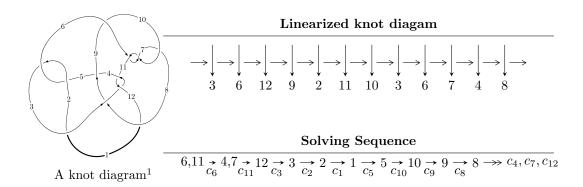
# $12n_{0503} \ (K12n_{0503})$



#### Ideals for irreducible components<sup>2</sup> of $X_{par}$

$$\begin{split} I_1^u &= \langle u^7 + u^6 + 3u^5 + 2u^4 + 2u^3 + 2u^2 + b, \ a - 1, \ u^8 + u^7 + 4u^6 + 3u^5 + 5u^4 + 4u^3 + u^2 + 3u - 1 \rangle \\ I_2^u &= \langle -u^2 + b + 2u, \ a + 1, \ u^3 - u^2 + 2u - 1 \rangle \\ I_3^u &= \langle u^{15} + 2u^{14} + 7u^{13} + 10u^{12} + 18u^{11} + 19u^{10} + 17u^9 + 12u^8 - 2u^7 - 3u^6 - 9u^5 - 4u^4 + 5u^3 + u^2 + 2b + 4u + 2u^{17} + 5u^{16} + \dots + 2a + 19u, \ u^{18} + 3u^{17} + \dots + 4u + 1 \rangle \\ I_4^u &= \langle u^2a - au + b + u, \ u^2a + a^2 - au + 3u^2 + a - u + 5, \ u^3 - u^2 + 2u - 1 \rangle \end{split}$$

\* 4 irreducible components of  $\dim_{\mathbb{C}} = 0$ , with total 35 representations.

<sup>&</sup>lt;sup>1</sup>The image of knot diagram is generated by the software "**Draw programme**" developed by Andrew Bartholomew(http://www.layer8.co.uk/maths/draw/index.htm#Running-draw), where we modified some parts for our purpose(https://github.com/CATsTAILs/LinksPainter).

 $<sup>^2</sup>$  All coefficients of polynomials are rational numbers. But the coefficients are sometimes approximated in decimal forms when there is not enough margin.

I. 
$$I_1^u = \langle u^7 + u^6 + 3u^5 + 2u^4 + 2u^3 + 2u^2 + b, \ a-1, \ u^8 + u^7 + 4u^6 + 3u^5 + 5u^4 + 4u^3 + u^2 + 3u - 1 \rangle$$

(i) Arc colorings

$$a_{6} = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_{4} = \begin{pmatrix} -u^{7} - u^{6} - 3u^{5} - 2u^{4} - 2u^{3} - 2u^{2} \end{pmatrix}$$

$$a_{7} = \begin{pmatrix} 1 \\ u^{2} \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} -u^{6} - u^{5} - 3u^{4} - 2u^{3} - u^{2} - 2u + 1 \end{pmatrix}$$

$$a_{3} = \begin{pmatrix} u^{2} + 1 \\ -u^{3} - u \end{pmatrix}$$

$$a_{2} = \begin{pmatrix} -u^{3} + u^{2} - u + 1 \\ -u^{3} - u \end{pmatrix}$$

$$a_{1} = \begin{pmatrix} u^{7} + u^{6} + 3u^{5} + 2u^{4} + 3u^{3} + u^{2} + 2u \\ u^{6} + u^{5} + u^{4} + 3u^{3} - 2u^{2} + 3u - 1 \end{pmatrix}$$

$$a_{5} = \begin{pmatrix} -u^{6} + u^{5} - 2u^{4} + 2u^{3} - u^{2} + u + 1 \\ -u^{6} - 2u^{4} - u^{2} \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} u \\ u^{3} + u \end{pmatrix}$$

$$a_{9} = \begin{pmatrix} u^{3} + 2u \\ u^{3} + u \end{pmatrix}$$

$$a_{8} = \begin{pmatrix} u^{2} + 1 \\ u^{4} + 2u^{2} \end{pmatrix}$$

- (ii) Obstruction class = -1
- (iii) Cusp Shapes =  $-4u^7 4u^6 12u^5 10u^4 10u^3 12u^2 + 2u 16u^4 12u^3 12u^3$

Crossings	u-Polynomials at each crossing
$c_1$	$u^{8} + 13u^{7} + 52u^{6} + 39u^{5} - 95u^{4} + 44u^{3} - 5u^{2} + 11u + 1$
$c_2, c_5, c_9$	$u^8 + u^7 - 6u^6 - 3u^5 + 5u^4 - 10u^3 + 5u^2 - u - 1$
$c_3, c_6, c_7$ $c_{10}, c_{11}$	$u^8 - u^7 + 4u^6 - 3u^5 + 5u^4 - 4u^3 + u^2 - 3u - 1$
$c_4$	$u^8 - 3u^7 - 4u^6 + 19u^5 - 33u^4 + 100u^3 + 91u^2 + 35u + 7$
c <sub>8</sub>	$u^8 + 7u^7 + 17u^6 + 16u^5 + 10u^4 + 28u^3 + 44u^2 + 32u + 8$
$c_{12}$	$u^8 - 6u^7 + 7u^6 + 18u^5 - 36u^4 - 10u^3 + 45u^2 - 14u - 12$

Crossings	Riley Polynomials at each crossing
$c_1$	$y^8 - 65y^7 + \dots - 131y + 1$
$c_2, c_5, c_9$	$y^8 - 13y^7 + 52y^6 - 39y^5 - 95y^4 - 44y^3 - 5y^2 - 11y + 1$
$c_3, c_6, c_7 \\ c_{10}, c_{11}$	$y^8 + 7y^7 + 20y^6 + 25y^5 + y^4 - 32y^3 - 33y^2 - 11y + 1$
$c_4$	$y^8 - 17y^7 + 64y^6 + 685y^5 - 3215y^4 - 17392y^3 + 819y^2 + 49y + 40y + 40y$
c <sub>8</sub>	$y^8 - 15y^7 + 85y^6 - 220y^5 + 268y^4 - 656y^3 + 304y^2 - 320y + 64$
$c_{12}$	$y^8 - 22y^7 + \dots - 1276y + 144$

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
u = 0.327709 + 0.937994I		
a = 1.00000	1.82186 - 2.79026I	-10.46165 + 4.33295I
b = 0.142755 + 0.492603I		
u = 0.327709 - 0.937994I		
a = 1.00000	1.82186 + 2.79026I	-10.46165 - 4.33295I
b = 0.142755 - 0.492603I		
u = -1.04994		
a = 1.00000	-16.6633	-16.3280
b = 1.57429		
u = 0.051026 + 1.292250I		
a = 1.00000	7.37589 - 2.10973I	-4.67802 + 3.20330I
b = 2.39119 - 1.00724I		
u = 0.051026 - 1.292250I		
a = 1.00000	7.37589 + 2.10973I	-4.67802 - 3.20330I
b = 2.39119 + 1.00724I		
u = -0.48935 + 1.37392I		
a = 1.00000	-7.96719 + 11.01890I	-10.38982 - 5.43515I
b = 1.78025 - 1.97737I		
u = -0.48935 - 1.37392I		
a = 1.00000	-7.96719 - 11.01890I	-10.38982 + 5.43515I
b = 1.78025 + 1.97737I		
u = 0.271177		
a = 1.00000	-0.602204	-16.6130
b = -0.202677		

II. 
$$I_2^u = \langle -u^2 + b + 2u, \ a+1, \ u^3 - u^2 + 2u - 1 \rangle$$

(i) Arc colorings

$$a_{6} = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_{4} = \begin{pmatrix} -1 \\ u^{2} - 2u \end{pmatrix}$$

$$a_{7} = \begin{pmatrix} 1 \\ u^{2} \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} -u \\ -u^{2} - u + 1 \end{pmatrix}$$

$$a_{3} = \begin{pmatrix} -u^{2} - 1 \\ -u^{2} + u - 1 \end{pmatrix}$$

$$a_{2} = \begin{pmatrix} -2u^{2} + u - 2 \\ -u^{2} + u - 1 \end{pmatrix}$$

$$a_{1} = \begin{pmatrix} -u^{2} - 1 \\ -u^{2} \end{pmatrix}$$

$$a_{5} = \begin{pmatrix} -u \\ -u \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} u \\ u^{2} - u + 1 \end{pmatrix}$$

$$a_{9} = \begin{pmatrix} u^{2} + 1 \\ u^{2} - u + 1 \end{pmatrix}$$

$$a_{8} = \begin{pmatrix} u^{2} + 1 \\ u^{2} - u + 1 \end{pmatrix}$$

- (ii) Obstruction class = 1
- (iii) Cusp Shapes =  $-8u^2 + 8u 20$

Crossings	u-Polynomials at each crossing
$c_1, c_6, c_7$ $c_{11}$	$u^3 - u^2 + 2u - 1$
$c_2$	$u^3 + u^2 - 1$
$c_3, c_{10}, c_{12}$	$u^3 + u^2 + 2u + 1$
$c_4$	$u^3 + 3u^2 + 2u - 1$
$c_5, c_9$	$u^3 - u^2 + 1$
c <sub>8</sub>	$u^3$

Crossings	Riley Polynomials at each crossing
$c_1, c_3, c_6 \\ c_7, c_{10}, c_{11} \\ c_{12}$	$y^3 + 3y^2 + 2y - 1$
$c_2, c_5, c_9$	$y^3 - y^2 + 2y - 1$
$C_4$	$y^3 - 5y^2 + 10y - 1$
<i>c</i> <sub>8</sub>	$y^3$

Solutions to $I_2^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
u = 0.215080 + 1.307140I		
a = -1.00000	6.04826 - 5.65624I	-4.98049 + 5.95889I
b = -2.09252 - 2.05200I		
u = 0.215080 - 1.307140I		
a = -1.00000	6.04826 + 5.65624I	-4.98049 - 5.95889I
b = -2.09252 + 2.05200I		
u = 0.569840		
a = -1.00000	-2.22691	-18.0390
b = -0.814963		

(i) Arc colorings

$$a_{6} = \begin{pmatrix} 1\\0 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 0\\u \end{pmatrix}$$

$$a_{4} = \begin{pmatrix} -u^{17} - \frac{5}{2}u^{16} + \dots - 4u^{2} - \frac{19}{2}u\\ -\frac{1}{2}u^{15} - u^{14} + \dots - 2u - \frac{1}{2} \end{pmatrix}$$

$$a_{7} = \begin{pmatrix} 1\\u^{2} \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} -\frac{5}{2}u^{17} - \frac{15}{2}u^{16} + \dots - \frac{31}{2}u - 7\\ -\frac{1}{2}u^{17} - \frac{5}{2}u^{16} + \dots - \frac{7}{2}u - 2 \end{pmatrix}$$

$$a_{3} = \begin{pmatrix} \frac{5}{2}u^{17} + 8u^{16} + \dots + 17u + 4\\ -\frac{1}{2}u^{17} - u^{15} + \dots + 6u + \frac{5}{2} \end{pmatrix}$$

$$a_{2} = \begin{pmatrix} 2u^{17} + 8u^{16} + \dots + 23u + \frac{13}{2}\\ -\frac{1}{2}u^{17} - u^{15} + \dots + 6u + \frac{5}{2} \end{pmatrix}$$

$$a_{1} = \begin{pmatrix} 2u^{17} + \frac{11}{2}u^{16} + \dots + \frac{23}{2}u + \frac{11}{2}\\ 2u^{17} + 6u^{16} + \dots + 7u + \frac{5}{2} \end{pmatrix}$$

$$a_{5} = \begin{pmatrix} -\frac{3}{2}u^{17} - \frac{7}{2}u^{16} + \dots - \frac{23}{2}u - 1\\ -\frac{1}{2}u^{17} - u^{16} + \dots - 3u - 1 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} u\\u^{3} + u \end{pmatrix}$$

$$a_{9} = \begin{pmatrix} u^{3} + 2u\\u^{3} + u \end{pmatrix}$$

$$a_{8} = \begin{pmatrix} u^{2} + 1\\u^{4} + 2u^{2} \end{pmatrix}$$

#### (ii) Obstruction class = -1

(iii) Cusp Shapes = 
$$\frac{1}{2}u^{17} + 4u^{16} + 13u^{15} + 37u^{14} + \frac{143}{2}u^{13} + \frac{251}{2}u^{12} + \frac{331}{2}u^{11} + \frac{375}{2}u^{10} + \frac{315}{2}u^9 + \frac{169}{2}u^8 + \frac{15}{2}u^7 - \frac{125}{2}u^6 - 62u^5 - \frac{73}{2}u^4 + \frac{13}{2}u^3 + 28u^2 + 18u - \frac{3}{2}u^8 + \frac{15}{2}u^8 + \frac{15$$

Crossings	u-Polynomials at each crossing
$c_1$	$u^{18} + 31u^{17} + \dots - 4u + 1$
$c_2, c_5, c_9$	$u^{18} + 3u^{17} + \dots + 4u + 1$
$c_3, c_6, c_7 \\ c_{10}, c_{11}$	$u^{18} - 3u^{17} + \dots - 4u + 1$
$c_4$	$u^{18} - 21u^{16} + \dots + 640u + 1709$
c <sub>8</sub>	$ (u^9 - 3u^8 - 4u^7 + 17u^6 - 8u^5 + u^4 - 9u^3 + 20u^2 - 12u + 8)^2 $
$c_{12}$	$(u^9 + 2u^8 - 4u^7 - 5u^6 + u^5 - 11u^4 + u^3 - 2u^2 + u - 3)^2$

Crossings	Riley Polynomials at each crossing
$c_1$	$y^{18} - 103y^{17} + \dots + 100y + 1$
$c_2,c_5,c_9$	$y^{18} - 31y^{17} + \dots + 4y + 1$
$c_3, c_6, c_7$ $c_{10}, c_{11}$	$y^{18} + 13y^{17} + \dots + 4y + 1$
$c_4$	$y^{18} - 42y^{17} + \dots - 5810040y + 2920681$
$c_8$	$(y^9 - 17y^8 + \dots - 176y - 64)^2$
$c_{12}$	$(y^9 - 12y^8 + 38y^7 + 13y^6 - 107y^5 - 135y^4 - 71y^3 - 68y^2 - 11y - 9)^2$

Solutions to $I_3^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
u = -1.030260 + 0.064097I		
a = 0.593567 - 1.271510I	-12.47200 + 5.60959I	-13.58318 - 2.91483I
b = 1.29698 - 0.73855I		
u = -1.030260 - 0.064097I		
a = 0.593567 + 1.271510I	-12.47200 - 5.60959I	-13.58318 + 2.91483I
b = 1.29698 + 0.73855I		
u = -0.210201 + 1.054780I		
a = -1.310130 + 0.002220I	4.64765 + 4.49302I	-9.27331 - 2.63055I
b = -1.54000 + 1.83413I		
u = -0.210201 - 1.054780I		
a = -1.310130 - 0.002220I	4.64765 - 4.49302I	-9.27331 + 2.63055I
b = -1.54000 - 1.83413I		
u = -0.132410 + 0.848357I		
a = -0.345719 - 0.790410I	-0.376754 + 0.892025I	-13.26164 - 1.57550I
b = -0.749423 + 0.610778I		
u = -0.132410 - 0.848357I		
a = -0.345719 + 0.790410I	-0.376754 - 0.892025I	-13.26164 + 1.57550I
b = -0.749423 - 0.610778I		
u = 0.716326 + 0.188635I		
a = -0.464508 - 1.061990I	-0.376754 - 0.892025I	-13.26164 + 1.57550I
b = -0.749423 - 0.610778I		
u = 0.716326 - 0.188635I		
a = -0.464508 + 1.061990I	-0.376754 + 0.892025I	-13.26164 - 1.57550I
b = -0.749423 + 0.610778I		
u = 0.227734 + 1.247250I		
a = 0.186877 + 0.242619I	2.67018 - 2.29545I	-5.81910 + 1.31175I
b = -0.116635 - 0.608467I		
u = 0.227734 - 1.247250I		
a =  0.186877 - 0.242619I	2.67018 + 2.29545I	-5.81910 - 1.31175I
b = -0.116635 + 0.608467I		

Solutions to $I_3^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
u = 0.273050 + 1.382370I		
a = -0.763279 + 0.001294I	4.64765 - 4.49302I	-9.27331 + 2.63055I
b = -1.54000 - 1.83413I		
u = 0.273050 - 1.382370I		
a = -0.763279 - 0.001294I	4.64765 + 4.49302I	-9.27331 - 2.63055I
b = -1.54000 + 1.83413I		
u = -0.554172 + 1.295970I		
a = -0.690827 + 0.723020I	-8.67732	-11.12553 + 0.I
b = 0.218157		
u = -0.554172 - 1.295970I		
a = -0.690827 - 0.723020I	-8.67732	-11.12553 + 0.I
b = 0.218157		
u = -0.53003 + 1.34802I		
a = 0.301448 + 0.645745I	-12.47200 + 5.60959I	-13.58318 - 2.91483I
b = 1.29698 - 0.73855I		
u = -0.53003 - 1.34802I		
a = 0.301448 - 0.645745I	-12.47200 - 5.60959I	-13.58318 + 2.91483I
b = 1.29698 + 0.73855I		
u = -0.260047 + 0.288335I		
a = 1.99257 - 2.58691I	2.67018 - 2.29545I	-5.81910 + 1.31175I
b = -0.116635 - 0.608467I		
u = -0.260047 - 0.288335I		
a = 1.99257 + 2.58691I	2.67018 + 2.29545I	-5.81910 - 1.31175I
b = -0.116635 + 0.608467I		

 $\text{IV. } I_4^u = \langle u^2a - au + b + u, \ u^2a + a^2 - au + 3u^2 + a - u + 5, \ u^3 - u^2 + 2u - 1 \rangle$ 

(i) Arc colorings

$$a_{6} = \begin{pmatrix} 1\\0 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 0\\u \end{pmatrix}$$

$$a_{4} = \begin{pmatrix} a\\-u^{2}a + au - u \end{pmatrix}$$

$$a_{7} = \begin{pmatrix} 1\\u^{2} \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} -au + 2u^{2} + a - u + 3\\-au + u^{2} + a + 1 \end{pmatrix}$$

$$a_{3} = \begin{pmatrix} -au + u^{2} + 1\\-u^{2}a + u^{2} - u + 1 \end{pmatrix}$$

$$a_{2} = \begin{pmatrix} -u^{2}a - au + 2u^{2} - u + 2\\-u^{2}a + u^{2} - u + 1 \end{pmatrix}$$

$$a_{1} = \begin{pmatrix} -u^{2}a - au + 3u^{2} + a - 2u + 4\\-u^{2}a + au + u^{2} - u + 2 \end{pmatrix}$$

$$a_{5} = \begin{pmatrix} au + a + 1\\au \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} u\\u^{2} - u + 1 \end{pmatrix}$$

$$a_{9} = \begin{pmatrix} u\\u^{2} - u + 1 \end{pmatrix}$$

- (ii) Obstruction class = 1
- (iii) Cusp Shapes =  $-3u^2a 2au + 2u 15$

Crossings	u-Polynomials at each crossing
$c_1, c_6, c_7$ $c_{11}$	$(u^3 - u^2 + 2u - 1)^2$
$c_2$	$(u^3 + u^2 - 1)^2$
$c_3,c_{10}$	$(u^3 + u^2 + 2u + 1)^2$
$c_4$	$u^6 - u^5 + 4u^4 - u^3 + 2u^2 + 2u + 1$
$c_5, c_9$	$(u^3 - u^2 + 1)^2$
<i>C</i> <sub>8</sub>	$u^6$
$c_{12}$	$(u^3 - u + 1)^2$

Crossings	Riley Polynomials at each crossing
$c_1, c_3, c_6 \\ c_7, c_{10}, c_{11}$	$(y^3 + 3y^2 + 2y - 1)^2$
$c_2, c_5, c_9$	$(y^3 - y^2 + 2y - 1)^2$
$C_4$	$y^6 + 7y^5 + 18y^4 + 21y^3 + 16y^2 + 1$
<i>c</i> <sub>8</sub>	$y^6$
$c_{12}$	$(y^3 - 2y^2 + y - 1)^2$

Solutions to $I_4^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
u = 0.215080 + 1.307140I		
a = 0.947279 + 0.320410I	6.04826	-8.87505 + 0.I
b = 1.32472		
u = 0.215080 + 1.307140I		
a = -0.069840 + 0.424452I	1.91067 - 2.82812I	-13.06248 + 4.84887I
b = -0.662359 - 0.562280I		
u = 0.215080 - 1.307140I		
a = 0.947279 - 0.320410I	6.04826	-8.87505 + 0.I
b = 1.32472		
u = 0.215080 - 1.307140I		
a = -0.069840 - 0.424452I	1.91067 + 2.82812I	-13.06248 - 4.84887I
b = -0.662359 + 0.562280I		
u = 0.569840		
a = -0.37744 + 2.29387I	1.91067 + 2.82812I	-13.06248 - 4.84887I
b = -0.662359 + 0.562280I		
u = 0.569840		
a = -0.37744 - 2.29387I	1.91067 - 2.82812I	-13.06248 + 4.84887I
b = -0.662359 - 0.562280I		

#### V. u-Polynomials

Crossings	u-Polynomials at each crossing
$c_1$	$(u^{3} - u^{2} + 2u - 1)^{3}$ $\cdot (u^{8} + 13u^{7} + 52u^{6} + 39u^{5} - 95u^{4} + 44u^{3} - 5u^{2} + 11u + 1)$ $\cdot (u^{18} + 31u^{17} + \dots - 4u + 1)$
$c_2$	$(u^{3} + u^{2} - 1)^{3}(u^{8} + u^{7} - 6u^{6} - 3u^{5} + 5u^{4} - 10u^{3} + 5u^{2} - u - 1)$ $\cdot (u^{18} + 3u^{17} + \dots + 4u + 1)$
$c_3,c_{10}$	$(u^{3} + u^{2} + 2u + 1)^{3}(u^{8} - u^{7} + 4u^{6} - 3u^{5} + 5u^{4} - 4u^{3} + u^{2} - 3u - 1)$ $\cdot (u^{18} - 3u^{17} + \dots - 4u + 1)$
$c_4$	$(u^{3} + 3u^{2} + 2u - 1)(u^{6} - u^{5} + 4u^{4} - u^{3} + 2u^{2} + 2u + 1)$ $\cdot (u^{8} - 3u^{7} - 4u^{6} + 19u^{5} - 33u^{4} + 100u^{3} + 91u^{2} + 35u + 7)$ $\cdot (u^{18} - 21u^{16} + \dots + 640u + 1709)$
$c_5,c_9$	$ (u^{3} - u^{2} + 1)^{3}(u^{8} + u^{7} - 6u^{6} - 3u^{5} + 5u^{4} - 10u^{3} + 5u^{2} - u - 1) $ $ \cdot (u^{18} + 3u^{17} + \dots + 4u + 1) $
$c_6, c_7, c_{11}$	$(u^{3} - u^{2} + 2u - 1)^{3}(u^{8} - u^{7} + 4u^{6} - 3u^{5} + 5u^{4} - 4u^{3} + u^{2} - 3u - 1)$ $\cdot (u^{18} - 3u^{17} + \dots - 4u + 1)$
$c_8$	$u^{9}(u^{8} + 7u^{7} + 17u^{6} + 16u^{5} + 10u^{4} + 28u^{3} + 44u^{2} + 32u + 8)$ $\cdot (u^{9} - 3u^{8} - 4u^{7} + 17u^{6} - 8u^{5} + u^{4} - 9u^{3} + 20u^{2} - 12u + 8)^{2}$
$c_{12}$	$(u^{3} - u + 1)^{2}(u^{3} + u^{2} + 2u + 1)$ $\cdot (u^{8} - 6u^{7} + 7u^{6} + 18u^{5} - 36u^{4} - 10u^{3} + 45u^{2} - 14u - 12)$ $\cdot (u^{9} + 2u^{8} - 4u^{7} - 5u^{6} + u^{5} - 11u^{4} + u^{3} - 2u^{2} + u - 3)^{2}$

### VI. Riley Polynomials

Crossings	Riley Polynomials at each crossing
$c_1$	$((y^3 + 3y^2 + 2y - 1)^3)(y^8 - 65y^7 + \dots - 131y + 1)$ $\cdot (y^{18} - 103y^{17} + \dots + 100y + 1)$
$c_2, c_5, c_9$	$(y^3 - y^2 + 2y - 1)^3$ $\cdot (y^8 - 13y^7 + 52y^6 - 39y^5 - 95y^4 - 44y^3 - 5y^2 - 11y + 1)$ $\cdot (y^{18} - 31y^{17} + \dots + 4y + 1)$
$c_3, c_6, c_7$ $c_{10}, c_{11}$	$(y^{3} + 3y^{2} + 2y - 1)^{3}$ $\cdot (y^{8} + 7y^{7} + 20y^{6} + 25y^{5} + y^{4} - 32y^{3} - 33y^{2} - 11y + 1)$ $\cdot (y^{18} + 13y^{17} + \dots + 4y + 1)$
$c_4$	$(y^3 - 5y^2 + 10y - 1)(y^6 + 7y^5 + 18y^4 + 21y^3 + 16y^2 + 1)$ $\cdot (y^8 - 17y^7 + 64y^6 + 685y^5 - 3215y^4 - 17392y^3 + 819y^2 + 49y + 49)$ $\cdot (y^{18} - 42y^{17} + \dots - 5810040y + 2920681)$
$c_8$	$y^{9}(y^{8} - 15y^{7} + \dots - 320y + 64)$ $\cdot (y^{9} - 17y^{8} + \dots - 176y - 64)^{2}$
$c_{12}$	$(y^{3} - 2y^{2} + y - 1)^{2}(y^{3} + 3y^{2} + 2y - 1)$ $\cdot (y^{8} - 22y^{7} + \dots - 1276y + 144)$ $\cdot (y^{9} - 12y^{8} + 38y^{7} + 13y^{6} - 107y^{5} - 135y^{4} - 71y^{3} - 68y^{2} - 11y - 9)^{2}$