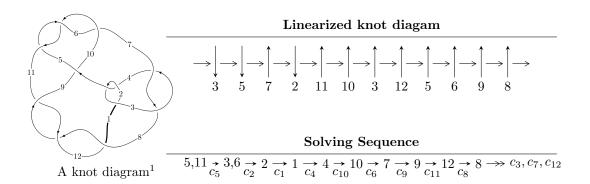
$12n_{0200} (K12n_{0200})$



Ideals for irreducible components² of X_{par}

$$\begin{split} I_1^u &= \langle -u^7 - u^6 - 4u^5 - 3u^4 - 4u^3 - 2u^2 + b, \ u^7 + u^6 + 5u^5 + 4u^4 + 7u^3 + 4u^2 + a + 2u, \\ &u^{11} + 2u^{10} + 8u^9 + 12u^8 + 22u^7 + 24u^6 + 24u^5 + 16u^4 + 9u^3 + u^2 + 2u + 1 \rangle \\ I_2^u &= \langle b + 1, \ -u^2 + a + u - 2, \ u^3 + 2u + 1 \rangle \\ I_3^u &= \langle b + 1, \ u^3 + a + u - 1, \ u^4 - u^3 + 2u^2 - 2u + 1 \rangle \end{split}$$

* 3 irreducible components of $\dim_{\mathbb{C}} = 0$, with total 18 representations.

¹The image of knot diagram is generated by the software "**Draw programme**" developed by Andrew Bartholomew(http://www.layer8.co.uk/maths/draw/index.htm#Running-draw), where we modified some parts for our purpose(https://github.com/CATsTAILs/LinksPainter).

² All coefficients of polynomials are rational numbers. But the coefficients are sometimes approximated in decimal forms when there is not enough margin.

I.
$$I_1^u = \langle -u^7 - u^6 - 4u^5 - 3u^4 - 4u^3 - 2u^2 + b, \ u^7 + u^6 + 5u^5 + 4u^4 + 7u^3 + 4u^2 + a + 2u, \ u^{11} + 2u^{10} + \dots + 2u + 1 \rangle$$

(i) Arc colorings

$$a_{5} = \begin{pmatrix} 1\\0 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 0\\u \end{pmatrix}$$

$$a_{3} = \begin{pmatrix} -u^{7} - u^{6} - 5u^{5} - 4u^{4} - 7u^{3} - 4u^{2} - 2u\\u^{7} + u^{6} + 4u^{5} + 3u^{4} + 4u^{3} + 2u^{2} \end{pmatrix}$$

$$a_{6} = \begin{pmatrix} 1\\-u^{2} \end{pmatrix}$$

$$a_{2} = \begin{pmatrix} -u^{5} - u^{4} - 3u^{3} - 2u^{2} - 2u\\u^{7} + u^{6} + 4u^{5} + 3u^{4} + 4u^{3} + 2u^{2} \end{pmatrix}$$

$$a_{1} = \begin{pmatrix} 3u^{7} - u^{6} + 12u^{5} - 3u^{4} + 12u^{3} - 2u^{2} + 2\\u^{9} + 4u^{8} + 5u^{7} + 17u^{6} + 7u^{5} + 18u^{4} + 2u^{3} + u^{2} + u \end{pmatrix}$$

$$a_{4} = \begin{pmatrix} u^{8} + u^{7} + 4u^{6} + 4u^{5} + 3u^{4} + 3u^{3} - 2u^{2} - u + 1\\u^{8} + 5u^{6} + u^{5} + 7u^{4} + 2u^{3} + 2u^{2} + u \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} -u\\u^{3} + u \end{pmatrix}$$

$$a_{7} = \begin{pmatrix} -u\\u^{3} + u \end{pmatrix}$$

$$a_{9} = \begin{pmatrix} u^{7} + 4u^{5} + 4u^{3}\\-u^{7} - 3u^{5} - 2u^{3} + u \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} u^{7} + 4u^{5} + 4u^{3}\\-u^{7} - 3u^{5} - 2u^{3} + u \end{pmatrix}$$

$$a_{8} = \begin{pmatrix} 2u^{10} + 2u^{9} + 12u^{8} + 10u^{7} + 24u^{6} + 16u^{5} + 16u^{4} + 8u^{3} + u^{2} + 1\\-2u^{10} - 3u^{9} + \dots - u - 1 \end{pmatrix}$$

(ii) Obstruction class = -1

$$= 4u^{10} + 8u^9 + 33u^8 + 46u^7 + 87u^6 + 82u^5 + 79u^4 + 38u^3 + 14u^2 - 8u + 11$$

(iv) u-Polynomials at the component

| Crossings | u-Polynomials at each crossing |
|-----------------------|---|
| c_1 | $u^{11} + 30u^{10} + \dots + 93u + 1$ |
| c_2, c_4 | $u^{11} - 8u^{10} + \dots + 13u - 1$ |
| c_{3}, c_{7} | $u^{11} - u^{10} + \dots - 64u - 128$ |
| c_5, c_6, c_{10} | $u^{11} - 2u^{10} + \dots + 2u - 1$ |
| c_8, c_{11}, c_{12} | $u^{11} + 12u^9 + 38u^7 + 2u^6 + 14u^5 + 12u^4 + 13u^3 + u^2 - 1$ |
| <i>c</i> ₉ | $u^{11} + 2u^{10} + \dots - 15u^2 - 8$ |

(v) Riley Polynomials at the component

| Crossings | Riley Polynomials at each crossing |
|-----------------------|---|
| c_1 | $y^{11} - 202y^{10} + \dots + 8901y - 1$ |
| c_2, c_4 | $y^{11} - 30y^{10} + \dots + 93y - 1$ |
| c_{3}, c_{7} | $y^{11} + 81y^{10} + \dots + 192512y - 16384$ |
| c_5, c_6, c_{10} | $y^{11} + 12y^{10} + \dots + 2y - 1$ |
| c_8, c_{11}, c_{12} | $y^{11} + 24y^{10} + \dots + 2y - 1$ |
| c ₉ | $y^{11} + 12y^{10} + \dots - 240y - 64$ |

(vi) Complex Volumes and Cusp Shapes

| Solutions to I_1^u | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape |
|---------------------------|---------------------------------------|---------------------|
| u = -0.810323 + 0.554853I | | |
| a = -2.69043 - 1.72437I | 15.5955 - 2.6821I | 1.82264 + 2.33402I |
| b = 2.74686 + 0.14673I | | |
| u = -0.810323 - 0.554853I | | |
| a = -2.69043 + 1.72437I | 15.5955 + 2.6821I | 1.82264 - 2.33402I |
| b = 2.74686 - 0.14673I | | |
| u = -0.096709 + 1.327340I | | |
| a = 0.467034 + 0.177497I | -3.51172 - 1.71507I | 5.41681 + 3.29736I |
| b = 0.180346 - 0.216613I | | |
| u = -0.096709 - 1.327340I | | |
| a = 0.467034 - 0.177497I | -3.51172 + 1.71507I | 5.41681 - 3.29736I |
| b = 0.180346 + 0.216613I | | |
| u = 0.303421 + 0.399714I | | |
| a = 0.70061 - 1.79618I | -1.58612 + 0.99841I | 0.02750 - 3.98074I |
| b = -0.761956 + 0.436521I | | |
| u = 0.303421 - 0.399714I | | |
| a = 0.70061 + 1.79618I | -1.58612 - 0.99841I | 0.02750 + 3.98074I |
| b = -0.761956 - 0.436521I | | |
| u = 0.09711 + 1.51180I | | |
| a = -0.238461 - 0.866072I | -8.01829 + 2.43510I | -1.52628 - 1.69137I |
| b = -1.01867 + 1.25733I | | |
| u = 0.09711 - 1.51180I | | |
| a = -0.238461 + 0.866072I | -8.01829 - 2.43510I | -1.52628 + 1.69137I |
| b = -1.01867 - 1.25733I | | |
| u = -0.29124 + 1.55535I | | |
| a = -0.51989 - 1.85777I | 8.71098 - 6.75197I | -1.02074 + 2.56276I |
| b = 2.80237 + 0.46328I | | |
| u = -0.29124 - 1.55535I | | |
| a = -0.51989 + 1.85777I | 8.71098 + 6.75197I | -1.02074 - 2.56276I |
| b = 2.80237 - 0.46328I | | |

| Solutions to I_1^u | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape |
|----------------------|---------------------------------------|------------|
| u = -0.404507 | | |
| a = 0.562272 | 0.648477 | 15.5600 |
| b = 0.102109 | | |

II.
$$I_2^u = \langle b+1, -u^2+a+u-2, u^3+2u+1 \rangle$$

(i) Arc colorings

$$a_{5} = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_{3} = \begin{pmatrix} u^{2} - u + 2 \\ -1 \end{pmatrix}$$

$$a_{6} = \begin{pmatrix} 1 \\ -u^{2} \end{pmatrix}$$

$$a_{2} = \begin{pmatrix} u^{2} - u + 1 \\ -1 \end{pmatrix}$$

$$a_{1} = \begin{pmatrix} -1 \\ 0 \end{pmatrix}$$

$$a_{4} = \begin{pmatrix} -1 \\ 0 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} -u \\ -u - 1 \end{pmatrix}$$

$$a_{7} = \begin{pmatrix} u^{2} + 1 \\ u \end{pmatrix}$$

$$a_{9} = \begin{pmatrix} 1 \\ -u - 1 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} u \\ -u^{2} \end{pmatrix}$$

$$a_{8} = \begin{pmatrix} u^{2} + 1 \\ u \end{pmatrix}$$

- (ii) Obstruction class = 1
- (iii) Cusp Shapes = $u^2 3u + 2$

(iv) u-Polynomials at the component

| Crossings | u-Polynomials at each crossing |
|--------------------------|--------------------------------|
| c_1, c_2 | $(u-1)^3$ |
| c_3, c_7 | u^3 |
| c_4 | $(u+1)^3$ |
| c_5, c_6, c_8 | $u^3 + 2u + 1$ |
| <i>c</i> ₉ | $u^3 - 3u^2 + 5u - 2$ |
| c_{10}, c_{11}, c_{12} | $u^3 + 2u - 1$ |

(v) Riley Polynomials at the component

| Crossings | Riley Polynomials at each crossing |
|--|------------------------------------|
| c_1, c_2, c_4 | $(y-1)^3$ |
| c_3, c_7 | y^3 |
| c_5, c_6, c_8 c_{10}, c_{11}, c_{12} | $y^3 + 4y^2 + 4y - 1$ |
| <i>c</i> 9 | $y^3 + y^2 + 13y - 4$ |

(vi) Complex Volumes and Cusp Shapes

| Solutions to I_2^u | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape |
|---------------------------|---------------------------------------|---------------------|
| u = 0.22670 + 1.46771I | | |
| a = -0.329484 - 0.802255I | -11.08570 + 5.13794I | -0.78288 - 3.73768I |
| b = -1.00000 | | |
| u = 0.22670 - 1.46771I | | |
| a = -0.329484 + 0.802255I | -11.08570 - 5.13794I | -0.78288 + 3.73768I |
| b = -1.00000 | | |
| u = -0.453398 | | |
| a = 2.65897 | -0.857735 | 3.56580 |
| b = -1.00000 | | |

III.
$$I_3^u = \langle b+1, u^3+a+u-1, u^4-u^3+2u^2-2u+1 \rangle$$

(i) Arc colorings

$$a_{5} = \begin{pmatrix} 1\\0 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 0\\u \end{pmatrix}$$

$$a_{3} = \begin{pmatrix} -u^{3} - u + 1\\-1 \end{pmatrix}$$

$$a_{6} = \begin{pmatrix} 1\\-u^{2} \end{pmatrix}$$

$$a_{2} = \begin{pmatrix} -u^{3} - u\\-1 \end{pmatrix}$$

$$a_{1} = \begin{pmatrix} -1\\0 \end{pmatrix}$$

$$a_{4} = \begin{pmatrix} -u\\u^{3} - u + 1\\-1 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} -u\\u^{3} + u \end{pmatrix}$$

$$a_{7} = \begin{pmatrix} u^{2} + 1\\-u^{3} - 2u + 1 \end{pmatrix}$$

$$a_{9} = \begin{pmatrix} u^{3} - 2u\\u^{3} + u \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} 2u^{3} - u^{2} + 3u - 3\\-u^{3} + u^{2} - u + 2 \end{pmatrix}$$

$$a_{8} = \begin{pmatrix} u^{2} + 1\\-u^{3} - 2u + 1 \end{pmatrix}$$

- (ii) Obstruction class = 1
- (iii) Cusp Shapes = $-5u^3 + 2u^2 6u + 5$

(iv) u-Polynomials at the component

| Crossings | u-Polynomials at each crossing |
|--------------------------|--------------------------------|
| c_1, c_2 | $(u-1)^4$ |
| c_3, c_7 | u^4 |
| <i>c</i> ₄ | $(u+1)^4$ |
| c_5, c_6, c_8 | $u^4 - u^3 + 2u^2 - 2u + 1$ |
| <i>c</i> 9 | $(u^2+u+1)^2$ |
| c_{10}, c_{11}, c_{12} | $u^4 + u^3 + 2u^2 + 2u + 1$ |

(v) Riley Polynomials at the component

| Crossings | Riley Polynomials at each crossing |
|---|------------------------------------|
| c_1, c_2, c_4 | $(y-1)^4$ |
| c_3, c_7 | y^4 |
| $c_5, c_6, c_8 \\ c_{10}, c_{11}, c_{12}$ | $y^4 + 3y^3 + 2y^2 + 1$ |
| c_9 | $(y^2+y+1)^2$ |

(vi) Complex Volumes and Cusp Shapes

| Solutions to I_3^u | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape |
|---------------------------|---------------------------------------|---------------------|
| u = 0.621744 + 0.440597I | | |
| a = 0.500000 - 0.866025I | -4.93480 + 2.02988I | 2.26314 - 3.67497I |
| b = -1.00000 | | |
| u = 0.621744 - 0.440597I | | |
| a = 0.500000 + 0.866025I | -4.93480 - 2.02988I | 2.26314 + 3.67497I |
| b = -1.00000 | | |
| u = -0.121744 + 1.306620I | | |
| a = 0.500000 + 0.866025I | -4.93480 - 2.02988I | -0.76314 + 2.38721I |
| b = -1.00000 | | |
| u = -0.121744 - 1.306620I | | |
| a = 0.500000 - 0.866025I | -4.93480 + 2.02988I | -0.76314 - 2.38721I |
| b = -1.00000 | | |

IV. u-Polynomials

| Crossings | u-Polynomials at each crossing |
|------------------|---|
| c_1 | $((u-1)^7)(u^{11} + 30u^{10} + \dots + 93u + 1)$ |
| c_2 | $((u-1)^7)(u^{11} - 8u^{10} + \dots + 13u - 1)$ |
| c_3, c_7 | $u^{7}(u^{11} - u^{10} + \dots - 64u - 128)$ |
| C4 | $((u+1)^7)(u^{11}-8u^{10}+\cdots+13u-1)$ |
| c_5, c_6 | $(u^3 + 2u + 1)(u^4 - u^3 + 2u^2 - 2u + 1)(u^{11} - 2u^{10} + \dots + 2u - 1)$ |
| c ₈ | $(u^{3} + 2u + 1)(u^{4} - u^{3} + 2u^{2} - 2u + 1)$ $\cdot (u^{11} + 12u^{9} + 38u^{7} + 2u^{6} + 14u^{5} + 12u^{4} + 13u^{3} + u^{2} - 1)$ |
| <i>c</i> 9 | $((u^{2}+u+1)^{2})(u^{3}-3u^{2}+5u-2)(u^{11}+2u^{10}+\cdots-15u^{2}-8)$ |
| c_{10} | $(u^3 + 2u - 1)(u^4 + u^3 + 2u^2 + 2u + 1)(u^{11} - 2u^{10} + \dots + 2u - 1)$ |
| c_{11}, c_{12} | $(u^{3} + 2u - 1)(u^{4} + u^{3} + 2u^{2} + 2u + 1)$ $\cdot (u^{11} + 12u^{9} + 38u^{7} + 2u^{6} + 14u^{5} + 12u^{4} + 13u^{3} + u^{2} - 1)$ |

V. Riley Polynomials

| Crossings | Riley Polynomials at each crossing |
|-----------------------|--|
| c_1 | $((y-1)^7)(y^{11} - 202y^{10} + \dots + 8901y - 1)$ |
| c_2, c_4 | $((y-1)^7)(y^{11}-30y^{10}+\cdots+93y-1)$ |
| c_3, c_7 | $y^7(y^{11} + 81y^{10} + \dots + 192512y - 16384)$ |
| c_5, c_6, c_{10} | $(y^3 + 4y^2 + 4y - 1)(y^4 + 3y^3 + 2y^2 + 1)(y^{11} + 12y^{10} + \dots + 2y - 1)$ |
| c_8, c_{11}, c_{12} | $(y^3 + 4y^2 + 4y - 1)(y^4 + 3y^3 + 2y^2 + 1)(y^{11} + 24y^{10} + \dots + 2y - 1)$ |
| <i>C</i> 9 | $((y^2 + y + 1)^2)(y^3 + y^2 + 13y - 4)(y^{11} + 12y^{10} + \dots - 240y - 64)$ |