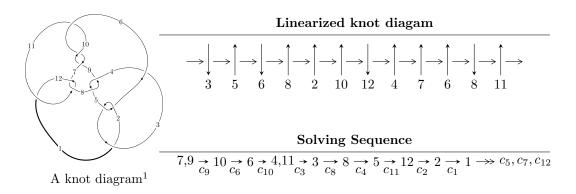
$12n_{0051} \ (K12n_{0051})$



Ideals for irreducible components² of X_{par}

$$\begin{split} I_1^u &= \langle -1.54023 \times 10^{25} u^{21} - 4.36397 \times 10^{25} u^{20} + \dots + 2.35281 \times 10^{27} b - 1.19412 \times 10^{26}, \\ &\quad 4.19615 \times 10^{28} u^{21} + 1.33730 \times 10^{29} u^{20} + \dots + 1.37404 \times 10^{30} a + 5.83977 \times 10^{30}, \\ &\quad u^{22} + 3u^{21} + \dots - 160u + 73 \rangle \\ I_2^u &= \langle b, \ 6u^3 a - 4u^2 a - 3u^3 + 4a^2 + 14au - 2u^2 - 6a - 7u - 7, \ u^4 - u^3 + 3u^2 - 2u + 1 \rangle \\ I_3^u &= \langle -a^4 u + a^3 u + a^3 - 2a^2 + 4au + 4b - 4a - 4u, \ a^5 + a^4 u - a^4 - 2a^3 u - 4a^2 u - 4a^2 + 4a - 4u + 4, \ u^2 + 1 \rangle \end{split}$$

* 3 irreducible components of $\dim_{\mathbb{C}} = 0$, with total 40 representations.

¹The image of knot diagram is generated by the software "**Draw programme**" developed by Andrew Bartholomew(http://www.layer8.co.uk/maths/draw/index.htm#Running-draw), where we modified some parts for our purpose(https://github.com/CATsTAILs/LinksPainter).

² All coefficients of polynomials are rational numbers. But the coefficients are sometimes approximated in decimal forms when there is not enough margin.

I.
$$I_1^u = \langle -1.54 \times 10^{25} u^{21} - 4.36 \times 10^{25} u^{20} + \dots + 2.35 \times 10^{27} b - 1.19 \times 10^{26}, \ 4.20 \times 10^{28} u^{21} + 1.34 \times 10^{29} u^{20} + \dots + 1.37 \times 10^{30} a + 5.84 \times 10^{30}, \ u^{22} + 3u^{21} + \dots - 160u + 73 \rangle$$

(i) Arc colorings

$$a_{7} = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_{9} = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} 1 \\ -u^{2} \end{pmatrix}$$

$$a_{6} = \begin{pmatrix} u^{3} + u \end{pmatrix}$$

$$a_{4} = \begin{pmatrix} -0.0305388u^{21} - 0.0973265u^{20} + \dots - 6.20155u - 4.25007 \\ 0.00654633u^{21} + 0.0185480u^{20} + \dots + 4.03131u + 0.0507530 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} u^{2} + 1 \\ -u^{4} - 2u^{2} \end{pmatrix}$$

$$a_{3} = \begin{pmatrix} -0.0269488u^{21} - 0.0862650u^{20} + \dots - 5.94433u - 3.75869 \\ 0.00399982u^{21} + 0.0101440u^{20} + \dots + 3.98951u - 0.419348 \end{pmatrix}$$

$$a_{8} = \begin{pmatrix} -0.0111557u^{21} - 0.0331545u^{20} + \dots - 11.4392u + 1.82405 \\ 0.00209278u^{21} + 0.00628667u^{20} + \dots + 2.38388u - 0.320958 \end{pmatrix}$$

$$a_{5} = \begin{pmatrix} -0.0325563u^{21} - 0.0995247u^{20} + \dots + 12.3684u - 1.68756 \\ 0.00662300u^{21} + 0.0176756u^{20} + \dots + 5.55048u - 0.614116 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} 0.00503747u^{21} + 0.0176554u^{20} + \dots + 0.745076u + 3.13839 \\ -0.000640784u^{21} - 0.00237253u^{20} + \dots - 0.108742u - 0.457982 \end{pmatrix}$$

$$a_{2} = \begin{pmatrix} 0.0016342u^{21} - 0.0404516u^{20} + \dots + 5.25864u - 5.57795 \\ 0.000768008u^{21} + 0.00322339u^{20} + \dots + 0.588075u + 0.675650 \end{pmatrix}$$

$$a_{1} = \begin{pmatrix} -0.00471751u^{21} - 0.0164802u^{20} + \dots + 0.689358u - 2.34200 \\ 0.000443931u^{21} + 0.00178731u^{20} + \dots + 0.0810747u + 0.491670 \end{pmatrix}$$

- (ii) Obstruction class = -1
- (iii) Cusp Shapes = $0.0299967u^{21} + 0.106465u^{20} + \cdots 19.9627u + 12.9465$

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
c_1	$u^{22} + 19u^{21} + \dots + 79u + 16$
c_2, c_5	$u^{22} + 7u^{21} + \dots + 35u + 4$
c_3	$u^{22} - 16u^{21} + \dots + 25000u + 3104$
c_4, c_8	$u^{22} - u^{21} + \dots + 1536u + 2048$
c_6, c_9, c_{10}	$u^{22} + 3u^{21} + \dots - 160u + 73$
c_7, c_{11}	$u^{22} + 3u^{21} + \dots + 182u + 73$
c_{12}	$u^{22} + 7u^{21} + \dots - 67032u + 5329$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
c_1	$y^{22} - 25y^{21} + \dots + 179903y + 256$
c_2, c_5	$y^{22} + 19y^{21} + \dots + 79y + 16$
c_3	$y^{22} - 78y^{21} + \dots + 78714048y + 9634816$
c_4, c_8	$y^{22} + 91y^{21} + \dots + 30670848y + 4194304$
c_6, c_9, c_{10}	$y^{22} + 45y^{21} + \dots + 149016y + 5329$
c_7,c_{11}	$y^{22} - 7y^{21} + \dots + 67032y + 5329$
c_{12}	$y^{22} + 85y^{21} + \dots + 2794246372y + 28398241$

(vi) Complex Volumes and Cusp Shapes

Solutions to I_1^u	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
u = 0.166885 + 0.855784I		
a = 0.884204 - 0.564449I	-1.86083 + 1.88410I	-4.29628 - 4.39442I
b = -0.685307 - 0.431142I		
u = 0.166885 - 0.855784I		
a = 0.884204 + 0.564449I	-1.86083 - 1.88410I	-4.29628 + 4.39442I
b = -0.685307 + 0.431142I		
u = 1.245170 + 0.161308I		
a = -0.584895 + 0.469137I	-3.01876 + 2.75600I	1.05384 - 1.99167I
b = 0.88430 - 1.76284I		
u = 1.245170 - 0.161308I		
a = -0.584895 - 0.469137I	-3.01876 - 2.75600I	1.05384 + 1.99167I
b = 0.88430 + 1.76284I		
u = 0.065911 + 1.393150I		
a = -0.167886 + 0.219714I	-7.41484 + 5.99413I	-4.98068 - 7.65331I
b = 0.208154 + 0.992360I		
u = 0.065911 - 1.393150I		
a = -0.167886 - 0.219714I	-7.41484 - 5.99413I	-4.98068 + 7.65331I
b = 0.208154 - 0.992360I		
u = -0.147428 + 0.530014I		
a = 2.56324 - 1.19415I	0.18307 - 2.82080I	2.85537 - 1.68871I
b = -0.391902 - 0.411319I		
u = -0.147428 - 0.530014I		
a = 2.56324 + 1.19415I	0.18307 + 2.82080I	2.85537 + 1.68871I
b = -0.391902 + 0.411319I		
u = 0.309359 + 0.401971I		
a = -0.508079 - 0.818004I	0.445026 + 1.231770I	4.87220 - 5.67709I
b = 0.193284 + 0.440196I		
u = 0.309359 - 0.401971I		
a = -0.508079 + 0.818004I	0.445026 - 1.231770I	4.87220 + 5.67709I
b = 0.193284 - 0.440196I		

Solutions to I_1^u	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
u = -0.14190 + 1.59059I		
a = -0.104582 - 0.310705I	-5.61868 + 1.54212I	1.66178 - 2.03716I
b = -0.841835 - 0.832729I		
u = -0.14190 - 1.59059I		
a = -0.104582 + 0.310705I	-5.61868 - 1.54212I	1.66178 + 2.03716I
b = -0.841835 + 0.832729I		
u = -0.009993 + 0.350116I		
a = -3.01267 - 0.71642I	0.96093 + 1.37462I	8.72525 - 4.65494I
b = 0.469397 + 0.461238I		
u = -0.009993 - 0.350116I		
a = -3.01267 + 0.71642I	0.96093 - 1.37462I	8.72525 + 4.65494I
b = 0.469397 - 0.461238I		
u = -0.69231 + 1.86047I		
a = -0.585229 - 1.015730I	15.9166 - 13.0727I	0.81219 + 5.19676I
b = 1.41273 - 1.99234I		
u = -0.69231 - 1.86047I		
a = -0.585229 + 1.015730I	15.9166 + 13.0727I	0.81219 - 5.19676I
b = 1.41273 + 1.99234I		
u = -0.61577 + 2.17742I		
a = 0.394124 + 0.984688I	19.2619 - 5.9056I	2.16347 + 1.69823I
b = -1.03067 + 2.69186I		
u = -0.61577 - 2.17742I		
a = 0.394124 - 0.984688I	19.2619 + 5.9056I	2.16347 - 1.69823I
b = -1.03067 - 2.69186I		
u = -1.57086 + 2.18266I		
a = 0.515590 + 0.201211I	-13.72130 - 3.06559I	0
b = 1.02473 + 4.03132I		
u = -1.57086 - 2.18266I		
a = 0.515590 - 0.201211I	-13.72130 + 3.06559I	0
b = 1.02473 - 4.03132I		

Solutions to I_1^u	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
u = -0.10906 + 2.96605I		
a = -0.102719 - 0.793534I	12.96110 + 1.49730I	0
b = -0.74289 - 4.42273I		
u = -0.10906 - 2.96605I		
a = -0.102719 + 0.793534I	12.96110 - 1.49730I	0
b = -0.74289 + 4.42273I		

II.
$$I_2^u = \langle b, 6u^3a - 3u^3 + \dots - 6a - 7, u^4 - u^3 + 3u^2 - 2u + 1 \rangle$$

(i) Arc colorings

$$a_{7} = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_{9} = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} 1 \\ -u^{2} \end{pmatrix}$$

$$a_{6} = \begin{pmatrix} -u \\ u^{3} + u \end{pmatrix}$$

$$a_{4} = \begin{pmatrix} a \\ 0 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} u^{2} + 1 \\ -u^{3} + u^{2} - 2u + 1 \end{pmatrix}$$

$$a_{3} = \begin{pmatrix} u^{3}a - 2u^{2}a + 2au \\ u^{3}a - 2u^{2}a + au \end{pmatrix}$$

$$a_{8} = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{5} = \begin{pmatrix} a \\ 0 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} u^{3} + 2u \\ -u^{3} + u^{2} - 2u + 1 \end{pmatrix}$$

$$a_{2} = \begin{pmatrix} u^{3}a - 2u^{2}a + \frac{3}{2}u^{3} + 2au - u^{2} + \frac{7}{2}u - \frac{3}{2} \\ u^{3}a - 2u^{2}a + au \end{pmatrix}$$

$$a_{1} = \begin{pmatrix} u \\ -u^{3} - u \end{pmatrix}$$

- (ii) Obstruction class = 1
- (iii) Cusp Shapes = $\frac{9}{2}u^3a 5u^2a \frac{19}{4}u^3 + \frac{21}{2}au + \frac{7}{2}u^2 \frac{7}{2}a \frac{55}{4}u + \frac{17}{4}u^2$

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
c_1, c_3, c_5	$(u^2 - u + 1)^4$
c_2	$(u^2+u+1)^4$
c_4, c_8	u^8
<i>C</i> ₆	$(u^4 + u^3 + 3u^2 + 2u + 1)^2$
	$(u^4 + u^3 + u^2 + 1)^2$
c_9, c_{10}, c_{12}	$(u^4 - u^3 + 3u^2 - 2u + 1)^2$
c_{11}	$(u^4 - u^3 + u^2 + 1)^2$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
c_1, c_2, c_3 c_5	$(y^2 + y + 1)^4$
c_4, c_8	y^8
c_6, c_9, c_{10} c_{12}	$(y^4 + 5y^3 + 7y^2 + 2y + 1)^2$
c_{7}, c_{11}	$(y^4 + y^3 + 3y^2 + 2y + 1)^2$

(vi) Complex Volumes and Cusp Shapes

Solutions to I_2^u	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
u = 0.395123 + 0.506844I		
a = -1.13839 - 1.09665I	0.21101 + 3.44499I	3.71851 - 10.46973I
b = 0		
u = 0.395123 + 0.506844I		
a = 1.51892 - 0.43755I	0.211005 - 0.614778I	1.372162 - 0.328352I
b = 0		
u = 0.395123 - 0.506844I		
a = -1.13839 + 1.09665I	0.21101 - 3.44499I	3.71851 + 10.46973I
b = 0		
u = 0.395123 - 0.506844I		
a = 1.51892 + 0.43755I	0.211005 + 0.614778I	1.372162 + 0.328352I
b = 0		
u = 0.10488 + 1.55249I		
a = -0.435815 + 0.100890I	-6.79074 + 5.19385I	0.529613 - 1.243149I
b = 0		
u = 0.10488 + 1.55249I		
a = 0.305281 + 0.326982I	-6.79074 + 1.13408I	-4.49529 - 1.20873I
b = 0		
u = 0.10488 - 1.55249I		
a = -0.435815 - 0.100890I	-6.79074 - 5.19385I	0.529613 + 1.243149I
b = 0		
u = 0.10488 - 1.55249I		
a = 0.305281 - 0.326982I	-6.79074 - 1.13408I	-4.49529 + 1.20873I
b = 0		

III. $I_3^u = \langle -a^4u + a^3u + \dots - 2a^2 - 4a, \ a^4u - 2a^3u + \dots + 4a + 4, \ u^2 + 1 \rangle$

(i) Arc colorings

$$a_{7} = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_{9} = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} 1 \\ 1 \end{pmatrix}$$

$$a_{6} = \begin{pmatrix} -u \\ 0 \end{pmatrix}$$

$$a_{4} = \begin{pmatrix} \frac{1}{4}a^{4}u - \frac{1}{4}a^{3}u + \dots + \frac{1}{2}a^{2} + a \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 0 \\ 1 \end{pmatrix}$$

$$a_{3} = \begin{pmatrix} -\frac{1}{4}a^{4}u + \frac{1}{4}a^{3}u + \dots + \frac{1}{4}a^{3} - \frac{1}{2}a^{2} \\ \frac{1}{4}a^{4}u - \frac{1}{4}a^{3}u + \dots + \frac{1}{2}a^{2} + a \end{pmatrix}$$

$$a_{8} = \begin{pmatrix} -\frac{1}{2}a^{3}u + a^{2}u + \dots + \frac{1}{2}a - 3 \end{pmatrix}$$

$$a_{5} = \begin{pmatrix} \frac{1}{4}a^{3}u - \frac{1}{2}a^{2}u + \dots - \frac{1}{4}a^{3} + 1 \\ -\frac{1}{2}a^{4}u + \frac{3}{4}a^{3}u + \dots - 2a^{2} - a \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} 1 \\ -\frac{1}{4}a^{4}u + \frac{1}{2}a^{3}u + \dots - \frac{1}{2}a + 1 \end{pmatrix}$$

$$a_{2} = \begin{pmatrix} \frac{1}{2}a^{4}u + \frac{1}{4}a^{3}u + \dots - 2a^{2} - \frac{1}{2}a \end{pmatrix}$$

$$a_{1} = \begin{pmatrix} -\frac{1}{4}a^{4}u + \frac{1}{2}a^{3}u + \dots + 2a^{2} + \frac{1}{2}a \end{pmatrix}$$

$$a_{1} = \begin{pmatrix} 1 \\ -\frac{1}{4}a^{4}u + \frac{1}{2}a^{3}u + \dots - a^{2} - \frac{1}{2}a \end{pmatrix}$$

- (ii) Obstruction class = 1
- (iii) Cusp Shapes = $a^4 + 2a^3u 2a^3 6a^2u + 8$

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
c_1	$(u^5 - 3u^4 + 4u^3 - u^2 - u + 1)^2$
c_2	$(u^5 - u^4 + 2u^3 - u^2 + u - 1)^2$
<i>c</i> ₃	$(u^5 + u^4 - 2u^3 - u^2 + u - 1)^2$
c_4, c_8	$u^{10} + 5u^8 + 8u^6 + 3u^4 - u^2 + 1$
<i>C</i> ₅	$(u^5 + u^4 + 2u^3 + u^2 + u + 1)^2$
c_6, c_7, c_9 c_{10}, c_{11}	$(u^2+1)^5$
c_{12}	$(u-1)^{10}$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
c_1	$(y^5 - y^4 + 8y^3 - 3y^2 + 3y - 1)^2$
c_{2}, c_{5}	$(y^5 + 3y^4 + 4y^3 + y^2 - y - 1)^2$
c_3	$(y^5 - 5y^4 + 8y^3 - 3y^2 - y - 1)^2$
c_4, c_8	$(y^5 + 5y^4 + 8y^3 + 3y^2 - y + 1)^2$
c_6, c_7, c_9 c_{10}, c_{11}	$(y+1)^{10}$
c_{12}	$(y-1)^{10}$

(vi) Complex Volumes and Cusp Shapes

Solutions to I_3^u	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
u = 1.000000I		
a = -0.794743 + 0.582062I	-5.87256 - 4.40083I	-0.74431 + 3.49859I
b = 0.21917 + 1.41878I		
u = 1.000000I		
a = -0.582062 + 0.794743I	-5.87256 + 4.40083I	-0.74431 - 3.49859I
b = -0.21917 + 1.41878I		
u = 1.000000I		
a = 0.821196 - 0.821196I	-2.40108	2.51886 + 0.I
b = -1.217740I		
u = 1.000000I		
a = 2.15793 + 0.60232I	-0.32910 + 1.53058I	3.48489 - 4.43065I
b = -0.549911 - 0.309916I		
u = 1.000000I		
a = -0.60232 - 2.15793I	-0.32910 - 1.53058I	3.48489 + 4.43065I
b = 0.549911 - 0.309916I		
u = -1.000000I		
a = -0.582062 - 0.794743I	-5.87256 + 4.40083I	-0.74431 - 3.49859I
b = -0.21917 - 1.41878I		
u = -1.000000I		
a = -0.794743 - 0.582062I	-5.87256 - 4.40083I	-0.74431 + 3.49859I
b = 0.21917 - 1.41878I		
u = -1.000000I		
a = 0.821196 + 0.821196I	-2.40108	2.51886 + 0.I
b = 1.217740I		
u = -1.000000I		
a = 2.15793 - 0.60232I	-0.32910 - 1.53058I	3.48489 + 4.43065I
b = -0.549911 + 0.309916I		
u = -1.000000I		
a = -0.60232 + 2.15793I	-0.32910 + 1.53058I	3.48489 - 4.43065I
b = 0.549911 + 0.309916I		

IV. u-Polynomials

Crossings	u-Polynomials at each crossing
c_1	$(u^{2} - u + 1)^{4}(u^{5} - 3u^{4} + 4u^{3} - u^{2} - u + 1)^{2}$ $\cdot (u^{22} + 19u^{21} + \dots + 79u + 16)$
c_2	$((u^{2} + u + 1)^{4})(u^{5} - u^{4} + \dots + u - 1)^{2}(u^{22} + 7u^{21} + \dots + 35u + 4)$
c_3	$(u^{2} - u + 1)^{4}(u^{5} + u^{4} - 2u^{3} - u^{2} + u - 1)^{2}$ $\cdot (u^{22} - 16u^{21} + \dots + 25000u + 3104)$
c_4, c_8	$u^{8}(u^{10} + 5u^{8} + \dots - u^{2} + 1)(u^{22} - u^{21} + \dots + 1536u + 2048)$
<i>C</i> 5	$((u^{2}-u+1)^{4})(u^{5}+u^{4}+\cdots+u+1)^{2}(u^{22}+7u^{21}+\cdots+35u+4)$
c_6	$((u^{2}+1)^{5})(u^{4}+u^{3}+3u^{2}+2u+1)^{2}(u^{22}+3u^{21}+\cdots-160u+73)$
c_7	$((u^{2}+1)^{5})(u^{4}+u^{3}+u^{2}+1)^{2}(u^{22}+3u^{21}+\cdots+182u+73)$
c_{9}, c_{10}	$((u^{2}+1)^{5})(u^{4}-u^{3}+3u^{2}-2u+1)^{2}(u^{22}+3u^{21}+\cdots-160u+73)$
c_{11}	$((u^{2}+1)^{5})(u^{4}-u^{3}+u^{2}+1)^{2}(u^{22}+3u^{21}+\cdots+182u+73)$
c_{12}	$(u-1)^{10}(u^4 - u^3 + 3u^2 - 2u + 1)^2$ $\cdot (u^{22} + 7u^{21} + \dots - 67032u + 5329)$

V. Riley Polynomials

Crossings	Riley Polynomials at each crossing
c_1	$(y^{2} + y + 1)^{4}(y^{5} - y^{4} + 8y^{3} - 3y^{2} + 3y - 1)^{2}$ $\cdot (y^{22} - 25y^{21} + \dots + 179903y + 256)$
c_2, c_5	$(y^{2} + y + 1)^{4}(y^{5} + 3y^{4} + 4y^{3} + y^{2} - y - 1)^{2}$ $\cdot (y^{22} + 19y^{21} + \dots + 79y + 16)$
c_3	$(y^{2} + y + 1)^{4}(y^{5} - 5y^{4} + 8y^{3} - 3y^{2} - y - 1)^{2}$ $\cdot (y^{22} - 78y^{21} + \dots + 78714048y + 9634816)$
c_4, c_8	$y^{8}(y^{5} + 5y^{4} + 8y^{3} + 3y^{2} - y + 1)^{2}$ $\cdot (y^{22} + 91y^{21} + \dots + 30670848y + 4194304)$
c_6, c_9, c_{10}	$(y+1)^{10}(y^4+5y^3+7y^2+2y+1)^2$ $\cdot (y^{22}+45y^{21}+\dots+149016y+5329)$
c_7, c_{11}	$(y+1)^{10}(y^4+y^3+3y^2+2y+1)^2$ $\cdot (y^{22}-7y^{21}+\dots+67032y+5329)$
c_{12}	$(y-1)^{10}(y^4 + 5y^3 + 7y^2 + 2y + 1)^2$ $\cdot (y^{22} + 85y^{21} + \dots + 2794246372y + 28398241)$