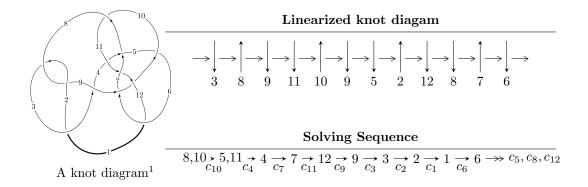
# $12n_{0637} \ (K12n_{0637})$



## Ideals for irreducible components $^2$ of $X_{\mathtt{par}}$

<sup>&</sup>lt;sup>1</sup>The image of knot diagram is generated by the software "**Draw programme**" developed by Andrew Bartholomew(http://www.layer8.co.uk/maths/draw/index.htm#Running-draw), where we modified some parts for our purpose(https://github.com/CATsTAILs/LinksPainter).

$$\begin{split} I_1^u &= \langle -35223725986u^{21} + 30523664755u^{20} + \dots + 210473051795b + 25821213245, \\ 740868672496u^{21} - 766689885741u^{20} + \dots + 210473051795a - 869880690251, \\ u^{22} - u^{21} + \dots - u + 1 \rangle \\ I_2^u &= \langle 3.78529 \times 10^{20}u^{19} - 4.63105 \times 10^{20}u^{18} + \dots + 8.62031 \times 10^{21}b - 2.24738 \times 10^{21}, \\ 2.73069 \times 10^{22}u^{19} - 2.50595 \times 10^{22}u^{18} + \dots + 8.62031 \times 10^{21}a - 1.80097 \times 10^{23}, \ u^{20} - u^{19} + \dots - 7u + 1 \rangle \\ I_3^u &= \langle -3.35706 \times 10^{35}u^{33} - 7.63609 \times 10^{35}u^{32} + \dots + 5.24183 \times 10^{36}b - 4.09915 \times 10^{36}, \\ 1.95717 \times 10^{37}u^{33} + 4.09915 \times 10^{36}u^{32} + \dots + 5.24183 \times 10^{36}a - 6.08409 \times 10^{37}, \ u^{34} - 9u^{32} + \dots - 5u + 1 \\ I_4^u &= \langle 16685766983482u^{15} + 6555188230121u^{14} + \dots + 453436720809281b + 250672039562051, \\ -35828884147u^{15} - 26710704549u^{14} + \dots + 766837175819a + 930772601969, \\ u^{16} - u^{15} + \dots - 20u + 13 \rangle \\ I_5^u &= \langle 3.61106 \times 10^{67}u^{31} + 1.33112 \times 10^{67}u^{30} + \dots + 5.05264 \times 10^{70}b - 7.80220 \times 10^{69}, \\ -2.81341 \times 10^{59}u^{31} - 1.32370 \times 10^{59}u^{30} + \dots + 1.01984 \times 10^{63}a + 2.59788 \times 10^{62}, \\ u^{32} + u^{31} + \dots - 1290u + 1501 \rangle \\ I_6^u &= \langle b - u, \ a, \ u^4 + u^3 + 3u^2 + 2u + 1 \rangle \\ I_7^u &= \langle 11u^7 + 19u^6 + 58u^5 + 65u^4 - 6u^3 - 34u^2 + 2b + 9u - 28, \ u^7 + u^6 + 4u^5 + 2u^4 - 5u^3 - 3u^2 + 2a + 3u - 3, \\ u^8 + u^7 + 4u^6 + 2u^5 - 5u^4 - 3u^3 + 3u^2 - 3u + 2 \rangle \\ I_8^u &= \langle b, \ a + 1, \ u + 1 \rangle \end{aligned}$$

\* 8 irreducible components of  $\dim_{\mathbb{C}} = 0$ , with total 137 representations.

 $<sup>^2</sup>$  All coefficients of polynomials are rational numbers. But the coefficients are sometimes approximated in decimal forms when there is not enough margin.

$$I. \\ I_1^u = \langle -3.52 \times 10^{10} u^{21} + 3.05 \times 10^{10} u^{20} + \dots + 2.10 \times 10^{11} b + 2.58 \times 10^{10}, \ 7.41 \times 10^{11} u^{21} - 7.67 \times 10^{11} u^{20} + \dots + 2.10 \times 10^{11} a - 8.70 \times 10^{11}, \ u^{22} - u^{21} + \dots - u + 1 \rangle$$

(i) Arc colorings

$$a_{8} = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{5} = \begin{pmatrix} -3.52002u^{21} + 3.64270u^{20} + \dots - 40.0291u + 4.13298 \\ 0.167355u^{21} - 0.145024u^{20} + \dots + 4.64270u - 0.122682 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 1 \\ u^{2} \end{pmatrix}$$

$$a_{4} = \begin{pmatrix} -3.52002u^{21} + 3.64270u^{20} + \dots - 39.0291u + 4.13298 \\ 0.167355u^{21} - 0.145024u^{20} + \dots + 4.64270u - 0.122682 \end{pmatrix}$$

$$a_{7} = \begin{pmatrix} -7.95997u^{21} + 8.71460u^{20} + \dots - 67.9417u + 11.7340 \\ 0.832645u^{21} - 0.854976u^{20} + \dots + 13.3573u - 0.877318 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} -3.13298u^{21} + 0.612962u^{20} + \dots - 16.2045u - 19.8962 \\ 0.122682u^{21} + 0.0446732u^{20} + \dots + 0.612962u + 3.52002 \end{pmatrix}$$

$$a_{9} = \begin{pmatrix} 7.72374u^{21} - 3.11644u^{20} + \dots + 40.9995u + 24.8315 \\ -0.754636u^{21} + 0.0893465u^{20} + \dots - 3.77408u - 7.95997 \end{pmatrix}$$

$$a_{3} = \begin{pmatrix} 2.10661u^{21} + 3.86613u^{20} + \dots + 4.19416u + 30.2779 \\ 4.12150u^{21} - 5.66719u^{20} + \dots + 21.5571u - 12.2542 \end{pmatrix}$$

$$a_{2} = \begin{pmatrix} 2.10661u^{21} + 3.86613u^{20} + \dots + 4.19416u + 30.2779 \\ 4.99760u^{21} - 7.47535u^{20} + \dots + 25.4233u - 18.2269 \end{pmatrix}$$

$$a_{1} = \begin{pmatrix} 2.98797u^{21} - 0.624862u^{20} + \dots + 15.5468u + 16.5435 \\ -0.145013u^{21} - 0.0118996u^{20} + \dots + 0.657635u - 3.35266 \end{pmatrix}$$

$$a_{6} = \begin{pmatrix} -3.35266u^{21} + 3.49767u^{20} + \dots - 35.3864u + 4.01030 \\ 0.167355u^{21} - 0.145024u^{20} + \dots + 4.64270u - 0.122682 \end{pmatrix}$$

#### (ii) Obstruction class = -1

(iii) Cusp Shapes  $= -\tfrac{1913935713454}{210473051795}u^{21} - \tfrac{1492818570442}{210473051795}u^{20} + \dots - \tfrac{6526154909884}{210473051795}u - \tfrac{14593217553892}{210473051795}u^{20} + \dots - \tfrac{1459321755389$ 

| Crossings                   | u-Polynomials at each crossing            |
|-----------------------------|---|
| $c_1$                       | $u^{22} + 8u^{21} + \dots + 160u + 64$    |
| $c_2, c_8$                  | $u^{22} + 6u^{21} + \dots + 32u + 8$      |
| $c_3$                       | $u^{22} - 6u^{21} + \dots - 5072u + 3880$ |
| $c_4, c_6, c_{10}$ $c_{12}$ | $u^{22} - u^{21} + \dots - u + 1$         |
| $c_5, c_{11}$               | $u^{22} - u^{21} + \dots - 16u + 10$      |
| $c_7, c_9$                  | $u^{22} - 9u^{21} + \dots - 15u + 19$     |

| Crossings                   | Riley Polynomials at each crossing                 |  |
|-----------------------------|--|--|
| $c_1$                       | $y^{22} + 12y^{21} + \dots + 28160y + 4096$        |  |
| $c_2, c_8$                  | $y^{22} + 8y^{21} + \dots + 160y + 64$             |  |
| $c_3$                       | $y^{22} + 16y^{21} + \dots + 18242976y + 15054400$ |  |
| $c_4, c_6, c_{10}$ $c_{12}$ | $y^{22} + 21y^{21} + \dots + 35y + 1$              |  |
| $c_5, c_{11}$               | $y^{22} + y^{21} + \dots + 624y + 100$             |  |
| $c_7, c_9$                  | $y^{22} - 9y^{21} + \dots - 187y + 361$            |  |

| Solutions to $I_1^u$      | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape          |
|---------------------------|---------------------------------------|---------------------|
| u = 0.251396 + 1.197270I  |                                       |                     |
| a = -0.727101 + 0.853670I | -1.69375 - 1.58224I                   | -2.92761 + 2.99168I |
| b = 0.733815 - 0.410169I  |                                       |                     |
| u = 0.251396 - 1.197270I  |                                       |                     |
| a = -0.727101 - 0.853670I | -1.69375 + 1.58224I                   | -2.92761 - 2.99168I |
| b = 0.733815 + 0.410169I  |                                       |                     |
| u = -0.439138 + 1.208940I |                                       |                     |
| a = -0.366754 + 0.753125I | 7.22176 + 4.64537I                    | -1.48411 - 2.36378I |
| b = 0.825819 + 0.642867I  |                                       |                     |
| u = -0.439138 - 1.208940I |                                       |                     |
| a = -0.366754 - 0.753125I | 7.22176 - 4.64537I                    | -1.48411 + 2.36378I |
| b = 0.825819 - 0.642867I  |                                       |                     |
| u = -0.100425 + 0.610392I |                                       |                     |
| a = -0.598286 - 0.326486I | -0.049452 + 1.407930I                 | -0.88049 - 5.93296I |
| b = 0.076424 + 0.802089I  |                                       |                     |
| u = -0.100425 - 0.610392I |                                       |                     |
| a = -0.598286 + 0.326486I | -0.049452 - 1.407930I                 | -0.88049 + 5.93296I |
| b = 0.076424 - 0.802089I  |                                       |                     |
| u = 0.311341 + 1.349370I  |                                       |                     |
| a = 0.386640 + 0.716640I  | 8.03816 + 1.82472I                    | -0.36555 - 2.90365I |
| b = -0.957311 + 0.438847I |                                       |                     |
| u = 0.311341 - 1.349370I  |                                       |                     |
| a = 0.386640 - 0.716640I  | 8.03816 - 1.82472I                    | -0.36555 + 2.90365I |
| b = -0.957311 - 0.438847I |                                       |                     |
| u = 0.70785 + 1.27677I    |                                       |                     |
| a = -0.942108 + 0.435063I | -2.15736 - 11.05600I                  | -5.86304 + 8.74726I |
| b = 0.985198 - 0.917340I  |                                       |                     |
| u = 0.70785 - 1.27677I    |                                       |                     |
| a = -0.942108 - 0.435063I | -2.15736 + 11.05600I                  | -5.86304 - 8.74726I |
| b = 0.985198 + 0.917340I  |                                       |                     |

| Solutions to $I_1^u$      | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape           |
|---------------------------|---------------------------------------|----------------------|
| u = -0.43272 + 1.42172I   |                                       |                      |
| a = 0.745026 + 0.586778I  | 2.42448 + 6.49307I                    | -0.75771 - 5.60630I  |
| b = -1.077150 - 0.571146I |                                       |                      |
| u = -0.43272 - 1.42172I   |                                       |                      |
| a = 0.745026 - 0.586778I  | 2.42448 - 6.49307I                    | -0.75771 + 5.60630I  |
| b = -1.077150 + 0.571146I |                                       |                      |
| u = -0.131155 + 0.475245I |                                       |                      |
| a = -1.59000 - 1.04889I   | -0.69331 + 1.97766I                   | -2.32963 - 3.06093I  |
| b = 0.069853 + 0.892314I  |                                       |                      |
| u = -0.131155 - 0.475245I |                                       |                      |
| a = -1.59000 + 1.04889I   | -0.69331 - 1.97766I                   | -2.32963 + 3.06093I  |
| b = 0.069853 - 0.892314I  |                                       |                      |
| u = 0.145985 + 0.422253I  |                                       |                      |
| a = 2.38098 - 1.30459I    | -2.79098 - 6.48658I                   | -4.59769 + 4.99587I  |
| b = -0.066959 + 0.920596I |                                       |                      |
| u = 0.145985 - 0.422253I  |                                       |                      |
| a = 2.38098 + 1.30459I    | -2.79098 + 6.48658I                   | -4.59769 - 4.99587I  |
| b = -0.066959 - 0.920596I |                                       |                      |
| u = 0.062233 + 0.424223I  |                                       |                      |
| a = 1.23180 - 2.37884I    | -4.30511 + 0.52403I                   | -12.36500 - 2.34222I |
| b = -0.029071 + 0.908159I |                                       |                      |
| u = 0.062233 - 0.424223I  |                                       |                      |
| a = 1.23180 + 2.37884I    | -4.30511 - 0.52403I                   | -12.36500 + 2.34222I |
| b = -0.029071 - 0.908159I |                                       |                      |
| u = -1.05080 + 1.58014I   |                                       |                      |
| a = 0.749692 + 0.219224I  | 7.00864 + 11.78040I                   | -2.49367 - 5.42252I  |
| b = -1.36686 - 1.21476I   |                                       |                      |
| u = -1.05080 - 1.58014I   |                                       |                      |
| a = 0.749692 - 0.219224I  | 7.00864 - 11.78040I                   | -2.49367 + 5.42252I  |
| b = -1.36686 + 1.21476I   |                                       |                      |

| Solutions to $I_1^u$      | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape          |
|---------------------------|---------------------------------------|---------------------|
| u = 1.17544 + 1.50294I    |                                       |                     |
| a = -0.769890 + 0.154115I | 5.9137 - 18.4120I                     | -4.00000 + 9.61591I |
| b = 1.30624 - 1.35244I    |                                       |                     |
| u = 1.17544 - 1.50294I    |                                       |                     |
| a = -0.769890 - 0.154115I | 5.9137 + 18.4120I                     | -4.00000 - 9.61591I |
| b = 1.30624 + 1.35244I    |                                       |                     |

 $\begin{matrix} I_2^u = \langle 3.79 \times 10^{20} u^{19} - 4.63 \times 10^{20} u^{18} + \dots + 8.62 \times 10^{21} b - 2.25 \times 10^{21}, \ 2.73 \times 10^{22} u^{19} - 2.51 \times 10^{22} u^{18} + \dots + 8.62 \times 10^{21} a - 1.80 \times 10^{23}, \ u^{20} - u^{19} + \dots - 7u + 1 \rangle \end{matrix}$ 

#### (i) Arc colorings

$$a_8 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{5} = \begin{pmatrix} -3.16774u^{19} + 2.90704u^{18} + \dots + 10.9832u + 20.8921 \\ -0.0439113u^{19} + 0.0537225u^{18} + \dots + 2.34279u + 0.260708 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 1 \\ u^{2} \end{pmatrix}$$

$$a_{4} = \begin{pmatrix} -3.16774u^{19} + 2.90704u^{18} + \dots + 11.9832u + 20.8921 \\ -0.0439113u^{19} + 0.0537225u^{18} + \dots + 2.34279u + 0.260708 \end{pmatrix}$$

$$a_{7} = \begin{pmatrix} -8.81122u^{19} + 7.79546u^{18} + \dots + 18.5918u + 54.1639 \\ -0.175015u^{19} + 0.186912u^{18} + \dots + 4.04373u + 1.27646 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} 3.92566u^{19} - 3.36351u^{18} + \dots + 33.8425u - 29.7066 \\ 0.0217085u^{19} - 0.0143026u^{18} + \dots + 0.00468521u - 0.781074 \end{pmatrix}$$

$$a_{9} = \begin{pmatrix} 2.88820u^{19} - 2.46456u^{18} + \dots + 26.3232u - 20.1143 \\ 0.0364007u^{19} - 0.0247875u^{18} + \dots + 0.0259089u - 0.598653 \end{pmatrix}$$

$$a_{1} = \begin{pmatrix} 1.64440u^{19} - 1.25672u^{18} + \dots + 38.9478u - 7.71164 \\ 0.0771122u^{19} - 0.0734388u^{18} + \dots + 0.753454u - 0.595866 \end{pmatrix}$$

$$a_{2} = \begin{pmatrix} 1.64440u^{19} - 1.25672u^{18} + \dots + 38.9478u - 7.71164 \\ 0.122553u^{19} - 0.0983998u^{18} + \dots + 1.82280u - 0.983543 \end{pmatrix}$$

$$a_{1} = \begin{pmatrix} 1.28627u^{19} - 1.10467u^{18} + \dots + 8.75002u - 13.9350 \\ -0.0118974u^{19} + 0.0110797u^{18} + \dots - 0.0513570u - 0.175015 \end{pmatrix}$$

$$a_{6} = \begin{pmatrix} -3.21165u^{19} + 2.96076u^{18} + \dots + 13.3259u + 21.1528 \\ -0.0439113u^{19} + 0.0537225u^{18} + \dots + 2.34279u + 0.260708 \end{pmatrix}$$

#### (ii) Obstruction class = -1

| Crossings                   | u-Polynomials at each crossing  |
|-----------------------------|---|
| $c_1$                       | $(u^{10} + 4u^9 + \dots - 12u + 16)^2$  |
| $c_2, c_8$                  | $ (u^{10} + 4u^9 + 10u^8 + 16u^7 + 19u^6 + 15u^5 + 6u^4 - 5u^3 - 11u^2 - 10u - 4)^2 $ |
| $c_3$                       | $(u^{10} - 4u^9 + \dots - 66u - 52)^2$  |
| $c_4, c_6, c_{10}$ $c_{12}$ | $u^{20} - u^{19} + \dots - 7u + 1$  |
| $c_5, c_{11}$               | $(u^{10} - 4u^8 - u^7 + 10u^6 + 3u^5 - 12u^4 - 4u^3 + 6u^2 + u - 1)^2$                |
| $c_7, c_9$                  | $u^{20} - 7u^{19} + \dots + 710u - 71$  |

| Crossings                   | Riley Polynomials at each crossing          |
|-----------------------------|---|
| $c_1$                       | $(y^{10} + 4y^9 + \dots - 1008y + 256)^2$   |
| $c_2, c_8$                  | $(y^{10} + 4y^9 + \dots - 12y + 16)^2$      |
| $c_3$                       | $(y^{10} + 4y^9 + \dots - 14028y + 2704)^2$ |
| $c_4, c_6, c_{10}$ $c_{12}$ | $y^{20} + 3y^{19} + \dots - 77y + 1$        |
| $c_5, c_{11}$               | $(y^{10} - 8y^9 + \dots - 13y + 1)^2$       |
| $c_7, c_9$                  | $y^{20} - 7y^{19} + \dots - 29394y + 5041$  |

| Solutions to $I_2^u$      | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape          |
|---------------------------|---------------------------------------|---------------------|
| u = 0.606294 + 1.022320I  |                                       |                     |
| a = 0.506435 + 1.185730I  | 6.80818 - 10.55520I                   | -2.80651 + 7.76192I |
| b = -1.20672 + 0.84674I   |                                       |                     |
| u = 0.606294 - 1.022320I  |                                       |                     |
| a = 0.506435 - 1.185730I  | 6.80818 + 10.55520I                   | -2.80651 - 7.76192I |
| b = -1.20672 - 0.84674I   |                                       |                     |
| u = 0.410689 + 1.146110I  |                                       |                     |
| a = -0.911522 + 0.251562I | 3.96203                               | 1.71627 + 0.I       |
| b = 1.21747               |                                       |                     |
| u = 0.410689 - 1.146110I  |                                       |                     |
| a = -0.911522 - 0.251562I | 3.96203                               | 1.71627 + 0.I       |
| b = 1.21747               |                                       |                     |
| u = -0.447983 + 1.156950I |                                       |                     |
| a = -0.650705 + 0.989358I | 7.99409 + 4.11330I                    | -0.72706 - 2.84018I |
| b = 1.31797 + 0.70573I    |                                       |                     |
| u = -0.447983 - 1.156950I |                                       |                     |
| a = -0.650705 - 0.989358I | 7.99409 - 4.11330I                    | -0.72706 + 2.84018I |
| b = 1.31797 - 0.70573I    |                                       |                     |
| u = -0.050609 + 0.749544I |                                       |                     |
| a = 1.71190 + 0.54431I    | -0.07213 - 3.52780I                   | -2.13233 + 4.34006I |
| b = -0.966704 + 0.315261I |                                       |                     |
| u = -0.050609 - 0.749544I |                                       |                     |
| a = 1.71190 - 0.54431I    | -0.07213 + 3.52780I                   | -2.13233 - 4.34006I |
| b = -0.966704 - 0.315261I |                                       |                     |
| u = -0.884394 + 1.054470I |                                       |                     |
| a = 0.719695 + 0.083108I  | -0.07213 + 3.52780I                   | -2.13233 - 4.34006I |
| b = -0.966704 - 0.315261I |                                       |                     |
| u = -0.884394 - 1.054470I |                                       |                     |
| a = 0.719695 - 0.083108I  | -0.07213 - 3.52780I                   | -2.13233 + 4.34006I |
| b = -0.966704 + 0.315261I |                                       |                     |

| Solutions to $I_2^u$      | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape          |
|---------------------------|---------------------------------------|---------------------|
| u = -1.53443              |                                       |                     |
| a = 0.408700              | -3.24417                              | 9.61450             |
| b = -0.572155             |                                       |                     |
| u = 1.70396 + 0.20280I    |                                       |                     |
| a = -0.406335 + 0.011690I | -6.86440 - 4.53571I                   | 10.5005 + 34.9465I  |
| b = 0.532805 - 0.044567I  |                                       |                     |
| u = 1.70396 - 0.20280I    |                                       |                     |
| a = -0.406335 - 0.011690I | -6.86440 + 4.53571I                   | 10.5005 - 34.9465I  |
| b = 0.532805 + 0.044567I  |                                       |                     |
| u = -0.213343             |                                       |                     |
| a = -7.88331              | -3.24417                              | 9.61450             |
| b = -0.572155             |                                       |                     |
| u = 1.03765 + 1.47270I    |                                       |                     |
| a = -0.661123 + 0.144524I | 7.99409 - 4.11330I                    | -0.72706 + 2.84018I |
| b = 1.31797 - 0.70573I    |                                       |                     |
| u = 1.03765 - 1.47270I    |                                       |                     |
| a = -0.661123 - 0.144524I | 7.99409 + 4.11330I                    | -0.72706 - 2.84018I |
| b = 1.31797 + 0.70573I    |                                       |                     |
| u = -1.16158 + 1.41196I   |                                       |                     |
| a = 0.665605 + 0.116987I  | 6.80818 + 10.55520I                   | -2.80651 - 7.76192I |
| b = -1.20672 - 0.84674I   |                                       |                     |
| u = -1.16158 - 1.41196I   |                                       |                     |
| a = 0.665605 - 0.116987I  | 6.80818 - 10.55520I                   | -2.80651 + 7.76192I |
| b = -1.20672 + 0.84674I   |                                       |                     |
| u = 0.159854 + 0.046896I  |                                       |                     |
| a = 11.26340 - 7.33066I   | -6.86440 + 4.53571I                   | 10.5005 - 34.9465I  |
| b = 0.532805 + 0.044567I  |                                       |                     |
| u = 0.159854 - 0.046896I  |                                       |                     |
| a = 11.26340 + 7.33066I   | -6.86440 - 4.53571I                   | 10.5005 + 34.9465I  |
| b = 0.532805 - 0.044567I  |                                       |                     |

#### TTT

 $\begin{matrix} I_3^u = \langle -3.36 \times 10^{35} u^{33} - 7.64 \times 10^{35} u^{32} + \dots + 5.24 \times 10^{36} b - 4.10 \times 10^{36}, \ 1.96 \times 10^{37} u^{33} + 4.10 \times 10^{36} u^{32} + \dots + 5.24 \times 10^{36} a - 6.08 \times 10^{37}, \ u^{34} - 9u^{32} + \dots - 5u + 1 \rangle \end{matrix}$ 

(i) Arc colorings

$$a_{8} = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{5} = \begin{pmatrix} -3.73375u^{33} - 0.782006u^{32} + \dots - 25.6210u + 11.6068 \\ 0.0640435u^{33} + 0.145676u^{32} + \dots - 1.17628u + 0.782006 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 1 \\ u^{2} \end{pmatrix}$$

$$a_{4} = \begin{pmatrix} -3.73375u^{33} - 0.782006u^{32} + \dots - 26.6210u + 11.6068 \\ 0.0640435u^{33} + 0.145676u^{32} + \dots - 1.17628u + 0.782006 \end{pmatrix}$$

$$a_{7} = \begin{pmatrix} -8.90770u^{33} - 2.14572u^{32} + \dots - 71.2828u + 27.4824 \\ -0.376603u^{33} + 0.0354177u^{32} + \dots - 0.644601u + 1.36371 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} -4.42221u^{33} - 0.993348u^{32} + \dots - 37.1005u + 14.3537 \\ -0.0610815u^{33} - 0.112187u^{32} + \dots + 1.07701u + 0.552701 \end{pmatrix}$$

$$a_{9} = \begin{pmatrix} 3.06716u^{33} + 0.825714u^{32} + \dots + 27.3561u - 9.54342 \\ 0.232957u^{33} + 0.180886u^{32} + \dots - 1.92567u - 0.0777394 \end{pmatrix}$$

$$a_{3} = \begin{pmatrix} 1.55716u^{33} + 0.844911u^{32} + \dots + 11.9349u - 1.31495 \\ -0.0686076u^{33} - 0.182006u^{32} + \dots + 3.42735u - 1.07782 \end{pmatrix}$$

$$a_{2} = \begin{pmatrix} 1.55716u^{33} + 0.844911u^{32} + \dots + 11.9349u - 1.31495 \\ 0.202905u^{33} - 0.0632946u^{32} + \dots + 6.09474u - 1.92273 \end{pmatrix}$$

$$a_{1} = \begin{pmatrix} 2.08828u^{33} + 0.392969u^{32} + \dots + 6.09474u - 1.92273 \\ 0.0856981u^{33} - 0.102474u^{32} + \dots + 2.98707u - 0.747975 \end{pmatrix}$$

$$a_{6} = \begin{pmatrix} -3.66970u^{33} - 0.636330u^{32} + \dots - 26.7973u + 12.3888 \\ 0.0640435u^{33} + 0.145676u^{32} + \dots - 1.17628u + 0.782006 \end{pmatrix}$$

- (ii) Obstruction class = 1
- (iii) Cusp Shapes =  $20.8441u^{33} + 4.37870u^{32} + \cdots + 173.006u 75.6418$

| Crossings             | u-Polynomials at each crossing           |
|-----------------------|--|
| $c_1$                 | $(u^{17} - 8u^{16} + \dots - 11u + 2)^2$ |
| $c_2, c_8$            | $u^{34} + 8u^{32} + \dots - 11u^2 - 2$   |
| $c_3$                 | $u^{34} + 12u^{32} + \dots - 99u^2 - 2$  |
| $c_4, c_{10}$         | $u^{34} - 9u^{32} + \dots - 5u + 1$      |
| $c_5, c_{11}$         | $u^{34} + 3u^{32} + \dots + 31u^2 - 2$   |
| $c_6, c_{12}$         | $u^{34} - 9u^{32} + \dots + 5u + 1$      |
| $c_7$                 | $u^{34} + 18u^{33} + \dots + 10u + 1$    |
| <i>c</i> <sub>9</sub> | $u^{34} - 18u^{33} + \dots - 10u + 1$    |

| Crossings                   | Riley Polynomials at each crossing        |
|-----------------------------|---|
| $c_1$                       | $(y^{17} + 10y^{16} + \dots - 11y - 4)^2$ |
| $c_2, c_8$                  | $(y^{17} + 8y^{16} + \dots - 11y - 2)^2$  |
| <i>c</i> <sub>3</sub>       | $(y^{17} + 12y^{16} + \dots - 99y - 2)^2$ |
| $c_4, c_6, c_{10}$ $c_{12}$ | $y^{34} - 18y^{33} + \dots - 5y + 1$      |
| $c_5,c_{11}$                | $(y^{17} + 3y^{16} + \dots + 31y - 2)^2$  |
| $c_{7}, c_{9}$              | $y^{34} - 14y^{33} + \dots - 4y + 1$      |

| Solutions to $I_3^u$      | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape           |
|---------------------------|---------------------------------------|----------------------|
| u = 0.948002 + 0.313646I  |                                       |                      |
| a = 1.49270 + 0.75341I    | -3.90984 - 7.35529I                   | -10.7026 + 11.0707I  |
| b = -0.201379 + 1.177010I |                                       |                      |
| u = 0.948002 - 0.313646I  |                                       |                      |
| a = 1.49270 - 0.75341I    | -3.90984 + 7.35529I                   | -10.7026 - 11.0707I  |
| b = -0.201379 - 1.177010I |                                       |                      |
| u = 0.956410 + 0.604090I  |                                       |                      |
| a = 1.388120 + 0.148389I  | -4.51641 - 1.30867I                   | -12.27157 + 0.31860I |
| b = -0.364697 + 1.081480I |                                       |                      |
| u = 0.956410 - 0.604090I  |                                       |                      |
| a = 1.388120 - 0.148389I  | -4.51641 + 1.30867I                   | -12.27157 - 0.31860I |
| b = -0.364697 - 1.081480I |                                       |                      |
| u = 0.301826 + 0.794742I  |                                       |                      |
| a = -0.242452 + 0.645424I | -3.12305 + 4.90974I                   | -4.98224 - 0.13853I  |
| b = -0.480417 - 1.259920I |                                       |                      |
| u = 0.301826 - 0.794742I  |                                       |                      |
| a = -0.242452 - 0.645424I | -3.12305 - 4.90974I                   | -4.98224 + 0.13853I  |
| b = -0.480417 + 1.259920I |                                       |                      |
| u = -1.127990 + 0.273851I |                                       |                      |
| a = -1.138540 + 0.718861I | -2.73299 + 3.07671I                   | -3.59376 - 6.57908I  |
| b = 0.208856 + 1.290280I  |                                       |                      |
| u = -1.127990 - 0.273851I |                                       |                      |
| a = -1.138540 - 0.718861I | -2.73299 - 3.07671I                   | -3.59376 + 6.57908I  |
| b = 0.208856 - 1.290280I  |                                       |                      |
| u = -0.070405 + 0.815044I |                                       |                      |
| a = 0.532860 + 0.628017I  | -2.73299 + 3.07671I                   | -3.59376 - 6.57908I  |
| b = -0.208856 - 1.290280I |                                       |                      |
| u = -0.070405 - 0.815044I |                                       |                      |
| a = 0.532860 - 0.628017I  | -2.73299 - 3.07671I                   | -3.59376 + 6.57908I  |
| b = -0.208856 + 1.290280I |                                       |                      |

| Solutions to $I_3^u$      | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape           |
|---------------------------|---------------------------------------|----------------------|
| u = 0.251748 + 1.192390I  |                                       |                      |
| a = 1.025750 - 0.598178I  | 4.34137 - 0.62662I                    | 0.702844 + 0.664865I |
| b = -1.286020 + 0.236008I |                                       |                      |
| u = 0.251748 - 1.192390I  |                                       |                      |
| a = 1.025750 + 0.598178I  | 4.34137 + 0.62662I                    | 0.702844 - 0.664865I |
| b = -1.286020 - 0.236008I |                                       |                      |
| u = -1.044090 + 0.683860I |                                       |                      |
| a = -0.761913 + 0.166704I | -1.39035 + 4.13256I                   | -8.96641 - 7.21181I  |
| b = 0.807885 + 0.507938I  |                                       |                      |
| u = -1.044090 - 0.683860I |                                       |                      |
| a = -0.761913 - 0.166704I | -1.39035 - 4.13256I                   | -8.96641 + 7.21181I  |
| b = 0.807885 - 0.507938I  |                                       |                      |
| u = 0.647873 + 0.299417I  |                                       |                      |
| a = 1.00359 + 1.26631I    | -1.39035 - 4.13256I                   | -8.96641 + 7.21181I  |
| b = -0.807885 + 0.507938I |                                       |                      |
| u = 0.647873 - 0.299417I  |                                       |                      |
| a = 1.00359 - 1.26631I    | -1.39035 + 4.13256I                   | -8.96641 - 7.21181I  |
| b = -0.807885 - 0.507938I |                                       |                      |
| u = -1.199710 + 0.613641I |                                       |                      |
| a = -1.068440 + 0.282667I | -3.12305 + 4.90974I                   | -4.98224 + 0.I       |
| b = 0.480417 + 1.259920I  |                                       |                      |
| u = -1.199710 - 0.613641I |                                       |                      |
| a = -1.068440 - 0.282667I | -3.12305 - 4.90974I                   | -4.98224 + 0.I       |
| b = 0.480417 - 1.259920I  |                                       |                      |
| u = 0.067240 + 0.640701I  |                                       |                      |
| a = -0.90142 + 1.12971I   | -3.90984 - 7.35529I                   | -10.7026 + 11.0707I  |
| b = 0.201379 - 1.177010I  |                                       |                      |
| u = 0.067240 - 0.640701I  |                                       |                      |
| a = -0.90142 - 1.12971I   | -3.90984 + 7.35529I                   | -10.7026 - 11.0707I  |
| b = 0.201379 + 1.177010I  |                                       |                      |

| Solutions to $I_3^u$      | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape           |
|---------------------------|---------------------------------------|----------------------|
| u = -0.504150 + 1.265790I |                                       |                      |
| a = -0.961784 - 0.364583I | 4.40017 + 6.90997I                    | 05.88125I            |
| b = 1.335370 + 0.453210I  |                                       |                      |
| u = -0.504150 - 1.265790I |                                       |                      |
| a = -0.961784 + 0.364583I | 4.40017 - 6.90997I                    | 0. + 5.88125I        |
| b = 1.335370 - 0.453210I  |                                       |                      |
| u = -0.604342             |                                       |                      |
| a = -2.59153              | -3.55226                              | -16.8940             |
| b = -0.342161             |                                       |                      |
| u = -1.39868              |                                       |                      |
| a = -0.540058             | -3.55226                              | -16.8940             |
| b = 0.342161              |                                       |                      |
| u = -0.179282 + 0.553299I |                                       |                      |
| a = 0.47174 + 1.58611I    | -4.51641 - 1.30867I                   | -12.27157 + 0.31860I |
| b = 0.364697 - 1.081480I  |                                       |                      |
| u = -0.179282 - 0.553299I |                                       |                      |
| a = 0.47174 - 1.58611I    | -4.51641 + 1.30867I                   | -12.27157 - 0.31860I |
| b = 0.364697 + 1.081480I  |                                       |                      |
| u = 1.56336 + 0.01828I    |                                       |                      |
| a = 0.097753 + 0.190650I  | 4.40017 - 6.90997I                    | 0. + 5.88125I        |
| b = -1.335370 + 0.453210I |                                       |                      |
| u = 1.56336 - 0.01828I    |                                       |                      |
| a = 0.097753 - 0.190650I  | 4.40017 + 6.90997I                    | 0 5.88125I           |
| b = -1.335370 - 0.453210I |                                       |                      |
| u = 0.329313 + 0.165692I  |                                       |                      |
| a = 4.37347 - 4.17301I    | -6.91964 + 4.44078I                   | -26.1531 + 27.7299I  |
| b = 0.480307 - 0.026404I  |                                       |                      |
| u = 0.329313 - 0.165692I  |                                       |                      |
| a = 4.37347 + 4.17301I    | -6.91964 - 4.44078I                   | -26.1531 - 27.7299I  |
| b = 0.480307 + 0.026404I  |                                       |                      |

| Solutions to $I_3^u$      | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape |
|---------------------------|---------------------------------------|------------|
| u = -1.61858 + 0.22328I   |                                       |            |
| a = -0.166497 + 0.131888I | 4.34137 + 0.62662I                    | 0          |
| b = 1.286020 + 0.236008I  |                                       |            |
| u = -1.61858 - 0.22328I   |                                       |            |
| a = -0.166497 - 0.131888I | 4.34137 - 0.62662I                    | 0          |
| b = 1.286020 - 0.236008I  |                                       |            |
| u = 1.67995 + 0.23279I    |                                       |            |
| a = 0.420857 - 0.044359I  | -6.91964 - 4.44078I                   | 0          |
| b = -0.480307 - 0.026404I |                                       |            |
| u = 1.67995 - 0.23279I    |                                       |            |
| a = 0.420857 + 0.044359I  | -6.91964 + 4.44078I                   | 0          |
| b = -0.480307 + 0.026404I |                                       |            |

IV. 
$$I_4^u = \langle 1.67 \times 10^{13} u^{15} + 6.56 \times 10^{12} u^{14} + \cdots + 4.53 \times 10^{14} b + 2.51 \times 10^{14}, \ -3.58 \times 10^{10} u^{15} - 2.67 \times 10^{10} u^{14} + \cdots + 7.67 \times 10^{11} a + 9.31 \times 10^{11}, \ u^{16} - u^{15} + \cdots - 20 u + 13 \rangle$$

#### (i) Arc colorings

$$a_{8} = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} 0.0467229u^{15} + 0.0348323u^{14} + \dots + 0.00279962u - 1.21378 \\ -0.0367984u^{15} - 0.0144567u^{14} + \dots - 0.0545409u - 0.552827 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 1 \\ u^{2} \end{pmatrix}$$

$$a_{4} = \begin{pmatrix} -0.00998312u^{15} + 0.0408553u^{14} + \dots - 1.07545u - 0.706390 \\ -0.00626482u^{15} - 0.0388182u^{14} + \dots - 0.331023u + 0.106053 \end{pmatrix}$$

$$a_{7} = \begin{pmatrix} 0.123646u^{15} - 0.0420908u^{14} + \dots + 0.00279962u - 2.75224 \\ -0.0640970u^{15} + 0.0544416u^{14} + \dots - 0.865462u + 1.19024 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} 0.0915566u^{15} - 0.0439717u^{14} + \dots + 0.747958u + 2.30975 \\ 0.0815552u^{15} - 0.0616476u^{14} + \dots - 0.279323u - 0.607398 \end{pmatrix}$$

$$a_{9} = \begin{pmatrix} 0.0915566u^{15} - 0.0274596u^{14} + \dots + 0.279323u - 0.965670 \\ -0.0815552u^{15} + 0.0616476u^{14} + \dots + 0.279323u + 1.60740 \end{pmatrix}$$

$$a_{3} = \begin{pmatrix} 0.114902u^{15} - 0.0966243u^{14} + \dots + 0.137579u - 0.901552 \\ 0.0610974u^{15} - 0.133458u^{14} + \dots + 0.137579u - 0.901552 \\ 0.0568444u^{15} - 0.0636001u^{14} + \dots + 0.137579u - 0.901552 \\ 0.0568444u^{15} - 0.0636001u^{14} + \dots + 0.820160u - 2.18073 \\ -0.0303001u^{15} - 0.0612608u^{14} + \dots + 1.56812u + 0.786613 \end{pmatrix}$$

$$a_{1} = \begin{pmatrix} 0.0902852u^{15} - 0.105232u^{14} + \dots + 0.820160u - 2.18073 \\ -0.0367984u^{15} + 0.0203756u^{14} + \dots + 1.56812u + 0.129018 \end{pmatrix}$$

$$a_{1} = \begin{pmatrix} 0.00992449u^{15} + 0.0203756u^{14} + \dots + 0.0517413u - 1.76661 \\ -0.0367984u^{15} - 0.0144567u^{14} + \dots - 0.0545409u - 0.552827 \end{pmatrix}$$

#### (ii) Obstruction class = -1

| Crossings                   | u-Polynomials at each crossing         |
|-----------------------------|--|
| $c_1$                       | $(u^4 + u^3 + 3u^2 + 2u + 1)^4$        |
| $c_{2}, c_{8}$              | $(u^4 - u^3 + u^2 + 1)^4$              |
| $c_3$                       | $(u^4 + u^3 + 5u^2 - u + 2)^4$         |
| $c_4, c_6, c_{10}$ $c_{12}$ | $u^{16} - u^{15} + \dots - 20u + 13$   |
| $c_5, c_{11}$               | $u^{16} - 3u^{15} + \dots + 198u + 97$ |
| $c_7, c_9$                  | $(u^2 + u + 1)^8$                      |

| Crossings                   | Riley Polynomials at each crossing          |
|-----------------------------|---|
| $c_1$                       | $(y^4 + 5y^3 + 7y^2 + 2y + 1)^4$            |
| $c_2, c_8$                  | $(y^4 + y^3 + 3y^2 + 2y + 1)^4$             |
| <i>c</i> <sub>3</sub>       | $(y^4 + 9y^3 + 31y^2 + 19y + 4)^4$          |
| $c_4, c_6, c_{10}$ $c_{12}$ | $y^{16} + 7y^{15} + \dots - 400y + 169$     |
| $c_5,c_{11}$                | $y^{16} - 13y^{15} + \dots - 37264y + 9409$ |
| $c_7, c_9$                  | $(y^2 + y + 1)^8$                           |

| Solutions to $I_4^u$      | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape           |
|---------------------------|---------------------------------------|----------------------|
| u = 0.092007 + 1.034470I  |                                       |                      |
| a = -0.787948 - 0.553421I | 6.79074 + 7.22373I                    | 1.82674 - 9.49300I   |
| b = 2.24681 - 1.28233I    |                                       |                      |
| u = 0.092007 - 1.034470I  |                                       |                      |
| a = -0.787948 + 0.553421I | 6.79074 - 7.22373I                    | 1.82674 + 9.49300I   |
| b = 2.24681 + 1.28233I    |                                       |                      |
| u = -0.239797 + 0.921033I |                                       |                      |
| a = 0.748218 - 0.737673I  | 6.79074 - 0.89580I                    | 1.82674 + 4.36340I   |
| b = -1.96980 - 1.53526I   |                                       |                      |
| u = -0.239797 - 0.921033I |                                       |                      |
| a = 0.748218 + 0.737673I  | 6.79074 + 0.89580I                    | 1.82674 - 4.36340I   |
| b = -1.96980 + 1.53526I   |                                       |                      |
| u = -0.639205 + 0.691048I |                                       |                      |
| a = -1.036040 + 0.234778I | -0.21101 + 5.47487I                   | -1.82674 - 11.83695I |
| b = 1.55457 + 0.29681I    |                                       |                      |
| u = -0.639205 - 0.691048I |                                       |                      |
| a = -1.036040 - 0.234778I | -0.21101 - 5.47487I                   | -1.82674 + 11.83695I |
| b = 1.55457 - 0.29681I    |                                       |                      |
| u = -0.811044 + 0.687008I |                                       |                      |
| a = -0.885567 + 0.317657I | -0.21101 + 2.64466I                   | -1.82674 - 2.01946I  |
| b = 0.759110 + 0.954489I  |                                       |                      |
| u = -0.811044 - 0.687008I |                                       |                      |
| a = -0.885567 - 0.317657I | -0.21101 - 2.64466I                   | -1.82674 + 2.01946I  |
| b = 0.759110 - 0.954489I  |                                       |                      |
| u = 1.275710 + 0.602283I  |                                       |                      |
| a = 0.582586 + 0.403811I  | -0.21101 - 5.47487I                   | -1.82674 + 11.83695I |
| b = -0.522944 + 0.714888I |                                       |                      |
| u = 1.275710 - 0.602283I  |                                       |                      |
| a = 0.582586 - 0.403811I  | -0.21101 + 5.47487I                   | -1.82674 - 11.83695I |
| b = -0.522944 - 0.714888I |                                       |                      |

| Solutions to $I_4^u$      | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape          |
|---------------------------|---------------------------------------|---------------------|
| u = 0.569666 + 0.091399I  |                                       |                     |
| a = 1.09347 + 1.34479I    | -0.21101 - 2.64466I                   | -1.82674 + 2.01946I |
| b = -0.605365 - 0.147963I |                                       |                     |
| u = 0.569666 - 0.091399I  |                                       |                     |
| a = 1.09347 - 1.34479I    | -0.21101 + 2.64466I                   | -1.82674 - 2.01946I |
| b = -0.605365 + 0.147963I |                                       |                     |
| u = -1.05226 + 1.78810I   |                                       |                     |
| a = -0.481970 + 0.004004I | 6.79074 + 0.89580I                    | 1.82674 - 4.36340I  |
| b = 0.782616 + 0.884305I  |                                       |                     |
| u = -1.05226 - 1.78810I   |                                       |                     |
| a = -0.481970 - 0.004004I | 6.79074 - 0.89580I                    | 1.82674 + 4.36340I  |
| b = 0.782616 - 0.884305I  |                                       |                     |
| u = 1.30493 + 1.71989I    |                                       |                     |
| a = 0.459558 + 0.057963I  | 6.79074 - 7.22373I                    | 1.82674 + 9.49300I  |
| b = -0.744996 + 0.955578I |                                       |                     |
| u = 1.30493 - 1.71989I    |                                       |                     |
| a = 0.459558 - 0.057963I  | 6.79074 + 7.22373I                    | 1.82674 - 9.49300I  |
| b = -0.744996 - 0.955578I |                                       |                     |

V. 
$$I_5^u = \langle 3.61 \times 10^{67} u^{31} + 1.33 \times 10^{67} u^{30} + \dots + 5.05 \times 10^{70} b - 7.80 \times 10^{69}, \ -2.81 \times 10^{59} u^{31} - 1.32 \times 10^{59} u^{30} + \dots + 1.02 \times 10^{63} a + 2.60 \times 10^{62}, \ u^{32} + u^{31} + \dots - 1290 u + 1501 \rangle$$

(i) Arc colorings

$$a_8 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} 0.000275867u^{31} + 0.000129795u^{30} + \cdots - 1.94837u - 0.254733 \\ -0.000714688u^{31} - 0.000263450u^{30} + \cdots + 1.30103u + 0.154418 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 1 \\ u^2 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} -0.000372259u^{31} - 0.000239040u^{30} + \cdots + 2.63416u - 0.264798 \\ -0.000812029u^{31} - 0.000379010u^{30} + \cdots + 2.63416u - 0.264798 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} -0.000214542u^{31} + 0.000103732u^{30} + \cdots + 1.76603u + 0.160004 \\ 0.000541250u^{31} + 0.000557760u^{30} + \cdots + 0.234939u - 0.714606 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} 0.000104855u^{31} + 0.000223448u^{30} + \cdots + 0.402197u + 1.00171 \\ 0.000587979u^{31} + 0.00023448u^{30} + \cdots + 0.402197u + 1.00171 \\ 0.000587979u^{31} + 0.000782374u^{30} + \cdots - 0.413622u + 0.911091 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} 0.0000192851u^{31} + 0.000101444u^{30} + \cdots - 1.67116u - 0.632751 \\ -0.00100745u^{31} - 0.000635526u^{30} + \cdots + 0.820704u - 0.169014 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} -0.000684276u^{31} - 0.000635526u^{30} + \cdots - 0.323358u + 0.130143 \\ -0.000111240u^{31} - 0.000635526u^{30} + \cdots + 4.84174u + 0.562738 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} -0.000684276u^{31} - 0.000635526u^{30} + \cdots - 0.323358u + 0.130143 \\ -0.00111240u^{31} - 0.000635526u^{30} + \cdots + 5.93173u + 0.489565 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} -0.000409598u^{31} - 0.000309788u^{30} + \cdots + 1.27330u - 0.416102 \\ -0.00130652u^{31} - 0.000309788u^{30} + \cdots + 2.57060u + 0.0601876 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} -0.000438821u^{31} - 0.000133655u^{30} + \cdots - 0.647334u - 0.100315 \\ -0.000714688u^{31} - 0.000263450u^{30} + \cdots + 1.30103u + 0.154418 \end{pmatrix}$$

- (ii) Obstruction class = -1
- (iii) Cusp Shapes =  $0.00301162u^{31} + 0.00331224u^{30} + \cdots + 2.94189u 18.0165$

| Crossings                   | u-Polynomials at each crossing           |
|-----------------------------|--|
| $c_1$                       | $(u^4 + u^3 + 3u^2 + 2u + 1)^8$          |
| $c_{2}, c_{8}$              | $(u^4 - u^3 + u^2 + 1)^8$                |
| <i>c</i> <sub>3</sub>       | $(u^4 + u^3 + 5u^2 - u + 2)^8$           |
| $c_4, c_6, c_{10}$ $c_{12}$ | $u^{32} + u^{31} + \dots - 1290u + 1501$ |
| $c_5, c_{11}$               | $(u^{16} + u^{15} + \dots + 2u + 19)^2$  |
| $c_7, c_9$                  | $(u^4 + u^3 - 2u + 1)^8$                 |

| Crossings                   | Riley Polynomials at each crossing                |
|-----------------------------|---|
| $c_1$                       | $(y^4 + 5y^3 + 7y^2 + 2y + 1)^8$                  |
| $c_2, c_8$                  | $(y^4 + y^3 + 3y^2 + 2y + 1)^8$                   |
| $c_3$                       | $(y^4 + 9y^3 + 31y^2 + 19y + 4)^8$                |
| $c_4, c_6, c_{10}$ $c_{12}$ | $y^{32} - 23y^{31} + \dots - 13272834y + 2253001$ |
| $c_5, c_{11}$               | $(y^{16} - y^{15} + \dots - 2512y + 361)^2$       |
| $c_7, c_9$                  | $(y^4 - y^3 + 6y^2 - 4y + 1)^8$                   |

| Solutions to $I_5^u$      | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape           |
|---------------------------|---------------------------------------|----------------------|
| u = 0.933125 + 0.345373I  |                                       |                      |
| a = 1.42512 + 0.60180I    | -3.50087 - 2.64466I                   | -13.82674 + 2.01946I |
| b = -0.507415 + 1.111340I |                                       |                      |
| u = 0.933125 - 0.345373I  |                                       |                      |
| a = 1.42512 - 0.60180I    | -3.50087 + 2.64466I                   | -13.82674 - 2.01946I |
| b = -0.507415 - 1.111340I |                                       |                      |
| u = -0.465677 + 0.912383I |                                       |                      |
| a = -1.41419 - 0.50791I   | 3.50087 + 0.89580I                    | -10.17326 - 4.36340I |
| b = 0.505216 + 0.080628I  |                                       |                      |
| u = -0.465677 - 0.912383I |                                       |                      |
| a = -1.41419 + 0.50791I   | 3.50087 - 0.89580I                    | -10.17326 + 4.36340I |
| b = 0.505216 - 0.080628I  |                                       |                      |
| u = 1.105300 + 0.270519I  |                                       |                      |
| a = -0.570130 - 0.030308I | 3.50087 - 7.22373I                    | -10.17326 + 9.49300I |
| b = 1.91342 - 1.12465I    |                                       |                      |
| u = 1.105300 - 0.270519I  |                                       |                      |
| a = -0.570130 + 0.030308I | 3.50087 + 7.22373I                    | -10.17326 - 9.49300I |
| b = 1.91342 + 1.12465I    |                                       |                      |
| u = 0.672655 + 0.976570I  |                                       |                      |
| a = 1.268540 - 0.275121I  | 3.50087 - 7.22373I                    | -10.17326 + 9.49300I |
| b = -0.621358 + 0.257578I |                                       |                      |
| u = 0.672655 - 0.976570I  |                                       |                      |
| a = 1.268540 + 0.275121I  | 3.50087 + 7.22373I                    | -10.17326 - 9.49300I |
| b = -0.621358 - 0.257578I |                                       |                      |
| u = -1.140760 + 0.351108I |                                       |                      |
| a = 0.544306 + 0.002963I  | 3.50087 + 0.89580I                    | -10.17326 - 4.36340I |
| b = -1.90215 - 0.76605I   |                                       |                      |
| u = -1.140760 - 0.351108I |                                       |                      |
| a = 0.544306 - 0.002963I  | 3.50087 - 0.89580I                    | -10.17326 + 4.36340I |
| b = -1.90215 + 0.76605I   |                                       |                      |

| Solutions to $I_5^u$      | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape           |
|---------------------------|---------------------------------------|----------------------|
| u = -1.190410 + 0.259439I |                                       |                      |
| a = -1.083940 + 0.648970I | -3.50087 + 2.64466I                   | -13.82674 - 2.01946I |
| b = -0.129086 + 1.200110I |                                       |                      |
| u = -1.190410 - 0.259439I |                                       |                      |
| a = -1.083940 - 0.648970I | -3.50087 - 2.64466I                   | -13.82674 + 2.01946I |
| b = -0.129086 - 1.200110I |                                       |                      |
| u = 1.166990 + 0.483595I  |                                       |                      |
| a = 1.139860 + 0.430615I  | -3.50087 - 5.47487I                   | -13.8267 + 11.8369I  |
| b = -0.387825 + 1.018230I |                                       |                      |
| u = 1.166990 - 0.483595I  |                                       |                      |
| a = 1.139860 - 0.430615I  | -3.50087 + 5.47487I                   | -13.8267 - 11.8369I  |
| b = -0.387825 - 1.018230I |                                       |                      |
| u = -0.662252 + 0.286911I |                                       |                      |
| a = 0.687346 + 0.581256I  | -3.50087 - 2.64466I                   | -13.82674 + 2.01946I |
| b = -0.129086 - 1.200110I |                                       |                      |
| u = -0.662252 - 0.286911I |                                       |                      |
| a = 0.687346 - 0.581256I  | -3.50087 + 2.64466I                   | -13.82674 - 2.01946I |
| b = -0.129086 + 1.200110I |                                       |                      |
| u = -0.594845 + 1.145980I |                                       |                      |
| a = 0.350970 + 0.360556I  | -3.50087 + 2.64466I                   | -13.82674 - 2.01946I |
| b = -0.507415 - 1.111340I |                                       |                      |
| u = -0.594845 - 1.145980I |                                       |                      |
| a = 0.350970 - 0.360556I  | -3.50087 - 2.64466I                   | -13.82674 + 2.01946I |
| b = -0.507415 + 1.111340I |                                       |                      |
| u = -1.187550 + 0.754071I |                                       |                      |
| a = -1.074840 + 0.204836I | -3.50087 + 5.47487I                   | -13.8267 - 11.8369I  |
| b = 0.62920 + 1.61384I    |                                       |                      |
| u = -1.187550 - 0.754071I |                                       |                      |
| a = -1.074840 - 0.204836I | -3.50087 - 5.47487I                   | -13.8267 + 11.8369I  |
| b = 0.62920 - 1.61384I    |                                       |                      |

| Solutions to $I_5^u$      | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape           |
|---------------------------|---------------------------------------|----------------------|
| u = 0.06626 + 1.43374I    |                                       |                      |
| a = 0.769490 - 0.746980I  | 3.50087 - 0.89580I                    | -10.17326 + 4.36340I |
| b = -1.90215 + 0.76605I   |                                       |                      |
| u = 0.06626 - 1.43374I    |                                       |                      |
| a = 0.769490 + 0.746980I  | 3.50087 + 0.89580I                    | -10.17326 - 4.36340I |
| b = -1.90215 - 0.76605I   |                                       |                      |
| u = 0.353208 + 0.331710I  |                                       |                      |
| a = -1.200900 + 0.596300I | -3.50087 - 5.47487I                   | -13.8267 + 11.8369I  |
| b = 0.62920 - 1.61384I    |                                       |                      |
| u = 0.353208 - 0.331710I  |                                       |                      |
| a = -1.200900 - 0.596300I | -3.50087 + 5.47487I                   | -13.8267 - 11.8369I  |
| b = 0.62920 + 1.61384I    |                                       |                      |
| u = 0.78661 + 1.34122I    |                                       |                      |
| a = -0.098220 + 0.406126I | -3.50087 + 5.47487I                   | -13.8267 - 11.8369I  |
| b = -0.387825 - 1.018230I |                                       |                      |
| u = 0.78661 - 1.34122I    |                                       |                      |
| a = -0.098220 - 0.406126I | -3.50087 - 5.47487I                   | -13.8267 + 11.8369I  |
| b = -0.387825 + 1.018230I |                                       |                      |
| u = -0.34699 + 1.54691I   |                                       |                      |
| a = -0.803463 - 0.545068I | 3.50087 + 7.22373I                    | -10.17326 - 9.49300I |
| b = 1.91342 + 1.12465I    |                                       |                      |
| u = -0.34699 - 1.54691I   |                                       |                      |
| a = -0.803463 + 0.545068I | 3.50087 - 7.22373I                    | -10.17326 + 9.49300I |
| b = 1.91342 - 1.12465I    |                                       |                      |
| u = -2.54575 + 0.33352I   |                                       |                      |
| a = 0.230694 + 0.103966I  | 3.50087 - 0.89580I                    | 0                    |
| b = 0.505216 - 0.080628I  |                                       |                      |
| u = -2.54575 - 0.33352I   |                                       |                      |
| a = 0.230694 - 0.103966I  | 3.50087 + 0.89580I                    | 0                    |
| b = 0.505216 + 0.080628I  |                                       |                      |
|                           |                                       |                      |

| Solutions to $I_5^u$      | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape |
|---------------------------|---------------------------------------|------------|
| u = 2.55009 + 0.74890I    |                                       |            |
| a = -0.204631 + 0.133712I | 3.50087 + 7.22373I                    | 0          |
| b = -0.621358 - 0.257578I |                                       |            |
| u = 2.55009 - 0.74890I    |                                       |            |
| a = -0.204631 - 0.133712I | 3.50087 - 7.22373I                    | 0          |
| b = -0.621358 + 0.257578I |                                       |            |

VI. 
$$I_6^u = \langle b-u, \ a, \ u^4+u^3+3u^2+2u+1 \rangle$$

(i) Arc colorings

$$a_{8} = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{5} = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 1 \\ u^{2} \end{pmatrix}$$

$$a_{4} = \begin{pmatrix} u \\ u^{3} + u \end{pmatrix}$$

$$a_{7} = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{9} = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{3} = \begin{pmatrix} u^{3} + 2u \\ u^{3} + u \end{pmatrix}$$

$$a_{2} = \begin{pmatrix} u^{3} + 2u \\ u^{3} + u^{2} + 2u + 1 \end{pmatrix}$$

$$a_{1} = \begin{pmatrix} -u^{2} - 1 \\ -u^{2} \end{pmatrix}$$

- (ii) Obstruction class = -1
- (iii) Cusp Shapes =  $-4u^3 4u^2 12u 6$

| Crossings                                      | u-Polynomials at each crossing |
|--|--------------------------------|
| $c_1, c_4, c_5$ $c_6, c_{10}, c_{11}$ $c_{12}$ | $u^4 + u^3 + 3u^2 + 2u + 1$    |
| $c_{2}, c_{8}$                                 | $u^4 + u^3 + u^2 + 1$          |
| <i>c</i> <sub>3</sub>                          | $u^4 - u^3 + 5u^2 + u + 2$     |
| $c_7, c_9$                                     | $u^4$                          |

| Crossings  | Riley Polynomials at each crossing |
|--|------------------------------------|
| $c_1, c_4, c_5 \\ c_6, c_{10}, c_{11} \\ c_{12}$ | $y^4 + 5y^3 + 7y^2 + 2y + 1$       |
| $c_2, c_8$                                       | $y^4 + y^3 + 3y^2 + 2y + 1$        |
| <i>c</i> <sub>3</sub>                            | $y^4 + 9y^3 + 31y^2 + 19y + 4$     |
| $c_7, c_9$                                       | $y^4$                              |

| Solutions to $I_6^u$      | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape          |
|---------------------------|---------------------------------------|---------------------|
| u = -0.395123 + 0.506844I |                                       |                     |
| a = 0                     | -0.21101 + 1.41510I                   | -1.82674 - 4.90874I |
| b = -0.395123 + 0.506844I |                                       |                     |
| u = -0.395123 - 0.506844I |                                       |                     |
| a = 0                     | -0.21101 - 1.41510I                   | -1.82674 + 4.90874I |
| b = -0.395123 - 0.506844I |                                       |                     |
| u = -0.10488 + 1.55249I   |                                       |                     |
| a = 0                     | 6.79074 + 3.16396I                    | 1.82674 - 2.56480I  |
| b = -0.10488 + 1.55249I   |                                       |                     |
| u = -0.10488 - 1.55249I   |                                       |                     |
| a = 0                     | 6.79074 - 3.16396I                    | 1.82674 + 2.56480I  |
| b = -0.10488 - 1.55249I   |                                       |                     |

VII. 
$$I_7^u = \langle 11u^7 + 19u^6 + \dots + 2b - 28, \ u^7 + u^6 + 4u^5 + 2u^4 - 5u^3 - 3u^2 + 2a + 3u - 3, \ u^8 + u^7 + \dots - 3u + 2 \rangle$$

(i) Arc colorings

$$a_{8} = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{5} = \begin{pmatrix} -\frac{1}{2}u^{7} - \frac{1}{2}u^{6} + \dots - \frac{3}{2}u + \frac{3}{2} \\ -\frac{11}{2}u^{7} - \frac{19}{2}u^{6} + \dots - \frac{9}{2}u + 14 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 1 \\ u^{2} \end{pmatrix}$$

$$a_{4} = \begin{pmatrix} -6u^{7} - 10u^{6} + \dots - 7u + \frac{31}{2} \\ -\frac{17}{2}u^{7} - 15u^{6} + \dots - \frac{11}{2}u + 22 \end{pmatrix}$$

$$a_{7} = \begin{pmatrix} -\frac{1}{2}u^{7} - \frac{1}{2}u^{6} + \dots - \frac{3}{2}u + \frac{3}{2} \\ -\frac{11}{2}u^{7} - \frac{19}{2}u^{6} + \dots - \frac{7}{2}u + 14 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} 7u^{7} + \frac{25}{2}u^{6} + \dots + 4u - \frac{31}{2} \\ 1 \end{pmatrix}$$

$$a_{9} = \begin{pmatrix} -7u^{7} - \frac{25}{2}u^{6} + \dots - 4u + \frac{33}{2} \\ -1 \end{pmatrix}$$

$$a_{3} = \begin{pmatrix} -\frac{19}{2}u^{7} - 17u^{6} + \dots - \frac{7}{2}u + \frac{51}{2} \\ -\frac{29}{2}u^{7} - 26u^{6} + \dots - \frac{13}{2}u + 38 \end{pmatrix}$$

$$a_{2} = \begin{pmatrix} -\frac{19}{2}u^{7} - 17u^{6} + \dots - \frac{7}{2}u + \frac{51}{2} \\ -\frac{41}{2}u^{7} - \frac{73}{2}u^{6} + \dots - 10u + 53 \end{pmatrix}$$

$$a_{1} = \begin{pmatrix} -8u^{7} - 14u^{6} - 43u^{5} - 49u^{4} + u^{3} + 23u^{2} - 5u + 23 \\ -8u^{7} - 14u^{6} - 43u^{5} - 49u^{4} + u^{3} + 23u^{2} - 5u + 22 \end{pmatrix}$$

$$a_{6} = \begin{pmatrix} -6u^{7} - 10u^{6} + \dots - 6u + \frac{31}{2} \\ -\frac{11}{2}u^{7} - \frac{19}{2}u^{6} + \dots - \frac{9}{2}u + 14 \end{pmatrix}$$

- (ii) Obstruction class = -1
- (iii) Cusp Shapes =  $52u^7 + 92u^6 + 278u^5 + 318u^4 18u^3 168u^2 + 30u 146$

| Crossings                   | u-Polynomials at each crossing                          |
|-----------------------------|---|
| $c_1, c_5, c_{11}$          | $(u^4 + u^3 + 3u^2 + 2u + 1)^2$                         |
| $c_2, c_8$                  | $(u^4 - u^3 + u^2 + 1)^2$                               |
| <i>C</i> 3                  | $(u^4 + u^3 + 5u^2 - u + 2)^2$                          |
| $c_4, c_6, c_{10}$ $c_{12}$ | $u^8 + u^7 + 4u^6 + 2u^5 - 5u^4 - 3u^3 + 3u^2 - 3u + 2$ |
| $c_7, c_9$                  | $(u+1)^8$   |

| Crossings                   | Riley Polynomials at each crossing                           |
|-----------------------------|--|
| $c_1, c_5, c_{11}$          | $(y^4 + 5y^3 + 7y^2 + 2y + 1)^2$                             |
| $c_{2}, c_{8}$              | $(y^4 + y^3 + 3y^2 + 2y + 1)^2$                              |
| <i>c</i> <sub>3</sub>       | $(y^4 + 9y^3 + 31y^2 + 19y + 4)^2$                           |
| $c_4, c_6, c_{10}$ $c_{12}$ | $y^8 + 7y^7 + 2y^6 - 32y^5 + 71y^4 - 11y^3 - 29y^2 + 3y + 4$ |
| $c_{7}, c_{9}$              | $(y-1)^8$  |

| Solutions to $I_7^u$      | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape           |
|---------------------------|---------------------------------------|----------------------|
| u = 0.772314 + 0.004686I  |                                       |                      |
| a = 1.294760 - 0.007855I  | -3.50087 - 1.41510I                   | -13.8267 + 4.9087I   |
| b = -0.395123 - 0.506844I |                                       |                      |
| u = 0.772314 - 0.004686I  |                                       |                      |
| a = 1.294760 + 0.007855I  | -3.50087 + 1.41510I                   | -13.8267 - 4.9087I   |
| b = -0.395123 + 0.506844I |                                       |                      |
| u = -1.167440 + 0.511530I |                                       |                      |
| a = -0.718612 - 0.314870I | -3.50087 + 1.41510I                   | -13.8267 - 4.9087I   |
| b = -0.395123 + 0.506844I |                                       |                      |
| u = -1.167440 - 0.511530I |                                       |                      |
| a = -0.718612 + 0.314870I | -3.50087 - 1.41510I                   | -13.8267 + 4.9087I   |
| b = -0.395123 - 0.506844I |                                       |                      |
| u = 0.090777 + 0.644863I  |                                       |                      |
| a = 0.21405 - 1.52058I    | 3.50087 - 3.16396I                    | -10.17326 + 2.56480I |
| b = -0.10488 - 1.55249I   |                                       |                      |
| u = 0.090777 - 0.644863I  |                                       |                      |
| a = 0.21405 + 1.52058I    | 3.50087 + 3.16396I                    | -10.17326 - 2.56480I |
| b = -0.10488 + 1.55249I   |                                       |                      |
| u = -0.19565 + 2.19735I   |                                       |                      |
| a = -0.040203 - 0.451513I | 3.50087 + 3.16396I                    | -10.17326 - 2.56480I |
| b = -0.10488 + 1.55249I   |                                       |                      |
| u = -0.19565 - 2.19735I   |                                       |                      |
| a = -0.040203 + 0.451513I | 3.50087 - 3.16396I                    | -10.17326 + 2.56480I |
| b = -0.10488 - 1.55249I   |                                       |                      |

VIII. 
$$I_8^u=\langle b,\; a+1,\; u+1 \rangle$$

(i) Arc colorings

$$a_8 = \begin{pmatrix} 0 \\ -1 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} -1\\0 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 1 \\ 1 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} 0 \\ 1 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} -1 \\ -1 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} 1 \\ 1 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} 0 \\ -1 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} 0 \\ 1 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} 0 \\ 1 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} 0 \\ 1 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} -1 \\ 0 \end{pmatrix}$$

- (ii) Obstruction class = 1
- (iii) Cusp Shapes = -12

| Crossings                           | u-Polynomials at each crossing |
|-------------------------------------|--------------------------------|
| $c_1, c_2, c_3 \\ c_5, c_8, c_{11}$ | u                              |
| $c_4, c_7, c_{10}$                  | u+1                            |
| $c_6, c_9, c_{12}$                  | u-1                            |

| Crossings                                | Riley Polynomials at each crossing |
|--|------------------------------------|
| $c_1, c_2, c_3 \\ c_5, c_8, c_{11}$      | y                                  |
| $c_4, c_6, c_7$<br>$c_9, c_{10}, c_{12}$ | y-1                                |

| Solutions to $I_8^u$ | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape |
|----------------------|---------------------------------------|------------|
| u = -1.00000         |                                       |            |
| a = -1.00000         | -3.28987                              | -12.0000   |
| b = 0                |                                       |            |

## IX. u-Polynomials

| Crossings             | u-Polynomials at each crossing  |
|-----------------------|---|
| $c_1$                 | $u(u^{4} + u^{3} + 3u^{2} + 2u + 1)^{15}(u^{10} + 4u^{9} + \dots - 12u + 16)^{2} $ $\cdot ((u^{17} - 8u^{16} + \dots - 11u + 2)^{2})(u^{22} + 8u^{21} + \dots + 160u + 64)$   |
| $c_2, c_8$            | $u(u^{4} - u^{3} + u^{2} + 1)^{14}(u^{4} + u^{3} + u^{2} + 1)$ $\cdot (u^{10} + 4u^{9} + 10u^{8} + 16u^{7} + 19u^{6} + 15u^{5} + 6u^{4} - 5u^{3} - 11u^{2} - 10u - 4)^{2}$ $\cdot (u^{22} + 6u^{21} + \dots + 32u + 8)(u^{34} + 8u^{32} + \dots - 11u^{2} - 2)$   |
| <i>c</i> <sub>3</sub> | $u(u^{4} - u^{3} + 5u^{2} + u + 2)(u^{4} + u^{3} + 5u^{2} - u + 2)^{14}$ $\cdot ((u^{10} - 4u^{9} + \dots - 66u - 52)^{2})(u^{22} - 6u^{21} + \dots - 5072u + 3880)$ $\cdot (u^{34} + 12u^{32} + \dots - 99u^{2} - 2)$  |
| $c_4, c_{10}$         | $(u+1)(u^{4} + u^{3} + 3u^{2} + 2u + 1)$ $\cdot (u^{8} + u^{7} + 4u^{6} + 2u^{5} - 5u^{4} - 3u^{3} + 3u^{2} - 3u + 2)$ $\cdot (u^{16} - u^{15} + \dots - 20u + 13)(u^{20} - u^{19} + \dots - 7u + 1)$ $\cdot (u^{22} - u^{21} + \dots - u + 1)(u^{32} + u^{31} + \dots - 1290u + 1501)$ $\cdot (u^{34} - 9u^{32} + \dots - 5u + 1)$ |
| $c_5, c_{11}$         | $u(u^{4} + u^{3} + 3u^{2} + 2u + 1)^{3}$ $\cdot (u^{10} - 4u^{8} - u^{7} + 10u^{6} + 3u^{5} - 12u^{4} - 4u^{3} + 6u^{2} + u - 1)^{2}$ $\cdot (u^{16} - 3u^{15} + \dots + 198u + 97)(u^{16} + u^{15} + \dots + 2u + 19)^{2}$ $\cdot (u^{22} - u^{21} + \dots - 16u + 10)(u^{34} + 3u^{32} + \dots + 31u^{2} - 2)$                    |
| $c_6, c_{12}$         | $(u-1)(u^{4} + u^{3} + 3u^{2} + 2u + 1)$ $\cdot (u^{8} + u^{7} + 4u^{6} + 2u^{5} - 5u^{4} - 3u^{3} + 3u^{2} - 3u + 2)$ $\cdot (u^{16} - u^{15} + \dots - 20u + 13)(u^{20} - u^{19} + \dots - 7u + 1)$ $\cdot (u^{22} - u^{21} + \dots - u + 1)(u^{32} + u^{31} + \dots - 1290u + 1501)$ $\cdot (u^{34} - 9u^{32} + \dots + 5u + 1)$ |
|                       | $u^{4}(u+1)^{9}(u^{2}+u+1)^{8}(u^{4}+u^{3}-2u+1)^{8}$ $\cdot (u^{20}-7u^{19}+\cdots+710u-71)(u^{22}-9u^{21}+\cdots-15u+19)$ $\cdot (u^{34}+18u^{33}+\cdots+10u+1)$  |
| <i>c</i> 9            | $u^{4}(u-1)(u+1)^{8}(u^{2}+u+1)^{8}(u^{4}+u^{3}-2u+1)^{8}$ $\cdot (u^{20}-7u^{19}+\cdots+710u-71)(u^{22}-9u^{21}+\cdots-15u+19)$ $\cdot (u^{34}-18u^{33}+\cdots-10u+1)$   |

## X. Riley Polynomials

| Crossings                   | Riley Polynomials at each crossing   |
|-----------------------------|--|
| $c_1$                       | $y(y^{4} + 5y^{3} + \dots + 2y + 1)^{15}(y^{10} + 4y^{9} + \dots - 1008y + 256)^{2} $ $\cdot ((y^{17} + 10y^{16} + \dots - 11y - 4)^{2})(y^{22} + 12y^{21} + \dots + 28160y + 4096)$   |
| $c_2, c_8$                  | $y(y^4 + y^3 + 3y^2 + 2y + 1)^{15}(y^{10} + 4y^9 + \dots - 12y + 16)^2$ $\cdot ((y^{17} + 8y^{16} + \dots - 11y - 2)^2)(y^{22} + 8y^{21} + \dots + 160y + 64)$   |
| $c_3$                       | $y(y^4 + 9y^3 + \dots + 19y + 4)^{15}(y^{10} + 4y^9 + \dots - 14028y + 2704)^2$ $\cdot (y^{17} + 12y^{16} + \dots - 99y - 2)^2$  |
|                             | $(y^{22} + 16y^{21} + \dots + 18242976y + 15054400)$   |
| $c_4, c_6, c_{10}$ $c_{12}$ | $(y-1)(y^{4} + 5y^{3} + 7y^{2} + 2y + 1)$ $\cdot (y^{8} + 7y^{7} + 2y^{6} - 32y^{5} + 71y^{4} - 11y^{3} - 29y^{2} + 3y + 4)$ $\cdot (y^{16} + 7y^{15} + \dots - 400y + 169)(y^{20} + 3y^{19} + \dots - 77y + 1)$ $\cdot (y^{22} + 21y^{21} + \dots + 35y + 1)$                   |
|                             | $(y^{32} - 23y^{31} + \dots - 13272834y + 2253001)$ $(y^{34} - 18y^{33} + \dots - 5y + 1)$   |
| $c_5, c_{11}$               | $y(y^{4} + 5y^{3} + \dots + 2y + 1)^{3}(y^{10} - 8y^{9} + \dots - 13y + 1)^{2}$ $\cdot (y^{16} - 13y^{15} + \dots - 37264y + 9409)$ $\cdot ((y^{16} - y^{15} + \dots - 2512y + 361)^{2})(y^{17} + 3y^{16} + \dots + 31y - 2)^{2}$ $\cdot (y^{22} + y^{21} + \dots + 624y + 100)$ |
| $c_7, c_9$                  | $y^{4}(y-1)^{9}(y^{2}+y+1)^{8}(y^{4}-y^{3}+6y^{2}-4y+1)^{8}$ $\cdot (y^{20}-7y^{19}+\cdots-29394y+5041)(y^{22}-9y^{21}+\cdots-187y+361)$ $\cdot (y^{34}-14y^{33}+\cdots-4y+1)$   |