

#### Ideals for irreducible components<sup>2</sup> of $X_{par}$

$$I_1^u = \langle u^{83} - u^{82} + \dots - u^2 - 1 \rangle$$

\* 1 irreducible components of  $\dim_{\mathbb{C}} = 0$ , with total 83 representations.

<sup>&</sup>lt;sup>1</sup>The image of knot diagram is generated by the software "**Draw programme**" developed by Andrew Bartholomew(http://www.layer8.co.uk/maths/draw/index.htm#Running-draw), where we modified some parts for our purpose(https://github.com/CATsTAILs/LinksPainter).

<sup>&</sup>lt;sup>2</sup> All coefficients of polynomials are rational numbers. But the coefficients are sometimes approximated in decimal forms when there is not enough margin.

I. 
$$I_1^u = \langle u^{83} - u^{82} + \dots - u^2 - 1 \rangle$$

(i) Arc colorings

$$a_{2} = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_{8} = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{7} = \begin{pmatrix} 1 \\ u^{2} \end{pmatrix}$$

$$a_{3} = \begin{pmatrix} u \\ u^{3} + u \end{pmatrix}$$

$$a_{4} = \begin{pmatrix} -u^{3} \\ u^{3} + u \end{pmatrix}$$

$$a_{9} = \begin{pmatrix} -u^{6} - u^{4} + 1 \\ u^{6} + 2u^{4} + u^{2} \end{pmatrix}$$

$$a_{5} = \begin{pmatrix} u^{9} + 2u^{7} + u^{5} - 2u^{3} - u \\ -u^{9} - 3u^{7} - 3u^{5} + u \end{pmatrix}$$

$$a_{1} = \begin{pmatrix} u^{3} \\ u^{5} + u^{3} + u \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} -u^{14} - 3u^{12} - 4u^{10} - u^{8} + 1 \\ -u^{16} - 4u^{14} - 8u^{12} - 8u^{10} - 4u^{8} + 2u^{6} + 4u^{4} + 2u^{2} \end{pmatrix}$$

$$a_{6} = \begin{pmatrix} -u^{39} - 10u^{37} + \dots + 7u^{7} + 6u^{5} \\ -u^{41} - 11u^{39} + \dots + 2u^{3} + u \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} -u^{23} - 6u^{21} - 16u^{19} - 20u^{17} - 4u^{15} + 22u^{13} + 26u^{11} + 6u^{9} - 9u^{7} - 6u^{5} \\ u^{23} + 7u^{21} + \dots + 2u^{3} + u \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} -u^{62} - 17u^{60} + \dots + 6u^{6} + 1 \\ u^{62} + 18u^{60} + \dots - 12u^{6} + u^{2} \end{pmatrix}$$

- (ii) Obstruction class = -1
- (iii) Cusp Shapes =  $4u^{81} 4u^{80} + \cdots + 4u 2$

#### (iv) u-Polynomials at the component

| Crossings             | u-Polynomials at each crossing            |
|-----------------------|---|
| $c_1$                 | $u^{83} + 47u^{82} + \dots - 2u - 1$      |
| $c_2, c_7$            | $u^{83} + u^{82} + \dots + u^2 + 1$       |
| $c_3, c_4, c_8$       | $u^{83} - u^{82} + \dots + 124u + 17$     |
| $c_5$                 | $u^{83} + u^{82} + \dots + 450u + 317$    |
| $c_6,c_{11}$          | $u^{83} - u^{82} + \dots + u^2 + 1$       |
| <i>c</i> <sub>9</sub> | $u^{83} - 11u^{82} + \dots + 98u - 29$    |
| $c_{10}$              | $u^{83} - 39u^{82} + \dots - 2u + 1$      |
| $c_{12}$              | $u^{83} - 5u^{82} + \dots - 2422u + 1767$ |

# (v) Riley Polynomials at the component

| Crossings             | Riley Polynomials at each crossing                 |
|-----------------------|--|
| $c_1$                 | $y^{83} - 21y^{82} + \dots - 6y - 1$               |
| $c_2, c_7$            | $y^{83} + 47y^{82} + \dots - 2y - 1$               |
| $c_3, c_4, c_8$       | $y^{83} - 89y^{82} + \dots + 16906y - 289$         |
| <i>C</i> <sub>5</sub> | $y^{83} - 17y^{82} + \dots + 3479646y - 100489$    |
| $c_6,c_{11}$          | $y^{83} + 39y^{82} + \dots - 2y - 1$               |
| <i>c</i> <sub>9</sub> | $y^{83} - 9y^{82} + \dots - 36274y - 841$          |
| $c_{10}$              | $y^{83} + 11y^{82} + \dots - 14y - 1$              |
| $c_{12}$              | $y^{83} + 27y^{82} + \dots - 121693646y - 3122289$ |

# (vi) Complex Volumes and Cusp Shapes

| Solutions to $I_1^u$      | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape          |
|---------------------------|---------------------------------------|---------------------|
| u = -0.133220 + 0.991655I | 0.112602 - 1.022790I                  | 0                   |
| u = -0.133220 - 0.991655I | 0.112602 + 1.022790I                  | 0                   |
| u = 0.464485 + 0.901515I  | 3.37380 + 4.66521I                    | 0                   |
| u = 0.464485 - 0.901515I  | 3.37380 - 4.66521I                    | 0                   |
| u = 0.460237 + 0.843965I  | 2.23760 - 2.68577I                    | -61.406699 + 0.10I  |
| u = 0.460237 - 0.843965I  | 2.23760 + 2.68577I                    | -61.406699 + 0.10I  |
| u = -0.412629 + 0.867916I | -0.09451 - 1.65097I                   | -2.00000 + 3.87536I |
| u = -0.412629 - 0.867916I | -0.09451 + 1.65097I                   | -2.00000 - 3.87536I |
| u = 0.180004 + 1.062710I  | -4.06382 - 0.99415I                   | 0                   |
| u = 0.180004 - 1.062710I  | -4.06382 + 0.99415I                   | 0                   |
| u = -0.158085 + 1.073960I | -2.03798 + 5.86401I                   | 0                   |
| u = -0.158085 - 1.073960I | -2.03798 - 5.86401I                   | 0                   |
| u = -0.481262 + 0.976359I | 2.43576 - 4.31801I                    | 0                   |
| u = -0.481262 - 0.976359I | 2.43576 + 4.31801I                    | 0                   |
| u = 0.240406 + 1.063530I  | -4.57539 + 0.99512I                   | 0                   |
| u = 0.240406 - 1.063530I  | -4.57539 - 0.99512I                   | 0                   |
| u = -0.272320 + 1.076070I | -3.03173 - 5.70325I                   | 0                   |
| u = -0.272320 - 1.076070I | -3.03173 + 5.70325I                   | 0                   |
| u = 0.442956 + 1.018750I  | -3.12620 + 5.10527I                   | 0                   |
| u = 0.442956 - 1.018750I  | -3.12620 - 5.10527I                   | 0                   |
| u = 0.481407 + 1.002460I  | -1.91913 + 6.94168I                   | 0                   |
| u = 0.481407 - 1.002460I  | -1.91913 - 6.94168I                   | 0                   |
| u = -0.405689 + 1.036190I | -2.06362 - 0.62641I                   | 0                   |
| u = -0.405689 - 1.036190I | -2.06362 + 0.62641I                   | 0                   |
| u = -0.493791 + 1.001660I | 0.34760 - 11.85990I                   | 0                   |
| u = -0.493791 - 1.001660I | 0.34760 + 11.85990I                   | 0                   |
| u = 0.869469 + 0.062981I  | -4.54025 - 10.83720I                  | -2.95711 + 7.16406I |
| u = 0.869469 - 0.062981I  | -4.54025 + 10.83720I                  | -2.95711 - 7.16406I |
| u = 0.870200 + 0.027576I  | -6.76117 + 1.63137I                   | -5.57883 - 2.57822I |
| u = 0.870200 - 0.027576I  | -6.76117 - 1.63137I                   | -5.57883 + 2.57822I |

| Solutions to $I_1^u$      | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape          |
|---------------------------|---------------------------------------|---------------------|
| u = -0.869280 + 0.038602I | -7.89508 + 3.30997I                   | -7.43042 - 3.23415I |
| u = -0.869280 - 0.038602I | -7.89508 - 3.30997I                   | -7.43042 + 3.23415I |
| u = -0.868116 + 0.056802I | -6.74487 + 5.74130I                   | -6.14356 - 3.20858I |
| u = -0.868116 - 0.056802I | -6.74487 - 5.74130I                   | -6.14356 + 3.20858I |
| u = 0.853560 + 0.057638I  | -2.00681 - 3.24204I                   | 0.21808 + 1.91880I  |
| u = 0.853560 - 0.057638I  | -2.00681 + 3.24204I                   | 0.21808 - 1.91880I  |
| u = 0.809740              | -2.84497                              | -3.18540            |
| u = 0.485858 + 0.628329I  | 2.83112 + 6.65892I                    | 2.83091 - 7.70358I  |
| u = 0.485858 - 0.628329I  | 2.83112 - 6.65892I                    | 2.83091 + 7.70358I  |
| u = -0.274315 + 0.744403I | -0.270932 - 1.367880I                 | -2.47570 + 5.35724I |
| u = -0.274315 - 0.744403I | -0.270932 + 1.367880I                 | -2.47570 - 5.35724I |
| u = -0.788512 + 0.033384I | 0.20844 + 3.73783I                    | 1.09851 - 4.05017I  |
| u = -0.788512 - 0.033384I | 0.20844 - 3.73783I                    | 1.09851 + 4.05017I  |
| u = -0.443590 + 0.624580I | 0.55457 - 2.06035I                    | -0.38344 + 4.13562I |
| u = -0.443590 - 0.624580I | 0.55457 + 2.06035I                    | -0.38344 - 4.13562I |
| u = 0.480548 + 0.557812I  | 4.32394 - 0.70252I                    | 6.01189 - 0.11159I  |
| u = 0.480548 - 0.557812I  | 4.32394 + 0.70252I                    | 6.01189 + 0.11159I  |
| u = -0.448739 + 1.209870I | -3.40183 - 0.64725I                   | 0                   |
| u = -0.448739 - 1.209870I | -3.40183 + 0.64725I                   | 0                   |
| u = -0.470662 + 1.211330I | -3.24116 - 8.31020I                   | 0                   |
| u = -0.470662 - 1.211330I | -3.24116 + 8.31020I                   | 0                   |
| u = 0.460140 + 1.220060I  | -6.43985 + 4.54605I                   | 0                   |
| u = 0.460140 - 1.220060I  | -6.43985 - 4.54605I                   | 0                   |
| u = -0.570994 + 0.382917I | 2.05864 + 7.62104I                    | 1.38296 - 6.80721I  |
| u = -0.570994 - 0.382917I | 2.05864 - 7.62104I                    | 1.38296 + 6.80721I  |
| u = 0.431215 + 1.244170I  | -5.94329 + 1.26047I                   | 0                   |
| u = 0.431215 - 1.244170I  | -5.94329 - 1.26047I                   | 0                   |
| u = -0.524837 + 0.426422I | 3.94874 + 0.21511I                    | 5.20374 - 0.31901I  |
| u = -0.524837 - 0.426422I | 3.94874 - 0.21511I                    | 5.20374 + 0.31901I  |
| u = 0.489637 + 1.231500I  | -5.52049 + 8.08364I                   | 0                   |

| Solutions to $I_1^u$      | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape          |
|---------------------------|---------------------------------------|---------------------|
| u = 0.489637 - 1.231500I  | -5.52049 - 8.08364I                   | 0                   |
| u = 0.428440 + 1.254520I  | -8.55613 - 6.29178I                   | 0                   |
| u = 0.428440 - 1.254520I  | -8.55613 + 6.29178I                   | 0                   |
| u = -0.432241 + 1.253290I | -10.73130 + 1.17929I                  | 0                   |
| u = -0.432241 - 1.253290I | -10.73130 - 1.17929I                  | 0                   |
| u = -0.443165 + 1.252520I | -11.81410 - 1.31817I                  | 0                   |
| u = -0.443165 - 1.252520I | -11.81410 + 1.31817I                  | 0                   |
| u = 0.449371 + 1.252030I  | -10.64110 + 6.29820I                  | 0                   |
| u = 0.449371 - 1.252030I  | -10.64110 - 6.29820I                  | 0                   |
| u = -0.492052 + 1.237880I | -10.2955 - 10.6345I                   | 0                   |
| u = -0.492052 - 1.237880I | -10.2955 + 10.6345I                   | 0                   |
| u = 0.495073 + 1.237260I  | -8.0709 + 15.7500I                    | 0                   |
| u = 0.495073 - 1.237260I  | -8.0709 - 15.7500I                    | 0                   |
| u = -0.483809 + 1.241760I | -11.51720 - 8.16214I                  | 0                   |
| u = -0.483809 - 1.241760I | -11.51720 + 8.16214I                  | 0                   |
| u = 0.478597 + 1.243910I  | -10.42700 + 3.19484I                  | 0                   |
| u = 0.478597 - 1.243910I  | -10.42700 - 3.19484I                  | 0                   |
| u = 0.546008 + 0.366004I  | -0.17694 - 2.80834I                   | -1.96326 + 3.21508I |
| u = 0.546008 - 0.366004I  | -0.17694 + 2.80834I                   | -1.96326 - 3.21508I |
| u = -0.545383 + 0.148864I | 0.31558 - 3.00332I                    | -1.47850 + 2.74614I |
| u = -0.545383 - 0.148864I | 0.31558 + 3.00332I                    | -1.47850 - 2.74614I |
| u = 0.500212 + 0.257889I  | -1.12463 - 1.27478I                   | -4.20587 + 3.81637I |
| u = 0.500212 - 0.257889I  | -1.12463 + 1.27478I                   | -4.20587 - 3.81637I |

## II. u-Polynomials

| Crossings       | u-Polynomials at each crossing            |
|-----------------|---|
| $c_1$           | $u^{83} + 47u^{82} + \dots - 2u - 1$      |
| $c_2, c_7$      | $u^{83} + u^{82} + \dots + u^2 + 1$       |
| $c_3, c_4, c_8$ | $u^{83} - u^{82} + \dots + 124u + 17$     |
| $c_5$           | $u^{83} + u^{82} + \dots + 450u + 317$    |
| $c_6, c_{11}$   | $u^{83} - u^{82} + \dots + u^2 + 1$       |
| <i>c</i> 9      | $u^{83} - 11u^{82} + \dots + 98u - 29$    |
| $c_{10}$        | $u^{83} - 39u^{82} + \dots - 2u + 1$      |
| $c_{12}$        | $u^{83} - 5u^{82} + \dots - 2422u + 1767$ |

## III. Riley Polynomials

| Crossings       | Riley Polynomials at each crossing                 |
|-----------------|--|
| $c_1$           | $y^{83} - 21y^{82} + \dots - 6y - 1$               |
| $c_2, c_7$      | $y^{83} + 47y^{82} + \dots - 2y - 1$               |
| $c_3, c_4, c_8$ | $y^{83} - 89y^{82} + \dots + 16906y - 289$         |
| $c_5$           | $y^{83} - 17y^{82} + \dots + 3479646y - 100489$    |
| $c_6, c_{11}$   | $y^{83} + 39y^{82} + \dots - 2y - 1$               |
| <i>c</i> 9      | $y^{83} - 9y^{82} + \dots - 36274y - 841$          |
| $c_{10}$        | $y^{83} + 11y^{82} + \dots - 14y - 1$              |
| $c_{12}$        | $y^{83} + 27y^{82} + \dots - 121693646y - 3122289$ |