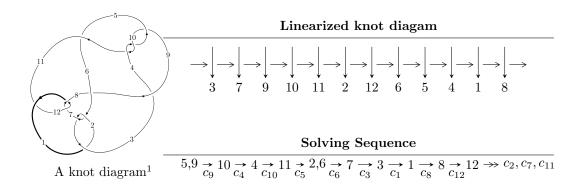
### $12a_{0575} (K12a_{0575})$



#### Ideals for irreducible components<sup>2</sup> of $X_{par}$

$$\begin{split} I_1^u &= \langle -2u^{37} + 3u^{36} + \dots + b - 3, \ -3u^{39} + 9u^{38} + \dots + 2a - 10, \ u^{40} - 3u^{39} + \dots + 6u - 2 \rangle \\ I_2^u &= \langle 5150u^{29}a - 9644u^{29} + \dots - 4195a - 8440, \ 2u^{29}a + u^{28} + \dots + a + 2, \ u^{30} + u^{29} + \dots + u + 1 \rangle \\ I_3^u &= \langle b - 1, \ -2u^3 + 3u^2 + 3a - 3u + 3, \ u^4 + 3u^2 + 3 \rangle \\ I_4^u &= \langle b + 1, \ u^2 + a - u + 1, \ u^4 + u^2 - 1 \rangle \end{split}$$

$$I_1^v = \langle a, \ b-1, \ v+1 \rangle$$

\* 5 irreducible components of  $\dim_{\mathbb{C}} = 0$ , with total 109 representations.

<sup>&</sup>lt;sup>1</sup>The image of knot diagram is generated by the software "**Draw programme**" developed by Andrew Bartholomew(http://www.layer8.co.uk/maths/draw/index.htm#Running-draw), where we modified some parts for our purpose(https://github.com/CATsTAILs/LinksPainter).

 $<sup>^2</sup>$  All coefficients of polynomials are rational numbers. But the coefficients are sometimes approximated in decimal forms when there is not enough margin.

I. 
$$I_1^u = \langle -2u^{37} + 3u^{36} + \dots + b - 3, -3u^{39} + 9u^{38} + \dots + 2a - 10, u^{40} - 3u^{39} + \dots + 6u - 2 \rangle$$

$$a_{5} = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_{9} = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} 1 \\ u^{2} \end{pmatrix}$$

$$a_{4} = \begin{pmatrix} u^{2} + 1 \\ u^{4} + 2u^{2} \end{pmatrix}$$

$$a_{2} = \begin{pmatrix} \frac{3}{2}u^{39} - \frac{9}{2}u^{38} + \dots - \frac{17}{2}u + 5 \\ 2u^{37} - 3u^{36} + \dots - 3u + 3 \end{pmatrix}$$

$$a_{6} = \begin{pmatrix} -u^{5} - 2u^{3} - u \\ -u^{7} - 3u^{5} - 2u^{3} + u \end{pmatrix}$$

$$a_{7} = \begin{pmatrix} -\frac{3}{2}u^{39} + \frac{5}{2}u^{38} + \dots + \frac{5}{2}u - 2 \\ -u^{39} + 2u^{38} + \dots + 3u - 1 \end{pmatrix}$$

$$a_{3} = \begin{pmatrix} u^{3} + 2u \\ u^{3} + u \end{pmatrix}$$

$$a_{1} = \begin{pmatrix} \frac{5}{2}u^{39} - \frac{15}{2}u^{38} + \dots - \frac{33}{2}u + 9 \\ 3u^{37} - 5u^{36} + \dots - 6u + 5 \end{pmatrix}$$

$$a_{8} = \begin{pmatrix} -u^{12} - 5u^{10} - 9u^{8} - 6u^{6} + u^{2} + 1 \\ -u^{14} - 6u^{12} - 13u^{10} - 10u^{8} + 2u^{6} + 4u^{4} - u^{2} \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} -\frac{3}{2}u^{39} + \frac{9}{2}u^{38} + \dots + \frac{21}{2}u - 4 \\ -2u^{37} + 3u^{36} + \dots + 4u - 3 \end{pmatrix}$$

- (ii) Obstruction class = -1
- (iii) Cusp Shapes =  $8u^{39} 14u^{38} + \cdots 20u 8$

| Crossings                | u-Polynomials at each crossing            |
|--------------------------|---|
| $c_1,c_{11}$             | $u^{40} + 17u^{39} + \dots + 19u + 1$     |
| $c_2, c_6, c_7$ $c_{12}$ | $u^{40} - u^{39} + \dots - u - 1$         |
| $c_3, c_5$               | $u^{40} - 3u^{39} + \dots + 10u - 2$      |
| $c_4, c_9, c_{10}$       | $u^{40} + 3u^{39} + \dots - 6u - 2$       |
| $c_8$                    | $u^{40} - 21u^{39} + \dots - 6214u + 562$ |

| Crossings                | Riley Polynomials at each crossing             |
|--------------------------|--|
| $c_1,c_{11}$             | $y^{40} + 23y^{39} + \dots - 67y + 1$          |
| $c_2, c_6, c_7$ $c_{12}$ | $y^{40} - 17y^{39} + \dots - 19y + 1$          |
| $c_3, c_5$               | $y^{40} - 27y^{39} + \dots + 64y + 4$          |
| $c_4, c_9, c_{10}$       | $y^{40} + 33y^{39} + \dots - 32y + 4$          |
| <i>c</i> <sub>8</sub>    | $y^{40} - 3y^{39} + \dots - 5405216y + 315844$ |

| Solutions to $I_1^u$      | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape          |
|---------------------------|---------------------------------------|---------------------|
| u = 0.033946 + 1.113580I  |                                       |                     |
| a = -0.443213 + 0.659546I | 2.62973 - 1.45530I                    | -8.41133 + 4.63856I |
| b = -0.529000 - 0.069966I |                                       |                     |
| u = 0.033946 - 1.113580I  |                                       |                     |
| a = -0.443213 - 0.659546I | 2.62973 + 1.45530I                    | -8.41133 - 4.63856I |
| b = -0.529000 + 0.069966I |                                       |                     |
| u = 0.833882 + 0.049861I  |                                       |                     |
| a = 0.866824 + 0.530873I  | -7.70738 + 2.92668I                   | -18.8392 - 4.9556I  |
| b = 0.179877 + 0.772910I  |                                       |                     |
| u = 0.833882 - 0.049861I  |                                       |                     |
| a = 0.866824 - 0.530873I  | -7.70738 - 2.92668I                   | -18.8392 + 4.9556I  |
| b = 0.179877 - 0.772910I  |                                       |                     |
| u = 0.366756 + 1.108260I  |                                       |                     |
| a = 1.59722 + 0.00494I    | -1.99390 + 8.37642I                   | -14.1780 - 5.1626I  |
| b = 1.77944 + 1.15129I    |                                       |                     |
| u = 0.366756 - 1.108260I  |                                       |                     |
| a = 1.59722 - 0.00494I    | -1.99390 - 8.37642I                   | -14.1780 + 5.1626I  |
| b = 1.77944 - 1.15129I    |                                       |                     |
| u = 0.817179 + 0.133455I  |                                       |                     |
| a = -2.11445 + 2.81732I   | -4.96679 - 12.67870I                  | -17.0433 + 8.8234I  |
| b = -2.01736 + 1.18808I   |                                       |                     |
| u = 0.817179 - 0.133455I  |                                       |                     |
| a = -2.11445 - 2.81732I   | -4.96679 + 12.67870I                  | -17.0433 - 8.8234I  |
| b = -2.01736 - 1.18808I   |                                       |                     |
| u = 0.218298 + 1.152810I  |                                       |                     |
| a = -0.690017 + 0.431742I | 2.56813 - 1.57777I                    | -7.38729 + 3.27205I |
| b = -0.822252 - 0.487537I |                                       |                     |
| u = 0.218298 - 1.152810I  |                                       |                     |
| a = -0.690017 - 0.431742I | 2.56813 + 1.57777I                    | -7.38729 - 3.27205I |
| b = -0.822252 + 0.487537I |                                       |                     |
|                           |                                       |                     |

| Solutions to $I_1^u$      | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape           |
|---------------------------|---------------------------------------|----------------------|
| u = -0.813800             |                                       |                      |
| a = -1.17657              | -5.88324                              | -14.0450             |
| b = -0.516311             |                                       |                      |
| u = 0.753305 + 0.134603I  |                                       |                      |
| a = 1.75806 - 1.14597I    | -0.35694 - 2.08784I                   | -11.36506 + 1.10964I |
| b = 1.39356 - 0.37494I    |                                       |                      |
| u = 0.753305 - 0.134603I  |                                       |                      |
| a = 1.75806 + 1.14597I    | -0.35694 + 2.08784I                   | -11.36506 - 1.10964I |
| b = 1.39356 + 0.37494I    |                                       |                      |
| u = 0.381450 + 1.215900I  |                                       |                      |
| a = -0.154097 + 0.151781I | -4.11653 - 7.29632I                   | -12.0000 + 8.2173I   |
| b = -0.323421 + 0.861671I |                                       |                      |
| u = 0.381450 - 1.215900I  |                                       |                      |
| a = -0.154097 - 0.151781I | -4.11653 + 7.29632I                   | -12.0000 - 8.2173I   |
| b = -0.323421 - 0.861671I |                                       |                      |
| u = -0.686189 + 0.170880I |                                       |                      |
| a = 0.15715 + 2.12370I    | 0.50362 + 4.50911I                    | -12.14030 - 7.25109I |
| b = 0.432447 + 0.716843I  |                                       |                      |
| u = -0.686189 - 0.170880I |                                       |                      |
| a = 0.15715 - 2.12370I    | 0.50362 - 4.50911I                    | -12.14030 + 7.25109I |
| b = 0.432447 - 0.716843I  |                                       |                      |
| u = -0.129451 + 0.688064I |                                       |                      |
| a = -0.409921 + 0.548317I | 2.57797 - 1.26521I                    | -7.12510 + 2.47533I  |
| b = -0.825583 + 0.231072I |                                       |                      |
| u = -0.129451 - 0.688064I |                                       |                      |
| a = -0.409921 - 0.548317I | 2.57797 + 1.26521I                    | -7.12510 - 2.47533I  |
| b = -0.825583 - 0.231072I |                                       |                      |
| u = -0.361326 + 1.266880I |                                       |                      |
| a = 0.659360 + 0.462083I  | -1.95240 + 4.22783I                   | -12.00000 + 0.I      |
| b = 0.516491 - 0.026454I  |                                       |                      |

| Solutions to $I_1^u$      | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape         |
|---------------------------|---------------------------------------|--------------------|
| u = -0.361326 - 1.266880I |                                       |                    |
| a = 0.659360 - 0.462083I  | -1.95240 - 4.22783I                   | -12.00000 + 0.I    |
| b = 0.516491 + 0.026454I  |                                       |                    |
| u = -0.391716 + 0.557095I |                                       |                    |
| a = 0.438882 + 0.839532I  | -0.63986 + 8.65751I                   | -12.8507 - 9.2010I |
| b = 1.51444 + 0.60899I    |                                       |                    |
| u = -0.391716 - 0.557095I |                                       |                    |
| a = 0.438882 - 0.839532I  | -0.63986 - 8.65751I                   | -12.8507 + 9.2010I |
| b = 1.51444 - 0.60899I    |                                       |                    |
| u = 0.373696 + 1.301330I  |                                       |                    |
| a = -0.998383 + 0.344441I | -3.49133 - 1.41285I                   | 0                  |
| b = -0.072953 - 0.689963I |                                       |                    |
| u = 0.373696 - 1.301330I  |                                       |                    |
| a = -0.998383 - 0.344441I | -3.49133 + 1.41285I                   | 0                  |
| b = -0.072953 + 0.689963I |                                       |                    |
| u = -0.212237 + 1.347650I |                                       |                    |
| a = -0.30613 + 1.72945I   | 3.73398 - 2.59581I                    | 0                  |
| b = 1.070540 + 0.223660I  |                                       |                    |
| u = -0.212237 - 1.347650I |                                       |                    |
| a = -0.30613 - 1.72945I   | 3.73398 + 2.59581I                    | 0                  |
| b = 1.070540 - 0.223660I  |                                       |                    |
| u = -0.542858 + 0.319373I |                                       |                    |
| a = -1.52946 - 1.40938I   | -1.40399 - 5.26208I                   | -14.5220 + 2.7158I |
| b = -1.067890 + 0.349863I |                                       |                    |
| u = -0.542858 - 0.319373I |                                       |                    |
| a = -1.52946 + 1.40938I   | -1.40399 + 5.26208I                   | -14.5220 - 2.7158I |
| b = -1.067890 - 0.349863I |                                       |                    |
| u = -0.289068 + 1.350620I |                                       |                    |
| a = 0.94267 - 1.37582I    | 5.28661 + 8.06862I                    | 0                  |
| b = -0.525974 - 1.055320I |                                       |                    |

|                | Solutions to $I_1^u$         | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape |
|----------------|------------------------------|---------------------------------------|------------|
| $\overline{u}$ | u = -0.289068 - 1.350620I    |                                       |            |
| а              | a = 0.94267 + 1.37582I       | 5.28661 - 8.06862I                    | 0          |
| t              | 0 = -0.525974 + 1.055320I    |                                       |            |
| $\overline{u}$ | u = 0.322258 + 1.346450I     |                                       |            |
| а              | a = -0.02734 + 1.57117I      | 4.30721 - 5.98911I                    | 0          |
| t              | 0 = -1.65332 + 0.31762I      |                                       |            |
| $\overline{u}$ | u = 0.322258 - 1.346450I     |                                       |            |
| а              | a = -0.02734 - 1.57117I      | 4.30721 + 5.98911I                    | 0          |
|                | 0 = -1.65332 - 0.31762I      |                                       |            |
| $\overline{u}$ | u = -0.018698 + 1.394080I    |                                       |            |
| а              | a = -0.777700 - 0.023034I    | 8.78475 - 0.92619I                    | 0          |
|                | 0 = 1.34120 - 0.55017I       |                                       |            |
| $\overline{u}$ | u = -0.018698 - 1.394080I    |                                       |            |
| а              | a = -0.777700 + 0.023034I    | 8.78475 + 0.92619I                    | 0          |
|                | o = 1.34120 + 0.55017I       |                                       |            |
| $\overline{u}$ | u = 0.353485 + 1.352330I     |                                       |            |
| а              | a = -0.60310 - 2.64696I      | -0.2892 - 16.8986I                    | 0          |
| _ <i>t</i>     | 0 = 2.18251 - 1.17429I       |                                       |            |
| u              | u = 0.353485 - 1.352330I     |                                       |            |
| а              | a = -0.60310 + 2.64696I      | -0.2892 + 16.8986I                    | 0          |
|                | 0 = 2.18251 + 1.17429I       |                                       |            |
|                | u = -0.075124 + 1.399150I    |                                       |            |
| а              | u = 1.270610 - 0.109417I     | 5.50017 + 10.01410I                   | 0          |
|                | 0 = -1.96624 - 0.40727I      |                                       |            |
| u              | a = -0.075124 - 1.399150I    |                                       |            |
| а              | u = 1.270610 + 0.109417I     | 5.50017 - 10.01410I                   | 0          |
| <i>t</i>       | $\rho = -1.96624 + 0.40727I$ |                                       |            |
| - 1            | u = 0.318625                 |                                       |            |
| (              | a = 0.902652                 | -0.549970                             | -17.8990   |
|                | b = 0.303261                 |                                       |            |

II. 
$$I_2^u = \langle 5150u^{29}a - 9644u^{29} + \dots - 4195a - 8440, \ 2u^{29}a + u^{28} + \dots + a + 2, \ u^{30} + u^{29} + \dots + u + 1 \rangle$$

$$a_{5} = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_{9} = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} 1 \\ u^{2} \end{pmatrix}$$

$$a_{4} = \begin{pmatrix} u^{2} + 1 \\ u^{4} + 2u^{2} \end{pmatrix}$$

$$a_{2} = \begin{pmatrix} -0.524066au^{29} + 0.981378u^{29} + \dots + 0.426885a + 0.858858 \end{pmatrix}$$

$$a_{6} = \begin{pmatrix} -u^{5} - 2u^{3} - u \\ -u^{7} - 3u^{5} - 2u^{3} + u \end{pmatrix}$$

$$a_{7} = \begin{pmatrix} -0.524066au^{29} + 0.981378u^{29} + \dots + 0.573115a + 0.858858 \\ -0.153658au^{29} + 0.981378u^{29} + \dots + 0.387300a + 0.950850 \end{pmatrix}$$

$$a_{8} = \begin{pmatrix} u^{3} + 2u \\ u^{3} + u \end{pmatrix}$$

$$a_{1} = \begin{pmatrix} 0.223873au^{29} + 0.289508u^{29} + \dots + 0.866185a + 0.429226 \\ -0.701537au^{29} + 1.67915u^{29} + \dots + 0.223873a + 1.28951 \end{pmatrix}$$

$$a_{8} = \begin{pmatrix} -u^{12} - 5u^{10} - 9u^{8} - 6u^{6} + u^{2} + 1 \\ -u^{14} - 6u^{12} - 13u^{10} - 10u^{8} + 2u^{6} + 4u^{4} - u^{2} \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} -0.00142465au^{29} + 0.311794u^{29} + \dots + 0.896306a + 1.12272 \\ -0.0934161au^{29} + 1.30192u^{29} + \dots - 0.0850717a + 1.18999 \end{pmatrix}$$

#### (ii) Obstruction class = -1

(iii) Cusp Shapes

$$= -4u^{29} - 4u^{28} - 48u^{27} - 44u^{26} - 248u^{25} - 208u^{24} - 700u^{23} - 536u^{22} - 1096u^{21} - 768u^{20} - 712u^{19} - 480u^{18} + 464u^{17} + 180u^{16} + 1092u^{15} + 464u^{14} + 380u^{13} + 196u^{12} - 444u^{11} - 40u^{10} - 308u^9 - 48u^8 + 80u^7 - 44u^6 + 76u^5 - 20u^4 - 8u^3 + 12u^2 - 8u - 14u^4 - 40u^{10} - 308u^9 - 48u^8 + 80u^7 - 44u^6 + 76u^5 - 20u^4 - 8u^3 + 12u^2 - 8u - 14u^4 - 40u^{10} - 308u^9 - 48u^8 - 48u^$$

| Crossings                | u-Polynomials at each crossing           |
|--------------------------|--|
| $c_1,c_{11}$             | $u^{60} + 33u^{59} + \dots + 4u + 1$     |
| $c_2, c_6, c_7$ $c_{12}$ | $u^{60} - u^{59} + \dots - 2u^2 + 1$     |
| $c_3, c_5$               | $(u^{30} + u^{29} + \dots + 5u + 5)^2$   |
| $c_4, c_9, c_{10}$       | $(u^{30} - u^{29} + \dots - u + 1)^2$    |
| c <sub>8</sub>           | $(u^{30} + 7u^{29} + \dots + 39u + 7)^2$ |

| Crossings                | Riley Polynomials at each crossing          |
|--------------------------|---|
| $c_1,c_{11}$             | $y^{60} - 13y^{59} + \dots + 28y + 1$       |
| $c_2, c_6, c_7$ $c_{12}$ | $y^{60} - 33y^{59} + \dots - 4y + 1$        |
| $c_3, c_5$               | $(y^{30} - 19y^{29} + \dots + 115y + 25)^2$ |
| $c_4, c_9, c_{10}$       | $(y^{30} + 25y^{29} + \dots + 3y + 1)^2$    |
| c <sub>8</sub>           | $(y^{30} + 5y^{29} + \dots + 383y + 49)^2$  |

| Solutions to $I_2^u$      | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape           |
|---------------------------|---------------------------------------|----------------------|
| u = -0.325991 + 1.102660I |                                       |                      |
| a = 0.808944 + 0.617632I  | 0.60611 - 3.12979I                    | -11.08128 + 1.86186I |
| b = 1.110360 - 0.539869I  |                                       |                      |
| u = -0.325991 + 1.102660I |                                       |                      |
| a = -1.50190 + 0.34099I   | 0.60611 - 3.12979I                    | -11.08128 + 1.86186I |
| b = -1.38771 + 1.17054I   |                                       |                      |
| u = -0.325991 - 1.102660I |                                       |                      |
| a = 0.808944 - 0.617632I  | 0.60611 + 3.12979I                    | -11.08128 - 1.86186I |
| b = 1.110360 + 0.539869I  |                                       |                      |
| u = -0.325991 - 1.102660I |                                       |                      |
| a = -1.50190 - 0.34099I   | 0.60611 + 3.12979I                    | -11.08128 - 1.86186I |
| b = -1.38771 - 1.17054I   |                                       |                      |
| u = -0.795029 + 0.135105I |                                       |                      |
| a = -1.69100 - 1.06948I   | -2.32727 + 7.24749I                   | -14.0714 - 5.6345I   |
| b = -1.45876 - 0.45086I   |                                       |                      |
| u = -0.795029 + 0.135105I |                                       |                      |
| a = 1.66235 + 2.98194I    | -2.32727 + 7.24749I                   | -14.0714 - 5.6345I   |
| b = 1.66006 + 1.29480I    |                                       |                      |
| u = -0.795029 - 0.135105I |                                       |                      |
| a = -1.69100 + 1.06948I   | -2.32727 - 7.24749I                   | -14.0714 + 5.6345I   |
| b = -1.45876 + 0.45086I   |                                       |                      |
| u = -0.795029 - 0.135105I |                                       |                      |
| a = 1.66235 - 2.98194I    | -2.32727 - 7.24749I                   | -14.0714 + 5.6345I   |
| b = 1.66006 - 1.29480I    |                                       |                      |
| u = 0.783573 + 0.097897I  |                                       |                      |
| a = 0.529648 + 0.504852I  | -7.47443 - 3.64220I                   | -19.1043 + 4.7217I   |
| b = -0.375462 + 0.767460I |                                       |                      |
| u = 0.783573 + 0.097897I  |                                       |                      |
| a = -1.52847 + 4.09603I   | -7.47443 - 3.64220I                   | -19.1043 + 4.7217I   |
| b = -1.54437 + 2.11232I   |                                       |                      |

| Solutions to $I_2^u$      | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape         |
|---------------------------|---------------------------------------|--------------------|
| u = 0.783573 - 0.097897I  |                                       |                    |
| a = 0.529648 - 0.504852I  | -7.47443 + 3.64220I                   | -19.1043 - 4.7217I |
| b = -0.375462 - 0.767460I |                                       |                    |
| u = 0.783573 - 0.097897I  |                                       |                    |
| a = -1.52847 - 4.09603I   | -7.47443 + 3.64220I                   | -19.1043 - 4.7217I |
| b = -1.54437 - 2.11232I   |                                       |                    |
| u = 0.319385 + 1.167960I  |                                       |                    |
| a = -0.260474 - 0.287792I | -4.22892 - 0.37332I                   | -16.2067 - 0.5347I |
| b = 0.228296 + 1.005900I  |                                       |                    |
| u = 0.319385 + 1.167960I  |                                       |                    |
| a = 2.13507 + 0.77166I    | -4.22892 - 0.37332I                   | -16.2067 - 0.5347I |
| b = 1.19273 + 2.00676I    |                                       |                    |
| u = 0.319385 - 1.167960I  |                                       |                    |
| a = -0.260474 + 0.287792I | -4.22892 + 0.37332I                   | -16.2067 + 0.5347I |
| b = 0.228296 - 1.005900I  |                                       |                    |
| u = 0.319385 - 1.167960I  |                                       |                    |
| a = 2.13507 - 0.77166I    | -4.22892 + 0.37332I                   | -16.2067 + 0.5347I |
| b = 1.19273 - 2.00676I    |                                       |                    |
| u = -0.754564 + 0.022245I |                                       |                    |
| a = -0.565229 + 0.120861I | -5.49797 + 0.02948I                   | -16.3720 + 0.4707I |
| b = 0.319648 + 0.177361I  |                                       |                    |
| u = -0.754564 + 0.022245I |                                       |                    |
| a = -2.54490 - 0.69654I   | -5.49797 + 0.02948I                   | -16.3720 + 0.4707I |
| b = -1.53986 - 0.33820I   |                                       |                    |
| u = -0.754564 - 0.022245I |                                       |                    |
| a = -0.565229 - 0.120861I | -5.49797 - 0.02948I                   | -16.3720 - 0.4707I |
| b = 0.319648 - 0.177361I  |                                       |                    |
| u = -0.754564 - 0.022245I |                                       |                    |
| a = -2.54490 + 0.69654I   | -5.49797 - 0.02948I                   | -16.3720 - 0.4707I |
| b = -1.53986 + 0.33820I   |                                       |                    |

| Solutions to $I_2^u$      | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape           |
|---------------------------|---------------------------------------|----------------------|
| u = -0.327133 + 1.241840I |                                       |                      |
| a = 1.081960 + 0.620280I  | -1.72825 + 3.89629I                   | -12.45772 - 4.15365I |
| b = 1.075050 - 0.682255I  |                                       |                      |
| u = -0.327133 + 1.241840I |                                       |                      |
| a = 0.564290 + 0.021783I  | -1.72825 + 3.89629I                   | -12.45772 - 4.15365I |
| b = -0.121679 + 0.416377I |                                       |                      |
| u = -0.327133 - 1.241840I |                                       |                      |
| a = 1.081960 - 0.620280I  | -1.72825 - 3.89629I                   | -12.45772 + 4.15365I |
| b = 1.075050 + 0.682255I  |                                       |                      |
| u = -0.327133 - 1.241840I |                                       |                      |
| a = 0.564290 - 0.021783I  | -1.72825 - 3.89629I                   | -12.45772 + 4.15365I |
| b = -0.121679 - 0.416377I |                                       |                      |
| u = -0.311870 + 1.296280I |                                       |                      |
| a = 0.908117 + 0.037740I  | -1.37739 + 3.85600I                   | -11.22500 - 2.05029I |
| b = -0.472487 - 0.133427I |                                       |                      |
| u = -0.311870 + 1.296280I |                                       |                      |
| a = 0.61787 + 2.03259I    | -1.37739 + 3.85600I                   | -11.22500 - 2.05029I |
| b = 2.01782 + 0.26010I    |                                       |                      |
| u = -0.311870 - 1.296280I |                                       |                      |
| a = 0.908117 - 0.037740I  | -1.37739 - 3.85600I                   | -11.22500 + 2.05029I |
| b = -0.472487 + 0.133427I |                                       |                      |
| u = -0.311870 - 1.296280I |                                       |                      |
| a = 0.61787 - 2.03259I    | -1.37739 - 3.85600I                   | -11.22500 + 2.05029I |
| b = 2.01782 - 0.26010I    |                                       |                      |
| u = 0.303367 + 0.581370I  |                                       |                      |
| a = -0.455082 + 0.808828I | 1.48330 - 3.51597I                    | -9.20488 + 5.12276I  |
| b = -1.36467 + 0.55806I   |                                       |                      |
| u = 0.303367 + 0.581370I  |                                       |                      |
| a = 0.244487 + 0.473840I  | 1.48330 - 3.51597I                    | -9.20488 + 5.12276I  |
| b = 0.651369 + 0.018555I  |                                       |                      |

| Solutions to $I_2^u$      | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape          |
|---------------------------|---------------------------------------|---------------------|
| u = 0.303367 - 0.581370I  |                                       |                     |
| a = -0.455082 - 0.808828I | 1.48330 + 3.51597I                    | -9.20488 - 5.12276I |
| b = -1.36467 - 0.55806I   |                                       |                     |
| u = 0.303367 - 0.581370I  |                                       |                     |
| a = 0.244487 - 0.473840I  | 1.48330 + 3.51597I                    | -9.20488 - 5.12276I |
| b = 0.651369 - 0.018555I  |                                       |                     |
| u = -0.035215 + 1.346940I |                                       |                     |
| a = 1.331800 + 0.361268I  | 1.86136 + 1.73295I                    | -8.68819 - 4.09879I |
| b = -2.13172 - 1.05581I   |                                       |                     |
| u = -0.035215 + 1.346940I |                                       |                     |
| a = -0.08388 + 1.50364I   | 1.86136 + 1.73295I                    | -8.68819 - 4.09879I |
| b = 0.147617 - 0.212500I  |                                       |                     |
| u = -0.035215 - 1.346940I |                                       |                     |
| a = 1.331800 - 0.361268I  | 1.86136 - 1.73295I                    | -8.68819 + 4.09879I |
| b = -2.13172 + 1.05581I   |                                       |                     |
| u = -0.035215 - 1.346940I |                                       |                     |
| a = -0.08388 - 1.50364I   | 1.86136 - 1.73295I                    | -8.68819 + 4.09879I |
| b = 0.147617 + 0.212500I  |                                       |                     |
| u = 0.255107 + 1.342090I  |                                       |                     |
| a = -0.772435 - 0.887903I | 5.03529 - 2.69486I                    | -6.58656 + 2.42783I |
| b = 0.045216 - 0.822216I  |                                       |                     |
| u = 0.255107 + 1.342090I  |                                       |                     |
| a = 0.21904 + 1.80021I    | 5.03529 - 2.69486I                    | -6.58656 + 2.42783I |
| b = -1.358140 + 0.357342I |                                       |                     |
| u = 0.255107 - 1.342090I  |                                       |                     |
| a = -0.772435 + 0.887903I | 5.03529 + 2.69486I                    | -6.58656 - 2.42783I |
| b = 0.045216 + 0.822216I  |                                       |                     |
| u = 0.255107 - 1.342090I  |                                       |                     |
| a = 0.21904 - 1.80021I    | 5.03529 + 2.69486I                    | -6.58656 - 2.42783I |
| b = -1.358140 - 0.357342I |                                       |                     |

| Solutions to $I_2^u$      | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape           |
|---------------------------|---------------------------------------|----------------------|
| u = 0.337934 + 1.329700I  |                                       |                      |
| a = -1.059820 + 0.153001I | -2.99171 - 7.69168I                   | -14.0304 + 6.9029I   |
| b = 0.458705 - 0.598884I  |                                       |                      |
| u = 0.337934 + 1.329700I  |                                       |                      |
| a = -1.48086 - 2.73805I   | -2.99171 - 7.69168I                   | -14.0304 + 6.9029I   |
| b = 1.79750 - 2.17416I    |                                       |                      |
| u = 0.337934 - 1.329700I  |                                       |                      |
| a = -1.059820 - 0.153001I | -2.99171 + 7.69168I                   | -14.0304 - 6.9029I   |
| b = 0.458705 + 0.598884I  |                                       |                      |
| u = 0.337934 - 1.329700I  |                                       |                      |
| a = -1.48086 + 2.73805I   | -2.99171 + 7.69168I                   | -14.0304 - 6.9029I   |
| b = 1.79750 + 2.17416I    |                                       |                      |
| u = 0.575326 + 0.209070I  |                                       |                      |
| a = 0.214276 + 1.370120I  | 0.241291 + 0.398317I                  | -12.06522 + 1.62643I |
| b = -0.024140 + 0.286200I |                                       |                      |
| u = 0.575326 + 0.209070I  |                                       |                      |
| a = 1.63714 - 1.36894I    | 0.241291 + 0.398317I                  | -12.06522 + 1.62643I |
| b = 1.045760 + 0.036819I  |                                       |                      |
| u = 0.575326 - 0.209070I  |                                       |                      |
| a = 0.214276 - 1.370120I  | 0.241291 - 0.398317I                  | -12.06522 - 1.62643I |
| b = -0.024140 - 0.286200I |                                       |                      |
| u = 0.575326 - 0.209070I  |                                       |                      |
| a = 1.63714 + 1.36894I    | 0.241291 - 0.398317I                  | -12.06522 - 1.62643I |
| b = 1.045760 - 0.036819I  |                                       |                      |
| u = -0.341616 + 1.350480I |                                       |                      |
| a = 0.00663 + 1.44057I    | 2.35082 + 11.35200I                   | -9.44655 - 7.31316I  |
| b = 1.66219 + 0.34651I    |                                       |                      |
| u = -0.341616 + 1.350480I |                                       |                      |
| a = 0.83289 - 2.47231I    | 2.35082 + 11.35200I                   | -9.44655 - 7.31316I  |
| b = -1.84709 - 1.33663I   |                                       |                      |

| Solutions to $I_2^u$      | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape          |
|---------------------------|---------------------------------------|---------------------|
| u = -0.341616 - 1.350480I |                                       |                     |
| a = 0.00663 - 1.44057I    | 2.35082 - 11.35200I                   | -9.44655 + 7.31316I |
| b = 1.66219 - 0.34651I    |                                       |                     |
| u = -0.341616 - 1.350480I |                                       |                     |
| a = 0.83289 + 2.47231I    | 2.35082 - 11.35200I                   | -9.44655 + 7.31316I |
| b = -1.84709 + 1.33663I   |                                       |                     |
| u = 0.051114 + 1.394540I  |                                       |                     |
| a = -1.201200 - 0.037073I | 7.60322 - 4.47665I                    | -4.97371 + 3.57345I |
| b = 1.89724 - 0.50837I    |                                       |                     |
| u = 0.051114 + 1.394540I  |                                       |                     |
| a = 0.588507 - 0.124880I  | 7.60322 - 4.47665I                    | -4.97371 + 3.57345I |
| b = -1.096760 - 0.435170I |                                       |                     |
| u = 0.051114 - 1.394540I  |                                       |                     |
| a = -1.201200 + 0.037073I | 7.60322 + 4.47665I                    | -4.97371 - 3.57345I |
| b = 1.89724 + 0.50837I    |                                       |                     |
| u = 0.051114 - 1.394540I  |                                       |                     |
| a = 0.588507 + 0.124880I  | 7.60322 + 4.47665I                    | -4.97371 - 3.57345I |
| b = -1.096760 + 0.435170I |                                       |                     |
| u = -0.234389 + 0.375701I |                                       |                     |
| a = 0.457879 + 0.838104I  | -3.42503 + 0.99510I                   | -14.4861 - 6.8230I  |
| b = 1.32986 + 0.99443I    |                                       |                     |
| u = -0.234389 + 0.375701I |                                       |                     |
| a = -1.19564 - 2.21012I   | -3.42503 + 0.99510I                   | -14.4861 - 6.8230I  |
| b = -0.416589 + 0.588948I |                                       |                     |
| u = -0.234389 - 0.375701I |                                       |                     |
| a = 0.457879 - 0.838104I  | -3.42503 - 0.99510I                   | -14.4861 + 6.8230I  |
| b = 1.32986 - 0.99443I    |                                       |                     |
| u = -0.234389 - 0.375701I |                                       |                     |
| a = -1.19564 + 2.21012I   | -3.42503 - 0.99510I                   | -14.4861 + 6.8230I  |
| b = -0.416589 - 0.588948I |                                       |                     |

III. 
$$I_3^u = \langle b-1, -2u^3 + 3u^2 + 3a - 3u + 3, u^4 + 3u^2 + 3 \rangle$$

$$a_{5} = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_{9} = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} 1 \\ u^{2} \end{pmatrix}$$

$$a_{4} = \begin{pmatrix} u \\ u^{3} + u \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} u^{2} + 1 \\ -u^{2} - 3 \end{pmatrix}$$

$$a_{2} = \begin{pmatrix} \frac{2}{3}u^{3} - u^{2} + u - 1 \\ 1 \end{pmatrix}$$

$$a_{6} = \begin{pmatrix} u^{3} + 2u \\ u^{3} + u \end{pmatrix}$$

$$a_{7} = \begin{pmatrix} \frac{1}{3}u^{3} + u^{2} + u + 1 \\ u^{3} + u - 1 \end{pmatrix}$$

$$a_{3} = \begin{pmatrix} u^{3} + 2u \\ u^{3} + u \end{pmatrix}$$

$$a_{1} = \begin{pmatrix} -\frac{1}{3}u^{3} - u^{2} - u - 1 \\ -u^{3} - u + 1 \end{pmatrix}$$

$$a_{8} = \begin{pmatrix} u^{2} + 1 \\ -u^{2} - 3 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} -\frac{1}{3}u^{3} - u \\ -u^{3} - u^{2} - u - 2 \end{pmatrix}$$

- (ii) Obstruction class = 1
- (iii) Cusp Shapes =  $4u^2 12$

| Crossings                | u-Polynomials at each crossing |
|--------------------------|--------------------------------|
| $c_1, c_2, c_7$ $c_{11}$ | $(u-1)^4$                      |
| $c_3, c_5, c_8$          | $u^4 - 3u^2 + 3$               |
| $c_4, c_9, c_{10}$       | $u^4 + 3u^2 + 3$               |
| $c_6, c_{12}$            | $(u+1)^4$                      |

| Crossings                              | Riley Polynomials at each crossing |
|--|------------------------------------|
| $c_1, c_2, c_6 \\ c_7, c_{11}, c_{12}$ | $(y-1)^4$                          |
| $c_3,c_5,c_8$                          | $(y^2 - 3y + 3)^2$                 |
| $c_4, c_9, c_{10}$                     | $(y^2 + 3y + 3)^2$                 |

| Solutions to $I_3^u$      | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape         |
|---------------------------|---------------------------------------|--------------------|
| u = 0.340625 + 1.271230I  |                                       |                    |
| a = -0.233945 - 0.669365I | -3.28987 - 4.05977I                   | -18.0000 + 3.4641I |
| b = 1.00000               |                                       |                    |
| u = 0.340625 - 1.271230I  |                                       |                    |
| a = -0.233945 + 0.669365I | -3.28987 + 4.05977I                   | -18.0000 - 3.4641I |
| b = 1.00000               |                                       |                    |
| u = -0.340625 + 1.271230I |                                       |                    |
| a = 1.23394 + 1.06269I    | -3.28987 + 4.05977I                   | -18.0000 - 3.4641I |
| b = 1.00000               |                                       |                    |
| u = -0.340625 - 1.271230I |                                       |                    |
| a = 1.23394 - 1.06269I    | -3.28987 - 4.05977I                   | -18.0000 + 3.4641I |
| b = 1.00000               |                                       |                    |

IV. 
$$I_4^u = \langle b+1, u^2+a-u+1, u^4+u^2-1 \rangle$$

$$a_{5} = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_{9} = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} 1 \\ u^{2} \end{pmatrix}$$

$$a_{4} = \begin{pmatrix} u \\ u^{3} + u \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} u^{2} + 1 \\ u^{2} + 1 \end{pmatrix}$$

$$a_{2} = \begin{pmatrix} -u^{2} + u - 1 \\ -1 \end{pmatrix}$$

$$a_{6} = \begin{pmatrix} -u^{3} - 2u \\ -u^{3} - u \end{pmatrix}$$

$$a_{7} = \begin{pmatrix} -u^{3} - 2u \\ -u^{3} - u - 1 \end{pmatrix}$$

$$a_{3} = \begin{pmatrix} u^{3} + 2u \\ u^{3} + u \end{pmatrix}$$

$$a_{1} = \begin{pmatrix} -u^{3} - u^{2} - u - 1 \\ -u^{3} - u - 1 \end{pmatrix}$$

$$a_{8} = \begin{pmatrix} -u^{2} - 1 \\ -u^{2} - 1 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} -u^{3} - u \\ -u^{3} + u^{2} - u \end{pmatrix}$$

- (ii) Obstruction class = 1
- (iii) Cusp Shapes =  $-4u^2 20$

| Crossings                   | u-Polynomials at each crossing |
|-----------------------------|--------------------------------|
| $c_1, c_6, c_{11}$ $c_{12}$ | $(u-1)^4$                      |
| $c_{2}, c_{7}$              | $(u+1)^4$                      |
| $c_3,c_5,c_8$               | $u^4 - u^2 - 1$                |
| $c_4, c_9, c_{10}$          | $u^4 + u^2 - 1$                |

| Crossings                              | Riley Polynomials at each crossing |
|--|------------------------------------|
| $c_1, c_2, c_6 \\ c_7, c_{11}, c_{12}$ | $(y-1)^4$                          |
| $c_3,c_5,c_8$                          | $(y^2-y-1)^2$                      |
| $c_4, c_9, c_{10}$                     | $(y^2+y-1)^2$                      |

| Solutions to $I_4^u$     | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape |
|--------------------------|---------------------------------------|------------|
| u = 0.786151             |                                       |            |
| a = -0.831883            | -7.23771                              | -22.4720   |
| b = -1.00000             |                                       |            |
| u = -0.786151            |                                       |            |
| a = -2.40419             | -7.23771                              | -22.4720   |
| b = -1.00000             |                                       |            |
| u = 1.272020I            |                                       |            |
| a = 0.618030 + 1.272020I | 0.657974                              | -13.5280   |
| b = -1.00000             |                                       |            |
| u = -1.272020I           |                                       |            |
| a = 0.618030 - 1.272020I | 0.657974                              | -13.5280   |
| b = -1.00000             |                                       |            |

V. 
$$I_1^v = \langle a, b-1, v+1 \rangle$$

$$a_5 = \begin{pmatrix} -1 \\ 0 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} -1 \\ 0 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} 0 \\ 1 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} -1 \\ 0 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} -1 \\ -1 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} -1 \\ 0 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} 1 \\ 1 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} 2 \\ 1 \end{pmatrix}$$

- (ii) Obstruction class = 1
- (iii) Cusp Shapes = -12

| Crossings                             | u-Polynomials at each crossing |
|---------------------------------------|--------------------------------|
| $c_1, c_2, c_7$ $c_{11}$              | u-1                            |
| $c_3, c_4, c_5$<br>$c_8, c_9, c_{10}$ | u                              |
| $c_6, c_{12}$                         | u+1                            |

| Crossings                              | Riley Polynomials at each crossing |
|--|------------------------------------|
| $c_1, c_2, c_6 \\ c_7, c_{11}, c_{12}$ | y-1                                |
| $c_3, c_4, c_5$<br>$c_8, c_9, c_{10}$  | y                                  |

| Solutions to $I_1^v$ | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape |
|----------------------|---------------------------------------|------------|
| v = -1.00000         |                                       |            |
| a = 0                | -3.28987                              | -12.0000   |
| b = 1.00000          |                                       |            |

VI. u-Polynomials

| Crossings          | u-Polynomials at each crossing   |
|--------------------|--|
| $c_1,c_{11}$       | $((u-1)^9)(u^{40}+17u^{39}+\cdots+19u+1)(u^{60}+33u^{59}+\cdots+4u+1)$   |
| $c_2, c_7$         | $((u-1)^5)(u+1)^4(u^{40}-u^{39}+\cdots-u-1)(u^{60}-u^{59}+\cdots-2u^2+1)$  |
| $c_3, c_5$         | $u(u^{4} - 3u^{2} + 3)(u^{4} - u^{2} - 1)(u^{30} + u^{29} + \dots + 5u + 5)^{2}$ $\cdot (u^{40} - 3u^{39} + \dots + 10u - 2)$        |
| $c_4, c_9, c_{10}$ | $u(u^{4} + u^{2} - 1)(u^{4} + 3u^{2} + 3)(u^{30} - u^{29} + \dots - u + 1)^{2}$ $\cdot (u^{40} + 3u^{39} + \dots - 6u - 2)$          |
| $c_6,c_{12}$       | $((u-1)^4)(u+1)^5(u^{40}-u^{39}+\cdots-u-1)(u^{60}-u^{59}+\cdots-2u^2+1)$  |
| C <sub>8</sub>     | $u(u^{4} - 3u^{2} + 3)(u^{4} - u^{2} - 1)(u^{30} + 7u^{29} + \dots + 39u + 7)^{2}$ $\cdot (u^{40} - 21u^{39} + \dots - 6214u + 562)$ |

VII. Riley Polynomials

| Crossings                | Riley Polynomials at each crossing  |
|--------------------------|---|
| $c_1,c_{11}$             | $((y-1)^9)(y^{40} + 23y^{39} + \dots - 67y + 1)(y^{60} - 13y^{59} + \dots + 28y + 1)$   |
| $c_2, c_6, c_7$ $c_{12}$ | $((y-1)^9)(y^{40}-17y^{39}+\cdots-19y+1)(y^{60}-33y^{59}+\cdots-4y+1)$  |
| $c_3,c_5$                | $y(y^{2} - 3y + 3)^{2}(y^{2} - y - 1)^{2}(y^{30} - 19y^{29} + \dots + 115y + 25)^{2}$ $\cdot (y^{40} - 27y^{39} + \dots + 64y + 4)$         |
| $c_4, c_9, c_{10}$       | $y(y^{2} + y - 1)^{2}(y^{2} + 3y + 3)^{2}(y^{30} + 25y^{29} + \dots + 3y + 1)^{2}$ $\cdot (y^{40} + 33y^{39} + \dots - 32y + 4)$            |
| c <sub>8</sub>           | $y(y^{2} - 3y + 3)^{2}(y^{2} - y - 1)^{2}(y^{30} + 5y^{29} + \dots + 383y + 49)^{2}$ $\cdot (y^{40} - 3y^{39} + \dots - 5405216y + 315844)$ |