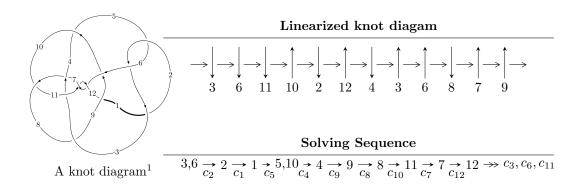
# $12n_{0449} \ (K12n_{0449})$



#### Ideals for irreducible components<sup>2</sup> of $X_{par}$

$$\begin{split} I_1^u &= \langle -4292389719u^{17} + 51152895286u^{16} + \dots + 4997872592b - 142666014976, \\ & 635549962u^{17} - 7071211853u^{16} + \dots + 4997872592a + 18555030320, \\ & u^{18} - 14u^{17} + \dots - 32u - 64 \rangle \\ I_2^u &= \langle 2861u^{12} + 19240u^{11} + \dots + 3447b - 26153, \ -10868u^{12} - 66331u^{11} + \dots + 17235a + 57767, \\ & u^{13} + 7u^{12} + 18u^{11} + 18u^{10} - 5u^9 - 30u^8 - 29u^7 - 5u^6 + 22u^5 + 26u^4 - u^3 - 25u^2 - 19u - 5 \rangle \\ I_3^u &= \langle -48036a^5u^2 - 192549a^4u^2 + \dots - 3719319a - 1942337, \ a^5u^2 - 3a^4u^2 + \dots + 13a + 8, \ u^3 + 2u^2 + 1 \rangle \\ I_4^u &= \langle b^2 + ba + a^2, \ a^3 + a^2 - 1, \ u - 1 \rangle \end{split}$$

\* 4 irreducible components of  $\dim_{\mathbb{C}} = 0$ , with total 55 representations.

<sup>&</sup>lt;sup>1</sup>The image of knot diagram is generated by the software "**Draw programme**" developed by Andrew Bartholomew(http://www.layer8.co.uk/maths/draw/index.htm#Running-draw), where we modified some parts for our purpose(https://github.com/CATsTAILs/LinksPainter).

<sup>&</sup>lt;sup>2</sup> All coefficients of polynomials are rational numbers. But the coefficients are sometimes approximated in decimal forms when there is not enough margin.

I.  $I_1^u = \langle -4.29 \times 10^9 u^{17} + 5.12 \times 10^{10} u^{16} + \dots + 5.00 \times 10^9 b - 1.43 \times 10^{11}, \ 6.36 \times 10^8 u^{17} - 7.07 \times 10^9 u^{16} + \dots + 5.00 \times 10^9 a + 1.86 \times 10^{10}, \ u^{18} - 14 u^{17} + \dots - 32 u - 64 \rangle$ 

(i) Arc colorings

$$a_{3} = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{6} = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_{2} = \begin{pmatrix} 1 \\ -u^{2} \end{pmatrix}$$

$$a_{1} = \begin{pmatrix} -u^{2} + 1 \\ -u^{2} \end{pmatrix}$$

$$a_{5} = \begin{pmatrix} u \\ -u^{3} + u \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} -0.127164u^{17} + 1.41484u^{16} + \dots + 2.40021u - 3.71259 \\ 0.858843u^{17} - 10.2349u^{16} + \dots + 31.2801u + 28.5453 \end{pmatrix}$$

$$a_{4} = \begin{pmatrix} -0.0537381u^{17} + 0.686664u^{16} + \dots - 3.43651u - 1.95932 \\ 0.0261593u^{17} - 0.244759u^{16} + \dots + 4.59772u + 1.60130 \end{pmatrix}$$

$$a_{9} = \begin{pmatrix} -0.127164u^{17} + 1.41484u^{16} + \dots + 2.40021u - 3.71259 \\ -0.0465960u^{17} + 0.240296u^{16} + \dots + 11.4471u + 5.15636 \end{pmatrix}$$

$$a_{8} = \begin{pmatrix} -0.0805681u^{17} + 1.17455u^{16} + \dots - 9.04691u - 8.86894 \\ -0.0465960u^{17} + 0.240296u^{16} + \dots + 11.4471u + 5.15636 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 0.161781u^{17} - 1.96128u^{16} + \dots + 9.04249u + 3.48865 \\ 0.189746u^{17} - 2.43818u^{16} + \dots + 14.8327u + 10.0529 \end{pmatrix}$$

$$a_{7} = \begin{pmatrix} 0.119990u^{17} - 1.53654u^{16} + \dots + 8.62391u + 4.68769 \\ 0.458477u^{17} - 5.52095u^{16} + \dots + 15.8725u + 14.8725 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} 0.0119305u^{17} - 0.112150u^{16} + \dots - 0.757572u + 2.47991 \\ 0.0656686u^{17} - 0.798814u^{16} + \dots + 3.67894u + 3.43924 \end{pmatrix}$$

(ii) Obstruction class = -1

(iii) Cusp Shapes = 
$$\frac{336395251}{1249468148}u^{17} - \frac{1919281435}{624734074}u^{16} + \dots - \frac{4336282305}{312367037}u + \frac{1452677222}{312367037}u^{16} + \dots + \frac{145267722}{312367037}u^{16} + \dots + \frac{145267722}{312367037}u^{16} + \dots + \frac{1452677222}{312367037}u^{16} + \dots + \frac{14$$

| Crossings      | u-Polynomials at each crossing              |
|----------------|---|
| $c_1$          | $u^{18} + 44u^{17} + \dots + 58880u + 4096$ |
| $c_{2}, c_{5}$ | $u^{18} + 14u^{17} + \dots + 32u - 64$      |
| $c_{3}, c_{7}$ | $u^{18} + u^{17} + \dots + u + 1$           |
| $c_4, c_8$     | $u^{18} + 15u^{16} + \dots - 2u - 1$        |
| $c_6, c_{11}$  | $u^{18} - 8u^{17} + \dots + 66u^2 - 4$      |
| $c_9,c_{12}$   | $u^{18} + u^{17} + \dots - 29u - 1$         |
| $c_{10}$       | $u^{18} - 17u^{17} + \dots - 112u + 8$      |

| Crossings       | Riley Polynomials at each crossing                    |  |  |
|-----------------|---|--|--|
| $c_1$           | $y^{18} - 180y^{17} + \dots - 1103757312y + 16777216$ |  |  |
| $c_2, c_5$      | $y^{18} - 44y^{17} + \dots - 58880y + 4096$           |  |  |
| $c_3, c_7$      | $y^{18} - 9y^{17} + \dots + 3y + 1$                   |  |  |
| $c_4, c_8$      | $y^{18} + 30y^{17} + \dots - 20y + 1$                 |  |  |
| $c_6, c_{11}$   | $y^{18} + 12y^{17} + \dots - 528y + 16$               |  |  |
| $c_{9}, c_{12}$ | $y^{18} + 43y^{17} + \dots - 425y + 1$                |  |  |
| $c_{10}$        | $y^{18} - 11y^{17} + \dots - 1312y + 64$              |  |  |

| Solutions to $I_1^u$      | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape          |
|---------------------------|---------------------------------------|---------------------|
| u = 0.899219              |                                       |                     |
| a = -0.0543767            | -1.46517                              | -7.81630            |
| b = 0.529143              |                                       |                     |
| u = 1.054770 + 0.455060I  |                                       |                     |
| a = -0.286687 + 0.255744I | -2.44657 - 1.20776I                   | -2.90617 + 2.14647I |
| b = 0.697632 + 0.987067I  |                                       |                     |
| u = 1.054770 - 0.455060I  |                                       |                     |
| a = -0.286687 - 0.255744I | -2.44657 + 1.20776I                   | -2.90617 - 2.14647I |
| b = 0.697632 - 0.987067I  |                                       |                     |
| u = 1.182210 + 0.365563I  |                                       |                     |
| a = -0.196661 - 0.172033I | -4.86247 - 0.74221I                   | -4.48012 - 1.53917I |
| b = -0.688510 + 0.458421I |                                       |                     |
| u = 1.182210 - 0.365563I  |                                       |                     |
| a = -0.196661 + 0.172033I | -4.86247 + 0.74221I                   | -4.48012 + 1.53917I |
| b = -0.688510 - 0.458421I |                                       |                     |
| u = 0.011252 + 0.650614I  |                                       |                     |
| a = 0.249333 + 0.938849I  | -1.41190 - 2.84945I                   | 2.25914 + 3.12009I  |
| b = 0.628633 + 0.554074I  |                                       |                     |
| u = 0.011252 - 0.650614I  |                                       |                     |
| a = 0.249333 - 0.938849I  | -1.41190 + 2.84945I                   | 2.25914 - 3.12009I  |
| b = 0.628633 - 0.554074I  |                                       |                     |
| u = -1.56372              |                                       |                     |
| a = -1.20023              | -1.13784                              | -8.76730            |
| b = 2.20274               |                                       |                     |
| u = -1.57964 + 0.17770I   |                                       |                     |
| a = 1.028070 + 0.171267I  | -5.95294 + 6.24667I                   | -5.65069 - 4.46750I |
| b = -1.99303 + 0.23309I   |                                       |                     |
| u = -1.57964 - 0.17770I   |                                       |                     |
| a = 1.028070 - 0.171267I  | -5.95294 - 6.24667I                   | -5.65069 + 4.46750I |
| b = -1.99303 - 0.23309I   |                                       |                     |

| Solutions to $I_1^u$      | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape          |
|---------------------------|---------------------------------------|---------------------|
| u = -0.337307 + 0.100488I |                                       |                     |
| a = -1.45027 - 1.37394I   | 1.118560 + 0.696320I                  | 7.37877 - 3.46588I  |
| b = -0.205154 - 0.227150I |                                       |                     |
| u = -0.337307 - 0.100488I |                                       |                     |
| a = -1.45027 + 1.37394I   | 1.118560 - 0.696320I                  | 7.37877 + 3.46588I  |
| b = -0.205154 + 0.227150I |                                       |                     |
| u = 2.31673 + 0.16616I    |                                       |                     |
| a = 0.176104 - 1.366420I  | 17.0902 - 12.5383I                    | -5.56236 + 5.19794I |
| b = -1.81352 + 4.75613I   |                                       |                     |
| u = 2.31673 - 0.16616I    |                                       |                     |
| a = 0.176104 + 1.366420I  | 17.0902 + 12.5383I                    | -5.56236 - 5.19794I |
| b = -1.81352 - 4.75613I   |                                       |                     |
| u = 2.30666 + 0.43513I    |                                       |                     |
| a = 0.124162 - 1.296380I  | 18.8942 + 0.4671I                     | -7.70038 + 0.38231I |
| b = -3.32718 + 4.18498I   |                                       |                     |
| u = 2.30666 - 0.43513I    |                                       |                     |
| a = 0.124162 + 1.296380I  | 18.8942 - 0.4671I                     | -7.70038 - 0.38231I |
| b = -3.32718 - 4.18498I   |                                       |                     |
| u = 2.37757 + 0.25374I    |                                       |                     |
| a = -0.141746 + 1.335690I | -17.0153 - 6.5912I                    | -3.54637 + 4.05505I |
| b = 2.33519 - 5.00160I    |                                       |                     |
| u = 2.37757 - 0.25374I    |                                       |                     |
| a = -0.141746 - 1.335690I | -17.0153 + 6.5912I                    | -3.54637 - 4.05505I |
| b = 2.33519 + 5.00160I    |                                       |                     |

II. 
$$I_2^u = \langle 2861u^{12} + 19240u^{11} + \dots + 3447b - 26153, -10868u^{12} - 66331u^{11} + \dots + 17235a + 57767, u^{13} + 7u^{12} + \dots - 19u - 5 \rangle$$

(i) Arc colorings

$$a_{3} = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{6} = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_{2} = \begin{pmatrix} -u^{2} + 1 \\ -u^{2} \end{pmatrix}$$

$$a_{5} = \begin{pmatrix} 0 \\ -u^{3} + u \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} 0.630577u^{12} + 3.84862u^{11} + \cdots + 10.2507u - 3.35173 \\ -0.829997u^{12} - 5.58167u^{11} + \cdots + 17.5666u + 7.58718 \end{pmatrix}$$

$$a_{4} = \begin{pmatrix} -0.00765883u^{12} - 0.137163u^{11} + \cdots + 1.89643u - 0.681288 \\ 0.0478677u^{12} + 0.190601u^{11} + \cdots + 1.76936u - 0.908616 \end{pmatrix}$$

$$a_{9} = \begin{pmatrix} 0.630577u^{12} + 3.84862u^{11} + \cdots + 10.2507u - 3.35173 \\ -0.321439u^{12} - 2.49405u^{11} + \cdots + 9.97650u + 4.76008 \end{pmatrix}$$

$$a_{8} = \begin{pmatrix} 0.952016u^{12} + 6.34267u^{11} + \cdots + 20.2272u - 8.11181 \\ -0.321439u^{12} - 2.49405u^{11} + \cdots + 9.97650u + 4.76008 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 0.265390u^{12} + 1.06603u^{11} + \cdots + 9.97650u + 4.76008 \\ -1.05628u^{12} - 6.69481u^{11} + \cdots + 18.3551u + 5.76124 \end{pmatrix}$$

$$a_{7} = \begin{pmatrix} -0.526429u^{12} - 2.96321u^{11} + \cdots + 4.12620u - 0.318132 \\ -0.0272701u^{12} + 0.319698u^{11} + \cdots + 4.18190u - 1.79954 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} 0.0912097u^{12} + 0.512272u^{11} + \cdots - 0.0696258u + 1.71958 \\ 0.0835509u^{12} + 0.375109u^{11} + \cdots + 0.826806u + 0.0382942 \end{pmatrix}$$

(ii) Obstruction class = 1

(iii) Cusp Shapes = 
$$\frac{9460}{3447}u^{12} + \frac{61031}{3447}u^{11} + \dots - \frac{23618}{383}u - \frac{94159}{3447}u^{11} + \dots$$

| Crossings     | u-Polynomials at each crossing          |
|---------------|---|
| $c_1$         | $u^{13} - 13u^{12} + \dots + 111u - 25$ |
| $c_2$         | $u^{13} + 7u^{12} + \dots - 19u - 5$    |
| $c_3, c_7$    | $u^{13} - u^{12} + \dots + 2u + 1$      |
| $c_4, c_8$    | $u^{13} + 9u^{11} + \dots + u + 1$      |
| $c_5$         | $u^{13} - 7u^{12} + \dots - 19u + 5$    |
| $c_6$         | $u^{13} - 3u^{12} + \dots - 10u + 4$    |
| $c_9, c_{12}$ | $u^{13} - u^{12} + \dots + 2u - 1$      |
| $c_{10}$      | $u^{13} + 8u^{12} + \dots - 99u - 27$   |
| $c_{11}$      | $u^{13} + 3u^{12} + \dots - 10u - 4$    |

| Crossings     | Riley Polynomials at each crossing        |
|---------------|---|
| $c_1$         | $y^{13} - 45y^{12} + \dots - 4029y - 625$ |
| $c_2, c_5$    | $y^{13} - 13y^{12} + \dots + 111y - 25$   |
| $c_3, c_7$    | $y^{13} - 5y^{12} + \dots + 16y - 1$      |
| $c_4, c_8$    | $y^{13} + 18y^{12} + \dots - 9y - 1$      |
| $c_6, c_{11}$ | $y^{13} + 9y^{12} + \dots - 20y - 16$     |
| $c_9,c_{12}$  | $y^{13} + 15y^{12} + \dots + 8y^2 - 1$    |
| $c_{10}$      | $y^{13} - 8y^{12} + \dots + 3807y - 729$  |

| Solutions to $I_2^u$      | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape          |
|---------------------------|---------------------------------------|---------------------|
| u = 0.856243 + 0.439666I  |                                       |                     |
| a = 0.053687 + 1.058490I  | -5.33979 - 2.00841I                   | -6.30003 + 4.09243I |
| b = 0.666388 - 0.086808I  |                                       |                     |
| u = 0.856243 - 0.439666I  |                                       |                     |
| a = 0.053687 - 1.058490I  | -5.33979 + 2.00841I                   | -6.30003 - 4.09243I |
| b = 0.666388 + 0.086808I  |                                       |                     |
| u = -0.056167 + 1.060590I |                                       |                     |
| a = -0.794885 - 0.705726I | -3.27208 - 3.50308I                   | -5.03802 + 3.23691I |
| b = -0.85889 - 1.67983I   |                                       |                     |
| u = -0.056167 - 1.060590I |                                       |                     |
| a = -0.794885 + 0.705726I | -3.27208 + 3.50308I                   | -5.03802 - 3.23691I |
| b = -0.85889 + 1.67983I   |                                       |                     |
| u = 1.10413               |                                       |                     |
| a = 0.938401              | -0.224822                             | 1.29960             |
| b = -0.651589             |                                       |                     |
| u = -1.074570 + 0.503982I |                                       |                     |
| a = -0.476495 - 0.014009I | -5.72718 + 8.88579I                   | -3.64178 - 7.62615I |
| b = -0.14184 - 1.44672I   |                                       |                     |
| u = -1.074570 - 0.503982I |                                       |                     |
| a = -0.476495 + 0.014009I | -5.72718 - 8.88579I                   | -3.64178 + 7.62615I |
| b = -0.14184 + 1.44672I   |                                       |                     |
| u = -1.033670 + 0.730191I |                                       |                     |
| a = 0.539770 + 0.500315I  | -3.61034 + 0.42465I                   | -7.93042 + 0.83468I |
| b = -1.15414 + 1.81649I   |                                       |                     |
| u = -1.033670 - 0.730191I |                                       |                     |
| a = 0.539770 - 0.500315I  | -3.61034 - 0.42465I                   | -7.93042 - 0.83468I |
| b = -1.15414 - 1.81649I   |                                       |                     |
| u = -0.537801 + 0.322672I |                                       |                     |
| a = 0.581072 - 0.696232I  | -1.38260 + 4.11097I                   | -0.96481 - 7.32347I |
| b = 0.576934 + 1.237160I  |                                       |                     |

| Solutions to $I_2^u$      | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape          |
|---------------------------|---------------------------------------|---------------------|
| u = -0.537801 - 0.322672I |                                       |                     |
| a = 0.581072 + 0.696232I  | -1.38260 - 4.11097I                   | -0.96481 + 7.32347I |
| b = 0.576934 - 1.237160I  |                                       |                     |
| u = -2.20610 + 0.12523I   |                                       |                     |
| a = 0.027651 - 1.287690I  | -18.3891 - 1.5099I                    | -4.27475 + 0.24744I |
| b = 0.73733 + 3.92048I    |                                       |                     |
| u = -2.20610 - 0.12523I   |                                       |                     |
| a = 0.027651 + 1.287690I  | -18.3891 + 1.5099I                    | -4.27475 - 0.24744I |
| b = 0.73733 - 3.92048I    |                                       |                     |

III. 
$$I_3^u = \langle -4.80 \times 10^4 a^5 u^2 - 1.93 \times 10^5 a^4 u^2 + \dots - 3.72 \times 10^6 a - 1.94 \times 10^6, \ a^5 u^2 - 3a^4 u^2 + \dots + 13a + 8, \ u^3 + 2u^2 + 1 \rangle$$

(i) Arc colorings

$$a_{3} = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{6} = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_{2} = \begin{pmatrix} 1 \\ -u^{2} \end{pmatrix}$$

$$a_{1} = \begin{pmatrix} -u^{2} + 1 \\ -u^{2} \end{pmatrix}$$

$$a_{5} = \begin{pmatrix} 2u^{2} + u + 1 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} 0.0107216a^{5}u^{2} + 0.0429770a^{4}u^{2} + \dots + 0.830153a + 0.433530 \end{pmatrix}$$

$$a_{4} = \begin{pmatrix} -0.0276588a^{5}u^{2} + 0.0409242a^{4}u^{2} + \dots - 0.707287a + 0.0149656 \\ 0.0276588a^{5}u^{2} - 0.0409242a^{4}u^{2} + \dots + 0.707287a + 0.985034 \end{pmatrix}$$

$$a_{9} = \begin{pmatrix} 0.0107216a^{5}u^{2} + 0.0429770a^{4}u^{2} + \dots + 0.830153a + 0.433530 \end{pmatrix}$$

$$a_{8} = \begin{pmatrix} -0.0107216a^{5}u^{2} + 0.0429770a^{4}u^{2} + \dots + 0.169847a - 0.433530 \\ 0.0107216a^{5}u^{2} + 0.0429770a^{4}u^{2} + \dots + 0.830153a + 0.433530 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} -0.114428a^{5}u^{2} + 0.0429770a^{4}u^{2} + \dots + 0.830153a + 0.433530 \\ 0.125150a^{5}u^{2} + 0.0317676a^{4}u^{2} + \dots + 0.830153a + 0.433530 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} -0.114428a^{5}u^{2} + 0.0317676a^{4}u^{2} + \dots + 0.830153a - 0.768759 \\ 0.125150a^{5}u^{2} + 0.0112093a^{4}u^{2} + \dots + 1.07483a - 0.768759 \end{pmatrix}$$

$$a_{7} = \begin{pmatrix} -0.0212085a^{5}u^{2} + 0.145939a^{4}u^{2} + \dots + 1.19184a + 0.989840 \\ 0.379146a^{5}u^{2} + 0.374514a^{4}u^{2} + \dots + 0.519904a + 0.992191 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} -0.135637a^{5}u^{2} + 0.177707a^{4}u^{2} + \dots + 0.519904a + 0.992191 \\ -0.135637a^{5}u^{2} + 0.0554376a^{4}u^{2} + \dots + 0.353544a - 1.34279 \end{pmatrix}$$

#### (ii) Obstruction class = -1

(iii) Cusp Shapes = 
$$-\frac{877944}{2240141}a^5u^2 - \frac{2031720}{2240141}a^4u^2 + \dots + \frac{2110148}{2240141}a - \frac{15981979}{2240141}$$

| Crossings      | u-Polynomials at each crossing           |
|----------------|--|
| $c_1$          | $(u^3 + 4u^2 - 4u + 1)^6$                |
| $c_{2}, c_{5}$ | $(u^3 - 2u^2 - 1)^6$                     |
| $c_3, c_7$     | $u^{18} + 2u^{17} + \dots - 129u^2 + 27$ |
| $c_4, c_8$     | $u^{18} + 20u^{16} + \dots + 180u + 11$  |
| $c_6, c_{11}$  | $(u^3 + u^2 + 2u + 1)^6$                 |
| $c_9, c_{12}$  | $u^{18} - 3u^{17} + \dots + 4276u + 383$ |
| $c_{10}$       | $(u^3 + u^2 - u - 2)^6$                  |

| Crossings       | Riley Polynomials at each crossing              |
|-----------------|---|
| $c_1$           | $(y^3 - 24y^2 + 8y - 1)^6$                      |
| $c_2, c_5$      | $(y^3 - 4y^2 - 4y - 1)^6$                       |
| $c_3, c_7$      | $y^{18} - 4y^{17} + \dots - 6966y + 729$        |
| $c_4, c_8$      | $y^{18} + 40y^{17} + \dots - 15834y + 121$      |
| $c_6, c_{11}$   | $(y^3 + 3y^2 + 2y - 1)^6$                       |
| $c_{9}, c_{12}$ | $y^{18} + 49y^{17} + \dots - 7285948y + 146689$ |
| $c_{10}$        | $(y^3 - 3y^2 + 5y - 4)^6$                       |

| Solutions to $I_3^u$      | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape          |
|---------------------------|---------------------------------------|---------------------|
| u = 0.102785 + 0.665457I  |                                       |                     |
| a = -0.271547 + 1.307830I | -1.13951 - 2.56897I                   | -0.10440 + 2.13317I |
| b = -0.22345 + 1.73716I   |                                       |                     |
| u = 0.102785 + 0.665457I  |                                       |                     |
| a = -1.48693 - 0.70223I   | -1.13951 - 2.56897I                   | -0.10440 + 2.13317I |
| b = -0.624969 - 0.126877I |                                       |                     |
| u = 0.102785 + 0.665457I  |                                       |                     |
| a = 1.56533 + 0.54666I    | -5.27710 - 5.39709I                   | -6.63367 + 5.11262I |
| b = -0.121877 + 0.223759I |                                       |                     |
| u = 0.102785 + 0.665457I  |                                       |                     |
| a = -0.029119 + 0.292106I | -5.27710 + 0.25915I                   | -6.63367 - 0.84628I |
| b = 0.310540 - 1.045640I  |                                       |                     |
| u = 0.102785 + 0.665457I  |                                       |                     |
| a = 2.67067 + 0.73911I    | -5.27710 + 0.25915I                   | -6.63367 - 0.84628I |
| b = 2.26454 + 0.01108I    |                                       |                     |
| u = 0.102785 + 0.665457I  |                                       |                     |
| a = -0.11892 - 2.98573I   | -5.27710 - 5.39709I                   | -6.63367 + 5.11262I |
| b = -0.48087 - 2.93264I   |                                       |                     |
| u = 0.102785 - 0.665457I  |                                       |                     |
| a = -0.271547 - 1.307830I | -1.13951 + 2.56897I                   | -0.10440 - 2.13317I |
| b = -0.22345 - 1.73716I   |                                       |                     |
| u = 0.102785 - 0.665457I  |                                       |                     |
| a = -1.48693 + 0.70223I   | -1.13951 + 2.56897I                   | -0.10440 - 2.13317I |
| b = -0.624969 + 0.126877I |                                       |                     |
| u = 0.102785 - 0.665457I  |                                       |                     |
| a = 1.56533 - 0.54666I    | -5.27710 + 5.39709I                   | -6.63367 - 5.11262I |
| b = -0.121877 - 0.223759I |                                       |                     |
| u = 0.102785 - 0.665457I  |                                       |                     |
| a = -0.029119 - 0.292106I | -5.27710 - 0.25915I                   | -6.63367 + 0.84628I |
| b = 0.310540 + 1.045640I  |                                       |                     |

| Solutions to $I_3^u$      | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape          |
|---------------------------|---------------------------------------|---------------------|
| u = 0.102785 - 0.665457I  |                                       |                     |
| a = 2.67067 - 0.73911I    | -5.27710 - 0.25915I                   | -6.63367 + 0.84628I |
| b = 2.26454 - 0.01108I    |                                       |                     |
| u = 0.102785 - 0.665457I  |                                       |                     |
| a = -0.11892 + 2.98573I   | -5.27710 + 5.39709I                   | -6.63367 - 5.11262I |
| b = -0.48087 + 2.93264I   |                                       |                     |
| u = -2.20557              |                                       |                     |
| a = -0.132067 + 1.061970I | 19.5761 + 2.8281I                     | -8.26193 - 2.97945I |
| b = 0.73082 - 2.94300I    |                                       |                     |
| u = -2.20557              |                                       |                     |
| a = -0.132067 - 1.061970I | 19.5761 - 2.8281I                     | -8.26193 + 2.97945I |
| b = 0.73082 + 2.94300I    |                                       |                     |
| u = -2.20557              |                                       |                     |
| a = 0.248720 + 1.254260I  | -15.7648                              | -1.73266 + 0.I      |
| b = -1.03878 - 3.80675I   |                                       |                     |
| u = -2.20557              |                                       |                     |
| a =  0.248720 - 1.254260I | -15.7648                              | -1.73266 + 0.I      |
| b = -1.03878 + 3.80675I   |                                       |                     |
| u = -2.20557              |                                       |                     |
| a = -0.44614 + 1.55281I   | 19.5761 - 2.8281I                     | -8.26193 + 2.97945I |
| b = 1.68404 - 4.99299I    |                                       |                     |
| u = -2.20557              |                                       |                     |
| a = -0.44614 - 1.55281I   | 19.5761 + 2.8281I                     | -8.26193 - 2.97945I |
| b = 1.68404 + 4.99299I    |                                       |                     |

IV. 
$$I_4^u = \langle b^2 + ba + a^2, \ a^3 + a^2 - 1, \ u - 1 \rangle$$

(i) Arc colorings

$$a_3 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} 0 \\ 1 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} 1 \\ -1 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} 0 \\ -1 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} a \\ b \end{pmatrix}$$

$$a_4 = \begin{pmatrix} ba + 1 \\ -ba - a^2 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} a \\ b+a \end{pmatrix}$$

$$a_8 = \begin{pmatrix} -b \\ b+a \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} a \\ b \end{pmatrix}$$

$$a_7 = \begin{pmatrix} a^2 + a - 1 \\ -a^2b + b + a \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} a^2 \\ ba + a^2 - 1 \end{pmatrix}$$

- (ii) Obstruction class = 1
- (iii) Cusp Shapes = 4a 3

| Crossings             | u-Polynomials at each crossing     |
|-----------------------|------------------------------------|
| $c_1, c_2$            | $(u-1)^6$                          |
| $c_3, c_4, c_7$ $c_8$ | $u^6 - u^5 + u^4 - 2u^3 + u^2 + 1$ |
| $c_5$                 | $(u+1)^6$                          |
| $c_6$                 | $(u^3 + u^2 + 2u + 1)^2$           |
| $c_9,c_{12}$          | $(u^3 + u^2 - 1)^2$                |
| $c_{10}$              | $u^6$                              |
| $c_{11}$              | $(u^3 - u^2 + 2u - 1)^2$           |

| Crossings             | Riley Polynomials at each crossing |
|-----------------------|------------------------------------|
| $c_1, c_2, c_5$       | $(y-1)^6$                          |
| $c_3, c_4, c_7$ $c_8$ | $y^6 + y^5 - y^4 + 3y^2 + 2y + 1$  |
| $c_6, c_{11}$         | $(y^3 + 3y^2 + 2y - 1)^2$          |
| $c_9, c_{12}$         | $(y^3 - y^2 + 2y - 1)^2$           |
| $c_{10}$              | $y^6$                              |

| Solutions to $I_4^u$      | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape          |
|---------------------------|---------------------------------------|---------------------|
| u = 1.00000               |                                       |                     |
| a = -0.877439 + 0.744862I | -4.66906 - 2.82812I                   | -6.50976 + 2.97945I |
| b = 1.083790 + 0.387453I  |                                       |                     |
| u = 1.00000               |                                       |                     |
| a = -0.877439 + 0.744862I | -4.66906 - 2.82812I                   | -6.50976 + 2.97945I |
| b = -0.206350 - 1.132320I |                                       |                     |
| u = 1.00000               |                                       |                     |
| a = -0.877439 - 0.744862I | -4.66906 + 2.82812I                   | -6.50976 - 2.97945I |
| b = 1.083790 - 0.387453I  |                                       |                     |
| u = 1.00000               |                                       |                     |
| a = -0.877439 - 0.744862I | -4.66906 + 2.82812I                   | -6.50976 - 2.97945I |
| b = -0.206350 + 1.132320I |                                       |                     |
| u = 1.00000               |                                       |                     |
| a = 0.754878              | -0.531480                             | 0.0195110           |
| b = -0.377439 + 0.653743I |                                       |                     |
| u = 1.00000               |                                       |                     |
| a = 0.754878              | -0.531480                             | 0.0195110           |
| b = -0.377439 - 0.653743I |                                       |                     |

### V. u-Polynomials

| Crossings             | u-Polynomials at each crossing   |
|-----------------------|--|
| $c_1$                 | $((u-1)^6)(u^3 + 4u^2 - 4u + 1)^6(u^{13} - 13u^{12} + \dots + 111u - 25)$ $\cdot (u^{18} + 44u^{17} + \dots + 58880u + 4096)$  |
| $c_2$                 | $((u-1)^6)(u^3 - 2u^2 - 1)^6(u^{13} + 7u^{12} + \dots - 19u - 5)$ $\cdot (u^{18} + 14u^{17} + \dots + 32u - 64)$   |
| $c_3, c_7$            | $(u^{6} - u^{5} + u^{4} - 2u^{3} + u^{2} + 1)(u^{13} - u^{12} + \dots + 2u + 1)$ $\cdot (u^{18} + u^{17} + \dots + u + 1)(u^{18} + 2u^{17} + \dots - 129u^{2} + 27)$ |
| $c_4, c_8$            | $(u^{6} - u^{5} + u^{4} - 2u^{3} + u^{2} + 1)(u^{13} + 9u^{11} + \dots + u + 1)$ $\cdot (u^{18} + 15u^{16} + \dots - 2u - 1)(u^{18} + 20u^{16} + \dots + 180u + 11)$ |
| $c_5$                 | $((u+1)^6)(u^3 - 2u^2 - 1)^6(u^{13} - 7u^{12} + \dots - 19u + 5)$ $\cdot (u^{18} + 14u^{17} + \dots + 32u - 64)$   |
| <i>c</i> <sub>6</sub> | $((u^3 + u^2 + 2u + 1)^8)(u^{13} - 3u^{12} + \dots - 10u + 4)$ $\cdot (u^{18} - 8u^{17} + \dots + 66u^2 - 4)$  |
| $c_9, c_{12}$         | $((u^{3} + u^{2} - 1)^{2})(u^{13} - u^{12} + \dots + 2u - 1)$ $\cdot (u^{18} - 3u^{17} + \dots + 4276u + 383)(u^{18} + u^{17} + \dots - 29u - 1)$                    |
| $c_{10}$              | $u^{6}(u^{3} + u^{2} - u - 2)^{6}(u^{13} + 8u^{12} + \dots - 99u - 27)$ $\cdot (u^{18} - 17u^{17} + \dots - 112u + 8)$   |
| $c_{11}$              | $((u^{3} - u^{2} + 2u - 1)^{2})(u^{3} + u^{2} + 2u + 1)^{6}(u^{13} + 3u^{12} + \dots - 10u - 4)$ $\cdot (u^{18} - 8u^{17} + \dots + 66u^{2} - 4)$                    |

## VI. Riley Polynomials

| Crossings     | Riley Polynomials at each crossing  |
|---------------|---|
| $c_1$         | $((y-1)^6)(y^3 - 24y^2 + 8y - 1)^6(y^{13} - 45y^{12} + \dots - 4029y - 625)$ $\cdot (y^{18} - 180y^{17} + \dots - 1103757312y + 16777216)$                                      |
| $c_2, c_5$    | $((y-1)^6)(y^3 - 4y^2 - 4y - 1)^6(y^{13} - 13y^{12} + \dots + 111y - 25)$ $\cdot (y^{18} - 44y^{17} + \dots - 58880y + 4096)$   |
| $c_3, c_7$    | $(y^{6} + y^{5} - y^{4} + 3y^{2} + 2y + 1)(y^{13} - 5y^{12} + \dots + 16y - 1)$ $\cdot (y^{18} - 9y^{17} + \dots + 3y + 1)(y^{18} - 4y^{17} + \dots - 6966y + 729)$             |
| $c_4, c_8$    | $(y^{6} + y^{5} - y^{4} + 3y^{2} + 2y + 1)(y^{13} + 18y^{12} + \dots - 9y - 1)$ $\cdot (y^{18} + 30y^{17} + \dots - 20y + 1)(y^{18} + 40y^{17} + \dots - 15834y + 121)$         |
| $c_6, c_{11}$ | $((y^3 + 3y^2 + 2y - 1)^8)(y^{13} + 9y^{12} + \dots - 20y - 16)$ $\cdot (y^{18} + 12y^{17} + \dots - 528y + 16)$  |
| $c_9, c_{12}$ | $((y^{3} - y^{2} + 2y - 1)^{2})(y^{13} + 15y^{12} + \dots + 8y^{2} - 1)$ $\cdot (y^{18} + 43y^{17} + \dots - 425y + 1)$ $\cdot (y^{18} + 49y^{17} + \dots - 7285948y + 146689)$ |
| $c_{10}$      | $y^{6}(y^{3} - 3y^{2} + 5y - 4)^{6}(y^{13} - 8y^{12} + \dots + 3807y - 729)$ $\cdot (y^{18} - 11y^{17} + \dots - 1312y + 64)$   |