## Jaypee University of Engineering & Technology, Guna

Probability Theory and Random Process (MA106)

## **Tutorial-3**

1. The RV X has the following probability distribution:

x : -2 -1 0

P(x): 0.4 k 0.2 0.3.

Find k and mean value of X.

- 2. A shipment of 6 television sets contains 2 defective sets. A hotel makes a random purchase of 3 of the sets. If X represents the no. of defectives in the lot purchased, find the probability distribution of X.
- 3. A random variable X may assume 4 values with probability  $\frac{1+3x}{4}$ ,  $\frac{1-x}{4}$ ,  $\frac{1+2x}{4}$ ,  $\frac{1-4x}{4}$ . Find the probability on x so that these values represent the probability of x.
- 4. If the random variable X takes the values 1,2,3 and 4 such that

2P(X=1)=3P(X=2)=P(X=3)=5P(X=4), find the probability distribution and cumulative distribution of X.

5. A random variable X has the following probability dathur x

: -2 -1 0 1 2 3

P(x): 0.1 k 0.2 2k 0.3 3k

- (i) Find k (ii) evaluate P(X < 2) and P(-2 < X < 2) (iii) find cdf of X, and evaluate the mean of X.
- 6. A random variable X has the following probability distribution:

x : 0 1 2 3 4 5 6 7

 $P(x) : 0 2\lambda 2\lambda \lambda 3\lambda \lambda^2 2\lambda^2 7\lambda^2 + \lambda$ 

(i) Find the value of  $\lambda$  (ii) evaluate P(1.5 < X < 4.5 | X > 2) (iii) the smallest value of K for which  $P(X \le K) > \frac{1}{2}$ .

7. A discrete random variable X has the following probability distribution:

x : 0 1 2 3 4 5 6 7 8

P(x): a 3a 5a 7a 9a 11a 18a 15a 17a

Find the value of a, P(X < 3), variance and probability distribution of X.