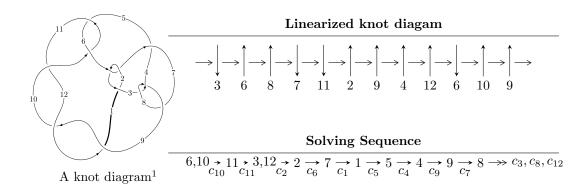
$12n_{0337} (K12n_{0337})$



Ideals for irreducible components² of X_{par}

$$I_1^u = \langle 8.75045 \times 10^{28} u^{62} + 5.63839 \times 10^{29} u^{61} + \dots + 4.42036 \times 10^{29} b + 4.19132 \times 10^{29}, \\ -8.61586 \times 10^{29} u^{62} + 6.95817 \times 10^{29} u^{61} + \dots + 2.21018 \times 10^{29} a + 3.02574 \times 10^{30}, \ u^{63} - u^{62} + \dots - 10u - 10u$$

* 2 irreducible components of $\dim_{\mathbb{C}} = 0$, with total 75 representations.

¹The image of knot diagram is generated by the software "**Draw programme**" developed by Andrew Bartholomew(http://www.layer8.co.uk/maths/draw/index.htm#Running-draw), where we modified some parts for our purpose(https://github.com/CATsTAILs/LinksPainter).

 $^{^2}$ All coefficients of polynomials are rational numbers. But the coefficients are sometimes approximated in decimal forms when there is not enough margin.

 $\begin{matrix} \text{I.} \\ I_1^u = \langle 8.75 \times 10^{28} u^{62} + 5.64 \times 10^{29} u^{61} + \dots + 4.42 \times 10^{29} b + 4.19 \times 10^{29}, \ -8.62 \times 10^{29} u^{62} + 6.96 \times 10^{29} u^{61} + \dots + 2.21 \times 10^{29} a + 3.03 \times 10^{30}, \ u^{63} - u^{62} + \dots - 10u + 1 \rangle \end{matrix}$

(i) Arc colorings

$$a_{6} = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 1 \\ u^{2} \end{pmatrix}$$

$$a_{3} = \begin{pmatrix} 3.89826u^{62} - 3.14824u^{61} + \dots + 86.3365u - 13.6900 \\ -0.197958u^{62} - 1.27555u^{61} + \dots + 12.6503u - 0.948184 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} u^{2} + 1 \\ u^{2} \end{pmatrix}$$

$$a_{2} = \begin{pmatrix} 3.89826u^{62} - 3.14824u^{61} + \dots + 86.3365u - 13.6900 \\ -0.929682u^{62} - 1.65830u^{61} + \dots + 16.2523u - 1.69821 \end{pmatrix}$$

$$a_{7} = \begin{pmatrix} 1.53828u^{62} - 0.187645u^{61} + \dots + 14.1508u - 6.97201 \\ 2.72772u^{62} - 1.67622u^{61} + \dots + 30.4294u - 4.29057 \end{pmatrix}$$

$$a_{1} = \begin{pmatrix} u^{6} + u^{4} + 2u^{2} + 1 \\ u^{6} + u^{2} \end{pmatrix}$$

$$a_{5} = \begin{pmatrix} u \\ u^{3} + u \end{pmatrix}$$

$$a_{4} = \begin{pmatrix} 0.471410u^{62} - 0.471626u^{61} + \dots + 16.3283u + 1.49775 \\ -2.28058u^{62} - 0.384216u^{61} + \dots + 9.13957u + 2.00704 \end{pmatrix}$$

$$a_{9} = \begin{pmatrix} u^{4} + u^{2} + 1 \\ u^{4} \end{pmatrix}$$

$$a_{1} = \begin{pmatrix} 1.43450u^{62} - 0.861770u^{61} + \dots + 27.0832u - 9.69122 \\ 1.91211u^{62} - 0.548333u^{61} + \dots + 17.6204u - 2.91399 \end{pmatrix}$$

- (ii) Obstruction class = -1
- (iii) Cusp Shapes = $2.06158u^{62} 4.22142u^{61} + \cdots + 98.6123u 19.1903$

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
c_1	$u^{63} + 23u^{62} + \dots - 11050u - 625$
c_2, c_6	$u^{63} - u^{62} + \dots + 40u - 25$
c_3, c_8	$u^{63} - u^{62} + \dots + 2u^2 - 1$
c_4	$u^{63} - 3u^{62} + \dots + 736u - 53$
c_5,c_{10}	$u^{63} + u^{62} + \dots - 10u - 1$
	$u^{63} - 35u^{62} + \dots + 4u - 1$
c_9, c_{11}, c_{12}	$u^{63} - 23u^{62} + \dots + 38u + 1$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
c_1	$y^{63} + 47y^{62} + \dots - 20571250y - 390625$
c_2, c_6	$y^{63} + 23y^{62} + \dots - 11050y - 625$
c_3, c_8	$y^{63} - 35y^{62} + \dots + 4y - 1$
c_4	$y^{63} + 49y^{62} + \dots + 209280y - 2809$
c_5,c_{10}	$y^{63} + 23y^{62} + \dots + 38y - 1$
c_7	$y^{63} - 7y^{62} + \dots + 4y - 1$
c_9, c_{11}, c_{12}	$y^{63} + 39y^{62} + \dots + 682y - 1$

(vi) Complex Volumes and Cusp Shapes

Solutions to I_1^u	$\int \sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
u = 0.615481 + 0.782024I		
a = 0.924724 + 0.192341I	-2.81026 - 3.12410I	1.80668 + 2.74088I
b = -0.085512 - 1.194750I		
u = 0.615481 - 0.782024I		
a = 0.924724 - 0.192341I	-2.81026 + 3.12410I	1.80668 - 2.74088I
b = -0.085512 + 1.194750I		
u = -0.817617 + 0.593503I		
a = 1.176330 - 0.407742I	-0.28869 - 4.27274I	0. + 2.20858I
b = -0.666725 - 0.147698I		
u = -0.817617 - 0.593503I		
a = 1.176330 + 0.407742I	-0.28869 + 4.27274I	0 2.20858I
b = -0.666725 + 0.147698I		
u = -0.822477 + 0.507948I		
a = -0.501572 - 1.068710I	4.20996 - 3.12624I	4.99490 + 1.04203I
b = 0.080964 - 0.498715I		
u = -0.822477 - 0.507948I		
a = -0.501572 + 1.068710I	4.20996 + 3.12624I	4.99490 - 1.04203I
b = 0.080964 + 0.498715I		
u = -0.654440 + 0.706606I		
a = 1.004440 - 0.278481I	-3.29416 - 2.07147I	-0.14477 + 3.47358I
b = -0.521492 + 0.799483I		
u = -0.654440 - 0.706606I		
a = 1.004440 + 0.278481I	-3.29416 + 2.07147I	-0.14477 - 3.47358I
b = -0.521492 - 0.799483I		
u = 0.822755 + 0.498425I		
a = 1.246610 + 0.349007I	4.25689 + 0.43803I	5.01449 + 0.38960I
b = -0.388160 + 0.165493I		
u = 0.822755 - 0.498425I		
a = 1.246610 - 0.349007I	4.25689 - 0.43803I	5.01449 - 0.38960I
b = -0.388160 - 0.165493I		

Solutions to I_1^u	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
u = -0.358362 + 0.992150I		
a = -0.074839 - 0.827034I	4.17413 + 3.04921I	11.13137 - 4.86659I
b = -0.15062 - 1.56941I		
u = -0.358362 - 0.992150I		
a = -0.074839 + 0.827034I	4.17413 - 3.04921I	11.13137 + 4.86659I
b = -0.15062 + 1.56941I		
u = 0.581922 + 0.742342I		
a = -0.988921 - 0.922896I	-2.47100 + 1.06449I	2.36761 - 0.85729I
b = 0.40243 - 1.83245I		
u = 0.581922 - 0.742342I		
a = -0.988921 + 0.922896I	-2.47100 - 1.06449I	2.36761 + 0.85729I
b = 0.40243 + 1.83245I		
u = 0.867209 + 0.606173I		
a = 1.202120 + 0.457899I	2.65432 + 9.47231I	4.00000 - 5.30483I
b = -0.693184 + 0.345225I		
u = 0.867209 - 0.606173I		
a = 1.202120 - 0.457899I	2.65432 - 9.47231I	4.00000 + 5.30483I
b = -0.693184 - 0.345225I		
u = 0.142481 + 0.926913I		
a = 1.282780 - 0.021406I	0.767985 + 0.824168I	9.41506 + 0.65151I
b = 0.772343 - 0.206200I		
u = 0.142481 - 0.926913I		
a = 1.282780 + 0.021406I	0.767985 - 0.824168I	9.41506 - 0.65151I
b = 0.772343 + 0.206200I		
u = -0.700176 + 0.840660I		
a = -0.765140 + 0.730947I	-4.60599 + 2.68345I	0
b = 0.23555 + 1.51474I		
u = -0.700176 - 0.840660I		
a = -0.765140 - 0.730947I	-4.60599 - 2.68345I	0
b = 0.23555 - 1.51474I		

Solutions to I_1^u	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
u = 0.628609 + 0.908068I		
a = 0.219058 + 0.696182I	-2.41121 - 1.77391I	0
b = 1.37912 + 1.43255I		
u = 0.628609 - 0.908068I		
a = 0.219058 - 0.696182I	-2.41121 + 1.77391I	0
b = 1.37912 - 1.43255I		
u = -0.026642 + 0.893006I		
a = -0.482850 - 0.230070I	0.96850 - 2.33689I	10.51063 + 3.88561I
b = -1.76148 - 0.77429I		
u = -0.026642 - 0.893006I		
a = -0.482850 + 0.230070I	0.96850 + 2.33689I	10.51063 - 3.88561I
b = -1.76148 + 0.77429I		
u = 0.603817 + 0.944430I		
a = -1.014530 - 0.651522I	-1.81973 - 5.79600I	0
b = -0.14337 - 1.71884I		
u = 0.603817 - 0.944430I		
a = -1.014530 + 0.651522I	-1.81973 + 5.79600I	0
b = -0.14337 + 1.71884I		
u = 0.052552 + 1.129890I		
a = -0.775773 - 0.796782I	5.89708 - 3.19125I	0
b = -1.07864 - 2.15641I		
u = 0.052552 - 1.129890I		
a = -0.775773 + 0.796782I	5.89708 + 3.19125I	0
b = -1.07864 + 2.15641I		
u = -0.767293 + 0.838686I		
a = -0.536133 + 0.727624I	-4.75625 + 2.66334I	0
b = 0.38652 + 1.38050I		
u = -0.767293 - 0.838686I		
a = -0.536133 - 0.727624I	-4.75625 - 2.66334I	0
b = 0.38652 - 1.38050I		

Solutions to I_1^u	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
u = -0.791545 + 0.338366I		
a = -0.47232 - 1.36375I	4.21373 + 5.84305I	4.20006 - 5.43025I
b = 0.146940 - 0.685183I		
u = -0.791545 - 0.338366I		
a = -0.47232 + 1.36375I	4.21373 - 5.84305I	4.20006 + 5.43025I
b = 0.146940 + 0.685183I		
u = -0.641851 + 0.958734I		
a = 0.290568 - 0.785458I	-2.52965 + 7.13795I	0
b = 1.28323 - 2.11096I		
u = -0.641851 - 0.958734I		
a = 0.290568 + 0.785458I	-2.52965 - 7.13795I	0
b = 1.28323 + 2.11096I		
u = 0.706658 + 0.446411I		
a = -0.295145 + 1.196460I	0.70382 - 1.36878I	1.16247 + 2.76782I
b = 0.201963 + 0.567576I		
u = 0.706658 - 0.446411I		
a = -0.295145 - 1.196460I	0.70382 + 1.36878I	1.16247 - 2.76782I
b = 0.201963 - 0.567576I		
u = -0.096687 + 1.163890I		
a = -0.845889 + 0.838885I	9.39173 + 8.34057I	0
b = -1.03193 + 2.21147I		
u = -0.096687 - 1.163890I		
a = -0.845889 - 0.838885I	9.39173 - 8.34057I	0
b = -1.03193 - 2.21147I		
u = 0.003658 + 1.168730I		
a = -0.699048 + 0.871689I	10.19250 - 1.37204I	0
b = -0.99139 + 2.10096I		
u = 0.003658 - 1.168730I		
a = -0.699048 - 0.871689I	10.19250 + 1.37204I	0
b = -0.99139 - 2.10096I		

Solutions to I_1^u	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
u = 0.796964 + 0.882251I		
a = -0.538356 - 0.100627I	-3.04388 - 0.13688I	0
b = 0.233347 - 0.784599I		
u = 0.796964 - 0.882251I		
a = -0.538356 + 0.100627I	-3.04388 + 0.13688I	0
b = 0.233347 + 0.784599I		
u = -0.752341 + 0.920918I		
a = -0.786716 + 0.409689I	-4.50104 + 3.08347I	0
b = 0.013060 + 1.198020I		
u = -0.752341 - 0.920918I		
a = -0.786716 - 0.409689I	-4.50104 - 3.08347I	0
b = 0.013060 - 1.198020I		
u = 0.804318 + 0.888939I		
a = -0.159292 - 0.605167I	-3.02941 - 5.85741I	0
b = 0.615657 - 1.226000I		
u = 0.804318 - 0.888939I		
a = -0.159292 + 0.605167I	-3.02941 + 5.85741I	0
b = 0.615657 + 1.226000I		
u = 0.617710 + 1.047470I		
a = 0.859697 - 0.364923I	2.35789 - 3.68565I	0
b = 0.97715 - 1.06171I		
u = 0.617710 - 1.047470I		
a = 0.859697 + 0.364923I	2.35789 + 3.68565I	0
b = 0.97715 + 1.06171I		
u = -0.567021 + 1.085240I		
a = 0.986354 + 0.368127I	6.42352 - 0.87285I	0
b = 1.018770 + 0.967931I		
u = -0.567021 - 1.085240I		
a = 0.986354 - 0.368127I	6.42352 + 0.87285I	0
b = 1.018770 - 0.967931I		

Solutions to I_1^u	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
u = -0.688188 + 1.054390I		
a = 0.386516 - 0.981629I	1.09750 + 9.92639I	0
b = 0.54971 - 2.74649I		
u = -0.688188 - 1.054390I		
a = 0.386516 + 0.981629I	1.09750 - 9.92639I	0
b = 0.54971 + 2.74649I		
u = 0.650788 + 1.081400I		
a = 0.309480 + 1.022320I	5.99769 - 5.93570I	0
b = 0.43116 + 2.53815I		
u = 0.650788 - 1.081400I		
a = 0.309480 - 1.022320I	5.99769 + 5.93570I	0
b = 0.43116 - 2.53815I		
u = -0.655982 + 1.078790I		
a = 0.836188 + 0.475018I	5.91225 + 8.64566I	0
b = 1.03372 + 1.10446I		
u = -0.655982 - 1.078790I		
a = 0.836188 - 0.475018I	5.91225 - 8.64566I	0
b = 1.03372 - 1.10446I		
u = 0.314549 + 0.662120I		
a = 0.218311 + 0.670532I	0.267822 - 1.158260I	3.61517 + 5.66198I
b = -0.011835 + 0.612906I		
u = 0.314549 - 0.662120I		
a = 0.218311 - 0.670532I	0.267822 + 1.158260I	3.61517 - 5.66198I
b = -0.011835 - 0.612906I		
u = 0.710541 + 1.068660I		
a = 0.425206 + 1.016740I	4.0664 - 15.3392I	0
b = 0.42500 + 2.83258I		
u = 0.710541 - 1.068660I		
a = 0.425206 - 1.016740I	4.0664 + 15.3392I	0
b = 0.42500 - 2.83258I		

Solutions to I_1^u	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
u = -0.516415		
a = 1.18250	1.52695	6.20940
b = -0.0216347		
u = 0.178816 + 0.052588I		
a = 0.97689 + 5.20866I	-1.74489 - 2.05954I	-4.07565 + 4.15680I
b = 0.848518 + 0.314174I		
u = 0.178816 - 0.052588I		
a = 0.97689 - 5.20866I	-1.74489 + 2.05954I	-4.07565 - 4.15680I
b = 0.848518 - 0.314174I		

$$II. \\ I_2^u = \langle u^5b + u^3b + 2u^2b + b^2 + 2bu - u^2 - u - 2, \ -u^4 + a - 1, \ u^6 + u^4 + 2u^2 + 1 \rangle$$

(i) Arc colorings

$$a_{6} = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 1 \\ u^{2} \end{pmatrix}$$

$$a_{3} = \begin{pmatrix} u^{4} + 1 \\ b \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} u^{2} + 1 \\ u^{2} \end{pmatrix}$$

$$a_{2} = \begin{pmatrix} u^{4} + 1 \\ -u^{4} - u^{2} + b - 1 \end{pmatrix}$$

$$a_{7} = \begin{pmatrix} u^{5} + u^{3} + 2u \\ u^{5}b + bu \end{pmatrix}$$

$$a_{1} = \begin{pmatrix} 0 \\ -u^{4} - u^{2} - 1 \end{pmatrix}$$

$$a_{5} = \begin{pmatrix} u \\ u^{3} + u \end{pmatrix}$$

$$a_{4} = \begin{pmatrix} u^{5}b - u^{5} - u^{3} + bu \\ -u^{3}b + 2u^{3} + u^{2} + b + 3u \end{pmatrix}$$

$$a_{9} = \begin{pmatrix} u^{4} + u^{2} + 1 \\ u^{4} \end{pmatrix}$$

$$a_{8} = \begin{pmatrix} u^{5}b + u^{5} + u^{3}b + bu + u \\ 2u^{5}b - u^{5} - 2u^{3} + bu - u \end{pmatrix}$$

- (ii) Obstruction class = 1
- (iii) Cusp Shapes = $4u^4 4u^3 4bu + 4u^2 + 8$

(iv) u-Polynomials at the component

` ,	
Crossings	u-Polynomials at each crossing
c_1	$(u-1)^{12}$
c_{2}, c_{6}	$(u^2+1)^6$
c_3, c_4, c_8	$(u^4 - u^2 + 1)^3$
c_5,c_{10}	$(u^6 + u^4 + 2u^2 + 1)^2$
	$(u^2+u+1)^6$
<i>c</i> ₉	$(u^3 + u^2 + 2u + 1)^4$
c_{11}, c_{12}	$(u^3 - u^2 + 2u - 1)^4$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
c_1	$(y-1)^{12}$
c_2, c_6	$(y+1)^{12}$
c_3, c_4, c_8	$(y^2 - y + 1)^6$
c_5, c_{10}	$(y^3 + y^2 + 2y + 1)^4$
	$(y^2 + y + 1)^6$
c_9, c_{11}, c_{12}	$(y^3 + 3y^2 + 2y - 1)^4$

(vi) Complex Volumes and Cusp Shapes

Solutions to I_2^u	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
u = 0.744862 + 0.877439I		
a = -0.662359 - 0.562280I	-4.66906 - 0.79824I	-1.50976 - 0.48465I
b = 1.06984 - 1.15137I		
u = 0.744862 + 0.877439I		
a = -0.662359 - 0.562280I	-4.66906 - 4.85801I	-1.50976 + 6.44355I
b = -0.07740 - 2.12527I		
u = 0.744862 - 0.877439I		
a = -0.662359 + 0.562280I	-4.66906 + 0.79824I	-1.50976 + 0.48465I
b = 1.06984 + 1.15137I		
u = 0.744862 - 0.877439I		
a = -0.662359 + 0.562280I	-4.66906 + 4.85801I	-1.50976 - 6.44355I
b = -0.07740 + 2.12527I		
u = -0.744862 + 0.877439I		
a = -0.662359 + 0.562280I	-4.66906 + 4.85801I	-1.50976 - 6.44355I
b = 0.507560 + 0.489013I		
u = -0.744862 + 0.877439I		
a = -0.662359 + 0.562280I	-4.66906 + 0.79824I	-1.50976 + 0.48465I
b = -0.63968 + 1.46291I		
u = -0.744862 - 0.877439I		
a = -0.662359 - 0.562280I	-4.66906 - 4.85801I	-1.50976 + 6.44355I
b = 0.507560 - 0.489013I		
u = -0.744862 - 0.877439I		
a = -0.662359 - 0.562280I	-4.66906 - 0.79824I	-1.50976 - 0.48465I
b = -0.63968 - 1.46291I		
u = 0.754878I		
a = 1.32472	-0.53148 - 2.02988I	5.01951 + 3.46410I
b = -0.577399 - 0.662359I		
u = 0.754878I		
a = 1.32472	-0.53148 + 2.02988I	5.01951 - 3.46410I
b = 1.71708 - 0.66236I		

Solutions to I_2^u	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
u = -0.754878I		
a = 1.32472	-0.53148 + 2.02988I	5.01951 - 3.46410I
b = -0.577399 + 0.662359I		
u = -0.754878I		
a = 1.32472	-0.53148 - 2.02988I	5.01951 + 3.46410I
b = 1.71708 + 0.66236I		

III. u-Polynomials

Crossings	u-Polynomials at each crossing
c_1	$((u-1)^{12})(u^{63} + 23u^{62} + \dots - 11050u - 625)$
c_2, c_6	$((u^2+1)^6)(u^{63}-u^{62}+\cdots+40u-25)$
c_3,c_8	$((u^4 - u^2 + 1)^3)(u^{63} - u^{62} + \dots + 2u^2 - 1)$
c_4	$((u^4 - u^2 + 1)^3)(u^{63} - 3u^{62} + \dots + 736u - 53)$
c_5,c_{10}	$((u6 + u4 + 2u2 + 1)2)(u63 + u62 + \dots - 10u - 1)$
C ₇	$((u^2+u+1)^6)(u^{63}-35u^{62}+\cdots+4u-1)$
<i>C</i> 9	$((u^3 + u^2 + 2u + 1)^4)(u^{63} - 23u^{62} + \dots + 38u + 1)$
c_{11}, c_{12}	$((u^3 - u^2 + 2u - 1)^4)(u^{63} - 23u^{62} + \dots + 38u + 1)$

IV. Riley Polynomials

Crossings	Riley Polynomials at each crossing
c_1	$((y-1)^{12})(y^{63} + 47y^{62} + \dots - 2.05713 \times 10^7 y - 390625)$
c_{2}, c_{6}	$((y+1)^{12})(y^{63}+23y^{62}+\cdots-11050y-625)$
c_3, c_8	$((y^2 - y + 1)^6)(y^{63} - 35y^{62} + \dots + 4y - 1)$
c_4	$((y^2 - y + 1)^6)(y^{63} + 49y^{62} + \dots + 209280y - 2809)$
c_5, c_{10}	$((y^3 + y^2 + 2y + 1)^4)(y^{63} + 23y^{62} + \dots + 38y - 1)$
c_7	$((y^2 + y + 1)^6)(y^{63} - 7y^{62} + \dots + 4y - 1)$
c_9, c_{11}, c_{12}	$((y^3 + 3y^2 + 2y - 1)^4)(y^{63} + 39y^{62} + \dots + 682y - 1)$