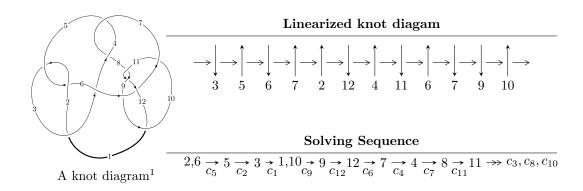
$12n_{0023} (K12n_{0023})$



Ideals for irreducible components² of X_{par}

$$\begin{split} I_1^u &= \langle -65383723517u^{23} - 453837508340u^{22} + \dots + 211475563064b - 190647925896, \\ &- 283168958672u^{23} - 1828538327515u^{22} + \dots + 422951126128a - 1427493398353, \\ u^{24} + 7u^{23} + \dots + 4u + 1 \rangle \\ I_2^u &= \langle -u^3 - u^2 + b - u, -u^3 + a - u + 1, u^4 + u^2 - u + 1 \rangle \\ I_3^u &= \langle 85a^4u - 127a^4 + 387a^3u - 586a^3 + 170a^2u - 254a^2 - 1331au + 661b + 690a - 639u + 76, \\ u^5 + u^4u + 5a^4 + 3a^3u + 4a^3 + 4a^2u - 6a^2 + 4au - 7a + 3u - 1, u^2 - u + 1 \rangle \\ I_4^u &= \langle -u^5 - u^4 - 2u^3 - u^2 + b - u - 1, -u^3 - 2u^2 + a - 2u - 1, u^6 + u^5 + 2u^4 + 2u^3 + 2u^2 + 2u + 1 \rangle \end{split}$$

* 4 irreducible components of $\dim_{\mathbb{C}} = 0$, with total 44 representations.

¹The image of knot diagram is generated by the software "**Draw programme**" developed by Andrew Bartholomew(http://www.layer8.co.uk/maths/draw/index.htm#Running-draw), where we modified some parts for our purpose(https://github.com/CATsTAILs/LinksPainter).

 $^{^2}$ All coefficients of polynomials are rational numbers. But the coefficients are sometimes approximated in decimal forms when there is not enough margin.

$$I. \\ I_1^u = \langle -6.54 \times 10^{10} u^{23} - 4.54 \times 10^{11} u^{22} + \dots + 2.11 \times 10^{11} b - 1.91 \times 10^{11}, \ -2.83 \times 10^{11} u^{23} - 1.83 \times 10^{12} u^{22} + \dots + 4.23 \times 10^{11} a - 1.43 \times 10^{12}, \ u^{24} + 7u^{23} + \dots + 4u + 1 \rangle$$

(i) Arc colorings

$$a_2 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_6 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} 1 \\ u^2 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} u^3 \\ u^5 + u^3 + u \end{pmatrix}$$

$$a_1 = \begin{pmatrix} 0.669508u^{23} + 4.32329u^{22} + \dots - 0.711116u + 3.37508 \\ 0.309179u^{23} + 2.14605u^{22} + \dots + 1.09437u + 0.901513 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} 0.360329u^{23} + 2.17723u^{22} + \dots + 1.09437u + 0.901513 \\ 0.309179u^{23} + 2.14605u^{22} + \dots + 1.09437u + 0.901513 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} 0.954675u^{23} + 6.60431u^{22} + \dots + 1.90437u + 0.901513 \\ 0.103867u^{23} + 0.631846u^{22} + \dots + 1.92070u + 0.466780 \end{pmatrix}$$

$$a_{7} = \begin{pmatrix} -0.379476u^{23} - 2.46625u^{22} + \dots + 1.86572u - 1.71578 \\ -0.260086u^{23} - 1.75059u^{22} + \dots - 0.202905u - 0.639562 \end{pmatrix}$$

$$a_{4} = \begin{pmatrix} -u^3 \\ u^3 + u \end{pmatrix}$$

$$a_{8} = \begin{pmatrix} -0.336233u^{23} - 2.26307u^{22} + \dots - 1.85658u - 1.73341 \\ -0.223668u^{23} - 1.41378u^{22} + \dots + 0.416575u - 0.352405 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 0.406427u^{23} + 2.72175u^{22} + \dots - 0.116545u + 1.59093 \\ 0.178954u^{23} + 1.12467u^{22} + \dots + 1.69860u + 0.508208 \end{pmatrix}$$

(ii) Obstruction class = -1

(iii) Cusp Shapes $= -\frac{372525508513}{422951126128}u^{23} - \frac{297894180927}{52868890766}u^{22} + \dots - \frac{5224084603407}{422951126128}u - \frac{308570800851}{52868890766}u^{23} + \dots - \frac{5224084603407}{422951126128}u^{23} + \dots - \frac{308570800851}{52868890766}u^{23} + \dots - \frac{3085708000851}{52868890766}u^{23} + \dots - \frac{3085708000851}{5286$

| Crossings | u-Polynomials at each crossing |
|---------------|---|
| c_1 | $u^{24} + 3u^{23} + \dots - 8u + 1$ |
| c_2, c_5 | $u^{24} + 7u^{23} + \dots + 4u + 1$ |
| c_3 | $u^{24} - 7u^{23} + \dots + 155372u + 47236$ |
| c_4, c_7 | $u^{24} + 2u^{23} + \dots + 7168u + 1024$ |
| c_6 | $u^{24} - 4u^{23} + \dots - 3u + 1$ |
| c_8, c_{11} | $u^{24} - 13u^{23} + \dots - 2u + 1$ |
| <i>c</i> 9 | $u^{24} - 2u^{23} + \dots + 2185u + 1831$ |
| c_{10} | $u^{24} + 4u^{23} + \dots - 3009503u + 1672193$ |
| c_{12} | $u^{24} + u^{23} + \dots - 5120u + 1024$ |

| Crossings | Riley Polynomials at each crossing |
|-----------------------|--|
| c_1 | $y^{24} + 43y^{23} + \dots + 60y + 1$ |
| c_2, c_5 | $y^{24} + 3y^{23} + \dots - 8y + 1$ |
| c ₃ | $y^{24} + 107y^{23} + \dots - 359116296y + 2231239696$ |
| c_4, c_7 | $y^{24} - 30y^{23} + \dots - 3145728y + 1048576$ |
| <i>C</i> ₆ | $y^{24} + 30y^{22} + \dots + y + 1$ |
| c_8, c_{11} | $y^{24} - 27y^{23} + \dots - 198y + 1$ |
| <i>c</i> 9 | $y^{24} + 20y^{23} + \dots + 72680737y + 3352561$ |
| c_{10} | $y^{24} + 132y^{23} + \dots + 20945455419869y + 2796229429249$ |
| c_{12} | $y^{24} - 57y^{23} + \dots - 1572864y + 1048576$ |

| Solutions to I_1^u | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape |
|---------------------------|---------------------------------------|---------------------|
| u = 0.389764 + 0.874669I | | |
| a = -2.77917 - 3.58598I | -2.26240 + 2.45863I | -0.58956 - 2.80745I |
| b = 0.772730 + 0.886269I | | |
| u = 0.389764 - 0.874669I | | |
| a = -2.77917 + 3.58598I | -2.26240 - 2.45863I | -0.58956 + 2.80745I |
| b = 0.772730 - 0.886269I | | |
| u = 0.531670 + 0.965706I | | |
| a = -1.110060 - 0.431467I | -0.14272 + 2.78886I | 1.24898 - 0.91559I |
| b = 0.161827 - 0.572669I | | |
| u = 0.531670 - 0.965706I | | |
| a = -1.110060 + 0.431467I | -0.14272 - 2.78886I | 1.24898 + 0.91559I |
| b = 0.161827 + 0.572669I | | |
| u = 0.476195 + 0.627959I | | |
| a = -0.327508 + 0.824390I | 0.84077 + 1.37467I | 5.35239 - 4.26754I |
| b = 0.002656 + 0.357569I | | |
| u = 0.476195 - 0.627959I | | |
| a = -0.327508 - 0.824390I | 0.84077 - 1.37467I | 5.35239 + 4.26754I |
| b = 0.002656 - 0.357569I | | |
| u = -0.686903 + 1.011450I | | |
| a = -0.675553 - 0.075442I | -5.30004 - 7.06597I | -3.39619 + 6.37751I |
| b = 0.016958 + 1.263390I | | |
| u = -0.686903 - 1.011450I | | |
| a = -0.675553 + 0.075442I | -5.30004 + 7.06597I | -3.39619 - 6.37751I |
| b = 0.016958 - 1.263390I | | |
| u = -0.539649 + 1.181310I | | |
| a = 0.959620 - 0.350796I | -5.91731 + 1.32680I | -4.55064 - 0.68264I |
| b = -1.16629 - 1.15098I | | |
| u = -0.539649 - 1.181310I | | |
| a = 0.959620 + 0.350796I | -5.91731 - 1.32680I | -4.55064 + 0.68264I |
| b = -1.16629 + 1.15098I | | |

| Solutions to I_1^u | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape |
|---------------------------|---------------------------------------|---------------------|
| u = 1.064580 + 0.846503I | | |
| a = -0.62366 - 1.42540I | 0.03963 + 1.93559I | 3.24137 - 4.51519I |
| b = 1.03585 - 3.55889I | | |
| u = 1.064580 - 0.846503I | | |
| a = -0.62366 + 1.42540I | 0.03963 - 1.93559I | 3.24137 + 4.51519I |
| b = 1.03585 + 3.55889I | | |
| u = -0.89305 + 1.24747I | | |
| a = -1.03439 - 1.00571I | 13.6003 - 6.5164I | -1.83375 + 2.31506I |
| b = -1.51651 + 1.14075I | | |
| u = -0.89305 - 1.24747I | | |
| a = -1.03439 + 1.00571I | 13.6003 + 6.5164I | -1.83375 - 2.31506I |
| b = -1.51651 - 1.14075I | | |
| u = -0.87342 + 1.29253I | | |
| a = 1.44913 + 1.22589I | 13.5215 - 14.1664I | -1.97832 + 6.01811I |
| b = 1.70664 - 2.23520I | | |
| u = -0.87342 - 1.29253I | | |
| a = 1.44913 - 1.22589I | 13.5215 + 14.1664I | -1.97832 - 6.01811I |
| b = 1.70664 + 2.23520I | | |
| u = -1.38451 + 0.86873I | | |
| a = -0.750407 - 0.670749I | 15.2941 - 1.5620I | -0.87276 + 1.81859I |
| b = -2.63229 - 0.87469I | | |
| u = -1.38451 - 0.86873I | | |
| a = -0.750407 + 0.670749I | 15.2941 + 1.5620I | -0.87276 - 1.81859I |
| b = -2.63229 + 0.87469I | | |
| u = -1.48666 + 0.74894I | | |
| a = 0.372127 + 0.956988I | 15.6939 + 6.0170I | -0.56934 - 2.21062I |
| b = 2.70664 + 2.90079I | | |
| u = -1.48666 - 0.74894I | | |
| a = 0.372127 - 0.956988I | 15.6939 - 6.0170I | -0.56934 + 2.21062I |
| b = 2.70664 - 2.90079I | | |

| Solutions to I_1^u | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape |
|---------------------------|---------------------------------------|---------------------|
| u = 0.166881 + 0.257157I | | |
| a = 2.61727 - 2.58686I | -2.60162 - 0.06406I | -5.33602 - 1.30009I |
| b = -0.422595 + 0.308191I | | |
| u = 0.166881 - 0.257157I | | |
| a = 2.61727 + 2.58686I | -2.60162 + 0.06406I | -5.33602 + 1.30009I |
| b = -0.422595 - 0.308191I | | |
| u = -0.264909 + 0.086925I | | |
| a = 0.90260 + 2.62839I | 0.00212 + 1.46917I | 0.28384 - 4.39333I |
| b = 0.334375 + 0.643835I | | |
| u = -0.264909 - 0.086925I | | |
| a = 0.90260 - 2.62839I | 0.00212 - 1.46917I | 0.28384 + 4.39333I |
| b = 0.334375 - 0.643835I | | |

II.
$$I_2^u = \langle -u^3 - u^2 + b - u, -u^3 + a - u + 1, u^4 + u^2 - u + 1 \rangle$$

(i) Arc colorings

$$a_{2} = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_{6} = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{5} = \begin{pmatrix} 1 \\ u^{2} \end{pmatrix}$$

$$a_{3} = \begin{pmatrix} u \\ u^{3} + u \end{pmatrix}$$

$$a_{1} = \begin{pmatrix} u^{3} \\ u^{2} \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} u^{3} + u - 1 \\ u^{3} + u^{2} + u \end{pmatrix}$$

$$a_{9} = \begin{pmatrix} -u^{2} - 1 \\ u^{3} + u^{2} + u \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} u^{3} \\ u^{2} \end{pmatrix}$$

$$a_{7} = \begin{pmatrix} -u^{3} + u^{2} - u + 1 \\ -u^{2} + u - 1 \end{pmatrix}$$

$$a_{4} = \begin{pmatrix} -u^{3} \\ u^{3} + u \end{pmatrix}$$

$$a_{8} = \begin{pmatrix} -u^{3} \\ -u^{2} \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} u^{3} - u^{2} - 1 \\ u^{3} + 2u^{2} + u \end{pmatrix}$$

- (ii) Obstruction class = 1
- (iii) Cusp Shapes = $u^3 6u^2 + 2u 7$

| Crossings | u-Polynomials at each crossing |
|-----------------------|--------------------------------|
| c_1 | $u^4 - 2u^3 + 3u^2 - u + 1$ |
| c_2, c_4 | $u^4 + u^2 + u + 1$ |
| c_3 | $u^4 + 3u^3 + 4u^2 + 3u + 2$ |
| c_5, c_7 | $u^4 + u^2 - u + 1$ |
| c_6 | $u^4 + 2u^3 + 3u^2 + u + 1$ |
| <i>c</i> ₈ | $(u-1)^4$ |
| c_9, c_{10} | $u^4 + u^3 + 3u^2 + 2u + 1$ |
| c_{11} | $(u+1)^4$ |
| c_{12} | u^4 |

| Crossings | Riley Polynomials at each crossing |
|-----------------------|------------------------------------|
| c_1, c_6 | $y^4 + 2y^3 + 7y^2 + 5y + 1$ |
| c_2, c_4, c_5 c_7 | $y^4 + 2y^3 + 3y^2 + y + 1$ |
| <i>c</i> ₃ | $y^4 - y^3 + 2y^2 + 7y + 4$ |
| c_8, c_{11} | $(y-1)^4$ |
| c_9,c_{10} | $y^4 + 5y^3 + 7y^2 + 2y + 1$ |
| c_{12} | y^4 |

| Solutions to I_2^u | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape |
|---------------------------|---------------------------------------|---------------------|
| u = 0.547424 + 0.585652I | | |
| a = -0.851808 + 0.911292I | -0.66484 + 1.39709I | -6.04449 - 2.35025I |
| b = 0.10488 + 1.55249I | | |
| u = 0.547424 - 0.585652I | | |
| a = -0.851808 - 0.911292I | -0.66484 - 1.39709I | -6.04449 + 2.35025I |
| b = 0.10488 - 1.55249I | | |
| u = -0.547424 + 1.120870I | | |
| a = 0.351808 + 0.720342I | -4.26996 - 7.64338I | -0.45551 + 9.20433I |
| b = 0.395123 - 0.506844I | | |
| u = -0.547424 - 1.120870I | | |
| a = 0.351808 - 0.720342I | -4.26996 + 7.64338I | -0.45551 - 9.20433I |
| b = 0.395123 + 0.506844I | | |

III.

$$I_3^u = \langle 85a^4u + 387a^3u + \dots + 690a + 76, \ a^4u + 3a^3u + \dots - 7a - 1, \ u^2 - u + 1 \rangle$$

(i) Arc colorings

$$a_{2} = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_{6} = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{5} = \begin{pmatrix} 1 \\ u - 1 \end{pmatrix}$$

$$a_{3} = \begin{pmatrix} u \\ u - 1 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} -1 \\ 0 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} 0.128593a^{4}u - 0.585477a^{3}u + \dots - 1.04387a - 0.114977 \end{pmatrix}$$

$$a_{9} = \begin{pmatrix} 0.128593a^{4}u + 0.585477a^{3}u + \dots + 2.04387a + 0.114977 \\ -0.128593a^{4}u - 0.585477a^{3}u + \dots + 2.04387a - 0.114977 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} 0.00605144a^{4}u - 0.0665658a^{3}u + \dots - 0.715582a - 0.806354 \\ 0.337368a^{4}u + 1.28896a^{3}u + \dots + 0.856278a - 0.204236 \end{pmatrix}$$

$$a_{7} = \begin{pmatrix} -0.0862330a^{4}u - 0.0514372a^{3}u + \dots + 4.05295a + 0.240545 \\ 0.611195a^{4}u + 2.27685a^{3}u + \dots + 2.72617a - 1.44175 \end{pmatrix}$$

$$a_{8} = \begin{pmatrix} 1 \\ u - 1 \end{pmatrix}$$

$$a_{8} = \begin{pmatrix} -0.0862330a^{4}u - 0.0514372a^{3}u + \dots - 4.05295a + 0.240545 \\ 0.611195a^{4}u + 2.27685a^{3}u + \dots + 2.72617a - 1.44175 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} -0.0269292a^{4}u + 0.249622a^{3}u + \dots - 5.06657a - 0.726172 \\ 0.611195a^{4}u + 2.27685a^{3}u + \dots + 2.72617a - 1.44175 \end{pmatrix}$$

(ii) Obstruction class = 1

(iii) Cusp Shapes
$$= \frac{1400}{661}a^4u - \frac{2675}{661}a^4 + \frac{3769}{661}a^3u - \frac{11557}{661}a^3 - \frac{4471}{661}a^2u - \frac{723}{661}a^2 - \frac{11463}{661}au + \frac{10937}{661}a - \frac{4148}{661}u - \frac{3453}{661}au + \frac{10937}{661}au - \frac{11463}{661}au - \frac{11463}{$$

| Crossings | u-Polynomials at each crossing |
|-----------------------|---------------------------------------|
| c_1,c_3,c_5 | $(u^2 - u + 1)^5$ |
| c_2 | $(u^2 + u + 1)^5$ |
| c_4, c_7 | u^{10} |
| <i>c</i> ₆ | $(u^5 - 3u^4 + 4u^3 - u^2 - u + 1)^2$ |
| <i>c</i> ₈ | $(u^5 + u^4 - 2u^3 - u^2 + u - 1)^2$ |
| c_9, c_{12} | $(u^5 + u^4 + 2u^3 + u^2 + u + 1)^2$ |
| c_{10}, c_{11} | $(u^5 - u^4 - 2u^3 + u^2 + u + 1)^2$ |

| Crossings | Riley Polynomials at each crossing |
|-----------------------|--|
| c_1, c_2, c_3 c_5 | $(y^2+y+1)^5$ |
| c_4, c_7 | y^{10} |
| c_6 | $(y^5 - y^4 + 8y^3 - 3y^2 + 3y - 1)^2$ |
| c_8, c_{10}, c_{11} | $(y^5 - 5y^4 + 8y^3 - 3y^2 - y - 1)^2$ |
| c_9,c_{12} | $(y^5 + 3y^4 + 4y^3 + y^2 - y - 1)^2$ |

| Solutions to I_3^u | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape |
|---------------------------|---------------------------------------|---------------------|
| u = 0.500000 + 0.866025I | | |
| a = 0.953786 - 0.485650I | -5.87256 + 6.43072I | -9.93110 - 1.72471I |
| b = 0.455697 + 1.200150I | | |
| u = 0.500000 + 0.866025I | | |
| a = -1.124940 - 0.303641I | -5.87256 - 2.37095I | -6.85700 + 6.98324I |
| b = 0.455697 - 1.200150I | | |
| u = 0.500000 + 0.866025I | | |
| a = -1.42401 + 0.21550I | -0.32910 + 3.56046I | -2.01870 - 9.75023I |
| b = -0.339110 - 0.822375I | | |
| u = 0.500000 + 0.866025I | | |
| a = 0.000387 + 0.371855I | -0.329100 + 0.499304I | -1.95395 - 0.91636I |
| b = -0.339110 + 0.822375I | | |
| u = 0.500000 + 0.866025I | | |
| a = -3.90523 - 0.66409I | -2.40108 + 2.02988I | 2.76075 + 3.67600I |
| b = 0.766826 | | |
| u = 0.500000 - 0.866025I | | |
| a = 0.953786 + 0.485650I | -5.87256 - 6.43072I | -9.93110 + 1.72471I |
| b = 0.455697 - 1.200150I | | |
| u = 0.500000 - 0.866025I | | |
| a = -1.124940 + 0.303641I | -5.87256 + 2.37095I | -6.85700 - 6.98324I |
| b = 0.455697 + 1.200150I | | |
| u = 0.500000 - 0.866025I | | |
| a = -1.42401 - 0.21550I | -0.32910 - 3.56046I | -2.01870 + 9.75023I |
| b = -0.339110 + 0.822375I | | |
| u = 0.500000 - 0.866025I | | |
| a = 0.000387 - 0.371855I | -0.329100 - 0.499304I | -1.95395 + 0.91636I |
| b = -0.339110 - 0.822375I | | |
| u = 0.500000 - 0.866025I | | |
| a = -3.90523 + 0.66409I | -2.40108 - 2.02988I | 2.76075 - 3.67600I |
| b = 0.766826 | | |

$$\text{IV. } I_4^u = \langle -u^5 - u^4 - 2u^3 - u^2 + b - u - 1, \ -u^3 - 2u^2 + a - 2u - 1, \ u^6 + u^5 + 2u^4 + 2u^3 + 2u^2 + 2u + 1 \rangle$$

(i) Arc colorings

$$a_{2} = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_{6} = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{5} = \begin{pmatrix} 1 \\ u^{2} \end{pmatrix}$$

$$a_{3} = \begin{pmatrix} u \\ u^{3} + u \end{pmatrix}$$

$$a_{1} = \begin{pmatrix} u^{3} + 2u^{2} + 2u + 1 \\ u^{5} + u^{4} + 2u^{3} + u^{2} + u + 1 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} u^{3} + 2u^{2} + 2u + 1 \\ u^{5} + u^{4} + 2u^{3} + u^{2} + u + 1 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} u^{5} - u^{4} - u^{3} + u^{2} + u \\ u^{5} + u^{4} + 2u^{3} + u^{2} + u + 1 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} u^{3} \\ u^{5} + u^{3} + u \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} u^{3} \\ u^{5} + u^{3} + u \end{pmatrix}$$

$$a_{13} = \begin{pmatrix} -u^{3} \\ u^{3} + u \end{pmatrix}$$

$$a_{4} = \begin{pmatrix} -u^{3} \\ u^{3} + u \end{pmatrix}$$

$$a_{8} = \begin{pmatrix} -u^{3} \\ -u^{5} - u^{3} - u \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} -u^{5} - u^{4} + u^{2} + u \\ 2u^{5} + u^{4} + 3u^{3} + u^{2} + 2u + 1 \end{pmatrix}$$

- (ii) Obstruction class = 1
- (iii) Cusp Shapes = $-u^5 u^4 8u^3 2u^2 5u 4$

| Crossings | u-Polynomials at each crossing |
|-----------------------|---|
| c_1 | $u^6 - 3u^5 + 4u^4 - 2u^3 + 1$ |
| c_2, c_4 | $u^6 - u^5 + 2u^4 - 2u^3 + 2u^2 - 2u + 1$ |
| c_3 | $(u^3 - u^2 + 1)^2$ |
| c_5, c_7 | $u^6 + u^5 + 2u^4 + 2u^3 + 2u^2 + 2u + 1$ |
| c_6 | $u^6 + 3u^5 + 4u^4 + 2u^3 + 1$ |
| <i>c</i> ₈ | $(u-1)^6$ |
| c_9, c_{10} | $u^6 + 2u^3 + 4u^2 + 3u + 1$ |
| c_{11} | $(u+1)^6$ |
| c_{12} | u^6 |

| Crossings | Riley Polynomials at each crossing |
|-----------------------|--------------------------------------|
| c_1, c_6 | $y^6 - y^5 + 4y^4 - 2y^3 + 8y^2 + 1$ |
| c_2, c_4, c_5 c_7 | $y^6 + 3y^5 + 4y^4 + 2y^3 + 1$ |
| <i>c</i> ₃ | $(y^3 - y^2 + 2y - 1)^2$ |
| c_8, c_{11} | $(y-1)^6$ |
| c_9,c_{10} | $y^6 + 8y^4 - 2y^3 + 4y^2 - y + 1$ |
| c_{12} | y^6 |

| Solutions to I_4^u | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape |
|---------------------------|---------------------------------------|---------------------|
| u = 0.498832 + 1.001300I | | |
| a = -0.88615 + 3.74409I | -1.91067 + 2.82812I | 5.15973 - 2.26538I |
| b = -1.14366 - 1.20015I | | |
| u = 0.498832 - 1.001300I | | |
| a = -0.88615 - 3.74409I | -1.91067 - 2.82812I | 5.15973 + 2.26538I |
| b = -1.14366 + 1.20015I | | |
| u = -0.284920 + 1.115140I | | |
| a = -0.854760 - 0.155763I | -6.04826 | -7.59911 + 2.50363I |
| b = 0.662359 + 0.362106I | | |
| u = -0.284920 - 1.115140I | | |
| a = -0.854760 + 0.155763I | -6.04826 | -7.59911 - 2.50363I |
| b = 0.662359 - 0.362106I | | |
| u = -0.713912 + 0.305839I | | |
| a = 0.240915 + 0.177333I | -1.91067 + 2.82812I | -0.06063 - 4.05868I |
| b = 0.481306 + 0.637866I | | |
| u = -0.713912 - 0.305839I | | |
| a = 0.240915 - 0.177333I | -1.91067 - 2.82812I | -0.06063 + 4.05868I |
| b = 0.481306 - 0.637866I | | |

V. u-Polynomials

| Crossings | u-Polynomials at each crossing |
|-----------------------|---|
| c_1 | $ (u^{2} - u + 1)^{5}(u^{4} - 2u^{3} + 3u^{2} - u + 1)(u^{6} - 3u^{5} + 4u^{4} - 2u^{3} + 1) $ $ \cdot (u^{24} + 3u^{23} + \dots - 8u + 1) $ |
| c_2 | $ (u^{2} + u + 1)^{5}(u^{4} + u^{2} + u + 1)(u^{6} - u^{5} + 2u^{4} - 2u^{3} + 2u^{2} - 2u + 1) $ $ \cdot (u^{24} + 7u^{23} + \dots + 4u + 1) $ |
| c_3 | $(u^{2} - u + 1)^{5}(u^{3} - u^{2} + 1)^{2}(u^{4} + 3u^{3} + 4u^{2} + 3u + 2)$ $\cdot (u^{24} - 7u^{23} + \dots + 155372u + 47236)$ |
| c_4 | $u^{10}(u^4 + u^2 + u + 1)(u^6 - u^5 + 2u^4 - 2u^3 + 2u^2 - 2u + 1)$ $\cdot (u^{24} + 2u^{23} + \dots + 7168u + 1024)$ |
| c_5 | $(u^{2} - u + 1)^{5}(u^{4} + u^{2} - u + 1)(u^{6} + u^{5} + 2u^{4} + 2u^{3} + 2u^{2} + 2u + 1)$ $\cdot (u^{24} + 7u^{23} + \dots + 4u + 1)$ |
| c_6 | $(u^{4} + 2u^{3} + 3u^{2} + u + 1)(u^{5} - 3u^{4} + 4u^{3} - u^{2} - u + 1)^{2}$ $\cdot (u^{6} + 3u^{5} + 4u^{4} + 2u^{3} + 1)(u^{24} - 4u^{23} + \dots - 3u + 1)$ |
| <i>c</i> ₇ | $u^{10}(u^4 + u^2 - u + 1)(u^6 + u^5 + 2u^4 + 2u^3 + 2u^2 + 2u + 1)$ $\cdot (u^{24} + 2u^{23} + \dots + 7168u + 1024)$ |
| c_8 | $((u-1)^{10})(u^5 + u^4 + \dots + u - 1)^2(u^{24} - 13u^{23} + \dots - 2u + 1)$ |
| c_9 | $(u^{4} + u^{3} + 3u^{2} + 2u + 1)(u^{5} + u^{4} + 2u^{3} + u^{2} + u + 1)^{2}$ $\cdot (u^{6} + 2u^{3} + 4u^{2} + 3u + 1)(u^{24} - 2u^{23} + \dots + 2185u + 1831)$ |
| c_{10} | $(u^{4} + u^{3} + 3u^{2} + 2u + 1)(u^{5} - u^{4} - 2u^{3} + u^{2} + u + 1)^{2}$ $\cdot (u^{6} + 2u^{3} + 4u^{2} + 3u + 1)(u^{24} + 4u^{23} + \dots - 3009503u + 1672193)$ |
| c_{11} | $((u+1)^{10})(u^5 - u^4 + \dots + u + 1)^2(u^{24} - 13u^{23} + \dots - 2u + 1)$ |
| c_{12} | $u^{10}(u^5 + u^4 + \dots + u + 1)^2(u^{24} + u^{23} + \dots - 5120u + 1024)$ 20 |

VI. Riley Polynomials

| Crossings | Riley Polynomials at each crossing |
|---------------|--|
| c_1 | $((y^{2} + y + 1)^{5})(y^{4} + 2y^{3} + \dots + 5y + 1)(y^{6} - y^{5} + \dots + 8y^{2} + 1)$ $\cdot (y^{24} + 43y^{23} + \dots + 60y + 1)$ |
| c_2, c_5 | $(y^{2} + y + 1)^{5}(y^{4} + 2y^{3} + 3y^{2} + y + 1)(y^{6} + 3y^{5} + 4y^{4} + 2y^{3} + 1)$ $\cdot (y^{24} + 3y^{23} + \dots - 8y + 1)$ |
| c_3 | $(y^{2} + y + 1)^{5}(y^{3} - y^{2} + 2y - 1)^{2}(y^{4} - y^{3} + 2y^{2} + 7y + 4)$ $\cdot (y^{24} + 107y^{23} + \dots - 359116296y + 2231239696)$ |
| c_4, c_7 | $y^{10}(y^4 + 2y^3 + 3y^2 + y + 1)(y^6 + 3y^5 + 4y^4 + 2y^3 + 1)$ $\cdot (y^{24} - 30y^{23} + \dots - 3145728y + 1048576)$ |
| c_6 | $(y^4 + 2y^3 + 7y^2 + 5y + 1)(y^5 - y^4 + 8y^3 - 3y^2 + 3y - 1)^2$ $\cdot (y^6 - y^5 + 4y^4 - 2y^3 + 8y^2 + 1)(y^{24} + 30y^{22} + \dots + y + 1)$ |
| c_8, c_{11} | $(y-1)^{10}(y^5 - 5y^4 + 8y^3 - 3y^2 - y - 1)^2$ $\cdot (y^{24} - 27y^{23} + \dots - 198y + 1)$ |
| <i>c</i> 9 | $(y^4 + 5y^3 + 7y^2 + 2y + 1)(y^5 + 3y^4 + 4y^3 + y^2 - y - 1)^2$ $\cdot (y^6 + 8y^4 - 2y^3 + 4y^2 - y + 1)$ $\cdot (y^{24} + 20y^{23} + \dots + 72680737y + 3352561)$ |
| c_{10} | $(y^4 + 5y^3 + 7y^2 + 2y + 1)(y^5 - 5y^4 + 8y^3 - 3y^2 - y - 1)^2$ $\cdot (y^6 + 8y^4 - 2y^3 + 4y^2 - y + 1)$ $\cdot (y^{24} + 132y^{23} + \dots + 20945455419869y + 2796229429249)$ |
| c_{12} | $y^{10}(y^5 + 3y^4 + 4y^3 + y^2 - y - 1)^2$ $\cdot (y^{24} - 57y^{23} + \dots - 1572864y + 1048576)$ |