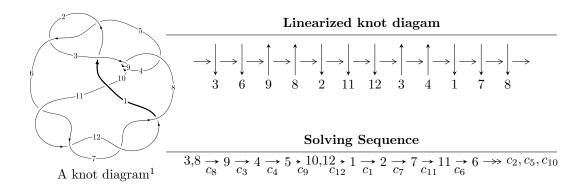
$12n_{0467} \ (K12n_{0467})$



Ideals for irreducible components² of X_{par}

$$I_1^u = \langle 140613342u^{26} + 233504827u^{25} + \dots + 1306898116b + 2324027520,$$

$$315767111u^{26} + 587740472u^{25} + \dots + 1306898116a - 1648431188, \ u^{27} + u^{26} + \dots - 4u - 4 \rangle$$

$$I_2^u = \langle 2b - 2a + u, \ 2a^2 - 2au - 2a + u - 1, \ u^2 - 2 \rangle$$

$$I_1^v = \langle a, \ b + v + 1, \ v^2 + v - 1 \rangle$$

* 3 irreducible components of $\dim_{\mathbb{C}} = 0$, with total 33 representations.

¹The image of knot diagram is generated by the software "**Draw programme**" developed by Andrew Bartholomew(http://www.layer8.co.uk/maths/draw/index.htm#Running-draw), where we modified some parts for our purpose(https://github.com/CATsTAILs/LinksPainter).

² All coefficients of polynomials are rational numbers. But the coefficients are sometimes approximated in decimal forms when there is not enough margin.

I.
$$I_1^u = \langle 1.41 \times 10^8 u^{26} + 2.34 \times 10^8 u^{25} + \dots + 1.31 \times 10^9 b + 2.32 \times 10^9, \ 3.16 \times 10^8 u^{26} + 5.88 \times 10^8 u^{25} + \dots + 1.31 \times 10^9 a - 1.65 \times 10^9, \ u^{27} + u^{26} + \dots - 4u - 4 \rangle$$

(i) Arc colorings

$$\begin{array}{l} a_3 = \begin{pmatrix} 0 \\ u \end{pmatrix} \\ a_8 = \begin{pmatrix} 1 \\ -u^2 \end{pmatrix} \\ a_4 = \begin{pmatrix} u \\ -u^3 + u \end{pmatrix} \\ a_5 = \begin{pmatrix} -u^3 + 2u \\ -u^3 + u \end{pmatrix} \\ a_{10} = \begin{pmatrix} -u^2 + 1 \\ u^4 - 2u^2 \end{pmatrix} \\ a_{12} = \begin{pmatrix} -0.241616u^{26} - 0.449722u^{25} + \cdots - 13.1892u + 1.26133 \\ -0.107593u^{26} - 0.178671u^{25} + \cdots - 2.19364u - 1.77828 \end{pmatrix} \\ a_1 = \begin{pmatrix} -0.134023u^{26} - 0.271051u^{25} + \cdots - 10.9955u + 3.03961 \\ -0.107593u^{26} - 0.178671u^{25} + \cdots - 10.9955u + 3.03961 \\ -0.107593u^{26} - 0.178671u^{25} + \cdots - 2.19364u - 1.77828 \end{pmatrix} \\ a_2 = \begin{pmatrix} -0.134023u^{26} - 0.271051u^{25} + \cdots - 10.9955u + 3.03961 \\ 0.0945547u^{26} - 0.183568u^{25} + \cdots - 3.27784u - 2.32639 \end{pmatrix} \\ a_7 = \begin{pmatrix} -0.673320u^{26} - 0.574468u^{25} + \cdots - 15.4301u + 0.529920 \\ -0.102694u^{26} + 0.0537208u^{25} + \cdots - 3.65606u - 0.825481 \end{pmatrix} \\ a_{11} = \begin{pmatrix} -0.00809889u^{26} + 0.000418223u^{25} + \cdots + 2.05151u + 3.50212 \\ 0.355054u^{26} + 0.372385u^{25} + \cdots + 7.65668u + 1.09099 \end{pmatrix} \\ a_6 = \begin{pmatrix} -0.409090u^{26} + 0.0395121u^{25} + \cdots - 4.08989u + 7.12801 \\ -0.180513u^{26} + 0.126995u^{25} + \cdots + 3.62778u + 1.76201 \end{pmatrix} \end{array}$$

(ii) Obstruction class = -1

(iii) Cusp Shapes =
$$-\frac{9879130}{326724529}u^{26} + \frac{101640265}{326724529}u^{25} + \dots - \frac{4373584718}{326724529}u + \frac{3242559308}{326724529}u$$

(iv) u-Polynomials at the component

| Crossings | u-Polynomials at each crossing |
|-----------------------------|---|
| c_1 | $u^{27} + 7u^{26} + \dots + 73u + 1$ |
| c_2, c_5 | $u^{27} + 3u^{26} + \dots + 7u + 1$ |
| c_3,c_8,c_9 | $u^{27} + u^{26} + \dots - 4u - 4$ |
| c_4 | $u^{27} - 3u^{26} + \dots + 612u + 220$ |
| c_6, c_7, c_{11} c_{12} | $u^{27} - 2u^{26} + \dots - 6u + 1$ |
| c_{10} | $u^{27} - 2u^{26} + \dots - 20u - 1$ |

(v) Riley Polynomials at the component

| Crossings | Riley Polynomials at each crossing |
|-----------------------------|--|
| c_1 | $y^{27} + 33y^{26} + \dots + 4113y - 1$ |
| c_2, c_5 | $y^{27} - 7y^{26} + \dots + 73y - 1$ |
| c_3, c_8, c_9 | $y^{27} - 37y^{26} + \dots + 336y - 16$ |
| c_4 | $y^{27} - 97y^{26} + \dots + 1370704y - 48400$ |
| c_6, c_7, c_{11} c_{12} | $y^{27} - 30y^{26} + \dots + 32y - 1$ |
| c_{10} | $y^{27} + 42y^{26} + \dots + 160y - 1$ |

(vi) Complex Volumes and Cusp Shapes

| Solutions to I_1^u | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape |
|---------------------------|---------------------------------------|-----------------------|
| u = 0.910258 + 0.590456I | | |
| a = 2.00698 + 1.21820I | -3.25530 + 7.25549I | -5.95539 - 6.08777I |
| b = 1.50366 - 0.20859I | | |
| u = 0.910258 - 0.590456I | | |
| a = 2.00698 - 1.21820I | -3.25530 - 7.25549I | -5.95539 + 6.08777I |
| b = 1.50366 + 0.20859I | | |
| u = -1.017290 + 0.392893I | | |
| a = 1.59907 - 0.86702I | -2.42951 - 1.33319I | -4.55270 + 1.10070I |
| b = 1.384080 + 0.097780I | | |
| u = -1.017290 - 0.392893I | | |
| a = 1.59907 + 0.86702I | -2.42951 + 1.33319I | -4.55270 - 1.10070I |
| b = 1.384080 - 0.097780I | | |
| u = -1.028180 + 0.401751I | | |
| a = -0.842937 + 0.402129I | 3.20449 - 4.27323I | -1.36721 + 6.77417I |
| b = -0.466581 - 0.606665I | | |
| u = -1.028180 - 0.401751I | | |
| a = -0.842937 - 0.402129I | 3.20449 + 4.27323I | -1.36721 - 6.77417I |
| b = -0.466581 + 0.606665I | | |
| u = 1.132760 + 0.119465I | | |
| a = -0.399911 + 0.146187I | 3.11947 + 0.51181I | -0.345493 + 0.472617I |
| b = -0.444802 - 0.471118I | | |
| u = 1.132760 - 0.119465I | | |
| a = -0.399911 - 0.146187I | 3.11947 - 0.51181I | -0.345493 - 0.472617I |
| b = -0.444802 + 0.471118I | | |
| u = 0.068539 + 0.776104I | | |
| a = -2.94508 - 0.05064I | -5.79751 - 2.66305I | -8.58849 + 2.68063I |
| b = -1.42888 - 0.10362I | | |
| u = 0.068539 - 0.776104I | | |
| a = -2.94508 + 0.05064I | -5.79751 + 2.66305I | -8.58849 - 2.68063I |
| b = -1.42888 + 0.10362I | | |

| Solutions to I_1^u | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape |
|--------------------------|---------------------------------------|---------------------|
| u = 0.701128 | | |
| a = -0.723697 | -9.07206 | -6.92100 |
| b = 1.54174 | | |
| u = 1.38081 | | |
| a = -0.782809 | 3.22160 | 2.65910 |
| b = -0.202634 | | |
| u = -1.43515 | | |
| a = 1.63913 | -3.96458 | -1.96340 |
| b = 1.62828 | | |
| u = 0.093206 + 0.505933I | | |
| a = 0.909549 - 0.188312I | -0.272367 + 1.017390I | -4.41879 - 6.56996I |
| b = 0.279075 - 0.365424I | | |
| u = 0.093206 - 0.505933I | | |
| a = 0.909549 + 0.188312I | -0.272367 - 1.017390I | -4.41879 + 6.56996I |
| b = 0.279075 + 0.365424I | | |
| u = -0.462517 | | |
| a = 1.41263 | -1.60060 | -3.53340 |
| b = 0.790251 | | |
| u = -1.60836 | | |
| a = -0.0902962 | -1.00091 | -6.04390 |
| b = -1.36994 | | |
| u = 0.389158 | | |
| a = -3.32064 | -10.0949 | 1.45710 |
| b = -1.64070 | | |
| u = -0.327289 | | |
| a = 3.18758 | -2.27386 | 5.71450 |
| b = -0.436653 | | |
| u = -1.70507 + 0.18041I | | |
| a = -1.29573 + 0.99047I | 5.77830 - 10.34990I | -4.51654 + 4.83744I |
| b = -1.58969 - 0.26870I | | |

| Solutions to I_1^u | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape |
|---------------------------|---------------------------------------|-----------------------|
| u = -1.70507 - 0.18041I | | |
| a = -1.29573 - 0.99047I | 5.77830 + 10.34990I | -4.51654 - 4.83744I |
| b = -1.58969 + 0.26870I | | |
| u = 1.74296 + 0.07415I | | |
| a = -1.029860 - 0.595198I | 7.48038 + 3.07161I | -3.06454 - 1.05246I |
| b = -1.47829 + 0.32375I | | |
| u = 1.74296 - 0.07415I | | |
| a = -1.029860 + 0.595198I | 7.48038 - 3.07161I | -3.06454 + 1.05246I |
| b = -1.47829 - 0.32375I | | |
| u = 1.74801 + 0.11240I | | |
| a = 0.591464 + 0.471611I | 13.1108 + 6.4432I | -1.45116 - 4.64591I |
| b = 0.634607 - 0.775759I | | |
| u = 1.74801 - 0.11240I | | |
| a = 0.591464 - 0.471611I | 13.1108 - 6.4432I | -1.45116 + 4.64591I |
| b = 0.634607 + 0.775759I | | |
| u = -1.76409 + 0.02868I | | |
| a = 0.245519 + 0.313706I | 13.66050 - 1.13182I | -0.424228 - 0.165787I |
| b = 0.451661 - 0.831495I | | |
| u = -1.76409 - 0.02868I | | |
| a = 0.245519 - 0.313706I | 13.66050 + 1.13182I | -0.424228 + 0.165787I |
| b = 0.451661 + 0.831495I | | |

II.
$$I_2^u = \langle 2b - 2a + u, \ 2a^2 - 2au - 2a + u - 1, \ u^2 - 2 \rangle$$

(i) Arc colorings

$$a_{3} = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_{8} = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{9} = \begin{pmatrix} 1 \\ -2 \end{pmatrix}$$

$$a_{4} = \begin{pmatrix} u \\ -u \end{pmatrix}$$

$$a_{5} = \begin{pmatrix} 0 \\ -u \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} -1 \\ 0 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} a \\ a - \frac{1}{2}u \end{pmatrix}$$

$$a_{1} = \begin{pmatrix} \frac{1}{2}u \\ a - \frac{1}{2}u \end{pmatrix}$$

$$a_{2} = \begin{pmatrix} \frac{1}{2}u \\ a + \frac{1}{2}u \end{pmatrix}$$

$$a_{7} = \begin{pmatrix} -\frac{1}{2}au - a + \frac{1}{2}u + \frac{1}{2} \\ -a + \frac{1}{2}u - 1 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} -\frac{1}{2}au - \frac{1}{2} \\ -a + \frac{1}{2}u - 1 \end{pmatrix}$$

$$a_{6} = \begin{pmatrix} \frac{1}{2}u \\ a - \frac{1}{2}u \end{pmatrix}$$

- (ii) Obstruction class = 1
- (iii) Cusp Shapes = -8

(iv) u-Polynomials at the component

| Crossings | u-Polynomials at each crossing |
|--------------------------|--------------------------------|
| c_1, c_5 | $(u-1)^4$ |
| c_2 | $(u+1)^4$ |
| $c_3, c_4, c_8 \ c_9$ | $(u^2-2)^2$ |
| c_6, c_7 | $(u^2 - u - 1)^2$ |
| c_{10}, c_{11}, c_{12} | $(u^2+u-1)^2$ |

(v) Riley Polynomials at the component

| Crossings | Riley Polynomials at each crossing |
|-------------------------------------|------------------------------------|
| c_1, c_2, c_5 | $(y-1)^4$ |
| $c_3, c_4, c_8 \ c_9$ | $(y-2)^4$ |
| c_6, c_7, c_{10} c_{11}, c_{12} | $(y^2 - 3y + 1)^2$ |

(vi) Complex Volumes and Cusp Shapes

| Solutions to I_2^u | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape |
|----------------------|---------------------------------------|------------|
| u = 1.41421 | | |
| a = 0.0890728 | 2.30291 | -8.00000 |
| b = -0.618034 | | |
| u = 1.41421 | | |
| a = 2.32514 | -5.59278 | -8.00000 |
| b = 1.61803 | | |
| u = -1.41421 | | |
| a = 0.910927 | -5.59278 | -8.00000 |
| b = 1.61803 | | |
| u = -1.41421 | | |
| a = -1.32514 | 2.30291 | -8.00000 |
| b = -0.618034 | | |

III.
$$I_1^v = \langle a, \ b+v+1, \ v^2+v-1 \rangle$$

(i) Arc colorings

$$a_3 = \begin{pmatrix} v \\ 0 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} v \\ 0 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} v \\ 0 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} 0 \\ -v - 1 \end{pmatrix}$$

$$a_{1} = \begin{pmatrix} v + 1 \\ -v - 1 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} v+1 \\ -v-1 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} 2v+1\\ -v-1 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} 1 \\ -v - 2 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} -v - 1 \\ v + 2 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} -v - 1 \\ v + 1 \end{pmatrix}$$

- (ii) Obstruction class = 1
- (iii) Cusp Shapes = -18

(iv) u-Polynomials at the component

| Crossings | u-Polynomials at each crossing |
|---------------------|--------------------------------|
| c_1, c_2 | $(u-1)^2$ |
| $c_3,c_4,c_8 \ c_9$ | u^2 |
| <i>C</i> 5 | $(u+1)^2$ |
| c_6, c_7, c_{10} | $u^2 + u - 1$ |
| c_{11}, c_{12} | u^2-u-1 |

(v) Riley Polynomials at the component

| Crossings | Riley Polynomials at each crossing |
|-------------------------------------|------------------------------------|
| c_1, c_2, c_5 | $(y-1)^2$ |
| $c_3, c_4, c_8 \ c_9$ | y^2 |
| c_6, c_7, c_{10} c_{11}, c_{12} | $y^2 - 3y + 1$ |

(vi) Complex Volumes and Cusp Shapes

| Solutions to I_1^v | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape |
|----------------------|---------------------------------------|------------|
| v = 0.618034 | | |
| a = 0 | -10.5276 | -18.0000 |
| b = -1.61803 | | |
| v = -1.61803 | | |
| a = 0 | -2.63189 | -18.0000 |
| b = 0.618034 | | |

IV. u-Polynomials

| Crossings | u-Polynomials at each crossing |
|-----------------------|---|
| c_1 | $((u-1)^6)(u^{27}+7u^{26}+\cdots+73u+1)$ |
| c_2 | $((u-1)^2)(u+1)^4(u^{27}+3u^{26}+\cdots+7u+1)$ |
| c_3,c_8,c_9 | $u^{2}(u^{2}-2)^{2}(u^{27}+u^{26}+\cdots-4u-4)$ |
| C ₄ | $u^{2}(u^{2}-2)^{2}(u^{27}-3u^{26}+\cdots+612u+220)$ |
| <i>C</i> ₅ | $((u-1)^4)(u+1)^2(u^{27}+3u^{26}+\cdots+7u+1)$ |
| c_{6}, c_{7} | $((u^2 - u - 1)^2)(u^2 + u - 1)(u^{27} - 2u^{26} + \dots - 6u + 1)$ |
| c_{10} | $((u^2 + u - 1)^3)(u^{27} - 2u^{26} + \dots - 20u - 1)$ |
| c_{11}, c_{12} | $(u^2 - u - 1)(u^2 + u - 1)^2(u^{27} - 2u^{26} + \dots - 6u + 1)$ |

V. Riley Polynomials

| Crossings | Riley Polynomials at each crossing |
|-----------------------------|--|
| c_1 | $((y-1)^6)(y^{27} + 33y^{26} + \dots + 4113y - 1)$ |
| c_2, c_5 | $((y-1)^6)(y^{27} - 7y^{26} + \dots + 73y - 1)$ |
| c_3,c_8,c_9 | $y^{2}(y-2)^{4}(y^{27}-37y^{26}+\cdots+336y-16)$ |
| c_4 | $y^{2}(y-2)^{4}(y^{27}-97y^{26}+\cdots+1370704y-48400)$ |
| c_6, c_7, c_{11} c_{12} | $((y^2 - 3y + 1)^3)(y^{27} - 30y^{26} + \dots + 32y - 1)$ |
| c_{10} | $((y^2 - 3y + 1)^3)(y^{27} + 42y^{26} + \dots + 160y - 1)$ |