

Ideals for irreducible components<sup>2</sup> of  $X_{par}$ 

$$I_1^u = \langle u^9 + u^8 - 4u^7 - 3u^6 + 5u^5 + u^4 - 2u^3 + 2u^2 + u + 1 \rangle$$

\* 1 irreducible components of  $\dim_{\mathbb{C}} = 0$ , with total 9 representations.

<sup>&</sup>lt;sup>1</sup>The image of knot diagram is generated by the software "**Draw programme**" developed by Andrew Bartholomew(http://www.layer8.co.uk/maths/draw/index.htm#Running-draw), where we modified some parts for our purpose(https://github.com/CATsTAILs/LinksPainter).

<sup>&</sup>lt;sup>2</sup> All coefficients of polynomials are rational numbers. But the coefficients are sometimes approximated in decimal forms when there is not enough margin.

I. 
$$I_1^u = \langle u^9 + u^8 - 4u^7 - 3u^6 + 5u^5 + u^4 - 2u^3 + 2u^2 + u + 1 \rangle$$

(i) Arc colorings

$$a_{2} = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_{7} = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{6} = \begin{pmatrix} 1 \\ u^{2} \end{pmatrix}$$

$$a_{1} = \begin{pmatrix} -u \\ -u^{3} + u \end{pmatrix}$$

$$a_{5} = \begin{pmatrix} -u^{2} + 1 \\ -u^{4} + 2u^{2} \end{pmatrix}$$

$$a_{3} = \begin{pmatrix} u^{5} - 2u^{3} + u \\ u^{7} - 3u^{5} + 2u^{3} + u \end{pmatrix}$$

$$a_{4} = \begin{pmatrix} -u^{4} + u^{2} + 1 \\ -u^{4} + 2u^{2} \end{pmatrix}$$

$$a_{8} = \begin{pmatrix} u^{8} - 3u^{6} + u^{4} + 2u^{2} + 1 \\ u^{8} - 4u^{6} + 4u^{4} \end{pmatrix}$$

- (ii) Obstruction class = -1
- (iii) Cusp Shapes =  $-4u^6 + 12u^4 4u^3 8u^2 + 8u + 2$

## (iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
$c_1, c_5, c_6$	$u^9 - u^8 - 4u^7 + 3u^6 + 5u^5 - u^4 - 2u^3 - 2u^2 + u - 1$
$c_2$	$u^9 + 3u^8 + 2u^7 - 5u^6 - u^5 + 13u^4 + 10u^3 - 2u^2 + u + 3$
$c_3, c_4, c_7$ $c_8$	$u^9 - u^8 + 6u^7 - 5u^6 + 11u^5 - 7u^4 + 6u^3 - 2u^2 + u - 1$

## (v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
$c_1, c_5, c_6$	$y^9 - 9y^8 + 32y^7 - 55y^6 + 45y^5 - 19y^4 + 16y^3 - 10y^2 - 3y - 1$
$c_2$	$y^9 - 5y^8 + 32y^7 - 87y^6 + 185y^5 - 223y^4 + 180y^3 - 62y^2 + 13y - 9$
$c_3, c_4, c_7$ $c_8$	$y^9 + 11y^8 + 48y^7 + 105y^6 + 121y^5 + 73y^4 + 20y^3 - 6y^2 - 3y - 1$

## (vi) Complex Volumes and Cusp Shapes

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
u = 0.482242 + 0.666986I	7.06362 + 2.21388I	4.24115 - 3.04598I
u = 0.482242 - 0.666986I	7.06362 - 2.21388I	4.24115 + 3.04598I
u = -1.28056	2.83680	1.66670
u = 1.380230 + 0.162431I	5.16280 + 3.41073I	5.88238 - 4.39642I
u = 1.380230 - 0.162431I	5.16280 - 3.41073I	5.88238 + 4.39642I
u = -0.230908 + 0.456719I	0.035384 - 1.109690I	0.55374 + 6.23947I
u = -0.230908 - 0.456719I	0.035384 + 1.109690I	0.55374 - 6.23947I
u = -1.49128 + 0.23430I	13.4612 - 5.5005I	7.48937 + 2.97298I
u = -1.49128 - 0.23430I	13.4612 + 5.5005I	7.48937 - 2.97298I

II. u-Polynomials

Crossings	u-Polynomials at each crossing
$c_1, c_5, c_6$	$u^9 - u^8 - 4u^7 + 3u^6 + 5u^5 - u^4 - 2u^3 - 2u^2 + u - 1$
$c_2$	$u^9 + 3u^8 + 2u^7 - 5u^6 - u^5 + 13u^4 + 10u^3 - 2u^2 + u + 3$
$c_3, c_4, c_7$ $c_8$	$u^9 - u^8 + 6u^7 - 5u^6 + 11u^5 - 7u^4 + 6u^3 - 2u^2 + u - 1$

III. Riley Polynomials

Crossings	Riley Polynomials at each crossing
$c_1, c_5, c_6$	$y^9 - 9y^8 + 32y^7 - 55y^6 + 45y^5 - 19y^4 + 16y^3 - 10y^2 - 3y - 1$
$c_2$	$y^9 - 5y^8 + 32y^7 - 87y^6 + 185y^5 - 223y^4 + 180y^3 - 62y^2 + 13y - 9$
$c_3, c_4, c_7$ $c_8$	$y^9 + 11y^8 + 48y^7 + 105y^6 + 121y^5 + 73y^4 + 20y^3 - 6y^2 - 3y - 1$