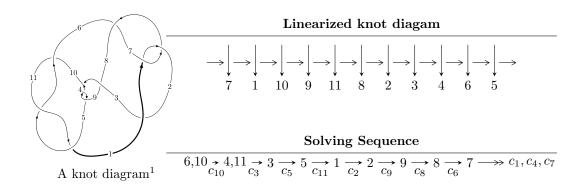
# $11a_{237} (K11a_{237})$



#### Ideals for irreducible components<sup>2</sup> of $X_{par}$

$$\begin{split} I_1^u &= \langle b-u,\ u^{19}-u^{18}+\dots+4a+1,\ u^{20}+11u^{18}+\dots+3u-1\rangle\\ I_2^u &= \langle -159484971u^{29}+121594878u^{28}+\dots+95716253b+570195911,\ -u^{29}+u^{28}+\dots+a+6,\\ u^{30}-u^{29}+\dots-6u+1\rangle\\ I_3^u &= \langle b+u,\ a^2-2au-a+u,\ u^2+1\rangle \end{split}$$

\* 3 irreducible components of  $\dim_{\mathbb{C}} = 0$ , with total 54 representations.

<sup>&</sup>lt;sup>1</sup>The image of knot diagram is generated by the software "**Draw programme**" developed by Andrew Bartholomew(http://www.layer8.co.uk/maths/draw/index.htm#Running-draw), where we modified some parts for our purpose(https://github.com/CATsTAILs/LinksPainter).

 $<sup>^2</sup>$  All coefficients of polynomials are rational numbers. But the coefficients are sometimes approximated in decimal forms when there is not enough margin.

I. 
$$I_1^u = \langle b-u, \ u^{19}-u^{18}+\cdots+4a+1, \ u^{20}+11u^{18}+\cdots+3u-1 \rangle$$

(i) Arc colorings

$$a_{6} = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{4} = \begin{pmatrix} -\frac{1}{4}u^{19} + \frac{1}{4}u^{18} + \dots + 3u - \frac{1}{4} \\ u \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 1 \\ u^{2} \end{pmatrix}$$

$$a_{3} = \begin{pmatrix} -\frac{1}{4}u^{19} + \frac{1}{4}u^{18} + \dots + 4u - \frac{1}{4} \\ u \end{pmatrix}$$

$$a_{5} = \begin{pmatrix} u \\ u^{3} + u \end{pmatrix}$$

$$a_{1} = \begin{pmatrix} u^{2} + 1 \\ u^{4} + 2u^{2} \end{pmatrix}$$

$$a_{2} = \begin{pmatrix} -\frac{1}{4}u^{19} + \frac{1}{4}u^{18} + \dots + 5u - \frac{1}{4} \\ \frac{1}{4}u^{19} - \frac{1}{4}u^{18} + \dots + u^{2} + \frac{1}{4} \end{pmatrix}$$

$$a_{9} = \begin{pmatrix} -\frac{1}{4}u^{19} - \frac{1}{4}u^{18} + \dots - \frac{1}{2}u + \frac{5}{4} \\ -u^{2} \end{pmatrix}$$

$$a_{8} = \begin{pmatrix} -\frac{1}{4}u^{19} - \frac{1}{4}u^{18} + \dots - \frac{1}{2}u + \frac{5}{4} \\ -u^{4} - 2u^{2} \end{pmatrix}$$

$$a_{7} = \begin{pmatrix} \frac{1}{2}u^{19} + \frac{1}{2}u^{18} + \dots + \frac{5}{2}u^{2} - 2u \\ \frac{1}{4}u^{19} - \frac{1}{4}u^{18} + \dots + u^{2} + \frac{1}{4} \end{pmatrix}$$

$$a_{7} = \begin{pmatrix} \frac{1}{2}u^{19} + \frac{1}{2}u^{18} + \dots + \frac{5}{2}u^{2} - 2u \\ \frac{1}{4}u^{19} - \frac{1}{4}u^{18} + \dots + u^{2} + \frac{1}{4} \end{pmatrix}$$

#### (ii) Obstruction class = -1

(iii) Cusp Shapes = 
$$-2u^{19} - 21u^{17} - 3u^{16} - 91u^{15} - 30u^{14} - 202u^{13} - 119u^{12} - 224u^{11} - 227u^{10} - 84u^9 - 181u^8 + 22u^7 + 14u^6 - 22u^5 + 64u^4 - 28u^3 - 25u^2 + 12u - 19u^2 - 224u^2 - 224u^2$$

## (iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
$c_1, c_7$	$u^{20} + 3u^{19} + \dots - 9u - 2$
$c_2, c_6$	$u^{20} + 7u^{19} + \dots + 33u + 4$
$c_3, c_4, c_5 \\ c_9, c_{10}, c_{11}$	$u^{20} + 11u^{18} + \dots - 3u - 1$
<i>c</i> <sub>8</sub>	$u^{20} - 3u^{19} + \dots - 48u - 32$

## (v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing	
$c_1, c_7$	$y^{20} - 7y^{19} + \dots - 33y + 4$	
$c_2, c_6$	$y^{20} + 13y^{19} + \dots - 561y + 16$	
$c_3, c_4, c_5 \\ c_9, c_{10}, c_{11}$	$y^{20} + 22y^{19} + \dots - 5y + 1$	
c <sub>8</sub>	$y^{20} - y^{19} + \dots + 3328y + 1024$	

## (vi) Complex Volumes and Cusp Shapes

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
u = -0.711644 + 0.213665I		
a = -0.992229 + 0.085972I	-0.77253 + 5.59830I	-13.4954 - 6.8250I
b = -0.711644 + 0.213665I		
u = -0.711644 - 0.213665I		
a = -0.992229 - 0.085972I	-0.77253 - 5.59830I	-13.4954 + 6.8250I
b = -0.711644 - 0.213665I		
u = -0.714807		
a = -0.946170	-4.75848	-19.2850
b = -0.714807		
u = 0.147507 + 1.344930I		
a = 1.07486 - 2.87571I	5.87096 + 0.28405I	-5.48153 - 0.41216I
b = 0.147507 + 1.344930I		
u = 0.147507 - 1.344930I		
a = 1.07486 + 2.87571I	5.87096 - 0.28405I	-5.48153 + 0.41216I
b = 0.147507 - 1.344930I		
u = 0.601815 + 0.228236I		
a = 0.950028 + 0.149217I	0.157185 - 0.414126I	-12.01664 + 2.08787I
b = 0.601815 + 0.228236I		
u = 0.601815 - 0.228236I		
a = 0.950028 - 0.149217I	0.157185 + 0.414126I	-12.01664 - 2.08787I
b = 0.601815 - 0.228236I		
u = 0.280299 + 1.365240I		
a = 1.37177 - 2.14002I	3.92725 - 7.17367I	-8.70322 + 5.73165I
b = 0.280299 + 1.365240I		
u = 0.280299 - 1.365240I		
a = 1.37177 + 2.14002I	3.92725 + 7.17367I	-8.70322 - 5.73165I
b = 0.280299 - 1.365240I		
u = -0.20040 + 1.40896I		
a = -1.00049 - 2.38403I	8.53664 + 4.27425I	-2.38649 - 3.51536I
b = -0.20040 + 1.40896I		

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
u = -0.20040 - 1.40896I		
a = -1.00049 + 2.38403I	8.53664 - 4.27425I	-2.38649 + 3.51536I
b = -0.20040 - 1.40896I		
u = 0.35253 + 1.44249I		
a = 1.15928 - 1.78353I	9.8480 - 13.6547I	-5.09222 + 8.08354I
b = 0.35253 + 1.44249I		
u = 0.35253 - 1.44249I		
a = 1.15928 + 1.78353I	9.8480 + 13.6547I	-5.09222 - 8.08354I
b = 0.35253 - 1.44249I		
u = -0.32179 + 1.45317I		
a = -1.09427 - 1.86772I	11.02130 + 7.69202I	-3.25100 - 3.40395I
b = -0.32179 + 1.45317I		
u = -0.32179 - 1.45317I		
a = -1.09427 + 1.86772I	11.02130 - 7.69202I	-3.25100 + 3.40395I
b = -0.32179 - 1.45317I		
u = 0.074422 + 0.475930I		
a = 0.299691 + 1.194600I	1.45151 - 2.34993I	-9.21397 + 4.74077I
b = 0.074422 + 0.475930I		
u = 0.074422 - 0.475930I		
a = 0.299691 - 1.194600I	1.45151 + 2.34993I	-9.21397 - 4.74077I
b = 0.074422 - 0.475930I		
u = -0.02313 + 1.54067I		
a = -0.08257 - 2.23973I	15.2534 + 3.0855I	-1.70716 - 2.62885I
b = -0.02313 + 1.54067I		
u = -0.02313 - 1.54067I		
a = -0.08257 + 2.23973I	15.2534 - 3.0855I	-1.70716 + 2.62885I
b = -0.02313 - 1.54067I		
u = 0.315603		
a = 0.574029	-0.553031	-18.0200
b = 0.315603		

II. 
$$I_2^u = \langle -1.59 \times 10^8 u^{29} + 1.22 \times 10^8 u^{28} + \dots + 9.57 \times 10^7 b + 5.70 \times 10^8, \ -u^{29} + u^{28} + \dots + a + 6, \ u^{30} - u^{29} + \dots - 6u + 1 \rangle$$

(i) Arc colorings

$$a_{6} = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{4} = \begin{pmatrix} u^{29} - u^{28} + \dots + 10u - 6 \\ 1.66623u^{29} - 1.27037u^{28} + \dots + 17.4027u - 5.95715 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 1 \\ u^{2} \end{pmatrix}$$

$$a_{3} = \begin{pmatrix} 2.66623u^{29} - 2.27037u^{28} + \dots + 27.4027u - 11.9571 \\ 1.66623u^{29} - 1.27037u^{28} + \dots + 17.4027u - 5.95715 \end{pmatrix}$$

$$a_{5} = \begin{pmatrix} u \\ u^{3} + u \end{pmatrix}$$

$$a_{1} = \begin{pmatrix} u^{2} + 1 \\ u^{4} + 2u^{2} \end{pmatrix}$$

$$a_{2} = \begin{pmatrix} 4.72929u^{29} - 3.69976u^{28} + \dots + 46.3017u - 17.7300 \\ 2.22042u^{29} - 1.73024u^{28} + \dots + 21.0519u - 7.17018 \end{pmatrix}$$

$$a_{9} = \begin{pmatrix} 5.95715u^{29} - 4.29092u^{28} + \dots + 56.4198u - 17.3402 \\ 0.395859u^{29} + 0.105883u^{28} + \dots + 4.04021u - 0.666227 \end{pmatrix}$$

$$a_{8} = \begin{pmatrix} 5.19351u^{29} - 3.62763u^{28} + \dots + 49.7650u - 14.1723 \\ -0.367778u^{29} + 0.769175u^{28} + \dots - 2.61459u + 1.50174 \end{pmatrix}$$

$$a_{7} = \begin{pmatrix} -6.74902u^{29} + 4.86232u^{28} + \dots - 65.5259u + 23.3729 \\ -2.01973u^{29} + 1.16256u^{28} + \dots - 17.2242u + 5.64291 \end{pmatrix}$$

$$a_{7} = \begin{pmatrix} -6.74902u^{29} + 4.86232u^{28} + \dots - 65.5259u + 23.3729 \\ -2.01973u^{29} + 1.16256u^{28} + \dots - 17.2242u + 5.64291 \end{pmatrix}$$

#### (ii) Obstruction class = -1

(iii) Cusp Shapes = 
$$\frac{583799292}{95716253}u^{29} - \frac{406184408}{95716253}u^{28} + \dots + \frac{4386525380}{95716253}u - \frac{2570388306}{95716253}u^{28} + \dots$$

## (iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing	
$c_1, c_7$	$(u^{15} - u^{14} + \dots + 2u - 1)^2$	
$c_2, c_6$	$(u^{15} + 5u^{14} + \dots + 12u^3 + 1)^2$	
$c_3, c_4, c_5 \\ c_9, c_{10}, c_{11}$	$u^{30} + u^{29} + \dots + 6u + 1$	
$c_8$	$(u^{15} + u^{14} + \dots - 4u - 1)^2$	

## (v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing	
$c_1, c_7$	$(y^{15} - 5y^{14} + \dots + 12y^3 - 1)^2$	
$c_2, c_6$	$(y^{15} + 11y^{14} + \dots - 84y^2 - 1)^2$	
$c_3, c_4, c_5 \\ c_9, c_{10}, c_{11}$	$y^{30} + 23y^{29} + \dots - 16y + 1$	
$c_8$	$(y^{15} - y^{14} + \dots + 16y - 1)^2$	

## (vi) Complex Volumes and Cusp Shapes

Solutions to $I_2^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
u = -0.171252 + 1.009920I		
a = 0.163210 + 0.962498I	1.46912 - 2.07402I	-11.82822 + 2.67122I
b = 0.318180 + 0.052816I		
u = -0.171252 - 1.009920I		
a = 0.163210 - 0.962498I	1.46912 + 2.07402I	-11.82822 - 2.67122I
b = 0.318180 - 0.052816I		
u = -0.607011 + 0.856391I		
a = 0.550893 + 0.777218I	6.82325 + 1.50523I	-3.84867 - 2.74048I
b = -0.108390 - 1.374740I		
u = -0.607011 - 0.856391I		
a = 0.550893 - 0.777218I	6.82325 - 1.50523I	-3.84867 + 2.74048I
b = -0.108390 + 1.374740I		
u = 0.879105 + 0.290763I		
a = -1.025350 + 0.339134I	4.31617 - 9.21780I	-8.14540 + 7.39135I
b = -0.28507 - 1.38638I		
u = 0.879105 - 0.290763I		
a = -1.025350 - 0.339134I	4.31617 + 9.21780I	-8.14540 - 7.39135I
b = -0.28507 + 1.38638I		
u = -0.836240 + 0.341718I		
a = 1.024720 + 0.418737I	5.27292 + 3.51852I	-6.28698 - 2.59027I
b = 0.241243 - 1.382540I		
u = -0.836240 - 0.341718I		
a = 1.024720 - 0.418737I	5.27292 - 3.51852I	-6.28698 + 2.59027I
b = 0.241243 + 1.382540I		
u = 0.587196 + 0.946781I		
a = -0.473090 + 0.762799I	6.30676 + 4.09199I	-4.95573 - 3.15094I
b = 0.171749 - 1.369410I		
u = 0.587196 - 0.946781I		
a = -0.473090 - 0.762799I	6.30676 - 4.09199I	-4.95573 + 3.15094I
b = 0.171749 + 1.369410I		

Solutions to $I_2^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
u = 0.269205 + 1.103370I		
a = -0.208705 + 0.855397I	1.86559	-10.56339 + 0.I
b = 0.269205 - 1.103370I		
u = 0.269205 - 1.103370I		
a = -0.208705 - 0.855397I	1.86559	-10.56339 + 0.I
b = 0.269205 + 1.103370I		
u = 0.119824 + 1.236680I		
a = -0.077620 + 0.801099I	2.93870 - 1.66084I	-6.48958 + 3.96405I
b = -0.505429 - 0.368881I		
u = 0.119824 - 1.236680I		
a = -0.077620 - 0.801099I	2.93870 + 1.66084I	-6.48958 - 3.96405I
b = -0.505429 + 0.368881I		
u = 0.706910 + 0.161570I		
a = -1.344380 + 0.307269I	-0.91830 - 3.60340I	-14.1637 + 4.4767I
b = -0.280017 - 1.247240I		
u = 0.706910 - 0.161570I		
a = -1.344380 - 0.307269I	-0.91830 + 3.60340I	-14.1637 - 4.4767I
b = -0.280017 + 1.247240I		
u = -0.280017 + 1.247240I		
a = 0.171369 + 0.763299I	-0.91830 + 3.60340I	-14.1637 - 4.4767I
b = 0.706910 - 0.161570I		
u = -0.280017 - 1.247240I		
a = 0.171369 - 0.763299I	-0.91830 - 3.60340I	-14.1637 + 4.4767I
b = 0.706910 + 0.161570I		
u = -0.505429 + 0.368881I		
a = 1.29090 + 0.94215I	2.93870 + 1.66084I	-6.48958 - 3.96405I
b = 0.119824 - 1.236680I		
u = -0.505429 - 0.368881I		
a = 1.29090 - 0.94215I	2.93870 - 1.66084I	-6.48958 + 3.96405I
b = 0.119824 + 1.236680I		

Solutions to $I_2^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
u = -0.108390 + 1.374740I		
a = 0.056998 + 0.722915I	6.82325 - 1.50523I	-3.84867 + 2.74048I
b = -0.607011 - 0.856391I		
u = -0.108390 - 1.374740I		
a = 0.056998 - 0.722915I	6.82325 + 1.50523I	-3.84867 - 2.74048I
b = -0.607011 + 0.856391I		
u = 0.171749 + 1.369410I		
a = -0.090167 + 0.718933I	6.30676 - 4.09199I	-4.95573 + 3.15094I
b = 0.587196 - 0.946781I		
u = 0.171749 - 1.369410I		
a = -0.090167 - 0.718933I	6.30676 + 4.09199I	-4.95573 - 3.15094I
b = 0.587196 + 0.946781I		
u = 0.241243 + 1.382540I		
a = -0.122482 + 0.701932I	5.27292 - 3.51852I	-6.28698 + 2.59027I
b = -0.836240 - 0.341718I		
u = 0.241243 - 1.382540I		
a = -0.122482 - 0.701932I	5.27292 + 3.51852I	-6.28698 - 2.59027I
b = -0.836240 + 0.341718I		
u = -0.28507 + 1.38638I		
a = 0.142301 + 0.692043I	4.31617 + 9.21780I	-8.14540 - 7.39135I
b = 0.879105 - 0.290763I		
u = -0.28507 - 1.38638I		
a = 0.142301 - 0.692043I	4.31617 - 9.21780I	-8.14540 + 7.39135I
b = 0.879105 + 0.290763I		
u = 0.318180 + 0.052816I		
a = -3.05860 + 0.50771I	1.46912 - 2.07402I	-11.82822 + 2.67122I
b = -0.171252 + 1.009920I		
u = 0.318180 - 0.052816I		
a = -3.05860 - 0.50771I	1.46912 + 2.07402I	-11.82822 - 2.67122I
b = -0.171252 - 1.009920I		

III. 
$$I_3^u=\langle b+u,\; a^2-2au-a+u,\; u^2+1 \rangle$$

(i) Arc colorings

and Arc Colorings
$$a_{6} = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{4} = \begin{pmatrix} a \\ -u \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 1 \\ -1 \end{pmatrix}$$

$$a_{3} = \begin{pmatrix} a - u \\ -u \end{pmatrix}$$

$$a_{5} = \begin{pmatrix} 0 \\ 0 \end{pmatrix}$$

$$a_{1} = \begin{pmatrix} 0 \\ -1 \end{pmatrix}$$

$$a_{2} = \begin{pmatrix} a - u \\ -a \end{pmatrix}$$

$$a_{9} = \begin{pmatrix} au + 1 \\ 1 \end{pmatrix}$$

$$a_{8} = \begin{pmatrix} au + 1 \\ 1 \end{pmatrix}$$

$$a_{7} = \begin{pmatrix} au - u + 1 \\ a \end{pmatrix}$$

$$a_{7} = \begin{pmatrix} au - u + 1 \\ a \end{pmatrix}$$

- (ii) Obstruction class = 1
- (iii) Cusp Shapes = 4a 4u 8

## (iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
$c_1, c_7$	$u^4 - u^2 + 1$
$c_2$	$(u^2+u+1)^2$
$c_3, c_4, c_5 \\ c_9, c_{10}, c_{11}$	$(u^2+1)^2$
<i>C</i> <sub>6</sub>	$(u^2 - u + 1)^2$
<i>c</i> <sub>8</sub>	$u^4$

## (v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing		
$c_1, c_7$	$(y^2 - y + 1)^2$		
$c_2, c_6$	$(y^2+y+1)^2$		
$c_3, c_4, c_5 \\ c_9, c_{10}, c_{11}$	$(y+1)^4$		
$c_8$	$y^4$		

## (vi) Complex Volumes and Cusp Shapes

	Solutions to $I_3^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
u =	1.000000I		
a =	0.500000 + 0.133975I	3.28987 + 2.02988I	-6.00000 - 3.46410I
b =	-1.000000I		
u =	1.000000I		
a =	0.50000 + 1.86603I	3.28987 - 2.02988I	-6.00000 + 3.46410I
b =	-1.000000I		
u =	-1.000000I		
a =	0.500000 - 0.133975I	3.28987 - 2.02988I	-6.00000 + 3.46410I
b =	1.000000I		
u =	-1.000000I		
a =	0.50000 - 1.86603I	3.28987 + 2.02988I	-6.00000 - 3.46410I
b =	1.000000I		

IV. u-Polynomials

Crossings	u-Polynomials at each crossing
$c_1, c_7$	$ (u^4 - u^2 + 1)(u^{15} - u^{14} + \dots + 2u - 1)^2(u^{20} + 3u^{19} + \dots - 9u - 2) $
$c_2$	$((u^{2} + u + 1)^{2})(u^{15} + 5u^{14} + \dots + 12u^{3} + 1)^{2}$ $\cdot (u^{20} + 7u^{19} + \dots + 33u + 4)$
$c_3, c_4, c_5 \\ c_9, c_{10}, c_{11}$	$((u^{2}+1)^{2})(u^{20}+11u^{18}+\cdots-3u-1)(u^{30}+u^{29}+\cdots+6u+1)$
<i>c</i> <sub>6</sub>	$((u^{2} - u + 1)^{2})(u^{15} + 5u^{14} + \dots + 12u^{3} + 1)^{2}$ $\cdot (u^{20} + 7u^{19} + \dots + 33u + 4)$
$c_8$	$u^{4}(u^{15} + u^{14} + \dots - 4u - 1)^{2}(u^{20} - 3u^{19} + \dots - 48u - 32)$

## V. Riley Polynomials

Crossings	Riley Polynomials at each crossing
$c_1, c_7$	$((y^{2} - y + 1)^{2})(y^{15} - 5y^{14} + \dots + 12y^{3} - 1)^{2}$ $\cdot (y^{20} - 7y^{19} + \dots - 33y + 4)$
$c_2, c_6$	$((y^{2} + y + 1)^{2})(y^{15} + 11y^{14} + \dots - 84y^{2} - 1)^{2}$ $\cdot (y^{20} + 13y^{19} + \dots - 561y + 16)$
$c_3, c_4, c_5 \\ c_9, c_{10}, c_{11}$	$((y+1)^4)(y^{20} + 22y^{19} + \dots - 5y + 1)(y^{30} + 23y^{29} + \dots - 16y + 1)$
c <sub>8</sub>	$y^{4}(y^{15} - y^{14} + \dots + 16y - 1)^{2}(y^{20} - y^{19} + \dots + 3328y + 1024)$