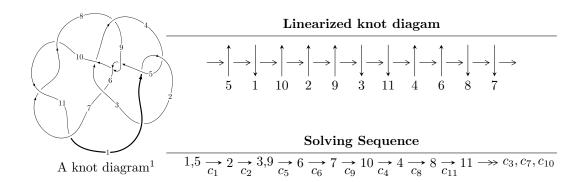
$11a_{29} (K11a_{29})$



Ideals for irreducible components² of X_{par}

$$I_1^u = \langle 4.99106 \times 10^{56} u^{60} - 5.54013 \times 10^{56} u^{59} + \dots + 3.76009 \times 10^{57} b - 3.71146 \times 10^{57},$$

$$- 3.10364 \times 10^{57} u^{60} + 5.28988 \times 10^{57} u^{59} + \dots + 1.12803 \times 10^{58} a - 3.91838 \times 10^{58}, \ u^{61} - 3u^{60} + \dots - 5u - 10^{58} u^{59} + 2u - 2, \ a + 1, \ u^2 + u + 1 \rangle$$

$$I_3^u = \langle 3b - 2u - 1, \ a + u, \ u^2 + u + 1 \rangle$$

* 3 irreducible components of $\dim_{\mathbb{C}} = 0$, with total 65 representations.

¹The image of knot diagram is generated by the software "**Draw programme**" developed by Andrew Bartholomew(http://www.layer8.co.uk/maths/draw/index.htm#Running-draw), where we modified some parts for our purpose(https://github.com/CATsTAILs/LinksPainter).

² All coefficients of polynomials are rational numbers. But the coefficients are sometimes approximated in decimal forms when there is not enough margin.

 $I. \\ I_1^u = \langle 4.99 \times 10^{56} u^{60} - 5.54 \times 10^{56} u^{59} + \dots + 3.76 \times 10^{57} b - 3.71 \times 10^{57}, \ -3.10 \times 10^{57} u^{60} + 5.29 \times 10^{57} u^{59} + \dots + 1.13 \times 10^{58} a - 3.92 \times 10^{58}, \ u^{61} - 3u^{60} + \dots - 5u + 9 \rangle$

(i) Arc colorings

$$a_{1} = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{5} = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_{2} = \begin{pmatrix} 1 \\ -u^{2} \end{pmatrix}$$

$$a_{3} = \begin{pmatrix} 0.275139u^{60} - 0.468950u^{59} + \dots + 4.47285u + 3.47366 \\ -0.132738u^{60} + 0.147340u^{59} + \dots - 4.15830u + 0.987068 \end{pmatrix}$$

$$a_{6} = \begin{pmatrix} 1.11106u^{60} - 2.61700u^{59} + \dots + 5.79571u - 5.77693 \\ -0.595122u^{60} + 2.16473u^{59} + \dots + 2.14031u + 12.7347 \end{pmatrix}$$

$$a_{7} = \begin{pmatrix} 0.302897u^{60} - 0.758393u^{59} + \dots + 2.22294u - 1.51536 \\ -0.161015u^{60} + 0.635343u^{59} + \dots + 2.73852u + 5.59822 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} 0.327154u^{60} - 0.474281u^{59} + \dots + 10.9343u + 2.92153 \\ -0.507182u^{60} + 1.24714u^{59} + \dots + 4.55730u + 2.94439 \end{pmatrix}$$

$$a_{4} = \begin{pmatrix} -u \\ u^{3} + u \end{pmatrix}$$

$$a_{8} = \begin{pmatrix} 0.849189u^{60} - 1.82096u^{59} + \dots + 7.07757u + 2.72833 \\ -0.575418u^{60} + 1.58164u^{59} + \dots - 3.44728u + 5.06368 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 0.289728u^{60} + 0.616900u^{59} + \dots + 6.66475u + 2.26231 \\ 0.0110587u^{60} - 0.250053u^{59} + \dots - 0.805308u - 1.89157 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} -0.289728u^{60} + 0.616900u^{59} + \dots + 6.66475u + 2.26231 \\ 0.0110587u^{60} - 0.250053u^{59} + \dots + 0.805308u - 1.89157 \end{pmatrix}$$

- (ii) Obstruction class = -1
- (iii) Cusp Shapes = $1.51281u^{60} 3.43786u^{59} + \cdots + 30.9340u 2.78257$

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
c_1, c_4	$u^{61} + 3u^{60} + \dots - 5u - 9$
c_2	$u^{61} + 21u^{60} + \dots - 1505u - 81$
c_3	$u^{61} - 3u^{60} + \dots - 1872u + 432$
c_5, c_9	$u^{61} - 3u^{60} + \dots + 3u - 1$
c_6	$9(9u^{61} - 30u^{60} + \dots + 293350u - 68375)$
c_7, c_{10}, c_{11}	$u^{61} - 3u^{60} + \dots + 3u - 1$
c ₈	$9(9u^{61} + 57u^{60} + \dots - 10059u - 2801)$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
c_1, c_4	$y^{61} + 21y^{60} + \dots - 1505y - 81$
c_2	$y^{61} + 41y^{60} + \dots + 37363y - 6561$
c_3	$y^{61} - 25y^{60} + \dots + 1897344y - 186624$
c_5, c_9	$y^{61} - 39y^{60} + \dots - 13y - 1$
c_6	$81(81y^{61} + 3546y^{60} + \dots - 9.00135 \times 10^{10}y - 4.67514 \times 10^{9})$
c_7, c_{10}, c_{11}	$y^{61} + 61y^{60} + \dots - 13y - 1$
c_8	$81(81y^{61} - 2259y^{60} + \dots + 1.36190 \times 10^8y - 7845601)$

(vi) Complex Volumes and Cusp Shapes

Solutions to I_1^u	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
u = 0.627295 + 0.781178I		
a = 0.779915 + 0.938460I	0.680796 - 0.488788I	8.37952 + 2.33314I
b = -0.133545 - 0.868985I		
u = 0.627295 - 0.781178I		
a = 0.779915 - 0.938460I	0.680796 + 0.488788I	8.37952 - 2.33314I
b = -0.133545 + 0.868985I		
u = -0.909616 + 0.468593I		
a = -1.059460 - 0.502224I	4.73566 - 1.67644I	12.36420 + 3.79278I
b = 1.43290 - 0.75784I		
u = -0.909616 - 0.468593I		
a = -1.059460 + 0.502224I	4.73566 + 1.67644I	12.36420 - 3.79278I
b = 1.43290 + 0.75784I		
u = 0.823832 + 0.641756I		
a = -0.493457 - 0.867597I	8.40390 - 4.08328I	6.32782 + 2.17005I
b = 0.171205 + 0.613586I		
u = 0.823832 - 0.641756I		
a = -0.493457 + 0.867597I	8.40390 + 4.08328I	6.32782 - 2.17005I
b = 0.171205 - 0.613586I		
u = 0.084826 + 0.951096I		
a = 0.768701 - 0.355562I	-3.04092 - 0.55487I	-5.63926 + 1.54785I
b = -0.926574 - 0.590119I		
u = 0.084826 - 0.951096I		
a = 0.768701 + 0.355562I	-3.04092 + 0.55487I	-5.63926 - 1.54785I
b = -0.926574 + 0.590119I		
u = 0.745313 + 0.734834I		
a = -0.69455 + 1.28009I	5.33189 - 0.62357I	6.90078 + 0.I
b = 1.59810 + 0.54771I		
u = 0.745313 - 0.734834I		
a = -0.69455 - 1.28009I	5.33189 + 0.62357I	6.90078 + 0.I
b = 1.59810 - 0.54771I		

Solutions to I_1^u	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
u = -0.592571 + 0.868966I		
a = 0.643580 + 0.821069I	2.11702 - 2.33942I	-10.06681 - 7.06956I
b = -3.23298 + 1.50658I		
u = -0.592571 - 0.868966I		
a = 0.643580 - 0.821069I	2.11702 + 2.33942I	-10.06681 + 7.06956I
b = -3.23298 - 1.50658I		
u = 0.869096 + 0.612382I		
a = 0.840207 - 1.089160I	5.98865 - 5.78069I	6.25624 + 4.52312I
b = -1.66751 - 0.62148I		
u = 0.869096 - 0.612382I		
a = 0.840207 + 1.089160I	5.98865 + 5.78069I	6.25624 - 4.52312I
b = -1.66751 + 0.62148I		
u = -0.510457 + 0.948104I		
a = 0.221723 - 0.095163I	-0.17638 - 2.59422I	0
b = -0.197711 - 0.400616I		
u = -0.510457 - 0.948104I		
a = 0.221723 + 0.095163I	-0.17638 + 2.59422I	0
b = -0.197711 + 0.400616I		
u = 0.642563 + 0.936820I		
a = -0.882906 - 0.630814I	0.17275 + 5.47510I	0
b = 0.433541 + 0.916219I		
u = 0.642563 - 0.936820I		
a = -0.882906 + 0.630814I	0.17275 - 5.47510I	0
b = 0.433541 - 0.916219I		
u = 0.318467 + 0.797607I		
a = -1.256550 + 0.401471I	-0.53178 + 3.55128I	-1.97116 + 0.53822I
b = 1.24853 + 0.72368I		
u = 0.318467 - 0.797607I		
a = -1.256550 - 0.401471I	-0.53178 - 3.55128I	-1.97116 - 0.53822I
b = 1.24853 - 0.72368I		

Solutions to I_1^u	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
u = -0.541792 + 0.666328I		
a = -0.443464 - 0.720747I	6.77383 - 1.39600I	1.94563 + 3.09396I
b = -1.80634 + 0.47653I		
u = -0.541792 - 0.666328I		
a = -0.443464 + 0.720747I	6.77383 + 1.39600I	1.94563 - 3.09396I
b = -1.80634 - 0.47653I		
u = -0.105247 + 1.136650I		
a = -0.528868 + 0.217428I	1.89473 - 3.39241I	0
b = 0.733637 + 0.607458I		
u = -0.105247 - 1.136650I		
a = -0.528868 - 0.217428I	1.89473 + 3.39241I	0
b = 0.733637 - 0.607458I		
u = -0.430215 + 0.742658I		
a = 0.120777 + 0.430167I	0.53014 - 1.40693I	5.62347 + 5.20497I
b = 0.656197 - 0.151023I		
u = -0.430215 - 0.742658I		
a = 0.120777 - 0.430167I	0.53014 + 1.40693I	5.62347 - 5.20497I
b = 0.656197 + 0.151023I		
u = 0.769003 + 0.845851I		
a = 1.196660 - 0.497619I	11.92950 + 1.96301I	0
b = -2.31477 - 0.56610I		
u = 0.769003 - 0.845851I		
a = 1.196660 + 0.497619I	11.92950 - 1.96301I	0
b = -2.31477 + 0.56610I		
u = -0.035967 + 0.854814I		
a = 0.563353 + 0.959661I	0.13425 - 1.52358I	1.52672 + 2.12846I
b = -0.057385 - 0.568156I		
u = -0.035967 - 0.854814I		
a = 0.563353 - 0.959661I	0.13425 + 1.52358I	1.52672 - 2.12846I
b = -0.057385 + 0.568156I		

Solutions to I_1^u	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
u = 0.757313 + 0.895285I		
a = 0.456980 - 1.227760I	11.77860 + 3.79247I	0
b = -1.41876 - 0.53071I		
u = 0.757313 - 0.895285I		
a = 0.456980 + 1.227760I	11.77860 - 3.79247I	0
b = -1.41876 + 0.53071I		
u = 1.008640 + 0.609371I		
a = -0.801725 + 0.933371I	13.1909 - 9.2873I	0
b = 1.70920 + 0.69780I		
u = 1.008640 - 0.609371I		
a = -0.801725 - 0.933371I	13.1909 + 9.2873I	0
b = 1.70920 - 0.69780I		
u = 0.699249 + 0.967906I		
a = -1.098020 + 0.664109I	4.62247 + 6.13062I	0
b = 2.41658 + 0.73364I		
u = 0.699249 - 0.967906I		
a = -1.098020 - 0.664109I	4.62247 - 6.13062I	0
b = 2.41658 - 0.73364I		
u = -0.312667 + 0.736573I		
a = -0.52054 - 1.36729I	6.16730 - 1.44795I	6.66665 + 4.19132I
b = -0.76632 - 2.47025I		
u = -0.312667 - 0.736573I		
a = -0.52054 + 1.36729I	6.16730 + 1.44795I	6.66665 - 4.19132I
b = -0.76632 + 2.47025I		
u = -0.141017 + 1.196910I		
a = -0.409903 - 0.838432I	-1.00556 - 4.64477I	0
b = 0.617600 + 0.023876I		
u = -0.141017 - 1.196910I		
a = -0.409903 + 0.838432I	-1.00556 + 4.64477I	0
b = 0.617600 - 0.023876I		

Solutions to I_1^u	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
u = -0.657124 + 1.017530I		
a = -0.322773 + 0.051413I	5.54533 - 3.61915I	0
b = 0.113526 + 0.695926I		
u = -0.657124 - 1.017530I		
a = -0.322773 - 0.051413I	5.54533 + 3.61915I	0
b = 0.113526 - 0.695926I		
u = 0.711728 + 1.036980I		
a = 0.745027 + 0.504667I	7.21133 + 9.84159I	0
b = -0.521745 - 0.778989I		
u = 0.711728 - 1.036980I		
a = 0.745027 - 0.504667I	7.21133 - 9.84159I	0
b = -0.521745 + 0.778989I		
u = -0.602854 + 0.415244I		
a = -0.754289 - 0.133208I	6.86257 - 1.40524I	4.78353 + 3.77219I
b = -0.631853 + 0.712874I		
u = -0.602854 - 0.415244I		
a = -0.754289 + 0.133208I	6.86257 + 1.40524I	4.78353 - 3.77219I
b = -0.631853 - 0.712874I		
u = 0.717435 + 1.062890I		
a = 0.966509 - 0.663460I	4.62032 + 11.67140I	0
b = -2.53101 - 0.75950I		
u = 0.717435 - 1.062890I		
a = 0.966509 + 0.663460I	4.62032 - 11.67140I	0
b = -2.53101 + 0.75950I		
u = -0.736476 + 1.080940I		
a = -0.590572 - 0.661323I	2.98645 - 4.33485I	0
b = 2.05889 - 0.64346I		
u = -0.736476 - 1.080940I		
a = -0.590572 + 0.661323I	2.98645 + 4.33485I	0
b = 2.05889 + 0.64346I		

Solutions to I_1^u	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
u = 0.762794 + 1.122440I		
a = -0.897935 + 0.616455I	11.5735 + 15.7181I	0
b = 2.61369 + 0.74270I		
u = 0.762794 - 1.122440I		
a = -0.897935 - 0.616455I	11.5735 - 15.7181I	0
b = 2.61369 - 0.74270I		
u = -1.265180 + 0.491129I		
a = 0.862536 + 0.296472I	11.53690 - 2.05353I	0
b = -1.81507 + 0.52494I		
u = -1.265180 - 0.491129I		
a = 0.862536 - 0.296472I	11.53690 + 2.05353I	0
b = -1.81507 - 0.52494I		
u = -0.23194 + 1.39578I		
a = 0.368146 + 0.755457I	4.72211 - 7.08106I	0
b = -0.844858 + 0.405684I		
u = -0.23194 - 1.39578I		
a = 0.368146 - 0.755457I	4.72211 + 7.08106I	0
b = -0.844858 - 0.405684I		
u = -0.91950 + 1.21328I		
a = 0.561522 + 0.564425I	9.38339 - 5.57107I	0
b = -1.88530 + 0.80608I		
u = -0.91950 - 1.21328I		
a = 0.561522 - 0.564425I	9.38339 + 5.57107I	0
b = -1.88530 - 0.80608I		
u = -0.408049		
a = 2.87652	2.58372	0.156380
b = -0.0942688		
u = 0.159087 + 0.350060I		
a = 0.83224 + 1.41611I	0.145306 - 1.198500I	1.41714 + 6.05642I
b = 0.161959 - 0.489660I		

Solutions to I_1^u	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
u = 0.159087 - 0.350060I		
a = 0.83224 - 1.41611I	0.145306 + 1.198500I	1.41714 - 6.05642I
b = 0.161959 + 0.489660I		

II.
$$I_2^u = \langle 3b + 2u - 2, \ a + 1, \ u^2 + u + 1 \rangle$$

(i) Arc colorings

a) Are colorings
$$a_{1} = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{5} = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_{2} = \begin{pmatrix} 1 \\ u+1 \end{pmatrix}$$

$$a_{3} = \begin{pmatrix} -u \\ u+1 \end{pmatrix}$$

$$a_{9} = \begin{pmatrix} -\frac{1}{2}u + \frac{2}{3} \\ -\frac{1}{3}u - \frac{2}{3} \end{pmatrix}$$

$$a_{6} = \begin{pmatrix} u \\ -\frac{1}{3}u - \frac{2}{3} \\ -u - 1 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} -u - 2 \\ -u + 1 \end{pmatrix}$$

$$a_{4} = \begin{pmatrix} -u \\ u+1 \end{pmatrix}$$

$$a_{8} = \begin{pmatrix} \frac{2}{3}u - \frac{2}{3} \\ -u \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} -\frac{1}{3}u - \frac{2}{3} \\ -u \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} -\frac{1}{3}u - \frac{2}{3} \\ -u \end{pmatrix}$$

- (ii) Obstruction class = 1
- (iii) Cusp Shapes = $8u + \frac{28}{3}$

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
$c_1, c_2, c_5 \\ c_{10}, c_{11}$	$u^2 + u + 1$
c_3	u^2
c_4, c_7, c_9	$u^2 - u + 1$
c_6, c_8	$3(3u^2 + 3u + 1)$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
c_1, c_2, c_4 c_5, c_7, c_9 c_{10}, c_{11}	$y^2 + y + 1$
<i>c</i> ₃	y^2
c_{6}, c_{8}	$9(9y^2 - 3y + 1)$

(vi) Complex Volumes and Cusp Shapes

Solutions to I_2^u	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
u = -0.500000 + 0.866025I		
a = -1.00000	-4.05977I	5.33333 + 6.92820I
b = 1.000000 - 0.577350I $u = -0.500000 - 0.866025I$		
a = -1.00000	4.05977I	5.33333 - 6.92820I
b = 1.000000 + 0.577350I		

III.
$$I_3^u = \langle 3b - 2u - 1, \ a + u, \ u^2 + u + 1 \rangle$$

(i) Arc colorings

a₁ Are colorings
$$a_1 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_2 = \begin{pmatrix} 1 \\ u+1 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} -u \\ u+1 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} \frac{2}{3}u + \frac{1}{3} \end{pmatrix}$$

$$a_6 = \begin{pmatrix} \frac{4}{3}u - \frac{1}{3} \\ \frac{4}{3}u - \frac{1}{3} \end{pmatrix}$$

$$a_7 = \begin{pmatrix} -\frac{1}{3}u + \frac{1}{3} \\ u \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} -2u - 1 \\ u+2 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} -u \\ u+1 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} -\frac{5}{3}u - \frac{1}{3} \\ u+1 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} -\frac{2}{3}u + \frac{2}{3} \\ u+1 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} -\frac{2}{3}u + \frac{2}{3} \\ u+1 \end{pmatrix}$$

- (ii) Obstruction class = 1
- (iii) Cusp Shapes = $\frac{8}{3}u + \frac{5}{3}$

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
$c_1, c_2, c_5 \\ c_{10}, c_{11}$	$u^2 + u + 1$
c_3	u^2
c_4, c_7, c_9	$u^2 - u + 1$
<i>C</i> ₆	$3(3u^2+1)$
<i>c</i> ₈	$3(3u^2 - 3u + 1)$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
c_1, c_2, c_4 c_5, c_7, c_9 c_{10}, c_{11}	$y^2 + y + 1$
<i>c</i> ₃	y^2
<i>c</i> ₆	$9(3y+1)^2$
<i>C</i> ₈	$9(9y^2 - 3y + 1)$

(vi) Complex Volumes and Cusp Shapes

Solutions to I_3^u	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
u = -0.500000 + 0.866025I		
a = 0.500000 - 0.866025I	0	0.33333 + 2.30940I
b = 0.577350I		
u = -0.500000 - 0.866025I		
a = 0.500000 + 0.866025I	0	0.33333 - 2.30940I
b = -0.577350I		

IV. u-Polynomials

Crossings	u-Polynomials at each crossing
c_1	$((u^2 + u + 1)^2)(u^{61} + 3u^{60} + \dots - 5u - 9)$
c_2	$((u^2 + u + 1)^2)(u^{61} + 21u^{60} + \dots - 1505u - 81)$
<i>C</i> ₃	$u^4(u^{61} - 3u^{60} + \dots - 1872u + 432)$
<i>C</i> ₄	$((u^2 - u + 1)^2)(u^{61} + 3u^{60} + \dots - 5u - 9)$
c_5	$((u^2 + u + 1)^2)(u^{61} - 3u^{60} + \dots + 3u - 1)$
c_6	$81(3u^2+1)(3u^2+3u+1)(9u^{61}-30u^{60}+\cdots+293350u-68375)$
c_7	$((u^2 - u + 1)^2)(u^{61} - 3u^{60} + \dots + 3u - 1)$
c_8	$81(3u^2 - 3u + 1)(3u^2 + 3u + 1)(9u^{61} + 57u^{60} + \dots - 10059u - 2801)$
c_9	$((u^2 - u + 1)^2)(u^{61} - 3u^{60} + \dots + 3u - 1)$
c_{10}, c_{11}	$((u^2 + u + 1)^2)(u^{61} - 3u^{60} + \dots + 3u - 1)$

V. Riley Polynomials

Crossings	Riley Polynomials at each crossing
c_1, c_4	$((y^2 + y + 1)^2)(y^{61} + 21y^{60} + \dots - 1505y - 81)$
c_2	$((y^2 + y + 1)^2)(y^{61} + 41y^{60} + \dots + 37363y - 6561)$
c_3	$y^4(y^{61} - 25y^{60} + \dots + 1897344y - 186624)$
c_5, c_9	$((y^2 + y + 1)^2)(y^{61} - 39y^{60} + \dots - 13y - 1)$
	$6561(3y+1)^{2}(9y^{2}-3y+1)$ $\cdot (81y^{61}+3546y^{60}+\cdots-90013453750y-4675140625)$
c_7, c_{10}, c_{11}	$((y^2 + y + 1)^2)(y^{61} + 61y^{60} + \dots - 13y - 1)$
c_8	$6561(9y^2 - 3y + 1)^2$ $\cdot (81y^{61} - 2259y^{60} + \dots + 136190379y - 7845601)$