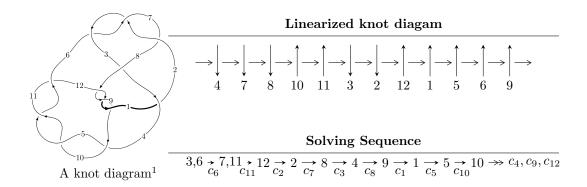
$12a_{1031} (K12a_{1031})$



Ideals for irreducible components² of X_{par}

$$\begin{split} I_1^u &= \langle -2.19647 \times 10^{18} u^{56} - 5.09545 \times 10^{18} u^{55} + \dots + 7.20554 \times 10^{18} b + 1.28415 \times 10^{19}, \\ &- 7.29984 \times 10^{18} u^{56} - 1.44902 \times 10^{19} u^{55} + \dots + 7.20554 \times 10^{18} a + 7.38518 \times 10^{19}, \ u^{57} + 2u^{56} + \dots - 8u - 10^{19} u^{56} + 10^{19} u^{5$$

* 3 irreducible components of $\dim_{\mathbb{C}} = 0$, with total 66 representations.

¹The image of knot diagram is generated by the software "**Draw programme**" developed by Andrew Bartholomew(http://www.layer8.co.uk/maths/draw/index.htm#Running-draw), where we modified some parts for our purpose(https://github.com/CATsTAILs/LinksPainter).

² All coefficients of polynomials are rational numbers. But the coefficients are sometimes approximated in decimal forms when there is not enough margin.

$$I. \\ I_1^u = \langle -2.20 \times 10^{18} u^{56} - 5.10 \times 10^{18} u^{55} + \dots + 7.21 \times 10^{18} b + 1.28 \times 10^{19}, \ -7.30 \times 10^{18} u^{56} - 1.45 \times 10^{19} u^{55} + \dots + 7.21 \times 10^{18} a + 7.39 \times 10^{19}, \ u^{57} + 2u^{56} + \dots - 8u + 1 \rangle$$

(i) Arc colorings

$$a_{3} = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_{6} = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{7} = \begin{pmatrix} 1 \\ u^{2} \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 1.01309u^{56} + 2.01098u^{55} + \dots + 4.60352u - 10.2493 \\ 0.304830u^{56} + 0.707157u^{55} + \dots + 1.30428u - 1.78217 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} 1.31792u^{56} + 2.71814u^{55} + \dots + 5.90780u - 12.0315 \\ 0.304830u^{56} + 0.707157u^{55} + \dots + 1.30428u - 1.78217 \end{pmatrix}$$

$$a_{2} = \begin{pmatrix} u \\ u^{3} + u \end{pmatrix}$$

$$a_{3} = \begin{pmatrix} u^{2} + 1 \\ u^{4} + 2u^{2} \end{pmatrix}$$

$$a_{4} = \begin{pmatrix} -u^{5} - 2u^{3} - u \\ -u^{7} - 3u^{5} - 2u^{3} + u \end{pmatrix}$$

$$a_{9} = \begin{pmatrix} 1.63554u^{56} + 3.51891u^{55} + \dots + 6.76669u - 12.1033 \\ 0.230341u^{56} + 0.550285u^{55} + \dots - 0.632533u - 1.56754 \end{pmatrix}$$

$$a_{1} = \begin{pmatrix} u^{9} + 4u^{7} + 5u^{5} + 2u^{3} + u \\ u^{11} + 5u^{9} + 8u^{7} + 3u^{5} - u^{3} + u \end{pmatrix}$$

$$a_{5} = \begin{pmatrix} -2.34155u^{56} - 5.04434u^{55} + \dots - 6.58540u + 15.6235 \\ -0.327980u^{56} - 0.616638u^{55} + \dots + 0.0250809u + 2.21226 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} -1.69640u^{56} - 3.90320u^{55} + \dots - 8.13650u + 12.0154 \\ -0.122593u^{56} - 0.0875092u^{55} + \dots + 1.34475u + 1.30123 \end{pmatrix}$$

(ii) Obstruction class = -1

(iii) Cusp Shapes =
$$-\frac{6051548760743078920}{3602767560289372397}u^{56} - \frac{8079139122240889311}{3602767560289372397}u^{55} + \cdots + \frac{59050771530991937522}{3602767560289372397}u + \frac{45876737479885210010}{3602767560289372397}$$

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
c_1	$u^{57} - 10u^{56} + \dots + 1976u + 97$
c_2, c_6, c_7	$u^{57} + 2u^{56} + \dots - 8u + 1$
c_3	$u^{57} - 2u^{56} + \dots - 7940u + 797$
c_4, c_5, c_{10} c_{11}	$u^{57} - u^{56} + \dots + 8u - 8$
c_8, c_9, c_{12}	$u^{57} - 4u^{56} + \dots + 53u + 7$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
c_1	$y^{57} + 38y^{56} + \dots + 7632286y - 9409$
c_2, c_6, c_7	$y^{57} + 54y^{56} + \dots + 70y - 1$
c_3	$y^{57} + 14y^{56} + \dots + 33141754y - 635209$
c_4, c_5, c_{10} c_{11}	$y^{57} - 71y^{56} + \dots + 960y - 64$
c_8, c_9, c_{12}	$y^{57} - 60y^{56} + \dots + 737y - 49$

(vi) Complex Volumes and Cusp Shapes

Solutions to I_1^u	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
u = -0.587296 + 0.676990I		
a = -0.992081 + 0.406961I	16.3335 - 4.5705I	10.56013 + 0.39432I
b = 1.68131 - 0.13190I		
u = -0.587296 - 0.676990I		
a = -0.992081 - 0.406961I	16.3335 + 4.5705I	10.56013 - 0.39432I
b = 1.68131 + 0.13190I		
u = -0.774867 + 0.380193I		
a = 0.56831 - 1.72511I	15.3379 + 9.2274I	8.88615 - 5.62844I
b = -1.67101 - 0.16539I		
u = -0.774867 - 0.380193I		
a = 0.56831 + 1.72511I	15.3379 - 9.2274I	8.88615 + 5.62844I
b = -1.67101 + 0.16539I		
u = 0.831356		
a = -0.649521	9.95066	7.73730
b = -1.63354		
u = 0.699421 + 0.384713I		
a = -0.52691 - 1.35735I	6.65268 - 6.38038I	7.53136 + 6.91744I
b = 0.861493 - 0.565331I		
u = 0.699421 - 0.384713I		
a = -0.52691 + 1.35735I	6.65268 + 6.38038I	7.53136 - 6.91744I
b = 0.861493 + 0.565331I		
u = -0.077518 + 1.200830I		
a = -0.441853 + 0.527455I	1.84442 + 1.53939I	0
b = 0.400809 + 0.440176I		
u = -0.077518 - 1.200830I		
a = -0.441853 - 0.527455I	1.84442 - 1.53939I	0
b = 0.400809 - 0.440176I		
u = -0.668942 + 0.396082I		
a = -1.19802 + 1.74930I	8.50640 + 4.83173I	6.80279 - 5.63364I
b = 1.62450 + 0.07831I		

Solutions to I_1^u	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
u = -0.668942 - 0.396082I		
a = -1.19802 - 1.74930I	8.50640 - 4.83173I	6.80279 + 5.63364I
b = 1.62450 - 0.07831I		
u = 0.540422 + 0.553317I		
a = 0.0227086 + 0.0584366I	7.32379 + 2.19374I	9.37328 - 0.81466I
b = -0.926422 - 0.476199I		
u = 0.540422 - 0.553317I		
a = 0.0227086 - 0.0584366I	7.32379 - 2.19374I	9.37328 + 0.81466I
b = -0.926422 + 0.476199I		
u = -0.558250 + 0.496865I		
a = 1.63555 - 0.91390I	8.95263 - 0.76794I	8.17007 - 0.54035I
b = -1.61760 + 0.02546I		
u = -0.558250 - 0.496865I		
a = 1.63555 + 0.91390I	8.95263 + 0.76794I	8.17007 + 0.54035I
b = -1.61760 - 0.02546I		
u = -0.271718 + 1.223630I		
a = -0.099179 - 0.634045I	5.53795 + 3.61211I	0
b = -0.666764 - 0.175562I		
u = -0.271718 - 1.223630I		
a = -0.099179 + 0.634045I	5.53795 - 3.61211I	0
b = -0.666764 + 0.175562I		
u = 0.206793 + 1.247570I		
a = 1.18787 + 1.19469I	7.77360 - 3.06996I	0
b = -1.46087 + 0.04757I		
u = 0.206793 - 1.247570I		
a = 1.18787 - 1.19469I	7.77360 + 3.06996I	0
b = -1.46087 - 0.04757I		
u = -0.601751 + 0.417912I		
a = 0.568911 - 0.774796I	4.25189 + 1.93714I	5.45403 - 3.24449I
b = 0.064485 - 0.762242I		

Solutions to I_1^u	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
u = -0.601751 - 0.417912I		
a = 0.568911 + 0.774796I	4.25189 - 1.93714I	5.45403 + 3.24449I
b = 0.064485 + 0.762242I		
u = 0.382994 + 1.209880I		
a = -0.90161 - 1.11860I	13.6861 - 4.3558I	0
b = 1.63564 - 0.03917I		
u = 0.382994 - 1.209880I		
a = -0.90161 + 1.11860I	13.6861 + 4.3558I	0
b = 1.63564 + 0.03917I		
u = -0.719732		
a = 1.06954	1.78784	6.76490
b = 0.676169		
u = 0.089195 + 1.288090I		
a = 1.043920 - 0.621762I	4.90426 - 1.61227I	0
b = -0.408562 - 0.408532I		
u = 0.089195 - 1.288090I		
a = 1.043920 + 0.621762I	4.90426 + 1.61227I	0
b = -0.408562 + 0.408532I		
u = 0.597316 + 0.299927I		
a = 0.75088 + 1.25022I	0.45756 - 3.37876I	3.99050 + 8.66171I
b = -0.698631 + 0.329985I		
u = 0.597316 - 0.299927I		
a = 0.75088 - 1.25022I	0.45756 + 3.37876I	3.99050 - 8.66171I
b = -0.698631 - 0.329985I		
u = 0.027116 + 1.350160I		
a = -2.00735 - 1.30623I	10.95220 - 0.52770I	0
b = 1.43950 - 0.16113I		
u = 0.027116 - 1.350160I		<u></u>
a = -2.00735 + 1.30623I	10.95220 + 0.52770I	0
b = 1.43950 + 0.16113I		

Solutions to I_1^u	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
u = 0.636143		
a = 0.899971	3.96768	-0.741900
b = 1.45279		
u = -0.206696 + 1.359410I		
a = 0.316733 + 0.033558I	3.73122 + 3.46475I	0
b = 0.059845 - 0.466800I		
u = -0.206696 - 1.359410I		
a = 0.316733 - 0.033558I	3.73122 - 3.46475I	0
b = 0.059845 + 0.466800I		
u = 0.186663 + 1.395260I		
a = 1.59178 + 0.51826I	6.49247 - 1.98805I	0
b = -0.833776 - 0.025880I		
u = 0.186663 - 1.395260I		
a = 1.59178 - 0.51826I	6.49247 + 1.98805I	0
b = -0.833776 + 0.025880I		
u = 0.22801 + 1.41445I		
a = -1.60611 - 0.79064I	5.94609 - 6.40773I	0
b = 0.802162 - 0.369008I		
u = 0.22801 - 1.41445I		
a = -1.60611 + 0.79064I	5.94609 + 6.40773I	0
b = 0.802162 + 0.369008I		
u = -0.545024 + 0.153075I		
a = -0.433814 + 0.605711I	-1.091470 + 0.719453I	-4.41448 - 2.05784I
b = -0.165016 + 0.402005I		
u = -0.545024 - 0.153075I		
a = -0.433814 - 0.605711I	-1.091470 - 0.719453I	-4.41448 + 2.05784I
b = -0.165016 - 0.402005I		
u = -0.22391 + 1.45684I		
a = -0.429922 - 0.136736I	10.28030 + 4.97302I	0
b = -0.103875 + 0.846114I		

Solutions to I_1^u	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
u = -0.22391 - 1.45684I		
a = -0.429922 + 0.136736I	10.28030 - 4.97302I	0
b = -0.103875 - 0.846114I		
u = -0.24951 + 1.45945I		
a = 2.70655 - 1.58438I	14.4830 + 8.1903I	0
b = -1.65433 - 0.10023I		
u = -0.24951 - 1.45945I		
a = 2.70655 + 1.58438I	14.4830 - 8.1903I	0
b = -1.65433 + 0.10023I		
u = 0.26230 + 1.45913I		
a = 1.44999 + 0.74312I	12.5896 - 9.8895I	0
b = -0.870143 + 0.634792I		
u = 0.26230 - 1.45913I		
a = 1.44999 - 0.74312I	12.5896 + 9.8895I	0
b = -0.870143 - 0.634792I		
u = -0.19701 + 1.46962I		
a = -3.02622 + 0.91279I	15.2659 + 1.9819I	0
b = 1.66182 + 0.00364I		
u = -0.19701 - 1.46962I		
a = -3.02622 - 0.91279I	15.2659 - 1.9819I	0
b = 1.66182 - 0.00364I		
u = 0.17782 + 1.47551I		
a = -1.061720 - 0.450691I	13.83430 - 0.35900I	0
b = 1.047880 + 0.514208I		
u = 0.17782 - 1.47551I		
a = -1.061720 + 0.450691I	13.83430 + 0.35900I	0
b = 1.047880 - 0.514208I		
u = 0.381646 + 0.332840I		
a = -0.862209 - 0.317769I	1.094310 + 0.315524I	8.13149 - 0.54452I
b = 0.612157 + 0.106984I		

Solutions to I_1^u	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
u = 0.381646 - 0.332840I		
a = -0.862209 + 0.317769I	1.094310 - 0.315524I	8.13149 + 0.54452I
b = 0.612157 - 0.106984I		
u = -0.29545 + 1.46817I		
a = -2.14517 + 1.69345I	-18.1941 + 13.1223I	0
b = 1.67802 + 0.19089I		
u = -0.29545 - 1.46817I		
a = -2.14517 - 1.69345I	-18.1941 - 13.1223I	0
b = 1.67802 - 0.19089I		
u = -0.14052 + 1.52399I		
a = 2.53882 - 0.31091I	-15.8713 - 2.1155I	0
b = -1.72718 + 0.11615I		
u = -0.14052 - 1.52399I		
a = 2.53882 + 0.31091I	-15.8713 + 2.1155I	0
b = -1.72718 - 0.11615I		
u = 0.357281		
a = -1.94262	1.04543	13.7800
b = 0.364334		
u = 0.132476		
a = -8.67705	6.53451	14.2000
b = -1.39067		

$$II. \\ I_2^u = \langle -u^2a - u^2 + b - a + u - 2, \ 2u^2a + a^2 + u^2 + 2a - 3u + 2, \ u^3 - u^2 + 2u - 1 \rangle$$

(i) Arc colorings

$$a_{3} = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_{6} = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{7} = \begin{pmatrix} 1 \\ u^{2} \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} u^{2}a + u^{2} + a - u + 2 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} u^{2}a + u^{2} + 2a - u + 2 \\ u^{2}a + u^{2} + a - u + 2 \end{pmatrix}$$

$$a_{2} = \begin{pmatrix} u \\ u^{2} - u + 1 \end{pmatrix}$$

$$a_{3} = \begin{pmatrix} u^{2} + 1 \\ u^{2} - u + 1 \end{pmatrix}$$

$$a_{4} = \begin{pmatrix} -1 \\ 0 \end{pmatrix}$$

$$a_{9} = \begin{pmatrix} -u^{2}a - 2a + u - 1 \\ -u^{2}a - a - 1 \end{pmatrix}$$

$$a_{1} = \begin{pmatrix} u^{2} + 1 \\ u^{2} - u + 1 \end{pmatrix}$$

$$a_{5} = \begin{pmatrix} -u^{2}a + au + u^{2} - 2a - 2u + 1 \\ 2 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} -u^{2}a - u^{2} - 2a + u - 2 \\ -u^{2}a - u^{2} - a + u - 2 \end{pmatrix}$$

- (ii) Obstruction class = 1
- (iii) Cusp Shapes = $-4u^2 + 4u + 4$

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
c_1	$(u^3 + u^2 - 1)^2$
c_2	$(u^3 + u^2 + 2u + 1)^2$
<i>c</i> ₃	$(u^3 - u^2 + 1)^2$
c_4, c_5, c_{10} c_{11}	$(u^2-2)^3$
c_{6}, c_{7}	$(u^3 - u^2 + 2u - 1)^2$
c_{8}, c_{9}	$(u-1)^{6}$
c_{12}	$(u+1)^6$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
c_1, c_3	$(y^3 - y^2 + 2y - 1)^2$
c_2, c_6, c_7	$(y^3 + 3y^2 + 2y - 1)^2$
c_4, c_5, c_{10} c_{11}	$(y-2)^6$
c_8, c_9, c_{12}	$(y-1)^6$

(vi) Complex Volumes and Cusp Shapes

Solutions to I_2^u	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
u = 0.215080 + 1.307140I		
a = -0.57853 - 1.61567I	9.60386 - 2.82812I	11.50976 + 2.97945I
b = 1.41421		
u = 0.215080 + 1.307140I		
a = 1.90324 + 0.49111I	9.60386 - 2.82812I	11.50976 + 2.97945I
b = -1.41421		
u = 0.215080 - 1.307140I		
a = -0.57853 + 1.61567I	9.60386 + 2.82812I	11.50976 - 2.97945I
b = 1.41421		
u = 0.215080 - 1.307140I		
a = 1.90324 - 0.49111I	9.60386 + 2.82812I	11.50976 - 2.97945I
b = -1.41421		
u = 0.569840		
a = -0.257160	5.46628	4.98050
b = 1.41421		
u = 0.569840		
a = -2.39228	5.46628	4.98050
b = -1.41421		

III.
$$I_3^u = \langle b, \; -u^2 + a - 1, \; u^3 + u^2 + 2u + 1 \rangle$$

(i) Arc colorings

$$a_{3} = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_{6} = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{7} = \begin{pmatrix} 1 \\ u^{2} \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} u^{2} + 1 \\ 0 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} u^{2} + 1 \\ 0 \end{pmatrix}$$

$$a_{2} = \begin{pmatrix} u \\ -u^{2} - u - 1 \end{pmatrix}$$

$$a_{8} = \begin{pmatrix} u^{2} + 1 \\ u^{2} + u + 1 \end{pmatrix}$$

$$a_{4} = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{9} = \begin{pmatrix} 2u^{2} + 2 \\ u^{2} + u + 1 \end{pmatrix}$$

$$a_{1} = \begin{pmatrix} -u^{2} - 1 \\ -u^{2} - u - 1 \end{pmatrix}$$

$$a_{5} = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} u^{2} + 1 \\ 0 \end{pmatrix}$$

- (ii) Obstruction class = 1
- (iii) Cusp Shapes = $-6u^2 4u 4$

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
c_1, c_3	$u^3 + u^2 - 1$
c_2	$u^3 - u^2 + 2u - 1$
c_4, c_5, c_{10} c_{11}	u^3
c_{6}, c_{7}	$u^3 + u^2 + 2u + 1$
c_8, c_9	$(u+1)^3$
c_{12}	$(u-1)^3$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
c_1, c_3	$y^3 - y^2 + 2y - 1$
c_2, c_6, c_7	$y^3 + 3y^2 + 2y - 1$
c_4, c_5, c_{10} c_{11}	y^3
c_8, c_9, c_{12}	$(y-1)^3$

(vi) Complex Volumes and Cusp Shapes

Solutions to I_3^u	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
u = -0.215080 + 1.307140I		
a = -0.662359 - 0.562280I	4.66906 + 2.82812I	6.83447 - 1.85489I
b = 0		
u = -0.215080 - 1.307140I		
a = -0.662359 + 0.562280I	4.66906 - 2.82812I	6.83447 + 1.85489I
b = 0		
u = -0.569840		
a = 1.32472	0.531480	-3.66890
b = 0		

IV. u-Polynomials

Crossings	u-Polynomials at each crossing
c_1	$((u^3 + u^2 - 1)^3)(u^{57} - 10u^{56} + \dots + 1976u + 97)$
c_2	$(u^3 - u^2 + 2u - 1)(u^3 + u^2 + 2u + 1)^2(u^{57} + 2u^{56} + \dots - 8u + 1)$
<i>c</i> ₃	$((u^3 - u^2 + 1)^2)(u^3 + u^2 - 1)(u^{57} - 2u^{56} + \dots - 7940u + 797)$
c_4, c_5, c_{10} c_{11}	$u^{3}(u^{2}-2)^{3}(u^{57}-u^{56}+\cdots+8u-8)$
c_6, c_7	$((u^3 - u^2 + 2u - 1)^2)(u^3 + u^2 + 2u + 1)(u^{57} + 2u^{56} + \dots - 8u + 1)$
c_{8}, c_{9}	$((u-1)^6)(u+1)^3(u^{57}-4u^{56}+\cdots+53u+7)$
c_{12}	$((u-1)^3)(u+1)^6(u^{57}-4u^{56}+\cdots+53u+7)$

V. Riley Polynomials

Crossings	Riley Polynomials at each crossing
c_1	$((y^3 - y^2 + 2y - 1)^3)(y^{57} + 38y^{56} + \dots + 7632286y - 9409)$
c_2, c_6, c_7	$((y^3 + 3y^2 + 2y - 1)^3)(y^{57} + 54y^{56} + \dots + 70y - 1)$
<i>c</i> ₃	$((y^3 - y^2 + 2y - 1)^3)(y^{57} + 14y^{56} + \dots + 3.31418 \times 10^7 y - 635209)$
c_4, c_5, c_{10} c_{11}	$y^{3}(y-2)^{6}(y^{57}-71y^{56}+\cdots+960y-64)$
c_8, c_9, c_{12}	$((y-1)^9)(y^{57} - 60y^{56} + \dots + 737y - 49)$