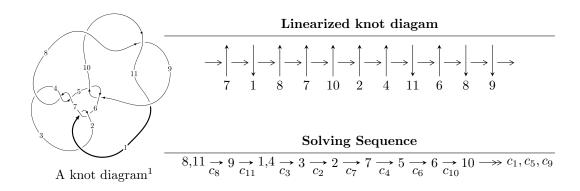
# $11n_{98} (K11n_{98})$



#### Ideals for irreducible components<sup>2</sup> of $X_{par}$

$$\begin{split} I_1^u &= \langle -325810u^{16} + 546213u^{15} + \dots + 3637114b - 2536642, \\ &- 877137u^{16} + 1987958u^{15} + \dots + 7274228a - 10784281, \ u^{17} - 2u^{16} + \dots + 13u - 4 \rangle \\ I_2^u &= \langle -u^{10} + u^9 + 4u^8 - 3u^7 - 6u^6 + 2u^5 + 2u^4 - u^2a + 3u^3 + 3u^2 + b + a - 3u - 2, \ 2u^{10} - 5u^9 + \dots - 4a + 5, \\ u^{11} - u^{10} - 4u^9 + 3u^8 + 6u^7 - 2u^6 - 2u^5 - 3u^4 - 3u^3 + 3u^2 + 2u + 1 \rangle \\ I_3^u &= \langle au + b + a + 2u + 3, \ a^2 + 2au + 4a + 2u + 6, \ u^2 + u - 1 \rangle \\ I_4^u &= \langle b - 1, \ 2a - 1, \ u - 1 \rangle \end{split}$$

\* 4 irreducible components of  $\dim_{\mathbb{C}} = 0$ , with total 44 representations.

<sup>&</sup>lt;sup>1</sup>The image of knot diagram is generated by the software "**Draw programme**" developed by Andrew Bartholomew(http://www.layer8.co.uk/maths/draw/index.htm#Running-draw), where we modified some parts for our purpose(https://github.com/CATsTAILs/LinksPainter).

<sup>&</sup>lt;sup>2</sup> All coefficients of polynomials are rational numbers. But the coefficients are sometimes approximated in decimal forms when there is not enough margin.

 $\begin{matrix} \text{I.} \\ I_1^u = \langle -3.26 \times 10^5 u^{16} + 5.46 \times 10^5 u^{15} + \dots + 3.64 \times 10^6 b - 2.54 \times 10^6, \ -8.77 \times 10^5 u^{16} + 1.99 \times 10^6 u^{15} + \dots + 7.27 \times 10^6 a - 1.08 \times 10^7, \ u^{17} - 2u^{16} + \dots + 13u - 4 \rangle \end{matrix}$ 

(i) Arc colorings

$$a_{8} = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_{9} = \begin{pmatrix} 1 \\ u^{2} \end{pmatrix}$$

$$a_{1} = \begin{pmatrix} -u \\ -u^{3} + u \end{pmatrix}$$

$$a_{4} = \begin{pmatrix} 0.120581u^{16} - 0.273288u^{15} + \cdots - 0.0580715u + 1.48253 \\ 0.0895793u^{16} - 0.150178u^{15} + \cdots + 0.0542218u + 0.697433 \end{pmatrix}$$

$$a_{3} = \begin{pmatrix} 0.0310022u^{16} - 0.123110u^{15} + \cdots - 0.112293u + 0.785100 \\ 0.0895793u^{16} - 0.150178u^{15} + \cdots + 0.0542218u + 0.697433 \end{pmatrix}$$

$$a_{2} = \begin{pmatrix} 0.239444u^{16} - 0.304221u^{15} + \cdots - 1.56094u + 1.51558 \\ 0.205575u^{16} - 0.224465u^{15} + \cdots - 0.728410u + 0.910041 \end{pmatrix}$$

$$a_{7} = \begin{pmatrix} 0.235464u^{16} - 0.270574u^{15} + \cdots - 0.673677u + 2.19687 \\ 0.182621u^{16} - 0.156800u^{15} + \cdots - 1.28067u + 0.925424 \end{pmatrix}$$

$$a_{5} = \begin{pmatrix} 0.360026u^{16} - 0.577509u^{15} + \cdots - 0.619016u + 2.99812 \\ 0.295154u^{16} - 0.374642u^{15} + \cdots - 1.67419u + 1.60747 \end{pmatrix}$$

$$a_{6} = \begin{pmatrix} 0.474993u^{16} - 0.539864u^{15} + \cdots - 1.82912u + 3.29061 \\ 0.410121u^{16} - 0.336997u^{15} + \cdots - 2.88429u + 1.89997 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} u \\ u \end{pmatrix}$$

(ii) Obstruction class = -1

(iii) Cusp Shapes = 
$$\frac{9594931}{7274228}u^{16} - \frac{15193461}{7274228}u^{15} + \dots + \frac{10670363}{7274228}u + \frac{21150807}{1818557}u^{16} + \dots + \frac{10670363}{7274228}u + \frac{10670363}{1818557}u^{16} + \dots + \frac{10670360}u^{16} + \dots + \frac{10670363}{1818557}u^{16} + \dots + \frac{10670363$$

Crossings	u-Polynomials at each crossing
$c_1, c_3, c_4$ $c_6, c_7$	$u^{17} - u^{16} + \dots - 4u^2 - 1$
$c_2$	$u^{17} + 5u^{16} + \dots - 8u - 1$
$c_5,c_9$	$u^{17} - 3u^{16} + \dots + 22u - 8$
$c_8, c_{10}, c_{11}$	$u^{17} - 2u^{16} + \dots + 13u - 4$

Crossings	Riley Polynomials at each crossing
$c_1, c_3, c_4$ $c_6, c_7$	$y^{17} + 5y^{16} + \dots - 8y - 1$
$c_2$	$y^{17} + 13y^{16} + \dots - 12y - 1$
$c_5, c_9$	$y^{17} + 9y^{16} + \dots - 12y - 64$
$c_8, c_{10}, c_{11}$	$y^{17} - 16y^{16} + \dots + 209y - 16$

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
u = -0.240053 + 0.973100I		
a = 0.644042 - 0.652010I	0.65577 + 8.75138I	0.84209 - 7.19652I
b = -0.678341 - 1.093890I		
u = -0.240053 - 0.973100I		
a = 0.644042 + 0.652010I	0.65577 - 8.75138I	0.84209 + 7.19652I
b = -0.678341 + 1.093890I		
u = -0.911746 + 0.271963I		
a = 0.521420 - 0.719384I	-1.69658 + 0.80451I	-2.69480 - 2.52231I
b = -0.187558 - 0.379982I		
u = -0.911746 - 0.271963I		
a = 0.521420 + 0.719384I	-1.69658 - 0.80451I	-2.69480 + 2.52231I
b = -0.187558 + 0.379982I		
u = 1.114510 + 0.218797I		
a = 0.635665 + 0.251760I	0.354258 - 0.834124I	0.06498 + 5.84789I
b = 1.157790 + 0.487195I		
u = 1.114510 - 0.218797I		
a = 0.635665 - 0.251760I	0.354258 + 0.834124I	0.06498 - 5.84789I
b = 1.157790 - 0.487195I		
u = -1.030910 + 0.649737I		
a = -0.466920 + 0.601803I	-1.75655 - 3.15519I	-1.08772 + 4.41422I
b = -0.583285 + 0.914805I		
u = -1.030910 - 0.649737I		
a = -0.466920 - 0.601803I	-1.75655 + 3.15519I	-1.08772 - 4.41422I
b = -0.583285 - 0.914805I		
u = 0.248382 + 0.709434I		
a = -0.785996 - 0.998686I	2.78581 - 2.60100I	4.98680 + 3.49505I
b = 0.784905 - 0.787523I		
u = 0.248382 - 0.709434I		
a = -0.785996 + 0.998686I	2.78581 + 2.60100I	4.98680 - 3.49505I
b = 0.784905 + 0.787523I		

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
u = -1.44333 + 0.29962I		
a = -0.27964 + 2.02194I	-2.68580 + 6.31167I	-1.34813 - 5.64607I
b = 0.606656 + 1.025000I		
u = -1.44333 - 0.29962I		
a = -0.27964 - 2.02194I	-2.68580 - 6.31167I	-1.34813 + 5.64607I
b = 0.606656 - 1.025000I		
u = 1.43553 + 0.42213I		
a = 0.59170 + 1.89308I	-4.6382 - 13.7590I	-2.60534 + 8.09148I
b = -0.678472 + 1.240020I		
u = 1.43553 - 0.42213I		
a = 0.59170 - 1.89308I	-4.6382 + 13.7590I	-2.60534 - 8.09148I
b = -0.678472 - 1.240020I		
u = 1.67968 + 0.04846I		
a = -0.20221 - 1.49330I	-11.59490 + 1.04318I	-1.35194 - 7.04363I
b = -0.239314 - 0.869369I		
u = 1.67968 - 0.04846I		
a = -0.20221 + 1.49330I	-11.59490 - 1.04318I	-1.35194 + 7.04363I
b = -0.239314 + 0.869369I		
u = 0.295856		
a = 1.43389	0.963952	10.6380
b = 0.635251		

$$I_2^u = \langle -u^{10} + u^9 + \dots + a - 2, \ 2u^{10} - 5u^9 + \dots - 4a + 5, \ u^{11} - u^{10} + \dots + 2u + 1 \rangle$$

(i) Arc colorings

$$a_{8} = \begin{pmatrix} 1\\0 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 0\\u \end{pmatrix}$$

$$a_{9} = \begin{pmatrix} 1\\u^{2} \end{pmatrix}$$

$$a_{4} = \begin{pmatrix} u^{10} - u^{9} - 4u^{8} + 3u^{7} + 6u^{6} - 2u^{5} - 2u^{4} + u^{2}a - 3u^{3} - 3u^{2} - a + 3u + 2 \end{pmatrix}$$

$$a_{3} = \begin{pmatrix} u^{10} - u^{9} - 4u^{8} + 3u^{7} + 6u^{6} - 2u^{5} - 2u^{4} + u^{2}a - 3u^{3} - 3u^{2} - a + 3u + 2 \end{pmatrix}$$

$$a_{2} = \begin{pmatrix} u^{10} - u^{9} - 4u^{8} + 3u^{7} + 6u^{6} - 2u^{5} - 2u^{4} + u^{2}a - 3u^{3} - 3u^{2} - a + 3u + 2 \end{pmatrix}$$

$$a_{2} = \begin{pmatrix} -u^{10} + u^{9} + \dots + 2a - 2\\u^{10} - u^{9} + \dots - a + 2 \end{pmatrix}$$

$$a_{7} = \begin{pmatrix} -u^{10}a + 2u^{10} + \dots - 2a + 3\\-u^{5}a - u^{6} + 2u^{3}a + 2u^{4} - au - 2 \end{pmatrix}$$

$$a_{5} = \begin{pmatrix} u^{7} - 2u^{5} + 2u\\u^{9} - 3u^{7} + 3u^{5} - u \end{pmatrix}$$

$$a_{6} = \begin{pmatrix} u^{7} - 2u^{5} + 2u\\u^{9} - 3u^{7} + 3u^{5} - u \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} u\\u \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} u\\u \end{pmatrix}$$

- (ii) Obstruction class = -1
- (iii) Cusp Shapes =  $4u^9 16u^7 4u^6 + 20u^5 + 12u^4 + 4u^3 8u^2 20u 6$

Crossings	u-Polynomials at each crossing		
$c_1, c_3, c_4$ $c_6, c_7$	$u^{22} + 3u^{21} + \dots + 24u + 9$		
$c_2$	$u^{22} + 11u^{21} + \dots + 432u + 81$		
$c_5,c_9$	$(u^{11} + u^{10} + 2u^9 + u^8 + 4u^7 + 2u^6 + 4u^5 + u^4 + 3u^3 - u^2 - 1)^2$		
$c_8, c_{10}, c_{11}$	$(u^{11} - u^{10} - 4u^9 + 3u^8 + 6u^7 - 2u^6 - 2u^5 - 3u^4 - 3u^3 + 3u^2 + 2u + 1)$		

Crossings	Riley Polynomials at each crossing
$c_1, c_3, c_4$ $c_6, c_7$	$y^{22} + 11y^{21} + \dots + 432y + 81$
$c_2$	$y^{22} - y^{21} + \dots + 35640y + 6561$
$c_5, c_9$	$(y^{11} + 3y^{10} + \dots - 2y - 1)^2$
$c_8, c_{10}, c_{11}$	$(y^{11} - 9y^{10} + \dots - 2y - 1)^2$

Solutions to $I_2^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
u = -1.14725		
a = -2.18308 + 3.31504I	-5.48524	0.376260
b = 0.181376 + 1.048190I		
u = -1.14725		
a = -2.18308 - 3.31504I	-5.48524	0.376260
b = 0.181376 - 1.048190I		
u = -0.044199 + 0.849205I		
a = 0.547434 + 0.348829I	2.35273 + 3.04152I	4.06121 - 2.82242I
b = -0.853835 + 0.533591I		
u = -0.044199 + 0.849205I		
a = -0.372720 + 0.162477I	2.35273 + 3.04152I	4.06121 - 2.82242I
b = 0.714099 + 0.923041I		
u = -0.044199 - 0.849205I		
a = 0.547434 - 0.348829I	2.35273 - 3.04152I	4.06121 + 2.82242I
b = -0.853835 - 0.533591I		
u = -0.044199 - 0.849205I		
a = -0.372720 - 0.162477I	2.35273 - 3.04152I	4.06121 + 2.82242I
b = 0.714099 - 0.923041I		
u = -1.232090 + 0.392876I		
a = 0.674566 - 0.370203I	-1.31282 + 1.41699I	0.791306 - 0.633731I
b = 0.623653 - 0.552777I		
u = -1.232090 + 0.392876I		
a = 0.48177 - 1.51619I	-1.31282 + 1.41699I	0.791306 - 0.633731I
b = -0.555909 - 0.782909I		
u = -1.232090 - 0.392876I		
a = 0.674566 + 0.370203I	-1.31282 - 1.41699I	0.791306 + 0.633731I
b = 0.623653 + 0.552777I		
u = -1.232090 - 0.392876I		
a = 0.48177 + 1.51619I	-1.31282 - 1.41699I	0.791306 + 0.633731I
b = -0.555909 + 0.782909I		

Solutions to $I_2^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
u = 1.317220 + 0.129556I		
a = 0.469425 + 0.990105I	-8.47148 - 2.94672I	-5.79937 + 4.11787I
b = -0.752651 + 0.945347I		
u = 1.317220 + 0.129556I		
a = -0.15850 - 2.09923I	-8.47148 - 2.94672I	-5.79937 + 4.11787I
b = -0.14927 - 1.48798I		
u = 1.317220 - 0.129556I		
a = 0.469425 - 0.990105I	-8.47148 + 2.94672I	-5.79937 - 4.11787I
b = -0.752651 - 0.945347I		
u = 1.317220 - 0.129556I		
a = -0.15850 + 2.09923I	-8.47148 + 2.94672I	-5.79937 - 4.11787I
b = -0.14927 + 1.48798I		
u = 1.304640 + 0.385413I		
a = -0.579828 + 0.055525I	-1.85809 - 7.47524I	-0.22908 + 5.55460I
b = -1.081770 - 0.344108I		
u = 1.304640 + 0.385413I		
a = -0.45041 - 1.69192I	-1.85809 - 7.47524I	-0.22908 + 5.55460I
b = 0.747184 - 1.181250I		
u = 1.304640 - 0.385413I		
a = -0.579828 - 0.055525I	-1.85809 + 7.47524I	-0.22908 - 5.55460I
b = -1.081770 + 0.344108I		
u = 1.304640 - 0.385413I		
a = -0.45041 + 1.69192I	-1.85809 + 7.47524I	-0.22908 - 5.55460I
b = 0.747184 + 1.181250I		
u = -0.271947 + 0.385187I		
a = 1.270550 + 0.259399I	-3.59460 + 1.13130I	-0.01220 - 6.05785I
b = -0.087548 + 1.187670I		
u = -0.271947 + 0.385187I		
a = 1.80079 + 2.03466I	-3.59460 + 1.13130I	-0.01220 - 6.05785I
b = -0.285332 - 0.830788I		

Solutions to $I_2^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
u = -0.271947 - 0.385187I		
a = 1.270550 - 0.259399I	-3.59460 - 1.13130I	-0.01220 + 6.05785I
b = -0.087548 - 1.187670I		
u = -0.271947 - 0.385187I		
a = 1.80079 - 2.03466I	-3.59460 - 1.13130I	-0.01220 + 6.05785I
b = -0.285332 + 0.830788I		

III.  $I_3^u = \langle au + b + a + 2u + 3, \ a^2 + 2au + 4a + 2u + 6, \ u^2 + u - 1 \rangle$ 

(i) Arc colorings

$$a_{8} = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_{9} = \begin{pmatrix} 1 \\ -u+1 \end{pmatrix}$$

$$a_{1} = \begin{pmatrix} -u \\ -u+1 \end{pmatrix}$$

$$a_{4} = \begin{pmatrix} a \\ -au-a-2u-3 \end{pmatrix}$$

$$a_{3} = \begin{pmatrix} au+2a+2u+3 \\ -au-a-2u-3 \end{pmatrix}$$

$$a_{2} = \begin{pmatrix} au+2a+u+3 \\ -au-a-3u-2 \end{pmatrix}$$

$$a_{7} = \begin{pmatrix} 2au+3a+6u+9 \\ -1 \end{pmatrix}$$

$$a_{5} = \begin{pmatrix} -au-a-2u-3 \\ 0 \end{pmatrix}$$

$$a_{6} = \begin{pmatrix} -a-u-2 \\ au+u+1 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} u \\ u \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} u \\ u \end{pmatrix}$$

- (ii) Obstruction class = 1
- (iii) Cusp Shapes = -8

Crossings	u-Polynomials at each crossing
$c_1, c_3, c_4$ $c_6, c_7$	$(u^2+1)^2$
$c_2$	$(u+1)^4$
$c_5, c_9$	$u^4 + 3u^2 + 1$
c <sub>8</sub>	$(u^2+u-1)^2$
$c_{10}, c_{11}$	$(u^2 - u - 1)^2$

Crossings	Riley Polynomials at each crossing
$c_1, c_3, c_4$ $c_6, c_7$	$(y+1)^4$
$c_2$	$(y-1)^4$
$c_5, c_9$	$(y^2 + 3y + 1)^2$
$c_8, c_{10}, c_{11}$	$(y^2 - 3y + 1)^2$

Solutions to $I_3^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
u = 0.618034		
a = -2.61803 + 0.61803I	-4.27683	-8.00000
b = -1.000000I		
u = 0.618034		
a = -2.61803 - 0.61803I	-4.27683	-8.00000
b = 1.000000I		
u = -1.61803		
a = -0.38197 + 1.61803I	-12.1725	-8.00000
b = 1.000000I		
u = -1.61803		
a = -0.38197 - 1.61803I	-12.1725	-8.00000
b = -1.000000I		

IV. 
$$I_4^u = \langle b - 1, \ 2a - 1, \ u - 1 \rangle$$

(i) Arc colorings

$$a_8 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 0 \\ 1 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} 1 \\ 1 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} -1\\0 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} 0.5 \\ 1 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} -0.5 \\ 1 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} 0.5 \\ 1 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} 1.5 \\ 1 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} 2 \\ 2 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} 2 \\ 2 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} 1 \\ 1 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} 1 \\ 1 \end{pmatrix}$$

- (ii) Obstruction class = 1
- (iii) Cusp Shapes = -2.25

Crossings	u-Polynomials at each crossing
$c_1, c_3, c_4$ $c_{10}, c_{11}$	u+1
$c_2, c_6, c_7$ $c_8$	u-1
$c_5, c_9$	u

Crossings	Riley Polynomials at each crossing
$c_1, c_2, c_3$ $c_4, c_6, c_7$ $c_8, c_{10}, c_{11}$	y-1
$c_5,c_9$	y

Solutions to $I_4^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
u = 1.00000		
a = 0.500000	0	-2.25000
b = 1.00000		

#### V. u-Polynomials

Crossings	u-Polynomials at each crossing
$c_1, c_3, c_4$	$(u+1)(u^2+1)^2(u^{17}-u^{16}+\cdots-4u^2-1)(u^{22}+3u^{21}+\cdots+24u+9)$
$c_2$	$(u-1)(u+1)^4(u^{17} + 5u^{16} + \dots - 8u - 1)$ $\cdot (u^{22} + 11u^{21} + \dots + 432u + 81)$
$c_5, c_9$	$u(u^{4} + 3u^{2} + 1)$ $\cdot (u^{11} + u^{10} + 2u^{9} + u^{8} + 4u^{7} + 2u^{6} + 4u^{5} + u^{4} + 3u^{3} - u^{2} - 1)^{2}$ $\cdot (u^{17} - 3u^{16} + \dots + 22u - 8)$
$c_6, c_7$	$(u-1)(u^2+1)^2(u^{17}-u^{16}+\cdots-4u^2-1)(u^{22}+3u^{21}+\cdots+24u+9)$
$c_8$	$(u-1)(u^{2}+u-1)^{2}$ $\cdot (u^{11}-u^{10}-4u^{9}+3u^{8}+6u^{7}-2u^{6}-2u^{5}-3u^{4}-3u^{3}+3u^{2}+2u+1)^{2}$ $\cdot (u^{17}-2u^{16}+\cdots+13u-4)$
$c_{10},c_{11}$	$ (u+1)(u^{2}-u-1)^{2} $ $ \cdot (u^{11}-u^{10}-4u^{9}+3u^{8}+6u^{7}-2u^{6}-2u^{5}-3u^{4}-3u^{3}+3u^{2}+2u+1)^{2} $ $ \cdot (u^{17}-2u^{16}+\cdots+13u-4) $

VI. Riley Polynomials

Crossings	Riley Polynomials at each crossing
$c_1, c_3, c_4$ $c_6, c_7$	$(y-1)(y+1)^4(y^{17} + 5y^{16} + \dots - 8y - 1)$ $\cdot (y^{22} + 11y^{21} + \dots + 432y + 81)$
$c_2$	$((y-1)^5)(y^{17} + 13y^{16} + \dots - 12y - 1)$ $\cdot (y^{22} - y^{21} + \dots + 35640y + 6561)$
$c_5, c_9$	$y(y^{2} + 3y + 1)^{2}(y^{11} + 3y^{10} + \dots - 2y - 1)^{2}$ $\cdot (y^{17} + 9y^{16} + \dots - 12y - 64)$
$c_8, c_{10}, c_{11}$	$(y-1)(y^2 - 3y + 1)^2(y^{11} - 9y^{10} + \dots - 2y - 1)^2$ $\cdot (y^{17} - 16y^{16} + \dots + 209y - 16)$