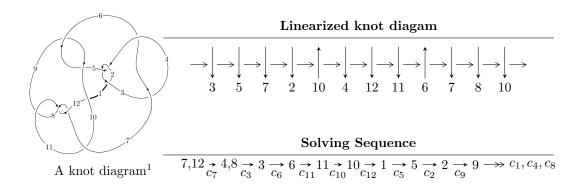
# $12n_{0112} \ (K12n_{0112})$



#### Ideals for irreducible components<sup>2</sup> of $X_{par}$

$$I_1^u = \langle 1077612353882483u^{46} + 6277936033129932u^{45} + \dots + 3412880928878836b - 505154446936889, \\ -1.84787 \times 10^{15}u^{46} - 8.27233 \times 10^{15}u^{45} + \dots + 3.41288 \times 10^{15}a - 4.21925 \times 10^{16}, \\ u^{47} + 4u^{46} + \dots + 19u + 1 \rangle$$

$$I_2^u = \langle b + u, u^2 + a - u + 3, u^3 - u^2 + 2u - 1 \rangle$$

$$I_3^u = \langle -2u^2a - au - u^2 + 5b - 3a - 3u + 1, a^2 + 2u^2 + a + 2, u^3 - u^2 + 2u - 1 \rangle$$

\* 3 irreducible components of  $\dim_{\mathbb{C}} = 0$ , with total 56 representations.

<sup>&</sup>lt;sup>1</sup>The image of knot diagram is generated by the software "**Draw programme**" developed by Andrew Bartholomew(http://www.layer8.co.uk/maths/draw/index.htm#Running-draw), where we modified some parts for our purpose(https://github.com/CATsTAILs/LinksPainter).

<sup>&</sup>lt;sup>2</sup> All coefficients of polynomials are rational numbers. But the coefficients are sometimes approximated in decimal forms when there is not enough margin.

I. 
$$I_1^u = \langle 1.08 \times 10^{15} u^{46} + 6.28 \times 10^{15} u^{45} + \dots + 3.41 \times 10^{15} b - 5.05 \times 10^{14}, \ -1.85 \times 10^{15} u^{46} - 8.27 \times 10^{15} u^{45} + \dots + 3.41 \times 10^{15} a - 4.22 \times 10^{16}, \ u^{47} + 4u^{46} + \dots + 19u + 1 \rangle$$

#### (i) Arc colorings

$$a_{7} = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_{4} = \begin{pmatrix} 0.541439u^{46} + 2.42386u^{45} + \dots + 24.5319u + 12.3627 \\ -0.315749u^{46} - 1.83948u^{45} + \dots - 7.06067u + 0.148014 \end{pmatrix}$$

$$a_{8} = \begin{pmatrix} 1 \\ u^{2} \end{pmatrix}$$

$$a_{3} = \begin{pmatrix} 0.225691u^{46} + 0.584374u^{45} + \dots + 17.4712u + 12.5108 \\ -0.315749u^{46} - 1.83948u^{45} + \dots - 7.06067u + 0.148014 \end{pmatrix}$$

$$a_{6} = \begin{pmatrix} 0.280491u^{46} - 1.05919u^{45} + \dots - 11.4369u - 5.46550 \\ -0.0627768u^{46} - 0.766991u^{45} + \dots + 0.136172u - 0.280491 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} u \\ u^{3} + u \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} u^{3} + 2u \\ u^{3} + u \end{pmatrix}$$

$$a_{5} = \begin{pmatrix} -0.348010u^{46} - 0.729833u^{45} + \dots - 18.8545u - 5.94845 \\ -0.0657486u^{46} + 0.160517u^{45} + \dots - 0.310668u - 0.351986 \end{pmatrix}$$

$$a_{2} = \begin{pmatrix} 0.421710u^{46} + 1.79404u^{45} + \dots + 25.1802u + 9.15766 \\ 0.0657486u^{46} - 0.160517u^{45} + \dots + 0.310668u + 0.351986 \end{pmatrix}$$

$$a_{9} = \begin{pmatrix} u^{2} + 1 \\ u^{4} + 2u^{2} \end{pmatrix}$$

#### (ii) Obstruction class = -1

### (iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
$c_1$	$u^{47} + 30u^{46} + \dots + 15u + 1$
$c_2, c_4$	$u^{47} - 4u^{46} + \dots - 7u - 1$
$c_3, c_6$	$u^{47} - 4u^{46} + \dots + 5u - 1$
$c_5, c_9$	$u^{47} - 3u^{46} + \dots - 1920u^2 + 512$
$c_7, c_8, c_{11}$	$u^{47} - 4u^{46} + \dots + 19u - 1$
$c_{10}$	$u^{47} + 4u^{46} + \dots + 847u - 49$
$c_{12}$	$u^{47} - 22u^{46} + \dots + 8436145u + 61891$

### (v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
$c_1$	$y^{47} - 22y^{46} + \dots + 563y - 1$
$c_2, c_4$	$y^{47} - 30y^{46} + \dots + 15y - 1$
$c_3, c_6$	$y^{47} + 6y^{46} + \dots + 15y - 1$
$c_5, c_9$	$y^{47} + 49y^{46} + \dots + 1966080y - 262144$
$c_7, c_8, c_{11}$	$y^{47} + 38y^{46} + \dots + 299y - 1$
$c_{10}$	$y^{47} - 50y^{46} + \dots + 706923y - 2401$
$c_{12}$	$y^{47} - 78y^{46} + \dots + 77502601952059y - 3830495881$

## (vi) Complex Volumes and Cusp Shapes

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
u = 0.990601		
a = 0.833676	-5.24020	-20.8000
b = 0.664625		
u = 0.786688 + 0.584594I		
a = -0.577297 + 0.239191I	-4.21325 - 2.69895I	-16.8130 + 7.1920I
b = -0.688477 - 0.244449I		
u = 0.786688 - 0.584594I		
a = -0.577297 - 0.239191I	-4.21325 + 2.69895I	-16.8130 - 7.1920I
b = -0.688477 + 0.244449I		
u = -0.937187 + 0.140092I		
a = -1.77830 + 0.44317I	-11.2714 + 9.6299I	-12.05023 - 5.56960I
b = -1.08476 + 1.02775I		
u = -0.937187 - 0.140092I		
a = -1.77830 - 0.44317I	-11.2714 - 9.6299I	-12.05023 + 5.56960I
b = -1.08476 - 1.02775I		
u = -0.909124 + 0.020827I		
a = -1.61166 - 0.74978I	-11.11700 + 1.76651I	-12.65951 - 0.89834I
b = -1.07056 - 1.08227I		
u = -0.909124 - 0.020827I		
a = -1.61166 + 0.74978I	-11.11700 - 1.76651I	-12.65951 + 0.89834I
b = -1.07056 + 1.08227I		
u = -0.884070 + 0.070567I		
a = 1.80575 - 0.63524I	-6.89137 + 3.99655I	-10.09960 - 2.77536I
b = 1.10158 - 1.05658I		
u = -0.884070 - 0.070567I		
a = 1.80575 + 0.63524I	-6.89137 - 3.99655I	-10.09960 + 2.77536I
b = 1.10158 + 1.05658I		
u = 0.066162 + 1.148650I		
a = 0.853937 + 0.565919I	1.43778 - 0.23607I	-8.00000 + 0.I
b = 0.908296 + 0.182917I		

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
u = 0.066162 - 1.148650I		
a = 0.853937 - 0.565919I	1.43778 + 0.23607I	-8.00000 + 0.I
b = 0.908296 - 0.182917I		
u = 0.193279 + 1.168140I		
a = 0.93146 + 1.53635I	0.26621 - 2.20233I	-8.00000 + 0.I
b = 0.201370 - 0.733758I		
u = 0.193279 - 1.168140I		
a = 0.93146 - 1.53635I	0.26621 + 2.20233I	-8.00000 + 0.I
b = 0.201370 + 0.733758I		
u = -0.165090 + 1.196660I		
a = 1.36966 + 0.81390I	5.59945 + 4.78062I	-8.00000 + 0.I
b = 0.37394 - 1.40206I		
u = -0.165090 - 1.196660I		
a = 1.36966 - 0.81390I	5.59945 - 4.78062I	-8.00000 + 0.I
b = 0.37394 + 1.40206I		
u = -0.083039 + 1.251340I		
a = -1.050290 - 0.729908I	6.38366 - 1.10832I	0
b = -0.032297 + 1.293670I		
u = -0.083039 - 1.251340I		
a = -1.050290 + 0.729908I	6.38366 + 1.10832I	0
b = -0.032297 - 1.293670I		
u = -0.528989 + 1.159830I		
a = -0.276035 - 0.628526I	-8.15630 - 4.45150I	0
b = -1.099140 - 0.886724I		
u = -0.528989 - 1.159830I		
a = -0.276035 + 0.628526I	-8.15630 + 4.45150I	0
b = -1.099140 + 0.886724I		
u = -0.431113 + 1.216070I		
a = 0.183252 + 0.675767I	-3.36307 + 0.70782I	0
b = 1.17095 + 0.89948I		

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
u = -0.431113 - 1.216070I		
a = 0.183252 - 0.675767I	-3.36307 - 0.70782I	0
b = 1.17095 - 0.89948I		
u = 0.268673 + 1.267170I		
a = -1.155430 + 0.312483I	2.34688 - 3.35469I	0
b = -0.561623 - 0.268923I		
u = 0.268673 - 1.267170I		
a = -1.155430 - 0.312483I	2.34688 + 3.35469I	0
b = -0.561623 + 0.268923I		
u = 0.195960 + 1.323790I		
a = -1.87522 - 1.08808I	1.76552 - 3.06033I	0
b = -0.483549 + 0.192110I		
u = 0.195960 - 1.323790I		
a = -1.87522 + 1.08808I	1.76552 + 3.06033I	0
b = -0.483549 - 0.192110I		
u = 0.660594		
a = -1.60556	-1.60120	-4.93400
b = -0.440165		
u = -0.442721 + 1.267860I		
a = -1.46962 - 0.89724I	-7.25263 + 3.05957I	0
b = -0.94426 + 1.16097I		
u = -0.442721 - 1.267860I		
a = -1.46962 + 0.89724I	-7.25263 - 3.05957I	0
b = -0.94426 - 1.16097I		
u = 0.492547 + 1.264850I		
a = 0.648333 - 0.236834I	-1.35004 - 5.25916I	0
b = 0.695100 + 0.386206I		
u = 0.492547 - 1.264850I		
a = 0.648333 + 0.236834I	-1.35004 + 5.25916I	0
b = 0.695100 - 0.386206I		

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
u = -0.431930 + 1.300870I		
a = -0.097552 - 0.602796I	-7.00155 + 6.55990I	0
b = -1.16017 - 0.97433I		
u = -0.431930 - 1.300870I		
a = -0.097552 + 0.602796I	-7.00155 - 6.55990I	0
b = -1.16017 + 0.97433I		
u = 0.113592 + 1.383630I		
a = -0.110146 - 0.914625I	4.86422 - 2.82003I	0
b = 0.324059 + 0.771489I		
u = 0.113592 - 1.383630I		
a = -0.110146 + 0.914625I	4.86422 + 2.82003I	0
b = 0.324059 - 0.771489I		
u = -0.403708 + 1.330620I		
a = 1.43895 + 0.94313I	-2.50308 + 8.61469I	0
b = 1.01510 - 1.16548I		
u = -0.403708 - 1.330620I		
a = 1.43895 - 0.94313I	-2.50308 - 8.61469I	0
b = 1.01510 + 1.16548I		
u = -0.41853 + 1.38032I		
a = -1.39448 - 0.94283I	-6.4847 + 14.4827I	0
b = -1.03069 + 1.11636I		
u = -0.41853 - 1.38032I		
a = -1.39448 + 0.94283I	-6.4847 - 14.4827I	0
b = -1.03069 - 1.11636I		
u = 0.532405 + 0.124560I		
a = -0.76238 - 2.70239I	-2.77991 - 0.46414I	-9.29269 - 10.51983I
b = -0.221659 + 0.420216I		
u = 0.532405 - 0.124560I		
a = -0.76238 + 2.70239I	-2.77991 + 0.46414I	-9.29269 + 10.51983I
b = -0.221659 - 0.420216I		

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
u = 0.380325 + 0.322466I		
a = 0.088091 - 0.742546I	-0.572975 - 1.134450I	-6.55719 + 6.13916I
b = 0.519940 + 0.346223I		
u = 0.380325 - 0.322466I		
a = 0.088091 + 0.742546I	-0.572975 + 1.134450I	-6.55719 - 6.13916I
b = 0.519940 - 0.346223I		
u = 0.20471 + 1.49097I		
a = -0.255203 + 0.595995I	2.62514 - 6.12394I	0
b = -0.547663 - 0.662712I		
u = 0.20471 - 1.49097I		
a = -0.255203 - 0.595995I	2.62514 + 6.12394I	0
b = -0.547663 + 0.662712I		
u = -0.394822 + 0.084126I		
a = 0.10651 + 2.29856I	2.33626 - 2.65352I	2.71092 + 0.17214I
b = 0.240504 + 1.222520I		
u = -0.394822 - 0.084126I		
a = 0.10651 - 2.29856I	2.33626 + 2.65352I	2.71092 - 0.17214I
b = 0.240504 - 1.222520I		
u = -0.0592454		
a = 10.7472	-1.19029	-8.22650
b = 0.523564		

II. 
$$I_2^u = \langle b+u, u^2+a-u+3, u^3-u^2+2u-1 \rangle$$

(i) Arc colorings

$$a_{7} = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_{4} = \begin{pmatrix} -u^{2} + u - 3 \\ -u \end{pmatrix}$$

$$a_{8} = \begin{pmatrix} 1 \\ u^{2} \end{pmatrix}$$

$$a_{3} = \begin{pmatrix} -u^{2} - 3 \\ -u \end{pmatrix}$$

$$a_{6} = \begin{pmatrix} -u \\ -u^{2} \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} u \\ u^{2} - u + 1 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} u^{2} + 1 \\ u^{2} - u + 1 \end{pmatrix}$$

$$a_{1} = \begin{pmatrix} -1 \\ 0 \end{pmatrix}$$

$$a_{5} = \begin{pmatrix} -u \\ -u^{2} \end{pmatrix}$$

$$a_{2} = \begin{pmatrix} -u^{2} - u - 2 \\ -u^{2} \end{pmatrix}$$

$$a_{9} = \begin{pmatrix} u^{2} + 1 \\ u^{2} - u + 1 \end{pmatrix}$$

- (ii) Obstruction class = 1
- (iii) Cusp Shapes =  $-12u^2 + 11u 24$

### (iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
$c_1, c_3, c_7$ $c_8$	$u^3 - u^2 + 2u - 1$
$c_2$	$u^3 + u^2 - 1$
$c_4, c_{10}, c_{12}$	$u^3 - u^2 + 1$
$c_5,c_9$	$u^3$
$c_6, c_{11}$	$u^3 + u^2 + 2u + 1$

## (v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
$c_1, c_3, c_6 \\ c_7, c_8, c_{11}$	$y^3 + 3y^2 + 2y - 1$
$c_2, c_4, c_{10}$ $c_{12}$	$y^3 - y^2 + 2y - 1$
$c_5, c_9$	$y^3$

## (vi) Complex Volumes and Cusp Shapes

Solutions to $I_2^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
u = 0.215080 + 1.307140I		
a = -1.122560 + 0.744862I	6.04826 - 5.65624I	-1.68581 + 7.63120I
b = -0.215080 - 1.307140I		
u = 0.215080 - 1.307140I		
a = -1.122560 - 0.744862I	6.04826 + 5.65624I	-1.68581 - 7.63120I
b = -0.215080 + 1.307140I		
u = 0.569840		
a = -2.75488	-2.22691	-21.6280
b = -0.569840		

$$I_3^u = \langle -2u^2a - au - u^2 + 5b - 3a - 3u + 1, \ a^2 + 2u^2 + a + 2, \ u^3 - u^2 + 2u - 1 
angle$$

(i) Arc colorings

$$a_{7} = \begin{pmatrix} 1\\0 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} 0\\u \end{pmatrix}$$

$$a_{4} = \begin{pmatrix} \frac{2}{5}u^{2}a + \frac{1}{5}u^{2} + \dots + \frac{3}{5}a - \frac{1}{5} \end{pmatrix}$$

$$a_{8} = \begin{pmatrix} 1\\u^{2} \end{pmatrix}$$

$$a_{3} = \begin{pmatrix} \frac{2}{5}u^{2}a + \frac{1}{5}u^{2} + \dots + \frac{8}{5}a - \frac{1}{5}\\\frac{2}{5}u^{2}a + \frac{1}{5}u^{2} + \dots + \frac{4}{5}a + \frac{17}{5} \end{pmatrix}$$

$$a_{6} = \begin{pmatrix} \frac{1}{5}u^{2}a + \frac{8}{5}u^{2} + \dots + \frac{4}{5}a + \frac{17}{5}\\-\frac{1}{5}u^{2}a + \frac{2}{5}u^{2} + \dots + \frac{1}{5}a + \frac{8}{5} \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} u\\u^{2} - u + 1 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} u^{2} + 1\\u^{2} - u + 1 \end{pmatrix}$$

$$a_{5} = \begin{pmatrix} \frac{1}{5}u^{2}a + \frac{8}{5}u^{2} + \dots + \frac{4}{5}a + \frac{17}{5}\\-\frac{1}{5}u^{2}a + \frac{2}{5}u^{2} + \dots + \frac{1}{5}a + \frac{8}{5} \end{pmatrix}$$

$$a_{2} = \begin{pmatrix} 2u^{2} + a - u + 3\\-\frac{1}{5}u^{2}a + \frac{2}{5}u^{2} + \dots + \frac{1}{5}a + \frac{8}{5} \end{pmatrix}$$

$$a_{9} = \begin{pmatrix} u^{2} + 1\\u^{2} - u + 1 \end{pmatrix}$$

- (ii) Obstruction class = 1
- (iii) Cusp Shapes =  $-\frac{17}{5}u^2a + \frac{24}{5}au \frac{21}{5}u^2 \frac{28}{5}a + \frac{2}{5}u \frac{74}{5}$

### (iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
$c_1, c_3, c_7$ $c_8$	$(u^3 - u^2 + 2u - 1)^2$
$c_2$	$(u^3 + u^2 - 1)^2$
$c_4, c_{10}, c_{12}$	$(u^3 - u^2 + 1)^2$
$c_5,c_9$	$u^6$
$c_6, c_{11}$	$(u^3 + u^2 + 2u + 1)^2$

## (v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
$c_1, c_3, c_6 \\ c_7, c_8, c_{11}$	$(y^3 + 3y^2 + 2y - 1)^2$
$c_2, c_4, c_{10}$ $c_{12}$	$(y^3 - y^2 + 2y - 1)^2$
$c_5, c_9$	$y^6$

## (vi) Complex Volumes and Cusp Shapes

Solutions to $I_3^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
u = 0.215080 + 1.307140I		
a = 0.824718 - 0.424452I	6.04826	-4.98605 + 1.29886I
b = -0.215080 + 1.307140I		
u = 0.215080 + 1.307140I		
a = -1.82472 + 0.42445I	1.91067 - 2.82812I	-11.5625 - 9.3388I
b = -0.569840		
u = 0.215080 - 1.307140I		
a = 0.824718 + 0.424452I	6.04826	-4.98605 - 1.29886I
b = -0.215080 - 1.307140I		
u = 0.215080 - 1.307140I		
a = -1.82472 - 0.42445I	1.91067 + 2.82812I	-11.5625 + 9.3388I
b = -0.569840		
u = 0.569840		
a = -0.50000 + 1.54901I	1.91067 + 2.82812I	-13.9515 - 6.1477I
b = -0.215080 + 1.307140I		
u = 0.569840		
a = -0.50000 - 1.54901I	1.91067 - 2.82812I	-13.9515 + 6.1477I
b = -0.215080 - 1.307140I		

IV. u-Polynomials

Crossings	u-Polynomials at each crossing
$c_1$	$((u^3 - u^2 + 2u - 1)^3)(u^{47} + 30u^{46} + \dots + 15u + 1)$
$c_2$	$((u^3 + u^2 - 1)^3)(u^{47} - 4u^{46} + \dots - 7u - 1)$
<i>c</i> 3	$((u^3 - u^2 + 2u - 1)^3)(u^{47} - 4u^{46} + \dots + 5u - 1)$
$c_4$	$((u^3 - u^2 + 1)^3)(u^{47} - 4u^{46} + \dots - 7u - 1)$
$c_5, c_9$	$u^9(u^{47} - 3u^{46} + \dots - 1920u^2 + 512)$
<i>c</i> <sub>6</sub>	$((u^3 + u^2 + 2u + 1)^3)(u^{47} - 4u^{46} + \dots + 5u - 1)$
$c_7, c_8$	$((u^3 - u^2 + 2u - 1)^3)(u^{47} - 4u^{46} + \dots + 19u - 1)$
$c_{10}$	$((u^3 - u^2 + 1)^3)(u^{47} + 4u^{46} + \dots + 847u - 49)$
$c_{11}$	$((u^3 + u^2 + 2u + 1)^3)(u^{47} - 4u^{46} + \dots + 19u - 1)$
$c_{12}$	$((u^3 - u^2 + 1)^3)(u^{47} - 22u^{46} + \dots + 8436145u + 61891)$

# V. Riley Polynomials

Crossings	Riley Polynomials at each crossing
$c_1$	$((y^3 + 3y^2 + 2y - 1)^3)(y^{47} - 22y^{46} + \dots + 563y - 1)$
$c_2,c_4$	$((y^3 - y^2 + 2y - 1)^3)(y^{47} - 30y^{46} + \dots + 15y - 1)$
$c_3, c_6$	$((y^3 + 3y^2 + 2y - 1)^3)(y^{47} + 6y^{46} + \dots + 15y - 1)$
$c_5,c_9$	$y^9(y^{47} + 49y^{46} + \dots + 1966080y - 262144)$
$c_7, c_8, c_{11}$	$((y^3 + 3y^2 + 2y - 1)^3)(y^{47} + 38y^{46} + \dots + 299y - 1)$
$c_{10}$	$((y^3 - y^2 + 2y - 1)^3)(y^{47} - 50y^{46} + \dots + 706923y - 2401)$
$c_{12}$	$(y^3 - y^2 + 2y - 1)^3$ $\cdot (y^{47} - 78y^{46} + \dots + 77502601952059y - 3830495881)$