

## Ideals for irreducible components<sup>2</sup> of $X_{par}$

$$I_1^u = \langle u^{15} - u^{14} - 4u^{13} + 5u^{12} + 6u^{11} - 10u^{10} + 7u^8 - 8u^7 + 4u^6 + 6u^5 - 8u^4 + 2u^3 + 2u^2 - 2u + 1 \rangle$$

\* 1 irreducible components of  $\dim_{\mathbb{C}} = 0$ , with total 15 representations.

<sup>&</sup>lt;sup>1</sup>The image of knot diagram is generated by the software "**Draw programme**" developed by Andrew Bartholomew(http://www.layer8.co.uk/maths/draw/index.htm#Running-draw), where we modified some parts for our purpose(https://github.com/CATsTAILs/LinksPainter).

<sup>&</sup>lt;sup>2</sup> All coefficients of polynomials are rational numbers. But the coefficients are sometimes approximated in decimal forms when there is not enough margin.

I. 
$$I_1^u = \langle u^{15} - u^{14} - 4u^{13} + 5u^{12} + 6u^{11} - 10u^{10} + 7u^8 - 8u^7 + 4u^6 + 6u^5 - 8u^4 + 2u^3 + 2u^2 - 2u + 1 \rangle$$

(i) Arc colorings

$$a_{3} = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{6} = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_{4} = \begin{pmatrix} 1 \\ u^{2} \end{pmatrix}$$

$$a_{7} = \begin{pmatrix} -u \\ -u^{3} + u \end{pmatrix}$$

$$a_{8} = \begin{pmatrix} -u^{3} \\ -u^{3} + u \end{pmatrix}$$

$$a_{2} = \begin{pmatrix} u^{6} - u^{4} + 1 \\ u^{6} - 2u^{4} + u^{2} \end{pmatrix}$$

$$a_{9} = \begin{pmatrix} -u^{9} + 2u^{7} - u^{5} - 2u^{3} + u \\ -u^{9} + 3u^{7} - 3u^{5} + u \end{pmatrix}$$

$$a_{1} = \begin{pmatrix} u^{12} - 3u^{10} + 3u^{8} + 2u^{6} - 4u^{4} + u^{2} + 1 \\ u^{12} - 4u^{10} + 6u^{8} - 2u^{6} - 3u^{4} + 2u^{2} \end{pmatrix}$$

$$a_{5} = \begin{pmatrix} u^{3} \\ u^{5} - u^{3} + u \end{pmatrix}$$

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- (ii) Obstruction class = -1
- (iii) Cusp Shapes  $= 4u^{13} 16u^{11} + 4u^{10} + 28u^9 12u^8 12u^7 + 16u^6 16u^5 + 24u^3 8u^2 + 2$

## (iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
$c_1, c_2, c_7$ $c_8$	$u^{15} - 3u^{14} + \dots - 8u^2 + 1$
$c_3, c_6$	$u^{15} - u^{14} + \dots - 2u + 1$
$c_4, c_9$	$u^{15} + u^{14} + \dots + 2u + 1$
$c_5$	$u^{15} + 9u^{14} + \dots - 4u^2 + 1$

## (v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
$c_1, c_2, c_7$ $c_8$	$y^{15} + 19y^{14} + \dots + 16y - 1$
$c_3, c_6$	$y^{15} - 9y^{14} + \dots + 4y^2 - 1$
$c_4, c_9$	$y^{15} + 3y^{14} + \dots + 8y^2 - 1$
$c_5$	$y^{15} - 5y^{14} + \dots + 8y - 1$

## (vi) Complex Volumes and Cusp Shapes

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
u = 0.023100 + 0.900040I	-8.02484 + 3.25615I	-3.67133 - 2.40088I
u = 0.023100 - 0.900040I	-8.02484 - 3.25615I	-3.67133 + 2.40088I
u = -0.863978	-1.25565	-8.48380
u = -1.093890 + 0.311098I	-3.39978 + 1.10849I	-7.51398 - 0.68443I
u = -1.093890 - 0.311098I	-3.39978 - 1.10849I	-7.51398 + 0.68443I
u = 0.747479 + 0.391613I	1.24227 - 1.75942I	2.85085 + 5.01461I
u = 0.747479 - 0.391613I	1.24227 + 1.75942I	2.85085 - 5.01461I
u = 1.070290 + 0.443484I	-2.41352 - 5.68434I	-4.20490 + 7.47679I
u = 1.070290 - 0.443484I	-2.41352 + 5.68434I	-4.20490 - 7.47679I
u = -1.268720 + 0.457284I	-11.97600 + 1.54935I	-7.09602 - 0.66420I
u = -1.268720 - 0.457284I	-11.97600 - 1.54935I	-7.09602 + 0.66420I
u = 1.260410 + 0.482704I	-11.7871 - 8.1923I	-6.69502 + 5.35870I
u = 1.260410 - 0.482704I	-11.7871 + 8.1923I	-6.69502 - 5.35870I
u = 0.193328 + 0.557909I	-0.02424 + 1.73642I	-0.42769 - 4.08118I
u = 0.193328 - 0.557909I	-0.02424 - 1.73642I	-0.42769 + 4.08118I

II. u-Polynomials

Crossings	u-Polynomials at each crossing
$c_1, c_2, c_7$ $c_8$	$u^{15} - 3u^{14} + \dots - 8u^2 + 1$
$c_3, c_6$	$u^{15} - u^{14} + \dots - 2u + 1$
$c_4, c_9$	$u^{15} + u^{14} + \dots + 2u + 1$
<i>C</i> <sub>5</sub>	$u^{15} + 9u^{14} + \dots - 4u^2 + 1$

III. Riley Polynomials

Crossings	Riley Polynomials at each crossing
$c_1, c_2, c_7$ $c_8$	$y^{15} + 19y^{14} + \dots + 16y - 1$
$c_3, c_6$	$y^{15} - 9y^{14} + \dots + 4y^2 - 1$
$c_4, c_9$	$y^{15} + 3y^{14} + \dots + 8y^2 - 1$
<i>C</i> <sub>5</sub>	$y^{15} - 5y^{14} + \dots + 8y - 1$