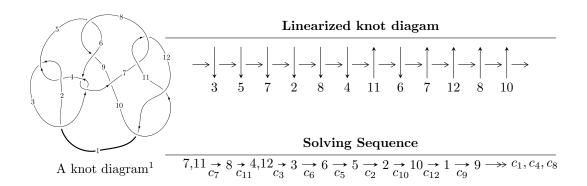
$12n_{0084} \ (K12n_{0084})$



Ideals for irreducible components² of X_{par}

$$\begin{split} I_1^u &= \langle -16510225313889u^{40} - 73379619742180u^{39} + \dots + 7015565688188b + 16563398292357, \\ &- 39282009802613u^{40} - 170243595424532u^{39} + \dots + 7015565688188a + 73325296186875, \\ &u^{41} + 5u^{40} + \dots + 5u - 1 \rangle \\ I_2^u &= \langle -u^2a - 2u^2 + b + a + u + 2, \ a^2 + 2au + 4u^2 + a - 4u + 4, \ u^3 - u^2 + 1 \rangle \\ I_3^u &= \langle u^2 + b, \ a - u, \ u^3 - u^2 + 1 \rangle \\ I_4^u &= \langle b, \ a + 1, \ u + 1 \rangle \end{split}$$

* 4 irreducible components of $\dim_{\mathbb{C}} = 0$, with total 51 representations.

¹The image of knot diagram is generated by the software "**Draw programme**" developed by Andrew Bartholomew(http://www.layer8.co.uk/maths/draw/index.htm#Running-draw), where we modified some parts for our purpose(https://github.com/CATsTAILs/LinksPainter).

² All coefficients of polynomials are rational numbers. But the coefficients are sometimes approximated in decimal forms when there is not enough margin.

$$I. \\ I_1^u = \langle -1.65 \times 10^{13} u^{40} - 7.34 \times 10^{13} u^{39} + \dots + 7.02 \times 10^{12} b + 1.66 \times 10^{13}, \ -3.93 \times 10^{13} u^{40} - 1.70 \times 10^{14} u^{39} + \dots + 7.02 \times 10^{12} a + 7.33 \times 10^{13}, \ u^{41} + 5 u^{40} + \dots + 5 u - 1 \rangle$$

$$a_{7} = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_{8} = \begin{pmatrix} 1 \\ -u^{2} \end{pmatrix}$$

$$a_{4} = \begin{pmatrix} 5.59926u^{40} + 24.2666u^{39} + \dots + 36.6437u - 10.4518 \\ 2.35337u^{40} + 10.4595u^{39} + \dots + 18.2641u - 2.36095 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} u \\ -u^{3} + u \end{pmatrix}$$

$$a_{3} = \begin{pmatrix} 7.95264u^{40} + 34.7261u^{39} + \dots + 54.9078u - 12.8128 \\ 2.35337u^{40} + 10.4595u^{39} + \dots + 18.2641u - 2.36095 \end{pmatrix}$$

$$a_{6} = \begin{pmatrix} -0.679973u^{40} - 2.74952u^{39} + \dots - 2.24406u + 4.15673 \\ 0.448072u^{40} + 2.09737u^{39} + \dots - 2.27213u - 0.275451 \end{pmatrix}$$

$$a_{5} = \begin{pmatrix} -0.0387129u^{40} - 1.20772u^{39} + \dots - 8.44788u + 4.53163 \\ -1.39663u^{40} - 6.29046u^{39} + \dots - 11.2359u + 1.38905 \end{pmatrix}$$

$$a_{2} = \begin{pmatrix} 5.78006u^{40} + 24.1415u^{39} + \dots + 36.8035u - 7.87601 \\ 1.39663u^{40} + 6.29046u^{39} + \dots + 11.2359u - 1.38905 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} -u^{3} \\ u^{5} - u^{3} + u \end{pmatrix}$$

$$a_{1} = \begin{pmatrix} -u^{3} \\ -u^{7} + u^{5} - 2u^{3} + u \end{pmatrix}$$

$$a_{9} = \begin{pmatrix} u^{5} - u \\ u^{5} - u^{3} + u \end{pmatrix}$$

(ii) Obstruction class = -1

(iii) Cusp Shapes $= \frac{93247797228429}{1753891422047}u^{40} + \frac{1555830189736099}{7015565688188}u^{39} + \dots + \frac{2808560039807687}{7015565688188}u - \frac{263248389242609}{3507782844094}$

Crossings	u-Polynomials at each crossing
c_1	$u^{41} + 29u^{40} + \dots + 71u + 1$
c_2, c_4	$u^{41} - 5u^{40} + \dots + 7u - 1$
c_3, c_6	$u^{41} - 4u^{40} + \dots - 10u + 2$
c_5, c_8	$u^{41} - 4u^{40} + \dots + 512u - 512$
c_{7}, c_{11}	$u^{41} - 5u^{40} + \dots + 5u + 1$
<i>c</i> ₉	$u^{41} + 3u^{40} + \dots - 19597u + 2017$
c_{10}, c_{12}	$u^{41} - 9u^{40} + \dots + 95u - 1$

Crossings	Riley Polynomials at each crossing
c_1	$y^{41} - 29y^{40} + \dots + 1223y - 1$
c_2, c_4	$y^{41} - 29y^{40} + \dots + 71y - 1$
c_3, c_6	$y^{41} + 42y^{39} + \dots + 56y - 4$
c_5, c_8	$y^{41} - 50y^{40} + \dots + 6160384y - 262144$
c_7, c_{11}	$y^{41} - 9y^{40} + \dots + 95y - 1$
c_9	$y^{41} + 135y^{40} + \dots + 36517343y - 4068289$
c_{10}, c_{12}	$y^{41} + 51y^{40} + \dots + 6127y - 1$

Solutions to I_1^u	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
u = 0.716889 + 0.703853I		
a = -0.43425 - 2.19682I	-4.60661 + 1.52902I	-5.50706 - 4.66307I
b = -0.336317 + 0.798192I		
u = 0.716889 - 0.703853I		
a = -0.43425 + 2.19682I	-4.60661 - 1.52902I	-5.50706 + 4.66307I
b = -0.336317 - 0.798192I		
u = -0.870049 + 0.467634I		
a = -1.164530 + 0.454430I	1.79473 + 0.06262I	2.65743 - 0.68980I
b = 0.135790 - 0.918035I		
u = -0.870049 - 0.467634I		
a = -1.164530 - 0.454430I	1.79473 - 0.06262I	2.65743 + 0.68980I
b = 0.135790 + 0.918035I		
u = 0.356456 + 0.980218I		
a = 0.282408 + 0.117731I	-7.17972 - 2.87745I	-9.28722 + 2.69256I
b = -1.039320 - 0.421414I		
u = 0.356456 - 0.980218I		
a = 0.282408 - 0.117731I	-7.17972 + 2.87745I	-9.28722 - 2.69256I
b = -1.039320 + 0.421414I		
u = -0.670401 + 0.652476I		
a = 1.010200 - 0.553099I	0.97725 - 4.44119I	-1.27945 + 4.71656I
b = 0.446012 + 1.120950I		
u = -0.670401 - 0.652476I		
a = 1.010200 + 0.553099I	0.97725 + 4.44119I	-1.27945 - 4.71656I
b = 0.446012 - 1.120950I		
u = 0.940640 + 0.501809I	0.70110 + 4.495501	0.94790 0.909717
a = -0.02791 + 1.96139I	-0.70118 + 4.43572I	-0.34738 - 6.39371I
b = 0.687266 - 0.758448I		
u = 0.940640 - 0.501809I	0.70110 4.405507	0.04500 : 0.0054 7
a = -0.02791 - 1.96139I	-0.70118 - 4.43572I	-0.34738 + 6.39371I
b = 0.687266 + 0.758448I		

Solutions to I_1^u	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
u = 0.877966 + 0.643589I		
a = 0.016521 + 1.234530I	-4.07708 + 3.51500I	-8.28852 - 2.95507I
b = -0.609480 - 0.518945I		
u = 0.877966 - 0.643589I		
a = 0.016521 - 1.234530I	-4.07708 - 3.51500I	-8.28852 + 2.95507I
b = -0.609480 + 0.518945I		
u = -0.854623 + 0.159200I		
a = -0.978695 + 0.858024I	1.46993 - 0.34552I	6.06026 + 0.56755I
b = 0.041696 - 0.419660I		
u = -0.854623 - 0.159200I		
a = -0.978695 - 0.858024I	1.46993 + 0.34552I	6.06026 - 0.56755I
b = 0.041696 + 0.419660I		
u = 0.877954 + 0.775956I		
a = -0.968702 - 0.351197I	-3.83803 + 2.91878I	4.79738 - 5.00057I
b = -0.598603 + 0.031599I		
u = 0.877954 - 0.775956I		
a = -0.968702 + 0.351197I	-3.83803 - 2.91878I	4.79738 + 5.00057I
b = -0.598603 - 0.031599I		
u = 0.537453 + 0.625371I		
a = -0.426437 - 0.272772I	-2.04074 - 0.11127I	-4.60725 + 0.35706I
b = 0.891755 + 0.389086I		
u = 0.537453 - 0.625371I		
a = -0.426437 + 0.272772I	-2.04074 + 0.11127I	-4.60725 - 0.35706I
b = 0.891755 - 0.389086I		
u = -0.802702		
a = -5.09181	-0.345711	-64.7260
b = -0.275758		
u = 1.139710 + 0.532282I		
a = 0.29262 - 1.64354I	-4.48025 + 8.31246I	0 7.85034I
b = -0.893901 + 0.701047I		

Solutions to I_1^u	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
u = 1.139710 - 0.532282I		
a = 0.29262 + 1.64354I	-4.48025 - 8.31246I	0. + 7.85034I
b = -0.893901 - 0.701047I		
u = -1.26772		
a = 0.964605	-0.787444	-12.1570
b = -0.640215		
u = -0.891473 + 0.933329I		
a = -0.528554 + 0.154006I	-10.38260 + 1.04574I	0
b = 1.25025 - 1.10628I		
u = -0.891473 - 0.933329I		
a = -0.528554 - 0.154006I	-10.38260 - 1.04574I	0
b = 1.25025 + 1.10628I		
u = -0.841724 + 0.990823I		
a = 0.377207 - 0.291737I	-15.1663 + 7.0683I	0
b = -1.21490 + 1.06493I		
u = -0.841724 - 0.990823I		
a = 0.377207 + 0.291737I	-15.1663 - 7.0683I	0
b = -1.21490 - 1.06493I		
u = -0.934438 + 0.935551I		
a = -0.61279 + 1.51752I	-14.6673 - 1.5212I	0
b = -1.12955 - 1.22573I		
u = -0.934438 - 0.935551I		
a = -0.61279 - 1.51752I	-14.6673 + 1.5212I	0
b = -1.12955 + 1.22573I		
u = -0.982434 + 0.885456I		
a = 0.67122 - 1.65206I	-10.08510 - 7.74293I	0
b = 1.17691 + 1.18848I		
u = -0.982434 - 0.885456I		
a = 0.67122 + 1.65206I	-10.08510 + 7.74293I	0
b = 1.17691 - 1.18848I		

Solutions to I_1^u	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
u = -0.962450 + 0.919824I		
a = 0.713562 - 0.200841I	-14.5747 - 5.2989I	0
b = -1.20978 + 1.14699I		
u = -0.962450 - 0.919824I		
a = 0.713562 + 0.200841I	-14.5747 + 5.2989I	0
b = -1.20978 - 1.14699I		
u = 0.961309 + 0.961016I		
a = -0.125970 + 0.554955I	-9.11622 + 3.51279I	0
b = 1.019520 - 0.111695I		
u = 0.961309 - 0.961016I		
a = -0.125970 - 0.554955I	-9.11622 - 3.51279I	0
b = 1.019520 + 0.111695I		
u = -1.039620 + 0.876652I		
a = -0.63077 + 1.75489I	-14.5120 - 13.9039I	0
b = -1.15233 - 1.13531I		
u = -1.039620 - 0.876652I		
a = -0.63077 - 1.75489I	-14.5120 + 13.9039I	0
b = -1.15233 + 1.13531I		
u = 0.629652 + 0.060391I		
a = -0.09621 + 3.42389I	3.87413 + 2.95359I	-12.9329 - 8.6631I
b = 0.189078 - 1.367880I		
u = 0.629652 - 0.060391I		
a = -0.09621 - 3.42389I	3.87413 - 2.95359I	-12.9329 + 8.6631I
b = 0.189078 + 1.367880I		
u = -0.512134 + 0.182325I		
a = 2.61667 + 0.05062I	-1.008150 - 0.694652I	-6.89267 - 0.99274I
b = 0.497781 - 0.337919I		
u = -0.512134 - 0.182325I		
a = 2.61667 - 0.05062I	-1.008150 + 0.694652I	-6.89267 + 0.99274I
b = 0.497781 + 0.337919I		

	Solutions to I_1^u	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
u =	= 0.113052		
a =	=-3.84398	-1.00335	-10.2280
b =	= 0.612202		

$$II. \\ I_2^u = \langle -u^2a - 2u^2 + b + a + u + 2, \ a^2 + 2au + 4u^2 + a - 4u + 4, \ u^3 - u^2 + 1 \rangle$$

$$a_{7} = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_{8} = \begin{pmatrix} 1 \\ -u^{2} \end{pmatrix}$$

$$a_{4} = \begin{pmatrix} u^{2}a + 2u^{2} - a - u - 2 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} u \\ -u^{2} + u + 1 \end{pmatrix}$$

$$a_{3} = \begin{pmatrix} u^{2}a + 2u^{2} - u - 2 \\ u^{2}a + 2u^{2} - a - u - 2 \end{pmatrix}$$

$$a_{6} = \begin{pmatrix} u^{2}a - au - a - 3 \\ u^{2}a + au + 3u^{2} \end{pmatrix}$$

$$a_{5} = \begin{pmatrix} u^{2}a - au - a - 3 \\ u^{2}a + au + 3u^{2} \end{pmatrix}$$

$$a_{2} = \begin{pmatrix} 2u^{2}a + 3u^{2} - a - 5 \\ u^{2}a + au + 3u^{2} \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} -u^{2} + 1 \\ -u^{2} \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} -1 \\ 0 \end{pmatrix}$$

$$a_{9} = \begin{pmatrix} 1 \\ -u^{2} \end{pmatrix}$$

- (ii) Obstruction class = 1
- (iii) Cusp Shapes = $-u^2a + 15au + 20u^2 + 11a + 4u + 4$

Crossings	u-Polynomials at each crossing
$c_1, c_3, c_9 \ c_{12}$	$(u^3 - u^2 + 2u - 1)^2$
c_2, c_{11}	$(u^3 + u^2 - 1)^2$
c_4, c_7	$(u^3 - u^2 + 1)^2$
c_5,c_8	u^6
c_6, c_{10}	$(u^3 + u^2 + 2u + 1)^2$

Crossings	Riley Polynomials at each crossing
$c_1, c_3, c_6 \\ c_9, c_{10}, c_{12}$	$(y^3 + 3y^2 + 2y - 1)^2$
c_2, c_4, c_7 c_{11}	$(y^3 - y^2 + 2y - 1)^2$
c_5, c_8	y^6

Solutions to I_2^u	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
u = 0.877439 + 0.744862I		
a = -1.06984 - 1.06527I	5.65624I	-3.29784 - 6.94206I
b = -0.215080 + 1.307140I		
u = 0.877439 + 0.744862I		
a = -1.68504 - 0.42445I	-4.13758 + 2.82812I	-24.3518 + 2.3339I
b = -0.569840		
u = 0.877439 - 0.744862I		
a = -1.06984 + 1.06527I	-5.65624I	-3.29784 + 6.94206I
b = -0.215080 - 1.307140I		
u = 0.877439 - 0.744862I		
a = -1.68504 + 0.42445I	-4.13758 - 2.82812I	-24.3518 - 2.3339I
b = -0.569840		
u = -0.754878		
a = 0.25488 + 3.03873I	4.13758 - 2.82812I	12.14969 - 2.71361I
b = -0.215080 - 1.307140I		
u = -0.754878		
a = 0.25488 - 3.03873I	4.13758 + 2.82812I	12.14969 + 2.71361I
b = -0.215080 + 1.307140I		

III.
$$I_3^u = \langle u^2 + b, \ a - u, \ u^3 - u^2 + 1 \rangle$$

a₇ =
$$\begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_{8} = \begin{pmatrix} 1 \\ -u^{2} \end{pmatrix}$$

$$a_{4} = \begin{pmatrix} u \\ -u^{2} \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} u \\ -u^{2} + u + 1 \end{pmatrix}$$

$$a_{3} = \begin{pmatrix} -u^{2} + u \\ -u^{2} \end{pmatrix}$$

$$a_{6} = \begin{pmatrix} u^{2} \\ -u^{2} + u + 1 \end{pmatrix}$$

$$a_{5} = \begin{pmatrix} u^{2} \\ -u^{2} + u + 1 \end{pmatrix}$$

$$a_{2} = \begin{pmatrix} u - 1 \\ -u^{2} + u + 1 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} -u^{2} + 1 \\ -u^{2} \end{pmatrix}$$

$$a_{1} = \begin{pmatrix} -1 \\ 0 \end{pmatrix}$$

$$a_{9} = \begin{pmatrix} 1 \\ -u^{2} \end{pmatrix}$$

- (ii) Obstruction class = 1
- (iii) Cusp Shapes = $2u^2 3u 2$

Crossings	u-Polynomials at each crossing
$c_1, c_3, c_9 \ c_{12}$	$u^3 - u^2 + 2u - 1$
c_2, c_{11}	$u^3 + u^2 - 1$
c_4, c_7	$u^3 - u^2 + 1$
c_5,c_8	u^3
c_6, c_{10}	$u^3 + u^2 + 2u + 1$

Crossings	Riley Polynomials at each crossing
c_1, c_3, c_6 c_9, c_{10}, c_{12}	$y^3 + 3y^2 + 2y - 1$
c_2, c_4, c_7 c_{11}	$y^3 - y^2 + 2y - 1$
c_5, c_8	y^3

Solutions to I_3^u	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
u = 0.877439 + 0.744862I		
a = 0.877439 + 0.744862I	0	-4.20216 + 0.37970I
b = -0.215080 - 1.307140I		
u = 0.877439 - 0.744862I		
a = 0.877439 - 0.744862I	0	-4.20216 - 0.37970I
b = -0.215080 + 1.307140I		
u = -0.754878		
a = -0.754878	0	1.40430
b = -0.569840		

IV.
$$I_4^u = \langle b, a+1, u+1 \rangle$$

$$a_7 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 0 \\ -1 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} 1 \\ -1 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} -1\\0 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} -1\\0 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} -1 \\ 0 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} 2 \\ -1 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} -3 \\ 1 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} 1 \\ -1 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} -2 \\ 1 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} 2 \\ -1 \end{pmatrix}$$

- (ii) Obstruction class = 1
- (iii) Cusp Shapes = 0

Crossings	u-Polynomials at each crossing
$c_1, c_2, c_8 \\ c_9, c_{11}, c_{12}$	u-1
c_3, c_6	u
c_4, c_5, c_7 c_{10}	u+1

Crossings	Riley Polynomials at each crossing
c_1, c_2, c_4 c_5, c_7, c_8 c_9, c_{10}, c_{11} c_{12}	y-1
c_3, c_6	y

Solutions to I_4^u	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
u = -1.00000		
a = -1.00000	0	0
b = 0		

V. u-Polynomials

Crossings	u-Polynomials at each crossing
c_1	$(u-1)(u^3 - u^2 + 2u - 1)^3(u^{41} + 29u^{40} + \dots + 71u + 1)$
c_2	$(u-1)(u^3+u^2-1)^3(u^{41}-5u^{40}+\cdots+7u-1)$
c_3	$u(u^3 - u^2 + 2u - 1)^3(u^{41} - 4u^{40} + \dots - 10u + 2)$
c_4	$(u+1)(u^3-u^2+1)^3(u^{41}-5u^{40}+\cdots+7u-1)$
c_5	$u^{9}(u+1)(u^{41} - 4u^{40} + \dots + 512u - 512)$
c_6	$u(u^{3} + u^{2} + 2u + 1)^{3}(u^{41} - 4u^{40} + \dots - 10u + 2)$
c ₇	$(u+1)(u^3-u^2+1)^3(u^{41}-5u^{40}+\cdots+5u+1)$
c_8	$u^{9}(u-1)(u^{41} - 4u^{40} + \dots + 512u - 512)$
c_9	$(u-1)(u^3 - u^2 + 2u - 1)^3(u^{41} + 3u^{40} + \dots - 19597u + 2017)$
c_{10}	$(u+1)(u^3+u^2+2u+1)^3(u^{41}-9u^{40}+\cdots+95u-1)$
c_{11}	$(u-1)(u^3+u^2-1)^3(u^{41}-5u^{40}+\cdots+5u+1)$
c_{12}	$(u-1)(u^3 - u^2 + 2u - 1)^3(u^{41} - 9u^{40} + \dots + 95u - 1)$ 22

VI. Riley Polynomials

Crossings	Riley Polynomials at each crossing
c_1	$(y-1)(y^3+3y^2+2y-1)^3(y^{41}-29y^{40}+\cdots+1223y-1)$
c_{2}, c_{4}	$(y-1)(y^3-y^2+2y-1)^3(y^{41}-29y^{40}+\cdots+71y-1)$
c_3, c_6	$y(y^3 + 3y^2 + 2y - 1)^3(y^{41} + 42y^{39} + \dots + 56y - 4)$
c_5,c_8	$y^{9}(y-1)(y^{41} - 50y^{40} + \dots + 6160384y - 262144)$
c_7, c_{11}	$(y-1)(y^3-y^2+2y-1)^3(y^{41}-9y^{40}+\cdots+95y-1)$
<i>c</i> 9	$(y-1)(y^3 + 3y^2 + 2y - 1)^3$ $\cdot (y^{41} + 135y^{40} + \dots + 36517343y - 4068289)$
c_{10},c_{12}	$(y-1)(y^3+3y^2+2y-1)^3(y^{41}+51y^{40}+\cdots+6127y-1)$