

A Journey in Functional Programming

An introduction to Haskell

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Section 1

Introduction - Syntax and Types

Haskell platform

A full comprehensive, development environment for Haskell¹².

Installation

- `$sudo apt-get install haskell-platform`

GHC (Great Glasgow Compiler): State of the art

GHCi A read-eval-print loop interpreter

Cabal Build/distribute/retrieve libraries

Haddock A high quality documentation generation tool for Haskell

¹<https://www.haskell.org/platform/index.html>

²<http://tryhaskell.org/>

Why Functional Programming? Why Haskell?

- ① Haskell's expressive power can improve productivity/understandability/maintanibility
 - Get best from compiled and interpreted languages
 - Can understand what complex library does
- ② Strong typed - Catches bugs at *compile time*
- ③ Powerful type inference engine
- ④ New Testing metologies
- ⑤ Automatic parallelization due to code purity

What really is Haskell?

Purely Functional language

- Functions are first-class object (same things as data)
- Deterministic - No Side Effect- same function call \Rightarrow same Output, EVER!
This *referential transparency* leaves room for compiler optimization and allow to mathematically prove correctness.
- **Evaluate expression** rather than execute instruction
- Function describes what data are, not what what to do to...
- Everything (variables, data structures...) is immutable

Haskell is Lazy

It won't execute anything until it is *really needed*

```
lazyFunction x y  
let f = x * (product [2..y])  
in if x==0 then 0 else f
```

f is never computed if $x = 0$.

- It is possible to define and work with infinite data structures
- Define new control structure just by defining a function.
- Reasoning about time/space complexity much more complicated



Hello World

Our First Program

Create a file *hello.hs* and compile with the followings

```
main = putStrLn "Hello World with Haskell"  
$ghc -o hello hello.hs
```

GHCi

Execute and play with GHCi by simply typing

```
reverse [1..10]  
:t foldl  
[1..]  
(filter (even) .reverse) [1..100]
```


Hello World - 2

Another example, the k^{th} Fibonacci number (type in GHCi):

```
let f a b k = if k==0 then a else f b (a+b) (k-1)
```

- Defines a recursive function f that takes a, b, k as parameters:
- Spaces are important. Are like function call operator $()$ in C-like languages.
- Wait, three space in $f a b k$: 3 function calls? YES!. **Every function in Haskell officially only takes one parameter.**
- f infact has type

```
f :: Integer -> (Integer -> (Integer -> Integer))
```

i.e. a function that takes an integer and return (the $->$) a function that takes an integer and return ...

```
f 0 :: Integer -> (Integer -> Integer)
```

```
f 0 1 :: Integer -> Integer
```

```
f 0 1 10 :: Integer
```

Hello World - 3

Number of distinct powers counting (Project Euler 29)

Consider all integer combinations of a, b for $2 \leq a, b \leq 100$: how many distinct terms are in the sequence generated by a^b ?

$$2^2 = 4, 2^3 = 8, 2^4 = 16, 2^5 = 32$$

$$3^2 = 9, 3^3 = 27, 3^4 = 81, 3^5 = 243$$

$$4^2 = 16, 4^3 = 64, 4^4 = 256, 4^5 = 1024$$

$$5^2 = 25, 5^3 = 125, 5^4 = 625, 5^5 = 3125$$

Naïve solution

```
np :: Integer -> Integer -> Int
np a b = let l = [a^b | a<-[2..a], b<-[2..b]]
  in length (remDup l)
  where
    remDup = (map head . group . sort)
```

Hello World - 3

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```

Statically Typed

- Haskell is strictly typed
- Helps in thinking and express program structure
- **Turns run-time errors into compile-time errors.** If it compiles, it must be correct is mostly true³.

Abstraction: Every idea, algorithm, and piece of data should occur exactly once in your code.

Haskell features as parametric polymorphis, typeclasses high-order functions greatly aid in fighting repetition.

³It is still quite possible to have errors in logic even in a type-correct program

What really is Haskell?

C-like vs Haskell

Code as the one that follows

```
int acc = 0;
for ( int i = 0; i < lst.length; i++ )
    acc = acc + 3 * lst[i];
```

is full of low-level details of iterating over an array by keeping track of a current index. It much elegantly translates in:

```
sum (map (*3) lst)
```

Other examples:

```
partition (even) [49, 58, 76, 82, 83, 90]
```

```
--prime number generation
```

```
let pgen (p:xs) = p : pgen [x|x <- xs, x `mod` p > 0]
```

```
take 40 (pgen [2..])
```

Section 2

Basics I

Syntax Basics

- Arithmetic and Boolean algebra works as expected

```
v1 = 12
```

```
v2 = mod (v1+3) 10
```

```
v3 = not $ True || (v2>=v1) --not (True || (v2>=v1))
```

- Function definition is made up of two part: type and body.

The body is made up of several *clause* that are evaluated (pattern matched) **top to bottom**.

```
1 exp _ 0 = 1
```

```
2 exp 0 _ = 0
```

```
3 exp a b = a * (exp a (b-1))
```

What if we swap line 2 and 3?

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```
5 exp 0 _ = 0
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6 exp a b = a * (exp a (b-1))
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What if we swap line 2 and 3?

- Comments:

```
--this is an inline comment
```

```
{-
```

```
All in here is comment
```

```
-}
```


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```
7 exp _ 0 = 1
```

```
8 exp 0 _ = 0
```

```
9 exp a b = a * (exp a (b-1))
```

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```
-}
```

Guards, where, let

- Guards, let and where constructs

```

1 fastExp :: Integer -> Integer -> Integer
2 fastExp _ 0 = 1
3 fastExp a 1 = a
4 fastExp a b
5   | b < 0 = undefined
6   | even b = res*res
7   | otherwise = let next=(fastExp a (b-1)) in (a * next)
8   where res=(fastExp a (div b 2))

```

Suppose we execute *fastExp* 2 7. The call stack would be

- fastExp 2 7 line 7 pattern match
- fastExp 2 6 line 6 pattern match

⁴Here for more informations: https://wiki.haskell.org/Let_vs_Where

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In contrast to where, let are expressions and can be used anywhere⁴.

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If, case

- if construct works as expected

```
1 div' n d = if d==0 then Nothing else Just (n/d)
```

- case construct

Useful when we don't wish to define a function every time we need to do pattern matching.

```
f p11 ... p1k = e1
```

```
...
```

```
f pn1 ... pnk = en
```

--where each p_{ij} is a pattern, is semantically equivalent

```
f x1 x2 ... xk = case (x1, ..., xk) of
```

```
(p11, ..., p1k) -> e1
```

```
...
```

```
(pn1, ..., pnk) -> en
```

All patterns of a function return the same type hence all the RHS of the case have the same type

case construct: example

case construct example

Pattern match “outside” the function definition. Note that all the cases return the same type (a list of b ’s in this case)

```
cE :: (Ord a) => a -> a -> [b]
cE a b xs = case (a `compare` b, xs) of
    (_, []) -> []
    (LT, xs) -> init xs
    (GT, xs) -> tail xs
    (EQ, xs) -> [head xs]
```

Ranges

ranges

Shortcut for listing stuff that can be enumerated. What if we need to test if a string contains a letter up to the lower case `j`? (Explicitly list all the letters is not the correct answer).

```
['a'..'j'] -- results in "abcdefghij" (String are [Char])
```

It work even in construction infinite list

```
[1,3..] -- results in [1,3,5,7,9,11,13,15.....]
```

and because of laziness we can (safely) do

```
take 10 [1,3..]
```

List Comprehension

list comprehension

It is a familiar concept for those who already have some experience in python. It resembles the mathematical set specification. For instance, let's compute the list of the factorial of the natural numbers

```
[product [2..x] | x<-[1..]]
```

More examples:

```
[[2..x*2] | x<-[1..]]
```

```
[filter (even) [2..x] | x<-[1..]]
```

```
--:m Data.Char (ord)
```

```
[let p=y*x in if even p then (negate p) else  
 (p*2) | x<-[1..10], y<-(map ord ['a'..'z'])]
```

```
--:m Data.List (nub)
```

```
nub $ map (\(x,y,z) -> z) [(a,b,c) | a<-[1..20], b<-[1..20],  
 c<-[1..20], a^2+b^2==c^2, a+b+c>10]
```