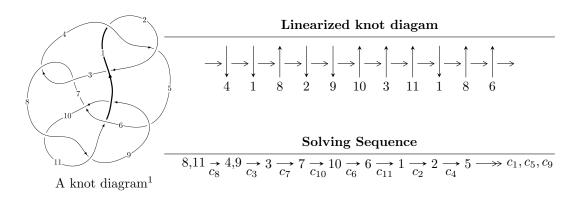
# $11n_{34} (K11n_{34})$



#### Ideals for irreducible components<sup>2</sup> of $X_{par}$

$$\begin{split} I_1^u &= \langle -3u^{10} + 32u^9 - 129u^8 + 203u^7 + 53u^6 - 484u^5 + 234u^4 + 343u^3 - 48u^2 + 32b - 158u - 11, \\ &- 9u^{10} + 101u^9 - 444u^8 + 857u^7 - 238u^6 - 1654u^5 + 1824u^4 + 793u^3 - 1185u^2 + 16a - 713u + 124, \\ &u^{11} - 11u^{10} + 47u^9 - 86u^8 + 12u^7 + 181u^6 - 170u^5 - 107u^4 + 111u^3 + 86u^2 - u + 1 \rangle \\ I_2^u &= \langle 3a^5 - 13a^4 + 7a^3 + 17a^2 + 13b + 21a - 7, \ a^6 - 6a^5 + 11a^4 - 4a^3 - a^2 - a + 1, \ u + 1 \rangle \\ I_3^u &= \langle b, \ -u^4 + 2u^3 + u^2 + a - 2u - 1, \ u^5 - u^4 - 2u^3 + u^2 + u + 1 \rangle \end{split}$$

\* 3 irreducible components of  $\dim_{\mathbb{C}} = 0$ , with total 22 representations.

<sup>&</sup>lt;sup>1</sup>The image of knot diagram is generated by the software "**Draw programme**" developed by Andrew Bartholomew(http://www.layer8.co.uk/maths/draw/index.htm#Running-draw), where we modified some parts for our purpose(https://github.com/CATsTAILs/LinksPainter).

<sup>&</sup>lt;sup>2</sup> All coefficients of polynomials are rational numbers. But the coefficients are sometimes approximated in decimal forms when there is not enough margin.

I. 
$$I_1^u = \langle -3u^{10} + 32u^9 + \dots + 32b - 11, \ -9u^{10} + 101u^9 + \dots + 16a + 124, \ u^{11} - 11u^{10} + \dots - u + 1 \rangle$$

(i) Arc colorings

$$a_{11} = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_{4} = \begin{pmatrix} 0.562500u^{10} - 6.31250u^{9} + \dots + 44.5625u - 7.75000 \\ \frac{3}{32}u^{10} - u^{9} + \dots + \frac{79}{16}u + \frac{11}{32} \end{pmatrix}$$

$$a_{9} = \begin{pmatrix} 1 \\ -u^{2} \end{pmatrix}$$

$$a_{3} = \begin{pmatrix} 0.468750u^{10} - 5.31250u^{9} + \dots + 39.6250u - 8.09375 \\ \frac{3}{32}u^{10} - u^{9} + \dots + \frac{79}{16}u + \frac{11}{32} \end{pmatrix}$$

$$a_{7} = \begin{pmatrix} -0.437500u^{10} + 4.31250u^{9} + \dots - 25.5625u - 4.37500 \\ \frac{7}{32}u^{10} - \frac{33}{16}u^{9} + \dots + \frac{31}{8}u - \frac{7}{32} \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} -u \\ u \end{pmatrix}$$

$$a_{6} = \begin{pmatrix} -0.218750u^{10} + 2.31250u^{9} + \dots - 25.6250u - 4.53125 \\ -0.0625000u^{9} + 0.562500u^{8} + \dots + 3.93750u - 0.0625000 \end{pmatrix}$$

$$a_{1} = \begin{pmatrix} 0.218750u^{10} - 2.43750u^{9} + \dots + 16.5000u - 2.46875 \\ \frac{1}{32}u^{10} - \frac{5}{16}u^{9} + \dots + \frac{9}{4}u + \frac{7}{32} \end{pmatrix}$$

$$a_{2} = \begin{pmatrix} 0.718750u^{10} - 7.87500u^{9} + \dots + 45.5625u - 11.2813 \\ -0.0937500u^{10} + 0.812500u^{9} + \dots + 45.5625u + 1.5625u + 4.50000 \\ -0.593750u^{10} + 5.56250u^{9} + \dots + 21.5625u + 4.50000 \\ -0.593750u^{10} - 3.06250u^{9} + \dots + 21.5625u + 4.50000 \\ -0.593750u^{10} - 3.06250u^{9} + \dots + 21.5625u + 4.50000 \\ -0.593750u^{10} + 5.56250u^{9} + \dots + 4.12500u + 0.343750 \end{pmatrix}$$

#### (ii) Obstruction class = -1

(iii) Cusp Shapes 
$$= \frac{1}{16}u^{10} - \frac{13}{16}u^9 + \frac{35}{8}u^8 - \frac{193}{16}u^7 + \frac{119}{8}u^6 + \frac{19}{4}u^5 - \frac{275}{8}u^4 + \frac{389}{16}u^3 + \frac{223}{16}u^2 - \frac{147}{16}u - \frac{39}{8}u^8 + \frac{19}{16}u^8 - \frac{19}{16}u^8$$

### (iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
$c_1, c_4$	$u^{11} - 10u^{10} + \dots + 10u - 1$
$c_2$	$u^{11} + 24u^{10} + \dots + 182u + 1$
$c_3, c_7$	$u^{11} + u^{10} + \dots + 96u - 32$
<i>C</i> <sub>5</sub>	$u^{11} + 13u^9 + \dots + 66u - 101$
$c_6$	$u^{11} - 2u^{10} + \dots + 136u - 1357$
$c_8, c_{10}$	$u^{11} + 11u^{10} + \dots - u - 1$
<i>c</i> 9	$u^{11} - u^{10} + \dots - 192u - 64$
$c_{11}$	$u^{11} + 2u^{10} + 2u^9 + 6u^7 + 12u^6 + 12u^5 + u^3 + 2u^2 + 2u + 1$

### (v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
$c_1, c_4$	$y^{11} - 24y^{10} + \dots + 182y - 1$
$c_2$	$y^{11} - 36y^{10} + \dots + 32578y - 1$
$c_3, c_7$	$y^{11} + 21y^{10} + \dots + 7680y - 1024$
<i>C</i> <sub>5</sub>	$y^{11} + 26y^{10} + \dots - 108562y - 10201$
	$y^{11} - 30y^{10} + \dots - 15893686y - 1841449$
$c_8, c_{10}$	$y^{11} - 27y^{10} + \dots - 171y - 1$
$c_9$	$y^{11} + 27y^{10} + \dots + 4096y - 4096$
$c_{11}$	$y^{11} + 16y^9 + 86y^7 + 160y^5 + 25y^3 - 1$

# (vi) Complex Volumes and Cusp Shapes

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
u = -1.16062		
a = -0.487360	2.30902	2.53950
b = -0.271903		
u = -0.570873 + 0.314013I		
a = -1.11819 + 1.14047I	0.69226 - 1.35881I	4.43349 + 4.96761I
b = -0.204727 + 0.543309I		
u = -0.570873 - 0.314013I		
a = -1.11819 - 1.14047I	0.69226 + 1.35881I	4.43349 - 4.96761I
b = -0.204727 - 0.543309I		
u = 0.0123536 + 0.1046970I		
a = -7.99180 + 4.91916I	-1.88779 - 0.79699I	-5.15274 - 0.95060I
b = 0.392173 + 0.533181I		
u = 0.0123536 - 0.1046970I		
a = -7.99180 - 4.91916I	-1.88779 + 0.79699I	-5.15274 + 0.95060I
b = 0.392173 - 0.533181I		
u = 1.99230 + 1.10149I		
a = -0.812502 + 0.545736I	-17.0622 + 11.2191I	1.86536 - 4.34062I
b = 2.19746 + 2.02033I		
u = 1.99230 - 1.10149I		
a = -0.812502 - 0.545736I	-17.0622 - 11.2191I	1.86536 + 4.34062I
b = 2.19746 - 2.02033I		
u = 2.11551 + 1.00650I		
a = 0.775984 - 0.370969I	-17.0176 + 3.4378I	1.85943 - 0.49918I
b = -1.98959 - 2.25555I		
u = 2.11551 - 1.00650I		
a = 0.775984 + 0.370969I	-17.0176 - 3.4378I	1.85943 + 0.49918I
b = -1.98959 + 2.25555I		
u = 2.53102 + 0.11992I		
a = -0.109810 - 0.279561I	2.86702 + 4.05320I	1.72472 - 1.91622I
b = 0.24063 + 3.13515I		

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
u = 2.53102 - 0.11992I		
a = -0.109810 + 0.279561I	2.86702 - 4.05320I	1.72472 + 1.91622I
b = 0.24063 - 3.13515I		

$$\text{II. } I_2^u = \\ \langle 3a^5 - 13a^4 + 7a^3 + 17a^2 + 13b + 21a - 7, \ a^6 - 6a^5 + 11a^4 - 4a^3 - a^2 - a + 1, \ u + 1 \rangle$$

(i) Arc colorings

$$a_{8} = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 0 \\ -1 \end{pmatrix}$$

$$a_{4} = \begin{pmatrix} -\frac{3}{13}a^{5} + a^{4} + \dots - \frac{21}{13}a + \frac{7}{13} \end{pmatrix}$$

$$a_{9} = \begin{pmatrix} 1 \\ -1 \end{pmatrix}$$

$$a_{3} = \begin{pmatrix} \frac{3}{13}a^{5} - a^{4} + \dots + \frac{34}{13}a - \frac{7}{13} \\ -\frac{3}{13}a^{5} + a^{4} + \dots - \frac{21}{13}a + \frac{7}{13} \end{pmatrix}$$

$$a_{7} = \begin{pmatrix} -1.53846a^{5} + 8a^{4} + \dots + 1.23077a + 1.92308 \\ \frac{15}{13}a^{5} - 6a^{4} + \dots - \frac{12}{13}a - \frac{9}{13} \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} 1 \\ -1 \end{pmatrix}$$

$$a_{6} = \begin{pmatrix} -1.15385a^{5} + 6a^{4} + \dots + 0.923077a + 0.692308 \\ \frac{10}{13}a^{5} - 4a^{4} + \dots - \frac{8}{13}a + \frac{7}{13} \end{pmatrix}$$

$$a_{1} = \begin{pmatrix} -2.07692a^{5} + 11a^{4} + \dots + 2.46154a + 2.84615 \\ 2.07692a^{5} - 11a^{4} + \dots - 2.46154a - 2.84615 \end{pmatrix}$$

$$a_{2} = \begin{pmatrix} -1.92308a^{5} + 10a^{4} + \dots + 1.53846a + 2.15385 \\ \frac{25}{13}a^{5} - 10a^{4} + \dots - \frac{7}{13}a - \frac{28}{13} \end{pmatrix}$$

$$a_{5} = \begin{pmatrix} -1.53846a^{5} + 8a^{4} + \dots + 1.23077a + 1.92308 \\ \frac{15}{13}a^{5} - 6a^{4} + \dots - \frac{12}{13}a - \frac{9}{13} \end{pmatrix}$$

$$a_{5} = \begin{pmatrix} -1.53846a^{5} + 8a^{4} + \dots + 1.23077a + 1.92308 \\ \frac{15}{13}a^{5} - 6a^{4} + \dots - \frac{12}{13}a - \frac{9}{13} \end{pmatrix}$$

(ii) Obstruction class = 1

(iii) Cusp Shapes = 
$$-\frac{92}{13}a^5 + 37a^4 - \frac{622}{13}a^3 - \frac{179}{13}a^2 - \frac{20}{13}a + \frac{180}{13}a^3$$

## (iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
$c_1, c_7$	$u^6 + u^5 - u^4 - 2u^3 + u + 1$
$c_2, c_{11}$	$u^6 + 3u^5 + 5u^4 + 4u^3 + 2u^2 + u + 1$
$c_3, c_4$	$u^6 - u^5 - u^4 + 2u^3 - u + 1$
$c_5, c_6$	$u^6 + u^5 + 2u^4 + 4u^3 + 5u^2 + 3u + 1$
<i>c</i> <sub>8</sub>	$(u+1)^6$
<i>c</i> <sub>9</sub>	$u^6$
$c_{10}$	$(u-1)^{6}$

## (v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
$c_1, c_3, c_4$ $c_7$	$y^6 - 3y^5 + 5y^4 - 4y^3 + 2y^2 - y + 1$
$c_2, c_{11}$	$y^6 + y^5 + 5y^4 + 6y^2 + 3y + 1$
$c_5, c_6$	$y^6 + 3y^5 + 6y^4 + 5y^2 + y + 1$
$c_8,c_{10}$	$(y-1)^6$
<i>C</i> 9	$y^6$

# (vi) Complex Volumes and Cusp Shapes

Solutions to $I_2^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
u = -1.00000		
a = 0.658836 + 0.177500I	1.64493 + 5.69302I	0.29418 - 8.33058I
b = -1.073950 - 0.558752I		
u = -1.00000		
a = 0.658836 - 0.177500I	1.64493 - 5.69302I	0.29418 + 8.33058I
b = -1.073950 + 0.558752I		
u = -1.00000		
a = -0.346225 + 0.393823I	3.53554 - 0.92430I	6.31051 + 0.25702I
b = 1.002190 - 0.295542I		
u = -1.00000		
a = -0.346225 - 0.393823I	3.53554 + 0.92430I	6.31051 - 0.25702I
b = 1.002190 + 0.295542I		
u = -1.00000		
a = 2.68739 + 0.76772I	-0.245672 + 0.924305I	-0.60470 + 5.55069I
b = -0.428243 + 0.664531I		
u = -1.00000		
a = 2.68739 - 0.76772I	-0.245672 - 0.924305I	-0.60470 - 5.55069I
b = -0.428243 - 0.664531I		

III. 
$$I_3^u = \langle b, \ -u^4 + 2u^3 + u^2 + a - 2u - 1, \ u^5 - u^4 - 2u^3 + u^2 + u + 1 \rangle$$

(i) Arc colorings

$$a_{8} = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_{4} = \begin{pmatrix} u^{4} - 2u^{3} - u^{2} + 2u + 1 \\ 0 \end{pmatrix}$$

$$a_{9} = \begin{pmatrix} 1 \\ -u^{2} \end{pmatrix}$$

$$a_{3} = \begin{pmatrix} u^{4} - 2u^{3} - u^{2} + 2u + 1 \\ 0 \end{pmatrix}$$

$$a_{7} = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} -u \\ u \end{pmatrix}$$

$$a_{6} = \begin{pmatrix} -u^{2} + 1 \\ u^{2} \end{pmatrix}$$

$$a_{1} = \begin{pmatrix} u^{4} - u^{2} - 1 \\ -u^{4} - u^{3} + u^{2} + 2u + 1 \end{pmatrix}$$

$$a_{2} = \begin{pmatrix} 2u^{4} - 2u^{3} - 2u^{2} + 2u \\ -u^{4} - u^{3} + u^{2} + 2u + 1 \end{pmatrix}$$

$$a_{5} = \begin{pmatrix} -u^{4} + u^{2} + 1 \\ u^{4} + u^{3} - u^{2} - 2u - 1 \end{pmatrix}$$

$$a_{5} = \begin{pmatrix} -u^{4} + u^{2} + 1 \\ u^{4} + u^{3} - u^{2} - 2u - 1 \end{pmatrix}$$

- (ii) Obstruction class = 1
- (iii) Cusp Shapes =  $-3u^4 u^3 + 2u^2 + 10u + 5$

### (iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
$c_1$	$(u-1)^5$
$c_2, c_4$	$(u+1)^5$
$c_3, c_7$	$u^5$
$c_5, c_9$	$u^5 + u^4 + 2u^3 + u^2 + u + 1$
$c_{6}, c_{8}$	$u^5 - u^4 - 2u^3 + u^2 + u + 1$
$c_{10}$	$u^5 + u^4 - 2u^3 - u^2 + u - 1$
$c_{11}$	$u^5 - 3u^4 + 4u^3 - u^2 - u + 1$

# (v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
$c_1, c_2, c_4$	$(y-1)^5$
$c_{3}, c_{7}$	$y^5$
$c_5, c_9$	$y^5 + 3y^4 + 4y^3 + y^2 - y - 1$
$c_6, c_8, c_{10}$	$y^5 - 5y^4 + 8y^3 - 3y^2 - y - 1$
$c_{11}$	$y^5 - y^4 + 8y^3 - 3y^2 + 3y - 1$

# (vi) Complex Volumes and Cusp Shapes

Solutions to $I_3^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
u = -1.21774		
a = 2.89210	0.756147	-9.00270
b = 0		
u = -0.309916 + 0.549911I		
a = 0.01014 + 1.59703I	-1.31583 - 1.53058I	1.45754 + 4.40323I
b = 0		
u = -0.309916 - 0.549911I		
a = 0.01014 - 1.59703I	-1.31583 + 1.53058I	1.45754 - 4.40323I
b = 0		
u = 1.41878 + 0.21917I		
a = 0.043806 - 0.365575I	4.22763 + 4.40083I	10.04378 - 5.20937I
b = 0		
u = 1.41878 - 0.21917I		
a = 0.043806 + 0.365575I	4.22763 - 4.40083I	10.04378 + 5.20937I
b = 0		

IV. u-Polynomials

Crossings	u-Polynomials at each crossing
$c_1$	$((u-1)^5)(u^6+u^5+\cdots+u+1)(u^{11}-10u^{10}+\cdots+10u-1)$
$c_2$	$(u+1)^5(u^6+3u^5+5u^4+4u^3+2u^2+u+1)$ $\cdot (u^{11}+24u^{10}+\cdots+182u+1)$
$c_3$	$u^{5}(u^{6} - u^{5} + \dots - u + 1)(u^{11} + u^{10} + \dots + 96u - 32)$
C4	$((u+1)^5)(u^6-u^5+\cdots-u+1)(u^{11}-10u^{10}+\cdots+10u-1)$
<i>C</i> <sub>5</sub>	$(u^{5} + u^{4} + 2u^{3} + u^{2} + u + 1)(u^{6} + u^{5} + 2u^{4} + 4u^{3} + 5u^{2} + 3u + 1)$ $\cdot (u^{11} + 13u^{9} + \dots + 66u - 101)$
$c_6$	$(u^{5} - u^{4} - 2u^{3} + u^{2} + u + 1)(u^{6} + u^{5} + 2u^{4} + 4u^{3} + 5u^{2} + 3u + 1)$ $\cdot (u^{11} - 2u^{10} + \dots + 136u - 1357)$
$c_7$	$u^{5}(u^{6} + u^{5} + \dots + u + 1)(u^{11} + u^{10} + \dots + 96u - 32)$
c <sub>8</sub>	$((u+1)^6)(u^5 - u^4 + \dots + u + 1)(u^{11} + 11u^{10} + \dots - u - 1)$
<i>c</i> 9	$u^{6}(u^{5} + u^{4} + \dots + u + 1)(u^{11} - u^{10} + \dots - 192u - 64)$
$c_{10}$	$((u-1)^6)(u^5+u^4+\cdots+u-1)(u^{11}+11u^{10}+\cdots-u-1)$
$c_{11}$	$(u^{5} - 3u^{4} + 4u^{3} - u^{2} - u + 1)(u^{6} + 3u^{5} + 5u^{4} + 4u^{3} + 2u^{2} + u + 1)$ $\cdot (u^{11} + 2u^{10} + 2u^{9} + 6u^{7} + 12u^{6} + 12u^{5} + u^{3} + 2u^{2} + 2u + 1)$

## V. Riley Polynomials

Crossings	Riley Polynomials at each crossing
$c_1, c_4$	$(y-1)^{5}(y^{6}-3y^{5}+5y^{4}-4y^{3}+2y^{2}-y+1)$ $\cdot (y^{11}-24y^{10}+\cdots+182y-1)$
$c_2$	$((y-1)^5)(y^6+y^5+\cdots+3y+1)(y^{11}-36y^{10}+\cdots+32578y-1)$
$c_3, c_7$	$y^{5}(y^{6} - 3y^{5} + 5y^{4} - 4y^{3} + 2y^{2} - y + 1)$ $\cdot (y^{11} + 21y^{10} + \dots + 7680y - 1024)$
<i>C</i> <sub>5</sub>	$(y^5 + 3y^4 + 4y^3 + y^2 - y - 1)(y^6 + 3y^5 + 6y^4 + 5y^2 + y + 1)$ $\cdot (y^{11} + 26y^{10} + \dots - 108562y - 10201)$
$c_6$	$(y^5 - 5y^4 + 8y^3 - 3y^2 - y - 1)(y^6 + 3y^5 + 6y^4 + 5y^2 + y + 1)$ $\cdot (y^{11} - 30y^{10} + \dots - 15893686y - 1841449)$
$c_8, c_{10}$	$((y-1)^6)(y^5 - 5y^4 + \dots - y - 1)(y^{11} - 27y^{10} + \dots - 171y - 1)$
<i>C</i> 9	$y^{6}(y^{5} + 3y^{4} + \dots - y - 1)(y^{11} + 27y^{10} + \dots + 4096y - 4096)$
$c_{11}$	$(y^5 - y^4 + 8y^3 - 3y^2 + 3y - 1)(y^6 + y^5 + 5y^4 + 6y^2 + 3y + 1)$ $\cdot (y^{11} + 16y^9 + 86y^7 + 160y^5 + 25y^3 - 1)$