Applications for Linear Data Structures CMPT 145

Bracket matching

- In a mathematical expression, we use brackets to indicate order of operations.
- Every open bracket must have a close bracket.

Matched: $(3+4) \times 5$ Unmatched: $(3+4) \times 5$ Unmatched: $3+4) \times 5$

• We allow brackets to be nested.

Matched: $((3+4) \times 5)$

Bracket Checking Problem

- Given: A string representing a mathematical expression
- Return: True if the brackets match properly, False otherwise.

True: $(3+4) \times 5$

True: $((3+4) \times 5)$

False: $(3+4\times5)$

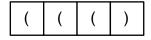
False: $3+4) \times 5$

Bracket Checking Algorithm

- Scan the text from the beginning character by character
 - If the current character is '(' push it on the stack.
 - If the current character is ')':
 - If you can pop the stack, do so. The ')' matches your stored '('.
 - If you cannot pop the stack, the ')' is unmatched.
 - If the current character is anything else, ignore it.
- If you reached the end of the text, and the stack is not empty, you have one or more unmatched '('.

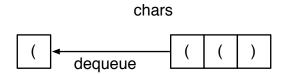
Visualizing the algorithm - Initially

chars



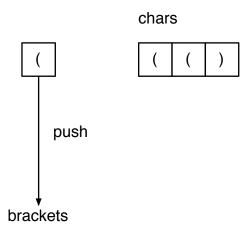
brackets

Visualizing the algorithm - First dequeue



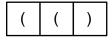
brackets

Visualizing the algorithm - First push



Visualizing the algorithm - After first push

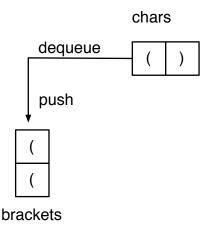
chars



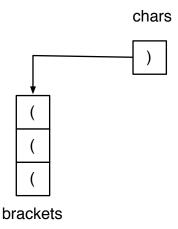


brackets

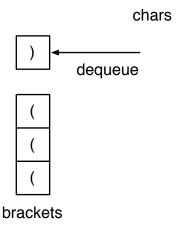
Visualizing the algorithm - Dequeue and push



Visualizing the algorithm - Dequeue and push

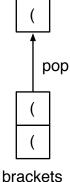


Visualizing the algorithm - Finding ')'



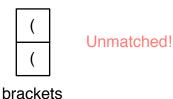
Visualizing the algorithm - Pop





Visualizing the algorithm - Empty queue

chars (empty)



Demo

Thinking about bracket checking

- Why do we use a LIFO stack to store '('?
- Could we use a FIFO gueue instead?
- Why do we use a FIFO queue to store ')'?

Doing arithmetic without brackets at all!

- Normally, we write arithmetic expressions like this: $((a+b)\times(c+d))\times e$.
- We use the brackets to indicate the order of operations.
- We don't need brackets at all, if we use something called *postfix notation*.
- Here's the same expression, using postfix notation.

$$a b + c d + \times e \times$$

Looks weird, but here's how to read it (left to right):

$$\underbrace{a \ b + c \ d + \times}_{e \times e} e \times$$

No brackets needed. Ever.

Post-fix examples

The following expression evaluates to 7:

$$34 +$$

The following expression evaluates to 12:

$$3.4 \times$$

The following expression evaluates to 8:

$$124 -$$

The following example evaluates to 42:

$$34 \times 56 \times +$$

Demo

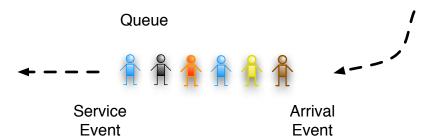
Queueing Simulation

- Assumption: Customers arrive randomly.
- Assumption: Service takes random amount of time.
- Question: How long do customers wait?

Key ideas

- Model the customers' arrival with an average arrival rate (customers per minute).
- Model the service time with an average service rate (customers per minute).
- Keep track of 3 things:
 - 1. Time of next customer arrival ("arrival event")
 - 2. Time of next customer service ("service event")
 - 3. The arrival times of customers who are waiting (queue)
- Time advances to the next event (not by a ticking clock)

Overview



The simulation algorithm

- Schedule the first arrival event
- Schedule the first service event
- Repeat:
 - While an arrival event must happen before a service event:
 - Enqueue the current arrival event
 - Schedule the next arrival event.
 - Handle the service event (e.g., calculate wait time)
 - Schedule the next service event:
 - If there is a customer waiting, start service immediately
 - Otherwise, start after the next customer arrives

Demo

Visualizing the algorithm - Initially

Queue

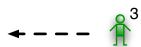
Service Event

nextService = 3 + 2

Arrival Event

First arrival

Queue



Service **Event**

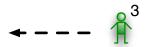
nextService = 5



Arrival **Event**

Schedule the next arrival

Queue



Service Event

nextService = 5



Arrival Event

nextArrival = 3+1

Second arrival





Service Event

nextService = 5



Arrival Event

Schedule the next arrival





Service Event

nextService = 5



Arrival Event

nextArrival = 4+2

First service complete





Service Event

nextService = 5



Arrival Event

Schedule the next service

Queue



Service Event

nextService = 5+2



Arrival Event

Arrival





Service Event

nextService = 7



Arrival Event

Schedule the next arrival





Service Event

nextService = 7



Arrival Event

nextArrival = 6+1

Service complete





Service Event

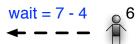
nextService = 7



Arrival Event

Schedule the next service

Queue



Service Event

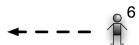
nextService = 7 + 5



Arrival Event

Clock advances to next arrival

Queue



Service Event

nextService = 12



Arrival Event

Arrival and schedule next arrival





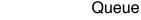
nextService = 12



Arrival Event

nextArrival = 7+2

Clock advances to next arrival





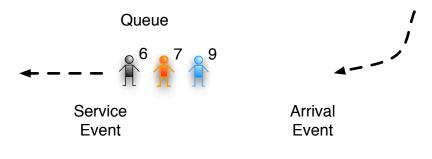
Service Event

nextService = 12



Arrival Event

Arrival and schedule next arrival



nextService = 12

nextArrival = 9+3

Service complete and schedule next service



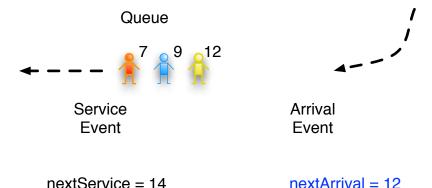
Service Event

nextService = 12+2



Arrival Event

Clock advances to next arrival



Linear ADTs: Queues and Stacks

- Interesting algorithms make use of stacks and queues!
- ADTs provide a useful abstraction to computational concepts
- You could implement all the algorithms without using ADTs, but
 - The ADT helps document the intentions of the program
 - The limited set of operations help prevent errors
 - Resulting code is much clearer