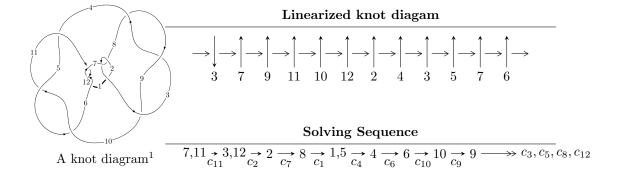
## $12n_{0642} \ (K12n_{0642})$



#### Ideals for irreducible components<sup>2</sup> of $X_{par}$

$$\begin{split} I_1^u &= \langle d-u,\ u^2 + 2c + 1,\ u^2 + 2b - 2u + 1,\ a - 1,\ u^3 + u^2 + 3u - 1 \rangle \\ I_2^u &= \langle d-u,\ u^3 - u^2 + 2c + 3u - 1,\ -u^3 + u^2 + 2b - 3u - 1,\ a - 1,\ u^4 + 4u^2 + 2u + 1 \rangle \\ I_3^u &= \langle d-u,\ u^3 - u^2 + 2c + 3u - 1,\ u^3 - u^2 + 2b + u - 1,\ -u^3 + u^2 + 2a - 5u + 3,\ u^4 + 4u^2 + 2u + 1 \rangle \\ I_4^u &= \langle u^3 - u^2 + 2d + 5u + 1,\ u^3 + c + 4u + 2,\ -u^3 + u^2 + 2b - 3u - 1,\ a - 1,\ u^4 + 4u^2 + 2u + 1 \rangle \\ I_5^u &= \langle u^3 + u^2 + 2d + 2u + 2,\ u^3 + 3u^2 + 4c + 4u + 4,\ u^3 + u^2 + b + u + 1,\ -u^3 - u^2 + 4a - 2u,\ u^4 + 3u^3 + 4u^2 + 4u + 4 \rangle \\ I_6^u &= \langle d-u,\ c-u+2,\ b+1,\ 2a+u+1,\ u^2-u+2 \rangle \\ I_7^u &= \langle d+u-1,\ 2c+u-1,\ b+1,\ 2a+u+1,\ u^2-u+2 \rangle \\ I_8^u &= \langle d+u-1,\ 2c+u-1,\ b+2u,\ a-1,\ u^2-u+2 \rangle \\ I_9^u &= \langle d,\ c+u,\ b+u,\ a+1,\ u^2+1 \rangle \\ I_{10}^u &= \langle d+u,\ c+u+1,\ b-1,\ a,\ u^2+1 \rangle \end{split}$$

 $<sup>^1\</sup>mathrm{The}$  image of knot diagram is generated by the software "**Draw programme**" developed by Andrew Bartholomew(http://www.layer8.co.uk/maths/draw/index.htm#Running-draw), where we modified some parts for our purpose(https://github.com/CATsTAILs/LinksPainter).

$$\begin{split} I^u_{11} &= \langle d+u,\ c+u+1,\ b+u,\ a+1,\ u^2+1 \rangle \\ I^u_{12} &= \langle d+u,\ cb+bu-u-1,\ a+1,\ u^2+1 \rangle \\ \\ I^v_1 &= \langle a,\ d-v,\ -av+c-v+1,\ b-1,\ v^2+1 \rangle \end{split}$$

- \* 12 irreducible components of  $\dim_{\mathbb{C}} = 0$ , with total 33 representations.
- \* 1 irreducible components of  $\dim_{\mathbb{C}} = 1$

<sup>&</sup>lt;sup>2</sup>All coefficients of polynomials are rational numbers. But the coefficients are sometimes approximated in decimal forms when there is not enough margin.

I.  $I_1^u = \langle d-u, u^2+2c+1, u^2+2b-2u+1, a-1, u^3+u^2+3u-1 \rangle$ 

$$a_{7} = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{3} = \begin{pmatrix} 1 \\ -\frac{1}{2}u^{2} + u - \frac{1}{2} \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} 1 \\ -u^{2} \end{pmatrix}$$

$$a_{2} = \begin{pmatrix} 1 \\ \frac{1}{2}u^{2} + u - \frac{1}{2} \end{pmatrix}$$

$$a_{3} = \begin{pmatrix} u \\ \frac{1}{2}u^{2} + u - \frac{1}{2} \end{pmatrix}$$

$$a_{4} = \begin{pmatrix} u \\ -\frac{1}{2}u^{2} - u + \frac{1}{2} \end{pmatrix}$$

$$a_{5} = \begin{pmatrix} u^{2} + 1 \\ -4u + 1 \end{pmatrix}$$

$$a_{5} = \begin{pmatrix} u^{2} + 1 \\ -4u + 1 \end{pmatrix}$$

$$a_{6} = \begin{pmatrix} -\frac{1}{2}u^{2} - u - \frac{1}{2} \\ u \end{pmatrix}$$

$$a_{6} = \begin{pmatrix} -u \\ -u^{2} - 2u + 1 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} \frac{1}{2}u^{2} + u + \frac{1}{2} \\ u^{2} \end{pmatrix}$$

$$a_{9} = \begin{pmatrix} \frac{1}{2}u^{2} + \frac{1}{2} \\ -\frac{1}{2}u^{2} - u + \frac{1}{2} \end{pmatrix}$$

- (ii) Obstruction class = -1
- (iii) Cusp Shapes =  $4u^2 + 8u + 18$

Crossings	u-Polynomials at each crossing	
$c_1$	$u^3 + 5u^2 + 11u - 1$	
$c_2, c_3, c_4$ $c_5, c_6, c_7$ $c_8, c_9, c_{10}$ $c_{11}, c_{12}$	$u^3 + u^2 + 3u - 1$	

Crossings	Riley Polynomials at each crossing		
$c_1$	$y^3 - 3y^2 + 131y - 1$		
$c_2, c_3, c_4$ $c_5, c_6, c_7$ $c_8, c_9, c_{10}$ $c_{11}, c_{12}$	$y^3 + 5y^2 + 11y - 1$		

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
u = 0.295598		
a = 1.00000		
b = -0.248091	0.476945	20.7140
c = -0.543689		
d = 0.295598		
u = -0.64780 + 1.72143I		
a = 1.00000		
b = 0.12405 + 2.83658I	12.0985 - 12.7092I	2.64285 + 4.85033I
c = 0.771845 + 1.115140I		
d = -0.64780 + 1.72143I		
u = -0.64780 - 1.72143I		
a = 1.00000		
b = 0.12405 - 2.83658I	12.0985 + 12.7092I	2.64285 - 4.85033I
c = 0.771845 - 1.115140I		
d = -0.64780 - 1.72143I		

$$II. \\ I_2^u = \langle d-u, \ u^3-u^2+2c+3u-1, \ -u^3+u^2+2b-3u-1, \ a-1, \ u^4+4u^2+2u+1 \rangle$$

$$a_{7} = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{3} = \begin{pmatrix} \frac{1}{2}u^{3} - \frac{1}{2}u^{2} + \frac{3}{2}u + \frac{1}{2} \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} 1 \\ -u^{2} \end{pmatrix}$$

$$a_{2} = \begin{pmatrix} \frac{1}{2}u^{3} + \frac{1}{2}u^{2} + \frac{3}{2}u + \frac{1}{2} \end{pmatrix}$$

$$a_{8} = \begin{pmatrix} \frac{1}{2}u^{3} - \frac{1}{2}u^{2} + \frac{1}{2}u - \frac{1}{2} \end{pmatrix}$$

$$a_{1} = \begin{pmatrix} u^{2} + 1 \\ 2u^{2} + 2u + 1 \end{pmatrix}$$

$$a_{2} = \begin{pmatrix} u^{2} + 1 \\ 2u^{2} + 2u + 1 \end{pmatrix}$$

$$a_{3} = \begin{pmatrix} -\frac{1}{2}u^{3} + \frac{1}{2}u^{2} - \frac{3}{2}u + \frac{1}{2} \\ u \end{pmatrix}$$

$$a_{4} = \begin{pmatrix} -\frac{1}{2}u^{3} + \frac{1}{2}u^{2} - \frac{5}{2}u + \frac{1}{2} \\ u \end{pmatrix}$$

$$a_{6} = \begin{pmatrix} -u \\ u^{3} + u \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} \frac{1}{2}u^{3} + \frac{1}{2}u^{2} + \frac{3}{2}u + \frac{3}{2} \\ u^{2} \end{pmatrix}$$

$$a_{9} = \begin{pmatrix} u^{3} + 4u + 2 \\ -1 \end{pmatrix}$$

- (ii) Obstruction class = -1
- (iii) Cusp Shapes =  $4u^3 + 14u + 12$

Crossings	u-Polynomials at each crossing
$c_1$	$u^4 + 8u^3 + 18u^2 + 4u + 1$
$c_2, c_4, c_5$ $c_6, c_7, c_{10}$ $c_{11}, c_{12}$	$u^4 + 4u^2 + 2u + 1$
$c_3, c_8, c_9$	$u^4 + 3u^3 + 4u^2 + 4u + 4$

Crossings	Riley Polynomials at each crossing		
$c_1$	$y^4 - 28y^3 + 262y^2 + 20y + 1$		
$c_2, c_4, c_5$ $c_6, c_7, c_{10}$ $c_{11}, c_{12}$	$y^4 + 8y^3 + 18y^2 + 4y + 1$		
$c_3, c_8, c_9$	$y^4 - y^3 + 16y + 16$		

Solutions to $I_2^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
u = -0.264316 + 0.422125I		
a = 1.00000		
b = 0.219104 + 0.751390I	-2.86313 - 1.17563I	8.79089 + 5.96277I
c = 0.780896 - 0.751390I		
d = -0.264316 + 0.422125I		
u = -0.264316 - 0.422125I		
a = 1.00000		
b = 0.219104 - 0.751390I	-2.86313 + 1.17563I	8.79089 - 5.96277I
c = 0.780896 + 0.751390I		
d = -0.264316 - 0.422125I		
u = 0.26432 + 1.99036I		
a = 1.00000		
b = 1.28090 - 1.27441I	19.3125 + 4.7517I	3.20911 - 2.00586I
c = -0.280896 + 1.274410I		
d = 0.26432 + 1.99036I		
u = 0.26432 - 1.99036I		
a = 1.00000		
b = 1.28090 + 1.27441I	19.3125 - 4.7517I	3.20911 + 2.00586I
c = -0.280896 - 1.274410I		
d = 0.26432 - 1.99036I		

 $\begin{aligned} \text{III. } I_3^u = \langle d-u, \ u^3-u^2+2c+3u-1, \ u^3-u^2+2b+u-1, \ -u^3+u^2+2a-5u+3, \ u^4+4u^2+2u+1 \rangle \end{aligned}$ 

$$a_{7} = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{3} = \begin{pmatrix} \frac{1}{2}u^{3} - \frac{1}{2}u^{2} + \frac{5}{2}u - \frac{3}{2} \\ -\frac{1}{2}u^{3} + \frac{1}{2}u^{2} - \frac{1}{2}u + \frac{1}{2} \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} 1 \\ -u^{2} \end{pmatrix}$$

$$a_{2} = \begin{pmatrix} \frac{1}{2}u^{3} - \frac{1}{2}u^{2} + \frac{5}{2}u - \frac{3}{2} \\ 1 \end{pmatrix}$$

$$a_{8} = \begin{pmatrix} \frac{3}{2}u^{3} - \frac{1}{2}u^{2} + \frac{11}{2}u + \frac{5}{2} \\ -\frac{1}{2}u^{3} + \frac{1}{2}u^{2} - \frac{3}{2}u - \frac{1}{2} \end{pmatrix}$$

$$a_{1} = \begin{pmatrix} u^{2} + 1 \\ 2u^{2} + 2u + 1 \end{pmatrix}$$

$$a_{5} = \begin{pmatrix} u^{2} + 1 \\ 2u^{2} + 2u + 1 \end{pmatrix}$$

$$a_{5} = \begin{pmatrix} -\frac{1}{2}u^{3} + \frac{1}{2}u^{2} - \frac{3}{2}u + \frac{1}{2} \\ u \end{pmatrix}$$

$$a_{4} = \begin{pmatrix} -\frac{1}{2}u^{3} + \frac{1}{2}u^{2} - \frac{5}{2}u + \frac{1}{2} \\ u \end{pmatrix}$$

$$a_{6} = \begin{pmatrix} -u \\ u^{3} + u \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} u^{3} + \frac{1}{2}u^{2} + \frac{3}{2}u + \frac{3}{2} \\ u^{2} \end{pmatrix}$$

$$a_{9} = \begin{pmatrix} u^{3} + 4u + 2 \\ -\frac{1}{2}u^{3} - \frac{1}{2}u^{2} - \frac{3}{2}u - \frac{1}{2} \end{pmatrix}$$

- (ii) Obstruction class = -1
- (iii) Cusp Shapes =  $4u^3 + 14u + 12$

Crossings	u-Polynomials at each crossing
$c_1$	$u^4 - u^3 + 16u + 16$
$c_2, c_7$	$u^4 + 3u^3 + 4u^2 + 4u + 4$
$c_3, c_4, c_5$ $c_6, c_8, c_9$ $c_{10}, c_{11}, c_{12}$	$u^4 + 4u^2 + 2u + 1$

Crossings	Riley Polynomials at each crossing
$c_1$	$y^4 - y^3 + 64y^2 - 256y + 256$
$c_2, c_7$	$y^4 - y^3 + 16y + 16$
$c_3, c_4, c_5$ $c_6, c_8, c_9$ $c_{10}, c_{11}, c_{12}$	$y^4 + 8y^3 + 18y^2 + 4y + 1$

Solutions to $I_3^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
u = -0.264316 + 0.422125I		
a = -2.04521 + 1.17351I		
b = 0.516580 - 0.329264I	-2.86313 - 1.17563I	8.79089 + 5.96277I
c = 0.780896 - 0.751390I		
d = -0.264316 + 0.422125I		
u = -0.264316 - 0.422125I		
a = -2.04521 - 1.17351I		
b = 0.516580 + 0.329264I	-2.86313 + 1.17563I	8.79089 - 5.96277I
c = 0.780896 + 0.751390I		
d = -0.264316 - 0.422125I		
u = 0.26432 + 1.99036I		
a = -0.454787 + 0.715953I		
b = -0.01658 + 3.26477I	19.3125 + 4.7517I	3.20911 - 2.00586I
c = -0.280896 + 1.274410I		
d = 0.26432 + 1.99036I		
u = 0.26432 - 1.99036I		
a = -0.454787 - 0.715953I		
b = -0.01658 - 3.26477I	19.3125 - 4.7517I	3.20911 + 2.00586I
c = -0.280896 - 1.274410I		
d = 0.26432 - 1.99036I		

$$\text{IV. } I_4^u = \langle u^3 - u^2 + 2d + 5u + 1, \ u^3 + c + 4u + 2, \ -u^3 + u^2 + 2b - 3u - 1, \ a - 1, \ u^4 + 4u^2 + 2u + 1 \rangle$$

$$a_{7} = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{3} = \begin{pmatrix} \frac{1}{2}u^{3} - \frac{1}{2}u^{2} + \frac{3}{2}u + \frac{1}{2} \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} 1 \\ -u^{2} \end{pmatrix}$$

$$a_{2} = \begin{pmatrix} \frac{1}{2}u^{3} + \frac{1}{2}u^{2} + \frac{3}{2}u + \frac{1}{2} \end{pmatrix}$$

$$a_{8} = \begin{pmatrix} \frac{1}{2}u^{3} - \frac{1}{2}u^{2} + \frac{1}{2}u - \frac{1}{2} \end{pmatrix}$$

$$a_{1} = \begin{pmatrix} u^{2} + 1 \\ 2u^{2} + 2u + 1 \end{pmatrix}$$

$$a_{2} = \begin{pmatrix} -\frac{1}{2}u^{3} - \frac{1}{2}u^{2} - \frac{5}{2}u - \frac{1}{2} \end{pmatrix}$$

$$a_{3} = \begin{pmatrix} -\frac{1}{2}u^{3} + \frac{1}{2}u^{2} - \frac{5}{2}u - \frac{1}{2} \end{pmatrix}$$

$$a_{4} = \begin{pmatrix} -\frac{1}{2}u^{3} - \frac{1}{2}u^{2} - \frac{3}{2}u - \frac{3}{2} \end{pmatrix}$$

$$a_{6} = \begin{pmatrix} -u \\ u^{3} + u \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} \frac{1}{2}u^{3} - \frac{1}{2}u^{2} + \frac{5}{2}u - \frac{1}{2} \\ -\frac{1}{2}u^{3} - \frac{1}{2}u^{2} - \frac{1}{2}u - \frac{3}{2} \end{pmatrix}$$

$$a_{9} = \begin{pmatrix} \frac{1}{2}u^{3} - \frac{1}{2}u^{2} + \frac{3}{2}u - \frac{1}{2} \\ -1 \end{pmatrix}$$

- (ii) Obstruction class = -1
- (iii) Cusp Shapes =  $4u^3 + 14u + 12$

Crossings	u-Polynomials at each crossing
$c_1$	$u^4 + 8u^3 + 18u^2 + 4u + 1$
$c_2, c_3, c_6 \\ c_7, c_8, c_9 \\ c_{11}, c_{12}$	$u^4 + 4u^2 + 2u + 1$
$c_4, c_5, c_{10}$	$u^4 + 3u^3 + 4u^2 + 4u + 4$

Crossings	Riley Polynomials at each crossing
$c_1$	$y^4 - 28y^3 + 262y^2 + 20y + 1$
$c_2, c_3, c_6$ $c_7, c_8, c_9$ $c_{11}, c_{12}$	$y^4 + 8y^3 + 18y^2 + 4y + 1$
$c_4, c_5, c_{10}$	$y^4 - y^3 + 16y + 16$

Solutions to $I_4^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
u = -0.264316 + 0.422125I		
a = 1.00000		
b = 0.219104 + 0.751390I	-2.86313 - 1.17563I	8.79089 + 5.96277I
c = -1.06556 - 1.70176I		
d = 0.045213 - 1.173520I		
u = -0.264316 - 0.422125I		
a = 1.00000		
b =  0.219104 - 0.751390I	-2.86313 + 1.17563I	8.79089 - 5.96277I
c = -1.06556 + 1.70176I		
d = 0.045213 + 1.173520I		
u = 0.26432 + 1.99036I		
a = 1.00000		
b = 1.28090 - 1.27441I	19.3125 + 4.7517I	3.20911 - 2.00586I
c = 0.065564 - 0.493715I		
d = -1.54521 - 0.71595I		
u = 0.26432 - 1.99036I		
a = 1.00000		
b = 1.28090 + 1.27441I	19.3125 - 4.7517I	3.20911 + 2.00586I
c =  0.065564 + 0.493715I		
d = -1.54521 + 0.71595I		

$$\text{V. } I_5^u = \langle u^3 + u^2 + 2d + 2u + 2, \ u^3 + 3u^2 + 4c + 4u + 4, \ u^3 + u^2 + b + u + 1, \ -u^3 - u^2 + 4a - 2u, \ u^4 + 3u^3 + 4u^2 + 4u + 4 \rangle$$

$$a_{7} = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{3} = \begin{pmatrix} \frac{1}{4}u^{3} + \frac{1}{4}u^{2} + \frac{1}{2}u \\ -u^{3} - u^{2} - u - 1 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} 1 \\ -u^{2} \end{pmatrix}$$

$$a_{2} = \begin{pmatrix} \frac{1}{4}u^{3} + \frac{1}{4}u^{2} + \frac{1}{2}u \\ 1 \end{pmatrix}$$

$$a_{8} = \begin{pmatrix} \frac{3}{4}u^{3} + \frac{5}{4}u^{2} + u + 2 \\ -\frac{1}{2}u^{3} - \frac{1}{2}u^{2} - 1 \end{pmatrix}$$

$$a_{1} = \begin{pmatrix} u^{2} + 1 \\ 3u^{3} + 2u^{2} + 4u + 4 \end{pmatrix}$$

$$a_{5} = \begin{pmatrix} -\frac{1}{4}u^{3} - \frac{3}{4}u^{2} - u - 1 \\ -\frac{1}{2}u^{3} - \frac{1}{2}u^{2} - u - 1 \end{pmatrix}$$

$$a_{4} = \begin{pmatrix} -\frac{1}{4}u^{3} - \frac{1}{4}u^{2} \\ -\frac{1}{2}u^{3} - \frac{1}{2}u^{2} - u - 1 \end{pmatrix}$$

$$a_{6} = \begin{pmatrix} u \\ u^{3} + u \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} -u \\ u^{3} + u \end{pmatrix}$$

$$a_{9} = \begin{pmatrix} -\frac{1}{2}u^{3} - u^{2} - \frac{1}{2}u - 1 \\ \frac{1}{2}u^{3} + \frac{3}{2}u^{2} + u + 2 \end{pmatrix}$$

- (ii) Obstruction class = -1
- (iii) Cusp Shapes =  $-u^3 5u^2 6u + 2$

Crossings	u-Polynomials at each crossing
$c_1$	$u^4 + 8u^3 + 18u^2 + 4u + 1$
$c_2, c_3, c_4$ $c_5, c_7, c_8$ $c_9, c_{10}$	$u^4 + 4u^2 + 2u + 1$
$c_6, c_{11}, c_{12}$	$u^4 + 3u^3 + 4u^2 + 4u + 4$

Crossings	Riley Polynomials at each crossing
$c_1$	$y^4 - 28y^3 + 262y^2 + 20y + 1$
$c_2, c_3, c_4$ $c_5, c_7, c_8$ $c_9, c_{10}$	$y^4 + 8y^3 + 18y^2 + 4y + 1$
$c_6, c_{11}, c_{12}$	$y^4 - y^3 + 16y + 16$

Solutions to $I_5^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
u = 0.045213 + 1.173520I		
a = -0.367842 + 0.211063I		
b = 0.516580 + 0.329264I	-2.86313 + 1.17563I	8.79089 - 5.96277I
c =  0.032782 - 0.850878I		
d = -0.264316 - 0.422125I		
u = 0.045213 - 1.173520I		
a = -0.367842 - 0.211063I		
b = 0.516580 - 0.329264I	-2.86313 - 1.17563I	8.79089 + 5.96277I
c = 0.032782 + 0.850878I		
d = -0.264316 + 0.422125I		
u = -1.54521 + 0.71595I		
a = -0.632158 + 0.995180I		
b = -0.01658 - 3.26477I	19.3125 - 4.7517I	3.20911 + 2.00586I
c = -0.532782 - 0.246857I		
d = 0.26432 - 1.99036I		
u = -1.54521 - 0.71595I		
a = -0.632158 - 0.995180I		
b = -0.01658 + 3.26477I	19.3125 + 4.7517I	3.20911 - 2.00586I
c = -0.532782 + 0.246857I		
d = 0.26432 + 1.99036I		

VI. 
$$I_6^u = \langle d-u, \ c-u+2, \ b+1, \ 2a+u+1, \ u^2-u+2 \rangle$$

$$a_{7} = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{3} = \begin{pmatrix} -\frac{1}{2}u - \frac{1}{2} \\ -1 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} 1 \\ -u + 2 \end{pmatrix}$$

$$a_{2} = \begin{pmatrix} -\frac{1}{2}u - \frac{1}{2} \\ 1 \end{pmatrix}$$

$$a_{3} = \begin{pmatrix} \frac{1}{2}u - \frac{3}{2} \\ 1 \end{pmatrix}$$

$$a_{4} = \begin{pmatrix} u - 1 \\ u + 2 \end{pmatrix}$$

$$a_{5} = \begin{pmatrix} u - 1 \\ u + 2 \end{pmatrix}$$

$$a_{4} = \begin{pmatrix} -2 \\ u \end{pmatrix}$$

$$a_{6} = \begin{pmatrix} -u \\ -2 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} -u - 1 \\ u - 2 \end{pmatrix}$$

$$a_{9} = \begin{pmatrix} -\frac{3}{2}u + \frac{1}{2} \\ -1 \end{pmatrix}$$

- (ii) Obstruction class = -1
- (iii) Cusp Shapes = 2

Crossings	u-Polynomials at each crossing		
$c_1$	$u^2 + 3u + 4$		
$c_2, c_3, c_4$ $c_5, c_6, c_7$ $c_8, c_9, c_{10}$ $c_{11}, c_{12}$	$u^2 - u + 2$		

Crossings	Riley Polynomials at each crossing		
$c_1$	$y^2 - y + 16$		
$c_2, c_3, c_4$ $c_5, c_6, c_7$ $c_8, c_9, c_{10}$ $c_{11}, c_{12}$	$y^2 + 3y + 4$		

Solutions	to $I_6^u \qquad \int \sqrt{-1}(\text{vol} + \sqrt{-1})$	$\overline{-1}CS$ ) Cusp shape
u = 0.50000 +	1.32288 <i>I</i>	
a = -0.750000 -	- 0.661438 <i>I</i>	
b = -1.00000	-8.22467	2.00000
c = -1.50000 +	1.32288I	
d = 0.50000 +	1.32288I	
u = 0.50000 -	1.32288I	
a = -0.750000 -	+ 0.661438 <i>I</i>	
b = -1.00000	-8.22467	2.00000
c = -1.50000 -	1.32288I	
d = 0.50000 -	1.32288I	

VII. 
$$I_7^u = \langle d+u-1, \ 2c+u-1, \ b+1, \ 2a+u+1, \ u^2-u+2 \rangle$$

a) Art colorings
$$a_7 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} -\frac{1}{2}u - \frac{1}{2} \\ -1 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} 1 \\ -u + 2 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} -\frac{1}{2}u - \frac{1}{2} \\ 1 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} \frac{1}{2}u - \frac{3}{2} \\ 1 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} u - 1 \\ u + 2 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} -\frac{1}{2}u + \frac{1}{2} \\ -u + 1 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} \frac{1}{2}u - \frac{1}{2} \\ -u + 1 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} -u \\ -2 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} -\frac{1}{2}u + \frac{1}{2} \\ -u - 1 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} \frac{1}{2}u - \frac{1}{2} \\ -1 \end{pmatrix}$$

- (ii) Obstruction class = -1
- (iii) Cusp Shapes = 2

Crossings	u-Polynomials at each crossing		
$c_1$	$u^2 + 3u + 4$		
$c_2, c_3, c_4$ $c_5, c_6, c_7$ $c_8, c_9, c_{10}$ $c_{11}, c_{12}$	$u^2 - u + 2$		

Crossings	Riley Polynomials at each crossing		
$c_1$	$y^2 - y + 16$		
$c_2, c_3, c_4$ $c_5, c_6, c_7$ $c_8, c_9, c_{10}$ $c_{11}, c_{12}$	$y^2 + 3y + 4$		

Solutions to $I_7^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
u = 0.50000 + 1.32288I		
a = -0.750000 - 0.661438I		
b = -1.00000	-8.22467	2.00000
c = 0.250000 - 0.661438I		
d = 0.50000 - 1.32288I		
u = 0.50000 - 1.32288I		
a = -0.750000 + 0.661438I		
b = -1.00000	-8.22467	2.00000
c =  0.250000 + 0.661438I		
d = 0.50000 + 1.32288I		

VIII. 
$$I_8^u = \langle d+u-1,\ 2c+u-1,\ b+2u,\ a-1,\ u^2-u+2 \rangle$$

$$a_{7} = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{3} = \begin{pmatrix} 1 \\ -2u \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} 1 \\ -u+2 \end{pmatrix}$$

$$a_{2} = \begin{pmatrix} 1 \\ -u-2 \end{pmatrix}$$

$$a_{3} = \begin{pmatrix} u \\ -2u+2 \end{pmatrix}$$

$$a_{4} = \begin{pmatrix} u \\ -2u+1 \end{pmatrix}$$

$$a_{4} = \begin{pmatrix} \frac{1}{2}u + \frac{1}{2} \\ -u+1 \end{pmatrix}$$

$$a_{6} = \begin{pmatrix} -\frac{1}{2}u + \frac{1}{2} \\ -u+1 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} -\frac{1}{2}u + \frac{1}{2} \\ -u-1 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} \frac{1}{2}u - \frac{1}{2} \\ -u-1 \end{pmatrix}$$

$$a_{20} = \begin{pmatrix} \frac{1}{2}u - \frac{1}{2} \\ -u+3 \end{pmatrix}$$

- (ii) Obstruction class = -1
- (iii) Cusp Shapes = 2

Crossings	u-Polynomials at each crossing		
$c_1$	$u^2 + 3u + 4$		
$c_2, c_3, c_4 \ c_5, c_6, c_7 \ c_8, c_9, c_{10} \ c_{11}, c_{12}$	$u^2 - u + 2$		

Crossings	Riley Polynomials at each crossing		
$c_1$	$y^2 - y + 16$		
$c_2, c_3, c_4 \ c_5, c_6, c_7 \ c_8, c_9, c_{10} \ c_{11}, c_{12}$	$y^2 + 3y + 4$		

Solutions to $I_8^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
u = 0.50000 + 1.32288I		
a = 1.00000		
b = -1.00000 - 2.64575I	-8.22467	2.00000
c = 0.250000 - 0.661438I		
d = 0.50000 - 1.32288I		
u = 0.50000 - 1.32288I		
a = 1.00000		
b = -1.00000 + 2.64575I	-8.22467	2.00000
c =  0.250000 + 0.661438I		
d = 0.50000 + 1.32288I		

IX. 
$$I_9^u=\langle d,\ c+u,\ b+u,\ a+1,\ u^2+1\rangle$$

$$a_7 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} -1 \\ -u \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} 1 \\ 1 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} -1 \\ -u+1 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} u \\ -1 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} 0 \\ 1 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} -u \\ 0 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} -u \\ 0 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} -u \\ 0 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} u+1 \\ -1 \end{pmatrix}$$

- (ii) Obstruction class = 1
- (iii) Cusp Shapes = 4

Crossings	u-Polynomials at each crossing
$c_1$	$(u-1)^2$
$c_2, c_3, c_6$ $c_7, c_8, c_9$ $c_{11}, c_{12}$	$u^2 + 1$
$c_4, c_5, c_{10}$	$u^2$

Crossings	Riley Polynomials at each crossing
$c_1$	$(y-1)^2$
$c_2, c_3, c_6$ $c_7, c_8, c_9$ $c_{11}, c_{12}$	$(y+1)^2$
$c_4, c_5, c_{10}$	$y^2$

Solutions to $I_9^u$		$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
u =	1.000000I		
a = -1.000	000		
b =	$-\ 1.000000I$	-4.93480	4.00000
c =	-1.000000I		
d =	0		
u =	-1.000000I		
a = -1.000	000		
b =	1.000000I	-4.93480	4.00000
c =	1.000000I		
d =	0		

X. 
$$I_{10}^u = \langle d+u, \ c+u+1, \ b-1, \ a, \ u^2+1 \rangle$$

$$a_7 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} 0 \\ 1 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} 1 \\ 1 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} 0 \\ 1 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_1 = \begin{pmatrix} 0 \\ 1 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} -u - 1 \\ -u \end{pmatrix}$$

$$a_4 = \begin{pmatrix} -1 \\ -u \end{pmatrix}$$

$$a_6 = \begin{pmatrix} -u \\ 0 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} u \\ -1 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} u \\ u-1 \end{pmatrix}$$

- (ii) Obstruction class = 1
- (iii) Cusp Shapes = 4

## (iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing		
$c_1, c_2, c_7$	$u^2$		
$c_3, c_4, c_5$ $c_6, c_8, c_9$ $c_{10}, c_{11}, c_{12}$	$u^2 + 1$		

Crossings	Riley Polynomials at each crossing		
$c_1, c_2, c_7$	$y^2$		
$c_3, c_4, c_5$ $c_6, c_8, c_9$ $c_{10}, c_{11}, c_{12}$	$(y+1)^2$		

Solutions to $I_{10}^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
u = 1.000000I		
a = 0		
b = 1.00000	-4.93480	4.00000
c = -1.00000 - 1.00000I		
d = -1.000000I		
u = -1.000000I		
a = 0		
b = 1.00000	-4.93480	4.00000
c = -1.00000 + 1.00000I		
d = 1.000000I		

XI. 
$$I_{11}^u = \langle d+u, \ c+u+1, \ b+u, \ a+1, \ u^2+1 \rangle$$

$$a_7 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} -1 \\ -u \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} 1 \\ 1 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} -1 \\ -u+1 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} u \\ -1 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} 0 \\ 1 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} -u - 1 \\ -u \end{pmatrix}$$

$$a_4 = \begin{pmatrix} -1 \\ -u \end{pmatrix}$$

$$a_6 = \begin{pmatrix} -u \\ 0 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} u \\ -1 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} u \\ -1 \end{pmatrix}$$

- (ii) Obstruction class = 1
- (iii) Cusp Shapes = 4

## (iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
$c_1$	$(u-1)^2$
$c_2, c_4, c_5$ $c_6, c_7, c_{10}$ $c_{11}, c_{12}$	$u^2 + 1$
$c_3, c_8, c_9$	$u^2$

Crossings	Riley Polynomials at each crossing
$c_1$	$(y-1)^2$
$c_2, c_4, c_5$ $c_6, c_7, c_{10}$ $c_{11}, c_{12}$	$(y+1)^2$
$c_3, c_8, c_9$	$y^2$

Soluti	ions to $I_{11}^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
u =	1.000000I		
a = -1.000	00		
b =	-1.000000I	-4.93480	4.00000
c = -1.000	00 - 1.00000I		
d =	-1.000000I		
u =	-1.000000I		
a = -1.000	00		
b =	1.000000I	-4.93480	4.00000
c = -1.000	00 + 1.00000I		
d =	1.000000I		

XII. 
$$I_{12}^u = \langle d+u, \ cb+bu-u-1, \ a+1, \ u^2+1 \rangle$$

$$a_7 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$
$$a_{11} = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} -1 \\ b \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} 1 \\ 1 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} -1 \\ b+1 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} u \\ -bu \end{pmatrix}$$

$$a_1 = \begin{pmatrix} 0 \\ 1 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} c \\ -u \end{pmatrix}$$

$$a_4 = \begin{pmatrix} c+u \\ -u \end{pmatrix}$$

$$a_6 = \begin{pmatrix} -u \\ 0 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} -cu + 1 \\ -1 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} -1 \\ -cu + u + 1 \\ -bu - 1 \end{pmatrix}$$

- (ii) Obstruction class = -1
- (iii) Cusp Shapes = -2
- (iv) u-Polynomials at the component : It cannot be defined for a positive dimension component.
- (v) Riley Polynomials at the component : It cannot be defined for a positive dimension component.

Solution to $I_{12}^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = \cdots$		
$a = \cdots$		
$b = \cdots$	-6.57974	-2.00000
$c = \cdots$		
$d = \cdots$		

XIII. 
$$I_1^v = \langle a, \ d-v, \ -av+c-v+1, \ b-1, \ v^2+1 \rangle$$

$$a_7 = \begin{pmatrix} v \\ 0 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} 0 \\ 1 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} 1 \\ 1 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} 0 \\ -v \end{pmatrix}$$

$$a_1 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} v - 1 \\ v \end{pmatrix}$$

$$a_4 = \begin{pmatrix} -1 \\ v \end{pmatrix}$$

$$a_6 = \begin{pmatrix} v \\ 0 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} -v \\ -1 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} -v \\ -v - 1 \end{pmatrix}$$

- (ii) Obstruction class = 1
- (iii) Cusp Shapes = 4

## (iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing		
$c_1$	$(u-1)^2$		
$c_2, c_3, c_4$ $c_5, c_7, c_8$ $c_9, c_{10}$	$u^2 + 1$		
$c_6, c_{11}, c_{12}$	$u^2$		

Crossings	Riley Polynomials at each crossing
$c_1$	$(y-1)^2$
$c_2, c_3, c_4$ $c_5, c_7, c_8$ $c_9, c_{10}$	$(y+1)^2$
$c_6, c_{11}, c_{12}$	$y^2$

Solutions to $I_1^v$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
v = 1.000000I		
a = 0		
b = 1.00000	-4.93480	4.00000
c = -1.00000 + 1.00000I		
d = 1.000000I		
v = -1.000000I		
a = 0		
b = 1.00000	-4.93480	4.00000
c = -1.00000 - 1.00000I		
d = -1.000000I		

XIV. u-Polynomials

Crossings	u-Polynomials at each crossing
$c_1$	$\begin{vmatrix} u^{2}(u-1)^{6}(u^{2}+3u+4)^{3}(u^{3}+5u^{2}+11u-1)(u^{4}-u^{3}+16u+16) \\ \cdot (u^{4}+8u^{3}+18u^{2}+4u+1)^{3} \end{vmatrix}$
$c_2, c_3, c_4$ $c_5, c_6, c_7$ $c_8, c_9, c_{10}$ $c_{11}, c_{12}$	$u^{2}(u^{2}+1)^{3}(u^{2}-u+2)^{3}(u^{3}+u^{2}+3u-1)(u^{4}+4u^{2}+2u+1)^{3}$ $\cdot (u^{4}+3u^{3}+4u^{2}+4u+4)$

XV. Riley Polynomials

Crossings	Riley Polynomials at each crossing
$c_1$	$y^{2}(y-1)^{6}(y^{2}-y+16)^{3}(y^{3}-3y^{2}+131y-1)$ $\cdot (y^{4}-28y^{3}+262y^{2}+20y+1)^{3}(y^{4}-y^{3}+64y^{2}-256y+256)$
$c_2, c_3, c_4 \ c_5, c_6, c_7 \ c_8, c_9, c_{10} \ c_{11}, c_{12}$	$y^{2}(y+1)^{6}(y^{2}+3y+4)^{3}(y^{3}+5y^{2}+11y-1)(y^{4}-y^{3}+16y+16)$ $\cdot (y^{4}+8y^{3}+18y^{2}+4y+1)^{3}$