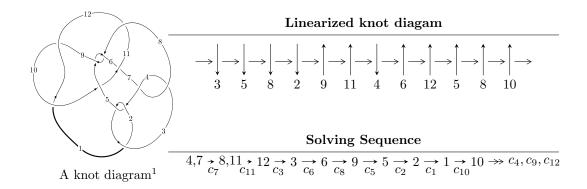
# $12n_{0214} \ (K12n_{0214})$



#### Ideals for irreducible components<sup>2</sup> of $X_{par}$

$$\begin{split} I_1^u &= \langle -2.09571 \times 10^{30} u^{16} - 2.07081 \times 10^{30} u^{15} + \dots + 6.08382 \times 10^{33} b + 8.49226 \times 10^{32}, \\ &- 1.33922 \times 10^{32} u^{16} - 1.76390 \times 10^{32} u^{15} + \dots + 6.08382 \times 10^{34} a - 1.49809 \times 10^{35}, \\ &u^{17} + u^{16} + \dots + 384 u - 256 \rangle \\ I_2^u &= \langle b, -u^8 + u^7 - 3u^6 + u^5 - 4u^4 + u^3 - 4u^2 + a - 2, \ u^9 - u^8 + 2u^7 - u^6 + 3u^5 - u^4 + 2u^3 + u + 1 \rangle \\ I_1^v &= \langle a, -941v^7 + 2551v^6 - 1791v^5 - 6184v^4 + 16309v^3 + 15249v^2 + 887b - 4192v - 1842, \\ &v^8 - 2v^7 + 8v^5 - 13v^4 - 28v^3 - 7v^2 + 3v + 1 \rangle \end{split}$$

\* 3 irreducible components of  $\dim_{\mathbb{C}} = 0$ , with total 34 representations.

<sup>&</sup>lt;sup>1</sup>The image of knot diagram is generated by the software "**Draw programme**" developed by Andrew Bartholomew(http://www.layer8.co.uk/maths/draw/index.htm#Running-draw), where we modified some parts for our purpose(https://github.com/CATsTAILs/LinksPainter).

 $<sup>^2</sup>$  All coefficients of polynomials are rational numbers. But the coefficients are sometimes approximated in decimal forms when there is not enough margin.

I. 
$$I_1^u = \langle -2.10 \times 10^{30} u^{16} - 2.07 \times 10^{30} u^{15} + \dots + 6.08 \times 10^{33} b + 8.49 \times 10^{32}, \ -1.34 \times 10^{32} u^{16} - 1.76 \times 10^{32} u^{15} + \dots + 6.08 \times 10^{34} a - 1.50 \times 10^{35}, \ u^{17} + u^{16} + \dots + 384 u - 256 \rangle$$

(i) Arc colorings

$$\begin{array}{l} a_4 = \begin{pmatrix} 0 \\ u \end{pmatrix} \\ a_7 = \begin{pmatrix} 1 \\ 0 \end{pmatrix} \\ a_8 = \begin{pmatrix} 1 \\ u^2 \end{pmatrix} \\ a_{11} = \begin{pmatrix} 0.00220128u^{16} + 0.00289932u^{15} + \cdots - 5.85108u + 2.46242 \\ 0.000344472u^{16} + 0.000340380u^{15} + \cdots - 1.54619u - 0.139587 \end{pmatrix} \\ a_{12} = \begin{pmatrix} 0.00303342u^{16} + 0.00362610u^{15} + \cdots - 7.69275u + 2.14413 \\ 0.000425453u^{16} + 0.000210059u^{15} + \cdots - 1.29270u - 0.166559 \end{pmatrix} \\ a_3 = \begin{pmatrix} u \\ u^3 + u \end{pmatrix} \\ a_6 = \begin{pmatrix} -0.00104394u^{16} - 0.000502159u^{15} + \cdots - 0.986241u - 0.762867 \\ -0.00028289u^{16} - 0.000242907u^{15} + \cdots + 0.747325u - 0.207566 \end{pmatrix} \\ a_9 = \begin{pmatrix} -0.00179545u^{16} - 0.00185026u^{15} + \cdots + 2.21680u + 0.967939 \\ -0.000259975u^{16} - 0.000427010u^{15} + \cdots + 0.794841u + 0.0755036 \end{pmatrix} \\ a_5 = \begin{pmatrix} -0.00105718u^{16} - 0.000691805u^{15} + \cdots + 2.07890u + 0.560650 \\ -0.000380922u^{16} - 0.000264026u^{15} + \cdots + 0.424147u + 0.138080 \end{pmatrix} \\ a_2 = \begin{pmatrix} 0.000938601u^{16} + 0.000588558u^{15} + \cdots + 2.91399u - 0.516106 \\ 0.000131921u^{16} + 0.0000588558u^{15} + \cdots + 2.50305u - 0.422569 \\ -0.000161339u^{16} - 0.0000427780u^{15} + \cdots + 1.20979u - 0.0450674 \end{pmatrix} \\ a_1 = \begin{pmatrix} 0.000676260u^{16} + 0.000427780u^{15} + \cdots + 0.692685u + 0.0744692 \end{pmatrix} \\ a_{10} = \begin{pmatrix} 0.00254189u^{16} + 0.00306982u^{15} + \cdots + 0.692685u + 0.0744692 \end{pmatrix} \\ a_{10} = \begin{pmatrix} 0.00254189u^{16} + 0.00306982u^{15} + \cdots + 0.692685u + 0.0744692 \end{pmatrix} \\ 0.000191963u^{16} + 6.02751 \times 10^{-6}u^{15} + \cdots - 0.601447u - 0.0925424 \end{pmatrix}$$

- (ii) Obstruction class = -1
- (iii) Cusp Shapes =  $0.0102860u^{16} + 0.00859873u^{15} + \cdots + 17.8393u + 1.47057$

### (iv) u-Polynomials at the component

| Crossings     | u-Polynomials at each crossing                |
|---------------|---|
| $c_1$         | $u^{17} + 37u^{16} + \dots + u + 1$           |
| $c_2, c_4$    | $u^{17} - 15u^{16} + \dots + 3u - 1$          |
| $c_3, c_7$    | $u^{17} + u^{16} + \dots + 384u - 256$        |
| $c_5, c_8$    | $u^{17} + 2u^{16} + \dots + 3u + 1$           |
| $c_6$         | $u^{17} + u^{16} + \dots - 512u - 512$        |
| $c_9, c_{12}$ | $u^{17} + 16u^{16} + \dots - 11u + 1$         |
| $c_{10}$      | $u^{17} - 3u^{16} + \dots - 167922u - 192217$ |
| $c_{11}$      | $u^{17} - 6u^{16} + \dots - 19686u + 2393$    |

### (v) Riley Polynomials at the component

| Crossings     | Riley Polynomials at each crossing                        |
|---------------|---|
| $c_1$         | $y^{17} - 57y^{16} + \dots - 7859y - 1$                   |
| $c_2, c_4$    | $y^{17} - 37y^{16} + \dots + y - 1$                       |
| $c_3, c_7$    | $y^{17} - 33y^{16} + \dots + 245760y - 65536$             |
| $c_5, c_8$    | $y^{17} + 12y^{16} + \dots + 25y - 1$                     |
|               | $y^{17} - 39y^{16} + \dots + 3670016y - 262144$           |
| $c_9, c_{12}$ | $y^{17} - 40y^{16} + \dots + 221y - 1$                    |
| $c_{10}$      | $y^{17} - 45y^{16} + \dots + 806894237728y - 36947375089$ |
| $c_{11}$      | $y^{17} - 38y^{16} + \dots + 475084108y - 5726449$        |

## (vi) Complex Volumes and Cusp Shapes

| Solutions to $I_1^u$      | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape          |
|---------------------------|---------------------------------------|---------------------|
| u = 0.634179 + 0.647207I  |                                       |                     |
| a = -0.59964 + 1.28467I   | -4.28789 + 1.16759I                   | -4.15148 + 0.42617I |
| b = -0.186633 - 0.343696I |                                       |                     |
| u = 0.634179 - 0.647207I  |                                       |                     |
| a = -0.59964 - 1.28467I   | -4.28789 - 1.16759I                   | -4.15148 - 0.42617I |
| b = -0.186633 + 0.343696I |                                       |                     |
| u = -0.690024 + 0.240704I |                                       |                     |
| a = 0.236937 - 1.076210I  | -1.52593 + 2.30609I                   | 0.84073 - 4.41351I  |
| b = 0.762159 + 0.184291I  |                                       |                     |
| u = -0.690024 - 0.240704I |                                       |                     |
| a = 0.236937 + 1.076210I  | -1.52593 - 2.30609I                   | 0.84073 + 4.41351I  |
| b =  0.762159 - 0.184291I |                                       |                     |
| u = -0.442272             |                                       |                     |
| a = 1.85319               | -1.26971                              | -9.85470            |
| b = 0.249683              |                                       |                     |
| u = 0.408620              |                                       |                     |
| a = 1.30764               | 1.02663                               | 10.5660             |
| b = -0.594904             |                                       |                     |
| u = 0.149177 + 0.310693I  |                                       |                     |
| a = 0.71057 - 3.54706I    | 0.959539 - 1.013620I                  | 4.00582 - 0.77460I  |
| b = -0.479273 - 0.632626I |                                       |                     |
| u = 0.149177 - 0.310693I  |                                       |                     |
| a = 0.71057 + 3.54706I    | 0.959539 + 1.013620I                  | 4.00582 + 0.77460I  |
| b = -0.479273 + 0.632626I |                                       |                     |
| u = 2.13688 + 2.10608I    |                                       |                     |
| a = 0.445317 + 0.501364I  | -16.2212 - 7.3387I                    | 3.75665 + 2.42096I  |
| b = -2.32289 + 2.38769I   |                                       |                     |
| u = 2.13688 - 2.10608I    |                                       |                     |
| a = 0.445317 - 0.501364I  | -16.2212 + 7.3387I                    | 3.75665 - 2.42096I  |
| b = -2.32289 - 2.38769I   |                                       |                     |

| Solutions to $I_1^u$        | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape           |
|-----------------------------|---------------------------------------|----------------------|
| u = -2.02549 + 2.27905I     |                                       |                      |
| a = -0.511301 + 0.473424I   | 19.0196 + 12.9458I                    | 0.98224 - 5.00778I   |
| b = 2.09738 + 2.40856I      |                                       |                      |
| u = -2.02549 - 2.27905I     |                                       |                      |
| a = -0.511301 - 0.473424I   | 19.0196 - 12.9458I                    | 0.98224 + 5.00778I   |
| b = 2.09738 - 2.40856I      |                                       |                      |
| u = -2.36097 + 2.01644I     |                                       |                      |
| a = -0.370113 + 0.467612I   | 19.0497 + 1.6784I                     | 0.985857 + 0.191287I |
| b = 2.49326 + 2.18000I      |                                       |                      |
| u = -2.36097 - 2.01644I     |                                       |                      |
| a = -0.370113 - 0.467612I   | 19.0497 - 1.6784I                     | 0.985857 - 0.191287I |
| b = 2.49326 - 2.18000I      |                                       |                      |
| u = -3.15648                |                                       |                      |
| a = 0.0710901               | 3.68181                               | 3.55300              |
| b = 3.69863                 |                                       |                      |
| u = 3.25130 + 0.32944I      |                                       |                      |
| a = -0.0277291 + 0.0915040I | -0.61891 - 5.84472I                   | 0.94829 + 2.62397I   |
| b = -3.54070 + 0.36634I     |                                       |                      |
| u = 3.25130 - 0.32944I      |                                       |                      |
| a = -0.0277291 - 0.0915040I | -0.61891 + 5.84472I                   | 0.94829 - 2.62397I   |
| b = -3.54070 - 0.36634I     |                                       |                      |

 $\text{II. } I_2^u = \langle b, \ -u^8 + u^7 - 3u^6 + u^5 - 4u^4 + u^3 - 4u^2 + a - 2, \ u^9 - u^8 + 2u^7 - u^6 + 3u^5 - u^4 + 2u^3 + u + 1 \rangle$ 

(i) Arc colorings

$$a_{4} = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_{7} = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{8} = \begin{pmatrix} 1 \\ u^{2} \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} u^{8} - u^{7} + 3u^{6} - u^{5} + 4u^{4} - u^{3} + 4u^{2} + 2 \\ 0 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} -u^{7} + 2u^{6} - u^{5} + 2u^{4} - u^{3} + 3u^{2} + u + 2 \\ u^{7} + 2u^{5} + 3u^{3} + u^{2} + 2u + 1 \end{pmatrix}$$

$$a_{3} = \begin{pmatrix} u \\ u^{3} + u \end{pmatrix}$$

$$a_{6} = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{9} = \begin{pmatrix} u^{2} + 1 \\ u^{2} \end{pmatrix}$$

$$a_{5} = \begin{pmatrix} u^{4} + u^{2} + 1 \\ u^{4} \end{pmatrix}$$

$$a_{2} = \begin{pmatrix} -u^{6} - u^{4} - 2u^{2} - 1 \\ -u^{8} - 2u^{6} - 2u^{4} - 2u^{2} \end{pmatrix}$$

$$a_{1} = \begin{pmatrix} -u^{2} - 1 \\ -u^{2} \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} -u^{7} + 2u^{6} - u^{5} + 2u^{4} - u^{3} + 4u^{2} + u + 3 \\ u^{7} + 2u^{5} + 3u^{3} + 2u^{2} + 2u + 1 \end{pmatrix}$$

- (ii) Obstruction class = 1
- (iii) Cusp Shapes =  $-4u^8 + 8u^7 13u^6 + 9u^5 17u^4 + 16u^3 13u^2 + 4u 4u^3 + 16u^3 13u^2 + 4u 4u^3 + 16u^3 13u^3 + 16u^3 16u^3 16u^3 + 16u^3 16u^3 16u^3 16u^3 + 16u^3 16u^3 16u^3 + 16u^3 16$

(iv) u-Polynomials at the component

| Crossings             | u-Polynomials at each crossing                                       |
|-----------------------|--|
| $c_1$                 | $u^9 - 5u^8 + 12u^7 - 15u^6 + 9u^5 + u^4 - 4u^3 + 2u^2 + u - 1$      |
| $c_2$                 | $u^9 + u^8 - 2u^7 - 3u^6 + u^5 + 3u^4 + 2u^3 - u - 1$                |
| $c_3$                 | $u^9 + u^8 + 2u^7 + u^6 + 3u^5 + u^4 + 2u^3 + u - 1$                 |
| $c_4$                 | $u^9 - u^8 - 2u^7 + 3u^6 + u^5 - 3u^4 + 2u^3 - u + 1$                |
| <i>C</i> <sub>5</sub> | $u^9 + 3u^8 + 8u^7 + 13u^6 + 17u^5 + 17u^4 + 12u^3 + 6u^2 + u - 1$   |
|                       | $u^9$  |
| $c_7$                 | $u^9 - u^8 + 2u^7 - u^6 + 3u^5 - u^4 + 2u^3 + u + 1$                 |
| c <sub>8</sub>        | $u^9 - 3u^8 + 8u^7 - 13u^6 + 17u^5 - 17u^4 + 12u^3 - 6u^2 + u + 1$   |
| <i>C</i> 9            | $(u+1)^9$  |
| $c_{10}$              | $u^9 + 2u^8 + 5u^7 + 22u^6 + 52u^5 + 63u^4 + 41u^3 + 10u^2 - 2u - 1$ |
| $c_{11}$              | $u^9 + 3u^8 + 3u^7 - 2u^6 + u^5 - 9u^4 + 3u^3 + 2u - 1$              |
| $c_{12}$              | $(u-1)^9$  |

## (v) Riley Polynomials at the component

| Crossings             | Riley Polynomials at each crossing                                  |
|-----------------------|---|
| $c_1$                 | $y^9 - y^8 + 12y^7 - 7y^6 + 37y^5 + y^4 - 10y^2 + 5y - 1$           |
| $c_2, c_4$            | $y^9 - 5y^8 + 12y^7 - 15y^6 + 9y^5 + y^4 - 4y^3 + 2y^2 + y - 1$     |
| $c_3, c_7$            | $y^9 + 3y^8 + 8y^7 + 13y^6 + 17y^5 + 17y^4 + 12y^3 + 6y^2 + y - 1$  |
| $c_5,c_8$             | $y^9 + 7y^8 + 20y^7 + 25y^6 + 5y^5 - 15y^4 + 22y^2 + 13y - 1$       |
| <i>c</i> <sub>6</sub> | $y^9$   |
| $c_9,c_{12}$          | $(y-1)^9$   |
| $c_{10}$              | $y^9 + 6y^8 + \dots + 24y - 1$                                      |
| $c_{11}$              | $y^9 - 3y^8 + 23y^7 + 62y^6 - 13y^5 - 57y^4 + 9y^3 - 6y^2 + 4y - 1$ |

### (vi) Complex Volumes and Cusp Shapes

| Solutions to $I_2^u$      | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape          |
|---------------------------|---------------------------------------|---------------------|
| u = -0.140343 + 0.966856I |                                       |                     |
| a = -0.483566 + 0.305056I | 3.42837 + 2.09337I                    | 7.05683 - 6.62869I  |
| b = 0                     |                                       |                     |
| u = -0.140343 - 0.966856I |                                       |                     |
| a = -0.483566 - 0.305056I | 3.42837 - 2.09337I                    | 7.05683 + 6.62869I  |
| b = 0                     |                                       |                     |
| u = -0.628449 + 0.875112I |                                       |                     |
| a = 1.022450 + 0.246780I  | 1.02799 + 2.45442I                    | 3.88318 - 3.00529I  |
| b = 0                     |                                       |                     |
| u = -0.628449 - 0.875112I |                                       |                     |
| a = 1.022450 - 0.246780I  | 1.02799 - 2.45442I                    | 3.88318 + 3.00529I  |
| b = 0                     |                                       |                     |
| u = 0.796005 + 0.733148I  |                                       |                     |
| a = -1.23246 + 1.62704I   | -2.72642 + 1.33617I                   | 1.90921 + 3.07774I  |
| b = 0                     |                                       |                     |
| u = 0.796005 - 0.733148I  |                                       |                     |
| a = -1.23246 - 1.62704I   | -2.72642 - 1.33617I                   | 1.90921 - 3.07774I  |
| b = 0                     |                                       |                     |
| u = 0.728966 + 0.986295I  |                                       |                     |
| a = 0.411691 + 0.129409I  | -1.95319 - 7.08493I                   | -2.13339 + 8.87891I |
| b = 0                     |                                       |                     |
| u = 0.728966 - 0.986295I  |                                       |                     |
| a = 0.411691 - 0.129409I  | -1.95319 + 7.08493I                   | -2.13339 - 8.87891I |
| b = 0                     |                                       |                     |
| u = -0.512358             |                                       |                     |
| a = 3.56378               | 0.446489                              | -13.4320            |
| b = 0                     |                                       |                     |

III. 
$$I_1^v = \langle a, -941v^7 + 2551v^6 + \dots + 887b - 1842, v^8 - 2v^7 + 8v^5 - 13v^4 - 28v^3 - 7v^2 + 3v + 1 \rangle$$

#### (i) Arc colorings

$$a_{4} = \begin{pmatrix} v \\ 0 \end{pmatrix}$$

$$a_{7} = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{8} = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 1.06088v^{7} - 2.87599v^{6} + \dots + 4.72604v + 2.07666 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} 1.06088v^{7} - 2.87599v^{6} + \dots + 4.72604v + 2.07666 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} 1.06088v^{7} - 2.87599v^{6} + \dots + 4.72604v + 2.07666 \end{pmatrix}$$

$$a_{3} = \begin{pmatrix} v \\ 0 \end{pmatrix}$$

$$a_{6} = \begin{pmatrix} -1.62683v^{7} + 3.57497v^{6} + \dots + 1.17926v - 3.82638 \end{pmatrix}$$

$$a_{9} = \begin{pmatrix} 1.62683v^{7} - 3.57497v^{6} + \dots + 1.17926v + 4.82638 \\ 2.38219v^{7} - 5.33258v^{6} + \dots - 1.21984v + 6.70349 \end{pmatrix}$$

$$a_{5} = \begin{pmatrix} -0.755355v^{7} + 1.75761v^{6} + \dots + 2.39910v - 1.87711 \\ -v^{7} + 2v^{6} - 8v^{4} + 13v^{3} + 28v^{2} + 7v - 3 \end{pmatrix}$$

$$a_{2} = \begin{pmatrix} 0.755355v^{7} - 1.75761v^{6} + \dots - 1.39910v + 1.87711 \\ v^{7} - 2v^{6} + 8v^{4} - 13v^{3} - 28v^{2} - 7v + 3 \end{pmatrix}$$

$$a_{1} = \begin{pmatrix} 0.755355v^{7} - 1.75761v^{6} + \dots - 2.39910v + 1.87711 \\ v^{7} - 2v^{6} + 8v^{4} - 13v^{3} - 28v^{2} - 7v + 3 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} 0.244645v^{7} - 0.242390v^{6} + \dots - 4.60090v + 1.12289 \\ v^{7} - 2v^{6} + 8v^{4} - 13v^{3} - 28v^{2} - 7v + 3 \end{pmatrix}$$

#### (ii) Obstruction class = 1

(iii) Cusp Shapes 
$$= \frac{7569}{887}v^7 - \frac{17105}{887}v^6 + \frac{3122}{887}v^5 + \frac{63760}{887}v^4 - \frac{119185}{887}v^3 - \frac{185558}{887}v^2 + \frac{17829}{887}v + \frac{32002}{887}v^3 - \frac{185558}{887}v^3 - \frac{185558}{887}v^3 + \frac{1887}{887}v^3 + \frac{18887}{887}v^3 + \frac{18887}{88$$

### (iv) u-Polynomials at the component

| Crossings             | u-Polynomials at each crossing                              |
|-----------------------|---|
| $c_1, c_2$            | $(u-1)^8$   |
| $c_{3}, c_{7}$        | $u^8$   |
| <i>C</i> <sub>4</sub> | $(u+1)^8$   |
| C <sub>5</sub>        | $u^8 + 3u^7 + 7u^6 + 10u^5 + 11u^4 + 10u^3 + 6u^2 + 4u + 1$ |
| <i>C</i> <sub>6</sub> | $u^8 + u^7 - u^6 - 2u^5 + u^4 + 2u^3 - 2u - 1$              |
| c <sub>8</sub>        | $u^8 - 3u^7 + 7u^6 - 10u^5 + 11u^4 - 10u^3 + 6u^2 - 4u + 1$ |
| <i>c</i> <sub>9</sub> | $u^8 - u^7 - 3u^6 + 2u^5 + 3u^4 - 2u - 1$                   |
| $c_{10}, c_{12}$      | $u^8 + u^7 - 3u^6 - 2u^5 + 3u^4 + 2u - 1$                   |
| $c_{11}$              | $u^8 - u^7 - u^6 + 2u^5 + u^4 - 2u^3 + 2u - 1$              |

## (v) Riley Polynomials at the component

| Crossings             | Riley Polynomials at each crossing                           |
|-----------------------|--|
| $c_1, c_2, c_4$       | $(y-1)^8$  |
| $c_3, c_7$            | $y^8$  |
| $c_5, c_8$            | $y^8 + 5y^7 + 11y^6 + 6y^5 - 17y^4 - 34y^3 - 22y^2 - 4y + 1$ |
| $c_6, c_{11}$         | $y^8 - 3y^7 + 7y^6 - 10y^5 + 11y^4 - 10y^3 + 6y^2 - 4y + 1$  |
| $c_9, c_{10}, c_{12}$ | $y^8 - 7y^7 + 19y^6 - 22y^5 + 3y^4 + 14y^3 - 6y^2 - 4y + 1$  |

### (vi) Complex Volumes and Cusp Shapes

| Solutions to $I_1^v$      | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape          |
|---------------------------|---------------------------------------|---------------------|
| v = -1.230330 + 0.083902I |                                       |                     |
| a = 0                     | -3.80435 + 2.57849I                   | -1.56478 - 3.68514I |
| b = 0.855237 + 0.665892I  |                                       |                     |
| v = -1.230330 - 0.083902I |                                       |                     |
| a = 0                     | -3.80435 - 2.57849I                   | -1.56478 + 3.68514I |
| b = 0.855237 - 0.665892I  |                                       |                     |
| v = -0.370895 + 0.073482I |                                       |                     |
| a = 0                     | 0.73474 - 6.44354I                    | 8.02705 + 7.90662I  |
| b = -1.031810 + 0.655470I |                                       |                     |
| v = -0.370895 - 0.073482I |                                       |                     |
| a = 0                     | 0.73474 + 6.44354I                    | 8.02705 - 7.90662I  |
| b = -1.031810 - 0.655470I |                                       |                     |
| v = 0.337834              |                                       |                     |
| a = 0                     | 4.85780                               | 14.7400             |
| b = 1.09818               |                                       |                     |
| v = 1.21928 + 2.03110I    |                                       |                     |
| a = 0                     | -0.604279 + 1.131230I                 | -3.30729 + 4.28492I |
| b = -0.570868 + 0.730671I |                                       |                     |
| v = 1.21928 - 2.03110I    |                                       |                     |
| a = 0                     | -0.604279 - 1.131230I                 | -3.30729 - 4.28492I |
| b = -0.570868 - 0.730671I |                                       |                     |
| v = 2.42604               |                                       |                     |
| a = 0                     | -0.799899                             | 9.95010             |
| b = -0.603304             |                                       |                     |

IV. u-Polynomials

| Crossings       | u-Polynomials at each crossing   |
|-----------------|--|
| $c_1$           | $(u-1)^8(u^9 - 5u^8 + 12u^7 - 15u^6 + 9u^5 + u^4 - 4u^3 + 2u^2 + u - 1)$ $\cdot (u^{17} + 37u^{16} + \dots + u + 1)$   |
| $c_2$           | $(u-1)^8(u^9 + u^8 - 2u^7 - 3u^6 + u^5 + 3u^4 + 2u^3 - u - 1)$ $\cdot (u^{17} - 15u^{16} + \dots + 3u - 1)$  |
| $c_3$           | $u^{8}(u^{9} + u^{8} + 2u^{7} + u^{6} + 3u^{5} + u^{4} + 2u^{3} + u - 1)$ $\cdot (u^{17} + u^{16} + \dots + 384u - 256)$   |
| $c_4$           | $(u+1)^8(u^9 - u^8 - 2u^7 + 3u^6 + u^5 - 3u^4 + 2u^3 - u + 1)$ $\cdot (u^{17} - 15u^{16} + \dots + 3u - 1)$  |
| $c_5$           | $(u^{8} + 3u^{7} + 7u^{6} + 10u^{5} + 11u^{4} + 10u^{3} + 6u^{2} + 4u + 1)$ $\cdot (u^{9} + 3u^{8} + 8u^{7} + 13u^{6} + 17u^{5} + 17u^{4} + 12u^{3} + 6u^{2} + u - 1)$ $\cdot (u^{17} + 2u^{16} + \dots + 3u + 1)$ |
| $c_6$           | $u^{9}(u^{8} + u^{7} + \dots - 2u - 1)(u^{17} + u^{16} + \dots - 512u - 512)$  |
| $c_7$           | $u^{8}(u^{9} - u^{8} + 2u^{7} - u^{6} + 3u^{5} - u^{4} + 2u^{3} + u + 1)$ $\cdot (u^{17} + u^{16} + \dots + 384u - 256)$   |
| $c_8$           | $(u^{8} - 3u^{7} + 7u^{6} - 10u^{5} + 11u^{4} - 10u^{3} + 6u^{2} - 4u + 1)$ $\cdot (u^{9} - 3u^{8} + 8u^{7} - 13u^{6} + 17u^{5} - 17u^{4} + 12u^{3} - 6u^{2} + u + 1)$ $\cdot (u^{17} + 2u^{16} + \dots + 3u + 1)$ |
| $c_9$           | $(u+1)^{9}(u^{8}-u^{7}-3u^{6}+2u^{5}+3u^{4}-2u-1)$ $\cdot (u^{17}+16u^{16}+\cdots-11u+1)$  |
| c <sub>10</sub> | $(u^{8} + u^{7} - 3u^{6} - 2u^{5} + 3u^{4} + 2u - 1)$ $\cdot (u^{9} + 2u^{8} + 5u^{7} + 22u^{6} + 52u^{5} + 63u^{4} + 41u^{3} + 10u^{2} - 2u - 1)$ $\cdot (u^{17} - 3u^{16} + \dots - 167922u - 192217)$           |
| $c_{11}$        | $(u^{8} - u^{7} - u^{6} + 2u^{5} + u^{4} - 2u^{3} + 2u - 1)$ $\cdot (u^{9} + 3u^{8} + 3u^{7} - 2u^{6} + u^{5} - 9u^{4} + 3u^{3} + 2u - 1)$ $\cdot (u^{17} - 6u^{16} + \dots - 19686u + 2393)$                      |
| $c_{12}$        | $(u-1)^{9}(u^{8} + u^{7} - 3u^{6} + 2u^{5} + 3u^{4} + 2u - 1)$ $\cdot (u^{17} + 16u^{16} + \dots - 11u + 1)$   |

### V. Riley Polynomials

| Crossings       | Riley Polynomials at each crossing   |
|-----------------|--|
| $c_1$           | $(y-1)^{8}(y^{9} - y^{8} + 12y^{7} - 7y^{6} + 37y^{5} + y^{4} - 10y^{2} + 5y - 1)$ $\cdot (y^{17} - 57y^{16} + \dots - 7859y - 1)$   |
| $c_2, c_4$      | $(y-1)^{8}(y^{9} - 5y^{8} + 12y^{7} - 15y^{6} + 9y^{5} + y^{4} - 4y^{3} + 2y^{2} + y - 1)$ $\cdot (y^{17} - 37y^{16} + \dots + y - 1)$   |
| $c_3, c_7$      | $y^{8}(y^{9} + 3y^{8} + 8y^{7} + 13y^{6} + 17y^{5} + 17y^{4} + 12y^{3} + 6y^{2} + y - 1)$ $\cdot (y^{17} - 33y^{16} + \dots + 245760y - 65536)$  |
| $c_5, c_8$      | $(y^{8} + 5y^{7} + 11y^{6} + 6y^{5} - 17y^{4} - 34y^{3} - 22y^{2} - 4y + 1)$ $\cdot (y^{9} + 7y^{8} + 20y^{7} + 25y^{6} + 5y^{5} - 15y^{4} + 22y^{2} + 13y - 1)$ $\cdot (y^{17} + 12y^{16} + \dots + 25y - 1)$ |
| $c_6$           | $y^{9}(y^{8} - 3y^{7} + 7y^{6} - 10y^{5} + 11y^{4} - 10y^{3} + 6y^{2} - 4y + 1)$ $\cdot (y^{17} - 39y^{16} + \dots + 3670016y - 262144)$   |
| $c_9, c_{12}$   | $(y-1)^{9}(y^{8}-7y^{7}+19y^{6}-22y^{5}+3y^{4}+14y^{3}-6y^{2}-4y+1)$ $\cdot (y^{17}-40y^{16}+\cdots+221y-1)$   |
| $c_{10}$        | $(y^8 - 7y^7 + 19y^6 - 22y^5 + 3y^4 + 14y^3 - 6y^2 - 4y + 1)$ $\cdot (y^9 + 6y^8 + \dots + 24y - 1)$ $\cdot (y^{17} - 45y^{16} + \dots + 806894237728y - 36947375089)$   |
| c <sub>11</sub> | $(y^8 - 3y^7 + 7y^6 - 10y^5 + 11y^4 - 10y^3 + 6y^2 - 4y + 1)$ $\cdot (y^9 - 3y^8 + 23y^7 + 62y^6 - 13y^5 - 57y^4 + 9y^3 - 6y^2 + 4y - 1)$ $\cdot (y^{17} - 38y^{16} + \dots + 475084108y - 5726449)$           |