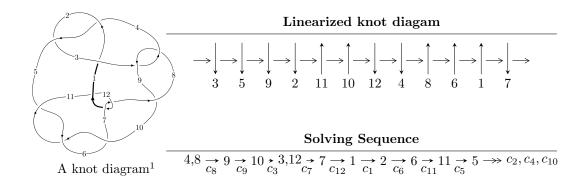
## $12a_{0155} (K12a_{0155})$



# Ideals for irreducible components<sup>2</sup> of $X_{par}$

$$\begin{split} I_1^u &= \langle -2.07210 \times 10^{79} u^{73} - 4.45872 \times 10^{79} u^{72} + \dots + 1.81105 \times 10^{80} b - 5.45671 \times 10^{80}, \\ & 9.44926 \times 10^{78} u^{73} + 1.37256 \times 10^{79} u^{72} + \dots + 6.03683 \times 10^{79} a + 2.79535 \times 10^{80}, \ u^{74} + 2u^{73} + \dots + 16u + I_2^u &= \langle 12u^8 a^2 - 12u^8 + \dots - 283a - 196, \ 2u^8 a^2 + 5u^8 a + \dots + 9a - 20, \\ & u^9 - u^8 + 2u^7 - u^6 + 3u^5 - u^4 + 2u^3 + u + 1 \rangle \\ I_3^u &= \langle u^{11} + 2u^9 + 2u^7 - u^3 + b, \ -u^{10} + u^9 - 3u^8 + 2u^7 - 5u^6 + 2u^5 - 4u^4 - 2u^2 + a - u - 1, \\ & u^{12} + 3u^{10} + 5u^8 + 4u^6 + 2u^4 + u^2 + 1 \rangle \end{split}$$

$$I_1^v = \langle a, -2v^3 + 3v^2 + 4b - 8v + 3, 2v^4 - v^3 + 5v^2 + v + 1 \rangle$$

\* 4 irreducible components of  $\dim_{\mathbb{C}} = 0$ , with total 117 representations.

<sup>&</sup>lt;sup>1</sup>The image of knot diagram is generated by the software "**Draw programme**" developed by Andrew Bartholomew(http://www.layer8.co.uk/maths/draw/index.htm#Running-draw), where we modified some parts for our purpose(https://github.com/CATsTAILs/LinksPainter).

<sup>&</sup>lt;sup>2</sup> All coefficients of polynomials are rational numbers. But the coefficients are sometimes approximated in decimal forms when there is not enough margin.

I. 
$$I_1^u = \langle -2.07 \times 10^{79} u^{73} - 4.46 \times 10^{79} u^{72} + \cdots + 1.81 \times 10^{80} b - 5.46 \times 10^{80}, \ 9.45 \times 10^{78} u^{73} + 1.37 \times 10^{79} u^{72} + \cdots + 6.04 \times 10^{79} a + 2.80 \times 10^{80}, \ u^{74} + 2u^{73} + \cdots + 16u + 64 \rangle$$

$$a_{4} = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_{8} = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{9} = \begin{pmatrix} 1 \\ u^{2} \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} u^{2}+1 \\ u^{2} \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} -0.156527u^{73} - 0.227365u^{72} + \dots - 9.44771u - 4.63049 \\ 0.114414u^{73} + 0.246195u^{72} + \dots + 18.2624u + 3.01301 \end{pmatrix}$$

$$a_{7} = \begin{pmatrix} -0.0427323u^{73} - 0.0222590u^{72} + \dots - 17.0843u - 2.73523 \\ 0.0558199u^{73} + 0.00860331u^{72} + \dots + 7.08355u - 20.4297 \end{pmatrix}$$

$$a_{1} = \begin{pmatrix} -0.247663u^{73} - 0.406614u^{72} + \dots - 47.8687u - 2.35262 \\ -0.0419160u^{73} - 0.134596u^{72} + \dots - 19.1036u - 12.4163 \end{pmatrix}$$

$$a_{2} = \begin{pmatrix} -0.200457u^{73} - 0.360919u^{72} + \dots - 39.4697u - 7.35311 \\ 0.00721908u^{73} - 0.0715981u^{72} + \dots - 12.9464u - 14.2988 \end{pmatrix}$$

$$a_{6} = \begin{pmatrix} -0.0796114u^{73} - 0.0728386u^{72} + \dots - 15.9420u + 4.33996 \\ 0.101084u^{73} + 0.0798881u^{72} + \dots + 11.6620u - 23.1448 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} -0.143338u^{73} - 0.243103u^{72} + \dots - 20.1363u + 2.92790 \\ -0.144745u^{73} - 0.280896u^{72} + \dots - 39.7884u + 8.31570 \end{pmatrix}$$

$$a_{5} = \begin{pmatrix} -0.150768u^{73} - 0.223403u^{72} + \dots - 14.3340u + 4.38601 \\ 0.0968957u^{73} + 0.183211u^{72} + \dots + 33.5347u + 6.73864 \end{pmatrix}$$

- (ii) Obstruction class = -1
- (iii) Cusp Shapes =  $-0.801859u^{73} 1.46138u^{72} + \cdots 97.4961u + 28.5646$

Crossings	u-Polynomials at each crossing
$c_1$	$u^{74} + 40u^{73} + \dots + 177u + 16$
$c_2, c_4$	$u^{74} - 4u^{73} + \dots - 35u + 4$
$c_{3}, c_{8}$	$u^{74} + 2u^{73} + \dots + 16u + 64$
$c_5, c_6, c_{10}$	$u^{74} + 2u^{73} + \dots + 78u + 9$
$c_7, c_{12}$	$u^{74} + 2u^{73} + \dots + 54u + 9$
<i>c</i> <sub>9</sub>	$u^{74} - 24u^{73} + \dots - 103168u + 4096$
$c_{11}$	$u^{74} - 26u^{73} + \dots - 2880u + 81$

Crossings	Riley Polynomials at each crossing
$c_1$	$y^{74} - 8y^{73} + \dots - 5953y + 256$
$c_2, c_4$	$y^{74} - 40y^{73} + \dots - 177y + 16$
$c_{3}, c_{8}$	$y^{74} + 24y^{73} + \dots + 103168y + 4096$
$c_5, c_6, c_{10}$	$y^{74} + 82y^{73} + \dots - 3456y + 81$
$c_7, c_{12}$	$y^{74} + 26y^{73} + \dots + 2880y + 81$
<i>C</i> 9	$y^{74} + 44y^{73} + \dots - 654376960y + 16777216$
$c_{11}$	$y^{74} + 58y^{73} + \dots + 591300y + 6561$

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
u = -1.016280 + 0.056443I		
a = -0.846246 - 0.233543I	-4.55260 - 4.71728I	-5.48750 + 5.97757I
b = -0.641966 - 0.915109I		
u = -1.016280 - 0.056443I		
a = -0.846246 + 0.233543I	-4.55260 + 4.71728I	-5.48750 - 5.97757I
b = -0.641966 + 0.915109I		
u = 0.715978 + 0.749309I		
a = -1.009060 + 0.512831I	-10.62080 + 2.16848I	-8.29410 + 0.I
b = -0.819433 + 1.097530I		
u = 0.715978 - 0.749309I		
a = -1.009060 - 0.512831I	-10.62080 - 2.16848I	-8.29410 + 0.I
b = -0.819433 - 1.097530I		
u = 1.018120 + 0.241002I		
a = -0.883835 - 0.063210I	-4.97717 - 0.27862I	-6.77921 + 0.I
b = -0.634326 - 0.779842I		
u = 1.018120 - 0.241002I		
a = -0.883835 + 0.063210I	-4.97717 + 0.27862I	-6.77921 + 0.I
b = -0.634326 + 0.779842I		
u = 0.101684 + 0.941180I		
a = -0.96039 + 1.37103I	-6.34170 + 2.58749I	-5.26885 - 2.40308I
b = 0.668786 - 0.848557I		
u = 0.101684 - 0.941180I		
a = -0.96039 - 1.37103I	-6.34170 - 2.58749I	-5.26885 + 2.40308I
b = 0.668786 + 0.848557I		
u = 0.702951 + 0.605779I		
a = 1.083580 - 0.777415I	-0.36424 + 2.16926I	-1.33400 - 2.94106I
b = 0.577935 - 0.892143I		
u = 0.702951 - 0.605779I		
a = 1.083580 + 0.777415I	-0.36424 - 2.16926I	-1.33400 + 2.94106I
b = 0.577935 + 0.892143I		

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
u = 0.455877 + 0.982311I		
a = 0.549167 + 0.442923I	-1.99851 - 5.40155I	0
b = 0.532038 + 0.022585I		
u = 0.455877 - 0.982311I		
a = 0.549167 - 0.442923I	-1.99851 + 5.40155I	0
b = 0.532038 - 0.022585I		
u = -0.688565 + 0.844832I		
a = -2.45152 - 0.54418I	-3.63561 + 3.57244I	0
b = -0.623313 + 0.954050I		
u = -0.688565 - 0.844832I		
a = -2.45152 + 0.54418I	-3.63561 - 3.57244I	0
b = -0.623313 - 0.954050I		
u = -0.922080 + 0.581194I		
a = -0.902921 - 0.473277I	-6.70976 - 5.72717I	0
b = -0.730349 - 1.085650I		
u = -0.922080 - 0.581194I		
a = -0.902921 + 0.473277I	-6.70976 + 5.72717I	0
b = -0.730349 + 1.085650I		
u = 0.400961 + 1.025910I		
a = 0.513025 - 0.645985I	3.87862 - 1.01189I	0
b = -0.156641 + 1.061890I		
u = 0.400961 - 1.025910I		
a = 0.513025 + 0.645985I	3.87862 + 1.01189I	0
b = -0.156641 - 1.061890I		
u = -0.039055 + 1.116760I		
a = -0.491876 - 1.057740I	5.21780 + 1.15055I	0
b = -0.338560 + 1.089190I		
u = -0.039055 - 1.116760I		
a = -0.491876 + 1.057740I	5.21780 - 1.15055I	0
b = -0.338560 - 1.089190I		1

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
u = -0.686707 + 0.883279I		
a = 1.136820 + 0.777943I	-3.51612 + 1.72512I	0
b = 0.710003 + 0.868137I		
u = -0.686707 - 0.883279I		
a = 1.136820 - 0.777943I	-3.51612 - 1.72512I	0
b = 0.710003 - 0.868137I		
u = -0.780808 + 0.406319I		
a = 1.069120 - 0.412845I	-0.190732 - 0.765674I	0.883971 + 0.910639I
b = 0.132045 - 0.962513I		
u = -0.780808 - 0.406319I		
a = 1.069120 + 0.412845I	-0.190732 + 0.765674I	0.883971 - 0.910639I
b = 0.132045 + 0.962513I		
u = 0.868207 + 0.709119I		
a = -1.316090 + 0.047838I	-8.22620 - 0.36510I	0
b = -0.932909 - 0.593077I		
u = 0.868207 - 0.709119I		
a = -1.316090 - 0.047838I	-8.22620 + 0.36510I	0
b = -0.932909 + 0.593077I		
u = -0.773522 + 0.832238I		
a = -1.388560 + 0.057416I	-11.98240 + 4.46440I	0
b = -1.017760 + 0.654828I		
u = -0.773522 - 0.832238I		
a = -1.388560 - 0.057416I	-11.98240 - 4.46440I	0
b = -1.017760 - 0.654828I		
u = -0.923574 + 0.692893I		
a = 1.084650 + 0.825348I	-3.34148 - 6.33239I	0
b = 0.628177 + 0.990952I		
u = -0.923574 - 0.692893I		
a = 1.084650 - 0.825348I	-3.34148 + 6.33239I	0
b = 0.628177 - 0.990952I		

$\begin{array}{c ccccccccccccccccccccccccccccccccccc$
$\begin{array}{c} b = -0.096809 + 0.216360I \\ \hline u = 0.643430 - 0.541266I \\ a = 0.11958 - 1.53542I \\ b = -0.096809 - 0.216360I \\ \hline u = 0.251058 + 1.133180I \\ a = -1.05747 + 0.95104I \\ u = 0.251058 - 1.133180I \\ a = -0.431302 - 1.095140I \\ \hline u = 0.251058 - 1.133180I \\ a = -1.05747 - 0.95104I \\ a = -0.431302 + 1.095140I \\ \hline u = 0.680178 + 0.965059I \\ \hline \end{array}  \begin{array}{c} b = -0.431302 + 1.095140I \\ \hline u = 0.680178 + 0.965059I \\ \hline \end{array}$
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$
$\begin{array}{c} b = -0.096809 - 0.216360I \\ \hline u = 0.251058 + 1.133180I \\ a = -1.05747 + 0.95104I & 4.59696 - 6.09538I & 0 \\ b = -0.431302 - 1.095140I \\ \hline u = 0.251058 - 1.133180I \\ a = -1.05747 - 0.95104I & 4.59696 + 6.09538I & 0 \\ \hline b = -0.431302 + 1.095140I \\ \hline u = 0.680178 + 0.965059I & & \\ \hline \end{array}$
$\begin{array}{c} u = & 0.251058 + 1.133180I \\ a = -1.05747 + 0.95104I & 4.59696 - 6.09538I & 0 \\ b = -0.431302 - 1.095140I & \\ u = & 0.251058 - 1.133180I \\ a = -1.05747 - 0.95104I & 4.59696 + 6.09538I & 0 \\ b = -0.431302 + 1.095140I & \\ u = & 0.680178 + 0.965059I & \\ \end{array}$
$\begin{array}{c} a = -1.05747 + 0.95104I & 4.59696 - 6.09538I & 0 \\ \underline{b} = -0.431302 - 1.095140I & \\ \overline{u} = & 0.251058 - 1.133180I \\ a = -1.05747 - 0.95104I & 4.59696 + 6.09538I & 0 \\ \underline{b} = -0.431302 + 1.095140I & \\ \overline{u} = & 0.680178 + 0.965059I & \\ \end{array}$
$\begin{array}{c} b = -0.431302 - 1.095140I \\ \hline u = 0.251058 - 1.133180I \\ a = -1.05747 - 0.95104I & 4.59696 + 6.09538I & 0 \\ \hline b = -0.431302 + 1.095140I \\ \hline u = 0.680178 + 0.965059I & \end{array}$
$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$
b = -0.431302 + 1.095140I $u = 0.680178 + 0.965059I$
u = 0.680178 + 0.965059I
0.00174 1.011791 0.00000 7.00001
a = 2.06174 - 1.01173I    -9.95050 - 7.53602I     0
b = 0.733930 + 1.124350I
u = 0.680178 - 0.965059I
a = 2.06174 + 1.01173I -9.95050 + 7.53602I 0
b = 0.733930 - 1.124350I
u = -0.760147 + 0.919939I
$a = 0.363285 + 1.114770I \mid -11.71740 + 1.32226I \mid 0$
b = 0.972224 + 0.550351I
u = -0.760147 - 0.919939I
$a = 0.363285 - 1.114770I \mid -11.71740 - 1.32226I \mid 0$
b = 0.972224 - 0.550351I
u = 0.785310 + 0.041797I
a = 1.032650 - 0.688989I $0.75306 + 2.46584I$ $1.27659 - 6.33944I$
b = 0.336202 - 0.946046I
u = 0.785310 - 0.041797I
$a = 1.032650 + 0.688989I \mid 0.75306 - 2.46584I \mid 1.27659 + 6.33944I$
b = 0.336202 + 0.946046I

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
u = 0.669060 + 1.015260I		
a = -2.02541 + 0.47750I	0.81052 - 7.48437I	0
b = -0.619534 - 1.034680I		
u = 0.669060 - 1.015260I		
a = -2.02541 - 0.47750I	0.81052 + 7.48437I	0
b = -0.619534 + 1.034680I		
u = -0.602047 + 1.071410I		
a = 0.540817 + 0.305119I	1.71998 + 5.88464I	0
b = -0.091548 - 1.090250I		
u = -0.602047 - 1.071410I		
a = 0.540817 - 0.305119I	1.71998 - 5.88464I	0
b = -0.091548 + 1.090250I		
u = -0.962055 + 0.769007I		
a = -1.407370 - 0.115629I	-11.46460 - 4.27058I	0
b = -0.982890 + 0.515422I		
u = -0.962055 - 0.769007I		
a = -1.407370 + 0.115629I	-11.46460 + 4.27058I	0
b = -0.982890 - 0.515422I		
u = 1.018000 + 0.713154I		
a = -0.877403 + 0.545175I	-9.5271 + 10.4754I	0
b = -0.723054 + 1.145040I		
u = 1.018000 - 0.713154I		
a = -0.877403 - 0.545175I	-9.5271 - 10.4754I	0
b = -0.723054 - 1.145040I		
u = -0.322053 + 1.215640I		
a = -0.289638 - 0.522660I	-0.063900 - 0.320410I	0
b = 0.510459 + 0.750000I		
u = -0.322053 - 1.215640I		
a = -0.289638 + 0.522660I	-0.063900 + 0.320410I	0
b = 0.510459 - 0.750000I		

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
u = 0.757308 + 1.014150I		
a = 0.521716 - 0.835498I	-7.29295 - 5.66257I	0
b = 0.980452 - 0.466162I		
u = 0.757308 - 1.014150I		
a = 0.521716 + 0.835498I	-7.29295 + 5.66257I	0
b = 0.980452 + 0.466162I		
u = 0.141074 + 1.267450I		
a = 0.314381 - 1.040930I	0.71079 - 3.98529I	0
b = 0.549097 + 0.971551I		
u = 0.141074 - 1.267450I		
a = 0.314381 + 1.040930I	0.71079 + 3.98529I	0
b = 0.549097 - 0.971551I		
u = -0.257906 + 0.673206I		
a = 0.875017 - 0.842641I	-0.25584 + 1.43316I	-2.89373 - 4.25664I
b = 0.362715 - 0.412513I		
u = -0.257906 - 0.673206I		
a = 0.875017 + 0.842641I	-0.25584 - 1.43316I	-2.89373 + 4.25664I
b = 0.362715 + 0.412513I		
u = 0.512625 + 1.186330I		
a = -0.180598 + 0.307148I	-1.73996 - 5.08791I	0
b = 0.462194 - 0.608975I		
u = 0.512625 - 1.186330I		
a = -0.180598 - 0.307148I	-1.73996 + 5.08791I	0
b = 0.462194 + 0.608975I		
u = -0.766224 + 1.056700I		
a = -2.02146 - 0.26151I	-2.19593 + 12.55800I	0
b = -0.666344 + 1.052100I		
u = -0.766224 - 1.056700I		
a = -2.02146 + 0.26151I	-2.19593 - 12.55800I	0
b = -0.666344 - 1.052100I		

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
u = -0.334080 + 1.262000I		
a = 0.739927 + 1.023500I	-0.23035 + 9.53465I	0
b = 0.574354 - 1.047070I		
u = -0.334080 - 1.262000I		
a = 0.739927 - 1.023500I	-0.23035 - 9.53465I	0
b = 0.574354 + 1.047070I		
u = -0.726282 + 1.091930I		
a = 1.77788 + 0.71191I	-5.15120 + 11.77850I	0
b = 0.700817 - 1.164010I		
u = -0.726282 - 1.091930I		
a = 1.77788 - 0.71191I	-5.15120 - 11.77850I	0
b = 0.700817 + 1.164010I		
u = -0.817220 + 1.044540I		
a = 0.714742 + 0.868490I	-10.5690 + 10.7948I	0
b = 1.041650 + 0.454586I		
u = -0.817220 - 1.044540I		
a = 0.714742 - 0.868490I	-10.5690 - 10.7948I	0
b = 1.041650 - 0.454586I		
u = 0.810773 + 1.098430I		
a = 1.85420 - 0.50706I	-8.2766 - 17.1352I	0
b = 0.716271 + 1.194250I		
u = 0.810773 - 1.098430I		
a = 1.85420 + 0.50706I	-8.2766 + 17.1352I	0
b = 0.716271 - 1.194250I		
u = -0.189049 + 0.597095I		
a = 2.34091 + 2.24975I	-0.892082 - 1.083450I	4.37786 - 0.74207I
b = -0.233253 - 0.857584I		
u = -0.189049 - 0.597095I		
a = 2.34091 - 2.24975I	-0.892082 + 1.083450I	4.37786 + 0.74207I
b = -0.233253 + 0.857584I		

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
u = -0.022832 + 0.605905I		
a = 1.015490 - 0.770054I	-0.20066 + 1.45515I	-0.46303 - 4.13714I
b = 0.451799 - 0.569597I		
u = -0.022832 - 0.605905I		
a = 1.015490 + 0.770054I	-0.20066 - 1.45515I	-0.46303 + 4.13714I
b = 0.451799 + 0.569597I		
u = 0.057884 + 0.497232I		
a = -1.161350 - 0.318274I	-8.05648 - 3.30418I	5.21911 + 6.27707I
b = -0.901151 - 0.915137I		
u = 0.057884 - 0.497232I		
a = -1.161350 + 0.318274I	-8.05648 + 3.30418I	5.21911 - 6.27707I
b = -0.901151 + 0.915137I		

II. 
$$I_2^u = \langle 12u^8a^2 - 12u^8 + \dots - 283a - 196, \ 2u^8a^2 + 5u^8a + \dots + 9a - 20, \ u^9 - u^8 + 2u^7 - u^6 + 3u^5 - u^4 + 2u^3 + u + 1 \rangle$$

$$a_{4} = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_{8} = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{9} = \begin{pmatrix} 1 \\ u^{2} \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} u^{2} + 1 \\ u^{2} \end{pmatrix}$$

$$a_{3} = \begin{pmatrix} u \\ u^{3} + u \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} 0.0424028a^{2}u^{8} + 0.0424028u^{8} + \dots + a + 0.692580 \end{pmatrix}$$

$$a_{7} = \begin{pmatrix} 0.0424028a^{2}u^{8} - 0.0424028u^{8} + \dots - 0.307420a^{2} + 1.30742 \end{pmatrix}$$

$$a_{1} = \begin{pmatrix} u^{2} + 1 \\ u^{2} \end{pmatrix}$$

$$a_{2} = \begin{pmatrix} u^{6} + u^{4} + 2u^{2} + 1 \\ u^{8} + 2u^{6} + 2u^{4} + 2u^{2} \end{pmatrix}$$

$$a_{6} = \begin{pmatrix} 0.0848057a^{2}u^{8} - 0.0848057u^{8} + \dots - 0.614841a^{2} + 2.61484 \\ 0.127208a^{2}u^{8} - 0.127208u^{8} + \dots - a + 1.92226 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 0.0424028a^{2}u^{8} - 0.0424028u^{8} + \dots + 2a - 0.692580 \\ 0.0424028a^{2}u^{8} - 0.0424028u^{8} + \dots + 2a + 1.30742 \end{pmatrix}$$

$$a_{5} = \begin{pmatrix} u^{4} + u^{2} + 1 \\ u^{4} \end{pmatrix}$$

- (ii) Obstruction class = -1
- (iii) Cusp Shapes =  $4u^7 4u^6 + 4u^5 4u^4 + 8u^3 4u^2 6$

Crossings	u-Polynomials at each crossing
$c_1$	$(u^9 + 5u^8 + 12u^7 + 15u^6 + 9u^5 - u^4 - 4u^3 - 2u^2 + u + 1)^3$
$c_{2}, c_{4}$	$(u^9 - u^8 - 2u^7 + 3u^6 + u^5 - 3u^4 + 2u^3 - u + 1)^3$
$c_{3}, c_{8}$	$(u^9 - u^8 + 2u^7 - u^6 + 3u^5 - u^4 + 2u^3 + u + 1)^3$
$c_5, c_6, c_7 \\ c_{10}, c_{12}$	$u^{27} + 9u^{25} + \dots + u + 1$
$c_9$	$(u^9 - 3u^8 + 8u^7 - 13u^6 + 17u^5 - 17u^4 + 12u^3 - 6u^2 + u + 1)^3$
$c_{11}$	$u^{27} - 18u^{26} + \dots + 13u + 1$

Crossings	Riley Polynomials at each crossing
$c_1$	$(y^9 - y^8 + 12y^7 - 7y^6 + 37y^5 + y^4 - 10y^2 + 5y - 1)^3$
$c_2, c_4$	$(y^9 - 5y^8 + 12y^7 - 15y^6 + 9y^5 + y^4 - 4y^3 + 2y^2 + y - 1)^3$
$c_3, c_8$	$(y^9 + 3y^8 + 8y^7 + 13y^6 + 17y^5 + 17y^4 + 12y^3 + 6y^2 + y - 1)^3$
$c_5, c_6, c_7 \\ c_{10}, c_{12}$	$y^{27} + 18y^{26} + \dots + 13y - 1$
<i>c</i> <sub>9</sub>	$(y^9 + 7y^8 + 20y^7 + 25y^6 + 5y^5 - 15y^4 + 22y^2 + 13y - 1)^3$
$c_{11}$	$y^{27} - 18y^{26} + \dots + 265y - 1$

Solutions to $I_2^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
u = -0.140343 + 0.966856I		
a = 0.824898 - 1.007270I	1.78344 + 2.09337I	0.51499 - 4.16283I
b = 0.277934 + 1.206900I		
u = -0.140343 + 0.966856I		
a = -0.429022 - 0.227708I	1.78344 + 2.09337I	0.51499 - 4.16283I
b = -0.658031 - 0.118772I		
u = -0.140343 + 0.966856I		
a = 1.61297 + 0.63923I	1.78344 + 2.09337I	0.51499 - 4.16283I
b = 0.380097 - 1.088130I		
u = -0.140343 - 0.966856I		
a = 0.824898 + 1.007270I	1.78344 - 2.09337I	0.51499 + 4.16283I
b = 0.277934 - 1.206900I		
u = -0.140343 - 0.966856I		
a = -0.429022 + 0.227708I	1.78344 - 2.09337I	0.51499 + 4.16283I
b = -0.658031 + 0.118772I		
u = -0.140343 - 0.966856I		
a = 1.61297 - 0.63923I	1.78344 - 2.09337I	0.51499 + 4.16283I
b = 0.380097 + 1.088130I		
u = -0.628449 + 0.875112I		
a = -0.725227 - 0.503645I	-0.61694 + 2.45442I	-2.32792 - 2.91298I
b = 0.082565 + 1.353850I		
u = -0.628449 + 0.875112I		
a = -0.666708 - 1.013420I	-0.61694 + 2.45442I	-2.32792 - 2.91298I
b = -0.663930 - 0.542279I		
u = -0.628449 + 0.875112I		
a = 1.94244 - 0.11561I	-0.61694 + 2.45442I	-2.32792 - 2.91298I
b = 0.581364 - 0.811567I		
u = -0.628449 - 0.875112I		
a = -0.725227 + 0.503645I	-0.61694 - 2.45442I	-2.32792 + 2.91298I
b = 0.082565 - 1.353850I		

Solutions to $I_2^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
u = -0.628449 - 0.875112I		
a = -0.666708 + 1.013420I	-0.61694 - 2.45442I	-2.32792 + 2.91298I
b = -0.663930 + 0.542279I		
u = -0.628449 - 0.875112I		
a = 1.94244 + 0.11561I	-0.61694 - 2.45442I	-2.32792 + 2.91298I
b = 0.581364 + 0.811567I		
u = 0.796005 + 0.733148I		
a = -1.263760 + 0.143919I	-4.37135 + 1.33617I	-7.28409 - 0.70175I
b = -0.021021 - 1.362970I		
u = 0.796005 + 0.733148I		
a = -0.81256 + 1.34091I	-4.37135 + 1.33617I	-7.28409 - 0.70175I
b = -0.617263 + 0.715712I		
u = 0.796005 + 0.733148I		
a = 1.93616 + 0.21716I	-4.37135 + 1.33617I	-7.28409 - 0.70175I
b = 0.638283 + 0.647255I		
u = 0.796005 - 0.733148I		
a = -1.263760 - 0.143919I	-4.37135 - 1.33617I	-7.28409 + 0.70175I
b = -0.021021 + 1.362970I		
u = 0.796005 - 0.733148I		
a = -0.81256 - 1.34091I	-4.37135 - 1.33617I	-7.28409 + 0.70175I
b = -0.617263 - 0.715712I		
u = 0.796005 - 0.733148I		
a = 1.93616 - 0.21716I	-4.37135 - 1.33617I	-7.28409 + 0.70175I
b = 0.638283 - 0.647255I		
u = 0.728966 + 0.986295I		
a = -0.877277 + 0.977536I	-3.59813 - 7.08493I	-5.57680 + 5.91335I
b = -0.774180 + 0.585725I		
u = 0.728966 + 0.986295I		
a = -0.598365 + 0.132184I	-3.59813 - 7.08493I	-5.57680 + 5.91335I
b = 0.08677 - 1.42529I		

Solutions to $I_2^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
u = 0.728966 + 0.986295I		
a = 1.86581 + 0.16138I	-3.59813 - 7.08493I	-5.57680 + 5.91335I
b = 0.687410 + 0.839570I		
u = 0.728966 - 0.986295I		
a = -0.877277 - 0.977536I	-3.59813 + 7.08493I	-5.57680 - 5.91335I
b = -0.774180 - 0.585725I		
u = 0.728966 - 0.986295I		
a = -0.598365 - 0.132184I	-3.59813 + 7.08493I	-5.57680 - 5.91335I
b = 0.08677 + 1.42529I		
u = 0.728966 - 0.986295I		
a = 1.86581 - 0.16138I	-3.59813 + 7.08493I	-5.57680 - 5.91335I
b = 0.687410 - 0.839570I		
u = -0.512358		
a = 1.42282	-1.19845	-8.65230
b = 0.247373		
u = -0.512358		
a = -4.52078 + 3.95478I	-1.19845	-8.65230
b = -0.123686 + 1.022690I		
u = -0.512358		
a = -4.52078 - 3.95478I	-1.19845	-8.65230
b = -0.123686 - 1.022690I		

$$\begin{array}{l} \text{III. } I_3^u = \langle u^{11} + 2u^9 + 2u^7 - u^3 + b, \ -u^{10} + u^9 + \dots + a - 1, \ u^{12} + 3u^{10} + \\ 5u^8 + 4u^6 + 2u^4 + u^2 + 1 \rangle \end{array}$$

$$a_{4} = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_{8} = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{9} = \begin{pmatrix} 1 \\ u^{2} \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} u^{2} + 1 \\ u^{2} \end{pmatrix}$$

$$a_{3} = \begin{pmatrix} u \\ u^{3} + u \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} u^{10} - u^{9} + 3u^{8} - 2u^{7} + 5u^{6} - 2u^{5} + 4u^{4} + 2u^{2} + u + 1 \\ -u^{11} - 2u^{9} - 2u^{7} + u^{3} \end{pmatrix}$$

$$a_{7} = \begin{pmatrix} -u^{10} - u^{9} - 3u^{8} - 2u^{7} - 5u^{6} - 2u^{5} - 4u^{4} - 2u^{2} + u \\ 1 \end{pmatrix}$$

$$a_{1} = \begin{pmatrix} u^{11} + 2u^{9} + 2u^{7} - u^{3} \\ 0 \end{pmatrix}$$

$$a_{2} = \begin{pmatrix} -u^{7} - 2u^{5} - 2u^{3} \\ -u^{7} - u^{5} + u \end{pmatrix}$$

$$a_{6} = \begin{pmatrix} -u^{10} - 3u^{8} - 5u^{6} + u^{5} - 4u^{4} + 2u^{3} - 2u^{2} + 2u \\ u^{11} + 3u^{9} + 4u^{7} + 3u^{5} + u^{3} + u + 1 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} -u^{11} + u^{10} - 3u^{9} + 3u^{8} - 4u^{7} + 5u^{6} - 2u^{5} + 4u^{4} + u^{3} + 2u^{2} + u + 1 \\ -u^{11} - 2u^{9} - 2u^{7} + u^{3} \end{pmatrix}$$

$$a_{5} = \begin{pmatrix} u^{9} + 2u^{7} + 3u^{5} + 2u^{3} + u \\ u^{11} + 3u^{9} + 4u^{7} + 3u^{5} + u^{3} + u \end{pmatrix}$$

- (ii) Obstruction class = 1
- (iii) Cusp Shapes =  $4u^{10} + 12u^8 + 16u^6 + 8u^4$

Crossings	u-Polynomials at each crossing
$c_1, c_9$	$(u^6 - 3u^5 + 5u^4 - 4u^3 + 2u^2 - u + 1)^2$
$c_2$	$(u^6 + u^5 - u^4 - 2u^3 + u + 1)^2$
$c_3,c_8$	$u^{12} + 3u^{10} + 5u^8 + 4u^6 + 2u^4 + u^2 + 1$
C4	$(u^6 - u^5 - u^4 + 2u^3 - u + 1)^2$
$c_5, c_6, c_7$ $c_{10}, c_{12}$	$(u^2+1)^6$
$c_{11}$	$(u+1)^{12}$

Crossings	Riley Polynomials at each crossing
$c_1, c_9$	$(y^6 + y^5 + 5y^4 + 6y^2 + 3y + 1)^2$
$c_2, c_4$	$(y^6 - 3y^5 + 5y^4 - 4y^3 + 2y^2 - y + 1)^2$
$c_3, c_8$	$(y^6 + 3y^5 + 5y^4 + 4y^3 + 2y^2 + y + 1)^2$
$c_5, c_6, c_7 \\ c_{10}, c_{12}$	$(y+1)^{12}$
$c_{11}$	$(y-1)^{12}$

Solutions to $I_3^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
u = 0.295542 + 1.002190I		
a = 0.272397 + 1.266420I	1.89061 - 0.92430I	1.71672 + 0.79423I
b = -1.000000I		
u = 0.295542 - 1.002190I		
a = 0.272397 - 1.266420I	1.89061 + 0.92430I	1.71672 - 0.79423I
b = 1.000000I		
u = -0.295542 + 1.002190I		
a = 1.266420 + 0.272397I	1.89061 + 0.92430I	1.71672 - 0.79423I
b = -1.000000I		
u = -0.295542 - 1.002190I		
a = 1.266420 - 0.272397I	1.89061 - 0.92430I	1.71672 + 0.79423I
b = 1.000000I		
u = 0.664531 + 0.428243I		
a = 0.79605 + 2.11811I	-1.89061 + 0.92430I	-5.71672 - 0.79423I
b = 1.000000I		
u = 0.664531 - 0.428243I		
a = 0.79605 - 2.11811I	-1.89061 - 0.92430I	-5.71672 + 0.79423I
b = -1.000000I		
u = -0.664531 + 0.428243I		
a = -2.11811 - 0.79605I	-1.89061 - 0.92430I	-5.71672 + 0.79423I
b = 1.000000I		
u = -0.664531 - 0.428243I		
a = -2.11811 + 0.79605I	-1.89061 + 0.92430I	-5.71672 - 0.79423I
b = -1.000000I		
u = 0.558752 + 1.073950I		
a = 0.950374 + 0.167130I	-5.69302I	-2.00000 + 5.51057I
b = 1.000000I		
u = 0.558752 - 1.073950I		
a = 0.950374 - 0.167130I	5.69302I	-2.00000 - 5.51057I
b = -1.000000I		

Solutions to $I_3^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
u = -0.558752 + 1.073950I		
a = -0.167130 - 0.950374I	5.69302I	-2.00000 - 5.51057I
b = 1.000000I		
u = -0.558752 - 1.073950I		
a = -0.167130 + 0.950374I	-5.69302I	-2.00000 + 5.51057I
b = -1.000000I		

IV. 
$$I_1^v = \langle a, -2v^3 + 3v^2 + 4b - 8v + 3, 2v^4 - v^3 + 5v^2 + v + 1 \rangle$$

$$a_{4} = \begin{pmatrix} v \\ 0 \end{pmatrix}$$

$$a_{8} = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{9} = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} 0 \\ \frac{1}{2}v^{3} - \frac{3}{4}v^{2} + 2v - \frac{3}{4} \end{pmatrix}$$

$$a_{7} = \begin{pmatrix} \frac{3}{2}v^{3} - \frac{5}{4}v^{2} + \frac{7}{2}v + \frac{1}{4} \end{pmatrix}$$

$$a_{1} = \begin{pmatrix} -\frac{1}{2}v^{3} + \frac{3}{4}v^{2} - 2v + \frac{3}{4} \\ 2v^{3} - v^{2} + 5v + 1 \end{pmatrix}$$

$$a_{2} = \begin{pmatrix} -\frac{1}{2}v^{3} + \frac{3}{4}v^{2} - v + \frac{3}{4} \\ 2v^{3} - v^{2} + 5v + 1 \end{pmatrix}$$

$$a_{6} = \begin{pmatrix} -\frac{3}{2}v^{3} + \frac{5}{4}v^{2} - \frac{7}{2}v + \frac{3}{4} \\ \frac{3}{2}v^{3} - \frac{5}{4}v^{2} + \frac{7}{2}v + \frac{1}{4} \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} -\frac{3}{2}v^{3} + \frac{1}{4}v^{2} - 3v - \frac{7}{4} \\ v^{2} - \frac{1}{2}v + \frac{5}{2} \end{pmatrix}$$

$$a_{5} = \begin{pmatrix} \frac{1}{2}v^{3} - \frac{3}{4}v^{2} + 2v - \frac{3}{4} \\ -2v^{3} + v^{2} - 5v - 1 \end{pmatrix}$$

- (ii) Obstruction class = 1
- (iii) Cusp Shapes =  $-2v^3 14$

Crossings	u-Polynomials at each crossing
$c_1, c_2$	$(u-1)^4$
$c_3,c_8,c_9$	$u^4$
$c_4$	$(u+1)^4$
$c_5, c_6, c_{11}$	$u^4 + u^3 + 3u^2 + 2u + 1$
	$u^4 + u^3 + u^2 + 1$
$c_{10}$	$u^4 - u^3 + 3u^2 - 2u + 1$
$c_{12}$	$u^4 - u^3 + u^2 + 1$

Crossings	Riley Polynomials at each crossing
$c_1, c_2, c_4$	$(y-1)^4$
$c_3, c_8, c_9$	$y^4$
$c_5, c_6, c_{10}$ $c_{11}$	$y^4 + 5y^3 + 7y^2 + 2y + 1$
$c_7, c_{12}$	$y^4 + y^3 + 3y^2 + 2y + 1$

Solutions to $I_1^v$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
v = -0.130534 + 0.427872I		
a = 0	-8.43568 + 3.16396I	-14.13894 + 0.11292I
b = -0.851808 + 0.911292I		
v = -0.130534 - 0.427872I		
a = 0	-8.43568 - 3.16396I	-14.13894 - 0.11292I
b = -0.851808 - 0.911292I		
v = 0.38053 + 1.53420I		
a = 0	-1.43393 - 1.41510I	-8.73606 + 5.88934I
b = 0.351808 + 0.720342I		
v = 0.38053 - 1.53420I		
a = 0	-1.43393 + 1.41510I	-8.73606 - 5.88934I
b = 0.351808 - 0.720342I		

## V. u-Polynomials

Crossings	u-Polynomials at each crossing
$c_1$	$(u-1)^{4}(u^{6} - 3u^{5} + 5u^{4} - 4u^{3} + 2u^{2} - u + 1)^{2}$ $\cdot (u^{9} + 5u^{8} + 12u^{7} + 15u^{6} + 9u^{5} - u^{4} - 4u^{3} - 2u^{2} + u + 1)^{3}$ $\cdot (u^{74} + 40u^{73} + \dots + 177u + 16)$
$c_2$	$(u-1)^{4}(u^{6} + u^{5} - u^{4} - 2u^{3} + u + 1)^{2}$ $\cdot (u^{9} - u^{8} - 2u^{7} + 3u^{6} + u^{5} - 3u^{4} + 2u^{3} - u + 1)^{3}$ $\cdot (u^{74} - 4u^{73} + \dots - 35u + 4)$
$c_3, c_8$	$u^{4}(u^{9} - u^{8} + 2u^{7} - u^{6} + 3u^{5} - u^{4} + 2u^{3} + u + 1)^{3}$ $\cdot (u^{12} + 3u^{10} + \dots + u^{2} + 1)(u^{74} + 2u^{73} + \dots + 16u + 64)$
$c_4$	$(u+1)^4(u^6 - u^5 - u^4 + 2u^3 - u + 1)^2$ $\cdot (u^9 - u^8 - 2u^7 + 3u^6 + u^5 - 3u^4 + 2u^3 - u + 1)^3$ $\cdot (u^{74} - 4u^{73} + \dots - 35u + 4)$
$c_5, c_6$	$((u^{2}+1)^{6})(u^{4}+u^{3}+3u^{2}+2u+1)(u^{27}+9u^{25}+\cdots+u+1)$ $\cdot (u^{74}+2u^{73}+\cdots+78u+9)$
$c_7$	$((u^{2}+1)^{6})(u^{4}+u^{3}+u^{2}+1)(u^{27}+9u^{25}+\cdots+u+1)$ $\cdot (u^{74}+2u^{73}+\cdots+54u+9)$
<i>c</i> <sub>9</sub>	$u^{4}(u^{6} - 3u^{5} + 5u^{4} - 4u^{3} + 2u^{2} - u + 1)^{2}$ $\cdot (u^{9} - 3u^{8} + 8u^{7} - 13u^{6} + 17u^{5} - 17u^{4} + 12u^{3} - 6u^{2} + u + 1)^{3}$ $\cdot (u^{74} - 24u^{73} + \dots - 103168u + 4096)$
$c_{10}$	$((u^{2}+1)^{6})(u^{4}-u^{3}+3u^{2}-2u+1)(u^{27}+9u^{25}+\cdots+u+1)$ $\cdot (u^{74}+2u^{73}+\cdots+78u+9)$
$c_{11}$	$((u+1)^{12})(u^4 + u^3 + 3u^2 + 2u + 1)(u^{27} - 18u^{26} + \dots + 13u + 1)$ $\cdot (u^{74} - 26u^{73} + \dots - 2880u + 81)$
$c_{12}$	$((u^{2}+1)^{6})(u^{4}-u^{3}+u^{2}+1)(u^{27}+9u^{25}+\cdots+u+1)$ $\cdot (u^{74}+2u^{73}+\cdots+54u+9)$

## VI. Riley Polynomials

Crossings	Riley Polynomials at each crossing
$c_1$	$(y-1)^4(y^6+y^5+5y^4+6y^2+3y+1)^2$ $\cdot (y^9-y^8+12y^7-7y^6+37y^5+y^4-10y^2+5y-1)^3$ $\cdot (y^{74}-8y^{73}+\cdots-5953y+256)$
$c_2, c_4$	$(y-1)^{4}(y^{6} - 3y^{5} + 5y^{4} - 4y^{3} + 2y^{2} - y + 1)^{2}$ $\cdot (y^{9} - 5y^{8} + 12y^{7} - 15y^{6} + 9y^{5} + y^{4} - 4y^{3} + 2y^{2} + y - 1)^{3}$ $\cdot (y^{74} - 40y^{73} + \dots - 177y + 16)$
$c_3, c_8$	$y^{4}(y^{6} + 3y^{5} + 5y^{4} + 4y^{3} + 2y^{2} + y + 1)^{2}$ $\cdot (y^{9} + 3y^{8} + 8y^{7} + 13y^{6} + 17y^{5} + 17y^{4} + 12y^{3} + 6y^{2} + y - 1)^{3}$ $\cdot (y^{74} + 24y^{73} + \dots + 103168y + 4096)$
$c_5, c_6, c_{10}$	$((y+1)^{12})(y^4 + 5y^3 + \dots + 2y + 1)(y^{27} + 18y^{26} + \dots + 13y - 1)$ $\cdot (y^{74} + 82y^{73} + \dots - 3456y + 81)$
$c_7, c_{12}$	$((y+1)^{12})(y^4+y^3+3y^2+2y+1)(y^{27}+18y^{26}+\cdots+13y-1)$ $\cdot (y^{74}+26y^{73}+\cdots+2880y+81)$
<i>c</i> 9	$y^{4}(y^{6} + y^{5} + 5y^{4} + 6y^{2} + 3y + 1)^{2}$ $\cdot (y^{9} + 7y^{8} + 20y^{7} + 25y^{6} + 5y^{5} - 15y^{4} + 22y^{2} + 13y - 1)^{3}$ $\cdot (y^{74} + 44y^{73} + \dots - 654376960y + 16777216)$
$c_{11}$	$((y-1)^{12})(y^4 + 5y^3 + \dots + 2y + 1)(y^{27} - 18y^{26} + \dots + 265y - 1)$ $\cdot (y^{74} + 58y^{73} + \dots + 591300y + 6561)$