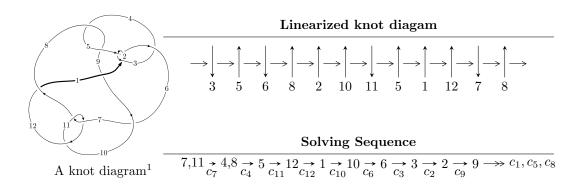
# $12n_{0036} \ (K12n_{0036})$



#### Ideals for irreducible components<sup>2</sup> of $X_{par}$

$$I_1^u = \langle 4u^{54} - 8u^{53} + \dots + u^2 + 2b, -4u^{54} + 8u^{53} + \dots + 2a + 7, u^{55} - 3u^{54} + \dots - 3u + 1 \rangle$$

$$I_2^u = \langle -u^2a + b, u^4 - u^2a + 2u^3 + a^2 - au + 3u^2 - a + 2u + 1, u^5 + u^4 + 2u^3 + u^2 + u + 1 \rangle$$

\* 2 irreducible components of  $\dim_{\mathbb{C}} = 0$ , with total 65 representations.

<sup>&</sup>lt;sup>1</sup>The image of knot diagram is generated by the software "**Draw programme**" developed by Andrew Bartholomew(http://www.layer8.co.uk/maths/draw/index.htm#Running-draw), where we modified some parts for our purpose(https://github.com/CATsTAILs/LinksPainter).

<sup>&</sup>lt;sup>2</sup> All coefficients of polynomials are rational numbers. But the coefficients are sometimes approximated in decimal forms when there is not enough margin.

I. 
$$I_1^u = \langle 4u^{54} - 8u^{53} + \dots + u^2 + 2b, -4u^{54} + 8u^{53} + \dots + 2a + 7, u^{55} - 3u^{54} + \dots - 3u + 1 \rangle$$

(i) Arc colorings

$$a_{7} = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_{4} = \begin{pmatrix} 2u^{54} - 4u^{53} + \dots + 4u - \frac{7}{2} \\ -2u^{54} + 4u^{53} + \dots - u^{3} - \frac{1}{2}u^{2} \end{pmatrix}$$

$$a_{8} = \begin{pmatrix} 1 \\ u^{2} \end{pmatrix}$$

$$a_{5} = \begin{pmatrix} 2u^{53} - 4u^{52} + \dots + \frac{1}{2}u^{2} - \frac{3}{2} \\ -u^{53} + \frac{5}{2}u^{52} + \dots - \frac{9}{2}u^{2} + 2u \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} -u \\ u \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} u^{3} \\ u^{3} + u \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} u^{3} \\ u^{3} + u \end{pmatrix}$$

$$a_{6} = \begin{pmatrix} -u^{6} - u^{4} + 1 \\ u^{6} + 2u^{4} + u^{2} \end{pmatrix}$$

$$a_{3} = \begin{pmatrix} u^{54} - \frac{3}{2}u^{53} + \dots + 3u - 2 \\ -u^{54} + \frac{3}{2}u^{53} + \dots - 2u^{2} + \frac{3}{2}u \end{pmatrix}$$

$$a_{2} = \begin{pmatrix} \frac{1}{2}u^{53} - u^{52} + \dots + \frac{7}{2}u^{3} + 1 \\ -\frac{1}{2}u^{53} + u^{52} + \dots + 2u^{3} + \frac{1}{2}u \end{pmatrix}$$

$$a_{9} = \begin{pmatrix} -u^{11} - 2u^{9} - 2u^{7} - u^{3} \\ -u^{13} - 3u^{11} - 5u^{9} - 4u^{7} - 2u^{5} + u^{3} + u \end{pmatrix}$$

- (ii) Obstruction class = -1
- (iii) Cusp Shapes =  $4u^{54} \frac{33}{2}u^{53} + \dots + 20u + \frac{1}{2}$

### (iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
$c_1$	$u^{55} + 32u^{54} + \dots - 18u - 1$
$c_2, c_5$	$u^{55} + 6u^{54} + \dots - 6u - 1$
$c_3$	$u^{55} - 6u^{54} + \dots - 18u - 1$
$c_4, c_8$	$u^{55} - u^{54} + \dots + 1024u - 1024$
$c_6, c_{12}$	$u^{55} - 3u^{54} + \dots + 379u - 73$
$c_{7}, c_{11}$	$u^{55} + 3u^{54} + \dots - 3u - 1$
<i>c</i> <sub>9</sub>	$u^{55} + 3u^{54} + \dots + 3u - 1$
$c_{10}$	$u^{55} - 29u^{54} + \dots - 3u + 1$

### (v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
$c_1$	$y^{55} - 12y^{54} + \dots - 414y - 1$
$c_2, c_5$	$y^{55} + 32y^{54} + \dots - 18y - 1$
$c_3$	$y^{55} - 56y^{54} + \dots - 2y - 1$
$c_4, c_8$	$y^{55} + 55y^{54} + \dots - 15728640y - 1048576$
$c_6, c_{12}$	$y^{55} - 35y^{54} + \dots - 79739y - 5329$
$c_7, c_{11}$	$y^{55} + 29y^{54} + \dots - 3y - 1$
$c_9$	$y^{55} + 65y^{54} + \dots - 3y - 1$
$c_{10}$	$y^{55} - 3y^{54} + \dots + 29y - 1$

# (vi) Complex Volumes and Cusp Shapes

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
u = -0.629268 + 0.778172I		
a = -1.18547 + 2.27384I	-6.39910 + 2.43818I	1.82381 - 3.17764I
b = 2.40744 - 0.92801I		
u = -0.629268 - 0.778172I		
a = -1.18547 - 2.27384I	-6.39910 - 2.43818I	1.82381 + 3.17764I
b = 2.40744 + 0.92801I		
u = -0.665364 + 0.741506I		
a = 1.20117 - 2.12038I	-10.52100 - 2.56871I	-1.299980 + 0.183319I
b = -2.43399 + 0.82779I		
u = -0.665364 - 0.741506I		
a = 1.20117 + 2.12038I	-10.52100 + 2.56871I	-1.299980 - 0.183319I
b = -2.43399 - 0.82779I		
u = 0.495253 + 0.911871I		
a = 0.959744 - 0.326051I	-1.67813 - 2.05989I	0. + 3.35425I
b = -1.043700 + 0.351476I		
u = 0.495253 - 0.911871I		
a = 0.959744 + 0.326051I	-1.67813 + 2.05989I	0 3.35425I
b = -1.043700 - 0.351476I		
u = -0.648513 + 0.820784I		
a = 1.28463 - 2.31577I	-10.29050 + 7.60349I	0 6.23847I
b = -2.45034 + 0.98315I		
u = -0.648513 - 0.820784I		
a = 1.28463 + 2.31577I	-10.29050 - 7.60349I	0. + 6.23847I
b = -2.45034 - 0.98315I		
u = 0.833853 + 0.223712I		
a = 0.45368 - 1.70191I	-7.04904 + 9.41227I	0.67128 - 5.21491I
b = 1.47926 + 0.68394I		
u = 0.833853 - 0.223712I		
a = 0.45368 + 1.70191I	-7.04904 - 9.41227I	0.67128 + 5.21491I
b = 1.47926 - 0.68394I		

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
u = 0.256410 + 0.818450I		
a = -0.479621 - 0.389548I	0.489184 - 1.277770I	5.06679 + 5.28091I
b = 0.216555 + 0.452958I		
u = 0.256410 - 0.818450I		
a = -0.479621 + 0.389548I	0.489184 + 1.277770I	5.06679 - 5.28091I
b = 0.216555 - 0.452958I		
u = 0.795256 + 0.293554I		
a = 0.39342 - 1.83875I	-8.21623 - 0.41016I	-0.923933 + 0.833875I
b = 1.14407 + 0.90240I		
u = 0.795256 - 0.293554I		
a = 0.39342 + 1.83875I	-8.21623 + 0.41016I	-0.923933 - 0.833875I
b = 1.14407 - 0.90240I		
u = -0.394472 + 1.087690I		
a = -1.50889 + 0.99463I	1.89318 - 0.05192I	0
b = 1.397460 + 0.027206I		
u = -0.394472 - 1.087690I		
a = -1.50889 - 0.99463I	1.89318 + 0.05192I	0
b = 1.397460 - 0.027206I		
u = 0.795981 + 0.235146I		
a = -0.47257 + 1.79828I	-3.68870 + 4.09212I	3.08841 - 2.21678I
b = -1.27580 - 0.65059I		
u = 0.795981 - 0.235146I		
a = -0.47257 - 1.79828I	-3.68870 - 4.09212I	3.08841 + 2.21678I
b = -1.27580 + 0.65059I		
u = 0.522439 + 0.613476I		
a = -0.397063 + 1.308290I	-2.54336 - 2.12347I	-1.98097 + 3.91876I
b = 0.133932 - 0.914279I		
u = 0.522439 - 0.613476I		
a = -0.397063 - 1.308290I	-2.54336 + 2.12347I	-1.98097 - 3.91876I
b = 0.133932 + 0.914279I		

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
u = -0.798934 + 0.043384I		
a = 0.0979918 + 0.0882666I	1.82991 - 1.15915I	1.11016 - 1.39618I
b = -0.341667 - 0.572577I		
u = -0.798934 - 0.043384I		
a = 0.0979918 - 0.0882666I	1.82991 + 1.15915I	1.11016 + 1.39618I
b = -0.341667 + 0.572577I		
u = 0.238525 + 1.182470I		
a = 0.409365 - 0.546134I	-3.53580 - 3.51533I	0
b = -0.256958 - 0.560255I		
u = 0.238525 - 1.182470I		
a = 0.409365 + 0.546134I	-3.53580 + 3.51533I	0
b = -0.256958 + 0.560255I		
u = 0.428974 + 1.129030I		
a = -0.472967 - 0.859039I	4.01128 - 1.20704I	0
b = 1.56190 + 1.45145I		
u = 0.428974 - 1.129030I		
a = -0.472967 + 0.859039I	4.01128 + 1.20704I	0
b = 1.56190 - 1.45145I		
u = 0.306193 + 1.184120I		
a = -0.040681 + 0.327783I	0.680788 + 0.637411I	0
b = 0.140846 + 0.893676I		
u = 0.306193 - 1.184120I		
a = -0.040681 - 0.327783I	0.680788 - 0.637411I	0
b = 0.140846 - 0.893676I		
u = 0.466924 + 1.132680I		
a = 0.97235 + 1.11590I	3.73819 - 6.60281I	0
b = -2.29775 - 1.19065I		
u = 0.466924 - 1.132680I		
a = 0.97235 - 1.11590I	3.73819 + 6.60281I	0
b = -2.29775 + 1.19065I		

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
u = -0.445970 + 1.141590I		
a = 0.898688 - 0.908912I	4.49847 + 3.98279I	0
b = -0.977538 + 0.234458I		
u = -0.445970 - 1.141590I		
a = 0.898688 + 0.908912I	4.49847 - 3.98279I	0
b = -0.977538 - 0.234458I		
u = -0.504119 + 1.119490I		
a = -0.72422 + 1.48566I	1.05362 + 7.50380I	0
b = 1.143880 - 0.723214I		
u = -0.504119 - 1.119490I		
a = -0.72422 - 1.48566I	1.05362 - 7.50380I	0
b = 1.143880 + 0.723214I		
u = -0.006646 + 0.753586I		
a = -1.23924 - 0.91553I	0.94796 - 1.37354I	8.29726 + 4.59305I
b = 0.221110 + 1.001110I		
u = -0.006646 - 0.753586I		
a = -1.23924 + 0.91553I	0.94796 + 1.37354I	8.29726 - 4.59305I
b = 0.221110 - 1.001110I		
u = 0.308957 + 1.222630I		
a = -0.150304 - 0.576649I	-2.51298 + 5.72465I	0
b =  0.145017 - 0.812504I		
u = 0.308957 - 1.222630I		
a = -0.150304 + 0.576649I	-2.51298 - 5.72465I	0
b = 0.145017 + 0.812504I		
u = 0.562093 + 1.144990I		
a = -2.01573 - 0.76521I	-5.70109 - 4.64931I	0
b = 2.80550 - 0.09124I		
u = 0.562093 - 1.144990I		
a = -2.01573 + 0.76521I	-5.70109 + 4.64931I	0
b = 2.80550 + 0.09124I		

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
u = 0.543221 + 1.166590I		
a = 2.03351 + 1.01526I	-0.93977 - 9.06965I	0
b = -3.03630 - 0.03630I		
u = 0.543221 - 1.166590I		
a = 2.03351 - 1.01526I	-0.93977 + 9.06965I	0
b = -3.03630 + 0.03630I		
u = -0.437917 + 1.210660I		
a = 0.760392 + 0.093272I	5.51374 + 3.19066I	0
b = -0.473659 - 0.350913I		
u = -0.437917 - 1.210660I		
a = 0.760392 - 0.093272I	5.51374 - 3.19066I	0
b = -0.473659 + 0.350913I		
u = -0.472267 + 1.211330I		
a = -0.320209 - 0.705624I	5.27082 + 5.76680I	0
b = -0.049480 + 0.606670I		
u = -0.472267 - 1.211330I		
a = -0.320209 + 0.705624I	5.27082 - 5.76680I	0
b = -0.049480 - 0.606670I		
u = 0.550577 + 1.182870I		
a = -2.18265 - 1.04941I	-4.1957 - 14.5134I	0
b = 3.13565 - 0.09179I		
u = 0.550577 - 1.182870I		
a = -2.18265 + 1.04941I	-4.1957 + 14.5134I	0
b = 3.13565 + 0.09179I		
u = -0.627951 + 0.254073I		
a = -0.152563 + 0.574638I	-1.41318 - 3.06748I	0.44741 + 4.00287I
b = 1.207510 + 0.084242I		
u = -0.627951 - 0.254073I		
a = -0.152563 - 0.574638I	-1.41318 + 3.06748I	0.44741 - 4.00287I
b = 1.207510 - 0.084242I		

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
u = -0.245896 + 0.622986I		
a = 1.09436 + 1.93010I	0.12059 + 2.86553I	2.35860 + 0.38000I
b = 0.66336 - 1.42809I		
u = -0.245896 - 0.622986I		
a = 1.09436 - 1.93010I	0.12059 - 2.86553I	2.35860 - 0.38000I
b = 0.66336 + 1.42809I		
u = -0.626935		
a = -0.0900412	1.42624	7.14390
b = -0.792661		
u = 0.586127 + 0.078855I		
a = -0.17208 + 2.32899I	0.91267 + 2.50494I	1.11924 - 3.76856I
b = -0.269979 - 0.036468I		
u = 0.586127 - 0.078855I		
a = -0.17208 - 2.32899I	0.91267 - 2.50494I	1.11924 + 3.76856I
b = -0.269979 + 0.036468I		

$$\text{II. } I_2^u = \\ \langle -u^2a+b, \ u^4-u^2a+2u^3+a^2-au+3u^2-a+2u+1, \ u^5+u^4+2u^3+u^2+u+1 \rangle$$

(i) Arc colorings

$$a_{7} = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_{4} = \begin{pmatrix} a \\ u^{2}a \end{pmatrix}$$

$$a_{8} = \begin{pmatrix} 1 \\ u^{2} \end{pmatrix}$$

$$a_{5} = \begin{pmatrix} a \\ u^{2}a \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} -u \\ u \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} -u \\ u \end{pmatrix}$$

$$a_{13} = \begin{pmatrix} -u^{3} \\ u^{3} + u \end{pmatrix}$$

$$a_{14} = \begin{pmatrix} -u^{3} \\ u^{3} + u \end{pmatrix}$$

$$a_{15} = \begin{pmatrix} -u^{3}a \\ u^{3}a + au \end{pmatrix}$$

$$a_{16} = \begin{pmatrix} -u^{3}a \\ u^{3}a + au \end{pmatrix}$$

$$a_{17} = \begin{pmatrix} -u^{3}a \\ u^{3}a - u^{4} - u^{3} + au - u^{2} \end{pmatrix}$$

$$a_{17} = \begin{pmatrix} 1 \\ u^{2}a \end{pmatrix}$$

$$a_{18} = \begin{pmatrix} 1 \\ u^{2}a \end{pmatrix}$$

- (ii) Obstruction class = 1
- (iii) Cusp Shapes =  $-5u^3a + u^4 + 6u^3 6au + 7u^2 a + 6u + 7u^3 6au + 7u^3$

### (iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
$c_1,c_3,c_5$	$(u^2 - u + 1)^5$
$c_2$	$(u^2 + u + 1)^5$
$c_4, c_8$	$u^{10}$
$c_6, c_9$	$(u^5 - u^4 - 2u^3 + u^2 + u + 1)^2$
	$(u^5 + u^4 + 2u^3 + u^2 + u + 1)^2$
$c_{10}$	$(u^5 + 3u^4 + 4u^3 + u^2 - u - 1)^2$
$c_{11}$	$(u^5 - u^4 + 2u^3 - u^2 + u - 1)^2$
$c_{12}$	$(u^5 + u^4 - 2u^3 - u^2 + u - 1)^2$

# (v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
$c_1, c_2, c_3$ $c_5$	$(y^2+y+1)^5$
$c_4, c_8$	$y^{10}$
$c_6, c_9, c_{12}$	$(y^5 - 5y^4 + 8y^3 - 3y^2 - y - 1)^2$
$c_7, c_{11}$	$(y^5 + 3y^4 + 4y^3 + y^2 - y - 1)^2$
$c_{10}$	$(y^5 - y^4 + 8y^3 - 3y^2 + 3y - 1)^2$

# (vi) Complex Volumes and Cusp Shapes

Solutions to $I_2^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
u = 0.339110 + 0.822375I		
a = -0.80632 + 1.36366I	0.32910 - 3.56046I	5.91654 + 9.74472I
b = -0.307991 - 1.215160I		
u = 0.339110 + 0.822375I		
a = 1.58413 + 0.01647I	0.329100 + 0.499304I	1.60756 + 0.92266I
b = -0.898363 + 0.874307I		
u = 0.339110 - 0.822375I		
a = -0.80632 - 1.36366I	0.32910 + 3.56046I	5.91654 - 9.74472I
b = -0.307991 + 1.215160I		
u = 0.339110 - 0.822375I		
a = 1.58413 - 0.01647I	0.329100 - 0.499304I	1.60756 - 0.92266I
b = -0.898363 - 0.874307I		
u = -0.766826		
a = 0.410598 + 0.711177I	2.40108 - 2.02988I	6.55976 + 4.16430I
b = 0.241441 + 0.418187I		
u = -0.766826		
a = 0.410598 - 0.711177I	2.40108 + 2.02988I	6.55976 - 4.16430I
b = 0.241441 - 0.418187I		
u = -0.455697 + 1.200150I		
a = -0.252108 + 0.649344I	5.87256 + 6.43072I	10.62344 - 8.02599I
b =  1.021040 - 0.524691I		
u = -0.455697 + 1.200150I		
a = -0.436295 - 0.543004I	5.87256 + 2.37095I	9.29269 + 1.50431I
b = -0.056121 + 1.146590I		
u = -0.455697 - 1.200150I		
a = -0.252108 - 0.649344I	5.87256 - 6.43072I	10.62344 + 8.02599I
b = 1.021040 + 0.524691I		
u = -0.455697 - 1.200150I		
a = -0.436295 + 0.543004I	5.87256 - 2.37095I	9.29269 - 1.50431I
b = -0.056121 - 1.146590I		

### III. u-Polynomials

Crossings	u-Polynomials at each crossing
$c_1$	$((u^2 - u + 1)^5)(u^{55} + 32u^{54} + \dots - 18u - 1)$
$c_2$	$((u^2+u+1)^5)(u^{55}+6u^{54}+\cdots-6u-1)$
$c_3$	$((u^2 - u + 1)^5)(u^{55} - 6u^{54} + \dots - 18u - 1)$
$c_4, c_8$	$u^{10}(u^{55} - u^{54} + \dots + 1024u - 1024)$
<i>C</i> <sub>5</sub>	$((u^2 - u + 1)^5)(u^{55} + 6u^{54} + \dots - 6u - 1)$
<i>c</i> <sub>6</sub>	$((u^5 - u^4 - 2u^3 + u^2 + u + 1)^2)(u^{55} - 3u^{54} + \dots + 379u - 73)$
C <sub>7</sub>	$((u^5 + u^4 + 2u^3 + u^2 + u + 1)^2)(u^{55} + 3u^{54} + \dots - 3u - 1)$
$c_9$	$((u^5 - u^4 - 2u^3 + u^2 + u + 1)^2)(u^{55} + 3u^{54} + \dots + 3u - 1)$
$c_{10}$	$((u^5 + 3u^4 + 4u^3 + u^2 - u - 1)^2)(u^{55} - 29u^{54} + \dots - 3u + 1)$
$c_{11}$	$((u^5 - u^4 + 2u^3 - u^2 + u - 1)^2)(u^{55} + 3u^{54} + \dots - 3u - 1)$
$c_{12}$	$((u^5 + u^4 - 2u^3 - u^2 + u - 1)^2)(u^{55} - 3u^{54} + \dots + 379u - 73)$

### IV. Riley Polynomials

Crossings	Riley Polynomials at each crossing
$c_1$	$((y^2 + y + 1)^5)(y^{55} - 12y^{54} + \dots - 414y - 1)$
$c_2, c_5$	$((y^2 + y + 1)^5)(y^{55} + 32y^{54} + \dots - 18y - 1)$
$c_3$	$((y^2 + y + 1)^5)(y^{55} - 56y^{54} + \dots - 2y - 1)$
$c_4, c_8$	$y^{10}(y^{55} + 55y^{54} + \dots - 1.57286 \times 10^7 y - 1048576)$
$c_6, c_{12}$	$((y^5 - 5y^4 + 8y^3 - 3y^2 - y - 1)^2)(y^{55} - 35y^{54} + \dots - 79739y - 5329)$
$c_7, c_{11}$	$((y^5 + 3y^4 + 4y^3 + y^2 - y - 1)^2)(y^{55} + 29y^{54} + \dots - 3y - 1)$
$c_9$	$((y^5 - 5y^4 + 8y^3 - 3y^2 - y - 1)^2)(y^{55} + 65y^{54} + \dots - 3y - 1)$
$c_{10}$	$((y^5 - y^4 + 8y^3 - 3y^2 + 3y - 1)^2)(y^{55} - 3y^{54} + \dots + 29y - 1)$