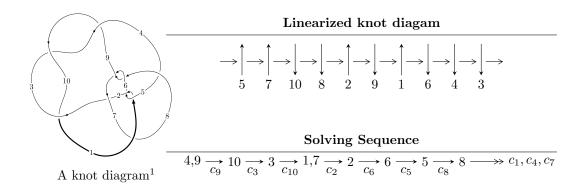
### $10_{90} (K10a_{92})$



#### Ideals for irreducible components<sup>2</sup> of $X_{par}$

$$I_1^u = \langle -3.45798 \times 10^{19} u^{39} - 4.51348 \times 10^{19} u^{38} + \dots + 2.27356 \times 10^{21} b + 2.73076 \times 10^{21}, \\ -7.03658 \times 10^{21} u^{39} + 1.13904 \times 10^{22} u^{38} + \dots + 6.82068 \times 10^{21} a + 1.48581 \times 10^{21}, \ u^{40} - 2u^{39} + \dots - 2u - 10^{21} u^{40} + 10^{21} u^{40} +$$

\* 2 irreducible components of  $\dim_{\mathbb{C}} = 0$ , with total 42 representations.

<sup>&</sup>lt;sup>1</sup>The image of knot diagram is generated by the software "**Draw programme**" developed by Andrew Bartholomew(http://www.layer8.co.uk/maths/draw/index.htm#Running-draw), where we modified some parts for our purpose(https://github.com/CATsTAILs/LinksPainter).

 $<sup>^2</sup>$  All coefficients of polynomials are rational numbers. But the coefficients are sometimes approximated in decimal forms when there is not enough margin.

 $I. \\ I_1^u = \langle -3.46 \times 10^{19} u^{39} - 4.51 \times 10^{19} u^{38} + \dots + 2.27 \times 10^{21} b + 2.73 \times 10^{21}, \ -7.04 \times 10^{21} u^{39} + 1.14 \times 10^{22} u^{38} + \dots + 6.82 \times 10^{21} a + 1.49 \times 10^{21}, \ u^{40} - 2u^{39} + \dots - 2u + 1 \rangle$ 

#### (i) Arc colorings

$$a_{4} = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_{9} = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} 1 \\ u^{2} \end{pmatrix}$$

$$a_{3} = \begin{pmatrix} u^{2} + 1 \\ u^{4} + 2u^{2} \end{pmatrix}$$

$$a_{7} = \begin{pmatrix} 1.03165u^{39} - 1.66999u^{38} + \dots - 9.20228u - 0.217839 \\ 0.0152095u^{39} + 0.0198520u^{38} + \dots + 0.294657u - 1.20110 \end{pmatrix}$$

$$a_{2} = \begin{pmatrix} -1.20596u^{39} + 2.67703u^{38} + \dots + 4.75631u - 2.57467 \\ 0.765706u^{39} - 1.55826u^{38} + \dots + 3.94732u - 1.22640 \end{pmatrix}$$

$$a_{6} = \begin{pmatrix} 1.04686u^{39} - 1.65014u^{38} + \dots - 8.90762u - 1.41894 \\ 0.0152095u^{39} + 0.0198520u^{38} + \dots + 0.294657u - 1.20110 \end{pmatrix}$$

$$a_{5} = \begin{pmatrix} -0.829665u^{39} + 2.71973u^{38} + \dots + 0.294657u - 1.20110 \\ 0.136920u^{39} - 0.520550u^{38} + \dots + 3.27950u - 1.01464 \end{pmatrix}$$

$$a_{8} = \begin{pmatrix} 1.00098u^{39} - 1.67814u^{38} + \dots - 9.29825u - 0.212902 \\ -0.101227u^{39} + 0.144212u^{38} + \dots - 9.00592179u - 1.04475 \end{pmatrix}$$

#### (ii) Obstruction class = -1

$$\begin{array}{l} \textbf{(iii) } \ \mathbf{Cusp \ Shapes} = -\frac{23709189092098357085641}{20462029573507327146753} u^{39} + \frac{5967042122571150693039}{2273558841500814127417} u^{38} + \cdots - \frac{151009571647058399841037}{6820676524502442382251} u + \frac{36425712582025581848210}{20462029573507327146753} \end{array}$$

### (iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
$c_1, c_5$	$u^{40} - 2u^{39} + \dots - 2u + 1$
$c_2$	$3(3u^{40} + 19u^{39} + \dots + 64u + 32)$
$c_3, c_9, c_{10}$	$u^{40} - 2u^{39} + \dots - 2u + 1$
$c_4$	$3(3u^{40} - 10u^{39} + \dots - 192u + 103)$
$c_6, c_8$	$u^{40} - 3u^{39} + \dots - 31u + 9$
C <sub>7</sub>	$u^{40} - 3u^{39} + \dots - 156u + 36$

# (v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
$c_1,c_5$	$y^{40} - 22y^{39} + \dots - 4y + 1$
$c_2$	$9(9y^{40} - 181y^{39} + \dots - 13312y + 1024)$
$c_3, c_9, c_{10}$	$y^{40} + 38y^{39} + \dots - 4y + 1$
C <sub>4</sub>	$9(9y^{40} + 38y^{39} + \dots + 78084y + 10609)$
$c_6, c_8$	$y^{40} - 21y^{39} + \dots + 389y + 81$
c <sub>7</sub>	$y^{40} - 15y^{39} + \dots - 7416y + 1296$

# (vi) Complex Volumes and Cusp Shapes

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
u = 0.718542 + 0.684654I		
a = -0.109960 - 0.256762I	1.29563 + 4.66233I	-0.05723 - 4.37430I
b = 1.052260 - 0.485181I		
u = 0.718542 - 0.684654I		
a = -0.109960 + 0.256762I	1.29563 - 4.66233I	-0.05723 + 4.37430I
b = 1.052260 + 0.485181I		
u = -0.875135 + 0.400189I		
a = 0.674482 + 0.656422I	-2.73210 + 3.80447I	-3.64129 - 6.83498I
b = 1.057710 - 0.370943I		
u = -0.875135 - 0.400189I		
a = 0.674482 - 0.656422I	-2.73210 - 3.80447I	-3.64129 + 6.83498I
b = 1.057710 + 0.370943I		
u = 0.812016 + 0.457171I		
a = 0.695937 - 0.974226I	0.61792 - 9.83239I	-1.42359 + 7.89553I
b = 1.221190 + 0.590650I		
u = 0.812016 - 0.457171I		
a = 0.695937 + 0.974226I	0.61792 + 9.83239I	-1.42359 - 7.89553I
b = 1.221190 - 0.590650I		
u = -0.668019 + 0.947602I		
a = 0.128837 + 0.281540I	-1.20798 + 1.63374I	$\int 5.34484 + 3.65075I$
b = 0.847605 + 0.160546I		
u = -0.668019 - 0.947602I		
a = 0.128837 - 0.281540I	-1.20798 - 1.63374I	5.34484 - 3.65075I
b = 0.847605 - 0.160546I		
u = 0.548023 + 0.473980I		
a = -0.128815 + 0.412875I	3.67375 - 4.20324I	2.19223 + 6.09439I
b = 0.217702 - 0.991146I		
u = 0.548023 - 0.473980I		
a = -0.128815 - 0.412875I	3.67375 + 4.20324I	2.19223 - 6.09439I
b = 0.217702 + 0.991146I		

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
u = 0.042556 + 1.284610I		
a = 0.906133 + 0.658831I	1.29749 - 1.62987I	0. + 3.54187I
b = -1.55343 - 0.24102I		
u = 0.042556 - 1.284610I		
a = 0.906133 - 0.658831I	1.29749 + 1.62987I	0 3.54187I
b = -1.55343 + 0.24102I		
u = 0.635260 + 0.284826I		
a = 1.38094 - 0.39057I	3.12136 + 0.50572I	2.23334 + 2.05026I
b = 0.418271 + 0.528348I		
u = 0.635260 - 0.284826I		
a = 1.38094 + 0.39057I	3.12136 - 0.50572I	2.23334 - 2.05026I
b = 0.418271 - 0.528348I		
u = 0.088735 + 1.341390I		
a = 0.61542 + 1.56781I	1.96980 - 1.69833I	0
b = -1.177540 - 0.538211I		
u = 0.088735 - 1.341390I		
a = 0.61542 - 1.56781I	1.96980 + 1.69833I	0
b = -1.177540 + 0.538211I		
u = -0.145572 + 1.361910I		
a = 0.63895 - 1.93494I	3.71762 + 5.12635I	0
b = -0.97948 + 1.02345I		
u = -0.145572 - 1.361910I		
a = 0.63895 + 1.93494I	3.71762 - 5.12635I	0
b = -0.97948 - 1.02345I		
u = -0.054010 + 1.410140I		
a = 1.50150 - 2.72344I	5.39390 + 0.19809I	0
b = -0.809247 + 0.079779I		
u = -0.054010 - 1.410140I		
a = 1.50150 + 2.72344I	5.39390 - 0.19809I	0
b = -0.809247 - 0.079779I		

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
u = 0.29805 + 1.43344I		
a = 0.374682 - 1.281700I	8.54985 - 3.07602I	0
b = 0.859448 + 0.587652I		
u = 0.29805 - 1.43344I		
a = 0.374682 + 1.281700I	8.54985 + 3.07602I	0
b = 0.859448 - 0.587652I		
u = -0.491071 + 0.191924I		
a = -0.398403 - 1.001630I	-1.16688 + 2.84021I	-5.40123 - 7.45362I
b = -1.093680 + 0.645721I		
u = -0.491071 - 0.191924I		
a = -0.398403 + 1.001630I	-1.16688 - 2.84021I	-5.40123 + 7.45362I
b = -1.093680 - 0.645721I		
u = -0.334189 + 0.406515I		
a = 0.489517 - 0.524451I	-0.073174 + 1.047740I	-1.21383 - 6.28305I
b = -0.086689 + 0.335230I		
u = -0.334189 - 0.406515I		
a = 0.489517 + 0.524451I	-0.073174 - 1.047740I	-1.21383 + 6.28305I
b = -0.086689 - 0.335230I		
u = -0.14754 + 1.48353I		
a = -0.198631 - 1.161320I	6.24860 + 2.92553I	0
b = 0.205553 + 0.846197I		
u = -0.14754 - 1.48353I		
a = -0.198631 + 1.161320I	6.24860 - 2.92553I	0
b = 0.205553 - 0.846197I		
u = 0.19425 + 1.47878I		
a = -0.63962 + 1.50949I	10.00150 - 6.93788I	0
b = 0.365197 - 1.279800I		
u = 0.19425 - 1.47878I		
a = -0.63962 - 1.50949I	10.00150 + 6.93788I	0
b = 0.365197 + 1.279800I		

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
u = -0.31725 + 1.49380I		
a = -0.15513 + 1.42791I	3.39122 + 8.09434I	0
b = 1.180340 - 0.563412I		
u = -0.31725 - 1.49380I		
a = -0.15513 - 1.42791I	3.39122 - 8.09434I	0
b = 1.180340 + 0.563412I		
u = 0.29587 + 1.50669I		
a = -0.25279 - 1.73575I	6.9750 - 13.8661I	0
b = 1.29708 + 0.71454I		
u = 0.29587 - 1.50669I		
a = -0.25279 + 1.73575I	6.9750 + 13.8661I	0
b = 1.29708 - 0.71454I		
u = 0.16112 + 1.56360I		
a = -0.602788 + 0.551528I	8.93627 + 1.59631I	0
b = 0.727804 - 0.598256I		
u = 0.16112 - 1.56360I		
a = -0.602788 - 0.551528I	8.93627 - 1.59631I	0
b = 0.727804 + 0.598256I		
u = 0.424864 + 0.027630I		
a = -1.51964 + 0.31762I	-2.32372 - 0.01230I	-6.85568 - 1.19794I
b = -1.269680 - 0.070813I		
u = 0.424864 - 0.027630I		
a = -1.51964 - 0.31762I	-2.32372 + 0.01230I	-6.85568 + 1.19794I
b = -1.269680 + 0.070813I		
u = -0.186501 + 0.360437I		
a = 3.93271 - 1.95945I	-0.113312 - 0.691322I	2.03417 - 9.81182I
b = -0.980417 - 0.195912I		
u = -0.186501 - 0.360437I		
a = 3.93271 + 1.95945I	-0.113312 + 0.691322I	2.03417 + 9.81182I
b = -0.980417 + 0.195912I		

II. 
$$I_2^u = \langle b+1, \ 3a-2u+1, \ u^2-u+1 \rangle$$

(i) Arc colorings

$$a_{4} = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_{9} = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} 1 \\ u - 1 \end{pmatrix}$$

$$a_{3} = \begin{pmatrix} u \\ u - 1 \end{pmatrix}$$

$$a_{1} = \begin{pmatrix} u \\ u - 2 \end{pmatrix}$$

$$a_{7} = \begin{pmatrix} \frac{2}{3}u - \frac{1}{3} \\ -1 \end{pmatrix}$$

$$a_{2} = \begin{pmatrix} \frac{2}{3}u - \frac{4}{3} \\ \frac{5}{3}u - \frac{4}{3} \end{pmatrix}$$

$$a_{6} = \begin{pmatrix} \frac{1}{3}u \\ \frac{1}{3}u \\ -1 \end{pmatrix}$$

$$a_{5} = \begin{pmatrix} \frac{1}{3}u \\ \frac{1}{3}u \\ \frac{1}{3}u - \frac{1}{3} \\ -1 \end{pmatrix}$$

$$a_{8} = \begin{pmatrix} \frac{2}{3}u - \frac{1}{3} \\ -1 \end{pmatrix}$$

- (ii) Obstruction class = 1
- (iii) Cusp Shapes =  $\frac{20}{3}u 9$

### (iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
$c_1, c_3$	$u^2 + u + 1$
$c_2$	$3(3u^2+1)$
$c_4$	$3(3u^2 - 3u + 1)$
$c_5, c_9, c_{10}$	$u^2 - u + 1$
	$(u-1)^2$
C <sub>7</sub>	$u^2$
c <sub>8</sub>	$(u+1)^2$

### (v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
$c_1, c_3, c_5$ $c_9, c_{10}$	$y^2 + y + 1$
$c_2$	$9(3y+1)^2$
$C_4$	$9(9y^2 - 3y + 1)$
$c_{6}, c_{8}$	$(y-1)^2$
c <sub>7</sub>	$y^2$

# (vi) Complex Volumes and Cusp Shapes

Solutions to $I_2^u$	$\int \sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
u = 0.500000 + 0.866025I		
a = 0.577350I	-1.64493 - 2.02988I	-5.66667 + 5.77350I
b = -1.00000		
u = 0.500000 - 0.866025I		
a = -0.577350I	-1.64493 + 2.02988I	-5.66667 - 5.77350I
b = -1.00000		

III. u-Polynomials

Crossings	u-Polynomials at each crossing
$c_1$	$ (u^2 + u + 1)(u^{40} - 2u^{39} + \dots - 2u + 1) $
$c_2$	$9(3u^2+1)(3u^{40}+19u^{39}+\cdots+64u+32)$
<i>c</i> 3	$(u^2 + u + 1)(u^{40} - 2u^{39} + \dots - 2u + 1)$
<i>C</i> <sub>4</sub>	$9(3u^2 - 3u + 1)(3u^{40} - 10u^{39} + \dots - 192u + 103)$
<i>C</i> <sub>5</sub>	$(u^2 - u + 1)(u^{40} - 2u^{39} + \dots - 2u + 1)$
<i>c</i> <sub>6</sub>	$((u-1)^2)(u^{40} - 3u^{39} + \dots - 31u + 9)$
C <sub>7</sub>	$u^2(u^{40} - 3u^{39} + \dots - 156u + 36)$
c <sub>8</sub>	$((u+1)^2)(u^{40} - 3u^{39} + \dots - 31u + 9)$
$c_9, c_{10}$	$(u^2 - u + 1)(u^{40} - 2u^{39} + \dots - 2u + 1)$

IV. Riley Polynomials

Crossings	Riley Polynomials at each crossing
$c_1, c_5$	$(y^2 + y + 1)(y^{40} - 22y^{39} + \dots - 4y + 1)$
$c_2$	$81(3y+1)^2(9y^{40}-181y^{39}+\cdots-13312y+1024)$
$c_3, c_9, c_{10}$	$(y^2 + y + 1)(y^{40} + 38y^{39} + \dots - 4y + 1)$
$c_4$	$81(9y^2 - 3y + 1)(9y^{40} + 38y^{39} + \dots + 78084y + 10609)$
$c_{6}, c_{8}$	$((y-1)^2)(y^{40}-21y^{39}+\cdots+389y+81)$
	$y^2(y^{40} - 15y^{39} + \dots - 7416y + 1296)$