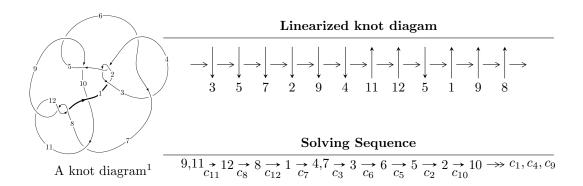
$12n_{0111} (K12n_{0111})$



Ideals for irreducible components² of X_{par}

$$\begin{split} I_1^u &= \langle -1.05669 \times 10^{17} u^{53} - 3.57059 \times 10^{17} u^{52} + \dots + 7.54024 \times 10^{16} b + 4.04284 \times 10^{16}, \\ &1.02527 \times 10^{17} u^{53} + 3.61000 \times 10^{17} u^{52} + \dots + 7.54024 \times 10^{16} a - 5.95597 \times 10^{17}, \ u^{54} + 4u^{53} + \dots - 13u - I_2^u &= \langle au - u^2 + b + a, \ -u^2 a + a^2 + 1, \ u^3 - u^2 + 2u - 1 \rangle \\ I_3^u &= \langle u^2 + b + u, \ -u^2 + a - 2, \ u^3 - u^2 + 2u - 1 \rangle \end{split}$$

* 3 irreducible components of $\dim_{\mathbb{C}} = 0$, with total 63 representations.

¹The image of knot diagram is generated by the software "**Draw programme**" developed by Andrew Bartholomew(http://www.layer8.co.uk/maths/draw/index.htm#Running-draw), where we modified some parts for our purpose(https://github.com/CATsTAILs/LinksPainter).

² All coefficients of polynomials are rational numbers. But the coefficients are sometimes approximated in decimal forms when there is not enough margin.

I.
$$I_1^u = \langle -1.06 \times 10^{17} u^{53} - 3.57 \times 10^{17} u^{52} + \dots + 7.54 \times 10^{16} b + 4.04 \times 10^{16}, \ 1.03 \times 10^{17} u^{53} + 3.61 \times 10^{17} u^{52} + \dots + 7.54 \times 10^{16} a - 5.96 \times 10^{17}, \ u^{54} + 4u^{53} + \dots - 13u - 1 \rangle$$

(i) Arc colorings

$$a_{9} = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} 1 \\ -u^{2} \end{pmatrix}$$

$$a_{8} = \begin{pmatrix} u^{2} + 1 \\ -u^{4} - 2u^{2} \end{pmatrix}$$

$$a_{4} = \begin{pmatrix} -1.35974u^{53} - 4.78764u^{52} + \dots + 20.4946u + 7.89891 \\ 1.40141u^{53} + 4.73538u^{52} + \dots - 10.6807u - 0.536168 \end{pmatrix}$$

$$a_{7} = \begin{pmatrix} -u^{3} - 2u \\ u^{3} + u \end{pmatrix}$$

$$a_{3} = \begin{pmatrix} 0.267734u^{53} + 0.167743u^{52} + \dots + 2.48003u + 6.45689 \\ -0.218764u^{53} - 0.990227u^{52} + \dots + 3.51913u + 0.584554 \end{pmatrix}$$

$$a_{6} = \begin{pmatrix} 0.166746u^{53} + 0.935589u^{52} + \dots - 14.0641u - 4.81630 \\ 0.693852u^{53} + 2.26828u^{52} + \dots - 3.45221u - 0.695131 \end{pmatrix}$$

$$a_{5} = \begin{pmatrix} 0.166746u^{53} + 0.935589u^{52} + \dots - 14.0641u - 4.81630 \\ 0.629304u^{53} + 2.35002u^{52} + \dots - 7.11080u - 0.963735 \end{pmatrix}$$

$$a_{2} = \begin{pmatrix} -1.06576u^{53} - 3.70343u^{52} + \dots + 13.6083u + 5.08949 \\ 0.272628u^{53} + 0.559742u^{52} + \dots + 6.49074u + 0.762024 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} -u^{6} - 3u^{4} - 2u^{2} + 1 \\ u^{8} + 4u^{6} + 4u^{4} \end{pmatrix}$$

(ii) Obstruction class = -1

(iii) Cusp Shapes

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
c_1	$u^{54} + 32u^{53} + \dots + u + 1$
c_2, c_4	$u^{54} - 4u^{53} + \dots - 7u + 1$
c_3, c_6	$u^{54} - 4u^{53} + \dots + 5u - 1$
c_5,c_9	$u^{54} + 3u^{53} + \dots + 1024u + 512$
c_7	$u^{54} - 4u^{53} + \dots - 37353u - 3137$
c_8, c_{11}, c_{12}	$u^{54} + 4u^{53} + \dots - 13u - 1$
c_{10}	$u^{54} + 8u^{53} + \dots - 5325u + 99$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
c_1	$y^{54} - 16y^{53} + \dots + 283y + 1$
c_{2}, c_{4}	$y^{54} - 32y^{53} + \dots - y + 1$
c_3, c_6	$y^{54} + 12y^{53} + \dots - y + 1$
c_5,c_9	$y^{54} - 49y^{53} + \dots - 9830400y + 262144$
c_7	$y^{54} + 20y^{53} + \dots - 1173862245y + 9840769$
c_8, c_{11}, c_{12}	$y^{54} + 52y^{53} + \dots - 133y + 1$
c_{10}	$y^{54} + 48y^{53} + \dots - 31673313y + 9801$

(vi) Complex Volumes and Cusp Shapes

Solutions to I_1^u	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
u = -0.634596 + 0.687676I		
a = -1.74382 - 0.72872I	-6.73797 + 6.00183I	-5.20384 - 3.02358I
b = 0.550252 - 0.214317I		
u = -0.634596 - 0.687676I		
a = -1.74382 + 0.72872I	-6.73797 - 6.00183I	-5.20384 + 3.02358I
b = 0.550252 + 0.214317I		
u = -0.795857 + 0.397748I		
a = 1.38136 + 1.64625I	-5.79563 - 10.85900I	-3.40249 + 7.71802I
b = -1.02366 - 1.50366I		
u = -0.795857 - 0.397748I		
a = 1.38136 - 1.64625I	-5.79563 + 10.85900I	-3.40249 - 7.71802I
b = -1.02366 + 1.50366I		
u = 0.819414 + 0.164591I		
a = 0.045931 + 0.903156I	1.37542 + 1.07510I	6.59040 - 4.82915I
b = -0.032318 - 0.835765I		
u = 0.819414 - 0.164591I		
a = 0.045931 - 0.903156I	1.37542 - 1.07510I	6.59040 + 4.82915I
b = -0.032318 + 0.835765I		
u = 0.561613 + 0.609285I		
a = 0.283506 + 0.301159I	-0.18821 + 3.22155I	0.22182 - 9.88990I
b = 0.177288 + 0.107732I		
u = 0.561613 - 0.609285I		
a = 0.283506 - 0.301159I	-0.18821 - 3.22155I	0.22182 + 9.88990I
b = 0.177288 - 0.107732I		
u = 0.236983 + 1.152610I		
a = 0.515739 + 0.748797I	-1.41186 + 2.56239I	0
b = 1.131300 - 0.506978I		
u = 0.236983 - 1.152610I		
a = 0.515739 - 0.748797I	-1.41186 - 2.56239I	0
b = 1.131300 + 0.506978I		

Solutions to I_1^u	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
u = -0.679423 + 0.455165I		
a = -1.58385 - 1.13509I	-6.34508 - 3.77283I	-4.72884 + 3.96733I
b = 0.366509 + 0.385296I		
u = -0.679423 - 0.455165I		
a = -1.58385 + 1.13509I	-6.34508 + 3.77283I	-4.72884 - 3.96733I
b = 0.366509 - 0.385296I		
u = -0.640093 + 0.500351I		
a = 1.67652 + 1.12666I	-6.52207 - 0.60653I	-5.07523 + 2.49392I
b = -0.94179 - 1.13103I		
u = -0.640093 - 0.500351I		
a = 1.67652 - 1.12666I	-6.52207 + 0.60653I	-5.07523 - 2.49392I
b = -0.94179 + 1.13103I		
u = -0.708133 + 0.388182I		
a = -1.33746 - 1.33573I	-2.10088 - 5.47985I	-0.81647 + 5.41146I
b = 0.90008 + 1.37571I		
u = -0.708133 - 0.388182I		
a = -1.33746 + 1.33573I	-2.10088 + 5.47985I	-0.81647 - 5.41146I
b = 0.90008 - 1.37571I		
u = -0.550906 + 0.548792I		
a = 1.53049 + 0.91002I	-2.76018 + 1.24868I	-2.45680 + 0.23951I
b = -0.231683 - 0.023654I		
u = -0.550906 - 0.548792I		
a = 1.53049 - 0.91002I	-2.76018 - 1.24868I	-2.45680 - 0.23951I
b = -0.231683 + 0.023654I		
u = -0.086880 + 1.268120I		
a = 0.059220 + 0.170114I	0.081517 + 1.100590I	0
b = 1.95815 + 1.14512I		
u = -0.086880 - 1.268120I		
a = 0.059220 - 0.170114I	0.081517 - 1.100590I	0
b = 1.95815 - 1.14512I		

Solutions to I_1^u	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
u = 0.222821 + 1.287610I		
a = -0.70821 + 2.27425I	-4.30040 + 3.00237I	0
b = 2.58514 - 0.05556I		
u = 0.222821 - 1.287610I		
a = -0.70821 - 2.27425I	-4.30040 - 3.00237I	0
b = 2.58514 + 0.05556I		
u = 0.045291 + 1.336850I		
a = -0.200212 - 0.862703I	-4.94061 + 0.29567I	0
b = -0.322922 + 0.424548I		
u = 0.045291 - 1.336850I		
a = -0.200212 + 0.862703I	-4.94061 - 0.29567I	0
b = -0.322922 - 0.424548I		
u = -0.120353 + 1.342440I		
a = 0.1148610 + 0.0757838I	-0.65798 - 4.90905I	0
b = -2.37287 - 1.45094I		
u = -0.120353 - 1.342440I		
a = 0.1148610 - 0.0757838I	-0.65798 + 4.90905I	0
b = -2.37287 + 1.45094I		
u = 0.403137 + 1.291980I		
a = -0.494203 - 0.685022I	-3.12056 + 5.51965I	0
b = -0.690162 + 0.956126I		
u = 0.403137 - 1.291980I		
a = -0.494203 + 0.685022I	-3.12056 - 5.51965I	0
b = -0.690162 - 0.956126I		
u = 0.596526 + 0.197093I		
a = 0.751854 + 0.525078I	1.36345 + 0.70118I	5.37506 - 2.07743I
b = -0.421332 - 0.698708I		
u = 0.596526 - 0.197093I		
a = 0.751854 - 0.525078I	1.36345 - 0.70118I	5.37506 + 2.07743I
b = -0.421332 + 0.698708I		

Solutions to I_1^u	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
u = 0.117312 + 1.368590I		
a = 0.561185 - 1.109220I	-6.00610 + 2.39609I	0
b = -3.04338 + 0.04770I		
u = 0.117312 - 1.368590I		
a = 0.561185 + 1.109220I	-6.00610 - 2.39609I	0
b = -3.04338 - 0.04770I		
u = 0.203162 + 1.375440I		
a = -0.469730 + 0.300689I	-3.65451 + 3.54341I	0
b = -0.058931 + 0.766086I		
u = 0.203162 - 1.375440I		
a = -0.469730 - 0.300689I	-3.65451 - 3.54341I	0
b = -0.058931 - 0.766086I		
u = 0.608391		
a = 5.71602	-0.276662	-47.3490
b = -3.05948		
u = -0.26697 + 1.46380I		
a = -0.075844 + 1.074870I	-8.06847 - 9.04274I	0
b = -2.17970 - 2.22655I		
u = -0.26697 - 1.46380I		
a = -0.075844 - 1.074870I	-8.06847 + 9.04274I	0
b = -2.17970 + 2.22655I		
u = -0.18633 + 1.48277I		
a = -0.255172 - 0.913294I	-9.29015 - 1.40800I	0
b = 0.40684 + 1.63138I		
u = -0.18633 - 1.48277I		
a = -0.255172 + 0.913294I	-9.29015 + 1.40800I	0
b = 0.40684 - 1.63138I		
u = -0.24427 + 1.48405I		
a = 0.129853 + 1.010100I	-12.6206 - 7.1463I	0
b = -0.43559 - 1.87912I		

Solutions to I_1^u	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
u = -0.24427 - 1.48405I		
a = 0.129853 - 1.010100I	-12.6206 + 7.1463I	0
b = -0.43559 + 1.87912I		
u = -0.22098 + 1.49116I		
a = -0.269071 - 1.035350I	-12.97630 - 3.73907I	0
b = 2.54361 + 2.25570I		
u = -0.22098 - 1.49116I		
a = -0.269071 + 1.035350I	-12.97630 + 3.73907I	0
b = 2.54361 - 2.25570I		
u = -0.30297 + 1.47888I		
a = 0.215622 - 1.288750I	-11.8373 - 14.8592I	0
b = 1.97823 + 2.43175I		
u = -0.30297 - 1.47888I		
a = 0.215622 + 1.288750I	-11.8373 + 14.8592I	0
b = 1.97823 - 2.43175I		
u = 0.20848 + 1.51432I		
a = -0.210573 - 0.018611I	-7.05949 + 6.12156I	0
b = 0.793889 - 0.374873I		
u = 0.20848 - 1.51432I		
a = -0.210573 + 0.018611I	-7.05949 - 6.12156I	0
b = 0.793889 + 0.374873I		
u = -0.14867 + 1.55204I		
a = 0.439962 + 0.955922I	-14.2294 + 3.2886I	0
b = -0.73812 - 1.45641I		
u = -0.14867 - 1.55204I		
a = 0.439962 - 0.955922I	-14.2294 - 3.2886I	0
b = -0.73812 + 1.45641I		
u = -0.436472 + 0.052368I		
a = -0.264450 + 0.059841I	3.76413 - 2.96919I	-10.33792 + 6.38001I
b = 0.14420 + 1.41205I		

Solutions to I_1^u	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
u = -0.436472 - 0.052368I		
a = -0.264450 - 0.059841I	3.76413 + 2.96919I	-10.33792 - 6.38001I
b = 0.14420 - 1.41205I		
u = 0.350769 + 0.150602I		
a = -3.77033 - 1.02650I	-1.153000 + 0.650417I	-5.27115 + 2.78805I
b = 1.286240 + 0.476185I		
u = 0.350769 - 0.150602I		
a = -3.77033 + 1.02650I	-1.153000 - 0.650417I	-5.27115 - 2.78805I
b = 1.286240 - 0.476185I		
u = -0.0936295		
a = 5.63764	-1.01364	-10.3540
b = 0.400918		

II.
$$I_2^u = \langle au - u^2 + b + a, -u^2a + a^2 + 1, u^3 - u^2 + 2u - 1 \rangle$$

(i) Arc colorings

$$a_{9} = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} -u \\ -u^{2} \end{pmatrix}$$

$$a_{8} = \begin{pmatrix} u^{2} + 1 \\ -u^{2} + u - 1 \end{pmatrix}$$

$$a_{1} = \begin{pmatrix} u^{2} + 1 \\ -u^{2} + u - 1 \end{pmatrix}$$

$$a_{4} = \begin{pmatrix} a \\ -au + u^{2} - a \end{pmatrix}$$

$$a_{7} = \begin{pmatrix} -u^{2} - 1 \\ u^{2} - u + 1 \end{pmatrix}$$

$$a_{3} = \begin{pmatrix} -u^{2}a + au - a + u \\ -au \end{pmatrix}$$

$$a_{6} = \begin{pmatrix} 0 \\ au - u^{2} - a + 2u - 2 \end{pmatrix}$$

$$a_{5} = \begin{pmatrix} 0 \\ au - u^{2} - a + 2u - 2 \end{pmatrix}$$

$$a_{2} = \begin{pmatrix} -u^{2}a + au - a + u \\ -2u^{2} + 2u - 2 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

- (ii) Obstruction class = 1
- (iii) Cusp Shapes = $-6u^2a + 2au + 2u^2 + a 3u + 10$

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
c_1, c_3, c_{11} c_{12}	$(u^3 - u^2 + 2u - 1)^2$
c_2	$(u^3 + u^2 - 1)^2$
c_4, c_7, c_{10}	$(u^3 - u^2 + 1)^2$
c_5, c_9	u^6
c_{6}, c_{8}	$(u^3 + u^2 + 2u + 1)^2$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
c_1, c_3, c_6 c_8, c_{11}, c_{12}	$(y^3 + 3y^2 + 2y - 1)^2$
c_2, c_4, c_7 c_{10}	$(y^3 - y^2 + 2y - 1)^2$
c_5, c_9	y^6

(vi) Complex Volumes and Cusp Shapes

Solutions to I_2^u	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
u = 0.215080 + 1.307140I		
a = -0.500000 - 0.424452I	5.65624I	0.00556 - 7.25775I
b = -1.60964 + 1.73159I		
u = 0.215080 + 1.307140I		
a = -1.16236 + 0.98673I	-4.13758 + 2.82812I	-6.47655 + 9.33882I
b = 1.039800 + 0.882689I		
u = 0.215080 - 1.307140I		
a = -0.500000 + 0.424452I	-5.65624I	0.00556 + 7.25775I
b = -1.60964 - 1.73159I		
u = 0.215080 - 1.307140I		
a = -1.16236 - 0.98673I	-4.13758 - 2.82812I	-6.47655 - 9.33882I
b = 1.039800 - 0.882689I		
u = 0.569840		
a = 0.162359 + 0.986732I	4.13758 + 2.82812I	8.97099 + 0.18883I
b = 0.06984 - 1.54901I		
u = 0.569840		
a = 0.162359 - 0.986732I	4.13758 - 2.82812I	8.97099 - 0.18883I
b = 0.06984 + 1.54901I		

III.
$$I_3^u = \langle u^2 + b + u, -u^2 + a - 2, u^3 - u^2 + 2u - 1 \rangle$$

(i) Arc colorings

$$a_{9} = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} -u \\ -u^{2} \end{pmatrix}$$

$$a_{8} = \begin{pmatrix} -u \\ u^{2} - u + 1 \end{pmatrix}$$

$$a_{1} = \begin{pmatrix} u^{2} + 1 \\ -u^{2} + u - 1 \end{pmatrix}$$

$$a_{4} = \begin{pmatrix} u^{2} + 2 \\ -u^{2} - u \end{pmatrix}$$

$$a_{7} = \begin{pmatrix} -u^{2} - 1 \\ u^{2} - u + 1 \end{pmatrix}$$

$$a_{3} = \begin{pmatrix} -u^{2} - 1 \\ u^{2} - u + 3 \\ -u^{2} - 1 \end{pmatrix}$$

$$a_{6} = \begin{pmatrix} 0 \\ -u^{2} + u \end{pmatrix}$$

$$a_{5} = \begin{pmatrix} 0 \\ -u^{2} + u \end{pmatrix}$$

$$a_{2} = \begin{pmatrix} 2u^{2} - u + 3 \\ -2u^{2} + 2u - 2 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

- (ii) Obstruction class = 1
- (iii) Cusp Shapes = $4u^2 3u + 4$

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
c_1, c_3, c_{11} c_{12}	$u^3 - u^2 + 2u - 1$
c_2	$u^3 + u^2 - 1$
c_4, c_7, c_{10}	$u^3 - u^2 + 1$
c_5, c_9	u^3
c_{6}, c_{8}	$u^3 + u^2 + 2u + 1$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
c_1, c_3, c_6 c_8, c_{11}, c_{12}	$y^3 + 3y^2 + 2y - 1$
c_2, c_4, c_7 c_{10}	$y^3 - y^2 + 2y - 1$
c_5, c_9	y^3

(vi) Complex Volumes and Cusp Shapes

Solutions to I_3^u	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
u = 0.215080 + 1.307140I		
a = 0.337641 + 0.562280I	0	-3.29468 - 1.67231I
b = 1.44728 - 1.86942I		
u = 0.215080 - 1.307140I		
a = 0.337641 - 0.562280I	0	-3.29468 + 1.67231I
b = 1.44728 + 1.86942I		
u = 0.569840		
a = 2.32472	0	3.58940
b = -0.894558		

IV. u-Polynomials

Crossings	u-Polynomials at each crossing
c_1	$((u^3 - u^2 + 2u - 1)^3)(u^{54} + 32u^{53} + \dots + u + 1)$
c_2	$((u^3 + u^2 - 1)^3)(u^{54} - 4u^{53} + \dots - 7u + 1)$
c_3	$((u^3 - u^2 + 2u - 1)^3)(u^{54} - 4u^{53} + \dots + 5u - 1)$
c_4	$((u^3 - u^2 + 1)^3)(u^{54} - 4u^{53} + \dots - 7u + 1)$
c_5, c_9	$u^9(u^{54} + 3u^{53} + \dots + 1024u + 512)$
<i>C</i> ₆	$((u^3 + u^2 + 2u + 1)^3)(u^{54} - 4u^{53} + \dots + 5u - 1)$
c_7	$((u^3 - u^2 + 1)^3)(u^{54} - 4u^{53} + \dots - 37353u - 3137)$
c ₈	$((u^3 + u^2 + 2u + 1)^3)(u^{54} + 4u^{53} + \dots - 13u - 1)$
c_{10}	$((u^3 - u^2 + 1)^3)(u^{54} + 8u^{53} + \dots - 5325u + 99)$
c_{11}, c_{12}	$((u^3 - u^2 + 2u - 1)^3)(u^{54} + 4u^{53} + \dots - 13u - 1)$

V. Riley Polynomials

Crossings	Riley Polynomials at each crossing
c_1	$((y^3 + 3y^2 + 2y - 1)^3)(y^{54} - 16y^{53} + \dots + 283y + 1)$
c_{2}, c_{4}	$((y^3 - y^2 + 2y - 1)^3)(y^{54} - 32y^{53} + \dots - y + 1)$
c_3, c_6	$((y^3 + 3y^2 + 2y - 1)^3)(y^{54} + 12y^{53} + \dots - y + 1)$
c_5,c_9	$y^9(y^{54} - 49y^{53} + \dots - 9830400y + 262144)$
c_7	$((y^3 - y^2 + 2y - 1)^3)(y^{54} + 20y^{53} + \dots - 1.17386 \times 10^9y + 9840769)$
c_8, c_{11}, c_{12}	$((y^3 + 3y^2 + 2y - 1)^3)(y^{54} + 52y^{53} + \dots - 133y + 1)$
c_{10}	$((y^3 - y^2 + 2y - 1)^3)(y^{54} + 48y^{53} + \dots - 31673313y + 9801)$