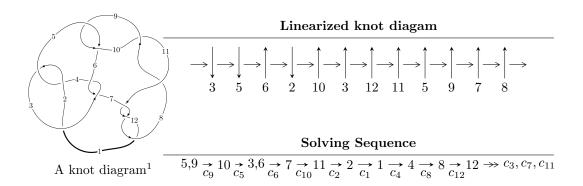
# $12n_{0120} \ (K12n_{0120})$



## Ideals for irreducible components<sup>2</sup> of $X_{par}$

$$\begin{split} I_1^u &= \langle 15121u^{16} - 24215u^{15} + \dots + 18155b - 26228, \ 15121u^{16} - 24215u^{15} + \dots + 18155a - 26228, \\ u^{17} - 2u^{16} + 2u^{15} + 7u^{13} - 14u^{12} + 14u^{11} - 2u^{10} + 7u^9 - 14u^8 + 14u^7 - 12u^6 - 2u^2 - u + 1 \rangle \\ I_2^u &= \langle -u^7 + u^6 + u^5 - 2u^4 - u^3 + 2u^2 + b + u - 2, \ -u^7 + u^6 + u^5 - 2u^4 - u^3 + 2u^2 + a - 2, \\ u^8 - u^7 - u^6 + 2u^5 + u^4 - 2u^3 + 2u - 1 \rangle \end{split}$$

\* 2 irreducible components of  $\dim_{\mathbb{C}} = 0$ , with total 25 representations.

<sup>&</sup>lt;sup>1</sup>The image of knot diagram is generated by the software "**Draw programme**" developed by Andrew Bartholomew(http://www.layer8.co.uk/maths/draw/index.htm#Running-draw), where we modified some parts for our purpose(https://github.com/CATsTAILs/LinksPainter).

 $<sup>^2</sup>$  All coefficients of polynomials are rational numbers. But the coefficients are sometimes approximated in decimal forms when there is not enough margin.

I. 
$$I_1^u = \langle 15121u^{16} - 24215u^{15} + \dots + 18155b - 26228, \ 15121u^{16} - 24215u^{15} + \dots + 18155a - 26228, \ u^{17} - 2u^{16} + \dots - u + 1 \rangle$$

(i) Arc colorings

$$a_{5} = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_{9} = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} 1 \\ -u^{2} \end{pmatrix}$$

$$a_{3} = \begin{pmatrix} -0.832884u^{16} + 1.33379u^{15} + \dots + 1.24985u + 1.44467 \\ -0.832884u^{16} + 1.33379u^{15} + \dots + 2.24985u + 1.44467 \end{pmatrix}$$

$$a_{6} = \begin{pmatrix} u \\ -u^{3} + u \end{pmatrix}$$

$$a_{7} = \begin{pmatrix} 0.102561u^{16} + 0.104654u^{15} + \dots - 0.0345359u - 0.615037 \\ 0.0863674u^{16} + 0.0881300u^{15} + \dots - 0.0290829u - 0.623189 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} -u^{2} + 1 \\ -u^{2} \end{pmatrix}$$

$$a_{2} = \begin{pmatrix} -0.832884u^{16} + 1.33379u^{15} + \dots + 1.24985u + 1.44467 \\ -0.830185u^{16} + 1.33655u^{15} + \dots + 1.74894u + 1.11270 \end{pmatrix}$$

$$a_{1} = \begin{pmatrix} 0.368438u^{16} - 0.644451u^{15} + \dots + 0.212669u - 0.317929 \\ 0.471000u^{16} - 0.539796u^{15} + \dots + 0.178133u - 0.932966 \end{pmatrix}$$

$$a_{4} = \begin{pmatrix} -0.816690u^{16} + 1.35032u^{15} + \dots + 1.24440u + 1.45282 \\ -0.719526u^{16} + 1.44946u^{15} + \dots + 2.21168u + 1.50174 \end{pmatrix}$$

$$a_{8} = \begin{pmatrix} u^{4} - u^{2} + 1 \\ u^{4} \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} -0.167337u^{16} - 0.170752u^{15} + \dots + 0.0563481u + 0.582429 \\ -0.140347u^{16} - 0.143211u^{15} + \dots + 0.0472597u - 0.737318 \end{pmatrix}$$

(ii) Obstruction class = -1

(iii) Cusp Shapes = 
$$-\frac{116556}{18155}u^{16} + \frac{32086}{3631}u^{15} + \dots + \frac{186341}{18155}u + \frac{375193}{18155}$$

### (iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
$c_1$	$u^{17} + 37u^{16} + \dots + 129u + 1$
$c_{2}, c_{4}$	$u^{17} - 9u^{16} + \dots - 9u + 1$
$c_{3}, c_{6}$	$u^{17} + 3u^{16} + \dots + 1664u - 256$
$c_5, c_9$	$u^{17} + 2u^{16} + \dots - u - 1$
$c_7, c_{11}, c_{12}$	$u^{17} + 2u^{16} + \dots - u + 1$
$c_8, c_{10}$	$u^{17} + 18u^{15} + \dots + 5u - 1$

## (v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
$c_1$	$y^{17} - 169y^{16} + \dots + 16813y - 1$
$c_{2}, c_{4}$	$y^{17} - 37y^{16} + \dots + 129y - 1$
$c_3, c_6$	$y^{17} + 51y^{16} + \dots + 835584y - 65536$
$c_5, c_9$	$y^{17} + 18y^{15} + \dots + 5y - 1$
$c_7, c_{11}, c_{12}$	$y^{17} - 12y^{16} + \dots + 5y - 1$
$c_8, c_{10}$	$y^{17} + 36y^{16} + \dots + 17y - 1$

### (vi) Complex Volumes and Cusp Shapes

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
u = 1.01926		
a = -0.421975	5.87185	17.0960
b = 0.597288		
u = -0.814269 + 0.697849I		
a = 0.772298 - 0.496323I	1.96725 - 4.89234I	8.35716 + 5.36349I
b = -0.041970 + 0.201526I		
u = -0.814269 - 0.697849I		
a = 0.772298 + 0.496323I	1.96725 + 4.89234I	8.35716 - 5.36349I
b = -0.041970 - 0.201526I		
u = 0.151212 + 0.886118I		
a = -0.24895 - 2.10381I	-2.98302 + 1.89910I	0.81624 - 3.73789I
b = -0.097735 - 1.217690I		
u = 0.151212 - 0.886118I		
a = -0.24895 + 2.10381I	-2.98302 - 1.89910I	0.81624 + 3.73789I
b = -0.097735 + 1.217690I		
u = 0.524511 + 0.603470I		
a = -0.232214 - 0.919977I	-1.41487 + 1.50880I	1.51941 - 3.79939I
b = 0.292297 - 0.316506I		
u = 0.524511 - 0.603470I		
a = -0.232214 + 0.919977I	-1.41487 - 1.50880I	1.51941 + 3.79939I
b = 0.292297 + 0.316506I		
u = -0.413009 + 0.524274I		
a = -0.410879 + 0.002963I	1.40326 + 0.77610I	7.08751 + 0.48404I
b = -0.823888 + 0.527237I		
u = -0.413009 - 0.524274I		
a = -0.410879 - 0.002963I	1.40326 - 0.77610I	7.08751 - 0.48404I
b = -0.823888 - 0.527237I		
u = -0.568174		
a = 0.153918	0.739304	14.0850
b = -0.414256		

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
u = 0.471408		
a = 2.32178	-0.391449	30.6130
b = 2.79318		
u = 1.08781 + 1.09421I		
a = -0.81831 + 1.23483I	-17.0915 + 9.8759I	4.86349 - 4.59062I
b = 0.26950 + 2.32904I		
u = 1.08781 - 1.09421I		
a = -0.81831 - 1.23483I	-17.0915 - 9.8759I	4.86349 + 4.59062I
b = 0.26950 - 2.32904I		
u = -1.09696 + 1.09725I		
a = 0.98973 + 1.18652I	18.1033 - 4.0499I	2.18495 + 1.91746I
b = -0.10723 + 2.28377I		
u = -1.09696 - 1.09725I		
a = 0.98973 - 1.18652I	18.1033 + 4.0499I	2.18495 - 1.91746I
b = -0.10723 - 2.28377I		
u = 1.09946 + 1.09842I		
a = -1.07854 + 1.01904I	-17.0762 - 1.7937I	4.77435 + 0.71535I
b = 0.02092 + 2.11746I		
u = 1.09946 - 1.09842I		
a = -1.07854 - 1.01904I	-17.0762 + 1.7937I	4.77435 - 0.71535I
b = 0.02092 - 2.11746I		

$$\text{II. } I_2^u = \langle -u^7 + u^6 + u^5 - 2u^4 - u^3 + 2u^2 + b + u - 2, \ -u^7 + u^6 + u^5 - 2u^4 - u^3 + 2u^2 + a - 2, \ u^8 - u^7 - u^6 + 2u^5 + u^4 - 2u^3 + 2u - 1 \rangle$$

(i) Arc colorings

$$a_{5} = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_{9} = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} 1 \\ -u^{2} \end{pmatrix}$$

$$a_{3} = \begin{pmatrix} u^{7} - u^{6} - u^{5} + 2u^{4} + u^{3} - 2u^{2} + 2 \\ u^{7} - u^{6} - u^{5} + 2u^{4} + u^{3} - 2u^{2} - u + 2 \end{pmatrix}$$

$$a_{6} = \begin{pmatrix} u \\ -u^{3} + u \end{pmatrix}$$

$$a_{7} = \begin{pmatrix} u \\ -u^{3} + u \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} -u^{2} + 1 \\ -u^{2} \end{pmatrix}$$

$$a_{2} = \begin{pmatrix} u^{7} - u^{6} - u^{5} + 2u^{4} + u^{3} - 2u^{2} + 2 \\ u^{7} - u^{6} - u^{5} + 2u^{4} + u^{3} - 2u^{2} - 2u + 2 \end{pmatrix}$$

$$a_{1} = \begin{pmatrix} 0 \\ -u \end{pmatrix}$$

$$a_{4} = \begin{pmatrix} u^{7} - u^{6} - u^{5} + 2u^{4} + u^{3} - 2u^{2} + 2 \\ u^{7} - u^{6} - u^{5} + 2u^{4} + u^{3} - 2u^{2} - u + 2 \end{pmatrix}$$

$$a_{8} = \begin{pmatrix} u^{4} - u^{2} + 1 \\ u^{4} \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} u^{6} + u^{4} - 2u^{2} + 1 \\ u^{4} + 2u^{4} + 2u^{3} - 2u^{2} - 2u + 1 \end{pmatrix}$$

- (ii) Obstruction class = 1
- (iii) Cusp Shapes =  $-2u^7 + 2u^6 4u^4 3u^3 + u^2 + 1$

### (iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
$c_1, c_2$	$(u-1)^8$
$c_3, c_6$	$u^8$
C <sub>4</sub>	$(u+1)^8$
<i>C</i> <sub>5</sub>	$u^8 + u^7 - u^6 - 2u^5 + u^4 + 2u^3 - 2u - 1$
	$u^8 - u^7 - 3u^6 + 2u^5 + 3u^4 - 2u - 1$
c <sub>8</sub>	$u^8 + 3u^7 + 7u^6 + 10u^5 + 11u^4 + 10u^3 + 6u^2 + 4u + 1$
<i>c</i> 9	$u^8 - u^7 - u^6 + 2u^5 + u^4 - 2u^3 + 2u - 1$
$c_{10}$	$u^8 - 3u^7 + 7u^6 - 10u^5 + 11u^4 - 10u^3 + 6u^2 - 4u + 1$
$c_{11}, c_{12}$	$u^8 + u^7 - 3u^6 - 2u^5 + 3u^4 + 2u - 1$

## (v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
$c_1, c_2, c_4$	$(y-1)^8$
$c_{3}, c_{6}$	$y^8$
$c_5, c_9$	$y^8 - 3y^7 + 7y^6 - 10y^5 + 11y^4 - 10y^3 + 6y^2 - 4y + 1$
$c_7, c_{11}, c_{12}$	$y^8 - 7y^7 + 19y^6 - 22y^5 + 3y^4 + 14y^3 - 6y^2 - 4y + 1$
$c_{8}, c_{10}$	$y^8 + 5y^7 + 11y^6 + 6y^5 - 17y^4 - 34y^3 - 22y^2 - 4y + 1$

## (vi) Complex Volumes and Cusp Shapes

Solutions to $I_2^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
u = 0.570868 + 0.730671I		
a = 0.663977 - 0.849844I	-0.604279 - 1.131230I	5.26238 + 0.22273I
b = 0.09311 - 1.58052I		
u = 0.570868 - 0.730671I		
a = 0.663977 + 0.849844I	-0.604279 + 1.131230I	5.26238 - 0.22273I
b = 0.09311 + 1.58052I		
u = -0.855237 + 0.665892I		
a = -0.727959 - 0.566792I	-3.80435 - 2.57849I	2.12884 + 3.87967I
b = 0.127279 - 1.232690I		
u = -0.855237 - 0.665892I		
a = -0.727959 + 0.566792I	-3.80435 + 2.57849I	2.12884 - 3.87967I
b = 0.127279 + 1.232690I		
u = -1.09818		
a = -0.910598	4.85780	7.72210
b = 0.187581		
u = 1.031810 + 0.655470I		
a = 0.690511 - 0.438656I	0.73474 + 6.44354I	7.14098 - 6.66742I
b = -0.341297 - 1.094130I		
u = 1.031810 - 0.655470I		
a = 0.690511 + 0.438656I	0.73474 - 6.44354I	7.14098 + 6.66742I
b = -0.341297 + 1.094130I		
u = 0.603304		
a = 1.65754	-0.799899	0.213560
b = 1.05424		

III. u-Polynomials

Crossings	u-Polynomials at each crossing
$c_1$	$((u-1)^8)(u^{17} + 37u^{16} + \dots + 129u + 1)$
$c_2$	$((u-1)^8)(u^{17}-9u^{16}+\cdots-9u+1)$
$c_3, c_6$	$u^8(u^{17} + 3u^{16} + \dots + 1664u - 256)$
$c_4$	$((u+1)^8)(u^{17} - 9u^{16} + \dots - 9u + 1)$
<i>C</i> <sub>5</sub>	$(u^8 + u^7 + \dots - 2u - 1)(u^{17} + 2u^{16} + \dots - u - 1)$
C <sub>7</sub>	$(u^8 - u^7 - 3u^6 + 2u^5 + 3u^4 - 2u - 1)(u^{17} + 2u^{16} + \dots - u + 1)$
<i>C</i> <sub>8</sub>	$(u^8 + 3u^7 + 7u^6 + 10u^5 + 11u^4 + 10u^3 + 6u^2 + 4u + 1)$ $\cdot (u^{17} + 18u^{15} + \dots + 5u - 1)$
<i>c</i> <sub>9</sub>	$(u^8 - u^7 + \dots + 2u - 1)(u^{17} + 2u^{16} + \dots - u - 1)$
$c_{10}$	$(u^8 - 3u^7 + 7u^6 - 10u^5 + 11u^4 - 10u^3 + 6u^2 - 4u + 1)$ $\cdot (u^{17} + 18u^{15} + \dots + 5u - 1)$
$c_{11}, c_{12}$	$(u^8 + u^7 - 3u^6 - 2u^5 + 3u^4 + 2u - 1)(u^{17} + 2u^{16} + \dots - u + 1)$

IV. Riley Polynomials

Crossings	Riley Polynomials at each crossing
$c_1$	$((y-1)^8)(y^{17}-169y^{16}+\cdots+16813y-1)$
$c_2, c_4$	$((y-1)^8)(y^{17} - 37y^{16} + \dots + 129y - 1)$
$c_3, c_6$	$y^8(y^{17} + 51y^{16} + \dots + 835584y - 65536)$
$c_5,c_9$	$(y^8 - 3y^7 + 7y^6 - 10y^5 + 11y^4 - 10y^3 + 6y^2 - 4y + 1)$ $\cdot (y^{17} + 18y^{15} + \dots + 5y - 1)$
$c_7, c_{11}, c_{12}$	$(y^8 - 7y^7 + 19y^6 - 22y^5 + 3y^4 + 14y^3 - 6y^2 - 4y + 1)$ $\cdot (y^{17} - 12y^{16} + \dots + 5y - 1)$
$c_8, c_{10}$	$(y^8 + 5y^7 + 11y^6 + 6y^5 - 17y^4 - 34y^3 - 22y^2 - 4y + 1)$ $\cdot (y^{17} + 36y^{16} + \dots + 17y - 1)$