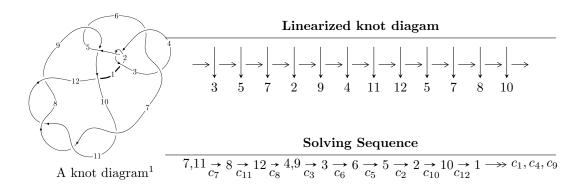
# $12n_{0105} (K12n_{0105})$



#### Ideals for irreducible components<sup>2</sup> of $X_{par}$

$$I_1^u = \langle 22873134u^{26} - 91748515u^{25} + \dots + 37746988b - 44822939,$$

$$63338341u^{26} - 295194910u^{25} + \dots + 37746988a - 66189548, \ u^{27} - 5u^{26} + \dots - 6u + 1 \rangle$$

$$I_2^u = \langle b, \ 2u^5 - u^4 - 7u^3 + u^2 + a + 5u + 4, \ u^6 - u^5 - 3u^4 + 2u^3 + 2u^2 + u - 1 \rangle$$

$$I_3^u = \langle -a^2 + b - 3a - 1, \ a^3 + 3a^2 + 2a + 1, \ u^2 + u - 1 \rangle$$

\* 3 irreducible components of  $\dim_{\mathbb{C}} = 0$ , with total 39 representations.

<sup>&</sup>lt;sup>1</sup>The image of knot diagram is generated by the software "**Draw programme**" developed by Andrew Bartholomew(http://www.layer8.co.uk/maths/draw/index.htm#Running-draw), where we modified some parts for our purpose(https://github.com/CATsTAILs/LinksPainter).

 $<sup>^2</sup>$  All coefficients of polynomials are rational numbers. But the coefficients are sometimes approximated in decimal forms when there is not enough margin.

I. 
$$I_1^u = \langle 2.29 \times 10^7 u^{26} - 9.17 \times 10^7 u^{25} + \dots + 3.77 \times 10^7 b - 4.48 \times 10^7, 6.33 \times 10^7 u^{26} - 2.95 \times 10^8 u^{25} + \dots + 3.77 \times 10^7 a - 6.62 \times 10^7, u^{27} - 5u^{26} + \dots - 6u + 1 \rangle$$

(i) Arc colorings

$$a_{7} = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_{8} = \begin{pmatrix} 1 \\ u^{2} \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} -u \\ -u^{3} + u \end{pmatrix}$$

$$a_{4} = \begin{pmatrix} -1.67797u^{26} + 7.82036u^{25} + \cdots - 8.45077u + 1.75351 \\ -0.605959u^{26} + 2.43062u^{25} + \cdots - 2.79918u + 1.18746 \end{pmatrix}$$

$$a_{9} = \begin{pmatrix} -u^{2} + 1 \\ -u^{4} + 2u^{2} \end{pmatrix}$$

$$a_{3} = \begin{pmatrix} -2.28393u^{26} + 10.2510u^{25} + \cdots - 11.2499u + 2.94096 \\ -0.605959u^{26} + 2.43062u^{25} + \cdots - 2.79918u + 1.18746 \end{pmatrix}$$

$$a_{6} = \begin{pmatrix} -0.101693u^{26} + 0.926944u^{25} + \cdots - 7.17642u + 3.14845 \\ 1.45363u^{26} - 5.69060u^{25} + \cdots + 5.80702u - 1.50691 \end{pmatrix}$$

$$a_{5} = \begin{pmatrix} 0.758454u^{26} - 2.47127u^{25} + \cdots - 3.68028u + 1.91598 \\ 0.144041u^{26} - 0.819382u^{25} + \cdots + 0.700822u - 0.562543 \end{pmatrix}$$

$$a_{2} = \begin{pmatrix} -1.05084u^{26} + 5.94352u^{25} + \cdots - 11.3894u + 3.35900 \\ -0.144041u^{26} + 0.819382u^{25} + \cdots - 0.700822u + 0.562543 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} u \\ u \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} u \\ u \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} u \\ u \end{pmatrix}$$

#### (ii) Obstruction class = -1

(iii) Cusp Shapes = 
$$-\frac{725958293}{18873494}u^{26} + \frac{3202886145}{18873494}u^{25} + \dots - \frac{5326606613}{18873494}u + \frac{1076937225}{18873494}u$$

#### (iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
$c_1$	$u^{27} + u^{26} + \dots + 514u + 1$
$c_2, c_4$	$u^{27} - 9u^{26} + \dots + 20u + 1$
$c_3, c_6$	$u^{27} - 3u^{26} + \dots + 128u + 64$
$c_5, c_9$	$u^{27} + 2u^{26} + \dots - 352u - 64$
$c_7, c_8, c_{10}$ $c_{11}$	$u^{27} + 5u^{26} + \dots - 6u - 1$
$c_{12}$	$u^{27} + u^{26} + \dots + 500u - 89$

### (v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
$c_1$	$y^{27} + 59y^{26} + \dots + 262978y - 1$
$c_2, c_4$	$y^{27} - y^{26} + \dots + 514y - 1$
$c_3, c_6$	$y^{27} + 45y^{26} + \dots + 180224y - 4096$
$c_5,c_9$	$y^{27} + 40y^{26} + \dots + 103424y - 4096$
$c_7, c_8, c_{10}$ $c_{11}$	$y^{27} - 29y^{26} + \dots - 14y - 1$
$c_{12}$	$y^{27} + 67y^{26} + \dots - 314794y - 7921$

## (vi) Complex Volumes and Cusp Shapes

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
u = -0.514269 + 0.943772I		
a = 0.96114 + 1.49139I	15.0681 - 1.4972I	-9.94344 - 0.11775I
b = -0.33697 - 2.32589I		
u = -0.514269 - 0.943772I		
a = 0.96114 - 1.49139I	15.0681 + 1.4972I	-9.94344 + 0.11775I
b = -0.33697 + 2.32589I		
u = -0.664233 + 0.874955I		
a = -1.06704 - 1.64357I	14.6013 + 7.4637I	-10.63048 - 4.31713I
b = -0.62816 + 2.16426I		
u = -0.664233 - 0.874955I		
a = -1.06704 + 1.64357I	14.6013 - 7.4637I	-10.63048 + 4.31713I
b = -0.62816 - 2.16426I		
u = -1.182480 + 0.163891I		
a = 0.485579 + 0.426627I	1.12392 + 3.54626I	-14.5183 - 3.2040I
b = 0.14520 - 1.74397I		
u = -1.182480 - 0.163891I		
a = 0.485579 - 0.426627I	1.12392 - 3.54626I	-14.5183 + 3.2040I
b = 0.14520 + 1.74397I		
u = 1.261340 + 0.096236I		
a = 0.969318 + 0.141624I	-4.50481 - 1.41612I	-14.8457 + 0.7290I
b = 0.808086 - 0.842084I		
u = 1.261340 - 0.096236I		
a = 0.969318 - 0.141624I	-4.50481 + 1.41612I	-14.8457 - 0.7290I
b = 0.808086 + 0.842084I		
u = -0.153216 + 0.715283I		
a = -0.15544 - 1.50896I	3.93766 - 0.32566I	-7.68828 - 0.01937I
b = -0.68505 + 1.29368I		
u = -0.153216 - 0.715283I		
a = -0.15544 + 1.50896I	3.93766 + 0.32566I	-7.68828 + 0.01937I
b = -0.68505 - 1.29368I		

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
u = -0.543053 + 0.346105I		
a = 0.952357 - 0.112943I	2.02138 + 3.53683I	-8.00351 - 9.60393I
b = 0.116929 - 1.071230I		
u = -0.543053 - 0.346105I		
a = 0.952357 + 0.112943I	2.02138 - 3.53683I	-8.00351 + 9.60393I
b = 0.116929 + 1.071230I		
u = 1.348160 + 0.304621I		
a = -0.990189 + 0.519594I	-0.78811 - 3.39068I	-12.00000 + 2.97054I
b = -1.27433 - 0.79621I		
u = 1.348160 - 0.304621I		
a = -0.990189 - 0.519594I	-0.78811 + 3.39068I	-12.00000 - 2.97054I
b = -1.27433 + 0.79621I		
u = 0.552139		
a = -7.52398	-2.46059	-111.160
b = -0.222467		
u = 1.53250 + 0.12438I		
a = 0.477076 + 0.429045I	-4.88486 - 5.37353I	-12.0000 + 7.7726I
b = 0.181555 + 0.768118I		
u = 1.53250 - 0.12438I		
a = 0.477076 - 0.429045I	-4.88486 + 5.37353I	-12.0000 - 7.7726I
b = 0.181555 - 0.768118I		
u = -1.55351 + 0.07692I		
a = -0.278760 + 0.128293I	-7.33821 + 0.72358I	-12.00000 + 0.I
b = 0.464875 + 0.727258I		
u = -1.55351 - 0.07692I		
a = -0.278760 - 0.128293I	-7.33821 - 0.72358I	-12.00000 + 0.I
b = 0.464875 - 0.727258I		
u = 0.440522		
a = -0.842102	-0.703245	-13.8830
b = 0.209937		

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
u = -1.60962		
a = -3.04132	-10.1232	-65.7520
b = -0.471477		
u = 1.56503 + 0.38318I		
a = 0.979548 - 0.112812I	8.39568 - 3.40964I	-12.00000 + 0.I
b = 0.04694 + 2.26665I		
u = 1.56503 - 0.38318I		
a = 0.979548 + 0.112812I	8.39568 + 3.40964I	-12.00000 + 0.I
b = 0.04694 - 2.26665I		
u = 1.61847 + 0.30353I		
a = -1.37457 + 0.38272I	7.09877 - 11.89130I	-12.00000 + 0.I
b = -0.75828 - 1.91136I		
u = 1.61847 - 0.30353I		
a = -1.37457 - 0.38272I	7.09877 + 11.89130I	-12.00000 + 0.I
b = -0.75828 + 1.91136I		
u = 0.093749 + 0.195668I		
a = -1.25531 + 1.76548I	-0.945949 + 0.075456I	-9.99859 + 1.12534I
b = 0.661199 + 0.033436I		
u = 0.093749 - 0.195668I		
a = -1.25531 - 1.76548I	-0.945949 - 0.075456I	-9.99859 - 1.12534I
b = 0.661199 - 0.033436I		

$$II. \\ I_2^u = \langle b, \ 2u^5 - u^4 - 7u^3 + u^2 + a + 5u + 4, \ u^6 - u^5 - 3u^4 + 2u^3 + 2u^2 + u - 1 \rangle$$

(i) Arc colorings

$$a_{7} = \begin{pmatrix} 1\\0 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 0\\u \end{pmatrix}$$

$$a_{8} = \begin{pmatrix} 1\\u^{2} \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} -u\\-u^{3} + u \end{pmatrix}$$

$$a_{4} = \begin{pmatrix} -2u^{5} + u^{4} + 7u^{3} - u^{2} - 5u - 4\\0 \end{pmatrix}$$

$$a_{9} = \begin{pmatrix} -u^{2} + 1\\-u^{4} + 2u^{2} \end{pmatrix}$$

$$a_{3} = \begin{pmatrix} -2u^{5} + u^{4} + 7u^{3} - u^{2} - 5u - 4\\0 \end{pmatrix}$$

$$a_{6} = \begin{pmatrix} 1\\0 \end{pmatrix}$$

$$a_{5} = \begin{pmatrix} -u^{5} + 2u^{3} + u\\-u^{5} + 3u^{3} - u \end{pmatrix}$$

$$a_{2} = \begin{pmatrix} -u^{5} + 2u^{3} + u\\-u^{5} - 3u^{3} + u \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} u\\u \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} u\\u \end{pmatrix}$$

$$a_{1} = \begin{pmatrix} u^{5} - 2u^{3} - u\\u^{5} - 3u^{3} + u \end{pmatrix}$$

- (ii) Obstruction class = 1
- (iii) Cusp Shapes =  $10u^5 6u^4 30u^3 + 5u^2 + 17u + 7u^2 + 17u + 17u$

### (iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
$c_1, c_2$	$(u-1)^6$
$c_3, c_6$	$u^6$
C4	$(u+1)^6$
<i>C</i> <sub>5</sub>	$u^6 + u^5 + 3u^4 + 2u^3 + 2u^2 + u - 1$
$c_{7}, c_{8}$	$u^6 - u^5 - 3u^4 + 2u^3 + 2u^2 + u - 1$
$c_9, c_{12}$	$u^6 - u^5 + 3u^4 - 2u^3 + 2u^2 - u - 1$
$c_{10}, c_{11}$	$u^6 + u^5 - 3u^4 - 2u^3 + 2u^2 - u - 1$

## (v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
$c_1, c_2, c_4$	$(y-1)^6$
$c_3, c_6$	$y^6$
$c_5, c_9, c_{12}$	$y^6 + 5y^5 + 9y^4 + 4y^3 - 6y^2 - 5y + 1$
$c_7, c_8, c_{10}$ $c_{11}$	$y^6 - 7y^5 + 17y^4 - 16y^3 + 6y^2 - 5y + 1$

## (vi) Complex Volumes and Cusp Shapes

Solutions to $I_2^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
u = -0.493180 + 0.575288I		
a = 0.631845 - 0.143944I	1.31531 + 1.97241I	-10.05095 - 2.83524I
b = 0		
u = -0.493180 - 0.575288I		
a = 0.631845 + 0.143944I	1.31531 - 1.97241I	-10.05095 + 2.83524I
b = 0		
u = 0.483672		
a = -5.85846	-2.38379	12.9340
b = 0		
u = 1.52087 + 0.16310I		
a = 0.453123 + 0.323434I	-5.34051 - 4.59213I	-15.4320 + 0.4465I
b = 0		
u = 1.52087 - 0.16310I		
a = 0.453123 - 0.323434I	-5.34051 + 4.59213I	-15.4320 - 0.4465I
b = 0		
u = -1.53904		
a = -1.31147	-9.30502	-17.9680
b = 0		

III. 
$$I_3^u = \langle -a^2 + b - 3a - 1, \ a^3 + 3a^2 + 2a + 1, \ u^2 + u - 1 \rangle$$

(i) Arc colorings

Are colorings
$$a_{7} = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_{8} = \begin{pmatrix} 1 \\ -u+1 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} -u \\ -u+1 \end{pmatrix}$$

$$a_{4} = \begin{pmatrix} a \\ a^{2}+3a+1 \end{pmatrix}$$

$$a_{9} = \begin{pmatrix} u \\ u \end{pmatrix}$$

$$a_{3} = \begin{pmatrix} a^{2}+4a+1 \\ a^{2}+3a+1 \end{pmatrix}$$

$$a_{6} = \begin{pmatrix} a+2 \\ a+2 \end{pmatrix}$$

$$a_{5} = \begin{pmatrix} a+2 \\ a+2 \end{pmatrix}$$

$$a_{2} = \begin{pmatrix} 2a+2 \\ a+2 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} u \\ u \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} -1 \\ 0 \end{pmatrix}$$

- (ii) Obstruction class = 1
- (iii) Cusp Shapes =  $-a^2u + 3au + a + 3u 9$

### (iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
$c_1, c_3$	$(u^3 - u^2 + 2u - 1)^2$
$c_2$	$(u^3 + u^2 - 1)^2$
$c_4$	$(u^3 - u^2 + 1)^2$
$c_5, c_9$	$u^6$
<i>C</i> <sub>6</sub>	$(u^3 + u^2 + 2u + 1)^2$
$c_{7}, c_{8}$	$(u^2+u-1)^3$
$c_{10}, c_{11}, c_{12}$	$(u^2 - u - 1)^3$

## (v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
$c_1, c_3, c_6$	$(y^3 + 3y^2 + 2y - 1)^2$
$c_2, c_4$	$(y^3 - y^2 + 2y - 1)^2$
$c_{5}, c_{9}$	$y^6$
$c_7, c_8, c_{10} \\ c_{11}, c_{12}$	$(y^2 - 3y + 1)^3$

## (vi) Complex Volumes and Cusp Shapes

Solutions to $I_3^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
u = 0.618034		
a = -0.337641 + 0.562280I	2.03717 + 2.82812I	-7.98462 + 1.83947I
b = -0.215080 + 1.307140I		
u = 0.618034		
a = -0.337641 - 0.562280I	2.03717 - 2.82812I	-7.98462 - 1.83947I
b = -0.215080 - 1.307140I		
u = 0.618034		
a = -2.32472	-2.10041	-17.1210
b = -0.569840		
u = -1.61803		
a = -0.337641 + 0.562280I	-5.85852 + 2.82812I	-12.87990 - 2.78145I
b = -0.215080 + 1.307140I		
u = -1.61803		
a = -0.337641 - 0.562280I	-5.85852 - 2.82812I	-12.87990 + 2.78145I
b = -0.215080 - 1.307140I		
u = -1.61803		
a = -2.32472	-9.99610	3.85000
b = -0.569840		

IV. u-Polynomials

Crossings	u-Polynomials at each crossing
$c_1$	$((u-1)^6)(u^3-u^2+2u-1)^2(u^{27}+u^{26}+\cdots+514u+1)$
$c_2$	$((u-1)^6)(u^3+u^2-1)^2(u^{27}-9u^{26}+\cdots+20u+1)$
<i>c</i> <sub>3</sub>	$u^{6}(u^{3} - u^{2} + 2u - 1)^{2}(u^{27} - 3u^{26} + \dots + 128u + 64)$
C <sub>4</sub>	$((u+1)^6)(u^3-u^2+1)^2(u^{27}-9u^{26}+\cdots+20u+1)$
<i>C</i> <sub>5</sub>	$u^{6}(u^{6} + u^{5} + \dots + u - 1)(u^{27} + 2u^{26} + \dots - 352u - 64)$
<i>c</i> <sub>6</sub>	$u^{6}(u^{3} + u^{2} + 2u + 1)^{2}(u^{27} - 3u^{26} + \dots + 128u + 64)$
$c_7, c_8$	$(u^{2} + u - 1)^{3}(u^{6} - u^{5} - 3u^{4} + 2u^{3} + 2u^{2} + u - 1)$ $\cdot (u^{27} + 5u^{26} + \dots - 6u - 1)$
<i>c</i> <sub>9</sub>	$u^{6}(u^{6} - u^{5} + \dots - u - 1)(u^{27} + 2u^{26} + \dots - 352u - 64)$
$c_{10}, c_{11}$	$(u^{2} - u - 1)^{3}(u^{6} + u^{5} - 3u^{4} - 2u^{3} + 2u^{2} - u - 1)$ $\cdot (u^{27} + 5u^{26} + \dots - 6u - 1)$
$c_{12}$	$(u^{2} - u - 1)^{3}(u^{6} - u^{5} + 3u^{4} - 2u^{3} + 2u^{2} - u - 1)$ $\cdot (u^{27} + u^{26} + \dots + 500u - 89)$

### V. Riley Polynomials

Crossings	Riley Polynomials at each crossing
$c_1$	$((y-1)^6)(y^3+3y^2+2y-1)^2(y^{27}+59y^{26}+\cdots+262978y-1)$
$c_2, c_4$	$((y-1)^6)(y^3-y^2+2y-1)^2(y^{27}-y^{26}+\cdots+514y-1)$
$c_3, c_6$	$y^{6}(y^{3} + 3y^{2} + 2y - 1)^{2}(y^{27} + 45y^{26} + \dots + 180224y - 4096)$
$c_5,c_9$	$y^{6}(y^{6} + 5y^{5} + 9y^{4} + 4y^{3} - 6y^{2} - 5y + 1)$ $\cdot (y^{27} + 40y^{26} + \dots + 103424y - 4096)$
$c_7, c_8, c_{10}$ $c_{11}$	$(y^{2} - 3y + 1)^{3}(y^{6} - 7y^{5} + 17y^{4} - 16y^{3} + 6y^{2} - 5y + 1)$ $\cdot (y^{27} - 29y^{26} + \dots - 14y - 1)$
$c_{12}$	$(y^2 - 3y + 1)^3(y^6 + 5y^5 + 9y^4 + 4y^3 - 6y^2 - 5y + 1)$ $\cdot (y^{27} + 67y^{26} + \dots - 314794y - 7921)$