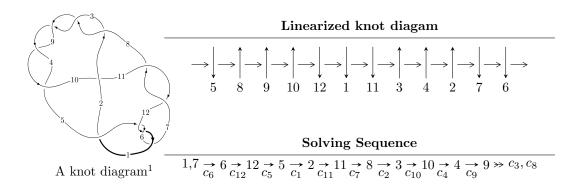
# $12a_{1276} (K12a_{1276})$



Ideals for irreducible components<sup>2</sup> of  $X_{par}$ 

$$I_1^u = \langle u^{36} - 14u^{34} + \dots - 2u + 1 \rangle$$
  
 $I_2^u = \langle u + 1 \rangle$ 

\* 2 irreducible components of  $\dim_{\mathbb{C}} = 0$ , with total 37 representations.

<sup>&</sup>lt;sup>1</sup>The image of knot diagram is generated by the software "**Draw programme**" developed by Andrew Bartholomew(http://www.layer8.co.uk/maths/draw/index.htm#Running-draw), where we modified some parts for our purpose(https://github.com/CATsTAILs/LinksPainter).

<sup>&</sup>lt;sup>2</sup> All coefficients of polynomials are rational numbers. But the coefficients are sometimes approximated in decimal forms when there is not enough margin.

I. 
$$I_1^u = \langle u^{36} - 14u^{34} + \dots - 2u + 1 \rangle$$

(i) Arc colorings

$$a_{1} = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_{7} = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{6} = \begin{pmatrix} 1 \\ -u^{2} \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} u \\ -u^{3} + u \end{pmatrix}$$

$$a_{5} = \begin{pmatrix} -u^{2} + 1 \\ u^{4} - 2u^{2} \end{pmatrix}$$

$$a_{2} = \begin{pmatrix} -u^{5} + 2u^{3} - u \\ u^{7} - 3u^{5} + 2u^{3} + u \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} -u^{3} + 2u \\ -u^{3} + u \end{pmatrix}$$

$$a_{8} = \begin{pmatrix} u^{6} - 3u^{4} + 2u^{2} + 1 \\ u^{6} - 2u^{4} + u^{2} \end{pmatrix}$$

$$a_{3} = \begin{pmatrix} u^{19} - 8u^{17} + 26u^{15} - 40u^{13} + 19u^{11} + 24u^{9} - 30u^{7} + 9u^{3} \\ u^{19} - 7u^{17} + 20u^{15} - 27u^{13} + 11u^{11} + 13u^{9} - 14u^{7} + 3u^{3} + u \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} u^{15} - 6u^{13} + 14u^{11} - 14u^{9} + 2u^{7} + 6u^{5} - 4u^{3} + 2u \\ -u^{17} + 7u^{15} - 19u^{13} + 22u^{11} - 3u^{9} - 14u^{7} + 6u^{5} + 2u^{3} + u \end{pmatrix}$$

$$a_{4} = \begin{pmatrix} u^{28} - 11u^{26} + \dots + u^{2} + 1 \\ -u^{30} + 12u^{28} + \dots + 8u^{4} - u^{2} \end{pmatrix}$$

$$a_{9} = \begin{pmatrix} -u^{32} + 13u^{30} + \dots + 2u^{2} + 1 \\ -u^{30} + 12u^{30} + \dots + 8u^{6} - 10u^{4} \end{pmatrix}$$

#### (ii) Obstruction class = -1

(iii) Cusp Shapes

$$=4u^{35} - 56u^{33} + 4u^{32} + 352u^{31} - 52u^{30} - 1276u^{29} + 300u^{28} + 2804u^{27} - 980u^{26} - 3340u^{25} + 1872u^{24} + 400u^{23} - 1720u^{22} + 5108u^{21} - 588u^{20} - 6980u^{19} + 3336u^{18} + 1544u^{17} - 2900u^{16} + 4732u^{15} - 552u^{14} - 4032u^{13} + 2344u^{12} - 448u^{11} - 840u^{10} + 1592u^{9} - 544u^{8} - 184u^{7} + 268u^{6} - 216u^{5} + 48u^{4} - 24u^{3} + 12u^{2} + 20u - 2$$

#### (iv) u-Polynomials at the component

| Crossings                     | u-Polynomials at each crossing          |
|-------------------------------|---|
| $c_1, c_7, c_{11}$            | $u^{36} + 3u^{35} + \dots - 30u - 7$    |
| $c_2, c_3, c_4$<br>$c_8, c_9$ | $u^{36} - 24u^{34} + \dots + 3u^2 + 1$  |
| $c_5, c_6, c_{12}$            | $u^{36} - 14u^{34} + \dots + 2u + 1$    |
| $c_{10}$                      | $u^{36} - 6u^{35} + \dots + 272u - 304$ |

## (v) Riley Polynomials at the component

| Crossings                     | Riley Polynomials at each crossing           |
|-------------------------------|--|
| $c_1, c_7, c_{11}$            | $y^{36} + 39y^{35} + \dots - 326y + 49$      |
| $c_2, c_3, c_4$<br>$c_8, c_9$ | $y^{36} - 48y^{35} + \dots + 6y + 1$         |
| $c_5, c_6, c_{12}$            | $y^{36} - 28y^{35} + \dots + 6y + 1$         |
| $c_{10}$                      | $y^{36} - 24y^{35} + \dots + 92000y + 92416$ |

## (vi) Complex Volumes and Cusp Shapes

| Solutions to $I_1^u$      | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape          |
|---------------------------|---------------------------------------|---------------------|
| u = 0.050369 + 0.890388I  | -18.9058 - 5.9322I                    | 9.90521 + 2.84532I  |
| u = 0.050369 - 0.890388I  | -18.9058 + 5.9322I                    | 9.90521 - 2.84532I  |
| u = -0.038390 + 0.874277I | 10.50350 + 4.44528I                   | 9.29426 - 3.93187I  |
| u = -0.038390 - 0.874277I | 10.50350 - 4.44528I                   | 9.29426 + 3.93187I  |
| u = 0.015851 + 0.853937I  | 6.10418 - 1.70405I                    | 5.05889 + 3.68915I  |
| u = 0.015851 - 0.853937I  | 6.10418 + 1.70405I                    | 5.05889 - 3.68915I  |
| u = 0.777405 + 0.185259I  | 11.28280 + 0.04041I                   | 5.42723 + 0.89925I  |
| u = 0.777405 - 0.185259I  | 11.28280 - 0.04041I                   | 5.42723 - 0.89925I  |
| u = 1.252890 + 0.044961I  | -2.90916 - 0.08413I                   | -0.68947 - 1.50895I |
| u = 1.252890 - 0.044961I  | -2.90916 + 0.08413I                   | -0.68947 + 1.50895I |
| u = -1.281930 + 0.128297I | -4.37662 + 2.52856I                   | -5.94778 - 5.32405I |
| u = -1.281930 - 0.128297I | -4.37662 - 2.52856I                   | -5.94778 + 5.32405I |
| u = 1.233580 + 0.435957I  | 16.9206 + 1.1935I                     | 6.78229 + 0.45952I  |
| u = 1.233580 - 0.435957I  | 16.9206 - 1.1935I                     | 6.78229 - 0.45952I  |
| u = -1.241030 + 0.416731I | 6.78682 + 0.17612I                    | 6.07706 + 0.51655I  |
| u = -1.241030 - 0.416731I | 6.78682 - 0.17612I                    | 6.07706 - 0.51655I  |
| u = 1.300760 + 0.181559I  | -1.26935 - 5.01630I                   | 1.24352 + 7.13074I  |
| u = 1.300760 - 0.181559I  | -1.26935 + 5.01630I                   | 1.24352 - 7.13074I  |
| u = 1.260470 + 0.393875I  | 2.24673 - 2.77191I                    | 1.60426 - 0.44575I  |
| u = 1.260470 - 0.393875I  | 2.24673 + 2.77191I                    | 1.60426 + 0.44575I  |
| u = -1.34160              | 5.39957                               | -0.485750           |
| u = -1.286130 + 0.392373I | 2.05223 + 6.17629I                    | 0.87692 - 6.64270I  |
| u = -1.286130 - 0.392373I | 2.05223 - 6.17629I                    | 0.87692 + 6.64270I  |
| u = -1.328350 + 0.209703I | 7.96118 + 6.17101I                    | 2.39842 - 5.27362I  |
| u = -1.328350 - 0.209703I | 7.96118 - 6.17101I                    | 2.39842 + 5.27362I  |
| u = 0.253274 + 0.597391I  | 12.89040 - 3.33854I                   | 8.26297 + 4.57844I  |
| u = 0.253274 - 0.597391I  | 12.89040 + 3.33854I                   | 8.26297 - 4.57844I  |
| u = 1.304210 + 0.403622I  | 6.31578 - 9.02541I                    | 5.28025 + 6.79809I  |
| u = 1.304210 - 0.403622I  | 6.31578 + 9.02541I                    | 5.28025 - 6.79809I  |
| u = -1.315470 + 0.411974I | 16.3071 + 10.5958I                    | 6.03260 - 5.51770I  |

| Solutions to $I_1^u$      | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape         |
|---------------------------|---------------------------------------|--------------------|
| u = -1.315470 - 0.411974I | 16.3071 - 10.5958I                    | 6.03260 + 5.51770I |
| u = -0.215467 + 0.524772I | 3.39035 + 2.53006I                    | 8.15428 - 6.42695I |
| u = -0.215467 - 0.524772I | 3.39035 - 2.53006I                    | 8.15428 + 6.42695I |
| u = -0.487225             | 1.85818                               | 3.26760            |
| u = 0.172360 + 0.345725I  | 0.027257 - 0.790103I                  | 0.84818 + 8.67184I |
| u = 0.172360 - 0.345725I  | 0.027257 + 0.790103I                  | 0.84818 - 8.67184I |

II. 
$$I_2^u = \langle u+1 \rangle$$

(i) Arc colorings

$$a_1 = \begin{pmatrix} 0 \\ -1 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} 1 \\ -1 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} -1\\0 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} 0 \\ -1 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} 0 \\ -1 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} -1\\0 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} -1 \\ -1 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} -1 \\ -1 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} 0 \\ -1 \end{pmatrix}$$

- (ii) Obstruction class = -1
- (iii) Cusp Shapes = 6

#### (iv) u-Polynomials at the component

| Crossings                                     | u-Polynomials at each crossing |
|---|--------------------------------|
| $c_1, c_7, c_{11}$                            | u                              |
| $c_2, c_3, c_4$ $c_5, c_6, c_8$ $c_9, c_{12}$ | u-1                            |
| $c_{10}$                                      | u+1                            |

## (v) Riley Polynomials at the component

| Crossings   | Riley Polynomials at each crossing |
|---|------------------------------------|
| $c_1, c_7, c_{11}$                                    | y                                  |
| $c_2, c_3, c_4$ $c_5, c_6, c_8$ $c_9, c_{10}, c_{12}$ | y-1                                |

## (vi) Complex Volumes and Cusp Shapes

| Solutions to $I_2^u$ | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape |
|----------------------|---------------------------------------|------------|
| u = -1.00000         | 1.64493                               | 6.00000    |

III. u-Polynomials

| Crossings                  | u-Polynomials at each crossing                 |
|----------------------------|--|
| $c_1, c_7, c_{11}$         | $u(u^{36} + 3u^{35} + \dots - 30u - 7)$        |
| $c_2, c_3, c_4 \ c_8, c_9$ | $(u-1)(u^{36} - 24u^{34} + \dots + 3u^2 + 1)$  |
| $c_5, c_6, c_{12}$         | $(u-1)(u^{36} - 14u^{34} + \dots + 2u + 1)$    |
| $c_{10}$                   | $(u+1)(u^{36} - 6u^{35} + \dots + 272u - 304)$ |

IV. Riley Polynomials

| Crossings                     | Riley Polynomials at each crossing                  |
|-------------------------------|---|
| $c_1, c_7, c_{11}$            | $y(y^{36} + 39y^{35} + \dots - 326y + 49)$          |
| $c_2, c_3, c_4$<br>$c_8, c_9$ | $(y-1)(y^{36} - 48y^{35} + \dots + 6y + 1)$         |
| $c_5, c_6, c_{12}$            | $(y-1)(y^{36}-28y^{35}+\cdots+6y+1)$                |
| $c_{10}$                      | $(y-1)(y^{36} - 24y^{35} + \dots + 92000y + 92416)$ |