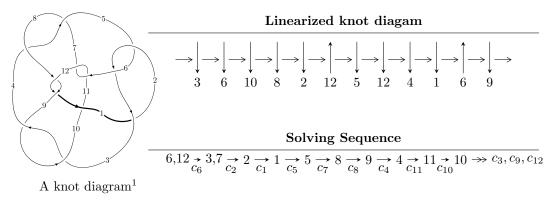
# $12n_{0515} \ (K12n_{0515})$



#### Ideals for irreducible components<sup>2</sup> of $X_{par}$

$$\begin{split} I_1^u &= \langle 8.22266 \times 10^{274} u^{59} - 2.15506 \times 10^{275} u^{58} + \dots + 2.34069 \times 10^{278} b - 6.04308 \times 10^{278}, \\ &1.35060 \times 10^{279} u^{59} - 3.78638 \times 10^{279} u^{58} + \dots + 8.33051 \times 10^{281} a - 1.96121 \times 10^{283}, \\ &u^{60} - 3 u^{59} + \dots - 11482 u + 3559 \rangle \\ I_2^u &= \langle -14967763 u^{15} - 2907851 u^{14} + \dots + 25980989 b + 31360586, \\ &50615010 u^{15} + 19279984 u^{14} + \dots + 25980989 a - 107875259, \\ &u^{16} + 2 u^{14} - 4 u^{13} - 6 u^{12} - 4 u^{11} + 5 u^{10} + 8 u^9 + 28 u^8 - 32 u^7 + 25 u^6 - 51 u^5 + 36 u^4 - 15 u^3 + 13 u^2 - 6 u + 1 u^8 + 12 u^8$$

\* 2 irreducible components of  $\dim_{\mathbb{C}} = 0$ , with total 76 representations.

<sup>&</sup>lt;sup>1</sup>The image of knot diagram is generated by the software "**Draw programme**" developed by Andrew Bartholomew(http://www.layer8.co.uk/maths/draw/index.htm#Running-draw), where we modified some parts for our purpose(https://github.com/CATsTAILs/LinksPainter).

 $<sup>^2</sup>$  All coefficients of polynomials are rational numbers. But the coefficients are sometimes approximated in decimal forms when there is not enough margin.

I. 
$$I_1^u = \langle 8.22 \times 10^{274} u^{59} - 2.16 \times 10^{275} u^{58} + \dots + 2.34 \times 10^{278} b - 6.04 \times 10^{278}, \ 1.35 \times 10^{279} u^{59} - 3.79 \times 10^{279} u^{58} + \dots + 8.33 \times 10^{281} a - 1.96 \times 10^{283}, \ u^{60} - 3u^{59} + \dots - 11482u + 3559 \rangle$$

(i) Arc colorings

$$a_{12} = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_{3} = \begin{pmatrix} -0.00162127u^{59} + 0.00454519u^{58} + \dots + 14.3091u + 23.5425 \\ -0.000351292u^{59} + 0.000920694u^{58} + \dots - 5.50751u + 2.58176 \end{pmatrix}$$

$$a_{7} = \begin{pmatrix} 1 \\ -u^{2} \end{pmatrix}$$

$$a_{2} = \begin{pmatrix} -0.00197256u^{59} + 0.00546589u^{58} + \dots + 8.80155u + 26.1243 \\ -0.000351292u^{59} + 0.000920694u^{58} + \dots - 5.50751u + 2.58176 \end{pmatrix}$$

$$a_{1} = \begin{pmatrix} -0.000985855u^{59} + 0.00264770u^{58} + \dots - 12.7756u + 10.9512 \\ 0.0000228831u^{59} - 0.000129239u^{58} + \dots - 3.83757u - 1.50813 \end{pmatrix}$$

$$a_{5} = \begin{pmatrix} -0.00191681u^{59} + 0.00522142u^{58} + \dots + 7.64525u + 28.4871 \\ -0.000498029u^{59} + 0.00130545u^{58} + \dots - 1.84746u + 4.50416 \end{pmatrix}$$

$$a_{8} = \begin{pmatrix} -0.00166805u^{59} + 0.00435306u^{58} + \dots - 14.8874u + 11.7806 \\ 0.000432015u^{59} - 0.00114140u^{58} + \dots - 0.328575u - 5.15749 \end{pmatrix}$$

$$a_{9} = \begin{pmatrix} -0.00166805u^{59} + 0.00435306u^{58} + \dots - 14.8874u + 11.7806 \\ 0.000199584u^{59} - 0.000435306u^{58} + \dots - 14.8874u + 11.7806 \\ 0.000199584u^{59} - 0.000526762u^{58} + \dots - 14.8874u + 11.7806 \\ 0.000199584u^{59} + 0.00207616u^{58} + \dots + 1.48938u + 14.5021 \\ -0.000400020u^{59} + 0.00107306u^{58} + \dots + 1.48938u + 14.5021 \\ -0.000400020u^{59} + 0.00107306u^{58} + \dots + 1.3474u - 23.9948 \\ a_{10} = \begin{pmatrix} 0.00242528u^{59} - 0.00649531u^{58} + \dots + 1.3474u - 23.9948 \\ 0.000228355u^{59} - 0.000590475u^{58} + \dots + 7.46556u - 2.03457 \end{pmatrix}$$

- (ii) Obstruction class = -1
- (iii) Cusp Shapes =  $0.00130054u^{59} 0.00350454u^{58} + \cdots 11.7943u 31.3032$

### (iv) u-Polynomials at the component

| Crossings     | u-Polynomials at each crossing             |
|---------------|--|
| $c_1$         | $u^{60} + 35u^{59} + \dots + 2933u + 361$  |
| $c_2, c_5$    | $u^{60} + u^{59} + \dots - 27u - 19$       |
| $c_3, c_9$    | $u^{60} + u^{59} + \dots + 46u - 43$       |
| $c_4, c_7$    | $u^{60} - 4u^{59} + \dots - 12u + 1$       |
| $c_6, c_{11}$ | $u^{60} - 3u^{59} + \dots - 11482u + 3559$ |
| $c_8,c_{12}$  | $u^{60} + 3u^{59} + \dots + 568u + 23$     |
| $c_{10}$      | $u^{60} + u^{59} + \dots + 15055u - 761$   |

### (v) Riley Polynomials at the component

| Crossings       | Riley Polynomials at each crossing                  |
|-----------------|---|
| $c_1$           | $y^{60} - 11y^{59} + \dots - 3170161y + 130321$     |
| $c_2, c_5$      | $y^{60} - 35y^{59} + \dots - 2933y + 361$           |
| $c_3, c_9$      | $y^{60} + 49y^{59} + \dots + 10526y + 1849$         |
| $c_4, c_7$      | $y^{60} + 2y^{59} + \dots - 46y + 1$                |
| $c_6, c_{11}$   | $y^{60} + 65y^{59} + \dots - 502242808y + 12666481$ |
| $c_{8}, c_{12}$ | $y^{60} - 47y^{59} + \dots - 56882y + 529$          |
| $c_{10}$        | $y^{60} - 23y^{59} + \dots - 95786899y + 579121$    |

## (vi) Complex Volumes and Cusp Shapes

| Solutions to $I_1^u$  | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$                 | Cusp shape          |
|---|---|---------------------|
| u = -1.007350 + 0.006718I                                     |   |                     |
| a = -0.051105 - 0.783732I                                     | 8.73644 + 2.57827I                                    | 3.69883 - 3.02158I  |
| b = -0.856821 + 0.663890I                                     |   |                     |
| u = -1.007350 - 0.006718I                                     |   |                     |
| a = -0.051105 + 0.783732I                                     | 8.73644 - 2.57827I                                    | 3.69883 + 3.02158I  |
| b = -0.856821 - 0.663890I                                     |   |                     |
| u = 0.167317 + 1.021400I                                      |   |                     |
| a = -0.69860 - 1.40758I                                       | 3.79265 - 1.97736I                                    | 0.36666 + 2.76154I  |
| b = 0.176226 + 0.887745I                                      |   |                     |
| u = 0.167317 - 1.021400I                                      | <b>_</b>  |                     |
| a = -0.69860 + 1.40758I                                       | 3.79265 + 1.97736I                                    | 0.36666 - 2.76154I  |
| b = 0.176226 - 0.887745I                                      |   |                     |
| u = 0.120119 + 0.949857I                                      | 0.000   | 0 00000 F 00000 F   |
| a = 0.243764 - 0.379978I                                      | -0.77619 + 1.28470I                                   | -6.96269 - 5.03629I |
| b = 0.032250 + 0.520457I $u = 0.120119 - 0.949857I$           |   |                     |
|   | 0.77610 1.004701                                      | C 0C0C0 + F 09C00 I |
| a = 0.243764 + 0.379978I                                      | -0.77619 - 1.28470I                                   | -6.96269 + 5.03629I |
| b = 0.032250 - 0.520457I $u = -0.436643 + 0.834573I$          |   |                     |
| a = -0.430043 + 0.334373I<br>a = 0.916522 + 0.292944I         | -0.52721 - 1.87425I                                   | -8.40865 + 2.07235I |
|   | -0.32721 - 1.874231                                   | -6.40800 + 2.072501 |
| $\frac{b = -0.973516 + 0.318596I}{u = -0.436643 - 0.834573I}$ |   |                     |
| a = 0.430043 - 0.094973I $a = 0.916522 - 0.292944I$           | -0.52721 + 1.87425I                                   | -8.40865 - 2.07235I |
| b = -0.973516 - 0.318596I                                     | 0.02121 7 1.014201                                    | 0.40000 - 2.012001  |
| u = 0.233820 + 1.070940I                                      |   |                     |
| a = -0.287355 - 0.183543I                                     | $\begin{vmatrix} -0.817883 + 0.949182I \end{vmatrix}$ | -8.00000 + 0.I      |
| b = 0.439508 + 0.589156I                                      |   |                     |
| u = 0.233820 - 1.070940I                                      |   |                     |
| a = -0.287355 + 0.183543I                                     | -0.817883 - 0.949182I                                 | -8.00000 + 0.I      |
| b = 0.439508 - 0.589156I                                      |   |                     |
|   | <u> </u>  |                     |

| Solutions to $I_1^u$      | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape          |
|---------------------------|---------------------------------------|---------------------|
| u = -0.783519 + 0.441750I |                                       |                     |
| a = 1.19806 - 1.78599I    | 2.59861 + 3.60251I                    | -5.47993 - 4.86448I |
| b = -0.902727 + 1.012570I |                                       |                     |
| u = -0.783519 - 0.441750I |                                       |                     |
| a = 1.19806 + 1.78599I    | 2.59861 - 3.60251I                    | -5.47993 + 4.86448I |
| b = -0.902727 - 1.012570I |                                       |                     |
| u = -0.346136 + 1.116180I |                                       |                     |
| a = -0.69410 + 1.24191I   | -3.89834 - 2.15588I                   | 0                   |
| b = -1.129160 - 0.396009I |                                       |                     |
| u = -0.346136 - 1.116180I |                                       |                     |
| a = -0.69410 - 1.24191I   | -3.89834 + 2.15588I                   | 0                   |
| b = -1.129160 + 0.396009I |                                       |                     |
| u = -1.280030 + 0.312941I |                                       |                     |
| a = -0.02697 - 1.54626I   | 5.59454 - 0.79177I                    | 0                   |
| b = 0.907660 + 0.163934I  |                                       |                     |
| u = -1.280030 - 0.312941I |                                       |                     |
| a = -0.02697 + 1.54626I   | 5.59454 + 0.79177I                    | 0                   |
| b = 0.907660 - 0.163934I  |                                       |                     |
| u = 0.673670 + 0.088043I  |                                       |                     |
| a = -1.13855 + 0.86484I   | 1.34053 + 2.69149I                    | -4.70869 - 3.74095I |
| b = 1.018250 - 0.455571I  |                                       |                     |
| u = 0.673670 - 0.088043I  |                                       |                     |
| a = -1.13855 - 0.86484I   | 1.34053 - 2.69149I                    | -4.70869 + 3.74095I |
| b = 1.018250 + 0.455571I  |                                       |                     |
| u = 0.179970 + 1.330630I  |                                       |                     |
| a = 0.613950 + 1.012280I  | -2.96619 + 5.50433I                   | 0                   |
| b = 1.119500 - 0.531381I  |                                       |                     |
| u = 0.179970 - 1.330630I  |                                       |                     |
| a = 0.613950 - 1.012280I  | -2.96619 - 5.50433I                   | 0                   |
| b = 1.119500 + 0.531381I  |                                       |                     |

| Solutions to $I_1^u$      | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape            |
|---------------------------|---------------------------------------|-----------------------|
| u = 1.342990 + 0.174597I  |                                       |                       |
| a = -0.48406 - 1.61748I   | 3.31510 - 2.64385I                    | 0                     |
| b = 0.662047 + 0.683351I  |                                       |                       |
| u = 1.342990 - 0.174597I  |                                       |                       |
| a = -0.48406 + 1.61748I   | 3.31510 + 2.64385I                    | 0                     |
| b = 0.662047 - 0.683351I  |                                       |                       |
| u = 0.631122 + 0.052699I  |                                       |                       |
| a = -0.61769 - 1.35412I   | 1.60978 - 2.58403I                    | -1.183332 - 0.037949I |
| b = 0.921626 + 0.670766I  |                                       |                       |
| u = 0.631122 - 0.052699I  |                                       |                       |
| a = -0.61769 + 1.35412I   | 1.60978 + 2.58403I                    | -1.183332 + 0.037949I |
| b = 0.921626 - 0.670766I  |                                       |                       |
| u = -0.520152 + 0.044751I |                                       |                       |
| a = 2.22330 + 0.65037I    | -1.347560 + 0.092496I                 | -5.86116 + 1.61635I   |
| b = -0.529944 - 0.260822I |                                       |                       |
| u = -0.520152 - 0.044751I |                                       |                       |
| a = 2.22330 - 0.65037I    | -1.347560 - 0.092496I                 | -5.86116 - 1.61635I   |
| b = -0.529944 + 0.260822I |                                       |                       |
| u = 0.37351 + 1.47885I    |                                       |                       |
| a = -0.042265 + 0.991284I | -2.44888 - 1.09682I                   | 0                     |
| b = 0.254547 - 0.892528I  |                                       |                       |
| u = 0.37351 - 1.47885I    |                                       |                       |
| a = -0.042265 - 0.991284I | -2.44888 + 1.09682I                   | 0                     |
| b = 0.254547 + 0.892528I  |                                       |                       |
| u = 0.379838 + 0.129064I  |                                       |                       |
| a = -2.69838 - 0.75915I   | 2.41343 - 4.02201I                    | -2.17904 + 4.26768I   |
| b = 0.310209 - 0.552194I  |                                       |                       |
| u = 0.379838 - 0.129064I  |                                       |                       |
| a = -2.69838 + 0.75915I   | 2.41343 + 4.02201I                    | -2.17904 - 4.26768I   |
| b = 0.310209 + 0.552194I  |                                       |                       |

| $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape   |
|---------------------------------------|--|
|                                       |  |
| -0.992150                             | -10.3910   |
|                                       |  |
|                                       |  |
| -6.51294 - 4.15782I                   | 0  |
|                                       |  |
|                                       |  |
| -6.51294 + 4.15782I                   | 0  |
|                                       |  |
|                                       |  |
| -2.29321 - 2.81632I                   | -7.40161 + 5.36260I  |
|                                       |  |
|                                       |  |
| -2.29321 + 2.81632I                   | -7.40161 - 5.36260I  |
|                                       |  |
|                                       |  |
| 0.20500 + 8.08474I                    | -6.89819 - 9.56475I  |
|                                       |  |
|                                       |  |
| 0.20500 - 8.08474I                    | -6.89819 + 9.56475I  |
|                                       |  |
|                                       |  |
| -5.68066                              | 0  |
|                                       |  |
|                                       |  |
| -5.36689 - 6.58267I                   | 0  |
|                                       |  |
|                                       |  |
| -5.36689 + 6.58267I                   | 0  |
|                                       |  |
|                                       | -0.992150 $-6.51294 - 4.15782I$ $-6.51294 + 4.15782I$ $-2.29321 - 2.81632I$ $-2.29321 + 2.81632I$ $0.20500 + 8.08474I$ $0.20500 - 8.08474I$ $-5.68066$ $-5.36689 - 6.58267I$ |

| Solutions to $I_1^u$      | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape |
|---------------------------|---------------------------------------|------------|
| u = 0.54349 + 1.71557I    |                                       |            |
| a = 0.182247 + 1.206790I  | -2.29420 + 9.43598I                   | 0          |
| b = -0.223941 - 1.051210I |                                       |            |
| u = 0.54349 - 1.71557I    |                                       |            |
| a = 0.182247 - 1.206790I  | -2.29420 - 9.43598I                   | 0          |
| b = -0.223941 + 1.051210I |                                       |            |
| u = 0.36459 + 1.77723I    |                                       |            |
| a = -0.882179 - 0.158077I | 0.50904 - 3.72563I                    | 0          |
| b = -0.848721 - 0.077580I |                                       |            |
| u = 0.36459 - 1.77723I    |                                       |            |
| a = -0.882179 + 0.158077I | 0.50904 + 3.72563I                    | 0          |
| b = -0.848721 + 0.077580I |                                       |            |
| u = 0.96428 + 1.53998I    |                                       |            |
| a = -0.035444 - 1.020920I | -7.16461 + 2.87399I                   | 0          |
| b = -1.264660 + 0.346449I |                                       |            |
| u = 0.96428 - 1.53998I    |                                       |            |
| a = -0.035444 + 1.020920I | -7.16461 - 2.87399I                   | 0          |
| b = -1.264660 - 0.346449I |                                       |            |
| u = 0.22234 + 1.88376I    |                                       |            |
| a = 0.101412 + 0.495797I  | -4.20439 + 4.30937I                   | 0          |
| b = 1.213340 - 0.305461I  |                                       |            |
| u = 0.22234 - 1.88376I    |                                       |            |
| a = 0.101412 - 0.495797I  | -4.20439 - 4.30937I                   | 0          |
| b = 1.213340 + 0.305461I  |                                       |            |
| u = 1.67961 + 0.89723I    |                                       |            |
| a = 0.479659 + 0.380032I  | -1.59063 - 4.29713I                   | 0          |
| b = -1.148550 - 0.220866I |                                       |            |
| u = 1.67961 - 0.89723I    |                                       |            |
| a = 0.479659 - 0.380032I  | -1.59063 + 4.29713I                   | 0          |
| b = -1.148550 + 0.220866I |                                       |            |

| Solutions to $I_1^u$      | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape |
|---------------------------|---------------------------------------|------------|
| u = 0.05205 + 1.91687I    |                                       |            |
| a = 0.162195 - 0.881999I  | -10.72230 + 1.07223I                  | 0          |
| b = -1.327950 + 0.474120I |                                       |            |
| u = 0.05205 - 1.91687I    |                                       |            |
| a = 0.162195 + 0.881999I  | -10.72230 - 1.07223I                  | 0          |
| b = -1.327950 - 0.474120I |                                       |            |
| u = -0.94156 + 1.78663I   |                                       |            |
| a = -0.116273 - 1.092550I | -10.53220 - 9.42728I                  | 0          |
| b = 1.304530 + 0.496577I  |                                       |            |
| u = -0.94156 - 1.78663I   |                                       |            |
| a = -0.116273 + 1.092550I | -10.53220 + 9.42728I                  | 0          |
| b = 1.304530 - 0.496577I  |                                       |            |
| u = -0.13842 + 2.02925I   |                                       |            |
| a = -0.253801 - 0.631347I | -7.82500 + 4.70197I                   | 0          |
| b = 1.39836 + 0.30006I    |                                       |            |
| u = -0.13842 - 2.02925I   |                                       |            |
| a = -0.253801 + 0.631347I | -7.82500 - 4.70197I                   | 0          |
| b = 1.39836 - 0.30006I    |                                       |            |
| u = 0.94830 + 1.92269I    |                                       |            |
| a = 0.160247 - 1.197610I  | -5.5691 + 15.3844I                    | 0          |
| b = -1.275950 + 0.609274I |                                       |            |
| u = 0.94830 - 1.92269I    |                                       |            |
| a = 0.160247 + 1.197610I  | -5.5691 - 15.3844I                    | 0          |
| b = -1.275950 - 0.609274I |                                       |            |
| u = -0.69511 + 2.27123I   |                                       |            |
| a = 0.392091 + 0.819280I  | -0.91388 - 7.09123I                   | 0          |
| b = -1.36545 - 0.50326I   |                                       |            |
| u = -0.69511 - 2.27123I   |                                       |            |
| a = 0.392091 - 0.819280I  | -0.91388 + 7.09123I                   | 0          |
| b = -1.36545 + 0.50326I   |                                       |            |

$$II. \\ I_2^u = \langle -1.50 \times 10^7 u^{15} - 2.91 \times 10^6 u^{14} + \dots + 2.60 \times 10^7 b + 3.14 \times 10^7, \ 5.06 \times 10^7 u^{15} + 1.93 \times 10^7 u^{14} + \dots + 2.60 \times 10^7 a - 1.08 \times 10^8, \ u^{16} + 2u^{14} + \dots - 6u + 1 \rangle$$

(i) Arc colorings

$$a_{6} = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_{3} = \begin{pmatrix} -1.94816u^{15} - 0.742080u^{14} + \cdots - 20.2601u + 4.15208 \\ 0.576104u^{15} + 0.111922u^{14} + \cdots + 7.08162u - 1.20706 \end{pmatrix}$$

$$a_{7} = \begin{pmatrix} 1 \\ -u^{2} \end{pmatrix}$$

$$a_{2} = \begin{pmatrix} -1.37205u^{15} - 0.630158u^{14} + \cdots - 13.1784u + 2.94503 \\ 0.576104u^{15} + 0.111922u^{14} + \cdots + 7.08162u - 1.20706 \end{pmatrix}$$

$$a_{1} = \begin{pmatrix} 0.635947u^{15} - 0.266901u^{14} + \cdots + 9.79214u - 6.41038 \\ 0.329868u^{15} + 0.589621u^{14} + \cdots - 0.434301u + 2.03882 \end{pmatrix}$$

$$a_{5} = \begin{pmatrix} 1.54782u^{15} + 0.0499397u^{14} + \cdots + 19.5088u - 4.73371 \\ -1.78902u^{15} - 0.836104u^{14} + \cdots - 15.5610u + 3.93263 \end{pmatrix}$$

$$a_{8} = \begin{pmatrix} -0.410379u^{15} + 0.364053u^{14} + \cdots - 8.98198u + 5.67013 \\ 1.06297u^{15} + 0.392340u^{14} + \cdots + 8.97100u - 3.59713 \end{pmatrix}$$

$$a_{9} = \begin{pmatrix} -0.410379u^{15} + 0.364053u^{14} + \cdots - 8.98198u + 5.67013 \\ 1.32987u^{15} + 0.589621u^{14} + \cdots + 11.5657u - 3.96118 \end{pmatrix}$$

$$a_{4} = \begin{pmatrix} -1.28768u^{15} - 0.560350u^{14} + \cdots - 10.7155u + 1.55549 \\ 2.08061u^{15} + 1.90825u^{14} + \cdots + 12.3794u - 2.05941 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} -u \\ u \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} -u \\ u \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} -0.376194u^{15} + 0.0413337u^{14} + \cdots - 5.33982u + 4.04169 \\ -1.16597u^{15} - 1.06395u^{14} + \cdots - 4.36721u - 0.249796 \end{pmatrix}$$

- (ii) Obstruction class = 1
- (iii) Cusp Shapes =  $\frac{171433056}{25980989}u^{15} + \frac{71506332}{25980989}u^{14} + \dots + \frac{1610812870}{25980989}u \frac{747202050}{25980989}u^{14} + \dots$

(iv) u-Polynomials at the component

| Crossings             | u-Polynomials at each crossing        |
|-----------------------|---------------------------------------|
| $c_1$                 | $u^{16} - 8u^{15} + \dots - 11u + 1$  |
| $c_2$                 | $u^{16} - 4u^{14} + \dots + u + 1$    |
| $c_3$                 | $u^{16} + 10u^{14} + \dots + 2u + 1$  |
| $c_4$                 | $u^{16} - 3u^{15} + \dots - 2u^2 + 1$ |
| C <sub>5</sub>        | $u^{16} - 4u^{14} + \dots - u + 1$    |
| <i>C</i> <sub>6</sub> | $u^{16} + 2u^{14} + \dots - 6u + 1$   |
| C <sub>7</sub>        | $u^{16} + 3u^{15} + \dots - 2u^2 + 1$ |
| $c_8$                 | $u^{16} + 4u^{15} + \dots + 4u + 1$   |
| <i>C</i> 9            | $u^{16} + 10u^{14} + \dots - 2u + 1$  |
| $c_{10}$              | $u^{16} - 12u^{15} + \dots - 39u + 7$ |
| $c_{11}$              | $u^{16} + 2u^{14} + \dots + 6u + 1$   |
| $c_{12}$              | $u^{16} - 4u^{15} + \dots - 4u + 1$   |

### (v) Riley Polynomials at the component

| Crossings     | Riley Polynomials at each crossing      |
|---------------|---|
| $c_1$         | $y^{16} + 8y^{15} + \dots + y + 1$      |
| $c_2, c_5$    | $y^{16} - 8y^{15} + \dots - 11y + 1$    |
| $c_3, c_9$    | $y^{16} + 20y^{15} + \dots + 16y + 1$   |
| $c_4, c_7$    | $y^{16} + 9y^{15} + \dots - 4y + 1$     |
| $c_6, c_{11}$ | $y^{16} + 4y^{15} + \dots - 10y + 1$    |
| $c_8,c_{12}$  | $y^{16} - 12y^{15} + \dots - 16y + 1$   |
| $c_{10}$      | $y^{16} + 14y^{14} + \dots + 299y + 49$ |

## (vi) Complex Volumes and Cusp Shapes

| Solutions to $I_2^u$      | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape           |
|---------------------------|---------------------------------------|----------------------|
| u = 0.848678 + 0.085474I  |                                       |                      |
| a = -0.348467 + 0.518085I | 8.17515 - 2.59376I                    | -11.23658 + 3.27423I |
| b = -0.877180 - 0.669466I |                                       |                      |
| u = 0.848678 - 0.085474I  |                                       |                      |
| a = -0.348467 - 0.518085I | 8.17515 + 2.59376I                    | -11.23658 - 3.27423I |
| b = -0.877180 + 0.669466I |                                       |                      |
| u = -0.197488 + 1.171200I |                                       |                      |
| a = -0.995321 + 0.627483I | -3.62157 - 3.10177I                   | -11.65478 + 4.58211I |
| b = -1.084020 - 0.313740I |                                       |                      |
| u = -0.197488 - 1.171200I |                                       |                      |
| a = -0.995321 - 0.627483I | -3.62157 + 3.10177I                   | -11.65478 - 4.58211I |
| b = -1.084020 + 0.313740I |                                       |                      |
| u = -0.358669 + 1.174890I |                                       |                      |
| a = 0.898291 + 0.084340I  | 1.24172 + 3.04680I                    | -4.72616 - 0.51189I  |
| b = 0.552813 + 0.248801I  |                                       |                      |
| u = -0.358669 - 1.174890I |                                       |                      |
| a = 0.898291 - 0.084340I  | 1.24172 - 3.04680I                    | -4.72616 + 0.51189I  |
| b = 0.552813 - 0.248801I  |                                       |                      |
| u = 1.311460 + 0.162263I  |                                       |                      |
| a = -0.32990 + 1.75849I   | 5.97555 + 1.37057I                    | -3.09878 - 6.37528I  |
| b = 0.884570 - 0.318899I  |                                       |                      |
| u = 1.311460 - 0.162263I  |                                       |                      |
| a = -0.32990 - 1.75849I   | 5.97555 - 1.37057I                    | -3.09878 + 6.37528I  |
| b = 0.884570 + 0.318899I  |                                       |                      |
| u = -0.258625 + 0.594122I |                                       |                      |
| a = 1.52106 + 0.93961I    | -2.15911 - 0.80662I                   | -14.01192 + 1.37171I |
| b = -0.724239 + 0.209142I |                                       |                      |
| u = -0.258625 - 0.594122I |                                       |                      |
| a = 1.52106 - 0.93961I    | -2.15911 + 0.80662I                   | -14.01192 - 1.37171I |
| b = -0.724239 - 0.209142I |                                       |                      |

| Solutions to $I_2^u$      | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape           |
|---------------------------|---------------------------------------|----------------------|
| u = -1.42499 + 0.57815I   |                                       |                      |
| a = 0.58297 - 1.70738I    | 3.90110 + 3.42244I                    | 1.25743 - 7.02245I   |
| b = -0.823392 + 0.939526I |                                       |                      |
| u = -1.42499 - 0.57815I   |                                       |                      |
| a = 0.58297 + 1.70738I    | 3.90110 - 3.42244I                    | 1.25743 + 7.02245I   |
| b = -0.823392 - 0.939526I |                                       |                      |
| u = 0.300412 + 0.138730I  |                                       |                      |
| a = -1.81674 - 2.37481I   | 1.09392 - 2.94039I                    | -12.11036 + 5.85027I |
| b = 0.864792 + 0.780054I  |                                       |                      |
| u = 0.300412 - 0.138730I  |                                       |                      |
| a = -1.81674 + 2.37481I   | 1.09392 + 2.94039I                    | -12.11036 - 5.85027I |
| b = 0.864792 - 0.780054I  |                                       |                      |
| u = -0.22078 + 1.83089I   |                                       |                      |
| a = -0.011897 + 0.531685I | -1.44728 + 6.14957I                   | -9.41886 - 5.41107I  |
| b = 1.206660 - 0.440272I  |                                       |                      |
| u = -0.22078 - 1.83089I   |                                       |                      |
| a = -0.011897 - 0.531685I | -1.44728 - 6.14957I                   | -9.41886 + 5.41107I  |
| b = 1.206660 + 0.440272I  |                                       |                      |

III. u-Polynomials

| Crossings             | u-Polynomials at each crossing  |
|-----------------------|---|
| $c_1$                 | $ (u^{16} - 8u^{15} + \dots - 11u + 1)(u^{60} + 35u^{59} + \dots + 2933u + 361) $ |
| $c_2$                 | $ (u^{16} - 4u^{14} + \dots + u + 1)(u^{60} + u^{59} + \dots - 27u - 19) $        |
| $c_3$                 | $ (u^{16} + 10u^{14} + \dots + 2u + 1)(u^{60} + u^{59} + \dots + 46u - 43) $      |
| $c_4$                 | $ (u^{16} - 3u^{15} + \dots - 2u^2 + 1)(u^{60} - 4u^{59} + \dots - 12u + 1) $     |
| $c_5$                 | $(u^{16} - 4u^{14} + \dots - u + 1)(u^{60} + u^{59} + \dots - 27u - 19)$          |
| $c_6$                 | $ (u^{16} + 2u^{14} + \dots - 6u + 1)(u^{60} - 3u^{59} + \dots - 11482u + 3559) $ |
| <i>C</i> <sub>7</sub> | $ (u^{16} + 3u^{15} + \dots - 2u^2 + 1)(u^{60} - 4u^{59} + \dots - 12u + 1) $     |
| $c_8$                 | $(u^{16} + 4u^{15} + \dots + 4u + 1)(u^{60} + 3u^{59} + \dots + 568u + 23)$       |
| $c_9$                 | $(u^{16} + 10u^{14} + \dots - 2u + 1)(u^{60} + u^{59} + \dots + 46u - 43)$        |
| $c_{10}$              | $(u^{16} - 12u^{15} + \dots - 39u + 7)(u^{60} + u^{59} + \dots + 15055u - 761)$   |
| $c_{11}$              | $(u^{16} + 2u^{14} + \dots + 6u + 1)(u^{60} - 3u^{59} + \dots - 11482u + 3559)$   |
| $c_{12}$              | $(u^{16} - 4u^{15} + \dots - 4u + 1)(u^{60} + 3u^{59} + \dots + 568u + 23)$ 18    |

### IV. Riley Polynomials

| Crossings     | Riley Polynomials at each crossing   |
|---------------|--|
| $c_1$         | $ (y^{16} + 8y^{15} + \dots + y + 1)(y^{60} - 11y^{59} + \dots - 3170161y + 130321) $              |
| $c_2, c_5$    | $(y^{16} - 8y^{15} + \dots - 11y + 1)(y^{60} - 35y^{59} + \dots - 2933y + 361)$                    |
| $c_3, c_9$    | $(y^{16} + 20y^{15} + \dots + 16y + 1)(y^{60} + 49y^{59} + \dots + 10526y + 1849)$                 |
| $c_4, c_7$    | $(y^{16} + 9y^{15} + \dots - 4y + 1)(y^{60} + 2y^{59} + \dots - 46y + 1)$                          |
| $c_6, c_{11}$ | $(y^{16} + 4y^{15} + \dots - 10y + 1)$ $\cdot (y^{60} + 65y^{59} + \dots - 502242808y + 12666481)$ |
| $c_8, c_{12}$ | $(y^{16} - 12y^{15} + \dots - 16y + 1)(y^{60} - 47y^{59} + \dots - 56882y + 529)$                  |
| $c_{10}$      | $(y^{16} + 14y^{14} + \dots + 299y + 49)$ $\cdot (y^{60} - 23y^{59} + \dots - 95786899y + 579121)$ |