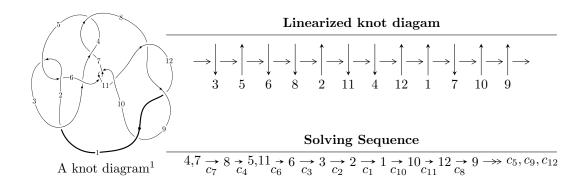
# $12a_{0008} (K12a_{0008})$



#### Ideals for irreducible components<sup>2</sup> of $X_{par}$

$$\begin{split} I_1^u &= \langle -3.82254 \times 10^{339} u^{104} - 5.03783 \times 10^{339} u^{103} + \dots + 5.84724 \times 10^{339} b - 5.55902 \times 10^{342}, \\ &1.82294 \times 10^{340} u^{104} + 2.22909 \times 10^{340} u^{103} + \dots + 2.33889 \times 10^{340} a + 2.44212 \times 10^{343}, \\ &u^{105} + 2u^{104} + \dots + 2048u + 1024 \rangle \\ I_2^u &= \langle b, -u^4 + 2u^3 + u^2 + a - 3u, \ u^5 - u^4 - 2u^3 + u^2 + u + 1 \rangle \\ \\ I_1^v &= \langle a, -152v^9 + 36v^8 - 216v^7 + 881v^6 - 468v^5 + 684v^4 - 1376v^3 + 252v^2 + 115b - 144v + 219, \\ &v^{10} - v^9 + 2v^8 - 7v^7 + 8v^6 - 9v^5 + 14v^4 - 10v^3 + 5v^2 - 3v + 1 \rangle \end{split}$$

\* 3 irreducible components of  $\dim_{\mathbb{C}} = 0$ , with total 120 representations.

<sup>&</sup>lt;sup>1</sup>The image of knot diagram is generated by the software "**Draw programme**" developed by Andrew Bartholomew(http://www.layer8.co.uk/maths/draw/index.htm#Running-draw), where we modified some parts for our purpose(https://github.com/CATsTAILs/LinksPainter).

 $<sup>^2</sup>$  All coefficients of polynomials are rational numbers. But the coefficients are sometimes approximated in decimal forms when there is not enough margin.

I. 
$$I_1^u = \langle -3.82 \times 10^{339} u^{104} - 5.04 \times 10^{339} u^{103} + \dots + 5.85 \times 10^{339} b - 5.56 \times 10^{342}, \ 1.82 \times 10^{340} u^{104} + 2.23 \times 10^{340} u^{103} + \dots + 2.34 \times 10^{340} a + 2.44 \times 10^{343}, \ u^{105} + 2u^{104} + \dots + 2048 u + 1024 \rangle$$

(i) Arc colorings

$$a_{4} = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_{7} = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{8} = \begin{pmatrix} 1 \\ u^{2} \end{pmatrix}$$

$$a_{5} = \begin{pmatrix} -u \\ -u^{3} + u \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} -0.779404u^{104} - 0.953053u^{103} + \cdots - 752.424u - 1044.13 \\ 0.653735u^{104} + 0.861575u^{103} + \cdots + 591.500u + 950.710 \end{pmatrix}$$

$$a_{6} = \begin{pmatrix} 1.76035u^{104} + 1.98543u^{103} + \cdots + 1749.68u + 2063.65 \\ -0.847121u^{104} - 1.09653u^{103} + \cdots - 781.787u - 1191.48 \end{pmatrix}$$

$$a_{3} = \begin{pmatrix} 0.959231u^{104} + 1.22999u^{103} + \cdots + 905.222u + 1333.17 \\ -1.35472u^{104} - 1.62405u^{103} + \cdots - 1278.29u - 1734.35 \end{pmatrix}$$

$$a_{2} = \begin{pmatrix} 1.51533u^{104} + 1.88583u^{103} + \cdots + 1422.48u + 2030.46 \\ -1.52651u^{104} - 1.83959u^{103} + \cdots - 1430.38u - 1964.33 \end{pmatrix}$$

$$a_{1} = \begin{pmatrix} -0.913226u^{104} - 0.888902u^{103} + \cdots - 1430.38u - 1964.33 \\ -1.79713u^{104} - 2.06159u^{103} + \cdots - 1766.75u - 2151.53 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} -0.125669u^{104} - 0.0914777u^{103} + \cdots - 160.924u - 93.4241 \\ 0.653735u^{104} + 0.861575u^{103} + \cdots + 591.500u + 950.710 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} -1.50997u^{104} - 1.64956u^{103} + \cdots - 1556.56u - 1732.04 \\ -0.184220u^{104} - 0.158133u^{103} + \cdots - 191.728u - 159.602 \end{pmatrix}$$

$$a_{9} = \begin{pmatrix} -0.561315u^{104} - 0.724978u^{103} + \cdots - 476.369u - 771.780 \\ 1.00686u^{104} + 1.15100u^{103} + \cdots + 1010.56u + 1206.98 \end{pmatrix}$$

- (ii) Obstruction class = -1
- (iii) Cusp Shapes =  $-1.68427u^{104} 1.92328u^{103} + \cdots 1794.45u 2081.91$

### (iv) u-Polynomials at the component

| Crossings          | u-Polynomials at each crossing                |
|--------------------|---|
| $c_1$              | $u^{105} + 53u^{104} + \dots - 7u - 1$        |
| $c_2, c_5$         | $u^{105} + 7u^{104} + \dots + 7u + 1$         |
| $c_3$              | $u^{105} - 7u^{104} + \dots + 40669u + 23377$ |
| $c_4, c_7$         | $u^{105} + 2u^{104} + \dots + 2048u + 1024$   |
| $c_6, c_{10}$      | $u^{105} + 3u^{104} + \dots + 96u + 32$       |
| $c_8, c_9, c_{12}$ | $u^{105} + 8u^{104} + \dots + 2u + 1$         |
| $c_{11}$           | $u^{105} - 39u^{104} + \dots - 14848u + 1024$ |

## (v) Riley Polynomials at the component

| Crossings          | Riley Polynomials at each crossing                      |
|--------------------|---|
| $c_1$              | $y^{105} + 5y^{104} + \dots - 47y - 1$                  |
| $c_2, c_5$         | $y^{105} + 53y^{104} + \dots - 7y - 1$                  |
| $c_3$              | $y^{105} - 43y^{104} + \dots + 5130220969y - 546484129$ |
| $c_4, c_7$         | $y^{105} - 60y^{104} + \dots + 25165824y - 1048576$     |
| $c_6, c_{10}$      | $y^{105} + 39y^{104} + \dots - 14848y - 1024$           |
| $c_8, c_9, c_{12}$ | $y^{105} - 90y^{104} + \dots - 206y - 1$                |
| $c_{11}$           | $y^{105} + 47y^{104} + \dots - 210108416y - 1048576$    |

## (vi) Complex Volumes and Cusp Shapes

| Solutions to $I_1^u$      | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape |
|---------------------------|---------------------------------------|------------|
| u = 0.966623 + 0.262000I  |                                       |            |
| a = 1.84206 - 0.44039I    | -0.62620 - 5.04939I                   | 0          |
| b = 0.613331 + 0.897632I  |                                       |            |
| u = 0.966623 - 0.262000I  |                                       |            |
| a = 1.84206 + 0.44039I    | -0.62620 + 5.04939I                   | 0          |
| b = 0.613331 - 0.897632I  |                                       |            |
| u = -0.994592 + 0.126675I |                                       |            |
| a = -0.11789 + 1.79257I   | -1.41343 + 1.12338I                   | 0          |
| b = -0.244604 - 1.112200I |                                       |            |
| u = -0.994592 - 0.126675I |                                       |            |
| a = -0.11789 - 1.79257I   | -1.41343 - 1.12338I                   | 0          |
| b = -0.244604 + 1.112200I |                                       |            |
| u = -0.156135 + 0.971665I |                                       |            |
| a = 0.04677 - 1.83355I    | 0.09747 - 2.29231I                    | 0          |
| b = 0.595883 + 0.703683I  |                                       |            |
| u = -0.156135 - 0.971665I |                                       |            |
| a = 0.04677 + 1.83355I    | 0.09747 + 2.29231I                    | 0          |
| b = 0.595883 - 0.703683I  |                                       |            |
| u = 0.996817 + 0.231114I  |                                       |            |
| a = -0.119338 - 0.216906I | 0.82031 - 3.49410I                    | 0          |
| b = 1.148970 + 0.105590I  |                                       |            |
| u = 0.996817 - 0.231114I  |                                       |            |
| a = -0.119338 + 0.216906I | 0.82031 + 3.49410I                    | 0          |
| b = 1.148970 - 0.105590I  |                                       |            |
| u = 0.830770 + 0.624559I  |                                       |            |
| a = 0.50740 - 1.47941I    | 8.20664 - 3.74731I                    | 0          |
| b = 0.195587 + 1.292660I  |                                       |            |
| u = 0.830770 - 0.624559I  |                                       |            |
| a = 0.50740 + 1.47941I    | 8.20664 + 3.74731I                    | 0          |
| b = 0.195587 - 1.292660I  |                                       |            |

| Solutions to $I_1^u$      | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape |
|---------------------------|---------------------------------------|------------|
| u = -1.06842              |                                       |            |
| a = -0.124114             | -1.78436                              | 0          |
| b = -0.549124             |                                       |            |
| u = 0.289155 + 1.029210I  |                                       |            |
| a = 0.010911 - 1.335340I  | 0.42759 + 4.73730I                    | 0          |
| b = 0.859812 + 0.584753I  |                                       |            |
| u = 0.289155 - 1.029210I  |                                       |            |
| a = 0.010911 + 1.335340I  | 0.42759 - 4.73730I                    | 0          |
| b = 0.859812 - 0.584753I  |                                       |            |
| u = -0.765537 + 0.753961I |                                       |            |
| a = 1.22243 + 0.93816I    | 6.95108 - 3.58416I                    | 0          |
| b = -0.075655 - 1.140690I |                                       |            |
| u = -0.765537 - 0.753961I |                                       |            |
| a = 1.22243 - 0.93816I    | 6.95108 + 3.58416I                    | 0          |
| b = -0.075655 + 1.140690I |                                       |            |
| u = 0.298691 + 1.037650I  |                                       |            |
| a = -0.200218 + 1.183490I | 4.62024 + 5.96188I                    | 0          |
| b = 0.621372 - 1.078950I  |                                       |            |
| u = 0.298691 - 1.037650I  |                                       |            |
| a = -0.200218 - 1.183490I | 4.62024 - 5.96188I                    | 0          |
| b = 0.621372 + 1.078950I  |                                       |            |
| u = -0.915190 + 0.048307I |                                       |            |
| a = 1.57055 - 0.49914I    | -0.915909 - 0.241093I                 | 0          |
| b = 0.606566 - 0.808414I  |                                       |            |
| u = -0.915190 - 0.048307I |                                       |            |
| a = 1.57055 + 0.49914I    | -0.915909 + 0.241093I                 | 0          |
| b = 0.606566 + 0.808414I  |                                       |            |
| u = -0.951368 + 0.522622I |                                       |            |
| a = 0.38217 + 1.61581I    | 6.29716 + 8.47800I                    | 0          |
| b = 0.252648 - 1.368440I  |                                       |            |

| Solutions to $I_1^u$      | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape |
|---------------------------|---------------------------------------|------------|
| u = -0.951368 - 0.522622I |                                       |            |
| a = 0.38217 - 1.61581I    | 6.29716 - 8.47800I                    | 0          |
| b = 0.252648 + 1.368440I  |                                       |            |
| u = 0.771518 + 0.768489I  |                                       |            |
| a = 0.94253 - 1.18145I    | 8.47050 - 1.50689I                    | 0          |
| b = 0.017151 + 1.183720I  |                                       |            |
| u = 0.771518 - 0.768489I  |                                       |            |
| a = 0.94253 + 1.18145I    | 8.47050 + 1.50689I                    | 0          |
| b = 0.017151 - 1.183720I  |                                       |            |
| u = -1.075900 + 0.190627I |                                       |            |
| a = -1.365470 + 0.159370I | 3.68939 + 3.33964I                    | 0          |
| b = -0.603761 + 1.042000I |                                       |            |
| u = -1.075900 - 0.190627I |                                       |            |
| a = -1.365470 - 0.159370I | 3.68939 - 3.33964I                    | 0          |
| b = -0.603761 - 1.042000I |                                       |            |
| u = -0.651392 + 0.879936I |                                       |            |
| a = 0.393010 + 0.894053I  | 3.44940 + 2.87203I                    | 0          |
| b = 0.194470 - 0.994625I  |                                       |            |
| u = -0.651392 - 0.879936I |                                       |            |
| a = 0.393010 - 0.894053I  | 3.44940 - 2.87203I                    | 0          |
| b = 0.194470 + 0.994625I  |                                       |            |
| u = -1.050100 + 0.314666I |                                       |            |
| a = -0.22948 - 1.92157I   | -0.96727 + 5.99715I                   | 0          |
| b = -0.037303 + 1.113740I |                                       |            |
| u = -1.050100 - 0.314666I |                                       |            |
| a = -0.22948 + 1.92157I   | -0.96727 - 5.99715I                   | 0          |
| b = -0.037303 - 1.113740I |                                       |            |
| u = -0.835876 + 0.304185I |                                       |            |
| a = -1.05229 - 1.03238I   | 2.39540 + 3.43521I                    | 0          |
| b = -0.825475 - 0.471650I |                                       |            |

| Solutions to $I_1^u$      | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape |
|---------------------------|---------------------------------------|------------|
| u = -0.835876 - 0.304185I |                                       |            |
| a = -1.05229 + 1.03238I   | 2.39540 - 3.43521I                    | 0          |
| b = -0.825475 + 0.471650I |                                       |            |
| u = 0.082150 + 1.110590I  |                                       |            |
| a = 0.169904 + 1.176230I  | -3.28334 + 1.14216I                   | 0          |
| b = -0.700136 - 0.769483I |                                       |            |
| u = 0.082150 - 1.110590I  |                                       |            |
| a = 0.169904 - 1.176230I  | -3.28334 - 1.14216I                   | 0          |
| b = -0.700136 + 0.769483I |                                       |            |
| u = 0.208245 + 0.860687I  |                                       |            |
| a = 0.059506 - 1.353310I  | -0.20460 + 2.27131I                   | 0          |
| b = -0.575289 + 0.870092I |                                       |            |
| u = 0.208245 - 0.860687I  |                                       |            |
| a = 0.059506 + 1.353310I  | -0.20460 - 2.27131I                   | 0          |
| b = -0.575289 - 0.870092I |                                       |            |
| u = 1.096560 + 0.354630I  |                                       |            |
| a = -1.50864 + 0.44399I   | 4.17470 - 8.90495I                    | 0          |
| b = -0.649802 - 1.079910I |                                       |            |
| u = 1.096560 - 0.354630I  |                                       |            |
| a = -1.50864 - 0.44399I   | 4.17470 + 8.90495I                    | 0          |
| b = -0.649802 + 1.079910I |                                       |            |
| u = 0.771031 + 0.344389I  |                                       |            |
| a = -0.34801 + 1.88152I   | 1.31907 - 1.85367I                    | 0          |
| b = -0.033449 - 0.956974I |                                       |            |
| u = 0.771031 - 0.344389I  |                                       |            |
| a = -0.34801 - 1.88152I   | 1.31907 + 1.85367I                    | 0          |
| b = -0.033449 + 0.956974I |                                       |            |
| u = -0.303689 + 1.129670I |                                       |            |
| a = 0.198606 + 1.374610I  | -2.80313 - 6.42495I                   | 0          |
| b = -0.673059 - 0.926013I |                                       |            |

| Solutions to $I_1^u$      | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape          |
|---------------------------|---------------------------------------|---------------------|
| u = -0.303689 - 1.129670I |                                       |                     |
| a = 0.198606 - 1.374610I  | -2.80313 + 6.42495I                   | 0                   |
| b = -0.673059 + 0.926013I |                                       |                     |
| u = -0.323418 + 0.718994I |                                       |                     |
| a = 0.351226 + 1.099770I  | 2.66939 - 0.70616I                    | 3.86014 + 0.I       |
| b = 0.817506 - 0.395832I  |                                       |                     |
| u = -0.323418 - 0.718994I |                                       |                     |
| a = 0.351226 - 1.099770I  | 2.66939 + 0.70616I                    | 3.86014 + 0.I       |
| b = 0.817506 + 0.395832I  |                                       |                     |
| u = -0.783043 + 0.032782I |                                       |                     |
| a = 0.05152 - 1.49817I    | 5.03761 - 2.14522I                    | -2.62234 - 0.68124I |
| b = 0.456650 + 1.312500I  |                                       |                     |
| u = -0.783043 - 0.032782I |                                       |                     |
| a = 0.05152 + 1.49817I    | 5.03761 + 2.14522I                    | -2.62234 + 0.68124I |
| b = 0.456650 - 1.312500I  |                                       |                     |
| u = -0.069329 + 1.225860I |                                       |                     |
| a = -0.207633 - 1.035880I | 0.91219 - 2.50907I                    | 0                   |
| b = 0.608931 + 0.965031I  |                                       |                     |
| u = -0.069329 - 1.225860I |                                       |                     |
| a = -0.207633 + 1.035880I | 0.91219 + 2.50907I                    | 0                   |
| b = 0.608931 - 0.965031I  |                                       |                     |
| u = 1.170060 + 0.463549I  |                                       |                     |
| a = -1.10322 + 1.53284I   | -0.62425 - 2.83456I                   | 0                   |
| b = -0.553441 - 0.934425I |                                       |                     |
| u = 1.170060 - 0.463549I  |                                       |                     |
| a = -1.10322 - 1.53284I   | -0.62425 + 2.83456I                   | 0                   |
| b = -0.553441 + 0.934425I |                                       |                     |
| u = -0.476116 + 0.565252I |                                       |                     |
| a = -0.304758 - 0.867417I | -0.87676 + 1.33458I                   | -5.87002 - 4.06416I |
| b = -0.445573 + 0.493036I |                                       |                     |

| Solutions to $I_1^u$       | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape          |
|----------------------------|---------------------------------------|---------------------|
| u = -0.476116 - 0.565252I  |                                       |                     |
| a = -0.304758 + 0.867417I  | -0.87676 - 1.33458I                   | -5.87002 + 4.06416I |
| b = -0.445573 - 0.493036I  |                                       |                     |
| u = 0.454580 + 0.569119I   |                                       |                     |
| a = -0.43556 + 2.37608I    | 1.83393 - 1.25356I                    | 7.30757 + 1.79196I  |
| b = 0.170218 - 0.693124I   |                                       |                     |
| u = 0.454580 - 0.569119I   |                                       |                     |
| a = -0.43556 - 2.37608I    | 1.83393 + 1.25356I                    | 7.30757 - 1.79196I  |
| b = 0.170218 + 0.693124I   |                                       |                     |
| u = -0.408160 + 1.210580I  |                                       |                     |
| a = -0.294514 - 1.182610I  | 1.90832 - 10.51360I                   | 0                   |
| b = 0.694328 + 1.069540I   |                                       |                     |
| u = -0.408160 - 1.210580I  |                                       |                     |
| a = -0.294514 + 1.182610I  | 1.90832 + 10.51360I                   | 0                   |
| b = 0.694328 - 1.069540I   |                                       |                     |
| u = -0.608380 + 0.375672I  |                                       |                     |
| a = 0.257068 + 0.458626I   | 2.88842 - 0.29217I                    | 2.82331 - 1.55863I  |
| b = 0.964533 - 0.182230I   |                                       |                     |
| u = -0.608380 - 0.375672I  |                                       |                     |
| a = 0.257068 - 0.458626I   | 2.88842 + 0.29217I                    | 2.82331 + 1.55863I  |
| b = 0.964533 + 0.182230I   |                                       |                     |
| u = -1.190280 + 0.531474I  |                                       |                     |
| a = -0.038155 - 0.170848I  | -0.03711 + 5.60715I                   | 0                   |
| b = -1.015260 - 0.612676I  |                                       |                     |
| u = -1.190280 - 0.531474I  |                                       |                     |
| a = -0.038155 + 0.170848I  | -0.03711 - 5.60715I                   | 0                   |
| b = -1.015260 + 0.612676I  |                                       |                     |
| u = 1.296260 + 0.215123I   |                                       |                     |
| a = 0.0286880 + 0.1014560I | -5.00588 - 4.15826I                   | 0                   |
| b = -0.625259 - 0.034743I  |                                       |                     |

| Solutions to $I_1^u$       | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape          |
|----------------------------|---------------------------------------|---------------------|
| u = 1.296260 - 0.215123I   |                                       |                     |
| a = 0.0286880 - 0.1014560I | -5.00588 + 4.15826I                   | 0                   |
| b = -0.625259 + 0.034743I  |                                       |                     |
| u = 0.540659 + 0.417528I   |                                       |                     |
| a = -0.08495 - 1.56537I    | 0.46462 + 2.21286I                    | 0.18906 - 1.66288I  |
| b = -0.396115 + 0.965766I  |                                       |                     |
| u = 0.540659 - 0.417528I   |                                       |                     |
| a = -0.08495 + 1.56537I    | 0.46462 - 2.21286I                    | 0.18906 + 1.66288I  |
| b = -0.396115 - 0.965766I  |                                       |                     |
| u = -1.262590 + 0.406275I  |                                       |                     |
| a = 0.043597 + 0.144135I   | -4.49634 + 1.94814I                   | 0                   |
| b = 0.808161 + 0.651447I   |                                       |                     |
| u = -1.262590 - 0.406275I  |                                       |                     |
| a = 0.043597 - 0.144135I   | -4.49634 - 1.94814I                   | 0                   |
| b = 0.808161 - 0.651447I   |                                       |                     |
| u = 0.501894 + 0.449298I   |                                       |                     |
| a = -0.061381 + 1.371720I  | 6.13895 + 5.63139I                    | 4.44596 + 0.50184I  |
| b = 0.532459 - 1.225220I   |                                       |                     |
| u = 0.501894 - 0.449298I   |                                       |                     |
| a = -0.061381 - 1.371720I  | 6.13895 - 5.63139I                    | 4.44596 - 0.50184I  |
| b = 0.532459 + 1.225220I   |                                       |                     |
| u = 0.538287 + 0.382734I   |                                       |                     |
| a = -2.47342 + 2.53276I    | 1.79965 - 1.45383I                    | 6.85530 + 8.54654I  |
| b = -0.174232 - 0.605006I  |                                       |                     |
| u = 0.538287 - 0.382734I   |                                       |                     |
| a = -2.47342 - 2.53276I    | 1.79965 + 1.45383I                    | 6.85530 - 8.54654I  |
| b = -0.174232 + 0.605006I  |                                       |                     |
| u = 0.650695 + 0.088990I   |                                       |                     |
| a = -3.07569 + 1.05876I    | 2.01640 + 1.51491I                    | -4.95811 - 2.51475I |
| b = -0.634565 + 0.388641I  |                                       |                     |

| Solutions to $I_1^u$      | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape          |
|---------------------------|---------------------------------------|---------------------|
| u = 0.650695 - 0.088990I  |                                       |                     |
| a = -3.07569 - 1.05876I   | 2.01640 - 1.51491I                    | -4.95811 + 2.51475I |
| b = -0.634565 - 0.388641I |                                       |                     |
| u = -1.315550 + 0.292996I |                                       |                     |
| a = -0.87266 - 1.20760I   | -5.04079 - 0.55525I                   | 0                   |
| b = -0.680138 + 0.916140I |                                       |                     |
| u = -1.315550 - 0.292996I |                                       |                     |
| a = -0.87266 + 1.20760I   | -5.04079 + 0.55525I                   | 0                   |
| b = -0.680138 - 0.916140I |                                       |                     |
| u = 1.241410 + 0.559646I  |                                       |                     |
| a = 1.06522 - 1.30685I    | -3.33108 - 7.60318I                   | 0                   |
| b = 0.693688 + 1.030650I  |                                       |                     |
| u = 1.241410 - 0.559646I  |                                       |                     |
| a = 1.06522 + 1.30685I    | -3.33108 + 7.60318I                   | 0                   |
| b = 0.693688 - 1.030650I  |                                       |                     |
| u = 1.313810 + 0.373086I  |                                       |                     |
| a = -0.235478 - 0.167465I | -4.67411 - 2.30128I                   | 0                   |
| b = -0.969130 + 0.703808I |                                       |                     |
| u = 1.313810 - 0.373086I  |                                       |                     |
| a = -0.235478 + 0.167465I | -4.67411 + 2.30128I                   | 0                   |
| b = -0.969130 - 0.703808I |                                       |                     |
| u = -0.406323 + 0.472980I |                                       |                     |
| a = -2.61611 - 2.10864I   | 0.98116 - 2.85208I                    | 4.87688 + 0.20930I  |
| b = 0.043443 + 0.684550I  |                                       |                     |
| u = -0.406323 - 0.472980I |                                       |                     |
| a = -2.61611 + 2.10864I   | 0.98116 + 2.85208I                    | 4.87688 - 0.20930I  |
| b = 0.043443 - 0.684550I  |                                       |                     |
| u = -1.266110 + 0.561926I |                                       |                     |
| a = -0.90672 - 1.64848I   | -3.30268 + 7.81911I                   | 0                   |
| b = -0.563296 + 1.011730I |                                       |                     |

| Solutions to $I_1^u$        | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape |
|-----------------------------|---------------------------------------|------------|
| u = -1.266110 - 0.561926I   |                                       |            |
| a = -0.90672 + 1.64848I     | -3.30268 - 7.81911I                   | 0          |
| b = -0.563296 - 1.011730I   |                                       |            |
| u = 1.268350 + 0.617290I    |                                       |            |
| a = 0.147260 + 0.059650I    | -2.66171 - 10.71770I                  | 0          |
| b = -1.069350 + 0.631867I   |                                       |            |
| u = 1.268350 - 0.617290I    |                                       |            |
| a = 0.147260 - 0.059650I    | -2.66171 + 10.71770I                  | 0          |
| b = -1.069350 - 0.631867I   |                                       |            |
| u = 1.26411 + 0.64010I      |                                       |            |
| a = -0.98809 + 1.20593I     | 1.61848 - 12.04680I                   | 0          |
| b = -0.756688 - 1.129680I   |                                       |            |
| u = 1.26411 - 0.64010I      |                                       |            |
| a = -0.98809 - 1.20593I     | 1.61848 + 12.04680I                   | 0          |
| b = -0.756688 + 1.129680I   |                                       |            |
| u = -1.39616 + 0.27043I     |                                       |            |
| a = -0.0275538 - 0.1189400I | -1.12946 - 1.52913I                   | 0          |
| b = -0.530086 - 0.789172I   |                                       |            |
| u = -1.39616 - 0.27043I     |                                       |            |
| a = -0.0275538 + 0.1189400I | -1.12946 + 1.52913I                   | 0          |
| b = -0.530086 + 0.789172I   |                                       |            |
| u = -1.37101 + 0.42124I     |                                       |            |
| a = 0.833638 + 1.030930I    | -8.14449 + 4.19574I                   | 0          |
| b = 0.753137 - 0.991259I    |                                       |            |
| u = -1.37101 - 0.42124I     |                                       |            |
| a = 0.833638 - 1.030930I    | -8.14449 - 4.19574I                   | 0          |
| b = 0.753137 + 0.991259I    |                                       |            |
| u = 1.41210 + 0.25259I      |                                       |            |
| a = 0.182134 + 0.133509I    | -8.93146 + 1.75969I                   | 0          |
| b = 0.846007 - 0.737444I    |                                       |            |

| $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape  |
|---------------------------------------|---|
|                                       |   |
| -8.93146 - 1.75969I                   | 0   |
|                                       |   |
|                                       |   |
| -0.33339 + 1.65387I                   | -2.68049 - 4.66999I   |
|                                       |   |
|                                       |   |
| -0.33339 - 1.65387I                   | -2.68049 + 4.66999I   |
|                                       |   |
|                                       |   |
| -7.39202 - 6.95911I                   | 0   |
|                                       |   |
|                                       |   |
| -7.39202 + 6.95911I                   | 0   |
|                                       |   |
|                                       |   |
| -5.9958 + 12.8200I                    | 0   |
|                                       |   |
|                                       |   |
| -5.9958 - 12.8200I                    | 0   |
|                                       |   |
|                                       |   |
| -3.48041 + 8.68972I                   | 0   |
|                                       |   |
|                                       |   |
| -3.48041 - 8.68972I                   | 0   |
|                                       |   |
|                                       |   |
| -0.9805 + 17.4101I                    | 0   |
|                                       |   |
|                                       | -8.93146 - 1.75969I $-0.33339 + 1.65387I$ $-0.33339 - 1.65387I$ $-7.39202 - 6.95911I$ $-7.39202 + 6.95911I$ $-5.9958 + 12.8200I$ $-5.9958 - 12.8200I$ $-3.48041 + 8.68972I$ $-3.48041 - 8.68972I$ |

| Solutions to $I_1^u$       | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape |
|----------------------------|---------------------------------------|------------|
| u = -1.30301 - 0.72418I    |                                       |            |
| a = -0.85428 + 1.34318I    | -0.9805 - 17.4101I                    | 0          |
| b = -0.783365 - 1.149260I  |                                       |            |
| u = 1.52631 + 0.11647I     |                                       |            |
| a = -0.144120 - 0.089973I  | -5.42904 + 5.71768I                   | 0          |
| b = -0.648982 + 0.791673I  |                                       |            |
| u = 1.52631 - 0.11647I     |                                       |            |
| a = -0.144120 + 0.089973I  | -5.42904 - 5.71768I                   | 0          |
| b = -0.648982 - 0.791673I  |                                       |            |
| u = 1.49316 + 0.40751I     |                                       |            |
| a = 0.1032100 + 0.0283296I | -4.43944 - 3.45605I                   | 0          |
| b = -0.492837 + 0.689740I  |                                       |            |
| u = 1.49316 - 0.40751I     |                                       |            |
| a = 0.1032100 - 0.0283296I | -4.43944 + 3.45605I                   | 0          |
| b = -0.492837 - 0.689740I  |                                       |            |

II. 
$$I_2^u = \langle b, -u^4 + 2u^3 + u^2 + a - 3u, u^5 - u^4 - 2u^3 + u^2 + u + 1 \rangle$$

(i) Arc colorings

$$a_{4} = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_{7} = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{8} = \begin{pmatrix} 1 \\ u^{2} \end{pmatrix}$$

$$a_{5} = \begin{pmatrix} -u \\ -u^{3} + u \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} u^{4} - 2u^{3} - u^{2} + 3u \\ 0 \end{pmatrix}$$

$$a_{6} = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{3} = \begin{pmatrix} u \\ u \end{pmatrix}$$

$$a_{2} = \begin{pmatrix} u^{4} - u^{2} - 1 \\ u^{4} - 2u^{2} \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} -1 \\ -u^{2} \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} u^{4} - 2u^{3} - u^{2} + 3u \\ 0 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} u^{4} - 2u^{3} - u^{2} + 3u \\ 0 \end{pmatrix}$$

$$a_{9} = \begin{pmatrix} u^{4} - 2u^{3} - u^{2} + 3u + 1 \\ u^{2} \end{pmatrix}$$

- (ii) Obstruction class = 1
- (iii) Cusp Shapes =  $-2u^4 + 7u^3 + 7u^2 13u 6$

### (iv) u-Polynomials at the component

| Crossings             | u-Polynomials at each crossing    |
|-----------------------|-----------------------------------|
| $c_1$                 | $u^5 - 3u^4 + 4u^3 - u^2 - u + 1$ |
| $c_2$                 | $u^5 - u^4 + 2u^3 - u^2 + u - 1$  |
| $c_3, c_4$            | $u^5 + u^4 - 2u^3 - u^2 + u - 1$  |
| $c_5$                 | $u^5 + u^4 + 2u^3 + u^2 + u + 1$  |
| $c_6, c_{10}, c_{11}$ | $u^5$                             |
| C <sub>7</sub>        | $u^5 - u^4 - 2u^3 + u^2 + u + 1$  |
| $c_{8}, c_{9}$        | $(u+1)^5$                         |
| $c_{12}$              | $(u-1)^5$                         |

# (v) Riley Polynomials at the component

| Crossings             | Riley Polynomials at each crossing |
|-----------------------|------------------------------------|
| $c_1$                 | $y^5 - y^4 + 8y^3 - 3y^2 + 3y - 1$ |
| $c_{2}, c_{5}$        | $y^5 + 3y^4 + 4y^3 + y^2 - y - 1$  |
| $c_3, c_4, c_7$       | $y^5 - 5y^4 + 8y^3 - 3y^2 - y - 1$ |
| $c_6, c_{10}, c_{11}$ | $y^5$                              |
| $c_8, c_9, c_{12}$    | $(y-1)^5$                          |

# (vi) Complex Volumes and Cusp Shapes

| Solutions to $I_2^u$      | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape          |
|---------------------------|---------------------------------------|---------------------|
| u = -1.21774              |                                       |                     |
| a = 0.674363              | -0.756147                             | 3.17260             |
| b = 0                     |                                       |                     |
| u = -0.309916 + 0.549911I |                                       |                     |
| a = -1.29977 + 2.14694I   | 1.31583 + 1.53058I                    | -1.50865 - 9.87103I |
| b = 0                     |                                       |                     |
| u = -0.309916 - 0.549911I |                                       |                     |
| a = -1.29977 - 2.14694I   | 1.31583 - 1.53058I                    | -1.50865 + 9.87103I |
| b = 0                     |                                       |                     |
| u = 1.41878 + 0.21917I    |                                       |                     |
| a = 0.462589 - 0.146410I  | -4.22763 - 4.40083I                   | 0.92237 + 5.80708I  |
| b = 0                     |                                       |                     |
| u = 1.41878 - 0.21917I    |                                       |                     |
| a = 0.462589 + 0.146410I  | -4.22763 + 4.40083I                   | 0.92237 - 5.80708I  |
| b = 0                     |                                       |                     |

III. 
$$I_1^v = \langle a, -152v^9 + 36v^8 + \dots + 115b + 219, \ v^{10} - v^9 + \dots - 3v + 1 \rangle$$

#### (i) Arc colorings

$$a_{4} = \begin{pmatrix} v \\ 0 \end{pmatrix}$$

$$a_{7} = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{8} = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{5} = \begin{pmatrix} v \\ 0 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 1.32174v^{9} - 0.313043v^{8} + \dots + 1.25217v - 1.90435 \end{pmatrix}$$

$$a_{6} = \begin{pmatrix} 1.35652v^{9} - 0.373913v^{8} + \dots + 1.49565v - 0.191304 \end{pmatrix}$$

$$a_{3} = \begin{pmatrix} -0.982609v^{9} + 0.469565v^{8} + \dots - 2.87826v + 1.35652 \\ -2.35652v^{9} + 1.37391v^{8} + \dots - 6.49565v + 3.19130 \end{pmatrix}$$

$$a_{2} = \begin{pmatrix} -0.469565v^{9} + 0.321739v^{8} + \dots - 2.28696v + 0.373913 \\ -2.35652v^{9} + 1.37391v^{8} + \dots - 6.49565v + 3.19130 \end{pmatrix}$$

$$a_{1} = \begin{pmatrix} -1.35652v^{9} + 0.321739v^{8} + \dots - 1.49565v + 0.191304 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} 1.32174v^{9} - 0.313043v^{8} + \dots + 1.25217v - 1.90435 \\ 1.32174v^{9} - 0.313043v^{8} + \dots + 1.25217v - 1.90435 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} -0.808696v^{9} + 0.165217v^{8} + \dots + 0.660870v + 2.92174 \\ 0.513043v^{9} - 0.147826v^{8} + \dots + 0.591304v + 1.01739 \end{pmatrix}$$

$$a_{9} = \begin{pmatrix} 0.808696v^{9} - 0.165217v^{8} + \dots + 0.660870v - 2.92174 \\ -1.02609v^{9} + 0.295652v^{8} + \dots - 1.18261v - 1.03478 \end{pmatrix}$$

#### (ii) Obstruction class = 1

(iii) Cusp Shapes 
$$= -\frac{281}{115}v^9 + \frac{118}{115}v^8 - \frac{363}{115}v^7 + \frac{1693}{115}v^6 - \frac{959}{115}v^5 + \frac{977}{115}v^4 - \frac{2683}{115}v^3 + \frac{251}{115}v^2 + \frac{793}{115}v + \frac{622}{115}v^3 + \frac{118}{115}v^3 + \frac{251}{115}v^2 + \frac{793}{115}v + \frac{622}{115}v^3 + \frac{118}{115}v^3 + \frac{$$

### (iv) u-Polynomials at the component

| Crossings             | u-Polynomials at each crossing         |
|-----------------------|--|
| $c_1, c_3, c_5$       | $(u^2 - u + 1)^5$                      |
| $c_2$                 | $(u^2 + u + 1)^5$                      |
| $c_4, c_7$            | $u^{10}$                               |
| <i>c</i> <sub>6</sub> | $(u^5 + u^4 + 2u^3 + u^2 + u + 1)^2$   |
| $c_8, c_9$            | $ (u^5 - u^4 - 2u^3 + u^2 + u + 1)^2 $ |
| $c_{10}$              | $(u^5 - u^4 + 2u^3 - u^2 + u - 1)^2$   |
| $c_{11}$              | $(u^5 - 3u^4 + 4u^3 - u^2 - u + 1)^2$  |
| $c_{12}$              | $(u^5 + u^4 - 2u^3 - u^2 + u - 1)^2$   |

## (v) Riley Polynomials at the component

| Crossings             | Riley Polynomials at each crossing     |
|-----------------------|--|
| $c_1, c_2, c_3$ $c_5$ | $(y^2 + y + 1)^5$                      |
| $c_4, c_7$            | $y^{10}$                               |
| $c_6, c_{10}$         | $(y^5 + 3y^4 + 4y^3 + y^2 - y - 1)^2$  |
| $c_8, c_9, c_{12}$    | $(y^5 - 5y^4 + 8y^3 - 3y^2 - y - 1)^2$ |
| $c_{11}$              | $(y^5 - y^4 + 8y^3 - 3y^2 + 3y - 1)^2$ |

# (vi) Complex Volumes and Cusp Shapes

| Solutions to $I_1^v$      | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape          |
|---------------------------|---------------------------------------|---------------------|
| v = 1.219640 + 0.330957I  |                                       |                     |
| a = 0                     | 0.329100 - 0.499304I                  | 2.43337 - 0.47576I  |
| b = 0.339110 - 0.822375I  |                                       |                     |
| v = 1.219640 - 0.330957I  |                                       |                     |
| a = 0                     | 0.329100 + 0.499304I                  | 2.43337 + 0.47576I  |
| b = 0.339110 + 0.822375I  |                                       |                     |
| v = -0.323203 + 1.221720I |                                       |                     |
| a = 0                     | 0.32910 - 3.56046I                    | -1.41726 + 7.41465I |
| b = 0.339110 + 0.822375I  |                                       |                     |
| v = -0.323203 - 1.221720I |                                       |                     |
| a = 0                     | 0.32910 + 3.56046I                    | -1.41726 - 7.41465I |
| b = 0.339110 - 0.822375I  |                                       |                     |
| v = 0.575710 + 0.191698I  |                                       |                     |
| a = 0                     | 5.87256 + 2.37095I                    | 7.21285 - 1.44195I  |
| b = -0.455697 + 1.200150I |                                       |                     |
| v = 0.575710 - 0.191698I  |                                       |                     |
| a = 0                     | 5.87256 - 2.37095I                    | 7.21285 + 1.44195I  |
| b = -0.455697 - 1.200150I |                                       |                     |
| v = -0.121840 + 0.594429I |                                       |                     |
| a = 0                     | 5.87256 - 6.43072I                    | 1.90884 + 7.88634I  |
| b = -0.455697 - 1.200150I |                                       |                     |
| v = -0.121840 - 0.594429I |                                       |                     |
| a = 0                     | 5.87256 + 6.43072I                    | 1.90884 - 7.88634I  |
| b = -0.455697 + 1.200150I |                                       |                     |
| v = -0.85031 + 1.47278I   |                                       |                     |
| a = 0                     | 2.40108 + 2.02988I                    | -0.13779 - 5.66929I |
| b = -0.766826             |                                       |                     |
| v = -0.85031 - 1.47278I   |                                       |                     |
| a = 0                     | 2.40108 - 2.02988I                    | -0.13779 + 5.66929I |
| b = -0.766826             |                                       |                     |

### IV. u-Polynomials

| Crossings             | u-Polynomials at each crossing  |
|-----------------------|---|
| $c_1$                 | $((u^{2}-u+1)^{5})(u^{5}-3u^{4}+\cdots-u+1)(u^{105}+53u^{104}+\cdots-7u-1)$   |
| $c_2$                 | $((u^{2}+u+1)^{5})(u^{5}-u^{4}+\cdots+u-1)(u^{105}+7u^{104}+\cdots+7u+1)$   |
| $c_3$                 | $(u^{2} - u + 1)^{5}(u^{5} + u^{4} - 2u^{3} - u^{2} + u - 1)$ $\cdot (u^{105} - 7u^{104} + \dots + 40669u + 23377)$ |
| $c_4$                 | $u^{10}(u^5 + u^4 + \dots + u - 1)(u^{105} + 2u^{104} + \dots + 2048u + 1024)$                                      |
| <i>C</i> 5            | $((u^{2}-u+1)^{5})(u^{5}+u^{4}+\cdots+u+1)(u^{105}+7u^{104}+\cdots+7u+1)$   |
| <i>c</i> <sub>6</sub> | $u^{5}(u^{5} + u^{4} + \dots + u + 1)^{2}(u^{105} + 3u^{104} + \dots + 96u + 32)$                                   |
| $c_7$                 | $u^{10}(u^5 - u^4 + \dots + u + 1)(u^{105} + 2u^{104} + \dots + 2048u + 1024)$                                      |
| $c_8, c_9$            | $((u+1)^5)(u^5-u^4+\cdots+u+1)^2(u^{105}+8u^{104}+\cdots+2u+1)$   |
| $c_{10}$              | $u^{5}(u^{5} - u^{4} + \dots + u - 1)^{2}(u^{105} + 3u^{104} + \dots + 96u + 32)$                                   |
| $c_{11}$              | $u^{5}(u^{5} - 3u^{4} + \dots - u + 1)^{2}(u^{105} - 39u^{104} + \dots - 14848u + 1024)$                            |
| c <sub>12</sub>       | $((u-1)^5)(u^5+u^4+\cdots+u-1)^2(u^{105}+8u^{104}+\cdots+2u+1)$   |

## V. Riley Polynomials

| Crossings          | Riley Polynomials at each crossing  |
|--------------------|---|
| $c_1$              | $((y^{2} + y + 1)^{5})(y^{5} - y^{4} + \dots + 3y - 1)(y^{105} + 5y^{104} + \dots - 47y - 1)$                                   |
| $c_{2}, c_{5}$     | $((y^2 + y + 1)^5)(y^5 + 3y^4 + \dots - y - 1)(y^{105} + 53y^{104} + \dots - 7y - 1)$   |
| $c_3$              | $(y^{2} + y + 1)^{5}(y^{5} - 5y^{4} + 8y^{3} - 3y^{2} - y - 1)$ $\cdot (y^{105} - 43y^{104} + \dots + 5130220969y - 546484129)$ |
| $c_4, c_7$         | $y^{10}(y^5 - 5y^4 + 8y^3 - 3y^2 - y - 1)$ $\cdot (y^{105} - 60y^{104} + \dots + 25165824y - 1048576)$                          |
| $c_6, c_{10}$      | $y^{5}(y^{5} + 3y^{4} + \dots - y - 1)^{2}(y^{105} + 39y^{104} + \dots - 14848y - 1024)$  |
| $c_8, c_9, c_{12}$ | $(y-1)^5(y^5 - 5y^4 + 8y^3 - 3y^2 - y - 1)^2$ $\cdot (y^{105} - 90y^{104} + \dots - 206y - 1)$                                  |
| $c_{11}$           | $y^{5}(y^{5} - y^{4} + 8y^{3} - 3y^{2} + 3y - 1)^{2}$ $\cdot (y^{105} + 47y^{104} + \dots - 210108416y - 1048576)$              |