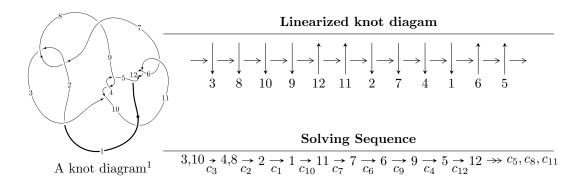
# $12a_{0752} (K12a_{0752})$



#### Ideals for irreducible components<sup>2</sup> of $X_{par}$

$$I_1^u = \langle 9.34661 \times 10^{34} u^{64} - 1.16625 \times 10^{35} u^{63} + \dots + 2.68953 \times 10^{35} b + 2.48209 \times 10^{35}, \\ -2.45811 \times 10^{33} u^{64} + 8.33232 \times 10^{33} u^{63} + \dots + 1.12064 \times 10^{34} a + 2.26849 \times 10^{34}, \ u^{65} - u^{64} + \dots + 12u - 12u$$

\* 2 irreducible components of  $\dim_{\mathbb{C}} = 0$ , with total 73 representations.

<sup>&</sup>lt;sup>1</sup>The image of knot diagram is generated by the software "**Draw programme**" developed by Andrew Bartholomew(http://www.layer8.co.uk/maths/draw/index.htm#Running-draw), where we modified some parts for our purpose(https://github.com/CATsTAILs/LinksPainter).

<sup>&</sup>lt;sup>2</sup> All coefficients of polynomials are rational numbers. But the coefficients are sometimes approximated in decimal forms when there is not enough margin.

 $\begin{matrix} \text{I.} \\ I_1^u = \langle 9.35 \times 10^{34} u^{64} - 1.17 \times 10^{35} u^{63} + \dots + 2.69 \times 10^{35} b + 2.48 \times 10^{35}, \ -2.46 \times 10^{33} u^{64} + 8.33 \times 10^{33} u^{63} + \dots + 1.12 \times 10^{34} a + 2.27 \times 10^{34}, \ u^{65} - u^{64} + \dots + 12 u - 4 \rangle \end{matrix}$ 

(i) Arc colorings

$$a_{3} = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_{4} = \begin{pmatrix} 1 \\ u^{2} \end{pmatrix}$$

$$a_{8} = \begin{pmatrix} 0.219349u^{64} - 0.743533u^{63} + \dots - 1.52002u - 2.02429 \\ -0.347518u^{64} + 0.433625u^{63} + \dots + 0.00867489u - 0.922871 \end{pmatrix}$$

$$a_{2} = \begin{pmatrix} -0.263361u^{64} + 0.721780u^{63} + \dots - 1.26586u - 4.04726 \\ -0.133396u^{64} - 0.108354u^{63} + \dots + 1.92192u - 0.715761 \end{pmatrix}$$

$$a_{1} = \begin{pmatrix} -0.396757u^{64} + 0.613426u^{63} + \dots + 0.656058u - 4.76302 \\ -0.133396u^{64} - 0.108354u^{63} + \dots + 1.92192u - 0.715761 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} -0.665779u^{64} + 1.57509u^{63} + \dots + 8.10654u - 7.87229 \\ 0.118149u^{64} - 0.522205u^{63} + \dots + 2.63479u - 0.297265 \end{pmatrix}$$

$$a_{7} = \begin{pmatrix} 0.637359u^{64} - 0.265428u^{63} + \dots + 0.870487u - 0.828079 \\ -0.193937u^{64} - 0.121331u^{63} + \dots - 2.80066u + 0.434278 \end{pmatrix}$$

$$a_{6} = \begin{pmatrix} 0.193937u^{64} + 0.511308u^{63} + \dots + 11.4864u - 2.05186 \\ 0.119417u^{64} + 0.0796398u^{63} + \dots + 2.46009u + 0.413703 \end{pmatrix}$$

$$a_{9} = \begin{pmatrix} u \\ u^{3} + u \end{pmatrix}$$

$$a_{5} = \begin{pmatrix} u \\ u^{3} + u \end{pmatrix}$$

$$a_{5} = \begin{pmatrix} u \\ u^{4} + 2u^{2} \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} -0.353724u^{64} + 0.868730u^{63} + \dots - 0.913544u - 4.49532 \\ -0.0369830u^{64} - 0.0480797u^{63} + \dots + 2.57325u - 0.708124 \end{pmatrix}$$

- (ii) Obstruction class = -1
- (iii) Cusp Shapes =  $-0.196131u^{64} + 0.795929u^{63} + \cdots + 1.11042u 13.7264$

#### (iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
$c_1, c_8$	$u^{65} + 21u^{64} + \dots - 19u + 25$
$c_{2}, c_{7}$	$u^{65} + u^{64} + \dots + 9u + 5$
$c_3, c_4, c_9$	$u^{65} + u^{64} + \dots + 12u + 4$
$c_5, c_6, c_{11}$ $c_{12}$	$u^{65} - u^{64} + \dots - 11u + 1$
$c_{10}$	$u^{65} - 15u^{64} + \dots + 14637u - 579$

#### (v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
$c_1, c_8$	$y^{65} + 51y^{64} + \dots + 23161y - 625$
$c_2, c_7$	$y^{65} - 21y^{64} + \dots - 19y - 25$
$c_3,c_4,c_9$	$y^{65} + 63y^{64} + \dots + 40y - 16$
$c_5, c_6, c_{11}$ $c_{12}$	$y^{65} + 75y^{64} + \dots + 33y - 1$
$c_{10}$	$y^{65} + 15y^{64} + \dots + 32505249y - 335241$

## (vi) Complex Volumes and Cusp Shapes

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
u = 0.102835 + 0.976475I		
a = -0.032757 + 1.095510I	1.74608 - 2.06336I	3.79758 + 4.39158I
b = -0.798701 - 0.498342I		
u = 0.102835 - 0.976475I		
a = -0.032757 - 1.095510I	1.74608 + 2.06336I	3.79758 - 4.39158I
b = -0.798701 + 0.498342I		
u = 0.906499 + 0.335695I		
a = -1.00090 + 1.11719I	-5.22317 - 9.63115I	-7.07608 + 7.08853I
b = -1.002750 - 0.732824I		
u = 0.906499 - 0.335695I		
a = -1.00090 - 1.11719I	-5.22317 + 9.63115I	-7.07608 - 7.08853I
b = -1.002750 + 0.732824I		
u = -0.863103 + 0.392575I		
a = 0.189374 + 0.143384I	-4.34155 + 3.82461I	-5.48743 - 2.35121I
b = -0.712709 - 0.812089I		
u = -0.863103 - 0.392575I		
a = 0.189374 - 0.143384I	-4.34155 - 3.82461I	-5.48743 + 2.35121I
b = -0.712709 + 0.812089I		
u = -0.646090 + 0.839750I		
a = 0.412776 + 1.185770I	-2.98842 + 1.42035I	0
b = 0.793279 - 0.769153I		
u = -0.646090 - 0.839750I		
a = 0.412776 - 1.185770I	-2.98842 - 1.42035I	0
b = 0.793279 + 0.769153I		
u = -0.622090 + 0.690604I		
a = 0.280367 + 0.412655I	2.97067 - 2.17133I	-0.55827 + 3.61156I
b = -0.850043 - 0.730237I		
u = -0.622090 - 0.690604I		
a = 0.280367 - 0.412655I	2.97067 + 2.17133I	-0.55827 - 3.61156I
b = -0.850043 + 0.730237I		

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
u = -0.810994 + 0.423522I		
a = 0.88886 + 1.24338I	2.05615 + 7.11041I	-3.69386 - 8.87039I
b = 0.957966 - 0.730403I		
u = -0.810994 - 0.423522I		
a = 0.88886 - 1.24338I	2.05615 - 7.11041I	-3.69386 + 8.87039I
b = 0.957966 + 0.730403I		
u = 0.267823 + 1.055660I		
a = -0.43521 + 1.61801I	-8.43583 + 0.53108I	0
b = -0.814658 + 0.091365I		
u = 0.267823 - 1.055660I		
a = -0.43521 - 1.61801I	-8.43583 - 0.53108I	0
b = -0.814658 - 0.091365I		
u = 0.738216 + 0.505729I		
a = -0.275387 + 0.232751I	2.62252 - 1.43772I	-1.92916 + 3.83462I
b = 0.771634 - 0.765297I		
u = 0.738216 - 0.505729I		
a = -0.275387 - 0.232751I	2.62252 + 1.43772I	-1.92916 - 3.83462I
b = 0.771634 + 0.765297I		
u = 0.685313 + 0.553849I		
a = -0.67132 + 1.35014I	2.82813 - 3.37856I	-0.87863 + 2.72445I
b = -0.896052 - 0.725197I		
u = 0.685313 - 0.553849I		
a = -0.67132 - 1.35014I	2.82813 + 3.37856I	-0.87863 - 2.72445I
b = -0.896052 + 0.725197I		
u = -0.210657 + 1.099830I		
a = 0.227640 + 1.282450I	-0.354198 + 0.463146I	0
b = 0.747845 - 0.100142I		
u = -0.210657 - 1.099830I		
a = 0.227640 - 1.282450I	-0.354198 - 0.463146I	0
b = 0.747845 + 0.100142I		

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
u = 0.634423 + 0.925822I		
a = -0.136818 + 0.495445I	-3.43259 + 4.27319I	0
b = 0.939159 - 0.735967I		
u = 0.634423 - 0.925822I		
a = -0.136818 - 0.495445I	-3.43259 - 4.27319I	0
b = 0.939159 + 0.735967I		
u = 0.696261 + 0.218895I		
a = 1.85017 + 0.05497I	-10.84640 - 4.13320I	-13.21141 + 4.39737I
b = 1.039610 + 0.156898I		
u = 0.696261 - 0.218895I		
a = 1.85017 - 0.05497I	-10.84640 + 4.13320I	-13.21141 - 4.39737I
b = 1.039610 - 0.156898I		
u = 0.042531 + 1.303050I		
a = -0.259174 + 0.846936I	2.32426 - 1.84830I	0
b = -1.051340 - 0.358180I		
u = 0.042531 - 1.303050I		
a = -0.259174 - 0.846936I	2.32426 + 1.84830I	0
b = -1.051340 + 0.358180I		
u = -0.543909 + 0.434620I		
a = -0.224764 + 0.261112I	-7.07962 + 1.85589I	-6.10075 - 3.40773I
b = -0.162639 + 0.576900I		
u = -0.543909 - 0.434620I		
a = -0.224764 - 0.261112I	-7.07962 - 1.85589I	-6.10075 + 3.40773I
b = -0.162639 - 0.576900I		
u = 0.046525 + 1.337050I	K 01000 0 F0100 F	
a = -1.26413 - 2.52442I	-5.01392 - 2.72133I	0
b = 0.872078 + 0.710596I		
u = 0.046525 - 1.337050I	K 01000 + 0 F01007	
a = -1.26413 + 2.52442I	-5.01392 + 2.72133I	0
b = 0.872078 - 0.710596I		

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
u = -0.179831 + 1.357410I		
a = 0.400953 + 0.852353I	1.60426 + 5.26138I	0
b = 1.104970 - 0.245801I		
u = -0.179831 - 1.357410I		
a = 0.400953 - 0.852353I	1.60426 - 5.26138I	0
b = 1.104970 + 0.245801I		
u = 0.129798 + 1.375160I		
a = 0.191467 + 0.722569I	-3.93915 + 0.11450I	0
b = 1.111650 - 0.471770I		
u = 0.129798 - 1.375160I		
a = 0.191467 - 0.722569I	-3.93915 - 0.11450I	0
b = 1.111650 + 0.471770I		
u = -0.589848 + 0.142876I		
a = -1.71897 + 0.20675I	-3.13502 + 2.54263I	-12.19167 - 6.47264I
b = -0.945800 + 0.132751I		
u = -0.589848 - 0.142876I		
a = -1.71897 - 0.20675I	-3.13502 - 2.54263I	-12.19167 + 6.47264I
b = -0.945800 - 0.132751I		
u = 0.26288 + 1.39636I		
a = -0.486577 + 0.820787I	-5.67735 - 7.60097I	0
b = -1.156320 - 0.188953I		
u = 0.26288 - 1.39636I		
a = -0.486577 - 0.820787I	-5.67735 + 7.60097I	0
b = -1.156320 + 0.188953I		
u = 0.05852 + 1.42211I		
a = -0.020754 + 0.973316I	5.50108 - 1.93754I	0
b = -0.067011 - 0.763857I		
u = 0.05852 - 1.42211I		
a = -0.020754 - 0.973316I	5.50108 + 1.93754I	0
b = -0.067011 + 0.763857I		
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Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
u = -0.17975 + 1.44172I		
a = 0.063972 + 0.963885I	-1.08595 + 4.44930I	0
b = 0.192321 - 0.811399I		
u = -0.17975 - 1.44172I		
a = 0.063972 - 0.963885I	-1.08595 - 4.44930I	0
b = 0.192321 + 0.811399I		
u = -0.10818 + 1.48887I		
a = 0.53625 - 1.98157I	4.95976 + 3.21067I	0
b = -0.926383 + 0.789415I		
u = -0.10818 - 1.48887I		
a = 0.53625 + 1.98157I	4.95976 - 3.21067I	0
b = -0.926383 - 0.789415I		
u = 0.499570		
a = 1.32716	-1.30268	-6.90340
b = 0.807460		
u = 0.04216 + 1.51719I		
a = 0.87256 - 1.55666I	5.21368 + 2.83714I	0
b = -0.847474 + 0.830941I		
u = 0.04216 - 1.51719I		
a = 0.87256 + 1.55666I	5.21368 - 2.83714I	0
b = -0.847474 - 0.830941I		
u = 0.35569 + 1.47673I		
a = 0.29387 - 2.00895I	0.5934 - 14.1941I	0
b = 1.050800 + 0.751869I		
u = 0.35569 - 1.47673I		
a = 0.29387 + 2.00895I	0.5934 + 14.1941I	0
b = 1.050800 - 0.751869I		
u = -0.32039 + 1.49216I		
a = -0.995709 - 0.809498I	1.74717 + 8.10835I	0
b = 0.677206 + 0.890530I		

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
u = -0.32039 - 1.49216I		
a = -0.995709 + 0.809498I	1.74717 - 8.10835I	0
b = 0.677206 - 0.890530I		
u = -0.29726 + 1.49890I		
a = -0.10605 - 2.00465I	8.28669 + 11.14520I	0
b = -1.025040 + 0.769571I		
u = -0.29726 - 1.49890I		
a = -0.10605 + 2.00465I	8.28669 - 11.14520I	0
b = -1.025040 - 0.769571I		
u = 0.22688 + 1.51321I		
a = -0.11620 - 1.98583I	9.55198 - 6.67114I	0
b = 0.991790 + 0.785678I		
u = 0.22688 - 1.51321I		
a = -0.11620 + 1.98583I	9.55198 + 6.67114I	0
b = 0.991790 - 0.785678I		
u = 0.24946 + 1.51401I		
a = 0.995693 - 0.981031I	9.21413 - 5.02177I	0
b = -0.725795 + 0.880563I		
u = 0.24946 - 1.51401I		
a = 0.995693 + 0.981031I	9.21413 + 5.02177I	0
b = -0.725795 - 0.880563I		
u = -0.17017 + 1.52793I		
a = -0.96695 - 1.18510I	10.22350 + 0.53227I	0
b = 0.776005 + 0.866492I		
u = -0.17017 - 1.52793I		
a = -0.96695 + 1.18510I	10.22350 - 0.53227I	0
b = 0.776005 - 0.866492I		
u = 0.244758 + 0.351804I		
a = 0.155281 + 0.307568I	-0.138519 - 0.946103I	-2.87476 + 7.19365I
b = 0.120495 + 0.345871I		

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
u = 0.244758 - 0.351804I		
a = 0.155281 - 0.307568I	-0.138519 + 0.946103I	-2.87476 - 7.19365I
b = 0.120495 - 0.345871I		
u = 0.282593 + 0.153006I		
a = -4.08925 - 1.68114I	-8.95062 + 1.80203I	-12.10355 - 2.75353I
b = -0.949049 + 0.506277I		
u = 0.282593 - 0.153006I		
a = -4.08925 + 1.68114I	-8.95062 - 1.80203I	-12.10355 + 2.75353I
b = -0.949049 - 0.506277I		
u = -0.180687 + 0.202078I		
a = 0.02811 + 3.86747I	-0.97228 + 2.21380I	-11.07503 - 3.04073I
b = 0.881222 - 0.565760I		
u = -0.180687 - 0.202078I		
a = 0.02811 - 3.86747I	-0.97228 - 2.21380I	-11.07503 + 3.04073I
b = 0.881222 + 0.565760I		

II. 
$$I_2^u = \langle -a^3u - 2a^2u - 3a^2 + au + 2b - 4a + 3u - 1, \ a^4 - 4a^3u + a^3 - 3a^2u - 4a^2 - 4a + 2u, \ u^2 + 1 \rangle$$

(i) Arc colorings

$$a_{3} = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_{4} = \begin{pmatrix} 1 \\ -1 \end{pmatrix}$$

$$a_{8} = \begin{pmatrix} \frac{1}{2}a^{3}u + a^{2}u + \dots + 2a + \frac{1}{2} \end{pmatrix}$$

$$a_{2} = \begin{pmatrix} -\frac{1}{2}a^{3}u - \frac{3}{2}a^{2}u + \dots - \frac{1}{2}a^{2} - \frac{1}{2}a \\ \frac{3}{2}a^{2}u + 2au + \dots + \frac{1}{2}a + \frac{1}{2} \end{pmatrix}$$

$$a_{1} = \begin{pmatrix} -\frac{1}{2}a^{3}u + \frac{3}{2}au + \dots - \frac{3}{2}a^{2} + \frac{1}{2} \\ \frac{3}{2}a^{2}u + 2au + \dots + \frac{1}{2}a + \frac{1}{2} \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} \frac{1}{2}a^{3}u - \frac{3}{2}au + \dots + \frac{3}{2}a^{2} - \frac{1}{2} \\ -a + 2u \end{pmatrix}$$

$$a_{7} = \begin{pmatrix} \frac{3}{2}a^{2}u - \frac{1}{2}u + \dots + \frac{3}{2}a + \frac{1}{2} \\ \frac{1}{2}a^{3}u + a^{2}u + \dots + 2a + \frac{1}{2} \end{pmatrix}$$

$$a_{6} = \begin{pmatrix} -\frac{3}{2}a^{2}u + \frac{1}{2}u + \dots - \frac{3}{2}a + \frac{1}{2} \\ -\frac{3}{2}a^{2}u + au + \dots - \frac{3}{2}a + \frac{1}{2} \end{pmatrix}$$

$$a_{9} = \begin{pmatrix} 0 \\ 0 \end{pmatrix}$$

$$a_{5} = \begin{pmatrix} 0 \\ -1 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} -\frac{1}{2}a^{3}u + \frac{3}{2}au + \dots + \frac{1}{2}a + 1 \end{pmatrix}$$

- (ii) Obstruction class = 1
- (iii) Cusp Shapes =  $2a^3 6a^2u + 4a^2 8au 2a 2u 10$

#### (iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
$c_1$	$(u^2 - u + 1)^4$
$c_2, c_7$	$(u^4 - u^2 + 1)^2$
$c_3, c_4, c_9$	$(u^2+1)^4$
$c_5, c_6, c_{11}$ $c_{12}$	$(u^4 + 3u^2 + 1)^2$
<i>c</i> <sub>8</sub>	$(u^2 + u + 1)^4$
$c_{10}$	$(u^2 + u - 1)^4$

## (v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
$c_1,c_8$	$(y^2 + y + 1)^4$
$c_2, c_7$	$(y^2 - y + 1)^4$
$c_3, c_4, c_9$	$(y+1)^8$
$c_5, c_6, c_{11} \\ c_{12}$	$(y^2 + 3y + 1)^4$
$c_{10}$	$(y^2 - 3y + 1)^4$

## (vi) Complex Volumes and Cusp Shapes

Solutions to $I_2^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
u = 1.000000I		
a = -0.809017 - 0.401259I	-7.23771 - 2.02988I	-6.00000 + 3.46410I
b = -0.866025 - 0.500000I		
u = 1.000000I		
a = 0.309017 + 0.464767I	0.65797 + 2.02988I	-6.00000 - 3.46410I
b = 0.866025 - 0.500000I		
u = 1.000000I		
a = 0.30902 + 1.53523I	0.65797 - 2.02988I	-6.00000 + 3.46410I
b = -0.866025 - 0.500000I		
u = 1.000000I		
a = -0.80902 + 2.40126I	-7.23771 + 2.02988I	-6.00000 - 3.46410I
b = 0.866025 - 0.500000I		
u = -1.000000I		
a = -0.809017 + 0.401259I	-7.23771 + 2.02988I	-6.00000 - 3.46410I
b = -0.866025 + 0.500000I		
u = -1.000000I		
a = 0.309017 - 0.464767I	0.65797 - 2.02988I	-6.00000 + 3.46410I
b = 0.866025 + 0.500000I		
u = -1.000000I		
a = 0.30902 - 1.53523I	0.65797 + 2.02988I	-6.00000 - 3.46410I
b = -0.866025 + 0.500000I		
u = -1.000000I		
a = -0.80902 - 2.40126I	-7.23771 - 2.02988I	-6.00000 + 3.46410I
b = 0.866025 + 0.500000I		

III. u-Polynomials

Crossings	u-Polynomials at each crossing
$c_1$	$((u^2 - u + 1)^4)(u^{65} + 21u^{64} + \dots - 19u + 25)$
$c_2, c_7$	$((u^4 - u^2 + 1)^2)(u^{65} + u^{64} + \dots + 9u + 5)$
$c_3, c_4, c_9$	$((u^2+1)^4)(u^{65}+u^{64}+\cdots+12u+4)$
$c_5, c_6, c_{11}$ $c_{12}$	$((u^4 + 3u^2 + 1)^2)(u^{65} - u^{64} + \dots - 11u + 1)$
c <sub>8</sub>	$((u^2 + u + 1)^4)(u^{65} + 21u^{64} + \dots - 19u + 25)$
$c_{10}$	$((u^2 + u - 1)^4)(u^{65} - 15u^{64} + \dots + 14637u - 579)$

IV. Riley Polynomials

Crossings	Riley Polynomials at each crossing
$c_1, c_8$	$((y^2 + y + 1)^4)(y^{65} + 51y^{64} + \dots + 23161y - 625)$
$c_2, c_7$	$((y^2 - y + 1)^4)(y^{65} - 21y^{64} + \dots - 19y - 25)$
$c_3, c_4, c_9$	$((y+1)^8)(y^{65}+63y^{64}+\cdots+40y-16)$
$c_5, c_6, c_{11}$ $c_{12}$	$((y^2+3y+1)^4)(y^{65}+75y^{64}+\cdots+33y-1)$
$c_{10}$	$((y^2 - 3y + 1)^4)(y^{65} + 15y^{64} + \dots + 3.25052 \times 10^7y - 335241)$