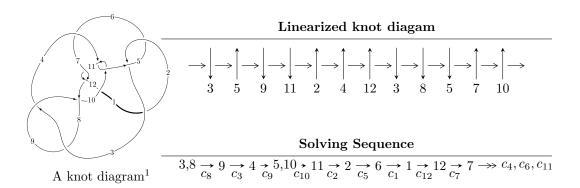
# $12n_{0447} (K12n_{0447})$



#### Ideals for irreducible components<sup>2</sup> of $X_{par}$

$$I_1^u = \langle -2.24038 \times 10^{33} u^{47} - 1.35892 \times 10^{32} u^{46} + \dots + 2.30349 \times 10^{33} b + 1.34156 \times 10^{34},$$

$$1.73741 \times 10^{34} u^{47} - 3.00948 \times 10^{33} u^{46} + \dots + 1.15175 \times 10^{34} a - 1.11706 \times 10^{35}, \ u^{48} - u^{47} + \dots - 2u + 5 \rangle$$

$$I_2^u = \langle -u^2 a + u^3 + b + a - u, \ a^2 u^2 + a^3 + 1, \ u^4 - u^2 + 1 \rangle$$

\* 2 irreducible components of  $\dim_{\mathbb{C}} = 0$ , with total 60 representations.

<sup>&</sup>lt;sup>1</sup>The image of knot diagram is generated by the software "**Draw programme**" developed by Andrew Bartholomew(http://www.layer8.co.uk/maths/draw/index.htm#Running-draw), where we modified some parts for our purpose(https://github.com/CATsTAILs/LinksPainter).

 $<sup>^2</sup>$  All coefficients of polynomials are rational numbers. But the coefficients are sometimes approximated in decimal forms when there is not enough margin.

 $\begin{matrix} \text{I.} \\ I_1^u = \langle -2.24 \times 10^{33} u^{47} - 1.36 \times 10^{32} u^{46} + \dots + 2.30 \times 10^{33} b + 1.34 \times 10^{34}, \ 1.74 \times 10^{34} u^{47} - 3.01 \times 10^{33} u^{46} + \dots + 1.15 \times 10^{34} a - 1.12 \times 10^{35}, \ u^{48} - u^{47} + \dots - 2u + 5 \rangle \end{matrix}$ 

(i) Arc colorings

$$a_{3} = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_{8} = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{9} = \begin{pmatrix} 1 \\ u^{2} \end{pmatrix}$$

$$a_{4} = \begin{pmatrix} -u \\ -u^{3} + u \end{pmatrix}$$

$$a_{5} = \begin{pmatrix} -1.50850u^{47} + 0.261297u^{46} + \dots + 4.48572u + 9.69889 \\ 0.972603u^{47} + 0.0589938u^{46} + \dots - 0.659198u - 5.82402 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} -u^{2} + 1 \\ u^{2} \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 1.16480u^{47} - 0.192201u^{46} + \dots - 4.27812u - 2.98881 \\ 1.24721u^{47} - 0.462790u^{46} + \dots - 6.68188u - 7.54251 \end{pmatrix}$$

$$a_{2} = \begin{pmatrix} 1.76087u^{47} + 0.00355222u^{46} + \dots - 4.42873u - 9.58615 \\ 0.817561u^{47} - 0.0937876u^{46} + \dots - 5.25658u - 6.61698 \end{pmatrix}$$

$$a_{6} = \begin{pmatrix} -1.61232u^{47} + 0.251322u^{46} + \dots + 3.62117u + 8.11692 \\ -0.821845u^{47} + 0.0692617u^{46} + \dots + 6.06620u + 5.24702 \end{pmatrix}$$

$$a_{1} = \begin{pmatrix} 1.76087u^{47} + 0.00355222u^{46} + \dots + 4.42873u - 9.58615 \\ -0.673929u^{47} - 0.140698u^{46} + \dots + 0.0189389u + 2.20515 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} 1.78030u^{47} + 0.0974277u^{46} + \dots - 4.61437u - 9.37957 \\ 0.553189u^{47} - 0.0489697u^{46} + \dots - 3.34948u - 4.95558 \end{pmatrix}$$

$$a_{7} = \begin{pmatrix} -2.55276u^{47} + 0.387556u^{46} + \dots + 8.31343u + 13.4329 \\ -0.486776u^{47} + 0.132833u^{46} + \dots + 4.46775u + 3.95207 \end{pmatrix}$$

- (ii) Obstruction class = -1
- (iii) Cusp Shapes =  $-0.327963u^{47} 0.0729656u^{46} + \cdots 4.23858u 0.466106$

### (iv) u-Polynomials at the component

| Crossings     | u-Polynomials at each crossing                  |
|---------------|---|
| $c_1$         | $u^{48} + 53u^{47} + \dots - 27678u + 289$      |
| $c_2, c_5$    | $u^{48} + 3u^{47} + \dots - 142u + 17$          |
| $c_3, c_8$    | $u^{48} - u^{47} + \dots - 2u + 5$              |
| $c_4, c_{10}$ | $u^{48} - u^{47} + \dots - 8u + 1$              |
| $c_6$         | $u^{48} + 5u^{47} + \dots - 7742u + 26561$      |
| $c_7, c_{11}$ | $u^{48} - u^{47} + \dots - 14u + 1$             |
| <i>c</i> 9    | $u^{48} + 29u^{47} + \dots - 36u + 25$          |
| $c_{12}$      | $u^{48} + 3u^{47} + \dots + 4284478u + 1826857$ |

### (v) Riley Polynomials at the component

| Crossings             | Riley Polynomials at each crossing                            |
|-----------------------|---|
| $c_1$                 | $y^{48} - 111y^{47} + \dots - 298879486y + 83521$             |
| $c_2, c_5$            | $y^{48} + 53y^{47} + \dots - 27678y + 289$                    |
| $c_{3}, c_{8}$        | $y^{48} - 29y^{47} + \dots + 36y + 25$                        |
| $c_4, c_{10}$         | $y^{48} + 13y^{47} + \dots + 14y + 1$                         |
| <i>C</i> <sub>6</sub> | $y^{48} + 31y^{47} + \dots + 12208109238y + 705486721$        |
| $c_7, c_{11}$         | $y^{48} - 39y^{47} + \dots - 86y + 1$                         |
| $c_9$                 | $y^{48} - 13y^{47} + \dots - 28896y + 625$                    |
| $c_{12}$              | $y^{48} + 41y^{47} + \dots + 44880385612764y + 3337406498449$ |

# (vi) Complex Volumes and Cusp Shapes

| Solutions to $I_1^u$                                | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape  |
|---|---------------------------------------|---|
| u = -0.108352 + 0.991513I                           |                                       |   |
| a = -1.65182 - 0.00446I                             | -7.23468 - 3.54967I                   | -1.53238 + 2.33493I                                   |
| b = 1.36066 + 0.53287I                              |                                       |   |
| u = -0.108352 - 0.991513I                           | 7 99469 + 9 540671                    | 1 52020 0 224027                                      |
| a = -1.65182 + 0.00446I                             | -7.23468 + 3.54967I                   | -1.53238 - 2.33493I                                   |
| b = 1.36066 - 0.53287I $u = 0.174873 + 0.981711I$   |                                       |   |
| a = 0.77425 + 0.00932I $a = 1.74425 + 0.00932I$     | -2.92990 + 8.29102I                   | 2.36664 - 4.88040I                                    |
| b = -1.41834 + 0.60453I                             | 2.02000   0.201021                    | 2.90001 1.000101                                      |
| u = 0.174873 - 0.981711I                            |                                       |   |
| a = 1.74425 - 0.00932I                              | -2.92990 - 8.29102I                   | 2.36664 + 4.88040I                                    |
| b = -1.41834 - 0.60453I                             |                                       |   |
| u = 0.030174 + 0.983574I                            |                                       |   |
| a = 1.55380 - 0.03101I                              | -3.56945 - 1.27655I                   | 1.43121 + 0.83260I                                    |
| b = -1.287640 + 0.465293I                           |                                       |   |
| u = 0.030174 - 0.983574I                            |                                       |   |
| a = 1.55380 + 0.03101I                              | -3.56945 + 1.27655I                   | 1.43121 - 0.83260I                                    |
| b = -1.287640 - 0.465293I                           |                                       |   |
| u = 0.881157 + 0.424614I                            | 0.00000 . 0.700101                    | 0 504155 . 0 055100 5                                 |
| a = -1.141540 - 0.360327I                           | 3.03026 + 0.73910I                    | -0.764157 + 0.955160I                                 |
| b = 0.731724 - 0.770961I $u = 0.881157 - 0.424614I$ |                                       |   |
| a = -1.141540 + 0.360327I                           | 3.03026 - 0.73910I                    | $\begin{vmatrix} -0.764157 - 0.955160I \end{vmatrix}$ |
| b = 0.731724 + 0.770961I                            | 0.00020 0.700101                      | 0.704107 0.3001001                                    |
| u = -0.955184 + 0.061016I                           |                                       |   |
| a = -0.450503 + 1.000600I                           | -0.935829 + 0.351963I                 | -4.28024 + 0.58826I                                   |
| b = -1.139020 - 0.816551I                           |                                       |   |
| u = -0.955184 - 0.061016I                           |                                       |   |
| a = -0.450503 - 1.000600I                           | -0.935829 - 0.351963I                 | -4.28024 - 0.58826I                                   |
| b = -1.139020 + 0.816551I                           |                                       |   |

| Solutions to $I_1^u$      | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape           |
|---------------------------|---------------------------------------|----------------------|
| u = 0.819695 + 0.488889I  |                                       |                      |
| a = 0.108560 - 0.099280I  | 1.72059 - 2.04540I                    | 7.89567 + 4.02405I   |
| b = 0.818403 - 0.513954I  |                                       |                      |
| u = 0.819695 - 0.488889I  |                                       |                      |
| a = 0.108560 + 0.099280I  | 1.72059 + 2.04540I                    | 7.89567 - 4.02405I   |
| b = 0.818403 + 0.513954I  |                                       |                      |
| u = -0.895933 + 0.584550I |                                       |                      |
| a = 0.571984 - 0.664326I  | -1.17884 + 2.22567I                   | -5.86884 - 3.07805I  |
| b = -0.915407 - 0.330137I |                                       |                      |
| u = -0.895933 - 0.584550I |                                       |                      |
| a = 0.571984 + 0.664326I  | -1.17884 - 2.22567I                   | -5.86884 + 3.07805I  |
| b = -0.915407 + 0.330137I |                                       |                      |
| u = 1.079750 + 0.223592I  |                                       |                      |
| a = 0.106506 + 0.739409I  | 1.98776 - 3.98499I                    | -0.58611 + 4.25564I  |
| b = 1.081550 - 0.643185I  |                                       |                      |
| u = 1.079750 - 0.223592I  |                                       |                      |
| a = 0.106506 - 0.739409I  | 1.98776 + 3.98499I                    | -0.58611 - 4.25564I  |
| b = 1.081550 + 0.643185I  |                                       |                      |
| u = 0.665759 + 0.587232I  |                                       |                      |
| a = -0.797687 - 0.156330I | 2.86945 + 0.64829I                    | 1.178037 - 0.420823I |
| b = 0.764248 - 0.205453I  |                                       |                      |
| u = 0.665759 - 0.587232I  |                                       |                      |
| a = -0.797687 + 0.156330I | 2.86945 - 0.64829I                    | 1.178037 + 0.420823I |
| b = 0.764248 + 0.205453I  |                                       |                      |
| u = 0.896239 + 0.683994I  |                                       |                      |
| a = -0.334230 - 0.804354I | 2.31381 - 5.68856I                    | 0.35737 + 7.14815I   |
| b = 0.831578 - 0.212398I  |                                       |                      |
| u = 0.896239 - 0.683994I  |                                       |                      |
| a = -0.334230 + 0.804354I | 2.31381 + 5.68856I                    | 0.35737 - 7.14815I   |
| b = 0.831578 + 0.212398I  |                                       |                      |

| Solutions to $I_1^u$      | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape          |
|---------------------------|---------------------------------------|---------------------|
| u = -1.129410 + 0.115901I |                                       |                     |
| a = 0.528176 + 0.194049I  | -2.25793 + 0.22669I                   | -3.88130 + 0.48636I |
| b = 0.823353 - 0.308996I  |                                       |                     |
| u = -1.129410 - 0.115901I |                                       |                     |
| a = 0.528176 - 0.194049I  | -2.25793 - 0.22669I                   | -3.88130 - 0.48636I |
| b = 0.823353 + 0.308996I  |                                       |                     |
| u = 0.841927 + 0.080741I  |                                       |                     |
| a = 0.86370 - 1.44512I    | 3.83049 - 3.07305I                    | 1.41041 + 1.51798I  |
| b = 1.24610 + 1.12698I    |                                       |                     |
| u = 0.841927 - 0.080741I  |                                       |                     |
| a = 0.86370 + 1.44512I    | 3.83049 + 3.07305I                    | 1.41041 - 1.51798I  |
| b = 1.24610 - 1.12698I    |                                       |                     |
| u = -0.994669 + 0.588297I |                                       |                     |
| a = 0.296924 + 0.239330I  | 4.59952 + 2.16567I                    | 4.10775 - 1.86694I  |
| b = -0.984134 - 0.447751I |                                       |                     |
| u = -0.994669 - 0.588297I |                                       |                     |
| a = 0.296924 - 0.239330I  | 4.59952 - 2.16567I                    | 4.10775 + 1.86694I  |
| b = -0.984134 + 0.447751I |                                       |                     |
| u = -1.112110 + 0.405732I |                                       |                     |
| a = 0.779825 + 1.100780I  | 2.60733 + 6.94232I                    | 0.84068 - 7.46411I  |
| b = 1.22762 - 1.41031I    |                                       |                     |
| u = -1.112110 - 0.405732I |                                       |                     |
| a = 0.779825 - 1.100780I  | 2.60733 - 6.94232I                    | 0.84068 + 7.46411I  |
| b = 1.22762 + 1.41031I    |                                       |                     |
| u = -0.555750 + 0.577343I |                                       |                     |
| a = -0.416557 - 0.803655I | 5.85592 + 2.51809I                    | 7.55361 - 3.16560I  |
| b = -0.515683 - 0.475483I |                                       |                     |
| u = -0.555750 - 0.577343I |                                       |                     |
| a = -0.416557 + 0.803655I | 5.85592 - 2.51809I                    | 7.55361 + 3.16560I  |
| b = -0.515683 + 0.475483I |                                       |                     |
|                           |                                       |                     |

| $\begin{array}{c} u = 1.163420 + 0.303926I \\ a = -0.536341 + 0.659705I \\ b = -1.100960 - 0.856931I \\ \hline u = 1.163420 - 0.303926I \\ a = -0.536341 - 0.659705I \\ b = -1.100960 + 0.856931I \\ \hline u = 1.262720 + 0.577522I \\ a = 0.268798 + 1.336830I \\ b = -2.09613 - 0.86670I \\ \hline u = 1.262720 - 0.577522I \\ a = 0.268798 - 1.336830I \\ b = -2.09613 + 0.86670I \\ \hline u = -1.343520 + 0.367319I \\ a = 0.348682 - 1.226170I \\ b = -1.204320 + 0.348043I \\ \hline u = 1.304590 + 0.505937I \\ a = 0.147430 + 1.094530I \\ b = -1.88535 - 0.79417I \\ \hline u = -1.318780 + 0.470886I \\ a = 0.389956 + 1.214920I \\ b = -1.162380 - 0.271439I \\ \hline u = -1.318780 - 0.470886I \\ a = 0.389956 + 1.214920I \\ b = -1.162380 - 0.271439I \\ \hline \end{array}$   | Solutions to $I_1^u$      | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape          |
|---|---------------------------|---------------------------------------|---------------------|
| $\begin{array}{c} b = -1.100960 - 0.856931I \\ \hline u = 1.163420 - 0.303926I \\ a = -0.536341 - 0.659705I \\ b = -1.100960 + 0.856931I \\ \hline u = 1.262720 + 0.577522I \\ a = 0.268798 + 1.336830I \\ b = -2.09613 - 0.86670I \\ \hline u = 1.262720 - 0.577522I \\ a = 0.268798 - 1.336830I \\ \hline b = -2.09613 + 0.86670I \\ \hline u = 1.343520 + 0.36670I \\ \hline u = -1.343520 + 0.36670I \\ \hline u = -1.343520 + 0.367319I \\ a = 0.348682 - 1.226170I \\ b = -1.204320 + 0.348043I \\ \hline u = -1.343520 - 0.367319I \\ a = 0.348682 + 1.226170I \\ b = -1.204320 + 0.348043I \\ \hline u = 1.304590 + 0.505937I \\ a = 0.147430 + 1.094530I \\ b = -1.88535 - 0.79417I \\ \hline u = 1.318780 + 0.470886I \\ a = 0.389956 + 1.214920I \\ a = 0.389956 + 1.2$  | u = 1.163420 + 0.303926I  |                                       |                     |
| $\begin{array}{c} u = & 1.163420 - 0.303926I \\ a = & -0.536341 - 0.659705I \\ b = & -1.100960 + 0.856931I \\ \hline u = & 1.262720 + 0.577522I \\ a = & 0.268798 + 1.336830I \\ b = & -2.09613 - 0.86670I \\ \hline u = & 1.262720 - 0.577522I \\ a = & 0.268798 - 1.336830I \\ b = & -2.09613 - 0.86670I \\ \hline u = & 1.262720 - 0.577522I \\ a = & 0.268798 - 1.336830I \\ b = & -2.09613 + 0.86670I \\ \hline u = & -1.343520 + 0.367319I \\ a = & 0.348682 - 1.226170I \\ b = & -1.204320 + 0.348043I \\ \hline u = & -1.343520 - 0.367319I \\ a = & 0.348682 + 1.226170I \\ b = & -1.204320 - 0.348043I \\ \hline u = & 1.304590 + 0.505937I \\ a = & 0.147430 + 1.094530I \\ b = & -1.88535 - 0.79417I \\ \hline u = & 1.304590 - 0.505937I \\ a = & 0.147430 - 1.094530I \\ b = & -1.88535 + 0.79417I \\ \hline u = & -1.318780 + 0.470886I \\ a = & 0.389956 - 1.214920I \\ a = & 0.389956 + 1.2$   | a = -0.536341 + 0.659705I | -3.28855 - 4.12116I                   | -4.45892 + 6.35434I |
| $\begin{array}{c} a = -0.536341 - 0.659705I \\ b = -1.100960 + 0.856931I \\ \hline u = 1.262720 + 0.577522I \\ a = 0.268798 + 1.336830I \\ b = -2.09613 - 0.86670I \\ \hline u = 1.262720 - 0.577522I \\ a = 0.268798 - 1.336830I \\ b = -2.09613 + 0.86670I \\ \hline u = -1.343520 + 0.367319I \\ a = 0.348682 - 1.226170I \\ a = 0.348682 - 1.226170I \\ b = -1.204320 + 0.348043I \\ \hline u = -1.343520 - 0.367319I \\ a = 0.348682 + 1.226170I \\ b = -1.204320 - 0.348043I \\ \hline u = 1.304590 + 0.505937I \\ a = 0.147430 + 1.094530I \\ b = -1.88535 - 0.79417I \\ \hline u = 1.318780 + 0.470886I \\ a = 0.389956 + 1.214920I \\ a = 0.778759 - 6.42660I \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \\$   | b = -1.100960 - 0.856931I |                                       |                     |
| $\begin{array}{c} b = -1.100960 + 0.856931I \\ u = 1.262720 + 0.577522I \\ a = 0.268798 + 1.336830I & -6.2609 - 13.9095I & 0 \\ b = -2.09613 - 0.86670I \\ u = 1.262720 - 0.577522I \\ a = 0.268798 - 1.336830I & -6.2609 + 13.9095I & 0 \\ b = -2.09613 + 0.86670I \\ u = -1.343520 + 0.367319I \\ a = 0.348682 - 1.226170I & -7.84517 - 3.63200I & 0 \\ b = -1.204320 + 0.348043I \\ u = -1.343520 - 0.367319I \\ a = 0.348682 + 1.226170I & -7.84517 + 3.63200I & 0 \\ b = -1.204320 - 0.348043I & 0 \\ u = 1.304590 + 0.505937I \\ a = 0.147430 + 1.094530I & -7.51956 - 4.03416I & 0 \\ b = -1.88535 - 0.79417I \\ u = 1.304590 - 0.505937I \\ a = 0.147430 - 1.094530I & -7.51956 + 4.03416I & 0 \\ b = -1.88535 + 0.79417I & 0 \\ u = -1.318780 + 0.470886I \\ a = 0.389956 - 1.214920I & -7.78759 + 6.42660I & 0 \\ b = -1.162380 + 0.271439I \\ u = -1.318780 - 0.470886I \\ a = 0.389956 + 1.214920I & -7.78759 - 6.42660I & 0 \\ \end{array}$  | u = 1.163420 - 0.303926I  |                                       |                     |
| $\begin{array}{c} u = & 1.262720 + 0.577522I \\ a = & 0.268798 + 1.336830I \\ b = & -2.09613 - 0.86670I \\ \hline u = & 1.262720 - 0.577522I \\ a = & 0.268798 - 1.336830I \\ b = & -2.09613 + 0.86670I \\ \hline u = & -1.343520 + 0.367319I \\ a = & 0.348682 - 1.226170I \\ b = & -1.204320 + 0.348043I \\ \hline u = & -1.343520 - 0.367319I \\ a = & 0.348682 + 1.226170I \\ a = & 0.348682 + 1.226170I \\ a = & 0.348682 + 1.226170I \\ a = & 0.348682 + 0.348043I \\ \hline u = & -1.204320 - 0.348043I \\ \hline u = & 1.304590 + 0.505937I \\ a = & 0.147430 + 1.094530I \\ a = & 0.147430 - 1.094530I \\ a = & 0.389956 - 1.214920I \\ a = & 0.389956 - 1.214920I \\ a = & 0.389956 + 1.214920I \\ a = & 0.38956 + 1.214920I \\ a = $   | a = -0.536341 - 0.659705I | -3.28855 + 4.12116I                   | -4.45892 - 6.35434I |
| $\begin{array}{c} a = & 0.268798 + 1.336830I \\ b = -2.09613 - 0.86670I \\ \hline u = & 1.262720 - 0.577522I \\ a = & 0.268798 - 1.336830I \\ \hline b = -2.09613 + 0.86670I \\ \hline u = & -1.343520 + 0.367319I \\ a = & 0.348682 - 1.226170I \\ \hline b = & -1.204320 + 0.348043I \\ \hline u = & -1.343520 - 0.367319I \\ a = & 0.348682 + 1.226170I \\ \hline a = & 0.348682 + 1.226170I \\ \hline a = & 0.348682 + 0.348043I \\ \hline u = & -1.304520 - 0.348043I \\ \hline u = & 1.304590 + 0.505937I \\ a = & 0.147430 + 1.094530I \\ \hline a = & 0.147430 - 1.094530I \\ \hline a = & 0.147430 - 1.094530I \\ \hline a = & 0.147430 - 1.094530I \\ \hline a = & 0.147430 + 0.470886I \\ a = & 0.389956 - 1.214920I \\ \hline a = & 0.389956 + 1.214920I \\ \hline a = & 0$      | b = -1.100960 + 0.856931I |                                       |                     |
| $\begin{array}{c} b = -2.09613 - 0.86670I \\ u = 1.262720 - 0.577522I \\ a = 0.268798 - 1.336830I & -6.2609 + 13.9095I \\ b = -2.09613 + 0.86670I \\ u = -1.343520 + 0.367319I \\ a = 0.348682 - 1.226170I & -7.84517 - 3.63200I \\ b = -1.204320 + 0.348043I \\ u = -1.343520 - 0.367319I \\ a = 0.348682 + 1.226170I & -7.84517 + 3.63200I \\ b = -1.204320 - 0.348043I \\ u = 1.304590 + 0.505937I \\ a = 0.147430 + 1.094530I & -7.51956 - 4.03416I \\ b = -1.88535 - 0.79417I \\ u = 1.304590 - 0.505937I \\ a = 0.147430 - 1.094530I & -7.51956 + 4.03416I \\ b = -1.88535 + 0.79417I \\ u = -1.318780 + 0.470886I \\ a = 0.389956 - 1.214920I & -7.78759 + 6.42660I \\ b = -1.162380 + 0.271439I \\ u = -1.318780 - 0.470886I \\ a = 0.389956 + 1.214920I & -7.78759 - 6.42660I \\ 0 \end{array}$  | u = 1.262720 + 0.577522I  |                                       |                     |
| $\begin{array}{c} u = & 1.262720 - 0.577522I \\ a = & 0.268798 - 1.336830I \\ b = -2.09613 + 0.86670I \\ \hline u = -1.343520 + 0.367319I \\ a = & 0.348682 - 1.226170I \\ \hline b = -1.204320 + 0.348043I \\ \hline u = -1.343520 - 0.367319I \\ a = & 0.348682 + 1.226170I \\ \hline b = -1.204320 - 0.348043I \\ \hline u = & 1.304590 + 0.505937I \\ a = & 0.147430 + 1.094530I \\ \hline b = -1.88535 - 0.79417I \\ \hline u = & 1.304590 - 0.505937I \\ a = & 0.147430 - 1.094530I \\ \hline b = -1.88535 + 0.79417I \\ \hline u = & -1.318780 + 0.470886I \\ a = & 0.389956 - 1.214920I \\ a = & 0.389956 + 1.214920I \\ \hline a = & 0.389956 + 1.21$                | a = 0.268798 + 1.336830I  | -6.2609 - 13.9095I                    | 0                   |
| $\begin{array}{c} a = & 0.268798 - 1.336830I \\ b = -2.09613 + 0.86670I \\ \hline u = -1.343520 + 0.367319I \\ a = & 0.348682 - 1.226170I \\ b = -1.204320 + 0.348043I \\ \hline u = -1.343520 - 0.367319I \\ a = & 0.348682 + 1.226170I \\ b = -1.204320 - 0.348043I \\ \hline u = & 0.348682 + 1.226170I \\ b = -1.204320 - 0.348043I \\ \hline u = & 1.304590 + 0.505937I \\ a = & 0.147430 + 1.094530I \\ b = -1.88535 - 0.79417I \\ \hline u = & 1.304590 - 0.505937I \\ a = & 0.147430 - 1.094530I \\ b = -1.88535 + 0.79417I \\ \hline u = & -1.318780 + 0.470886I \\ a = & 0.389956 - 1.214920I \\ a = & 0.138780 - 0.470886I \\ a = & 0.389956 + 1.214920I \\ \hline a$                                   | b = -2.09613 - 0.86670I   |                                       |                     |
| $\begin{array}{c} b = -2.09613 + 0.86670I \\ u = -1.343520 + 0.367319I \\ a = 0.348682 - 1.226170I - 7.84517 - 3.63200I \\ b = -1.204320 + 0.348043I \\ \hline u = -1.343520 - 0.367319I \\ a = 0.348682 + 1.226170I - 7.84517 + 3.63200I \\ b = -1.204320 - 0.348043I \\ \hline u = 1.304590 + 0.505937I \\ a = 0.147430 + 1.094530I - 7.51956 - 4.03416I \\ b = -1.88535 - 0.79417I \\ \hline u = 1.304590 - 0.505937I \\ a = 0.147430 - 1.094530I - 7.51956 + 4.03416I \\ b = -1.88535 + 0.79417I \\ \hline u = -1.318780 + 0.470886I \\ a = 0.389956 - 1.214920I - 7.78759 + 6.42660I \\ b = -1.162380 + 0.271439I \\ \hline u = -1.318780 - 0.470886I \\ a = 0.389956 + 1.214920I - 7.78759 - 6.42660I \\ a = 0.389956 + 1.214920I - 7.78759 - 6.42660I \\ \end{array}$  | u = 1.262720 - 0.577522I  |                                       |                     |
| $\begin{array}{c} u = -1.343520 + 0.367319I \\ a = 0.348682 - 1.226170I \\ b = -1.204320 + 0.348043I \\ \hline \\ u = -1.343520 - 0.367319I \\ a = 0.348682 + 1.226170I \\ b = -1.204320 - 0.348043I \\ \hline \\ u = 1.304590 + 0.505937I \\ a = 0.147430 + 1.094530I \\ b = -1.88535 - 0.79417I \\ \hline \\ u = 1.304590 - 0.505937I \\ a = 0.147430 - 1.094530I \\ b = -1.88535 + 0.79417I \\ \hline \\ u = -1.318780 + 0.470886I \\ a = 0.389956 - 1.214920I \\ a = 0.389956 + 1.21492$  | a = 0.268798 - 1.336830I  | -6.2609 + 13.9095I                    | 0                   |
| $\begin{array}{cccccccccccccccccccccccccccccccccccc$  |                           |                                       |                     |
| $\begin{array}{c} b = -1.204320 + 0.348043I \\ \hline u = -1.343520 - 0.367319I \\ a = 0.348682 + 1.226170I & -7.84517 + 3.63200I \\ b = -1.204320 - 0.348043I \\ \hline u = 1.304590 + 0.505937I \\ a = 0.147430 + 1.094530I & -7.51956 - 4.03416I \\ \hline u = 1.304590 - 0.505937I \\ a = 0.147430 - 1.094530I & -7.51956 + 4.03416I \\ \hline u = 1.304590 - 0.505937I \\ a = 0.147430 - 1.094530I & -7.51956 + 4.03416I \\ \hline u = -1.318780 + 0.470886I \\ a = 0.389956 - 1.214920I & -7.78759 + 6.42660I \\ \hline u = -1.318780 - 0.470886I \\ a = 0.389956 + 1.214920I & -7.78759 - 6.42660I \\ \hline a = 0.389956 + 1.214920I & -7.78759 - 6.42660I \\ \hline \end{array}$   | u = -1.343520 + 0.367319I |                                       |                     |
| $\begin{array}{c} u = -1.343520 - 0.367319I \\ a = 0.348682 + 1.226170I \\ b = -1.204320 - 0.348043I \\ \hline u = 1.304590 + 0.505937I \\ a = 0.147430 + 1.094530I \\ b = -1.88535 - 0.79417I \\ \hline u = 1.304590 - 0.505937I \\ a = 0.147430 - 1.094530I \\ a = 0.147430 - 1.094530I \\ a = 0.188535 + 0.79417I \\ \hline u = -1.318780 + 0.470886I \\ a = 0.389956 - 1.214920I \\ a = 0.389956 + 1.214920I \\ \hline u = -1.318780 - 0.470886I \\ a = 0.389956 + 1.214920I \\ \hline a = 0.389956 + 1.214920I \\ $ | a = 0.348682 - 1.226170I  | -7.84517 - 3.63200I                   | 0                   |
| $\begin{array}{cccccccccccccccccccccccccccccccccccc$  | b = -1.204320 + 0.348043I |                                       |                     |
| $\begin{array}{c} b = -1.204320 - 0.348043I \\ \hline u = 1.304590 + 0.505937I \\ a = 0.147430 + 1.094530I & -7.51956 - 4.03416I & 0 \\ b = -1.88535 - 0.79417I \\ \hline u = 1.304590 - 0.505937I \\ a = 0.147430 - 1.094530I & -7.51956 + 4.03416I & 0 \\ b = -1.88535 + 0.79417I \\ \hline u = -1.318780 + 0.470886I \\ a = 0.389956 - 1.214920I & -7.78759 + 6.42660I & 0 \\ b = -1.162380 + 0.271439I \\ \hline u = -1.318780 - 0.470886I \\ a = 0.389956 + 1.214920I & -7.78759 - 6.42660I & 0 \\ \end{array}$  | u = -1.343520 - 0.367319I |                                       |                     |
| $\begin{array}{c} u = & 1.304590 + 0.505937I \\ a = & 0.147430 + 1.094530I \\ b = -1.88535 - 0.79417I \\ \hline u = & 1.304590 - 0.505937I \\ a = & 0.147430 - 1.094530I \\ b = -1.88535 + 0.79417I \\ \hline u = -1.318780 + 0.470886I \\ a = & 0.389956 - 1.214920I \\ \hline u = -1.318780 - 0.470886I \\ a = & 0.389956 + 1.214920I \\ \hline u = -1.318780 - 0.470886I \\ a = & 0.389956 + 1.214920I \\ \hline \end{array}$  | a = 0.348682 + 1.226170I  | -7.84517 + 3.63200I                   | 0                   |
| $\begin{array}{c} a = & 0.147430 + 1.094530I & -7.51956 - 4.03416I & 0 \\ b = -1.88535 - 0.79417I & & & & \\ \hline u = & 1.304590 - 0.505937I & & & & \\ a = & 0.147430 - 1.094530I & -7.51956 + 4.03416I & 0 \\ b = -1.88535 + 0.79417I & & & & \\ \hline u = -1.318780 + 0.470886I & & & \\ a = & 0.389956 - 1.214920I & -7.78759 + 6.42660I & 0 \\ b = -1.162380 + 0.271439I & & & \\ \hline u = -1.318780 - 0.470886I & & & \\ a = & 0.389956 + 1.214920I & -7.78759 - 6.42660I & 0 \\ \end{array}$  | b = -1.204320 - 0.348043I |                                       |                     |
| $\begin{array}{c} b = -1.88535 - 0.79417I \\ u = 1.304590 - 0.505937I \\ a = 0.147430 - 1.094530I - 7.51956 + 4.03416I \\ b = -1.88535 + 0.79417I \\ \hline u = -1.318780 + 0.470886I \\ a = 0.389956 - 1.214920I - 7.78759 + 6.42660I \\ b = -1.162380 + 0.271439I \\ \hline u = -1.318780 - 0.470886I \\ a = 0.389956 + 1.214920I - 7.78759 - 6.42660I \\ \end{array}$  | u = 1.304590 + 0.505937I  |                                       |                     |
| $\begin{array}{c} u = & 1.304590 - 0.505937I \\ a = & 0.147430 - 1.094530I - 7.51956 + 4.03416I & 0 \\ b = & -1.88535 + 0.79417I & 0 \\ u = & -1.318780 + 0.470886I \\ a = & 0.389956 - 1.214920I - 7.78759 + 6.42660I & 0 \\ b = & -1.162380 + 0.271439I \\ u = & -1.318780 - 0.470886I \\ a = & 0.389956 + 1.214920I - 7.78759 - 6.42660I & 0 \\ \end{array}$   | a = 0.147430 + 1.094530I  | -7.51956 - 4.03416I                   | 0                   |
| $\begin{array}{c} a = & 0.147430 - 1.094530I & -7.51956 + 4.03416I & 0 \\ b = -1.88535 + 0.79417I & & & \\ \hline u = -1.318780 + 0.470886I & & & \\ a = & 0.389956 - 1.214920I & -7.78759 + 6.42660I & 0 \\ b = -1.162380 + 0.271439I & & & \\ \hline u = -1.318780 - 0.470886I & & & \\ a = & 0.389956 + 1.214920I & -7.78759 - 6.42660I & 0 \\ \end{array}$  | b = -1.88535 - 0.79417I   |                                       |                     |
| $\begin{array}{c ccccccccccccccccccccccccccccccccccc$   | u = 1.304590 - 0.505937I  |                                       |                     |
| $\begin{array}{c} u = -1.318780 + 0.470886I \\ a = 0.389956 - 1.214920I & -7.78759 + 6.42660I & 0 \\ b = -1.162380 + 0.271439I \\ u = -1.318780 - 0.470886I \\ a = 0.389956 + 1.214920I & -7.78759 - 6.42660I & 0 \end{array}$  | a = 0.147430 - 1.094530I  | -7.51956 + 4.03416I                   | 0                   |
| $\begin{array}{cccccccccccccccccccccccccccccccccccc$  | b = -1.88535 + 0.79417I   |                                       |                     |
| $\begin{array}{c ccccccccccccccccccccccccccccccccccc$   | u = -1.318780 + 0.470886I |                                       |                     |
| u = -1.318780 - 0.470886I $a = 0.389956 + 1.214920I -7.78759 - 6.42660I$ 0  | a = 0.389956 - 1.214920I  | -7.78759 + 6.42660I                   | 0                   |
| a = 0.389956 + 1.214920I -7.78759 - 6.42660I  | b = -1.162380 + 0.271439I |                                       |                     |
|   | u = -1.318780 - 0.470886I |                                       |                     |
| b = -1.162380 - 0.271439I   | a = 0.389956 + 1.214920I  | -7.78759 - 6.42660I                   | 0                   |
|   | b = -1.162380 - 0.271439I |                                       |                     |

| Solutions to $I_1^u$      | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape         |
|---------------------------|---------------------------------------|--------------------|
| u = -1.288130 + 0.550367I |                                       |                    |
| a = -0.228557 + 1.218180I | -10.8644 + 9.0813I                    | 0                  |
| b = 2.00350 - 0.82275I    |                                       |                    |
| u = -1.288130 - 0.550367I |                                       |                    |
| a = -0.228557 - 1.218180I | -10.8644 - 9.0813I                    | 0                  |
| b = 2.00350 + 0.82275I    |                                       |                    |
| u = 1.340310 + 0.422305I  |                                       |                    |
| a = -0.370934 - 1.220450I | -11.84160 - 1.40433I                  | 0                  |
| b = 1.180220 + 0.312167I  |                                       |                    |
| u = 1.340310 - 0.422305I  |                                       |                    |
| a = -0.370934 + 1.220450I | -11.84160 + 1.40433I                  | 0                  |
| b = 1.180220 - 0.312167I  |                                       |                    |
| u = -0.222716 + 0.468775I |                                       |                    |
| a = -2.01359 - 1.24143I   | 5.14299 - 3.26209I                    | 6.73158 + 4.68534I |
| b = 0.560309 + 1.188780I  |                                       |                    |
| u = -0.222716 - 0.468775I |                                       |                    |
| a = -2.01359 + 1.24143I   | 5.14299 + 3.26209I                    | 6.73158 - 4.68534I |
| b = 0.560309 - 1.188780I  |                                       |                    |
| u = -0.036037 + 0.440473I |                                       |                    |
| a = 0.933153 - 0.958140I  | 0.077905 + 1.136720I                  | 0.96258 - 6.02333I |
| b = -0.419907 + 0.597866I |                                       |                    |
| u = -0.036037 - 0.440473I |                                       |                    |
| a = 0.933153 + 0.958140I  | 0.077905 - 1.136720I                  | 0.96258 + 6.02333I |
| b = -0.419907 - 0.597866I |                                       |                    |

II. 
$$I_2^u = \langle -u^2a + u^3 + b + a - u, \ a^2u^2 + a^3 + 1, \ u^4 - u^2 + 1 \rangle$$

(i) Arc colorings

$$a_{3} = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_{8} = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{9} = \begin{pmatrix} 1 \\ u^{2} \end{pmatrix}$$

$$a_{4} = \begin{pmatrix} -u \\ -u^{3} + u \end{pmatrix}$$

$$a_{5} = \begin{pmatrix} u^{2}a - u^{3} - a + u \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} -u^{2} + 1 \\ u^{2} \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} -u^{3}a - u^{2} + 1 \\ au \end{pmatrix}$$

$$a_{2} = \begin{pmatrix} -a^{2}u \\ -u^{3}a^{2} + a^{2}u - a + u \end{pmatrix}$$

$$a_{6} = \begin{pmatrix} -a^{2}u^{2} + a^{2} - u^{2} + a \\ a^{2}u^{2} + a^{2}u - u^{3} - a + u + 1 \end{pmatrix}$$

$$a_{1} = \begin{pmatrix} -a^{2}u \\ a^{2}u - a + u \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} u^{3}a^{2} - 2a^{2}u - u^{2}a + u^{3} \\ -u^{3}a^{2} + a^{2}u \end{pmatrix}$$

$$a_{7} = \begin{pmatrix} u^{3}a^{2} - a^{2}u^{2} - u^{2}a + a^{2} - u^{2} + 2a + u \\ a^{2}u^{2} + u^{2}a - a + 1 \end{pmatrix}$$

- (ii) Obstruction class = 1
- (iii) Cusp Shapes =  $4u^2a + 4u^2 4a$

### (iv) u-Polynomials at the component

| Crossings             | u-Polynomials at each crossing        |
|-----------------------|---------------------------------------|
| $c_1$                 | $(u^3 - u^2 + 2u - 1)^4$              |
| $c_{2}, c_{5}$        | $(u^6 + u^4 + 2u^2 + 1)^2$            |
| $c_3, c_8$            | $(u^4 - u^2 + 1)^3$                   |
| $c_4,c_{10}$          | $(u^2+1)^6$                           |
| <i>c</i> <sub>6</sub> | $u^{12} - 8u^{11} + \dots - 40u + 25$ |
| $c_7, c_{11}$         | $(u^6 - 3u^4 + 2u^2 + 1)^2$           |
| $c_9$                 | $(u^2 + u + 1)^6$                     |
| $c_{12}$              | $u^{12} + 4u^{11} + \dots - 90u + 25$ |

### (v) Riley Polynomials at the component

| Crossings             | Riley Polynomials at each crossing        |
|-----------------------|---|
| $c_1$                 | $(y^3 + 3y^2 + 2y - 1)^4$                 |
| $c_2, c_5$            | $(y^3 + y^2 + 2y + 1)^4$                  |
| $c_{3}, c_{8}$        | $(y^2 - y + 1)^6$                         |
| $c_4,c_{10}$          | $(y+1)^{12}$                              |
|                       | $y^{12} + 6y^{11} + \dots + 2100y + 625$  |
| $c_7,c_{11}$          | $(y^3 - 3y^2 + 2y + 1)^4$                 |
| <i>c</i> <sub>9</sub> | $(y^2 + y + 1)^6$                         |
| $c_{12}$              | $y^{12} - 30y^{10} + \dots - 4050y + 625$ |

# (vi) Complex Volumes and Cusp Shapes

| Solutions to $I_2^u$      | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape          |
|---------------------------|---------------------------------------|---------------------|
| u = 0.866025 + 0.500000I  |                                       |                     |
| a = -1.083790 - 0.387453I | 4.66906 + 0.79824I                    | 5.50976 + 0.48465I  |
| b = 1.74346 - 1.24486I    |                                       |                     |
| u = 0.866025 + 0.500000I  |                                       |                     |
| a = 0.206350 - 1.132320I  | 4.66906 - 4.85801I                    | 5.50976 + 6.44355I  |
| b = 1.74346 + 0.24486I    |                                       |                     |
| u = 0.866025 + 0.500000I  |                                       |                     |
| a = 0.377439 + 0.653743I  | 0.53148 - 2.02988I                    | -1.01951 + 3.46410I |
| b = 0.111148 - 0.500000I  |                                       |                     |
| u = 0.866025 - 0.500000I  |                                       |                     |
| a = -1.083790 + 0.387453I | 4.66906 - 0.79824I                    | 5.50976 - 0.48465I  |
| b = 1.74346 + 1.24486I    |                                       |                     |
| u = 0.866025 - 0.500000I  |                                       |                     |
| a = 0.206350 + 1.132320I  | 4.66906 + 4.85801I                    | 5.50976 - 6.44355I  |
| b = 1.74346 - 0.24486I    |                                       |                     |
| u = 0.866025 - 0.500000I  |                                       |                     |
| a = 0.377439 - 0.653743I  | 0.53148 + 2.02988I                    | -1.01951 - 3.46410I |
| b = 0.111148 + 0.500000I  |                                       |                     |
| u = -0.866025 + 0.500000I |                                       |                     |
| a = -1.083790 + 0.387453I | 4.66906 - 0.79824I                    | 5.50976 - 0.48465I  |
| b = 0.011413 + 0.244862I  |                                       |                     |
| u = -0.866025 + 0.500000I |                                       |                     |
| a = 0.206350 + 1.132320I  | 4.66906 + 4.85801I                    | 5.50976 - 6.44355I  |
| b = 0.011413 - 1.244860I  |                                       |                     |
| u = -0.866025 + 0.500000I |                                       |                     |
| a = 0.377439 - 0.653743I  | 0.53148 + 2.02988I                    | -1.01951 - 3.46410I |
| b = -1.62090 - 0.50000I   |                                       |                     |
| u = -0.866025 - 0.500000I |                                       |                     |
| a = -1.083790 - 0.387453I | 4.66906 + 0.79824I                    | 5.50976 + 0.48465I  |
| b = 0.011413 - 0.244862I  |                                       |                     |

| Solutions to $I_2^u$      | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape          |
|---------------------------|---------------------------------------|---------------------|
| u = -0.866025 - 0.500000I |                                       |                     |
| a =  0.206350 - 1.132320I | 4.66906 - 4.85801I                    | 5.50976 + 6.44355I  |
| b = 0.011413 + 1.244860I  |                                       |                     |
| u = -0.866025 - 0.500000I |                                       |                     |
| a = 0.377439 + 0.653743I  | 0.53148 - 2.02988I                    | -1.01951 + 3.46410I |
| b = -1.62090 + 0.50000I   |                                       |                     |

III. u-Polynomials

| Crossings     | u-Polynomials at each crossing  |
|---------------|---|
| $c_1$         | $((u^3 - u^2 + 2u - 1)^4)(u^{48} + 53u^{47} + \dots - 27678u + 289)$                            |
| $c_2, c_5$    | $((u6 + u4 + 2u2 + 1)2)(u48 + 3u47 + \dots - 142u + 17)$  |
| $c_3, c_8$    | $((u^4 - u^2 + 1)^3)(u^{48} - u^{47} + \dots - 2u + 5)$   |
| $c_4, c_{10}$ | $((u^2+1)^6)(u^{48}-u^{47}+\cdots-8u+1)$  |
| $c_6$         | $(u^{12} - 8u^{11} + \dots - 40u + 25)(u^{48} + 5u^{47} + \dots - 7742u + 26561)$               |
| $c_7, c_{11}$ | $((u^6 - 3u^4 + 2u^2 + 1)^2)(u^{48} - u^{47} + \dots - 14u + 1)$                                |
| <i>c</i> 9    | $((u^2 + u + 1)^6)(u^{48} + 29u^{47} + \dots - 36u + 25)$                                       |
| $c_{12}$      | $(u^{12} + 4u^{11} + \dots - 90u + 25)$ $\cdot (u^{48} + 3u^{47} + \dots + 4284478u + 1826857)$ |

### IV. Riley Polynomials

| Crossings             | Riley Polynomials at each crossing  |
|-----------------------|---|
| $c_1$                 | $((y^3 + 3y^2 + 2y - 1)^4)(y^{48} - 111y^{47} + \dots - 2.98879 \times 10^8y + 83521)$                            |
| $c_2, c_5$            | $((y^3 + y^2 + 2y + 1)^4)(y^{48} + 53y^{47} + \dots - 27678y + 289)$  |
| $c_3, c_8$            | $((y^2 - y + 1)^6)(y^{48} - 29y^{47} + \dots + 36y + 25)$   |
| $c_4,c_{10}$          | $((y+1)^{12})(y^{48}+13y^{47}+\cdots+14y+1)$  |
| $c_6$                 | $(y^{12} + 6y^{11} + \dots + 2100y + 625)$ $\cdot (y^{48} + 31y^{47} + \dots + 12208109238y + 705486721)$         |
| $c_7, c_{11}$         | $((y^3 - 3y^2 + 2y + 1)^4)(y^{48} - 39y^{47} + \dots - 86y + 1)$  |
| <i>c</i> <sub>9</sub> | $((y^2 + y + 1)^6)(y^{48} - 13y^{47} + \dots - 28896y + 625)$   |
| $c_{12}$              | $(y^{12} - 30y^{10} + \dots - 4050y + 625)$ $\cdot (y^{48} + 41y^{47} + \dots + 44880385612764y + 3337406498449)$ |