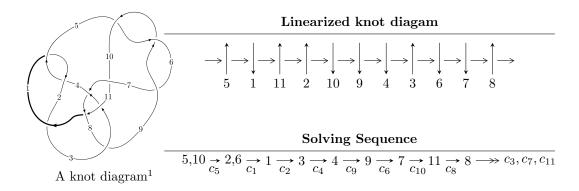
# $11a_{69} (K11a_{69})$



#### Ideals for irreducible components<sup>2</sup> of $X_{par}$

$$I_1^u = \langle 1.93466 \times 10^{44} u^{69} + 1.74032 \times 10^{45} u^{68} + \dots + 8.25681 \times 10^{45} b + 7.83469 \times 10^{45},$$
  
$$5.13127 \times 10^{45} u^{69} + 8.43947 \times 10^{44} u^{68} + \dots + 8.25681 \times 10^{45} a - 4.71677 \times 10^{45}, \ u^{70} + u^{69} + \dots + 5u + 1 \rangle$$

\* 1 irreducible components of  $\dim_{\mathbb{C}} = 0$ , with total 70 representations.

<sup>&</sup>lt;sup>1</sup>The image of knot diagram is generated by the software "**Draw programme**" developed by Andrew Bartholomew(http://www.layer8.co.uk/maths/draw/index.htm#Running-draw), where we modified some parts for our purpose(https://github.com/CATsTAILs/LinksPainter).

<sup>&</sup>lt;sup>2</sup> All coefficients of polynomials are rational numbers. But the coefficients are sometimes approximated in decimal forms when there is not enough margin.

 $\begin{matrix} \text{I.} \\ I_1^u = \langle 1.93 \times 10^{44} u^{69} + 1.74 \times 10^{45} u^{68} + \dots + 8.26 \times 10^{45} b + 7.83 \times 10^{45}, \ 5.13 \times 10^{45} u^{69} + 8.44 \times 10^{44} u^{68} + \dots + 8.26 \times 10^{45} a - 4.72 \times 10^{45}, \ u^{70} + u^{69} + \dots + 5u + 1 \rangle \end{matrix}$ 

(i) Arc colorings

$$a_{5} = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_{2} = \begin{pmatrix} -0.621458u^{69} - 0.102212u^{68} + \dots - 1.03500u + 0.571258 \\ -0.0234310u^{69} - 0.210773u^{68} + \dots - 5.77695u - 0.948876 \end{pmatrix}$$

$$a_{6} = \begin{pmatrix} 1 \\ u^{2} \end{pmatrix}$$

$$a_{1} = \begin{pmatrix} -0.598027u^{69} + 0.108561u^{68} + \dots + 4.74196u + 1.52013 \\ -0.0234310u^{69} - 0.210773u^{68} + \dots - 5.77695u - 0.948876 \end{pmatrix}$$

$$a_{3} = \begin{pmatrix} -0.755347u^{69} + 0.563488u^{68} + \dots - 11.1749u - 1.14377 \\ 0.00374491u^{69} - 0.220825u^{68} + \dots - 5.42897u - 1.96817 \end{pmatrix}$$

$$a_{4} = \begin{pmatrix} -0.586927u^{69} + 0.648245u^{68} + \dots - 11.4105u - 1.27713 \\ -0.0206773u^{69} - 0.191932u^{68} + \dots - 5.40917u - 1.81465 \end{pmatrix}$$

$$a_{9} = \begin{pmatrix} u \\ u^{3} + u \end{pmatrix}$$

$$a_{7} = \begin{pmatrix} u^{2} + 1 \\ u^{4} + 2u^{2} \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} -u^{5} - 2u^{3} - u \\ -u^{7} - 3u^{5} - 2u^{3} + u \end{pmatrix}$$

$$a_{8} = \begin{pmatrix} -0.196281u^{69} + 0.196656u^{68} + \dots - 2.97884u - 0.704438 \\ -0.119642u^{69} - 0.282284u^{68} + \dots + 2.93455u + 0.00852081 \end{pmatrix}$$

$$a_{8} = \begin{pmatrix} -0.196281u^{69} + 0.196656u^{68} + \dots - 2.97884u - 0.704438 \\ -0.119642u^{69} - 0.282284u^{68} + \dots + 2.93455u + 0.00852081 \end{pmatrix}$$

- (ii) Obstruction class = -1
- (iii) Cusp Shapes =  $-3.55662u^{69} 1.96540u^{68} + \cdots + 29.0576u + 10.9549$

#### (iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
$c_1, c_4$	$u^{70} + u^{69} + \dots + 7u + 1$
$c_2$	$u^{70} + 29u^{69} + \dots + 7u + 1$
<i>c</i> <sub>3</sub>	$u^{70} + 7u^{69} + \dots + u + 1$
$c_5, c_6, c_9$	$u^{70} - u^{69} + \dots - 5u + 1$
	$u^{70} + 3u^{69} + \dots - 23u + 1$
<i>c</i> <sub>8</sub>	$u^{70} + u^{69} + \dots + 49u + 4$
$c_{10}$	$u^{70} + u^{69} + \dots - 1887u + 578$
$c_{11}$	$u^{70} - 5u^{69} + \dots - u + 1$

## (v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
$c_1, c_4$	$y^{70} + 29y^{69} + \dots + 7y + 1$
$c_2$	$y^{70} + 25y^{69} + \dots + 347y + 1$
$c_3$	$y^{70} + 5y^{69} + \dots + 7y + 1$
$c_5, c_6, c_9$	$y^{70} + 61y^{69} + \dots - 5y + 1$
	$y^{70} - 71y^{69} + \dots - 45y + 1$
<i>C</i> <sub>8</sub>	$y^{70} - 75y^{69} + \dots - 401y + 16$
$c_{10}$	$y^{70} - 15y^{69} + \dots - 869601y + 334084$
$c_{11}$	$y^{70} - 7y^{69} + \dots - 5y + 1$

## (vi) Complex Volumes and Cusp Shapes

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
u = -0.484335 + 0.875355I		
a = -0.060674 + 0.946739I	0.05172 - 8.00134I	0
b = -0.620167 + 1.091350I		
u = -0.484335 - 0.875355I		
a = -0.060674 - 0.946739I	0.05172 + 8.00134I	0
b = -0.620167 - 1.091350I		
u = 0.236828 + 1.056350I		
a = 0.383136 - 0.264141I	1.23691 - 2.50489I	0
b = -0.489406 - 0.250651I		
u = 0.236828 - 1.056350I		
a = 0.383136 + 0.264141I	1.23691 + 2.50489I	0
b = -0.489406 + 0.250651I		
u = 0.829379 + 0.365662I		
a = 0.94611 + 1.69775I	-2.85780 - 3.99529I	-10.44720 + 9.33363I
b = -0.469428 + 0.973496I		
u = 0.829379 - 0.365662I		
a = 0.94611 - 1.69775I	-2.85780 + 3.99529I	-10.44720 - 9.33363I
b = -0.469428 - 0.973496I		
u = 0.899262 + 0.112004I		
a = -0.09567 - 1.68409I	-3.33093 + 1.52607I	-13.07472 - 1.31899I
b = -0.406148 - 0.936613I		
u = 0.899262 - 0.112004I		
a = -0.09567 + 1.68409I	-3.33093 - 1.52607I	-13.07472 + 1.31899I
b = -0.406148 + 0.936613I		
u = -0.289959 + 1.067950I		
a = 1.02846 - 1.50899I	-3.16104 - 0.50300I	0
b = -0.140513 - 1.175150I		
u = -0.289959 - 1.067950I		
a = 1.02846 + 1.50899I	-3.16104 + 0.50300I	0
b = -0.140513 + 1.175150I		

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
u = -0.403491 + 0.782625I		
a = 0.390557 - 0.716194I	1.92693 - 2.73519I	2.12851 + 1.17713I
b = -0.768228 - 0.457281I		
u = -0.403491 - 0.782625I		
a = 0.390557 + 0.716194I	1.92693 + 2.73519I	2.12851 - 1.17713I
b = -0.768228 + 0.457281I		
u = 0.499100 + 1.027490I		
a = 0.80149 + 1.34174I	-0.50648 - 6.46270I	0
b = -0.507327 + 1.004450I		
u = 0.499100 - 1.027490I		
a = 0.80149 - 1.34174I	-0.50648 + 6.46270I	0
b = -0.507327 - 1.004450I		
u = -0.814672 + 0.264193I		
a = 0.73755 - 2.31927I	-1.87843 + 12.59620I	-3.11036 - 9.02697I
b = -0.652177 - 1.126720I		
u = -0.814672 - 0.264193I		
a = 0.73755 + 2.31927I	-1.87843 - 12.59620I	-3.11036 + 9.02697I
b = -0.652177 + 1.126720I		
u = -0.764380 + 0.264018I		
a = -0.812441 - 0.044328I	0.17592 + 6.93073I	-0.67959 - 5.56176I
b = -0.884444 + 0.447119I		
u = -0.764380 - 0.264018I		
a = -0.812441 + 0.044328I	0.17592 - 6.93073I	-0.67959 + 5.56176I
b = -0.884444 - 0.447119I		
u = 0.562477 + 0.578232I		
a = 0.208519 - 0.713965I	-1.94107 - 0.75277I	-7.49106 + 4.95501I
b = -0.297139 - 0.882531I		
u = 0.562477 - 0.578232I		
a = 0.208519 + 0.713965I	-1.94107 + 0.75277I	-7.49106 - 4.95501I
b = -0.297139 + 0.882531I		

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
u = -0.745456 + 0.148738I		
a = -0.36458 + 2.64857I	-5.92974 + 4.34707I	-7.96325 - 5.56332I
b = -0.050089 + 1.257290I		
u = -0.745456 - 0.148738I		
a = -0.36458 - 2.64857I	-5.92974 - 4.34707I	-7.96325 + 5.56332I
b = -0.050089 - 1.257290I		
u = -0.107903 + 1.245720I		
a = 0.523629 - 1.003470I	1.99705 - 2.44523I	0
b = 0.416221 - 1.189180I		
u = -0.107903 - 1.245720I		
a = 0.523629 + 1.003470I	1.99705 + 2.44523I	0
b = 0.416221 + 1.189180I		
u = 0.200108 + 1.261720I		
a = 0.32731 + 2.79217I	2.39518 - 0.54119I	0
b = 0.401964 + 0.917807I		
u = 0.200108 - 1.261720I		
a = 0.32731 - 2.79217I	2.39518 + 0.54119I	0
b = 0.401964 - 0.917807I		
u = 0.368590 + 1.279980I		
a = -0.036929 - 0.922221I	0.95320 - 3.02207I	0
b = -0.254902 - 0.847557I		
u = 0.368590 - 1.279980I		
a = -0.036929 + 0.922221I	0.95320 + 3.02207I	0
b = -0.254902 + 0.847557I		
u = 0.193666 + 1.332510I		
a = -0.68225 - 2.26640I	3.56607 - 0.95896I	0
b = 0.541955 + 0.776960I		
u = 0.193666 - 1.332510I		
a = -0.68225 + 2.26640I	3.56607 + 0.95896I	0
b = 0.541955 - 0.776960I		

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
u = -0.150263 + 1.338740I		
a = -0.223687 + 0.346604I	5.26003 - 1.16982I	0
b = 0.838536 - 0.993294I		
u = -0.150263 - 1.338740I		
a = -0.223687 - 0.346604I	5.26003 + 1.16982I	0
b = 0.838536 + 0.993294I		
u = 0.231094 + 1.328390I		
a = -3.66836 - 1.80527I	3.11019 - 5.29914I	0
b = 0.536274 - 0.919865I		
u = 0.231094 - 1.328390I		
a = -3.66836 + 1.80527I	3.11019 + 5.29914I	0
b = 0.536274 + 0.919865I		
u = 0.611770 + 0.194791I		
a = 0.407403 + 0.167127I	-1.37636 - 0.69918I	-5.13733 + 2.33652I
b = -0.224664 - 0.169997I		
u = 0.611770 - 0.194791I		
a = 0.407403 - 0.167127I	-1.37636 + 0.69918I	-5.13733 - 2.33652I
b = -0.224664 + 0.169997I		
u = -0.613468 + 0.166353I		
a = -0.44642 + 2.95844I	-0.93135 + 4.88535I	-2.28013 - 10.40687I
b = 0.616639 + 1.172650I		
u = -0.613468 - 0.166353I		
a = -0.44642 - 2.95844I	-0.93135 - 4.88535I	-2.28013 + 10.40687I
b = 0.616639 - 1.172650I		
u = 0.200597 + 1.358150I		
a = 0.286571 + 0.255300I	3.63488 - 3.48634I	0
b = 0.250675 - 0.338013I		
u = 0.200597 - 1.358150I		
a = 0.286571 - 0.255300I	3.63488 + 3.48634I	0
b = 0.250675 + 0.338013I		
	1	

Solutions to $I_1^u$	$\int \sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
u = -0.183760 + 1.364120I		
a = -0.072592 + 0.787390I	6.67319 + 1.90375I	0
b = 1.003970 - 0.281861I		
u = -0.183760 - 1.364120I		
a = -0.072592 - 0.787390I	6.67319 - 1.90375I	0
b = 1.003970 + 0.281861I		
u = -0.247821 + 1.358540I		
a = -1.60160 + 1.37832I	3.90043 + 8.04691I	0
b = 0.693479 + 1.215560I		
u = -0.247821 - 1.358540I		
a = -1.60160 - 1.37832I	3.90043 - 8.04691I	0
b = 0.693479 - 1.215560I		
u = -0.212109 + 1.366200I		
a = -0.941802 + 0.648116I	6.29345 + 5.42481I	0
b = 1.001640 + 0.651261I		
u = -0.212109 - 1.366200I		
a = -0.941802 - 0.648116I	6.29345 - 5.42481I	0
b = 1.001640 - 0.651261I		
u = -0.303558 + 1.351170I		
a = -0.92726 + 1.21935I	-1.19896 + 8.13596I	0
b = 0.006202 + 1.312430I		
u = -0.303558 - 1.351170I		
a = -0.92726 - 1.21935I	-1.19896 - 8.13596I	0
b = 0.006202 - 1.312430I		
u = 0.594534 + 0.061490I		
a = -2.14747 - 5.13430I	-1.29895 - 2.30609I	11.5630 - 16.8929I
b = 0.485312 - 0.908136I		
u = 0.594534 - 0.061490I		
a = -2.14747 + 5.13430I	-1.29895 + 2.30609I	11.5630 + 16.8929I
b = 0.485312 + 0.908136I		

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
u = -0.30882 + 1.41041I		
a = -0.018285 - 0.748543I	5.50503 + 10.82290I	0
b = -0.938125 + 0.475226I		
u = -0.30882 - 1.41041I		
a = -0.018285 + 0.748543I	5.50503 - 10.82290I	0
b = -0.938125 - 0.475226I		
u = -0.33175 + 1.41736I		
a = 1.66811 - 1.38164I	3.4715 + 16.7403I	0
b = -0.680160 - 1.138340I		
u = -0.33175 - 1.41736I		
a = 1.66811 + 1.38164I	3.4715 - 16.7403I	0
b = -0.680160 + 1.138340I		
u = 0.26824 + 1.43648I		
a = 0.320427 + 0.345844I	4.08495 - 3.81337I	0
b = -0.519294 - 0.588568I		
u = 0.26824 - 1.43648I		
a = 0.320427 - 0.345844I	4.08495 + 3.81337I	0
b = -0.519294 + 0.588568I		
u = -0.487601 + 0.208801I		
a = 0.30455 + 1.43000I	1.32084 + 2.75218I	4.00267 - 8.42337I
b = 0.833768 + 0.669179I		
u = -0.487601 - 0.208801I		
a = 0.30455 - 1.43000I	1.32084 - 2.75218I	4.00267 + 8.42337I
b = 0.833768 - 0.669179I		
u = -0.04696 + 1.47919I		
a = 1.013550 - 0.079452I	9.19605 - 1.61168I	0
b = -0.776577 - 0.650017I		
u = -0.04696 - 1.47919I		
a = 1.013550 + 0.079452I	9.19605 + 1.61168I	0
b = -0.776577 + 0.650017I		

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
u = 0.34186 + 1.45082I		
a = 1.47158 + 1.05054I	2.91206 - 8.27553I	0
b = -0.558838 + 0.987517I		
u = 0.34186 - 1.45082I		
a = 1.47158 - 1.05054I	2.91206 + 8.27553I	0
b = -0.558838 - 0.987517I		
u = -0.00295 + 1.51219I		
a = 0.927152 + 0.098522I	8.13804 - 7.06461I	0
b = -0.667838 + 0.997816I		
u = -0.00295 - 1.51219I		
a =  0.927152 - 0.098522I	8.13804 + 7.06461I	0
b = -0.667838 - 0.997816I		
u = 0.473311 + 0.093934I		
a = 2.06318 - 1.63899I	-0.93813 + 1.54075I	-3.94589 - 11.49495I
b = 0.437497 + 0.816872I		
u = 0.473311 - 0.093934I		
a = 2.06318 + 1.63899I	-0.93813 - 1.54075I	-3.94589 + 11.49495I
b = 0.437497 - 0.816872I		
u = -0.380898 + 0.262790I		
a = 1.44857 + 0.52153I	1.64058 - 0.33786I	6.07692 - 1.73353I
b = 0.728444 - 0.317658I		
u = -0.380898 - 0.262790I		
a = 1.44857 - 0.52153I	1.64058 + 0.33786I	6.07692 + 1.73353I
b = 0.728444 + 0.317658I		
u = -0.130656 + 0.280023I		
a = 1.342180 - 0.108395I	0.54295 - 2.64582I	2.44579 + 0.83594I
b = 0.612892 - 0.951335I		
u = -0.130656 - 0.280023I		
a = 1.342180 + 0.108395I	0.54295 + 2.64582I	2.44579 - 0.83594I
b = 0.612892 + 0.951335I		

II. u-Polynomials

Crossings	u-Polynomials at each crossing
$c_1, c_4$	$u^{70} + u^{69} + \dots + 7u + 1$
$c_2$	$u^{70} + 29u^{69} + \dots + 7u + 1$
$c_3$	$u^{70} + 7u^{69} + \dots + u + 1$
$c_5, c_6, c_9$	$u^{70} - u^{69} + \dots - 5u + 1$
C <sub>7</sub>	$u^{70} + 3u^{69} + \dots - 23u + 1$
<i>C</i> <sub>8</sub>	$u^{70} + u^{69} + \dots + 49u + 4$
$c_{10}$	$u^{70} + u^{69} + \dots - 1887u + 578$
$c_{11}$	$u^{70} - 5u^{69} + \dots - u + 1$

## III. Riley Polynomials

Crossings	Riley Polynomials at each crossing
$c_1, c_4$	$y^{70} + 29y^{69} + \dots + 7y + 1$
$c_2$	$y^{70} + 25y^{69} + \dots + 347y + 1$
<i>c</i> <sub>3</sub>	$y^{70} + 5y^{69} + \dots + 7y + 1$
$c_5, c_6, c_9$	$y^{70} + 61y^{69} + \dots - 5y + 1$
	$y^{70} - 71y^{69} + \dots - 45y + 1$
<i>c</i> <sub>8</sub>	$y^{70} - 75y^{69} + \dots - 401y + 16$
$c_{10}$	$y^{70} - 15y^{69} + \dots - 869601y + 334084$
$c_{11}$	$y^{70} - 7y^{69} + \dots - 5y + 1$