
\$ Term	<u>– num * id</u>	4,1	red. 4
\$ Expr	<u>– num * id</u>	none	shift
\$ Expr_	<u>num * id</u>	none	shift
\$ Expr_ num	<u>*</u> <u>id</u>	8,3	red. 8
\$ Expr_ Factor	<u>*</u> <u>id</u>	7,3	red. 7
\$ Expr_ Term	* <u>id</u>	none	shift
\$ Expr_ Term *	<u>id</u>	none	shift
\$ Expr_ Term * id		9,5	red. 9
\$ Expr = Term * Factor		5,5	red. 5
\$ Expr_ Term		3,3	red. 3
\$ Expr		1,1	red. 1
\$ Goal		none	accept

5 shifts +
9 reduces +
1 accept

- 1. Shift until the top of the stack is the right end of a handle
- 2. Find the left end of the handle within stack & reduce

Example

Stack	Input	Action	
\$	<u>id – num * id</u>	shift	(Goal)
\$ <u>id</u>	<u>– num * id</u>	red. 9	Goal
\$ Factor	<u>– num * id</u>	red. 7	
\$ Term	<u>– num * id</u>	red. 4	(Expr)
\$ Expr	<u>– num * id</u>	shift	
\$ Expr_	<u>num * id</u>	shift	Expr - Term
\$ Expr_ num	<u>* id</u>	red. 8	LADI) - Term
\$ Expr_ Factor	<u>* id</u>	red. 7	
\$ Expr_ Term	<u>* id</u>	shift	(Term) (Term) * (Fact.)
\$ Expr_ Term *	<u>id</u>	shift	
\$ Expr_ Term * id		red. 9	(Fact) (Fact) <id,y></id,y>
\$ Expr = Term * Factor		red. 5	(Fact.) (Fact.) <io,y></io,y>
\$ Expr = Term		red. 3	↓ ↓
\$ Expr		red. 1	<id,x> <num,<mark>2></num,<mark></id,x>
\$ Goal		accept	

bottom-up building

Shift-reduce Parsing

- Shift reduce parsers are easily built and easily understood
- A shift-reduce parser has just four actions
 - Shift next word is shifted onto the stack
 - Reduce right end of handle is at top of stack
 - Locate left end of handle within the stack
 - Pop handle off stack & push appropriate //s
 - Accept stop parsing & report success
 - Error call an error reporting/recovery routine

- Handle finding is key
- handle is on stack
- finite set of handles
- \Rightarrow use a DFA!

- Critical Question: How can we know when we have found a handle without generating lots of different derivations?
 - Answer: we use look ahead in the grammar along with tables produced as the result of analyzing the grammar.
 - LR(1) parsers build a DFA that runs over the stack & finds them

Another Bottom-Up Parser

LR(1) Parsers

- LR(1) parsers are table-driven, shift-reduce parsers that use a limited right context (1 token) for handle recognition
- LR(1) parsers recognize languages that have an LR(1) grammar

Informal definition:

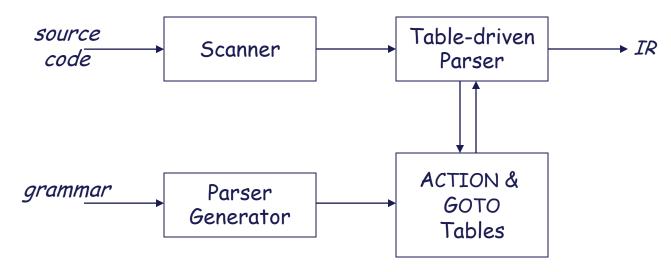
A grammar is LR(1) if, given a rightmost derivation

$$S \Rightarrow \gamma_0 \Rightarrow \gamma_1 \Rightarrow \gamma_2 \Rightarrow ... \Rightarrow \gamma_{n-1} \Rightarrow \gamma_n \Rightarrow sentence$$

- We can
 - 1. isolate the handle of each right-sentential form γ_i , and
 - 2. determine the production with which to reduce, by scanning γ_i from left-to-right, going at most 1 symbol beyond the right end of the handle of γ_i

LR(1) Parsers

A table-driven LR(1) parser looks like



- Tables <u>can</u> be built by hand
- However, this is a perfect task to automate

LR(1) Skeleton Parser

```
stack.push(INVALID); stack.push(s_0);
not_found = true;
token = scanner.next_token();
do while (not_found) {
     s = stack.top();
     if (ACTION[s,token] == "shift s<sub>next</sub>") then {
            stack.push(token); stack.push(S_{next});
            token ← scanner.next_token();
     else if (ACTION[s,token] == "reduce A \rightarrow \beta") then {
           stack.popnum(2*|\beta|); // pop 2*|\beta| symbols
           s = stack.top();
           stack.push(A); stack.push(GOTO[s,A]);
     else if ( ACTION[s,token] == "accept"
                            & token == EOF ) then {
           not found = false:
      else report a syntax error and recover;
report success;
```

The skeleton parser

- push tokens & NTs along with DFA states
- uses ACTION & GOTO tables (DFA)
- · does | words | shifts
- does |derivation| reductions
- · does 1 accept
- detects errors by failure of 3 other cases

LR(1) Parsers

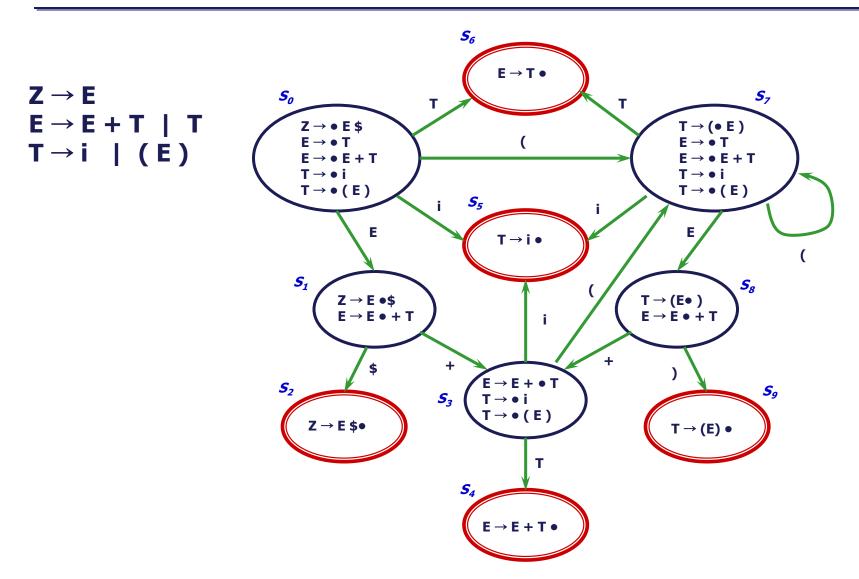
* How does this LR(1) stuff work?

- Unambiguous grammar ⇒ unique rightmost derivation
- Keep upper fringe on a stack
 - All active handles include top of stack (TOS)
 - Shift inputs until TOS is right end of a handle
- Language of handles is regular (finite)
 - Build a handle-recognizing DFA
 - ACTION & GOTO tables encode the DFA

The Big Picture

- Model the state of the parser
- Use two functions goto(s, X) and closure(s)
 - goto() is analogous to move() in subset construction (NFA→DFA)
 - closure() adds information to form a state
- Build up the states and transition functions of the DFA
- Use this information to fill in the ACTION and GOTO tables

LR(0) example



Summary

Bottom-up parser

- Reverse rightmost derivation
- Handle pruning, reduction

Shift-reduce parser

- Reduce if found a handle in stack
- Otherwise, shift a token (push on to stack)

* LR(1) parser

- Discover handles from DFA
- ACTION, GOTO tables from DFA