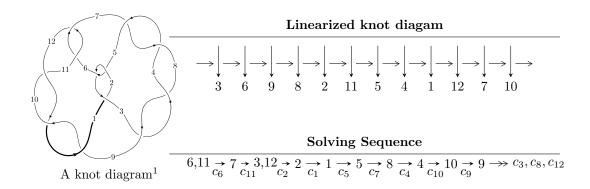
$12a_{0356} \ (K12a_{0356})$



Ideals for irreducible components² of X_{par}

$$I_1^u = \langle -5.66231 \times 10^{18} u^{58} + 4.32374 \times 10^{18} u^{57} + \dots + 8.19653 \times 10^{18} b + 1.17819 \times 10^{19},$$

$$7.79962 \times 10^{19} u^{58} - 1.20924 \times 10^{20} u^{57} + \dots + 4.91792 \times 10^{19} a - 4.08773 \times 10^{20}, \ u^{59} - 2u^{58} + \dots + u + 3 \rangle$$

$$I_2^u = \langle b - 1, \ a^2 + 2au + 3u^2 - 2a - 6u + 3, \ u^3 - u^2 + 1 \rangle$$

$$I_3^u = \langle b + 1, \ a + u + 1, \ u^3 + u^2 - 1 \rangle$$

* 3 irreducible components of $\dim_{\mathbb{C}} = 0$, with total 68 representations.

¹The image of knot diagram is generated by the software "**Draw programme**" developed by Andrew Bartholomew(http://www.layer8.co.uk/maths/draw/index.htm#Running-draw), where we modified some parts for our purpose(https://github.com/CATsTAILs/LinksPainter).

² All coefficients of polynomials are rational numbers. But the coefficients are sometimes approximated in decimal forms when there is not enough margin.

 $\begin{matrix} \text{I.} \\ I_1^u = \langle -5.66 \times 10^{18} u^{58} + 4.32 \times 10^{18} u^{57} + \dots + 8.20 \times 10^{18} b + 1.18 \times 10^{19}, \ 7.80 \times 10^{19} u^{58} - 1.21 \times 10^{20} u^{57} + \dots + 4.92 \times 10^{19} a - 4.09 \times 10^{20}, \ u^{59} - 2u^{58} + \dots + u + 3 \rangle \end{matrix}$

(i) Arc colorings

$$a_{6} = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_{7} = \begin{pmatrix} 1 \\ u^{2} \end{pmatrix}$$

$$a_{3} = \begin{pmatrix} -1.58596u^{58} + 2.45885u^{57} + \dots + 9.55113u + 8.31191 \\ 0.690818u^{58} - 0.527509u^{57} + \dots - 0.607836u - 1.43742 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} -u \\ -u^{3} + u \end{pmatrix}$$

$$a_{2} = \begin{pmatrix} -0.895140u^{58} + 1.93134u^{57} + \dots + 8.94330u + 6.87449 \\ 0.690818u^{58} - 0.527509u^{57} + \dots - 0.607836u - 1.43742 \end{pmatrix}$$

$$a_{1} = \begin{pmatrix} -u^{5} - u \\ -u^{7} + u^{5} - 2u^{3} + u \end{pmatrix}$$

$$a_{5} = \begin{pmatrix} 1.92952u^{58} - 2.67059u^{57} + \dots - 12.7404u - 7.85154 \\ -0.222016u^{58} - 0.0475838u^{57} + \dots + 0.650562u - 0.281439 \end{pmatrix}$$

$$a_{8} = \begin{pmatrix} 1.18721u^{58} - 1.74998u^{57} + \dots + 3.24272u + 0.910386 \\ 0.412864u^{58} - 0.942970u^{57} + \dots - 5.73768u - 1.86980 \end{pmatrix}$$

$$a_{4} = \begin{pmatrix} -1.56955u^{58} + 2.85972u^{57} + \dots + 12.4812u + 9.51305 \\ 0.495410u^{58} - 0.282318u^{57} + \dots + 1.25035u - 0.561736 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} u^{3} \\ u^{5} - u^{3} + u \end{pmatrix}$$

$$a_{9} = \begin{pmatrix} u^{7} + 2u^{3} \\ u^{9} - u^{7} + 3u^{5} - 2u^{3} + u \end{pmatrix}$$

(ii) Obstruction class = -1

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
c_1	$u^{59} + 24u^{58} + \dots - 32u + 1$
c_2,c_5	$u^{59} + 4u^{58} + \dots - 4u + 1$
c_3, c_4, c_7 c_8	$u^{59} - u^{58} + \dots + 64u^2 + 8$
c_6, c_{11}	$u^{59} - 2u^{58} + \dots + u + 3$
c_9, c_{10}, c_{12}	$u^{59} + 14u^{58} + \dots + 157u + 9$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
c_1	$y^{59} + 32y^{58} + \dots - 1936y - 1$
c_{2}, c_{5}	$y^{59} - 24y^{58} + \dots - 32y - 1$
c_3, c_4, c_7 c_8	$y^{59} + 73y^{58} + \dots - 1024y - 64$
c_6, c_{11}	$y^{59} - 14y^{58} + \dots + 157y - 9$
c_9, c_{10}, c_{12}	$y^{59} + 66y^{58} + \dots - 1307y - 81$

(vi) Complex Volumes and Cusp Shapes

Solutions to I_1^u	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
u = -0.950749 + 0.085534I		
a = 1.40102 + 0.37767I	-2.20168 - 1.55351I	-13.9942 + 4.5761I
b = 0.881025 + 0.388729I		
u = -0.950749 - 0.085534I		
a = 1.40102 - 0.37767I	-2.20168 + 1.55351I	-13.9942 - 4.5761I
b = 0.881025 - 0.388729I		
u = 0.955755 + 0.424887I		
a = 1.39192 - 1.56772I	-0.26151 - 6.93624I	-11.4611 + 10.0156I
b = 1.001090 + 0.566158I		
u = 0.955755 - 0.424887I		
a = 1.39192 + 1.56772I	-0.26151 + 6.93624I	-11.4611 - 10.0156I
b = 1.001090 - 0.566158I		
u = 1.061230 + 0.059722I		
a = -1.249430 + 0.518825I	5.44848 + 2.62573I	-10.72193 - 2.36500I
b = -0.871450 + 0.680013I		
u = 1.061230 - 0.059722I		
a = -1.249430 - 0.518825I	5.44848 - 2.62573I	-10.72193 + 2.36500I
b = -0.871450 - 0.680013I		
u = 0.808456 + 0.470326I		
a = -0.499696 - 0.009506I	1.30057 - 2.44037I	-6.97566 + 5.43591I
b = 0.399158 - 0.576724I		
u = 0.808456 - 0.470326I		
a = -0.499696 + 0.009506I	1.30057 + 2.44037I	-6.97566 - 5.43591I
b = 0.399158 + 0.576724I		
u = -0.841496 + 0.395242I		
a = -0.96036 - 2.04635I	-1.79109 + 3.29910I	-14.9386 - 5.3714I
b = -0.942517 + 0.431284I		
u = -0.841496 - 0.395242I		
a = -0.96036 + 2.04635I	-1.79109 - 3.29910I	-14.9386 + 5.3714I
b = -0.942517 - 0.431284I		

Solutions to I_1^u	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
u = -0.428912 + 0.779191I		
a = 0.069578 - 1.101110I	10.95100 + 1.36331I	-3.49056 - 2.36160I
b = -0.759172 + 0.857390I		
u = -0.428912 - 0.779191I		
a = 0.069578 + 1.101110I	10.95100 - 1.36331I	-3.49056 + 2.36160I
b = -0.759172 - 0.857390I		
u = -1.039320 + 0.443029I		
a = -1.56082 - 1.25858I	7.76213 + 9.14001I	-12.0000 - 7.5958I
b = -1.062320 + 0.707142I		
u = -1.039320 - 0.443029I		
a = -1.56082 + 1.25858I	7.76213 - 9.14001I	-12.0000 + 7.5958I
b = -1.062320 - 0.707142I		
u = 0.883608 + 0.704164I		
a = 0.236690 - 0.559685I	1.94353 - 2.69934I	0
b = 0.746146 - 0.071860I		
u = 0.883608 - 0.704164I		
a = 0.236690 + 0.559685I	1.94353 + 2.69934I	0
b = 0.746146 + 0.071860I		
u = -0.995779 + 0.541016I		
a = 0.394659 - 0.390928I	9.11589 + 3.43180I	-12.00000 + 0.I
b = -0.608688 - 0.798203I		
u = -0.995779 - 0.541016I		
a = 0.394659 + 0.390928I	9.11589 - 3.43180I	-12.00000 + 0.I
b = -0.608688 + 0.798203I		
u = -0.865723 + 0.753965I		
a = -0.987861 + 0.232003I	7.97460 + 2.84682I	0
b = 0.0644711 - 0.1218690I		
u = -0.865723 - 0.753965I		
a = -0.987861 - 0.232003I	7.97460 - 2.84682I	0
b = 0.0644711 + 0.1218690I		

Solutions to I_1^u	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
u = -0.287017 + 0.779308I		
a = 0.328056 + 0.939299I	10.23980 - 4.73907I	-4.25165 + 2.78795I
b = -0.992597 - 0.783531I		
u = -0.287017 - 0.779308I		
a = 0.328056 - 0.939299I	10.23980 + 4.73907I	-4.25165 - 2.78795I
b = -0.992597 + 0.783531I		
u = -0.718782 + 0.401065I		
a = 1.86408 + 0.41857I	3.40228 + 1.59157I	-9.70315 - 4.05404I
b = 1.231790 + 0.111942I		
u = -0.718782 - 0.401065I		
a = 1.86408 - 0.41857I	3.40228 - 1.59157I	-9.70315 + 4.05404I
b = 1.231790 - 0.111942I		
u = 0.779291 + 0.186002I		
a = -1.76043 + 0.35358I	-2.95013 - 0.58618I	-15.2527 + 9.8012I
b = -1.092770 + 0.150850I		
u = 0.779291 - 0.186002I		
a = -1.76043 - 0.35358I	-2.95013 + 0.58618I	-15.2527 - 9.8012I
b = -1.092770 - 0.150850I		
u = -0.893562 + 0.803723I		
a = -0.002799 - 0.814217I	2.63289 + 3.01191I	0
b = -1.251010 - 0.015615I		
u = -0.893562 - 0.803723I		
a = -0.002799 + 0.814217I	2.63289 - 3.01191I	0
b = -1.251010 + 0.015615I		
u = -0.854945 + 0.893449I		
a = -0.723640 - 1.049790I	8.28053 - 4.23254I	0
b = 1.036460 + 0.751160I		
u = -0.854945 - 0.893449I		
a = -0.723640 + 1.049790I	8.28053 + 4.23254I	0
b = 1.036460 - 0.751160I		

Solutions to I_1^u	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
u = 0.886324 + 0.866549I		
a = 0.98642 - 1.06679I	5.94223 - 0.39886I	0
b = -0.845945 + 0.735665I		
u = 0.886324 - 0.866549I		
a = 0.98642 + 1.06679I	5.94223 + 0.39886I	0
b = -0.845945 - 0.735665I		
u = 0.832835 + 0.926311I		
a = 0.571242 - 0.903844I	16.9600 + 7.2294I	0
b = -1.18749 + 0.79875I		
u = 0.832835 - 0.926311I		
a = 0.571242 + 0.903844I	16.9600 - 7.2294I	0
b = -1.18749 - 0.79875I		
u = -0.897663 + 0.871706I		
a = -0.13642 + 1.69360I	9.36550 + 1.73164I	0
b = 0.673711 - 0.844140I		
u = -0.897663 - 0.871706I		
a = -0.13642 - 1.69360I	9.36550 - 1.73164I	0
b = 0.673711 + 0.844140I		
u = 0.915394 + 0.861826I		
a = -0.067431 - 0.859114I	10.78160 - 3.19575I	0
b = 1.48127 - 0.02057I		
u = 0.915394 - 0.861826I		
a = -0.067431 + 0.859114I	10.78160 + 3.19575I	0
b = 1.48127 + 0.02057I		
u = 0.938182 + 0.846227I		
a = 0.00707 + 2.10628I	5.77879 - 5.95695I	0
b = -0.898285 - 0.723052I		
u = 0.938182 - 0.846227I		
a = 0.00707 - 2.10628I	5.77879 + 5.95695I	0
b = -0.898285 + 0.723052I		

Solutions to I_1^u	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
u = -0.933873 + 0.857641I		
a = -1.114390 - 0.849709I	9.25182 + 4.67664I	0
b = 0.624353 + 0.869336I		
u = -0.933873 - 0.857641I		
a = -1.114390 + 0.849709I	9.25182 - 4.67664I	0
b = 0.624353 - 0.869336I		
u = 0.875079 + 0.923683I		
a = -0.06377 + 1.45605I	18.8901 + 0.4011I	0
b = -0.571370 - 1.103440I		
u = 0.875079 - 0.923683I		
a = -0.06377 - 1.45605I	18.8901 - 0.4011I	0
b = -0.571370 + 1.103440I		
u = 0.469446 + 0.544141I		
a = -0.223809 - 1.235640I	2.26071 - 1.37979I	-4.27858 + 3.91647I
b = 0.654076 + 0.529004I		
u = 0.469446 - 0.544141I		
a = -0.223809 + 1.235640I	2.26071 + 1.37979I	-4.27858 - 3.91647I
b = 0.654076 - 0.529004I		
u = 0.667363 + 0.266454I		
a = -0.70482 - 2.96122I	2.81040 - 1.03770I	-8.02636 + 6.84259I
b = 0.852790 + 0.242476I		
u = 0.667363 - 0.266454I		
a = -0.70482 + 2.96122I	2.81040 + 1.03770I	-8.02636 - 6.84259I
b = 0.852790 - 0.242476I		
u = -0.972360 + 0.842990I		
a = 0.31648 + 2.17743I	7.90798 + 10.65770I	0
b = 1.070130 - 0.736498I		
u = -0.972360 - 0.842990I		
a = 0.31648 - 2.17743I	7.90798 - 10.65770I	0
b = 1.070130 + 0.736498I		

Solutions to I_1^u	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
u = 0.312980 + 0.623983I		
a = -0.499965 + 1.002160I	1.73082 + 3.05513I	-5.72428 - 4.49353I
b = 0.872314 - 0.581880I		
u = 0.312980 - 0.623983I		
a = -0.499965 - 1.002160I	1.73082 - 3.05513I	-5.72428 + 4.49353I
b = 0.872314 + 0.581880I		
u = 1.002690 + 0.845529I		
a = -0.53525 + 2.09749I	16.4153 - 13.7600I	0
b = -1.20584 - 0.77319I		
u = 1.002690 - 0.845529I		
a = -0.53525 - 2.09749I	16.4153 + 13.7600I	0
b = -1.20584 + 0.77319I		
u = 0.980128 + 0.871697I		
a = 1.090820 - 0.722028I	18.5511 - 7.0143I	0
b = -0.524644 + 1.106680I		
u = 0.980128 - 0.871697I		
a = 1.090820 + 0.722028I	18.5511 + 7.0143I	0
b = -0.524644 - 1.106680I		
u = -0.450920 + 0.353539I		
a = 1.152780 + 0.540477I	-0.634650 - 0.118465I	-11.69433 - 0.33232I
b = -0.620312 - 0.297342I		
u = -0.450920 - 0.353539I		
a = 1.152780 - 0.540477I	-0.634650 + 0.118465I	-11.69433 + 0.33232I
b = -0.620312 + 0.297342I		
u = -0.475308		
a = 0.893509	-0.673099	-14.6220
b = -0.308761		

II.
$$I_2^u = \langle b-1, a^2+2au+3u^2-2a-6u+3, u^3-u^2+1 \rangle$$

(i) Arc colorings

$$a_{6} = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_{7} = \begin{pmatrix} 1 \\ u^{2} \end{pmatrix}$$

$$a_{3} = \begin{pmatrix} a \\ 1 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} -u \\ -u^{2} + u + 1 \end{pmatrix}$$

$$a_{2} = \begin{pmatrix} 1 \\ 1 \end{pmatrix}$$

$$a_{1} = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{5} = \begin{pmatrix} -a \\ -1 \end{pmatrix}$$

$$a_{8} = \begin{pmatrix} -a - 3u + 4 \\ -u^{2}a + u^{2} + 1 \end{pmatrix}$$

$$a_{4} = \begin{pmatrix} u^{2}a + a - 1 \\ u^{2}a - au - u^{2} - a + 1 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} u^{2} - 1 \\ -u^{2} \end{pmatrix}$$

$$a_{9} = \begin{pmatrix} -1 \\ -u^{2} \end{pmatrix}$$

- (ii) Obstruction class = 1
- (iii) Cusp Shapes = 4u 12

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
c_1, c_5	$(u-1)^{6}$
c_2	$(u+1)^6$
c_3, c_4, c_7 c_8	$(u^2+2)^3$
c_6	$(u^3 - u^2 + 1)^2$
c_9,c_{10}	$(u^3 - u^2 + 2u - 1)^2$
c_{11}	$(u^3 + u^2 - 1)^2$
c_{12}	$(u^3 + u^2 + 2u + 1)^2$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
c_1, c_2, c_5	$(y-1)^6$
c_3, c_4, c_7 c_8	$(y+2)^6$
c_6, c_{11}	$(y^3 - y^2 + 2y - 1)^2$
c_9, c_{10}, c_{12}	$(y^3 + 3y^2 + 2y - 1)^2$

(vi) Complex Volumes and Cusp Shapes

Solutions to I_2^u	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
u = 0.877439 + 0.744862I		
a = 1.175960 - 0.571534I	6.31400 - 2.82812I	-8.49024 + 2.97945I
b = 1.00000		
u = 0.877439 + 0.744862I		
a = -0.930832 - 0.918189I	6.31400 - 2.82812I	-8.49024 + 2.97945I
b = 1.00000		
u = 0.877439 - 0.744862I		
a = 1.175960 + 0.571534I	6.31400 + 2.82812I	-8.49024 - 2.97945I
b = 1.00000		
u = 0.877439 - 0.744862I		
a = -0.930832 + 0.918189I	6.31400 + 2.82812I	-8.49024 - 2.97945I
b = 1.00000		
u = -0.754878		
a = 1.75488 + 2.48177I	2.17641	-15.0200
b = 1.00000		
u = -0.754878		
a = 1.75488 - 2.48177I	2.17641	-15.0200
b = 1.00000		

III.
$$I_3^u = \langle b+1, \ a+u+1, \ u^3+u^2-1 \rangle$$

(i) Arc colorings

a) Are colorings
$$a_{6} = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_{7} = \begin{pmatrix} 1 \\ u^{2} \end{pmatrix}$$

$$a_{3} = \begin{pmatrix} -u - 1 \\ -1 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} -u - 2 \\ -1 \end{pmatrix}$$

$$a_{1} = \begin{pmatrix} -1 \\ 0 \end{pmatrix}$$

$$a_{5} = \begin{pmatrix} -u - 1 \\ -1 \end{pmatrix}$$

$$a_{8} = \begin{pmatrix} 1 \\ u^{2} \end{pmatrix}$$

$$a_{4} = \begin{pmatrix} -u - 1 \\ -1 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} -u^{2} + 1 \\ u^{2} \end{pmatrix}$$

$$a_{9} = \begin{pmatrix} 1 \\ u^{2} \end{pmatrix}$$

- (ii) Obstruction class = 1
- (iii) Cusp Shapes = $4u^2 + 2u 16$

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
c_1, c_2	$(u-1)^3$
c_3, c_4, c_7 c_8	u^3
c_5	$(u+1)^3$
c_6	$u^3 + u^2 - 1$
c_9,c_{10}	$u^3 - u^2 + 2u - 1$
c_{11}	$u^3 - u^2 + 1$
c_{12}	$u^3 + u^2 + 2u + 1$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
c_1, c_2, c_5	$(y-1)^3$
c_3, c_4, c_7 c_8	y^3
c_6, c_{11}	$y^3 - y^2 + 2y - 1$
c_9, c_{10}, c_{12}	$y^3 + 3y^2 + 2y - 1$

(vi) Complex Volumes and Cusp Shapes

Solutions to I_3^u	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
u = -0.877439 + 0.744862I		
a = -0.122561 - 0.744862I	1.37919 + 2.82812I	-16.8946 - 3.7388I
b = -1.00000		
u = -0.877439 - 0.744862I		
a = -0.122561 + 0.744862I	1.37919 - 2.82812I	-16.8946 + 3.7388I
b = -1.00000		
u = 0.754878		
a = -1.75488	-2.75839	-12.2110
b = -1.00000		

IV. u-Polynomials

Crossings	u-Polynomials at each crossing
c_1	$((u-1)^9)(u^{59} + 24u^{58} + \dots - 32u + 1)$
c_2	$((u-1)^3)(u+1)^6(u^{59}+4u^{58}+\cdots-4u+1)$
c_3, c_4, c_7 c_8	$u^{3}(u^{2}+2)^{3}(u^{59}-u^{58}+\cdots+64u^{2}+8)$
c_5	$((u-1)^6)(u+1)^3(u^{59}+4u^{58}+\cdots-4u+1)$
c_6	$((u^3 - u^2 + 1)^2)(u^3 + u^2 - 1)(u^{59} - 2u^{58} + \dots + u + 3)$
c_9, c_{10}	$((u^3 - u^2 + 2u - 1)^3)(u^{59} + 14u^{58} + \dots + 157u + 9)$
c_{11}	$(u^3 - u^2 + 1)(u^3 + u^2 - 1)^2(u^{59} - 2u^{58} + \dots + u + 3)$
c_{12}	$((u^3 + u^2 + 2u + 1)^3)(u^{59} + 14u^{58} + \dots + 157u + 9)$

V. Riley Polynomials

Crossings	Riley Polynomials at each crossing
c_1	$((y-1)^9)(y^{59} + 32y^{58} + \dots - 1936y - 1)$
c_2,c_5	$((y-1)^9)(y^{59}-24y^{58}+\cdots-32y-1)$
c_3, c_4, c_7 c_8	$y^{3}(y+2)^{6}(y^{59}+73y^{58}+\cdots-1024y-64)$
c_6, c_{11}	$((y^3 - y^2 + 2y - 1)^3)(y^{59} - 14y^{58} + \dots + 157y - 9)$
c_9, c_{10}, c_{12}	$((y^3 + 3y^2 + 2y - 1)^3)(y^{59} + 66y^{58} + \dots - 1307y - 81)$