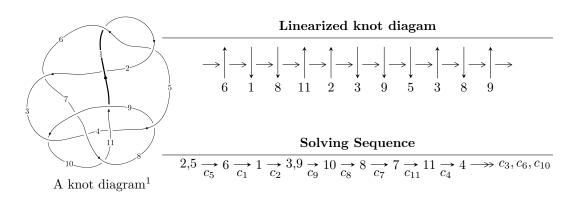
# $11n_{85} (K11n_{85})$



#### Ideals for irreducible components<sup>2</sup> of $X_{par}$

$$I_1^u = \langle -2u^{22} - 2u^{21} + \dots + 4b - 2, \ 2u^{22} + u^{21} + \dots + 4a - 2, \ u^{23} + 2u^{22} + \dots + 4u + 2 \rangle$$

$$I_2^u = \langle b + 1, \ u^3 + 2u^2 + 2a + 4, \ u^4 + 2u^2 + 2 \rangle$$

$$I_3^u = \langle -a^2u + 2b + a - 2, \ a^3 + 2a^2u - au + 2a + 2, \ u^2 - u + 1 \rangle$$

$$I_1^v = \langle a, \ b - 1, \ v - 1 \rangle$$

\* 4 irreducible components of  $\dim_{\mathbb{C}} = 0$ , with total 34 representations.

<sup>&</sup>lt;sup>1</sup>The image of knot diagram is generated by the software "**Draw programme**" developed by Andrew Bartholomew(http://www.layer8.co.uk/maths/draw/index.htm#Running-draw), where we modified some parts for our purpose(https://github.com/CATsTAILs/LinksPainter).

<sup>&</sup>lt;sup>2</sup> All coefficients of polynomials are rational numbers. But the coefficients are sometimes approximated in decimal forms when there is not enough margin.

$$I_1^u = \langle -2u^{22} - 2u^{21} + \dots + 4b - 2, \ 2u^{22} + u^{21} + \dots + 4a - 2, \ u^{23} + 2u^{22} + \dots + 4u + 2 \rangle$$

$$a_{2} = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_{5} = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{6} = \begin{pmatrix} 1 \\ -u^{2} \end{pmatrix}$$

$$a_{1} = \begin{pmatrix} -u \\ u^{3} + u \end{pmatrix}$$

$$a_{3} = \begin{pmatrix} -\frac{1}{2}u^{22} - \frac{1}{4}u^{21} + \dots - \frac{1}{2}u + \frac{1}{2} \\ \frac{1}{2}u^{22} + \frac{1}{2}u^{21} + \dots + \frac{1}{2}u + \frac{1}{2} \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} -\frac{1}{4}u^{18} - u^{16} + \dots + \frac{1}{2}u + \frac{1}{2} \\ -\frac{1}{2}u^{13} - \frac{3}{2}u^{11} + \dots - u^{3} - u \end{pmatrix}$$

$$a_{8} = \begin{pmatrix} \frac{1}{4}u^{21} + u^{19} + \dots - \frac{1}{2}u^{3} + 1 \\ \frac{1}{2}u^{22} + \frac{1}{2}u^{21} + \dots + \frac{1}{2}u + \frac{1}{2} \end{pmatrix}$$

$$a_{7} = \begin{pmatrix} -u^{6} - u^{4} + 1 \\ u^{8} + 2u^{6} + 2u^{4} \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} \frac{1}{2}u^{22} + \frac{3}{4}u^{21} + \dots - \frac{1}{2}u - \frac{1}{2} \\ \frac{1}{2}u^{22} + \frac{1}{2}u^{21} + \dots + \frac{3}{2}u + \frac{1}{2} \end{pmatrix}$$

$$a_{4} = \begin{pmatrix} -\frac{1}{4}u^{21} - u^{19} + \dots - \frac{3}{2}u^{3} - u \\ -\frac{1}{4}u^{21} - \frac{5}{4}u^{19} + \dots + \frac{1}{2}u^{2} + \frac{1}{2}u \end{pmatrix}$$

$$a_{4} = \begin{pmatrix} -\frac{1}{4}u^{21} - u^{19} + \dots - \frac{3}{2}u^{3} - u \\ -\frac{1}{4}u^{21} - \frac{5}{4}u^{19} + \dots + \frac{1}{2}u^{2} + \frac{1}{2}u \end{pmatrix}$$

#### (ii) Obstruction class = -1

(iii) Cusp Shapes = 
$$2u^{22} + 4u^{21} + 10u^{20} + 16u^{19} + 24u^{18} + 34u^{17} + 30u^{16} + 40u^{15} + 16u^{14} + 30u^{13} + 32u^{11} + 8u^{10} + 46u^{9} + 14u^{8} + 42u^{7} - 8u^{6} + 2u^{5} - 24u^{4} + 2u^{3} + 4u^{2} + 10u^{10} + 10u^$$

Crossings	u-Polynomials at each crossing
$c_1, c_5$	$u^{23} + 2u^{22} + \dots + 4u + 2$
$c_2$	$u^{23} + 10u^{22} + \dots + 8u - 4$
$c_3$	$u^{23} + 27u^{21} + \dots - 7u + 1$
$c_4, c_9$	$u^{23} - 2u^{22} + \dots + 9u + 1$
	$u^{23} - 2u^{22} + \dots - 88u + 16$
	$u^{23} + 2u^{22} + \dots - 11u + 1$
<i>c</i> <sub>8</sub>	$u^{23} + 2u^{22} + \dots - 3u + 1$
$c_{10}$	$u^{23} - 5u^{22} + \dots + 128u + 1706$
$c_{11}$	$u^{23} + 8u^{22} + \dots + 1035u + 297$

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
u = 0.887093 + 0.448454I		
a = 0.492271 + 1.285580I	11.55830 - 6.04378I	2.90457 + 2.40956I
b = -1.14839 - 1.01565I		
u = 0.887093 - 0.448454I		
a = 0.492271 - 1.285580I	11.55830 + 6.04378I	2.90457 - 2.40956I
b = -1.14839 + 1.01565I		
u = -0.865908 + 0.562605I		
a = 0.29789 + 1.55245I	12.26940 - 1.86843I	3.51927 + 2.09858I
b = -0.94225 - 1.16788I		
u = -0.865908 - 0.562605I		
a = 0.29789 - 1.55245I	12.26940 + 1.86843I	3.51927 - 2.09858I
b = -0.94225 + 1.16788I		
u = -0.126252 + 0.927958I		
a = 0.472434 + 0.373694I	-1.83455 + 1.28121I	-6.39377 - 3.70883I
b = 0.816023 - 0.401741I		
u = -0.126252 - 0.927958I		
a = 0.472434 - 0.373694I	-1.83455 - 1.28121I	-6.39377 + 3.70883I
b = 0.816023 + 0.401741I		
u = -0.687410 + 0.551797I		
a = 0.93433 - 1.33726I	2.63493 + 2.12803I	3.22069 - 2.55962I
b = -0.566101 + 0.784858I		
u = -0.687410 - 0.551797I		
a = 0.93433 + 1.33726I	2.63493 - 2.12803I	3.22069 + 2.55962I
b = -0.566101 - 0.784858I		
u = -0.439313 + 1.087580I		
a = -1.12704 + 1.03997I	-4.16811 - 3.61856I	-9.97032 + 4.29272I
b = -1.028740 - 0.075248I		
u = -0.439313 - 1.087580I		
a = -1.12704 - 1.03997I	-4.16811 + 3.61856I	-9.97032 - 4.29272I
b = -1.028740 + 0.075248I		

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
u = -0.611535 + 1.029680I		
a = 0.57884 - 1.78933I	1.22653 - 7.16348I	-0.15345 + 7.54828I
b = 0.744103 + 0.840632I		
u = -0.611535 - 1.029680I		
a = 0.57884 + 1.78933I	1.22653 + 7.16348I	-0.15345 - 7.54828I
b = 0.744103 - 0.840632I		
u = 0.470162 + 1.125140I		
a = -1.139790 - 0.221923I	-0.75408 + 3.78076I	1.64329 - 3.83078I
b = -0.174623 + 0.267387I		
u = 0.470162 - 1.125140I		
a = -1.139790 + 0.221923I	-0.75408 - 3.78076I	1.64329 + 3.83078I
b = -0.174623 - 0.267387I		
u = 0.066964 + 1.228960I		
a = 0.900031 + 0.128011I	5.54974 - 3.50228I	-1.93120 + 2.15966I
b = 0.988654 + 0.944921I		
u = 0.066964 - 1.228960I		
a = 0.900031 - 0.128011I	5.54974 + 3.50228I	-1.93120 - 2.15966I
b = 0.988654 - 0.944921I		
u = -0.694097 + 1.072020I		
a = -1.125380 + 0.108515I	10.72870 - 3.91001I	1.79235 + 2.50229I
b = 0.83601 - 1.20931I		
u = -0.694097 - 1.072020I		
a = -1.125380 - 0.108515I	10.72870 + 3.91001I	1.79235 - 2.50229I
b = 0.83601 + 1.20931I		
u = 0.652491 + 1.132530I		
a = 1.13140 + 1.85064I	9.4833 + 11.7267I	0.34491 - 6.55767I
b = 1.20493 - 0.95597I		
u = 0.652491 - 1.132530I		
a = 1.13140 - 1.85064I	9.4833 - 11.7267I	0.34491 + 6.55767I
b = 1.20493 + 0.95597I		

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
u = 0.601530 + 0.285314I		
a = 1.041030 - 0.706848I	1.74084 + 0.44680I	5.28361 - 1.38333I
b = -0.179556 + 0.418301I		
u = 0.601530 - 0.285314I		
a = 1.041030 + 0.706848I	1.74084 - 0.44680I	5.28361 + 1.38333I
b = -0.179556 - 0.418301I		
u = -0.507450		
a = 0.0879637	-1.46388	-6.51990
b = 0.899884		

II. 
$$I_2^u = \langle b+1, \ u^3+2u^2+2a+4, \ u^4+2u^2+2 \rangle$$

$$a_{2} = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_{5} = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{6} = \begin{pmatrix} 1 \\ -u^{2} \end{pmatrix}$$

$$a_{1} = \begin{pmatrix} -u \\ u^{3} + u \end{pmatrix}$$

$$a_{3} = \begin{pmatrix} -u^{3} \\ -u^{3} - u \end{pmatrix}$$

$$a_{9} = \begin{pmatrix} -\frac{1}{2}u^{3} - u^{2} - 2 \\ -1 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} \frac{1}{2}u^{3} - u^{2} - 2 \\ u^{3} + u - 1 \end{pmatrix}$$

$$a_{8} = \begin{pmatrix} -\frac{1}{2}u^{3} - u^{2} - 3 \\ -1 \end{pmatrix}$$

$$a_{7} = \begin{pmatrix} -1 \\ 0 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} -\frac{3}{2}u^{3} - u^{2} - u - 3 \\ -1 \end{pmatrix}$$

$$a_{4} = \begin{pmatrix} \frac{3}{2}u^{3} + u^{2} + u + 4 \\ 1 \end{pmatrix}$$

$$a_{4} = \begin{pmatrix} \frac{3}{2}u^{3} + u^{2} + u + 4 \\ 1 \end{pmatrix}$$

- (ii) Obstruction class = 1
- (iii) Cusp Shapes =  $-4u^2 8$

Crossings	u-Polynomials at each crossing
$c_1,c_5$	$u^4 + 2u^2 + 2$
$c_2$	$(u^2 + 2u + 2)^2$
$c_3$	$u^4 + 4u^3 + 4u^2 + 1$
$c_4$	$(u+1)^4$
$c_6, c_{10}$	$u^4 - 2u^2 + 2$
$c_7, c_8, c_9$	$(u-1)^4$
$c_{11}$	$u^4 - 4u^3 + 4u^2 + 1$

Crossings	Riley Polynomials at each crossing
$c_1, c_5$	$(y^2 + 2y + 2)^2$
$c_2$	$(y^2+4)^2$
$c_3,c_{11}$	$y^4 - 8y^3 + 18y^2 + 8y + 1$
$c_4, c_7, c_8$ $c_9$	$(y-1)^4$
$c_6, c_{10}$	$(y^2 - 2y + 2)^2$

Solutions to $I_2^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
u = 0.455090 + 1.098680I		
a = -0.223113 - 0.678203I	-2.46740 + 3.66386I	-4.00000 - 4.00000I
b = -1.00000		
u = 0.455090 - 1.098680I		
a = -0.223113 + 0.678203I	-2.46740 - 3.66386I	-4.00000 + 4.00000I
b = -1.00000		
u = -0.455090 + 1.098680I		
a = -1.77689 + 1.32180I	-2.46740 - 3.66386I	-4.00000 + 4.00000I
b = -1.00000		
u = -0.455090 - 1.098680I		
a = -1.77689 - 1.32180I	-2.46740 + 3.66386I	-4.00000 - 4.00000I
b = -1.00000		

III. 
$$I_3^u = \langle -a^2u + 2b + a - 2, \ a^3 + 2a^2u - au + 2a + 2, \ u^2 - u + 1 \rangle$$

$$a_{2} = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_{5} = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{6} = \begin{pmatrix} 1 \\ -u+1 \end{pmatrix}$$

$$a_{1} = \begin{pmatrix} -u \\ u-1 \end{pmatrix}$$

$$a_{3} = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{9} = \begin{pmatrix} \frac{1}{2}a^{2}u - \frac{1}{2}a + 1 \\ \frac{1}{2}a^{2}u - \frac{1}{2}a + 1 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} \frac{1}{2}a^{2}u + \frac{1}{2}a + 1 \\ \frac{1}{2}a^{2}u - \frac{1}{2}a + 1 \end{pmatrix}$$

$$a_{8} = \begin{pmatrix} \frac{1}{2}a^{2}u + \frac{1}{2}a + 1 \\ \frac{1}{2}a^{2}u - \frac{1}{2}a + 1 \end{pmatrix}$$

$$a_{7} = \begin{pmatrix} u \\ -u+1 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} -\frac{1}{2}a^{2}u - \frac{1}{2}a + 1 \\ -\frac{1}{2}a^{2}u + \frac{1}{2}a - 1 \end{pmatrix}$$

$$a_{4} = \begin{pmatrix} -\frac{1}{2}a^{2}u - \frac{1}{2}a + 1 \\ \frac{1}{2}a^{2}u - \frac{1}{2}a^{2} + \frac{1}{2}au - a + u \end{pmatrix}$$

$$a_{4} = \begin{pmatrix} -\frac{1}{2}a^{2}u - \frac{1}{2}a + 1 \\ \frac{1}{2}a^{2}u - \frac{1}{2}a^{2} + \frac{1}{2}au - a + u \end{pmatrix}$$

- (ii) Obstruction class = -1
- (iii) Cusp Shapes = -4u + 2

Crossings	u-Polynomials at each crossing
$c_1, c_5$	$(u^2 - u + 1)^3$
$c_2, c_6$	$(u^2+u+1)^3$
$c_3, c_4, c_8$ $c_9$	$u^6 - 2u^4 - u^3 + u^2 + u + 1$
$c_7$	$u^6 + 4u^5 + 6u^4 + 3u^3 - u^2 - u + 1$
$c_{10}$	$u^6$
$c_{11}$	$u^6 - 4u^5 + 6u^4 - 3u^3 - u^2 + u + 1$

Crossings	Riley Polynomials at each crossing
$c_1, c_2, c_5$ $c_6$	$(y^2+y+1)^3$
$c_3, c_4, c_8$ $c_9$	$y^6 - 4y^5 + 6y^4 - 3y^3 - y^2 + y + 1$
$c_7, c_{11}$	$y^6 - 4y^5 + 10y^4 - 11y^3 + 19y^2 - 3y + 1$
$c_{10}$	$y^6$

Solutions to $I_3^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
u = 0.500000 + 0.866025I $a = 0.412728 + 1.011420I$ $b = 0.218964 - 0.666188I$	2.02988 <i>I</i>	0 3.46410I
u = 0.500000 + 0.866025I $a = -0.562490 - 0.528127I$ $b = 1.033350 + 0.428825I$	2.02988I	0 3.46410I
u = 0.500000 + 0.866025I $a = -0.85024 - 2.21534I$ $b = -1.252310 + 0.237364I$	2.02988I	0 3.46410I
u = 0.500000 - 0.866025I $a = 0.412728 - 1.011420I$ $b = 0.218964 + 0.666188I$	-2.02988I	0. + 3.46410I
u = 0.500000 - 0.866025I $a = -0.562490 + 0.528127I$ $b = 1.033350 - 0.428825I$	-2.02988I	0. + 3.46410I
u = 0.500000 - 0.866025I $a = -0.85024 + 2.21534I$ $b = -1.252310 - 0.237364I$	-2.02988I	0. + 3.46410I

IV. 
$$I_1^v = \langle a, \ b-1, \ v-1 \rangle$$

$$a_2 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} 0 \\ 1 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} 1 \\ 1 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} 1 \\ 1 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 1 \\ 1 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} 2 \\ 1 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} 2 \\ 1 \end{pmatrix}$$

- (ii) Obstruction class = 1
- (iii) Cusp Shapes = 0

Crossings	u-Polynomials at each crossing
$c_1, c_2, c_5 \\ c_6, c_{10}$	u
$c_3, c_4, c_7$ $c_{11}$	u-1
$c_8, c_9$	u+1

Crossings	Riley Polynomials at each crossing
$c_1, c_2, c_5$ $c_6, c_{10}$	y
$c_3, c_4, c_7$ $c_8, c_9, c_{11}$	y-1

Solutions to $I_1^v$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
v = 1.00000		
a = 0	0	0
b = 1.00000		

#### V. u-Polynomials

Crossings	u-Polynomials at each crossing
$c_1,c_5$	$u(u^{2} - u + 1)^{3}(u^{4} + 2u^{2} + 2)(u^{23} + 2u^{22} + \dots + 4u + 2)$
$c_2$	$u(u^{2} + u + 1)^{3}(u^{2} + 2u + 2)^{2}(u^{23} + 10u^{22} + \dots + 8u - 4)$
$c_3$	$(u-1)(u^4 + 4u^3 + 4u^2 + 1)(u^6 - 2u^4 - u^3 + u^2 + u + 1)$ $\cdot (u^{23} + 27u^{21} + \dots - 7u + 1)$
C4	$(u-1)(u+1)^4(u^6-2u^4+\cdots+u+1)(u^{23}-2u^{22}+\cdots+9u+1)$
<i>C</i> <sub>6</sub>	$u(u^{2} + u + 1)^{3}(u^{4} - 2u^{2} + 2)(u^{23} - 2u^{22} + \dots - 88u + 16)$
$c_7$	$((u-1)^5)(u^6+4u^5+\cdots-u+1)(u^{23}+2u^{22}+\cdots-11u+1)$
<i>c</i> <sub>8</sub>	$((u-1)^4)(u+1)(u^6-2u^4+\cdots+u+1)(u^{23}+2u^{22}+\cdots-3u+1)$
<i>C</i> 9	$((u-1)^4)(u+1)(u^6-2u^4+\cdots+u+1)(u^{23}-2u^{22}+\cdots+9u+1)$
$c_{10}$	$u^{7}(u^{4} - 2u^{2} + 2)(u^{23} - 5u^{22} + \dots + 128u + 1706)$
$c_{11}$	$(u-1)(u^4 - 4u^3 + 4u^2 + 1)(u^6 - 4u^5 + 6u^4 - 3u^3 - u^2 + u + 1)$ $\cdot (u^{23} + 8u^{22} + \dots + 1035u + 297)$

### VI. Riley Polynomials

Crossings	Riley Polynomials at each crossing
$c_1,c_5$	$y(y^{2} + y + 1)^{3}(y^{2} + 2y + 2)^{2}(y^{23} + 10y^{22} + \dots + 8y - 4)$
$c_2$	$y(y^2+4)^2(y^2+y+1)^3(y^{23}+6y^{22}+\cdots+160y-16)$
$c_3$	$(y-1)(y^4 - 8y^3 + \dots + 8y + 1)(y^6 - 4y^5 + \dots + y + 1)$ $\cdot (y^{23} + 54y^{22} + \dots + 25y - 1)$
$c_4, c_9$	$(y-1)^{5}(y^{6} - 4y^{5} + 6y^{4} - 3y^{3} - y^{2} + y + 1)$ $\cdot (y^{23} - 34y^{22} + \dots - 27y - 1)$
$c_6$	$y(y^{2}-2y+2)^{2}(y^{2}+y+1)^{3}(y^{23}+2y^{22}+\cdots+960y-256)$
<i>C</i> <sub>7</sub>	$(y-1)^{5}(y^{6} - 4y^{5} + 10y^{4} - 11y^{3} + 19y^{2} - 3y + 1)$ $\cdot (y^{23} + 46y^{22} + \dots - 135y - 1)$
$c_8$	$((y-1)^5)(y^6-4y^5+\cdots+y+1)(y^{23}-2y^{22}+\cdots-11y-1)$
$c_{10}$	$y^{7}(y^{2}-2y+2)^{2}(y^{23}+41y^{22}+\cdots-1.22873\times10^{7}y-2910436)$
$c_{11}$	$(y-1)(y^4 - 8y^3 + 18y^2 + 8y + 1)$ $\cdot (y^6 - 4y^5 + 10y^4 - 11y^3 + 19y^2 - 3y + 1)$ $\cdot (y^{23} - 26y^{22} + \dots + 935793y - 88209)$