



Uber and Lyft prices prediction

STATISTICAL LEARNING FINAL PROJECT

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2039097

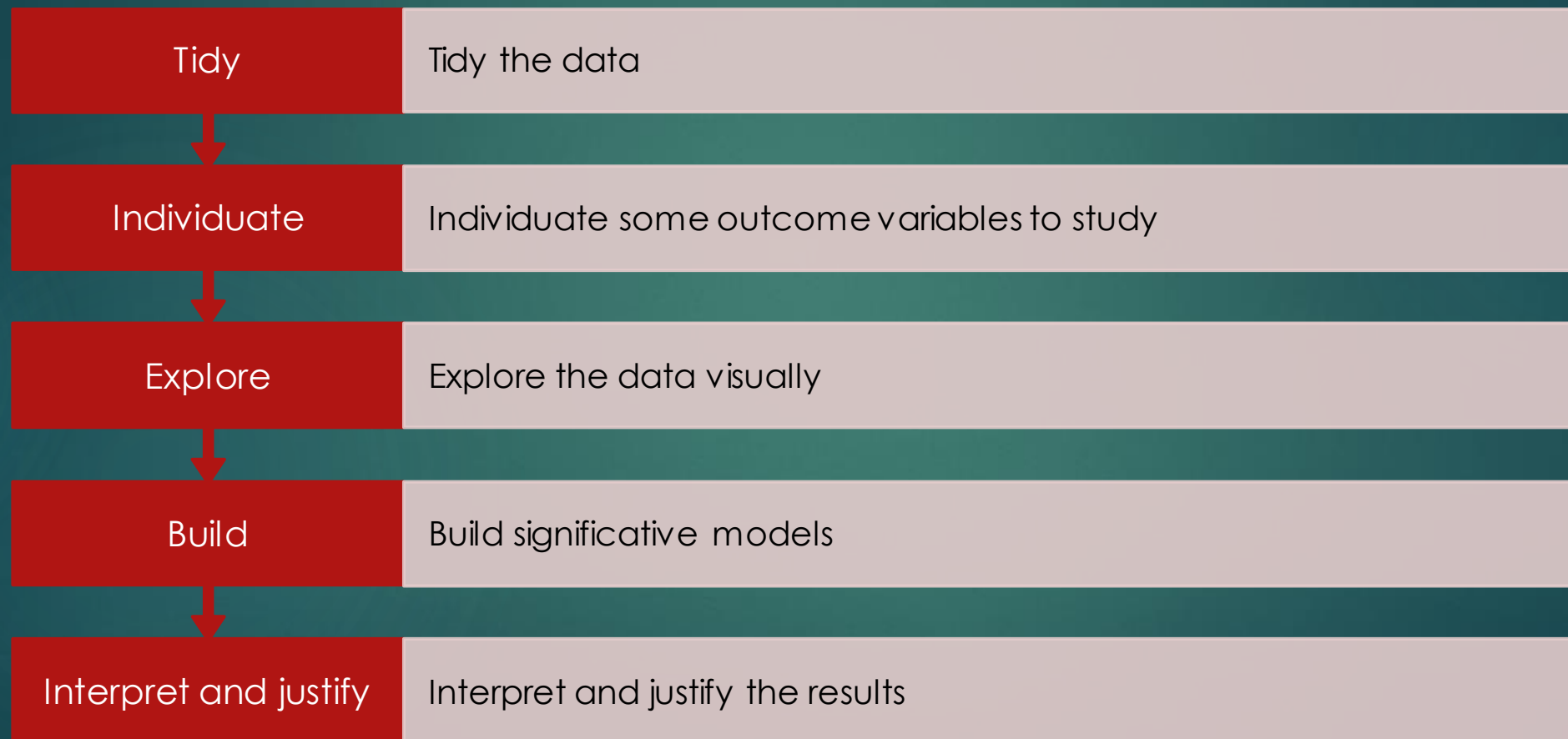
Obtaining Data

Source: Kaggle

Data collection: Website of
Massachusetts State, USA

Data set of size 693,071
rows and 57 columns

Outline of the project:



Features in Data Set

- ▶ The rideshare dataset contain 56 features:
- ▶ "id", "timestamp", "hour", "day", "month", "datetime", "timezone", "source", "destination", "cab_type", "product_id", "name", "price", "distance", "surge_multiplier", "latitude", "longitude", "sunriseTime", "uvIndexTime", "sunsetTime", "short_summary", "long_summary", "windGustTime", "icon"
- ▶ "visibility", "dewpoint", "pressure", "windBearing", "cloudCover", "uvIndex", "ozone", "moonPhase", "preciplIntensityMax", "preciplntesity", "precipProbability", "humidity", "windSpeed", "windGust", "visibility.1"
- ▶ "temperatureMin", "temperatureMinTime", "temperatureMax", "temperatureMaxTime", "apparentTemperatureMin", "apparentTemperatureMinTime", "apparentTemperatureMax", "apparentTemperatureMaxTime", "temperature", "temperatureHigh", "temperatureHighTime", "temperatureLow", "apparentTempertaure", "temperatureLowTime".

Climate
Related
features

Temperature
related
features

❖ Clean & Filter Data(Pre-processing)

- ▶ Initially, checks for NAN, infinite values, and missing values are done and 55,095 missing values are present in the data which are omitted.
- ▶ Both “visibility” and “visibility.1” features have exactly the same data in their columns one of them is dropped.
- ▶ Checks for skewness are done on all numeric features and 15 features are found to be negatively skewed and 26 features are found to be positively skewed.
- ▶ Since skewness is greater than 3 for "surge_multiplier" and "precipIntensity" features we apply cube root transformation is applied to normalize and reduce the skewness of the features.

Clean & Filter Data(Pre- processing)

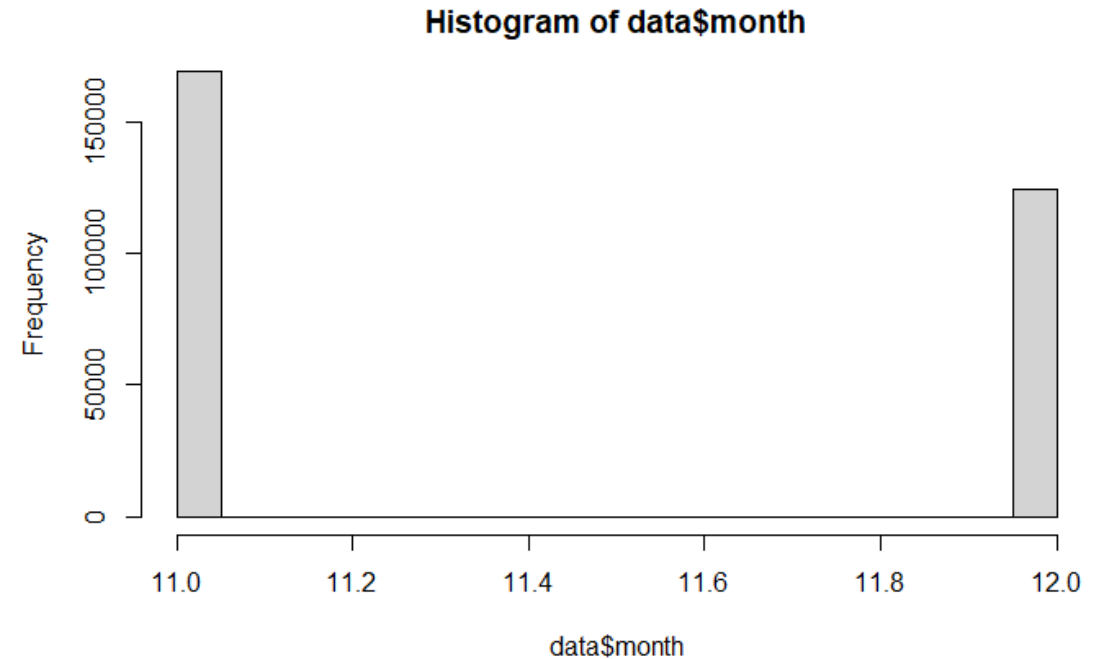
- ▶ Outliers are found by using the interquartile range.
- ▶ Features whose outliers(>10%) are:
- ▶ latitude \leftarrow **0.127 %**
- ▶ Visibility \leftarrow **0.197 %**
- ▶ temperatureHigh \leftarrow **0.236 %**
- ▶ apparentTemperatureHigh \leftarrow **0.103 %**
- ▶ apparentTemperatureLow \leftarrow **0.126 %**
- ▶ temperatureMax \leftarrow **0.197 %**
- ▶ apparentTemperatureMin \leftarrow **0.109 %**
- ▶ **After deleting rows with outlier values, the final dimension used is 293877 rows and 56 columns.**

Clean & Filter Data (Pre- processing)

- ▶ There are 11 features with character datatype are:
- ▶ Id, datetime, timezone, source, destination, cab_type, product_id, name, short_summary, long_summary, icon
- ▶ Since every row of the “id” feature values are unique and every row of the “timezone” feature has the same value.
- ▶ From the above 2 features model does not learn anything so they can be discarded.
- ▶ Finally, in the feature “product_id” we have unidentified information so this feature can be dropped as well.
- ▶ Therefore, there are 8 categorical features remaining to which one hot encoding is applied to convert them to binary vectors
- ▶ Therefore, the final size of our data frame is **293,877 rows and 102 columns**

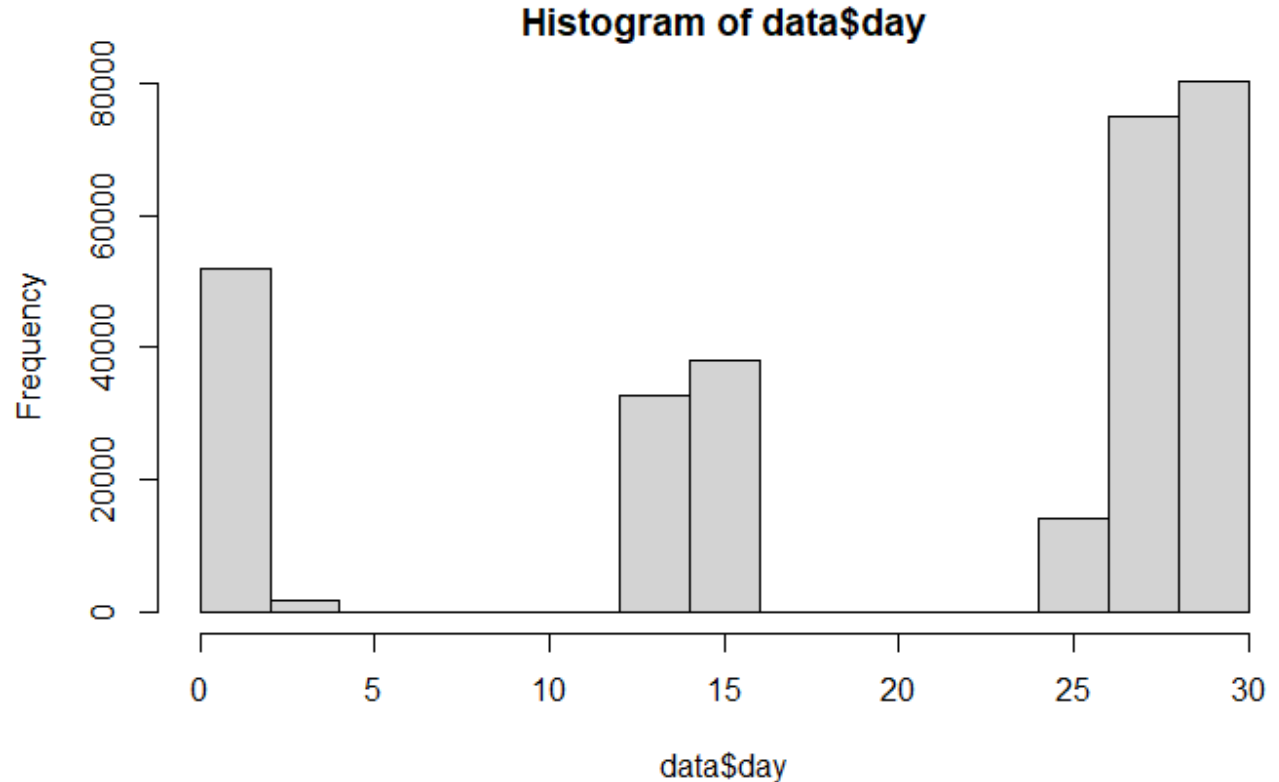
Exploratory Data Analysis (EDA)

- ▶ In which months did most of the rides occur?
- ▶ It appears that we only have November and December data in our monthly data
- ▶ November \leftarrow 169512 values
December \leftarrow 124365 values



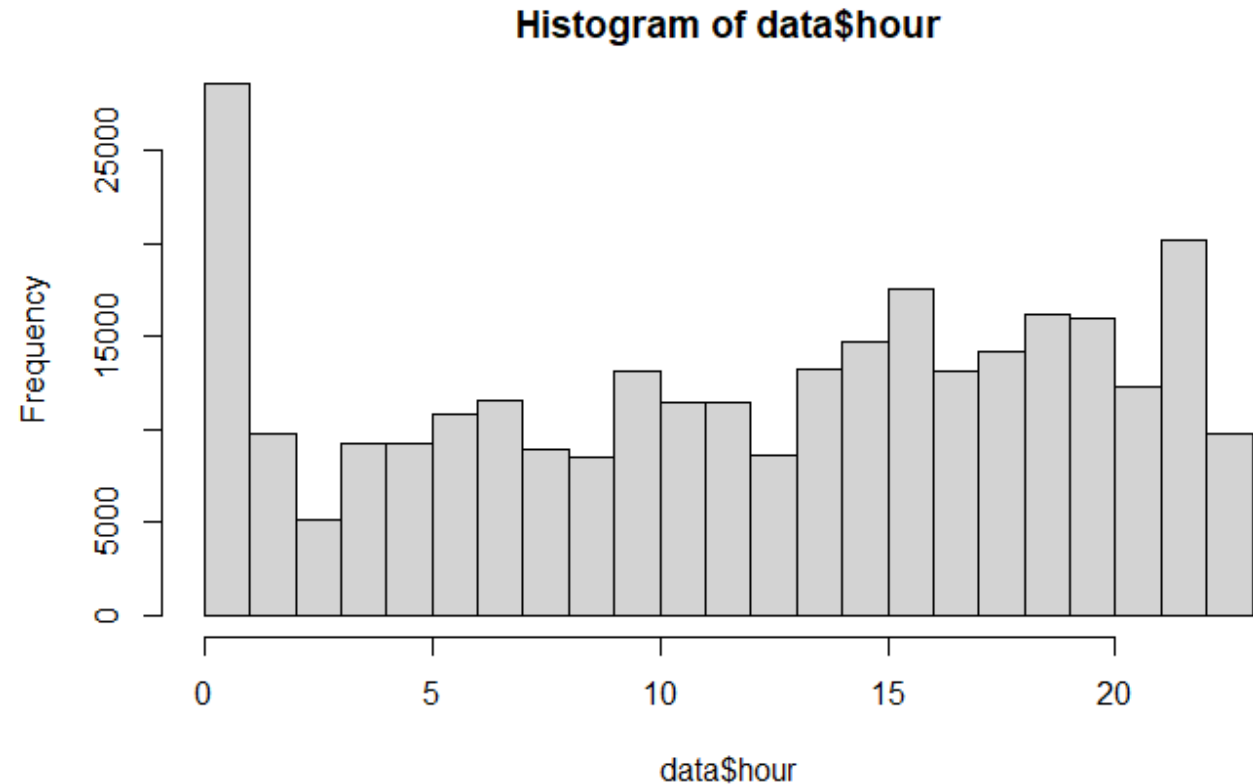
❖ Exploratory Data Analysis (EDA)

- ▶ On what dates most rides have not taken place?
- ▶ We have many gaps in data between 4th - 12th days and from 17th - 25th days data are not present in each month



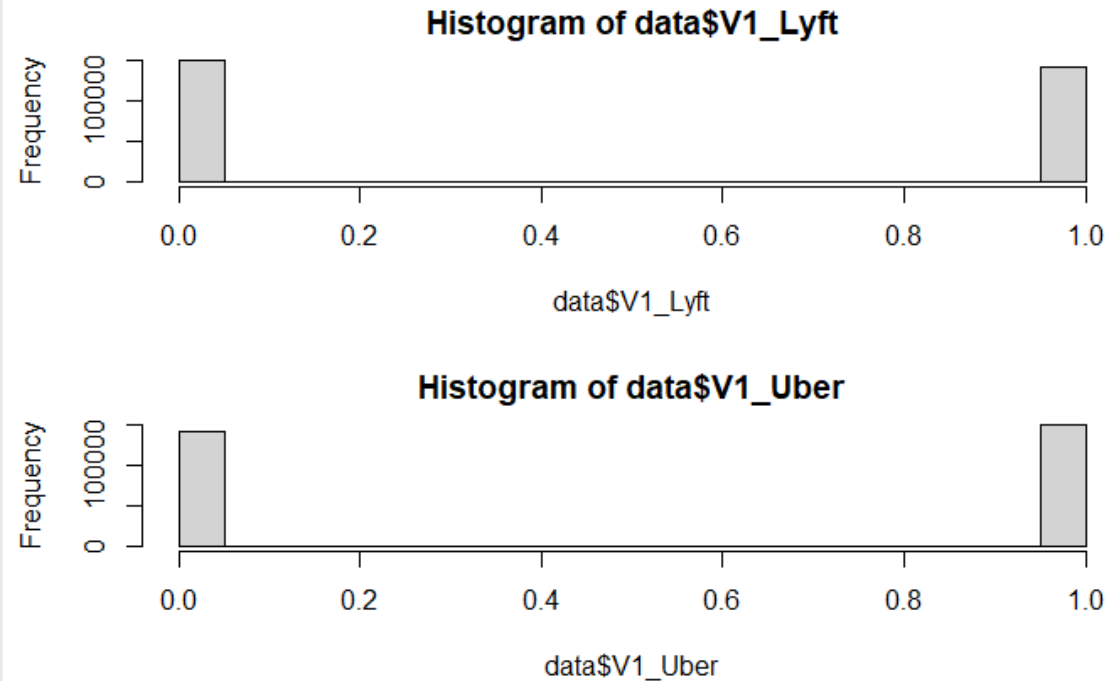
Exploratory Data Analysis (EDA)

- ▶ How many hours of data are logged?
- ▶ We have logged data of 24hrs



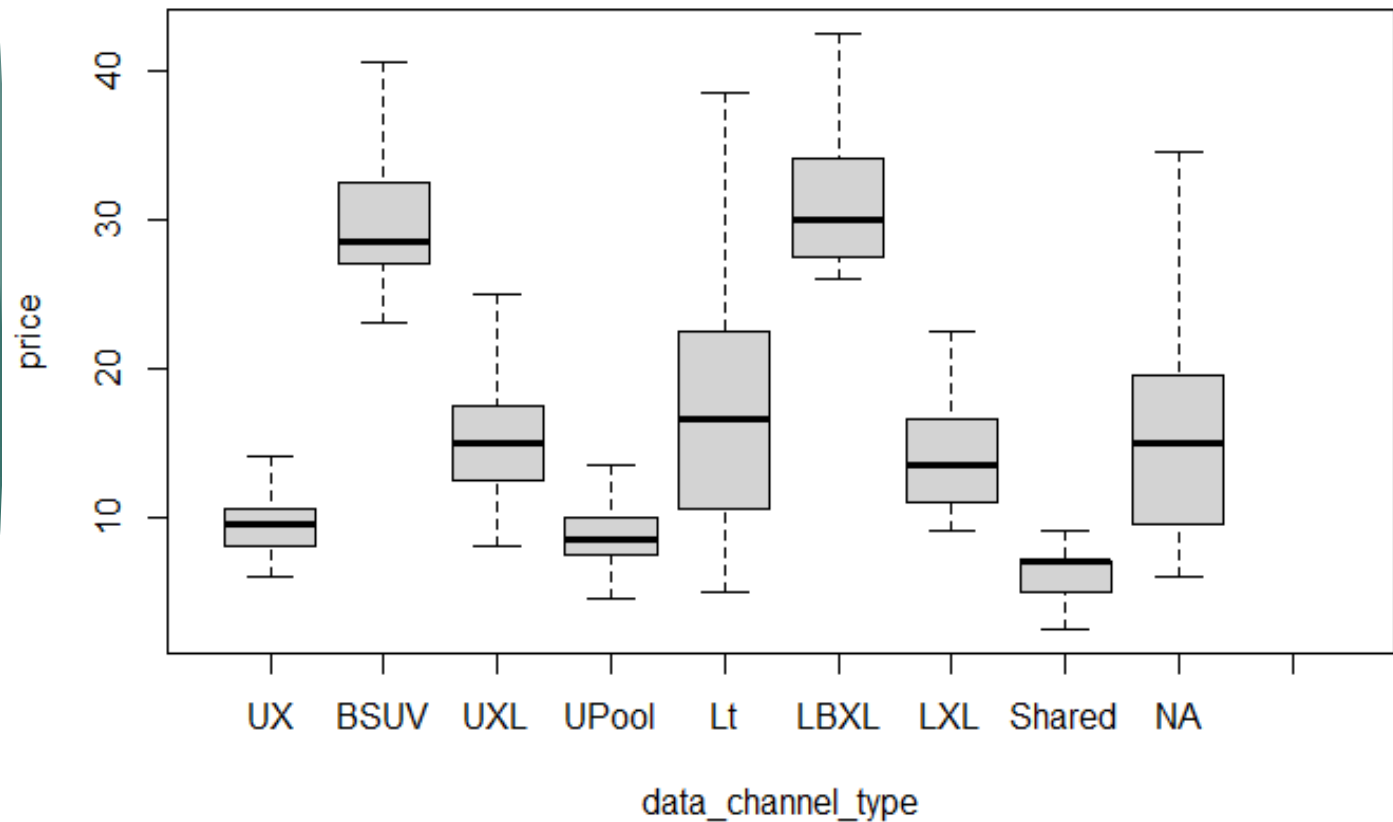
Exploratory Data Analysis (EDA)

- ▶ What company cabs are used more?
- ▶ Uber and Lyft categories have almost same size
- ▶ Uber \leftarrow 151,560 values
- ▶ Lyft \leftarrow 142,317 values



Exploratory Data Analysis (EDA)

- ▶ Which cab has best price per mile?
- ▶ Firstly, Lyft XL has a slightly lower fare per mile than UberXL.
- ▶ Uber Black SUV shows a lower rate than Lyft Black XL.
- ▶ Lyft's ordinary ride when compared to UberX has higher fares per mile.



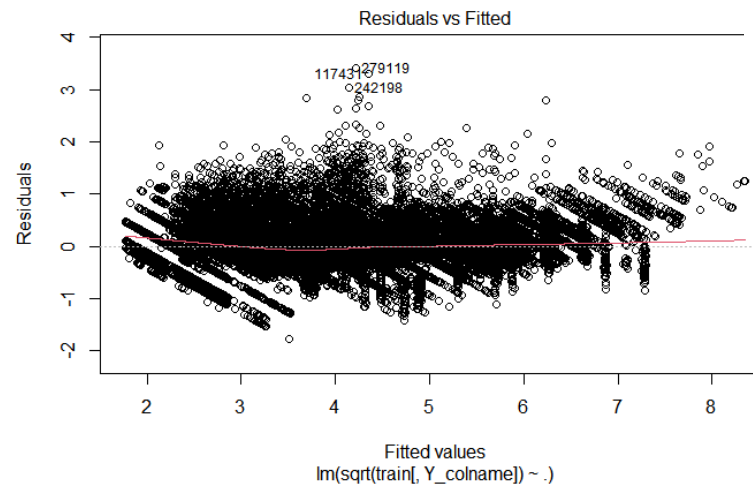
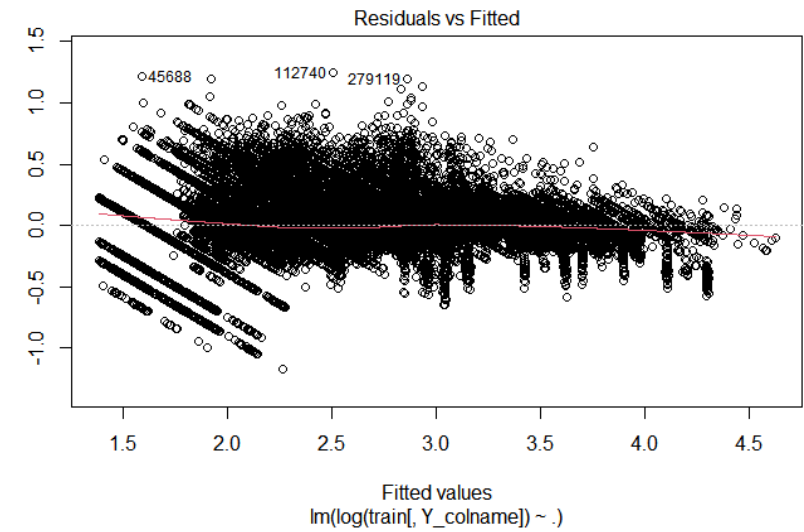
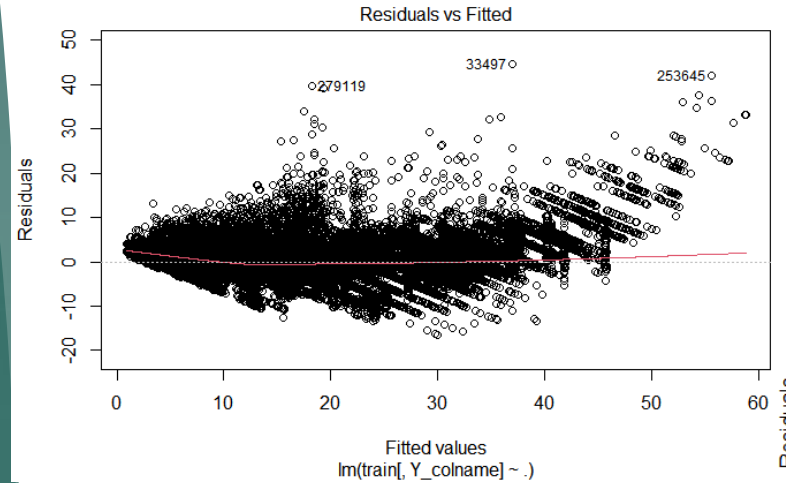
❖ Model Building

- ▶ 293,877 rows are taken and randomly split into training(60%), test(20%), and validation(20%) sets which are used to train, validate and test the model.
- ▶ Before building a linear model 4 assumptions are needed to be checked.
- ▶ The checking of assumptions are done by training 3 models below:
 - ▶ 1) linear model
 - ▶ 2) linear model with log applied
 - ▶ 3) linear model with sqrt applied

There are 4 assumptions considered for linear regression are :

1) There is a linear relationship between the predictors (x) and the outcome (y).

2) Residual Errors have a mean value of zero.



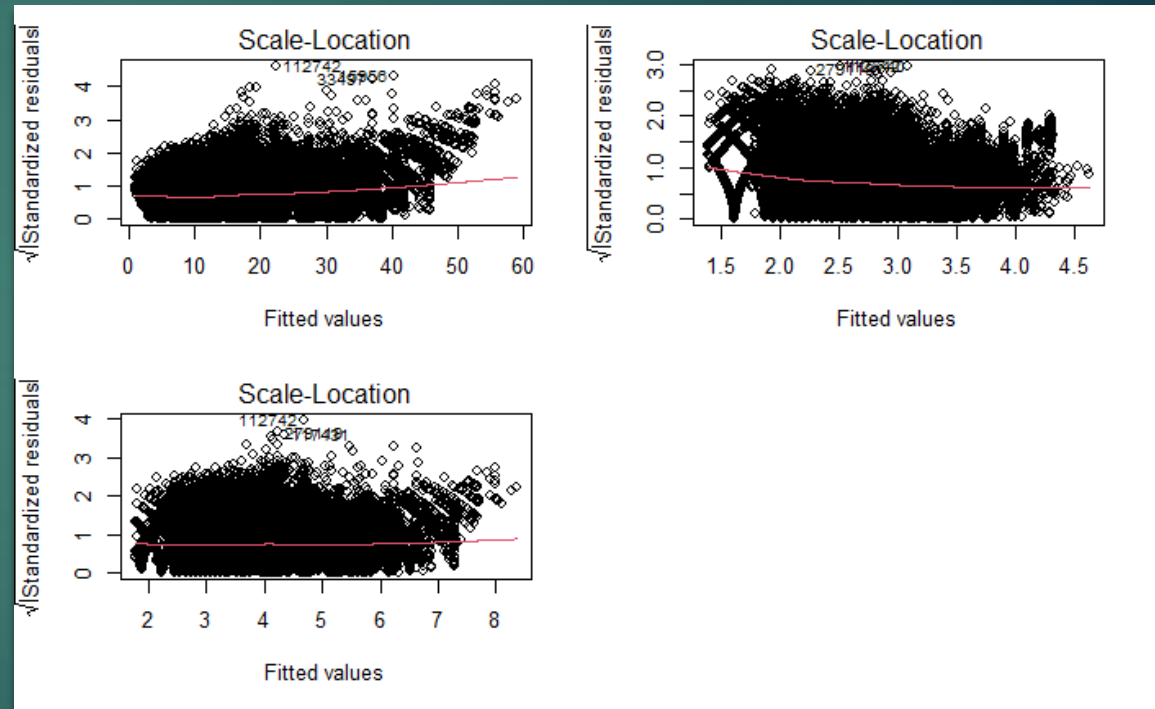
3) Predictors (x) are independent and observed with negligible error

- ▶ We use Durbin Watson test in which null hypothesis of the test states that there is no auto-correlation of residuals.
- ▶ Implicitly, our target has enough evidence and fail to reject H_0 hypotheses.
- ▶ Therefore all 3 models which we assumed have no auto correlation among their predicted variables.

```
lag Autocorrelation D-W Statistic p-value
1      -0.00428263      2.008562  0.082
Alternative hypothesis: rho != 0
lag Autocorrelation D-W Statistic p-value
1      -0.002703031     2.005401  0.282
Alternative hypothesis: rho != 0
lag Autocorrelation D-W Statistic p-value
1      -0.004471079     2.008937  0.07
Alternative hypothesis: rho != 0
```

4) Residual errors have constant variance

- ▶ The red line is roughly horizontal across the plot.
- ▶ But, to check homoscedasticity we use Breusch-Pagan Test since it is not clear from the red line that we have constant variance.



Breusch-Pagan Test

- ▶ From the output we can see that the p-value of the test is less than 0.05, we reject the null hypothesis.
- ▶ We have sufficient evidence to say that heteroscedasticity is present in the regression model which means there may be some non constant variance which is not desirable.

```
studentized Breusch-Pagan test
```


```
data:  assumption_test_model  
BP = 21247, df = 84, p-value < 2.2e-16
```

```
studentized Breusch-Pagan test
```

```
data:  assumption_test_model_log  
BP = 23192, df = 84, p-value < 2.2e-16
```

```
studentized Breusch-Pagan test
```

```
data:  assumption_test_model_sqrt  
BP = 10260, df = 84, p-value < 2.2e-16
```

- 
- ▶ Several assumptions are satisfied by 3 linear models.
 - ▶ Now, we experiment with the following models by training them:
 - Full linear model
 - Poisson GLM (log transform of target variable)
 - Backward and forward coefficients selection is done and best models, based on Bayesian Information Criterion and Mallows's C_p coefficient are trained.
 - ▶ After training the models, we compare and select the best in terms of:
 - Adjusted R^2
 - Akaike Information Criterion
 - Bayesian Information Criterion
 - Number of parameters
 - Validation R^2

1) Full linear model

- ▶ The adjusted R squared for the full linear model is 0.9247 with p-value less than 0.05
- ▶ With other techniques, we will try to improve these metrics while decreasing the number of parameters considered.

```
Call:
lm(formula = train[, Y_colname] ~ ., data = train[, X_colnames])
```

```
Residuals:
    Min       1Q   Median       3Q      Max
-16.542  -1.425  -0.154   1.263   53.568
```

```
Coefficients: (17 not defined because of singularities)
```

	Estimate	Std. Error	t value	Pr(> t)
(Intercept)	-2.323e+04	3.250e+04	-0.715	0.474705
timestamp	-6.150e-06	5.787e-06	-1.063	0.287957
hour	2.433e-02	2.097e-02	1.160	0.245893
day	5.604e-01	5.015e-01	1.117	0.263853
month	1.685e+01	1.504e+01	1.120	0.262759
distance	2.901e+00	6.873e-03	422.095	< 2e-16 ***
surge_multiplier	6.832e+01	7.340e-01	791.914	< 2e-16 ***
V1_Back.Bay.1	-7.017e-02	2.928e-02	-2.396	0.016555 *
V1_Beacon.Hill.1	-3.747e-01	2.928e-02	-12.795	< 2e-16 ***
V1_Boston.University.1	-5.070e-01	3.051e-02	-16.617	< 2e-16 ***
V1_Fenway.1	-2.971e-01	2.989e-02	-9.943	< 2e-16 ***
V1_Financial.District.1	3.079e-01	2.946e-02	10.449	< 2e-16 ***
V1_Haymarket.Square.1	1.949e-01	2.970e-02	6.564	5.26e-11 ***
V1_North.End.1	3.581e-01	2.936e-02	12.198	< 2e-16 ***
V1_North.Station.1	1.799e-04	2.917e-02	0.006	0.995079
V1_Northeastern.University.1	-5.122e-01	2.984e-02	-17.163	< 2e-16 ***
V1_South.Station.1	NA	NA	NA	NA
V1_Theatre.District.1	4.572e-01	2.934e-02	15.581	< 2e-16 ***
V1_West.End.1	NA	NA	NA	NA

Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1

```
Residual standard error: 2.506 on 176241 degrees of freedom
Multiple R-squared: 0.9281, Adjusted R-squared: 0.9281
F-statistic: 2.71e+04 on 84 and 176241 DF, p-value: < 2.2e-16
```

2) Poisson GLM

- ▶ Log transformation is used to increase R squared up to 0.9386 from 0.9247.
- ▶ To improve these metrics while decreasing the number of parameters considered forward and backward selection are used.

```
Call:
lm(formula = log(train[, Y_colname]) ~ ., data = train[, X_colnames])

Residuals:
    Min       1Q   Median       3Q      Max
-1.16268 -0.07493 -0.00433  0.06844  1.24677

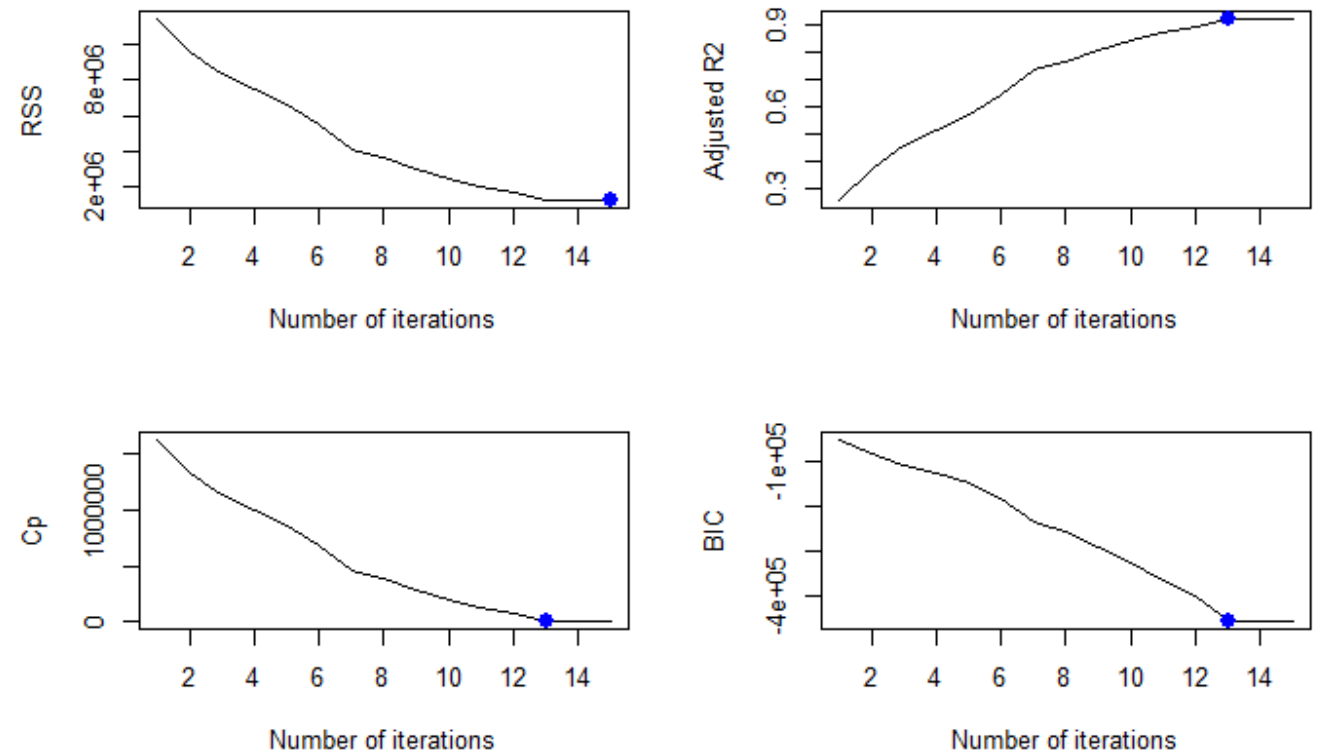
Coefficients: (17 not defined because of singularities)
              Estimate Std. Error t value Pr(>|t|)
(Intercept) -2.897e+03  1.827e+03  -1.586  0.112799
timestamp    -3.978e-07  3.253e-07  -1.223  0.221367
hour          1.421e-03  1.179e-03   1.206  0.227964
day           3.479e-02  2.819e-02   1.234  0.217062
month         1.046e+00  8.456e-01   1.237  0.216184
distance      1.754e-01  3.863e-04  454.001 < 2e-16 ***
surge_multiplier 2.597e+00  1.315e-02  197.415 < 2e-16 ***
latitude      4.609e-01  2.609e-01   1.766  0.077330 .
longitude     -6.897e-01  3.658e-01  -1.886  0.059343 .
V1_.Possible.Drizzle.      NA         NA      NA      NA
V1_Back.Bay.1             -2.518e-03  1.646e-03  -1.530  0.125977
V1_Beacon.Hill.1          -5.183e-03  1.646e-03  -3.149  0.001639 **
V1_Boston.University.1    -4.110e-02  1.715e-03 -23.967 < 2e-16 ***
V1_Fenway.1               -2.122e-02  1.680e-03 -12.635 < 2e-16 ***
V1_Financial.District.1   -3.426e-02  1.656e-03 -20.689 < 2e-16 ***
V1_Haymarket.Square.1     -1.514e-02  1.669e-03  -9.072 < 2e-16 ***
V1_North.End.1             1.751e-02  1.650e-03  10.611 < 2e-16 ***
V1_North.Station.1        -7.108e-03  1.639e-03  -4.336  1.45e-05 ***
V1_Northeastern.University.1 -2.905e-02  1.677e-03 -17.317 < 2e-16 ***
V1_South.Station.1         NA         NA      NA      NA
V1_Theatre.District.1      2.784e-02  1.649e-03  16.878 < 2e-16 ***
V1_West.End.1              NA         NA      NA      NA
---
Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1

Residual standard error: 0.1408 on 176241 degrees of freedom
Multiple R-squared:  0.9387,    Adjusted R-squared:  0.9386
F-statistic: 3.211e+04 on 84 and 176241 DF, p-value: < 2.2e-16
```

3) Linear model (forward / backward model selection)

- Many correlated indices were removed by trial & error method and `nvmax` is chosen 15 for both forward and backward subset selection.

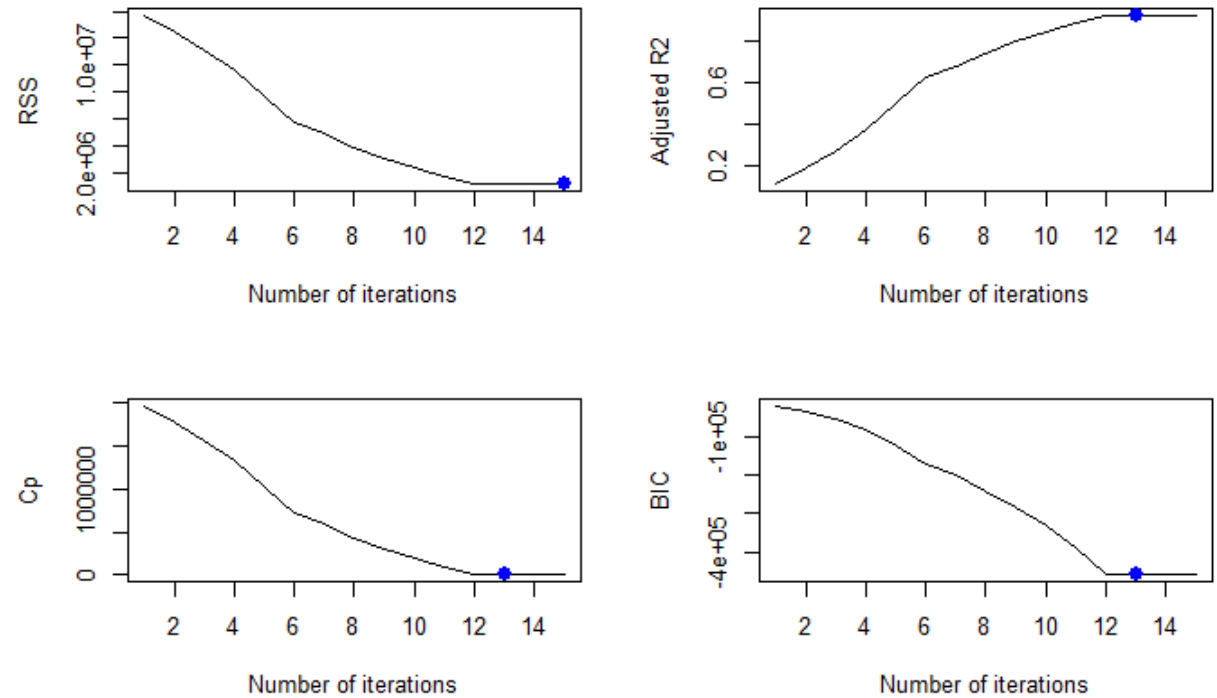
Forward subsets



3) Linear model (forward / backward model selection)

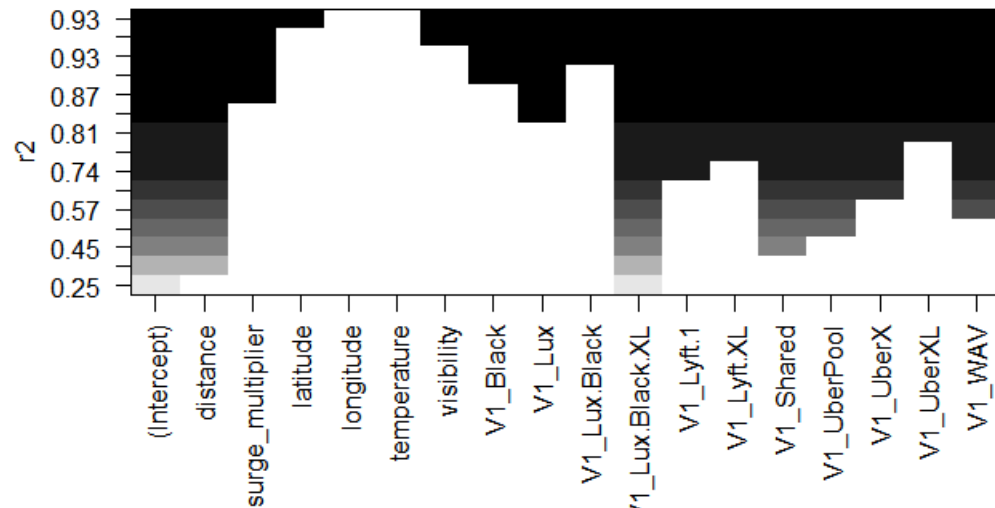
- ▶ Best number of parameters in Backward selection and Forward selection are same with
- ▶ BIC $\rightarrow 13$
- ▶ Cp $\rightarrow 13$

Backward subsets

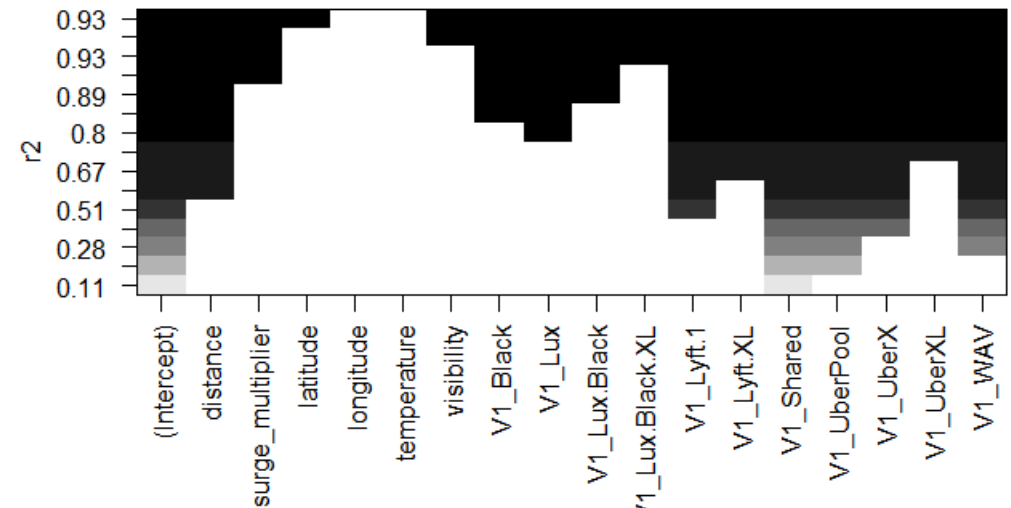


- ▶ To represent the most significant variables, we used variable elimination plots based on r^2 value.
- ▶ After elimination of variables, best BIC and Cp model are retrained.

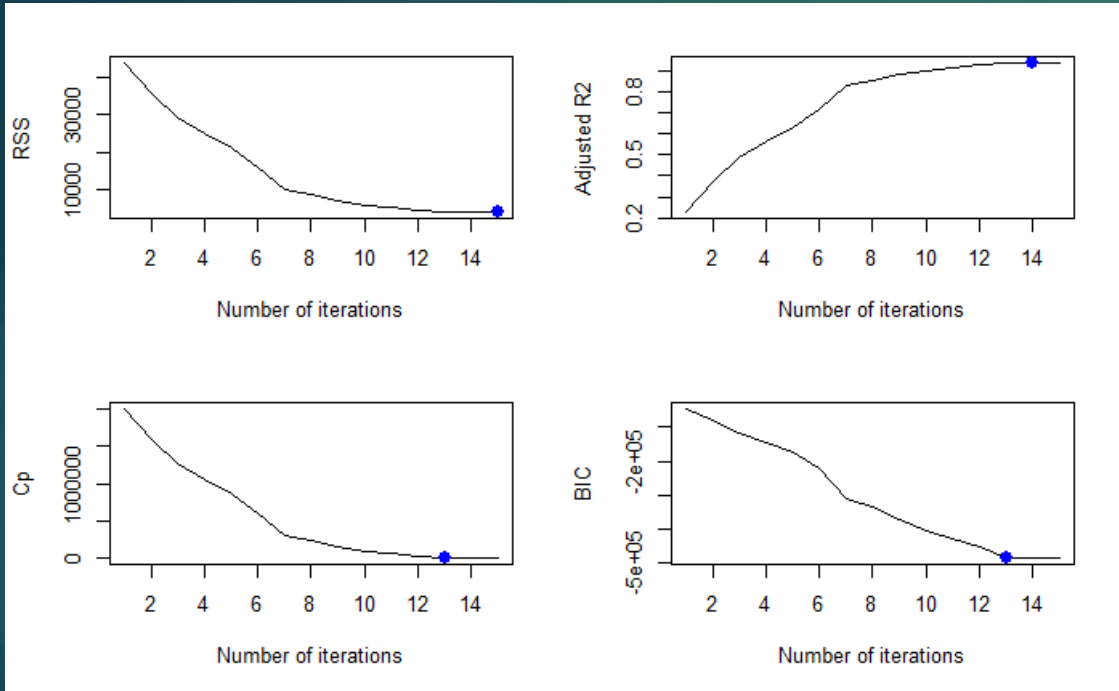
forward



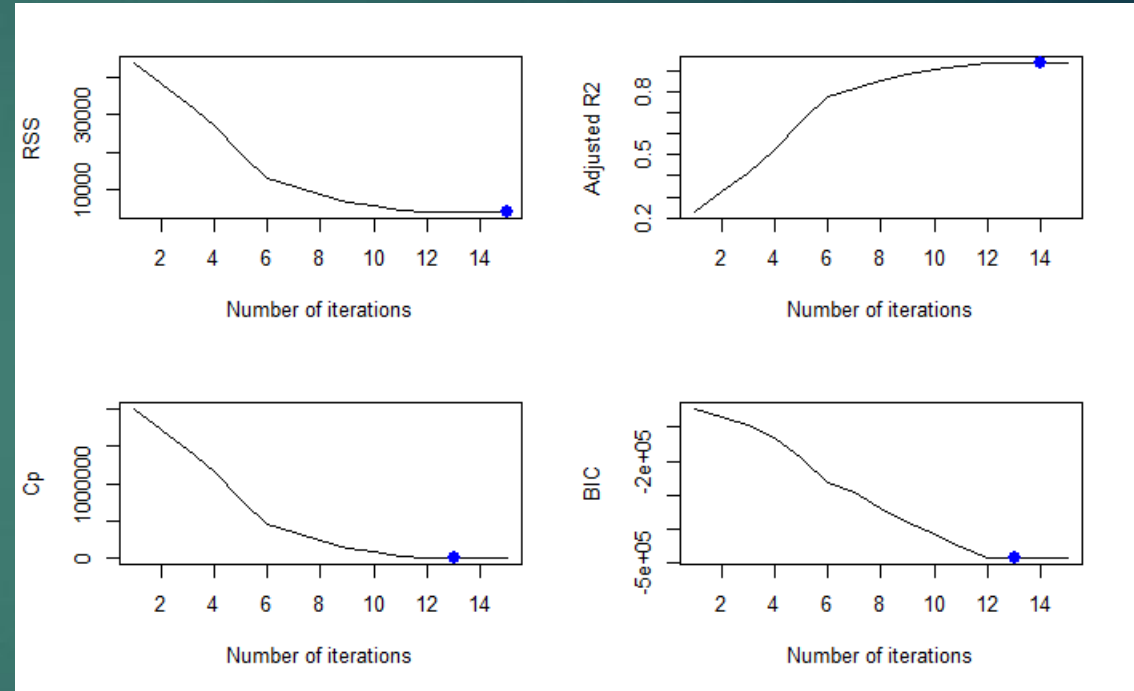
backward



4) Forward / backward selection for $\log(Y)$ transform



Forward subsets

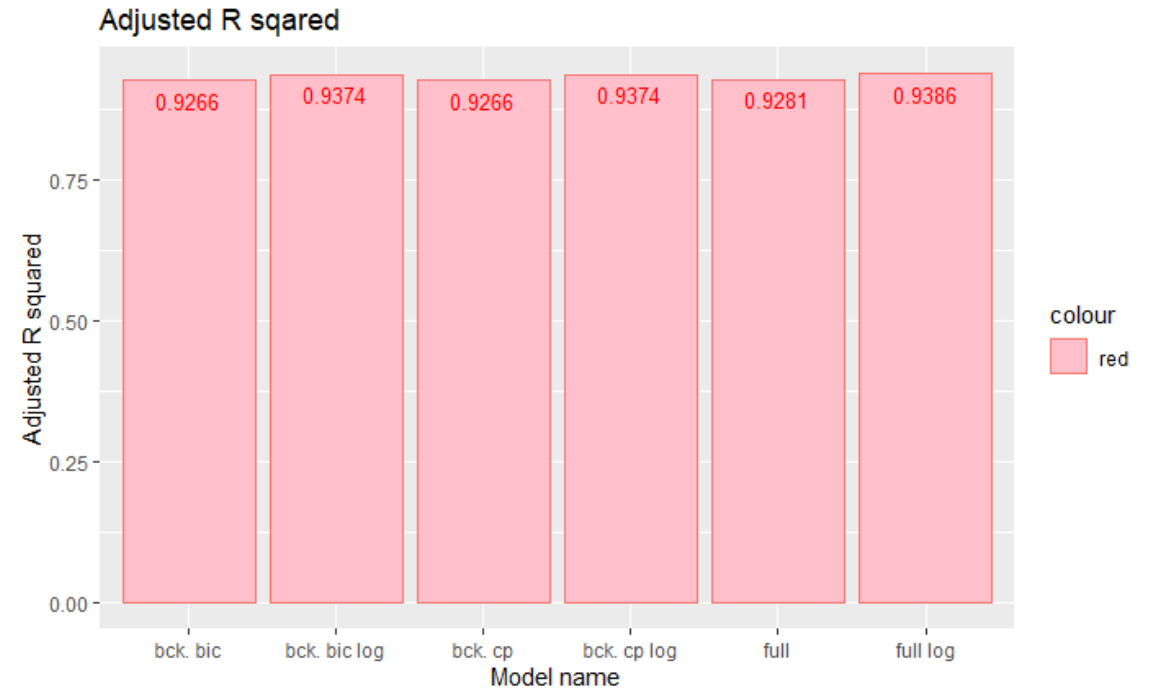


Backward subsets

Number of best coefficients for both selections are BIC→13 & Cp→13

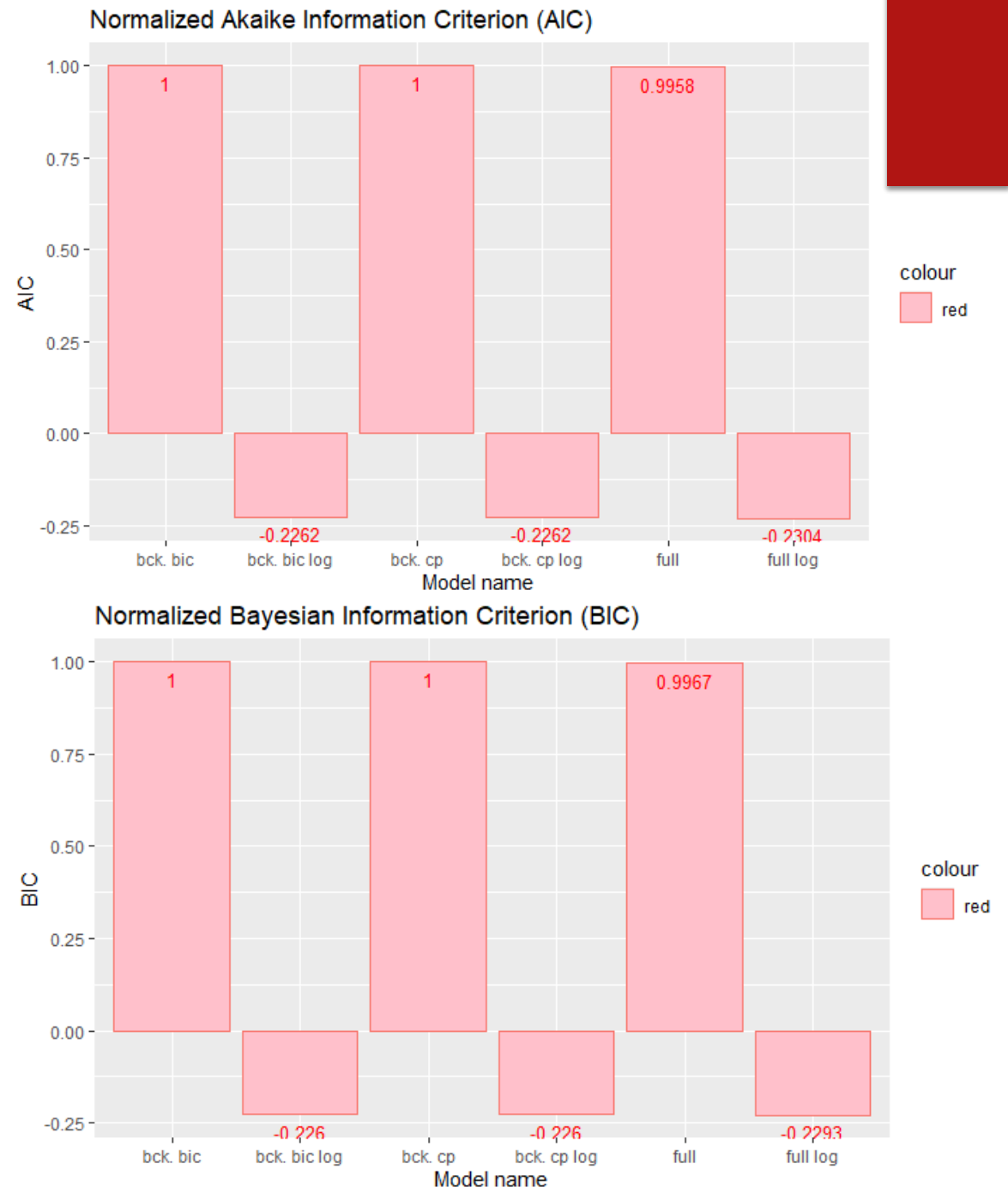
❖ Comparison of models

- ▶ **Comparison of adjusted R^2**
- ▶ From the plot we can say that independent of parameter selection technique generalized linear model was capable of achieving better R^2 results.



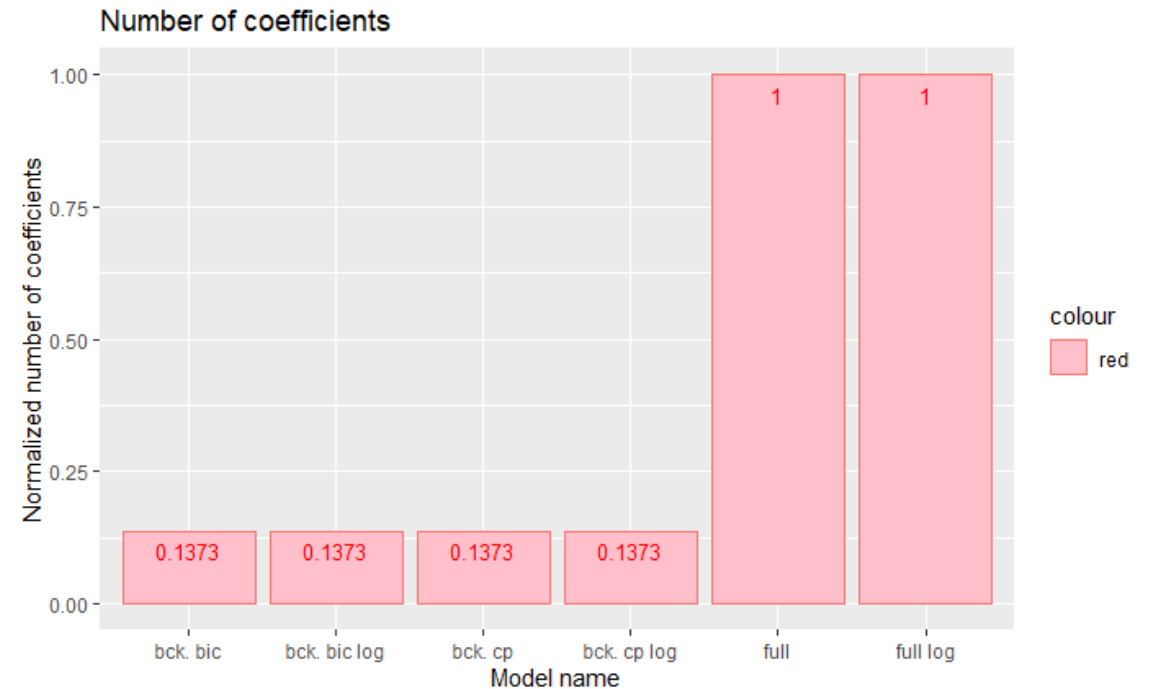
2) Comparison of AIC and BIC

- ▶ A remarkable difference is also observed in terms of Akaike and Bayesian information criteria
- ▶ The lower the AIC and BIC the better, and a negative AIC or BIC indicates a lower degree of information loss than a positive AIC or BIC



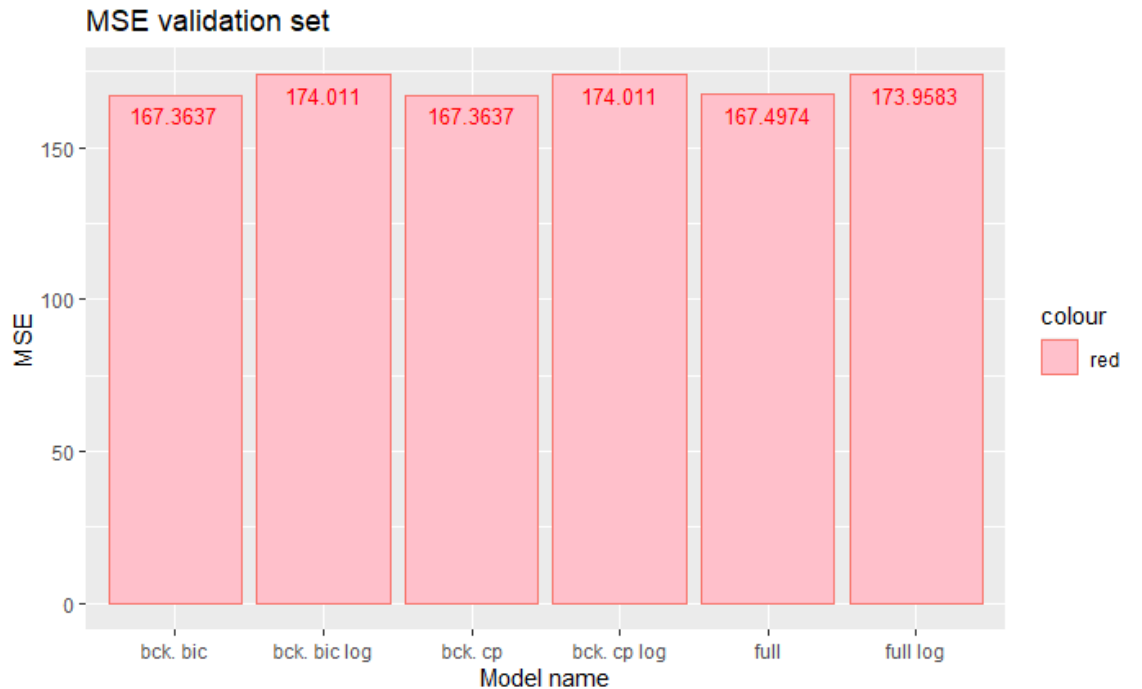
4) Comparison based on number of parameters

► A powerful result can be made here - having up to 87 percent less parameters, the lightweight models like GLM with backward selection and GLM log model with backward selection were able to achieve better R squared metrics with less parameters.



5) Comparison Based on Validation Set.

- ▶ On the validation set, all models achieved comparable results.
- ▶ **Conclusion:**
- ▶ The best model is a Poisson GLM, with backward coefficients selection.
- ▶ It has 87% less parameters than full model, allowing for around 0.9386 adjusted R squared.





Thank you