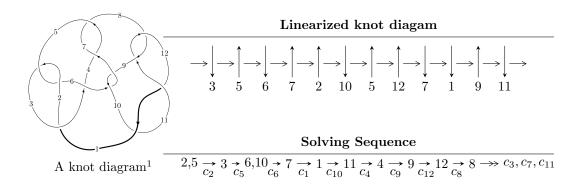
# $12n_{0018} \ (K12n_{0018})$



#### Ideals for irreducible components<sup>2</sup> of $X_{par}$

$$\begin{split} I_1^u &= \langle 2.62383 \times 10^{39} u^{61} - 1.19751 \times 10^{40} u^{60} + \dots + 3.98732 \times 10^{38} b - 9.31049 \times 10^{39}, \\ &- 3.15003 \times 10^{39} u^{61} + 1.51549 \times 10^{40} u^{60} + \dots + 1.99366 \times 10^{38} a + 1.87829 \times 10^{40}, \\ &u^{62} - 5u^{61} + \dots - 19u + 1 \rangle \\ I_2^u &= \langle a^3 u + a^3 - 2a^2 - 3au + b - a + u + 1, \ a^4 + 2a^3 u - 3a^2 u - 3a^2 + a + u, \ u^2 + u + 1 \rangle \end{split}$$

\* 2 irreducible components of  $\dim_{\mathbb{C}} = 0$ , with total 70 representations.

<sup>&</sup>lt;sup>1</sup>The image of knot diagram is generated by the software "**Draw programme**" developed by Andrew Bartholomew(http://www.layer8.co.uk/maths/draw/index.htm#Running-draw), where we modified some parts for our purpose(https://github.com/CATsTAILs/LinksPainter).

<sup>&</sup>lt;sup>2</sup> All coefficients of polynomials are rational numbers. But the coefficients are sometimes approximated in decimal forms when there is not enough margin.

I. 
$$I_1^u = \langle 2.62 \times 10^{39} u^{61} - 1.20 \times 10^{40} u^{60} + \dots + 3.99 \times 10^{38} b - 9.31 \times 10^{39}, \ -3.15 \times 10^{39} u^{61} + 1.52 \times 10^{40} u^{60} + \dots + 1.99 \times 10^{38} a + 1.88 \times 10^{40}, \ u^{62} - 5 u^{61} + \dots - 19 u + 1 \rangle$$

(i) Arc colorings

$$a_{2} = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{5} = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_{6} = \begin{pmatrix} 1 \\ -u^{2} \end{pmatrix}$$

$$a_{6} = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} 15.8002u^{61} - 76.0156u^{60} + \dots + 1227.65u - 94.2130 \\ -6.58044u^{61} + 30.0330u^{60} + \dots - 304.461u + 23.3502 \end{pmatrix}$$

$$a_{7} = \begin{pmatrix} -15.9053u^{61} + 77.9924u^{60} + \dots - 1333.00u + 105.025 \\ 8.30759u^{61} - 33.2844u^{60} + \dots + 178.838u - 14.4250 \end{pmatrix}$$

$$a_{1} = \begin{pmatrix} u^{2} + 1 \\ -u^{4} \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 19.2096u^{61} - 92.8297u^{60} + \dots + 1541.75u - 118.551 \\ -8.39084u^{61} + 37.4877u^{60} + \dots - 309.379u + 23.5628 \end{pmatrix}$$

$$a_{4} = \begin{pmatrix} u^{4} + u^{2} + 1 \\ u^{4} \end{pmatrix}$$

$$a_{9} = \begin{pmatrix} 23.0925u^{61} - 111.738u^{60} + \dots + 1863.68u - 145.752 \\ -10.1051u^{61} + 43.0078u^{60} + \dots - 361.476u + 28.7800 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} 15.5897u^{61} - 75.0040u^{60} + \dots + 1258.28u - 100.587 \\ -1.52637u^{61} + 10.2099u^{60} + \dots + 1333.00u - 105.025 \\ -10.5447u^{61} + 39.2440u^{60} + \dots + 1333.00u - 105.025 \\ -10.5447u^{61} + 39.2440u^{60} + \dots - 192.085u + 15.9594 \end{pmatrix}$$

- (ii) Obstruction class = -1
- (iii) Cusp Shapes =  $32.0809u^{61} 157.631u^{60} + \cdots + 2379.84u 187.341$

#### (iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
$c_1$	$u^{62} + 33u^{61} + \dots - 77u + 1$
$c_2, c_5$	$u^{62} + 5u^{61} + \dots + 19u + 1$
$c_3$	$u^{62} - 5u^{61} + \dots + 28315u + 1921$
$c_4, c_7$	$u^{62} + 5u^{61} + \dots - 1152u + 256$
$c_{6}, c_{9}$	$u^{62} - 3u^{61} + \dots - 3u + 1$
$c_8,c_{11}$	$u^{62} + 3u^{61} + \dots - 5u + 1$
$c_{10}, c_{12}$	$u^{62} + 23u^{61} + \dots + 11u + 1$

## (v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
$c_1$	$y^{62} - 3y^{61} + \dots - 3593y + 1$
$c_2, c_5$	$y^{62} + 33y^{61} + \dots - 77y + 1$
$c_3$	$y^{62} - 39y^{61} + \dots - 237987197y + 3690241$
$c_4, c_7$	$y^{62} + 45y^{61} + \dots + 1261568y + 65536$
$c_{6}, c_{9}$	$y^{62} + 15y^{61} + \dots + 11y + 1$
$c_{8}, c_{11}$	$y^{62} + 23y^{61} + \dots + 11y + 1$
$c_{10}, c_{12}$	$y^{62} + 35y^{61} + \dots - 185y + 1$

# (vi) Complex Volumes and Cusp Shapes

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
u = 0.965704 + 0.297719I		
a = -1.43043 - 0.52995I	-1.29157 - 10.33450I	0
b = -0.306577 + 0.174570I		
u = 0.965704 - 0.297719I		
a = -1.43043 + 0.52995I	-1.29157 + 10.33450I	0
b = -0.306577 - 0.174570I		
u = -0.411885 + 0.945709I		
a = -2.27569 + 1.18972I	-0.55472 - 4.37820I	0
b = -1.71285 + 1.28141I		
u = -0.411885 - 0.945709I		
a = -2.27569 - 1.18972I	-0.55472 + 4.37820I	0
b = -1.71285 - 1.28141I		
u = -0.508605 + 0.906380I		
a = 2.86917 - 1.37868I	-0.017864 - 0.355429I	0
b = 2.47102 - 1.51786I		
u = -0.508605 - 0.906380I		
a = 2.86917 + 1.37868I	-0.017864 + 0.355429I	0
b = 2.47102 + 1.51786I		
u = 0.892742 + 0.303283I		
a = 1.40786 + 0.50551I	0.27929 - 4.71522I	0
b = 0.211520 - 0.223149I		
u = 0.892742 - 0.303283I		
a = 1.40786 - 0.50551I	0.27929 + 4.71522I	0
b = 0.211520 + 0.223149I		
u = -0.930590 + 0.096301I		
a = 0.057491 - 0.985327I	3.48850 - 2.47160I	10.13177 + 3.68218I
b = -0.005994 - 0.189910I		
u = -0.930590 - 0.096301I		
a = 0.057491 + 0.985327I	3.48850 + 2.47160I	10.13177 - 3.68218I
b = -0.005994 + 0.189910I		

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
u = 0.374481 + 0.850793I		
a = -0.743628 + 0.575009I	6.46808 + 4.86140I	0
b = 0.77387 + 1.47048I		
u = 0.374481 - 0.850793I		
a = -0.743628 - 0.575009I	6.46808 - 4.86140I	0
b = 0.77387 - 1.47048I		
u = 0.891739 + 0.124753I		
a = -1.43390 - 0.46536I	-5.82429 - 3.24893I	-2.83073 + 2.56223I
b = -0.330798 + 0.437779I		
u = 0.891739 - 0.124753I		
a = -1.43390 + 0.46536I	-5.82429 + 3.24893I	-2.83073 - 2.56223I
b = -0.330798 - 0.437779I		
u = -0.531933 + 0.965807I		
a = 0.024523 - 1.037090I	-0.14262 - 2.78903I	0
b = 0.21487 - 1.50621I		
u = -0.531933 - 0.965807I		
a = 0.024523 + 1.037090I	-0.14262 + 2.78903I	0
b = 0.21487 + 1.50621I		
u = 0.382543 + 0.801832I		
a = 0.843253 - 0.451303I	6.61497 - 1.56581I	0. + 8.95092I
b = -0.78761 - 1.22730I		
u = 0.382543 - 0.801832I		
a = 0.843253 + 0.451303I	6.61497 + 1.56581I	0 8.95092I
b = -0.78761 + 1.22730I		
u = -0.480114 + 0.743056I		
a = 2.00911 - 1.21894I	0.46926 - 3.71058I	-6.23280 + 11.34763I
b = 1.67487 - 1.75063I		
u = -0.480114 - 0.743056I		
a = 2.00911 + 1.21894I	0.46926 + 3.71058I	-6.23280 - 11.34763I
b = 1.67487 + 1.75063I		

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
u = -0.094130 + 0.841210I		
a = -1.51231 + 1.09297I	-1.62196 + 1.23455I	-2.69106 - 2.17099I
b = -0.499665 + 1.237070I		
u = -0.094130 - 0.841210I		
a = -1.51231 - 1.09297I	-1.62196 - 1.23455I	-2.69106 + 2.17099I
b = -0.499665 - 1.237070I		
u = -0.257077 + 1.145650I		
a = -0.587485 + 0.772224I	-3.22451 - 2.34711I	0
b = -0.87373 + 1.43182I		
u = -0.257077 - 1.145650I		
a = -0.587485 - 0.772224I	-3.22451 + 2.34711I	0
b = -0.87373 - 1.43182I		
u = -0.900002 + 0.754167I		
a = 0.124095 - 0.287439I	2.84220 - 0.80883I	0
b = -0.145127 + 0.264679I		
u = -0.900002 - 0.754167I		
a = 0.124095 + 0.287439I	2.84220 + 0.80883I	0
b = -0.145127 - 0.264679I		
u = -0.475785 + 0.628202I		
a = 1.193400 - 0.639563I	0.84056 - 1.37461I	5.29052 + 4.27881I
b = 0.566847 - 0.143962I		
u = -0.475785 - 0.628202I		
a = 1.193400 + 0.639563I	0.84056 + 1.37461I	5.29052 - 4.27881I
b = 0.566847 + 0.143962I		
u = 0.442572 + 1.154760I		
a = 0.043171 + 0.738046I	-3.45908 + 2.42252I	0
b = -0.93124 + 1.40738I		
u = 0.442572 - 1.154760I		
a = 0.043171 - 0.738046I	-3.45908 - 2.42252I	0
b = -0.93124 - 1.40738I		

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
u = 0.745927 + 0.110754I		
a = -1.277990 + 0.457571I	-1.84493 - 3.74840I	0.35274 + 2.59409I
b = -0.255752 - 0.786572I		
u = 0.745927 - 0.110754I		
a = -1.277990 - 0.457571I	-1.84493 + 3.74840I	0.35274 - 2.59409I
b = -0.255752 + 0.786572I		
u = 0.468807 + 1.155530I		
a = -0.152066 + 1.342220I	-3.26706 + 5.72300I	0
b = 0.48466 + 2.34406I		
u = 0.468807 - 1.155530I		
a = -0.152066 - 1.342220I	-3.26706 - 5.72300I	0
b = 0.48466 - 2.34406I		
u = 0.406251 + 1.185420I		
a = 0.29707 - 1.44572I	-5.55349 + 0.20577I	0
b = -0.37469 - 2.34822I		
u = 0.406251 - 1.185420I		
a = 0.29707 + 1.44572I	-5.55349 - 0.20577I	0
b = -0.37469 + 2.34822I		
u = -0.893686 + 0.884980I		
a = 0.0151757 + 0.0943643I	2.47898 - 5.65478I	0
b = 0.275198 - 0.425254I		
u = -0.893686 - 0.884980I		
a = 0.0151757 - 0.0943643I	2.47898 + 5.65478I	0
b = 0.275198 + 0.425254I		
u = 0.236000 + 1.238430I		
a = -0.245273 + 0.777145I	-4.87637 - 1.25419I	0
b = -0.93517 + 1.48259I		
u = 0.236000 - 1.238430I		
a = -0.245273 - 0.777145I	-4.87637 + 1.25419I	0
b = -0.93517 - 1.48259I		

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
u = -0.331100 + 0.640866I		
a = -1.73450 + 0.49909I	0.414871 + 0.997099I	-2.34753 + 0.60698I
b = -1.35558 + 1.35491I		
u = -0.331100 - 0.640866I		
a = -1.73450 - 0.49909I	0.414871 - 0.997099I	-2.34753 - 0.60698I
b = -1.35558 - 1.35491I		
u = 0.493150 + 1.180330I		
a = -0.100543 - 0.798998I	-4.93269 + 8.34798I	0
b = 0.89247 - 1.38242I		
u = 0.493150 - 1.180330I		
a = -0.100543 + 0.798998I	-4.93269 - 8.34798I	0
b = 0.89247 + 1.38242I		
u = -0.576496 + 1.167110I		
a = 0.393868 - 0.624631I	0.37776 - 2.87804I	0
b = 0.650024 - 1.142500I		
u = -0.576496 - 1.167110I		
a = 0.393868 + 0.624631I	0.37776 + 2.87804I	0
b = 0.650024 + 1.142500I		
u = 0.594113 + 1.186310I		
a = 0.175111 + 1.386080I	-2.39832 + 10.17330I	0
b = 0.62258 + 2.42837I		
u = 0.594113 - 1.186310I		
a = 0.175111 - 1.386080I	-2.39832 - 10.17330I	0
b = 0.62258 - 2.42837I		
u = 0.376293 + 1.276620I		
a = 0.095158 - 0.866722I	-10.22650 + 1.13523I	0
b = 0.90036 - 1.47315I		
u = 0.376293 - 1.276620I		
a = 0.095158 + 0.866722I	-10.22650 - 1.13523I	0
b = 0.90036 + 1.47315I		

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
u = 0.524584 + 1.228200I		
a = -0.01293 - 1.50624I	-9.15566 + 8.36279I	0
b = -0.52627 - 2.46501I		
u = 0.524584 - 1.228200I		
a = -0.01293 + 1.50624I	-9.15566 - 8.36279I	0
b = -0.52627 + 2.46501I		
u = 0.217473 + 1.339040I		
a = 0.291562 - 0.877888I	-6.91925 - 6.39307I	0
b = 0.94031 - 1.49949I		
u = 0.217473 - 1.339040I		
a = 0.291562 + 0.877888I	-6.91925 + 6.39307I	0
b = 0.94031 + 1.49949I		
u = 0.616616 + 1.212360I		
a = -0.23484 - 1.44633I	-4.0936 + 16.0686I	0
b = -0.64668 - 2.46160I		
u = 0.616616 - 1.212360I		
a = -0.23484 + 1.44633I	-4.0936 - 16.0686I	0
b = -0.64668 + 2.46160I		
u = -0.506958 + 1.275800I		
a = -0.538448 + 0.655638I	-0.59026 - 7.53314I	0
b = -0.82392 + 1.18632I		
u = -0.506958 - 1.275800I		
a = -0.538448 - 0.655638I	-0.59026 + 7.53314I	0
b = -0.82392 - 1.18632I		
u = 0.616968 + 0.058257I		
a = 1.42943 + 0.57487I	-0.28090 - 1.52056I	2.54136 + 2.72708I
b = 0.066901 - 0.636161I		
u = 0.616968 - 0.058257I		
a = 1.42943 - 0.57487I	-0.28090 + 1.52056I	2.54136 - 2.72708I
b = 0.066901 + 0.636161I		

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
u = 0.152397 + 0.009114I		
a = 3.01058 + 2.43110I	-0.056975 - 1.373480I	-0.36734 + 4.59681I
b = -0.233834 - 0.560896I		
u = 0.152397 - 0.009114I		
a = 3.01058 - 2.43110I	-0.056975 + 1.373480I	-0.36734 - 4.59681I
b = -0.233834 + 0.560896I		

$$II. \\ I_2^u = \langle a^3u + a^3 - 2a^2 - 3au + b - a + u + 1, \ a^4 + 2a^3u - 3a^2u - 3a^2 + a + u, \ u^2 + u + 1 \rangle$$

(i) Arc colorings

$$a_{2} = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{5} = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_{3} = \begin{pmatrix} 1 \\ u+1 \end{pmatrix}$$

$$a_{6} = \begin{pmatrix} u \\ u \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} -a^{3}u - a^{3} + 2a^{2} + 3au + a - u - 1 \end{pmatrix}$$

$$a_{7} = \begin{pmatrix} -a^{3}u - a^{3} + a^{2} + au + 2u + 2 \end{pmatrix}$$

$$a_{1} = \begin{pmatrix} -u \\ -u \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} -a^{3}u + 2a^{2}u + 2a^{2} - 2a - u \\ -2a^{3}u - a^{3} + 2a^{2}u + 4a^{2} + 3au - 2a - 2u - 1 \end{pmatrix}$$

$$a_{4} = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_{9} = \begin{pmatrix} a^{3}u + a^{3} - 3a^{2} - 4au + a + 2u + 2 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} -2a^{3}u - a^{3} + a^{2}u + 2a^{2} + au - a + 2u + 2 \end{pmatrix}$$

$$a_{8} = \begin{pmatrix} 0 \\ -a^{3}u - a^{3} + a^{2}u + 2a^{2} + au - a + 2u + 2 \end{pmatrix}$$

- (ii) Obstruction class = 1
- (iii) Cusp Shapes =  $-a^3u 3a^3 3a^2u + a^2 3a + 9u + 10$

#### (iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
$c_1, c_3, c_5$	$(u^2 - u + 1)^4$
$c_2$	$(u^2+u+1)^4$
$c_4, c_7$	$u^8$
$c_6, c_{10}$	$(u^4 - u^3 + 3u^2 - 2u + 1)^2$
<i>C</i> <sub>8</sub>	$(u^4 - u^3 + u^2 + 1)^2$
$c_9,c_{12}$	$(u^4 + u^3 + 3u^2 + 2u + 1)^2$
$c_{11}$	$(u^4 + u^3 + u^2 + 1)^2$

## (v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
$c_1, c_2, c_3$ $c_5$	$(y^2 + y + 1)^4$
$c_4, c_7$	$y^8$
$c_6, c_9, c_{10}$ $c_{12}$	$(y^4 + 5y^3 + 7y^2 + 2y + 1)^2$
$c_8, c_{11}$	$(y^4 + y^3 + 3y^2 + 2y + 1)^2$

# (vi) Complex Volumes and Cusp Shapes

Solutions to $I_2^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
u = -0.500000 + 0.866025I		
a = 0.576953 + 0.283088I	6.79074 - 5.19385I	8.12668 + 10.02124I
b = -0.819983 + 0.968508I		
u = -0.500000 + 0.866025I		
a = -0.533637 - 0.358112I	6.79074 + 1.13408I	5.34148 + 6.40875I
b = 0.75842 - 1.22518I		
u = -0.500000 + 0.866025I		
a = -0.58443 - 1.44211I	-0.21101 - 3.44499I	-0.01166 + 14.06194I
b = -0.34305 - 2.03771I		
u = -0.500000 + 0.866025I		
a = 1.54112 - 0.21492I	-0.211005 - 0.614778I	-4.95650 + 1.55100I
b = 0.904615 - 0.303685I		
u = -0.500000 - 0.866025I		
a = 0.576953 - 0.283088I	6.79074 + 5.19385I	8.12668 - 10.02124I
b = -0.819983 - 0.968508I		
u = -0.500000 - 0.866025I		
a = -0.533637 + 0.358112I	6.79074 - 1.13408I	5.34148 - 6.40875I
b = 0.75842 + 1.22518I		
u = -0.500000 - 0.866025I		
a = -0.58443 + 1.44211I	-0.21101 + 3.44499I	-0.01166 - 14.06194I
b = -0.34305 + 2.03771I		
u = -0.500000 - 0.866025I		
a = 1.54112 + 0.21492I	-0.211005 + 0.614778I	-4.95650 - 1.55100I
b = 0.904615 + 0.303685I		

## III. u-Polynomials

Crossings	u-Polynomials at each crossing
$c_1$	$((u^2 - u + 1)^4)(u^{62} + 33u^{61} + \dots - 77u + 1)$
$c_2$	$((u^2 + u + 1)^4)(u^{62} + 5u^{61} + \dots + 19u + 1)$
$c_3$	$((u^2 - u + 1)^4)(u^{62} - 5u^{61} + \dots + 28315u + 1921)$
$c_4, c_7$	$u^8(u^{62} + 5u^{61} + \dots - 1152u + 256)$
<i>C</i> <sub>5</sub>	$((u^2 - u + 1)^4)(u^{62} + 5u^{61} + \dots + 19u + 1)$
<i>c</i> <sub>6</sub>	$((u^4 - u^3 + 3u^2 - 2u + 1)^2)(u^{62} - 3u^{61} + \dots - 3u + 1)$
<i>c</i> <sub>8</sub>	$((u^4 - u^3 + u^2 + 1)^2)(u^{62} + 3u^{61} + \dots - 5u + 1)$
$c_9$	$((u^4 + u^3 + 3u^2 + 2u + 1)^2)(u^{62} - 3u^{61} + \dots - 3u + 1)$
$c_{10}$	$((u^4 - u^3 + 3u^2 - 2u + 1)^2)(u^{62} + 23u^{61} + \dots + 11u + 1)$
$c_{11}$	$((u^4 + u^3 + u^2 + 1)^2)(u^{62} + 3u^{61} + \dots - 5u + 1)$
$c_{12}$	$((u4 + u3 + 3u2 + 2u + 1)2)(u62 + 23u61 + \dots + 11u + 1)$

IV. Riley Polynomials

Crossings	Riley Polynomials at each crossing
$c_1$	$((y^2 + y + 1)^4)(y^{62} - 3y^{61} + \dots - 3593y + 1)$
$c_2, c_5$	$((y^2 + y + 1)^4)(y^{62} + 33y^{61} + \dots - 77y + 1)$
$c_3$	$((y^2 + y + 1)^4)(y^{62} - 39y^{61} + \dots - 2.37987 \times 10^8 y + 3690241)$
$c_4, c_7$	$y^8(y^{62} + 45y^{61} + \dots + 1261568y + 65536)$
$c_6, c_9$	$((y^4 + 5y^3 + 7y^2 + 2y + 1)^2)(y^{62} + 15y^{61} + \dots + 11y + 1)$
$c_8, c_{11}$	$((y^4 + y^3 + 3y^2 + 2y + 1)^2)(y^{62} + 23y^{61} + \dots + 11y + 1)$
$c_{10}, c_{12}$	$((y^4 + 5y^3 + 7y^2 + 2y + 1)^2)(y^{62} + 35y^{61} + \dots - 185y + 1)$