

Tutorial-1

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① if "P represents This book is good" and "Q represents This book is cheap" write following sentences in symbolic form

- 1] This book is good and cheap
- 2] This book is not got but cheap
- 3] costly but good
- 4] neither good nor cheap
- 5] either good or cheap

② Construct truth table $((P \vee Q) \rightarrow (P \vee R)) \rightarrow (R \vee Q)$

③ Show that $(P \wedge Q) \vee (P \wedge \neg Q) \equiv P$

④ Obtain a disjunctive normal form of $P \vee (\neg P \rightarrow (Q \vee (Q \rightarrow \neg R)))$

⑤ find disjunctive normal function

P	Q	R	α
T	T	T	T
T	T	F	F
T	F	T	F
T	F	F	T
F	T	T	T
F	T	F	F
F	F	T	F
F	F	F	T

- * Lexical Analysis
 - * Syntax Analysis
 - * Semantic Analysis
 - * Code optimization
 - * Code generation
- } Platform independent
- } Machine dependent

$P \rightarrow Q$ if P then Q - jaha $P \rightarrow T$ ho vaha Q ki value likh to remain T

$P \leftrightarrow Q$ P is equivalent to Q

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- ① i) $P \wedge Q$
 ii) $\neg P \wedge Q$
 iii) $P \wedge \neg Q$
 iv) $\neg P \wedge \neg Q$ or $\neg(P \vee Q)$

- i) $\neg P \wedge Q$
 ii) $\neg P \wedge \neg Q$ or $\neg(P \vee Q)$

② $(P \vee Q) \rightarrow (P \vee R) \rightarrow (R \vee Q)$

P	Q	R	$P \vee Q$	$P \vee R$	$R \vee Q$	$(P \vee Q) \rightarrow (P \vee R)$	$(P \vee Q) \rightarrow (P \vee R) \rightarrow (R \vee Q)$
0	0	0	0	0	0	1	0
0	0	1	0	1	1	1	1
0	1	0	1	0	1	0	1
0	1	1	1	1	1	1	1
1	0	0	1	1	0	1	0
1	0	1	1	1	1	1	1
1	1	0	1	1	1	1	1
1	1	1	1	1	1	1	1

③ $(P \wedge Q) \vee (P \wedge \neg Q)$

P	Q	$P \wedge Q$	$\neg Q$	$P \wedge \neg Q$	$(P \wedge Q) \vee (P \wedge \neg Q)$
0	0	0	1	0	0
0	1	0	0	0	0
1	0	0	1	1	1
1	1	1	0	0	1

④ disjunctive Normal form

$(a \oplus b) \vee (\neg a \wedge b \wedge \neg c) \Rightarrow$ product ka sum
 product sum $(\neg a \wedge b \vee \neg c) \Rightarrow X$

Sum not allowed
in product

$((a \wedge b) \wedge (c \vee \neg c)) \Rightarrow (a \wedge b \wedge c) \vee (a \wedge b \wedge \neg c)$

$A \vee \neg A = \text{True}$, $A \wedge \neg A = \text{False}$

* Equivalence of WFF - two WFF α and β
 are set to be equivalent if α equilite β
 is tautology $(\alpha \equiv \beta)$

* Logical Identities -

$$\alpha = (Q \rightarrow R) \vee (P \rightarrow R) \wedge (P \vee Q) \wedge (Q \rightarrow P) \leftrightarrow (P \vee R)$$

$$\beta = (P \rightarrow Q) \leftrightarrow R$$

Identities -

- ① $(P \vee P) \equiv P$ ② $(P \wedge P) \equiv P$
- ③ $(P \vee Q) \equiv (Q \vee P)$ ④ $(P \wedge Q) \equiv (Q \wedge P)$
- ⑤ $(P \vee Q) \vee R \equiv P \vee (Q \vee R)$ ⑥ $P \wedge (Q \wedge R) \equiv (P \wedge Q) \wedge R$
- ⑦ $P \vee (Q \wedge R) \equiv (P \vee Q) \wedge (P \vee R)$ ⑧ $P \wedge (Q \vee R) \equiv (P \wedge Q) \vee (P \wedge R)$
- ⑨ $P \vee (P \wedge Q) \equiv P$ ⑩ $P \wedge (P \vee Q) \equiv P$
- ⑪ $\neg(P \vee Q) \equiv \neg P \wedge \neg Q$ ⑫ $\neg(P \wedge Q) \equiv \neg P \vee \neg Q$
- ⑬ $P \equiv \neg(\neg P)$
- ⑭ $P \vee \neg P \equiv T$
- ⑮ $P \vee T \equiv T$ ⑯ $P \vee F \equiv P$
- ⑰ $P \wedge T \equiv P$ ⑱ $P \wedge F \equiv F$
- ⑲ $(P \rightarrow Q) \wedge (P \rightarrow \neg Q) \equiv \neg P$
- ⑳ $P \rightarrow Q \equiv \neg Q \rightarrow \neg P$
- ㉑ $P \rightarrow Q \equiv \neg P \vee Q$

$$\underline{㉒} \quad (P \wedge Q) \vee (P \wedge \neg Q) = P$$

Sentence into Propositional Form -

Let P be the propositional variable for $P = \text{it is rainy}$
 $Q = \text{I have the time}$, $R = \text{I will go to a movie}$

① I will not go to movie if it is rainy

②

Normal Form of WFF -

① Disjunctive ^{Normal} Form - ② Conjunctive Normal Form
Steps -

- ① Eliminate implication and equality using logical Identities
- ② Eliminate negation before sums and product.
the resulting formula as negation only before the propagation value
- ③ Use above steps to obtain the formula for sum of product of literals.

Q PV ($\neg P \rightarrow (QV(Q \rightarrow \neg R))$) , convert this Conjunctive normal form to Disjunctive normal form.

$$\begin{aligned}
 & PV (\neg P \rightarrow (QV(Q \rightarrow \neg R))) \\
 \Rightarrow & PV (\neg P \rightarrow (QV(\neg Q V \neg R))) \quad \{ P \rightarrow Q = \neg P V Q \} \\
 \Rightarrow & PV (\neg P \rightarrow (QV \neg Q) V \neg R) \\
 & P V \neg (\neg P) V Q V \neg Q V \neg R \\
 & PVP V QV \neg QV \neg R \\
 & PVQV \neg QV \neg R
 \end{aligned}$$

Tutorial-2

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R+

① Let $R = \{(1,2), (2,3), (2,4)\}$ be a relation in $\{1, 2, 3, 4\}$. find,

② If $A = \{a, b\}$ and $B = \{b, c\}$, find

(a) $(A \cup B)^*$

(b) $(A \cap B)^*$

(c) $(A - B)^*$

(d) $A^* \cap B^*$

(e) $(B - A)^*$

③ A finite automaton M has state set $Q = \{q_0 : q_1, q_2\}$.

Its input alphabet is $\Sigma = \{0, 1\}$, with q_0 being the initial state and $F = \{q_0\}$. The transition "f" is given by the following transition table.

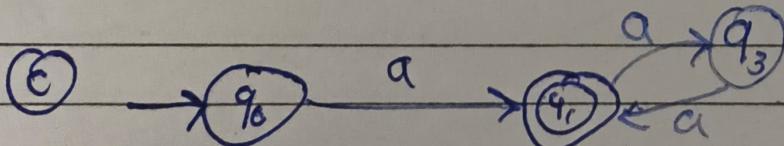
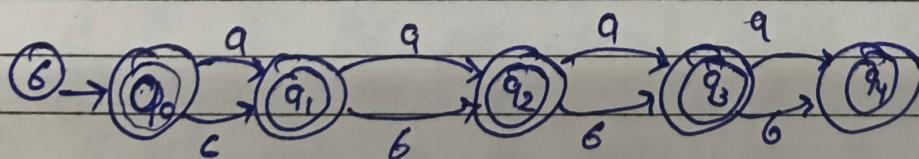
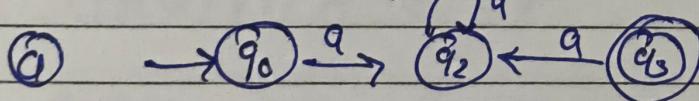
δ	0	1
q_0	q_2	q_1
q_1	q_1	q_0
q_2	q_2	q_2

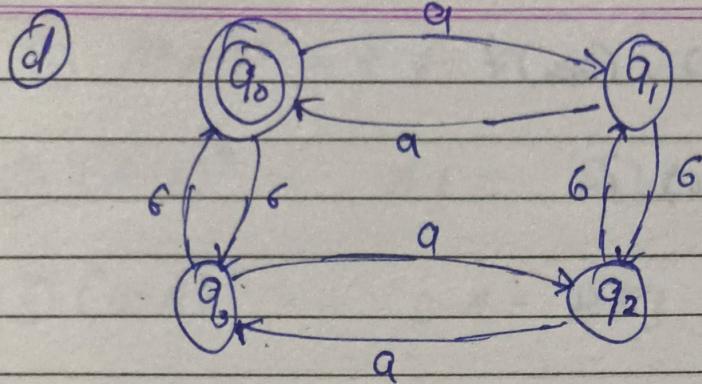
Give the state diagram for M

and describe the language $L(M)$.

④ Sheep go 'baal' or 'baaa!' and so on. They do not go 'baaa' or 'ba!' or '!' or ". Construct a finite automaton (with input alphabet $\Sigma = \{a, b, ;, !\}$) that recognizes "Sheep-talk".

⑤ Find the language of following FA:





⑥ Find the FA of following language.

⑦ $L = \{a^{2n} \mid n \geq 0\}$

⑧ $L = \{a^n 6^m \mid n, m \geq 0\}$

⑨ $L = \{a, 6, aa, 66, aaa, 666, \dots\}$

⑩ $L = \{\text{Set of all strings over } \{0, 1\} \text{ starting with } 0 \text{ ending with } 1\}$

Ans - 2 $A = \{a, 6\}, B = \{6, c\}$

① $\Rightarrow (A \cup B)^*$ $\Rightarrow A \cup B = abc \Rightarrow (A \cup B)^* = \emptyset$

Ans - 1 $R = \{(1, 2), (2, 3), (2, 4)\}$

$S = \{1, 2, 3, 4\}$

R^+ = transitive Closur

$A \cdot B \Rightarrow \text{if } \langle a, b \rangle \in A \text{ and } \langle b, c \rangle \in B \text{ then } \langle a, c \rangle \in A \cdot B$

but if $\langle a, c \rangle \in A \cdot B$ or $\langle a, c \rangle \in B \cdot A$ then $\langle a, c \rangle \notin A \cdot B$

$$R^2 = R \cdot R, R^3 = R^2 \cdot R$$

$$R^+ = RVR^2VR^3\dots$$

$1,2 \rightarrow 23$
 $1,2 \rightarrow 2,3$

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Sol-1 $R = \{(1,2), (2,3), (3,4)\}$

$R^2 = R \cdot R = \{(1,3), (2,4)\}$

$R^3 \Rightarrow R^2 \cdot R = \emptyset$

$R^4 \Rightarrow R^3 \cdot R = \emptyset \dots$

$R^+ = \{(1,2), (2,3), (3,4), (1,3), (1,4)\}$

Sol-2 $A = \{a, b\}$, $B = \{b, c\}$
 $S = \{a, b, c\}$

① $(A \cup B)^* \Rightarrow A \cup B = abc \Rightarrow (A \cup B)^* = \emptyset$

② $(A \cap B)^* \Rightarrow A \cap B = \emptyset \Rightarrow (A \cap B)^* = \{a, b\}$

③ $A^* \cup B^* \Rightarrow$

$X^* = \text{kleene closure or Kleene star}$

$X = \{a, b\}$

$X^* = \{\emptyset, a, b, aa, ab, ba, bb, aaa, \dots\}$

① $(A \cup B)^* = A \cup B = abc$

$(A \cup B)^* = \{\emptyset, a, b, c, ab, ac, bc, abc, aab, aac, abc, baa, bcc, ccc, cba, caa, \dots\}$
 Set of all strings

② $(A \cap B)^* = A \cap B = \emptyset$

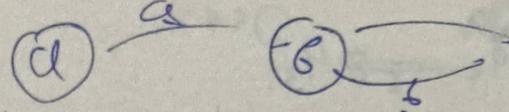
$(A \cap B)^* = \{\emptyset, b, bb, bbb, \dots\}$

③ $A^* \cup B^* = A^* = \{\emptyset, a, b, ab, ba, aab, aab, \dots\}$

$B^* = \{\emptyset, b, c, bb, cc, bc, cb, \dots\}$

$A^* \cup B^* = \{\emptyset, a, b, c, ab, ac, ba, bc, aab, aac, aab, \dots\}$

Set of all the strings over either $\{a, b\}$ or $\{b, c\}$



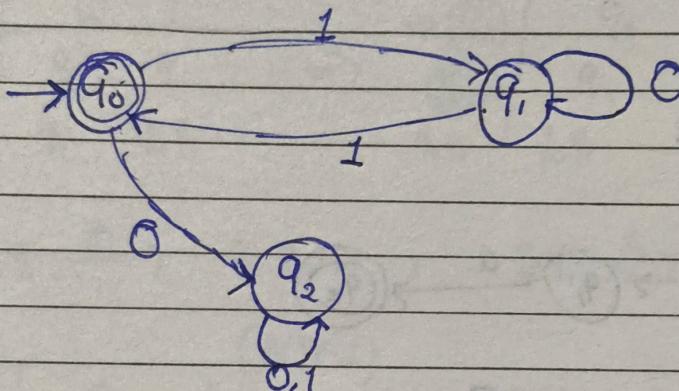
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$$\textcircled{5} \quad A^* \cap B^* = \{ \phi, 6, 66, 666, \dots \}$$

$$\textcircled{6} \quad (A-6)^* = A \cdot 6 = \{ a \} \Rightarrow a^*$$

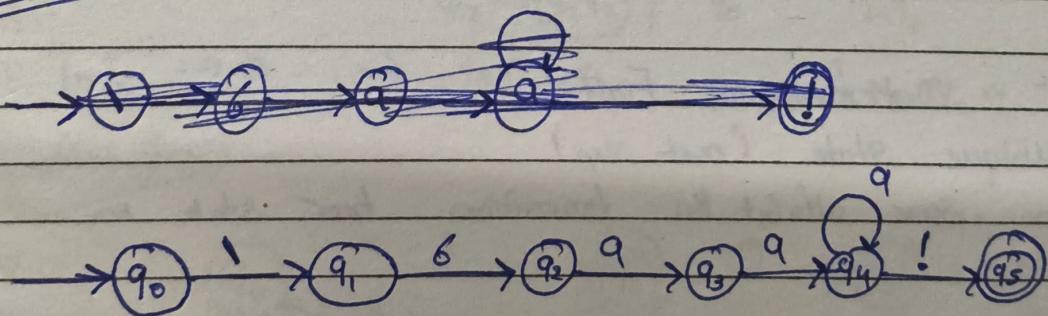
$$\textcircled{7} \quad (B-A)^* = B-A = \{ c \} \Rightarrow c^*$$

~~(03)~~



$\Rightarrow (10^*1)^*$, starts and ends with 1 and all other 1's will appear in pairs

~~Sol 4~~



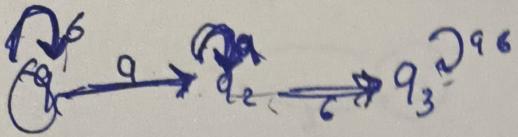
~~Sol 5~~

i) Null

ii) $\{ \phi, (a+b), (a+b)(a+b), (a+b)(a+b)(a+b), \dots \}$

Set of all strings over a and b with max length 4.

$$L = \{ x \in \{a,b\}^* \mid |x| \leq 4 \}$$



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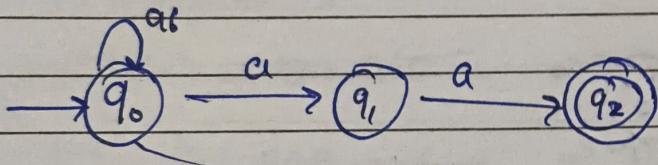
(3)

$a^* = \{ \epsilon, a, aaa, aaaa, \dots \}$

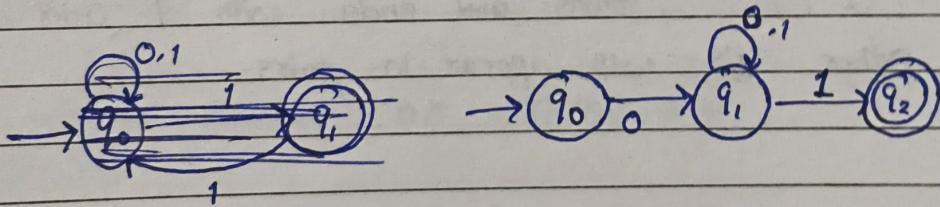
$L = \{ a^n | n \text{ is odd number} \}$

(4) no of a's and no. of b's are even.

a a at last



a 0 start end 1



DFA - Deterministic Finite

i) Unique state (next step)

ii) then same alphabet ka transition haur state me

The equivalence of N DFA and DFA (Conversion from N DFA to DFA)

ii) The DFA can simulate the behavior of N DFA by increasing the no. of states.

iii) Any NDFA is similar to DFA having same capabilities

iii) If L is the set of accepted language of NDFA then we can find a DFA which Accept the same language

Ex

State	0	1		State	0	1	
$\rightarrow q_0$	q_0	q_1	\Rightarrow	$\rightarrow q_0$	q_0	q_1	
q_1	q_1	q_0, q_1		q_1	q_1	q_0, q_1	
				q_0, q_1	q_0, q_1	q_0, q_1	

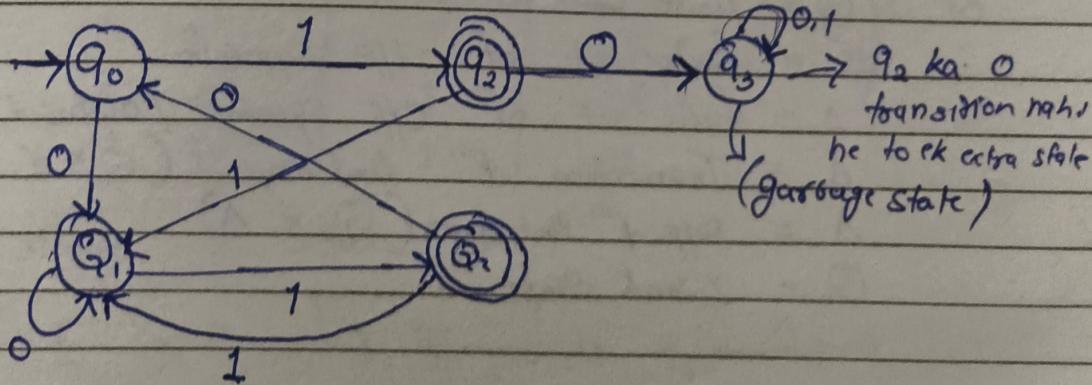
$$q_0 q_1 \xrightarrow{0} q_0 q_1, \quad q_0 q_1 \xrightarrow{1} q_1 \cup (q_0 q_1) \Rightarrow q_0 q_1$$

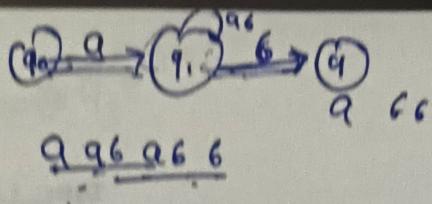
Ex

State	0	1	(NDFA)	State	0	1	(DFA)
$\rightarrow q_0$	$q_0 q_1$	q_2		$\rightarrow q_0$	$q_0 q_1$	q_2	
q_1	q_0	q_1	\Rightarrow	q_1	-	$q_0 q_1$	
q_2	-	$q_0 q_1$		q_2	$q_0 q_1$	q_1, q_2	

$q_0 q_1 \xrightarrow{0} 0 \Rightarrow q_0 q_1 \cup q_0, \quad q_0 q_1 \xrightarrow{1} q_2 q_1,$

transition graph





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$$\textcircled{Q} \quad L = a^n \bar{a}^n$$

→

FA with O/P

① Mealy Machine -

A FA or FSA have binary output that is they accept string or they do not accept the given string.

This was decided on the basis of processing of the input string from initial state to last symbol of the input string.

We want to remove this restriction from the given FA where the o/p f^n can be chosen from , when the o/p f^n $Z(t)$ chosen from other alphabet . If o/p f^n $Z(t)$ is a f^n of present state $q(t)$ and present input symbol $x(t)$ then the machine is called Mealy Machine.

② Moorey Machine

If $Z(t) = \lambda(q(t))$, then it is called Moorey Machine - it is a couple quantity of $Q = \text{finite set of state}$

$\Sigma = \text{finite set of i/p symbols}$

$A = \text{finite set of o/p symbols / alphabet}$

$\delta = \text{Transition } f^n \text{ that map's } (Q \times \Sigma = Q)$

$\lambda = \text{o/p } f^n \text{ that map's } (Q = A)$

$Q_0 = \text{Initial State}$

Memory - 1 output \rightarrow O/P associate with State

Memory - 2 output \rightarrow O/P associate with Transition

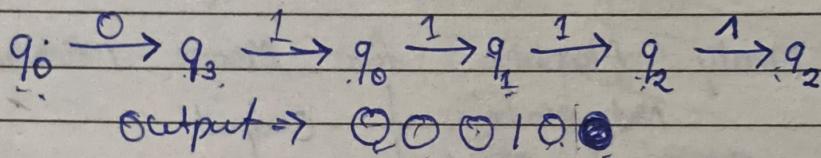
add

00110

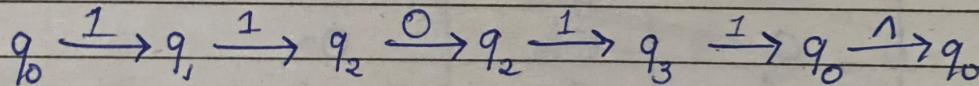
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P state	Next state		O/P
	q ₀ 0	q ₁ 1	
$\rightarrow q_0$	q ₃	q ₁	0
q ₁	q ₁	q ₂	1
q ₂	q ₂	q ₃	0
q ₃	q ₃	q ₀	0

\otimes Input string = 01111 $\Sigma = \{0, 1\}$, $A = \{q_0, q_1, q_2, q_3\}$



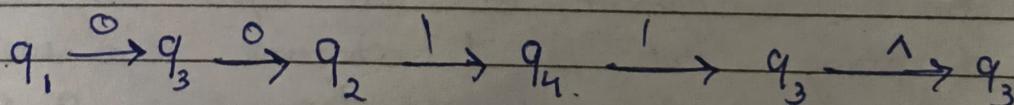
\otimes Input string = 11011



Output 010000

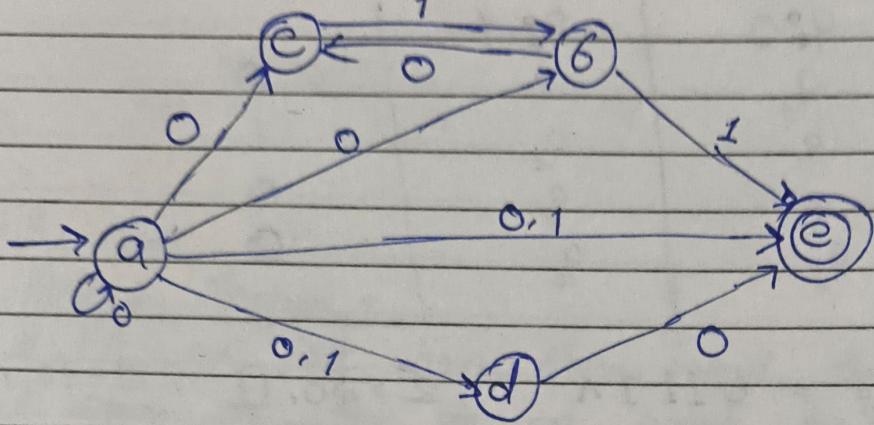
P state	Next state	
	$a=0$	$a=1$
$\rightarrow q_0$	State q ₃	O/P 0
q ₁	q ₁	1
q ₂	q ₂	1
q ₃	q ₄	1
q ₄	q ₄	0

Input string $\Rightarrow 00000011$



Output = 0100

① Equivalent DFA for the NDFA



② Equivalent Mealy Machine for Moore Machine

Present State	Next state		Output
	$a=0$	$a=1$	
$\rightarrow a$	d	6	1
6	a	d	0
c	c	c	0
d	6	a	1

③ find equivalent Moore Machine for Mealy Machine

Present state	Next State			
	$a=0$	O/P	$a=1$	O/P
$\rightarrow a$	d	0	6	1
6	a	1	d	0
c	c	1	c	0
d	6	0	a	1

④ The One's Compliment of an input bit string is a string that has 1 wherever there was 0 0, and a 0 wherever there was 1 1, for example, the One's compliment of 001 is 110
Construct Mealy Machine for one's compliment.

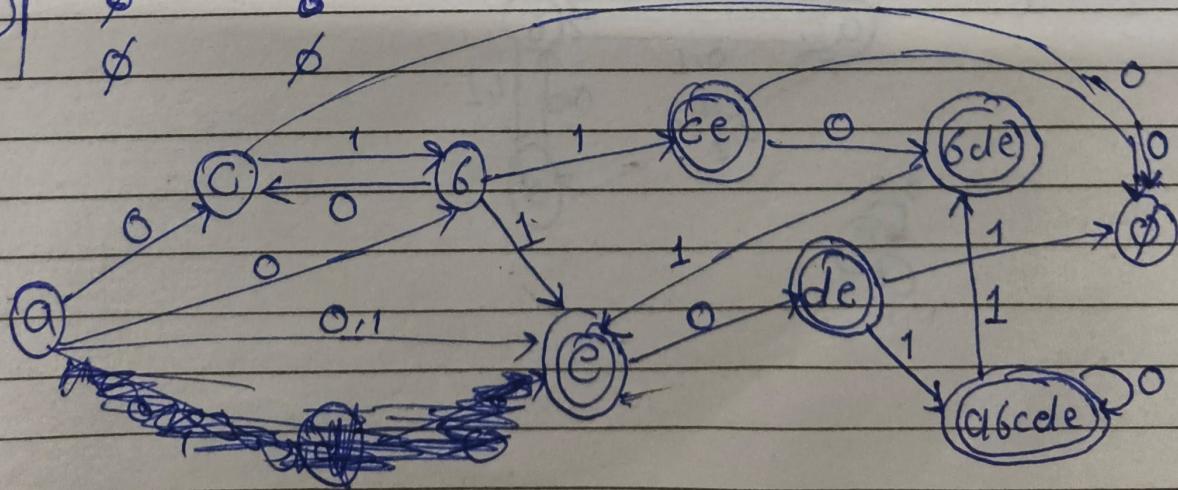
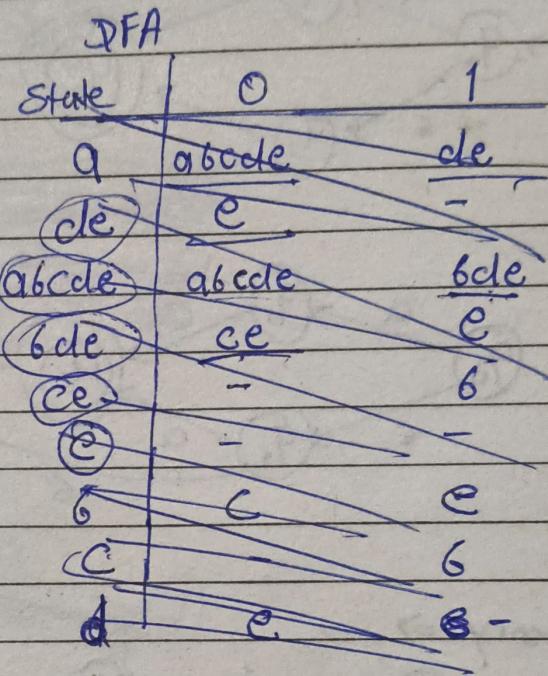
⑤ Construct a nondeterministic finite automation accepting $\{q_0, q_3\}$ and use it to find a deterministic automation accepting the same set.

Sol-1

<u>N DFA \Rightarrow</u>	
State	0 1
$\rightarrow q$	a,c,b,d,e
q	c
b	-
c	b
d	-
e	-

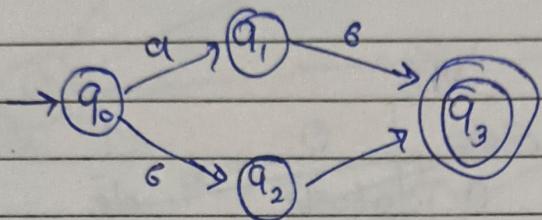
<u>DFA \Rightarrow</u>	
State	0 1
$\rightarrow q$	a,b,c,d,e
q	c
b	e
c	\emptyset
d	\emptyset
e	\emptyset

$abcde$	a,b,c,d,e	b,d,e
$cl\bar{e}$	c	\emptyset
$b\bar{d}e$	\emptyset	e
ce	\emptyset	b
\emptyset	\emptyset	\emptyset

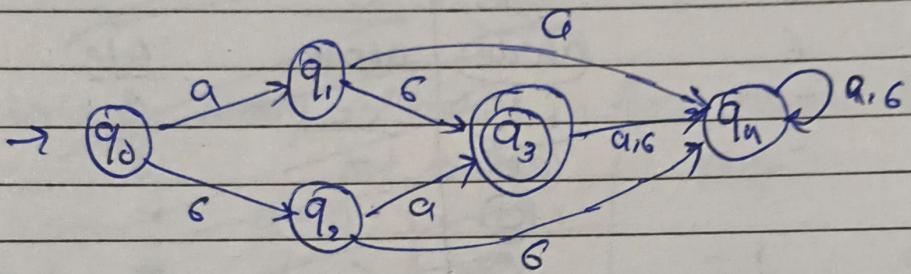


Q5 $S_{ab, G_2} \rightarrow$ Construct NDFA automation
and use it to find DF for same set

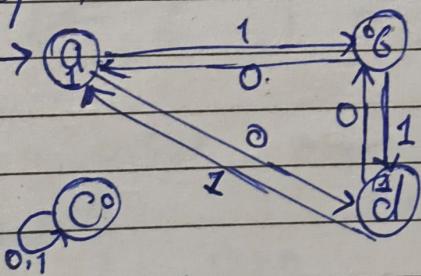
NDFA



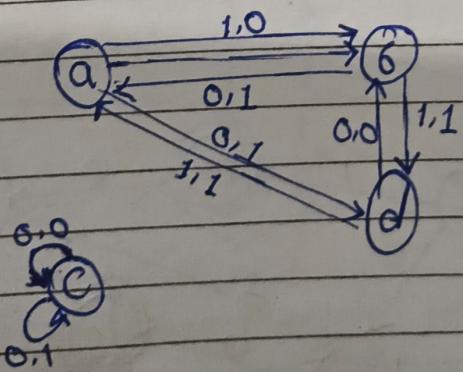
DFA

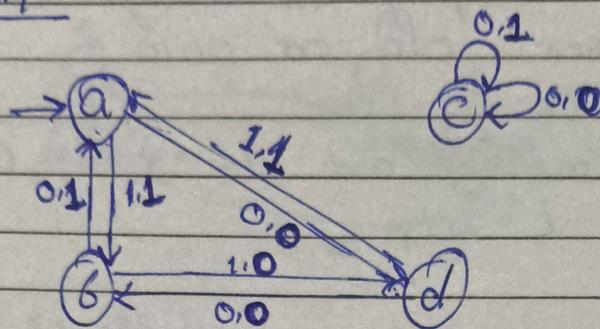
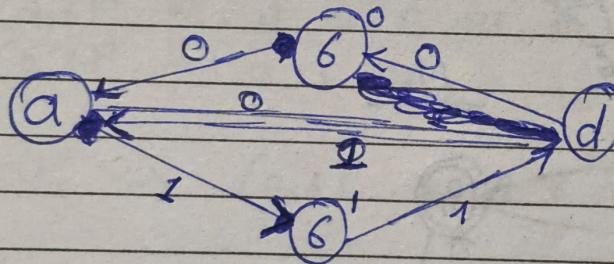
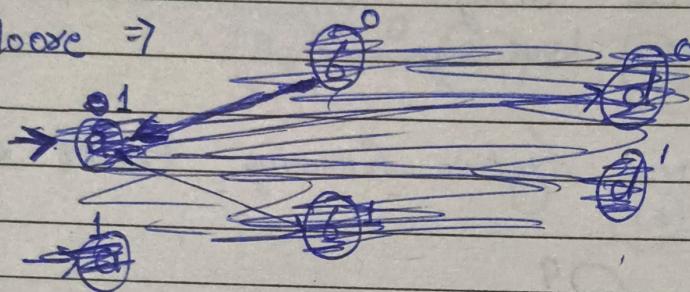


Q-2 Morrisy \Rightarrow



Mcally \Rightarrow



Q-3Mcaly \Rightarrow Moore \Rightarrow 

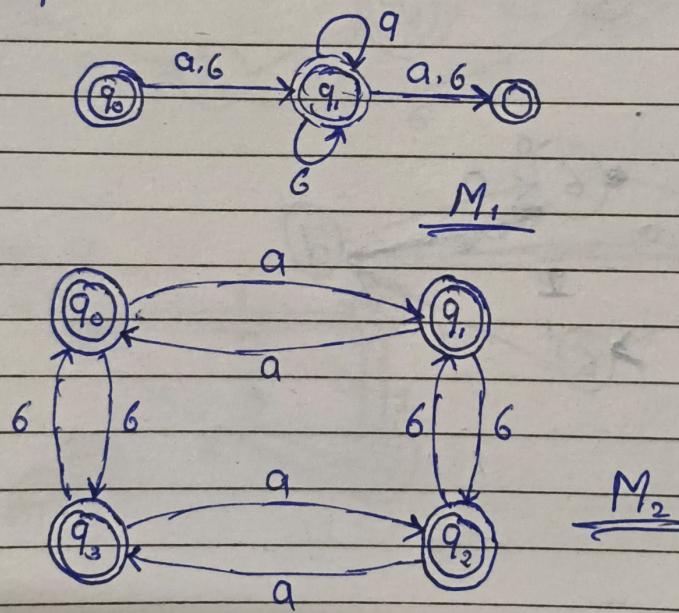
$$(a, 6)^* \Rightarrow \Delta, a, 6, aa, 66, a6, 6a$$

$$(a, 6)^+ \Rightarrow a, 6, a6, 6a$$

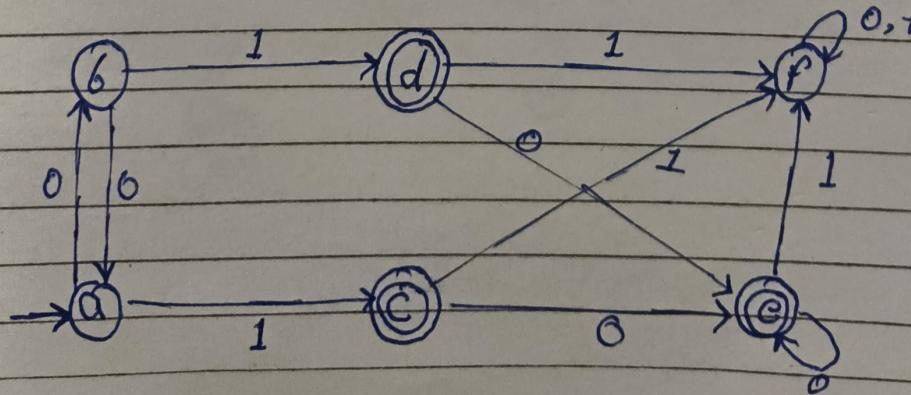
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- (1) Construct an FA accepting all strings over $\{0, 1\}^*$ ending with either 010 or 0010.
- (2) If $L_1 = \{s_1 \in (a, 6)^*\}$ and $L_2 = \{s_2 \in (a, 6)^+\}$ draw FA for $L = L_1 L_2$.
- (3) Draw FA for all strings over $\{0, 1\}^*$ consisting 010 or 111 as substring.
- (4) Prove or disprove whether following FA M_1 and M_2 are equivalent.



- (5) Use equivalence method to minimize the given FA.



$a, 6, a6, 6a, a96, 666$

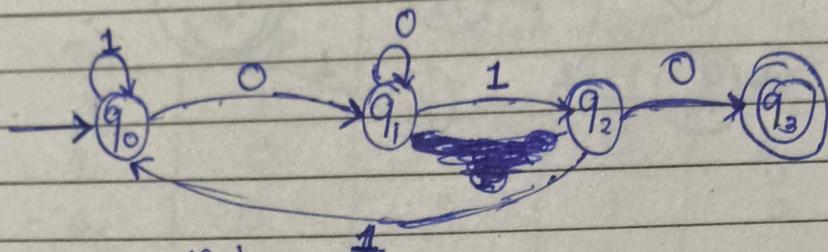
1010

00001
100110010
1011010
001110

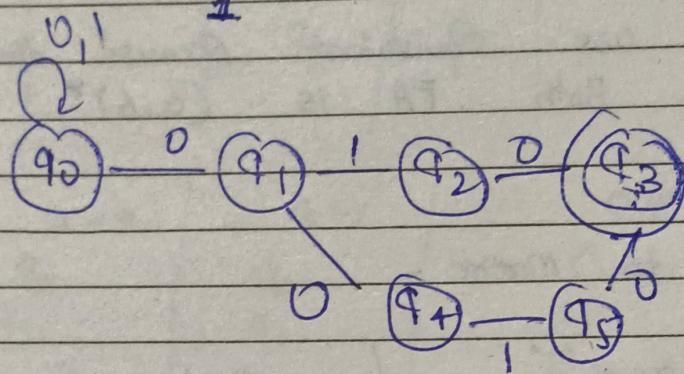
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1010 and 0010

Sol-1



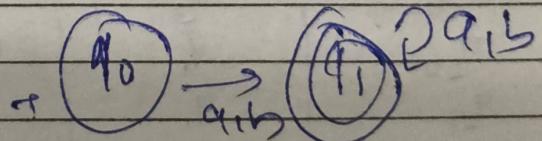
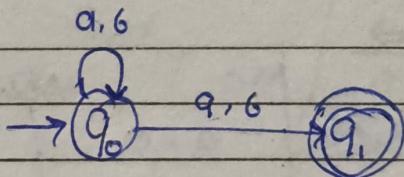
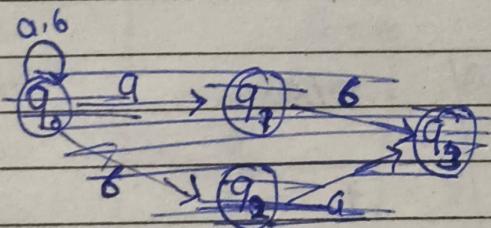
$\frac{0}{0}$
 $\frac{0}{0}$
 $\frac{0}{0} 010$



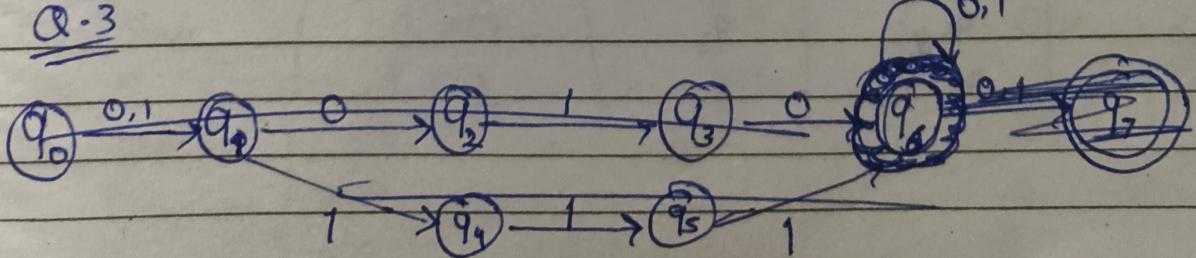
$$\underline{S01 \cdot 2L_1 = (a, 6)^*} \Rightarrow a, 6, a6, 6a, \dots$$

$$L_2 = (a, 6)^+ \Rightarrow a, 6, a6, 6a, \dots$$

$$L = L_1 \cup L_2 \Rightarrow (a, 6)^+ = a, 6, a6, 6a,$$

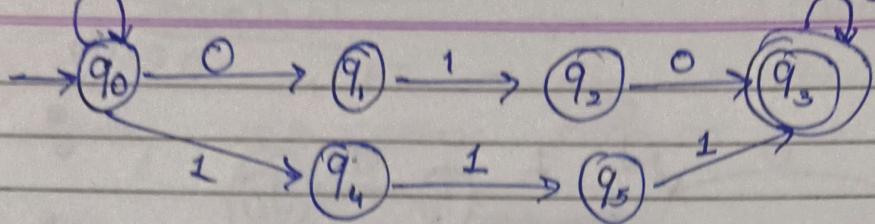


Q-3



Sol-3
0.1

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Q-4 Both are equivalent because the language for Both FA is $(a, b)^*$

Mealy to Moore -

Mealy \Rightarrow

	a=0		a=1		$q_1 \rightarrow 1$ $q_2 \rightarrow 0, 1$ $q_3 \rightarrow 0$ $q_4 \rightarrow 0, 1$
	State	O/P	State	O/P	
$\rightarrow q_1$	q_3	0	q_2	0	
q_2	q_1	1	q_4	0	
q_3	q_2	1	q_1	1	
q_4	q_4	1	q_3	0	

Moore \Rightarrow

P State	a=0	Next	O/P
$\rightarrow q_1$	q_3	q_{20}	1
q_{20}	q_1	q_{40}	0
q_{21}	q_1	q_{40}	1
q_3	q_{21}	q_1	0
q_{40}	q_{42}	q_3	0
q_{41}	q_{41}	q_3	1

\oplus Melay \Rightarrow

Pstate	$a = 0$		$a = 1$		$q_i \rightarrow 0, 1$ $q_2 \rightarrow 0, 1$ $q_3 \rightarrow 0, 1$ $q_4 \rightarrow 0, 1$
	State	O/P	State	O/P	
$\rightarrow q_1$	q_3	1	q_2	1	
q_2	q_1	0	q_4	0	
q_3	q_2	0	q_1	1	
q_4	q_4	1	q_3	0	

 \ominus Moosay \Rightarrow

Pstate	$a = 0$		$a = 1$		O/P
	State	O/P	State	O/P	
P_{10}	q_{31}		q_{21}		0
P_{11}	q_{31}		q_{81}		1
P_{20}	q_{10}		q_{40}		0
P_{21}	q_{10}		q_{40}		1
P_{30}	q_{20}		q_{11}		0
P_{31}	q_{20}		q_{11}		1
P_{40}	q_{41}		q_{30}		0
P_{41}	q_{41}		q_{30}		1

<u>\oplus</u> Pstate	$a = 0$		$a = 1$		$q_i \rightarrow \emptyset$ $q_2 \rightarrow z_1, z_2$ $q_3 \rightarrow z_1, z_2$
	State	O/P	State	O/P	
$\rightarrow q_1$	q_2	z_1	q_3	z_1	
q_2	q_2	z_2	q_3	z_1	
q_3	q_2	z_1	q_3	z_2	

Pstate	$a = z_1$		$a = z_2$		O/P -, ^, \emptyset
	State	O/P	State	O/P	
$\rightarrow q_1$	$q_2 z_1$		$q_3 z_1$		
$q_2 z_1$	$q_2 z_2$		$q_3 z_1$		z_1
$q_2 z_2$	$q_2 z_2$		$q_3 z_1$		z_2
$q_3 z_1$	$q_2 z_1$		$q_3 z_2$		z_1
$q_3 z_2$	$q_2 z_1$		$q_3 z_2$		z_2

Moory to Melay \Rightarrow

P State	$a=0$	$a=1$	O/P
$\rightarrow q_0$	q_3	q_1	0
q_1	q_1	q_2	1
q_2	q_2	q_3	0
q_3	q_3	q_0	0

Melay \Rightarrow

P State	$a=0$		$a=1$	
	State	O/P	State	O/P
$\rightarrow q_0$	q_3	0	q_1	1
q_1	q_1	1	q_2	0
q_2	q_2	0	q_3	0
q_3	q_3	0	q_0	0

Minimization of FA

- ① Equivalence method
- ② Table filling Method

① Equivalence Method -

if Two states Q_1 and Q_2 are said to be equivalent ~~if~~ if both for the input $S(Q_1, x)$ and $S(Q_2, x)$ are in the final state or both are in non final state.

iii Two state Q_1 and Q_2 are said to be K equivalent ($K \geq 0$) if both the states are in final state or are in non final state for all string of length K or less

* Steps of Minimization -

- a) find π_0 (set of final and non final state)
- b) find π_1 from π_0 (set of one-equivalent)
- c) find π_{n+1} fill $\pi_{n+1} = \pi_n$

Q

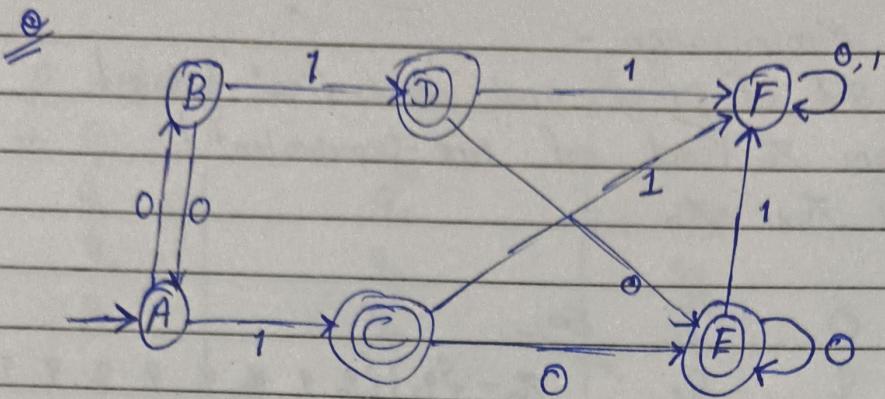
State	0	1	SOL
$\rightarrow q_0$	q_1	q_5	$\pi_0 = \{q_2\} \{q_0, q_1, q_3, q_4, q_5, q_6, q_7\}$
q_1	q_6	q_2	
(q_2)	q_6	q_2	$\pi_1 = \{q_2\} \{q_0, q_4, q_6\} \{q_1, q_3, q_5, q_7\}$
q_3	q_2	q_6	$\pi_1 = \{q_2\} \{q_0, q_4, q_6\} \{q_1, q_3, q_5, q_7\}$
q_4	q_7	q_5	
q_5	q_2	q_6	$\pi_2 = \{q_2\} \{q_0, q_4\} \{q_6\} \{q_1, q_7\} \{q_3, q_5\}$
q_6	q_6	q_4	$\pi_2 = \{q_2\} \{q_0, q_4\} \{q_6\} \{q_1, q_7\} \{q_3, q_5\}$
q_7	q_6	q_2	

$$\pi_2 = \pi_3$$

State	0	1
$\rightarrow (q_0, q_4)$	(q_1, q_7)	(q_3, q_5)
(q_4, q_7)	q_6	q_2
(q_2)	q_0, q_4	q_2
(q_3, q_5)	-	-
(q_6)	-	-

Minimization using Table filling method.

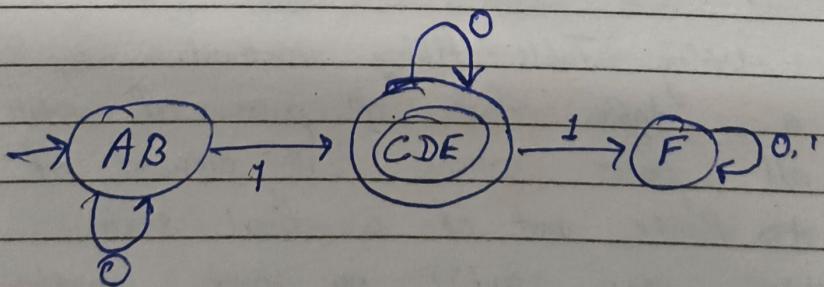
- ① Draw a table for all pairs of states
- ② Make all pairs where P is element of final table to P is not of a final state.
- ③ Repeat this step until no more marking can be made
- ④ Combine all the unmark pair and make them single state in the minimize FA.

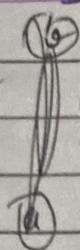


	A	B	C	D	E	F
A	x					
B		x				
C	v		x			
D	v	v		x		
E	v	v			x	
F	v	v	v	v	v	x

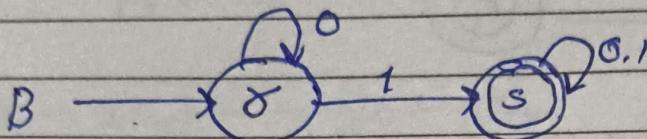
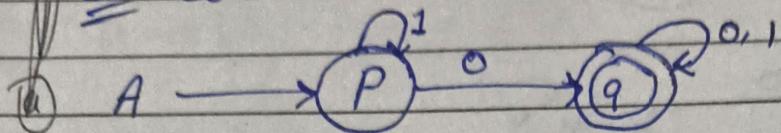
* normal se final jone vala ho usi ko mask karna hai

* Ek normal and ek final state hoga compulsory he



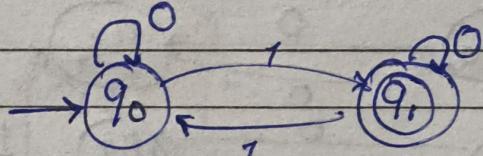
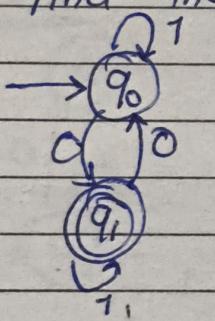
Tute-5

Q-1 Construct $A \cap B$ where A and B is given

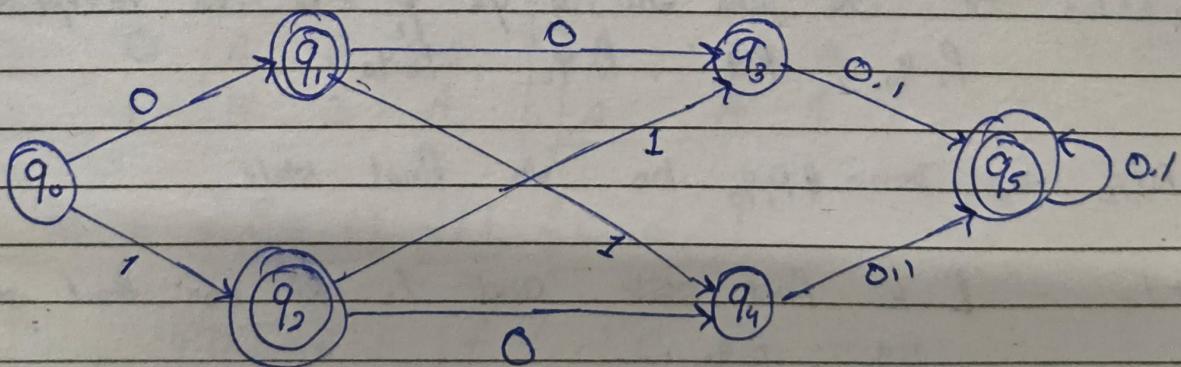


Q-2 $L_1 = \{ \text{ starts with } a \text{ and ends with } b \}$ and $L_2 = \{ \text{ starts with } b \text{ and ends with } a \}$. Then find $L = L_1 \cup L_2$ or
 $L = L_1 + L_2$

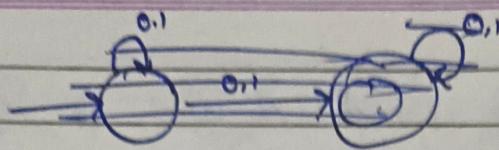
Q-3 find the product of two FA given below:



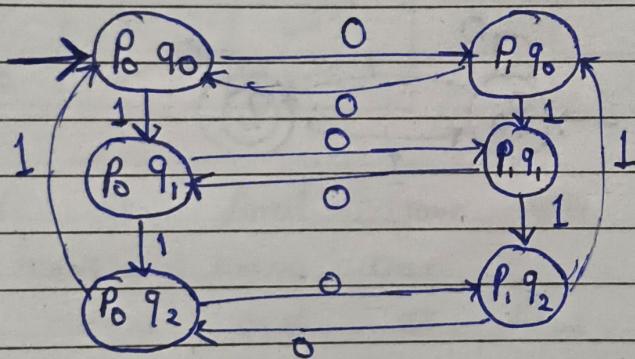
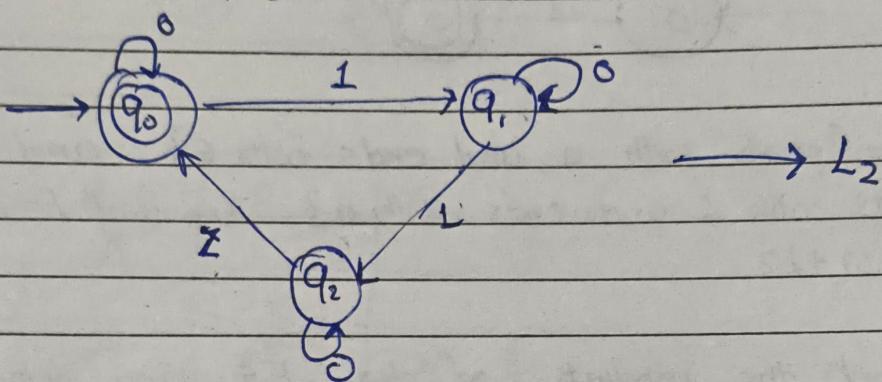
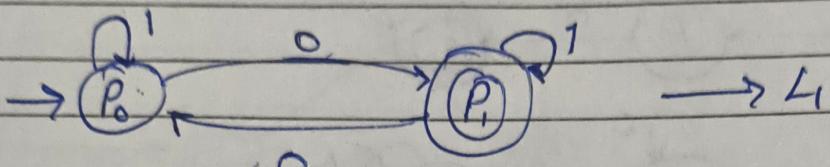
Q-4 Minimize the DFA shown below using table filling method:



Sol 1-1



Eg



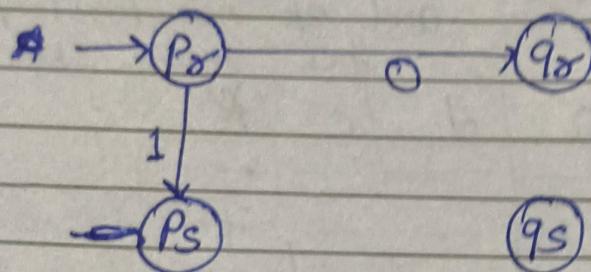
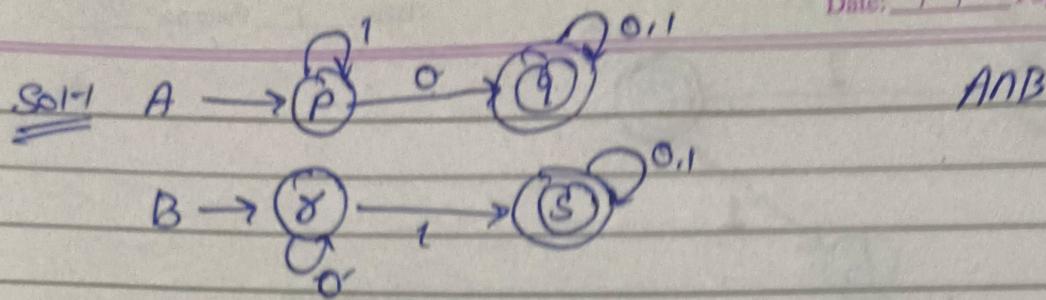
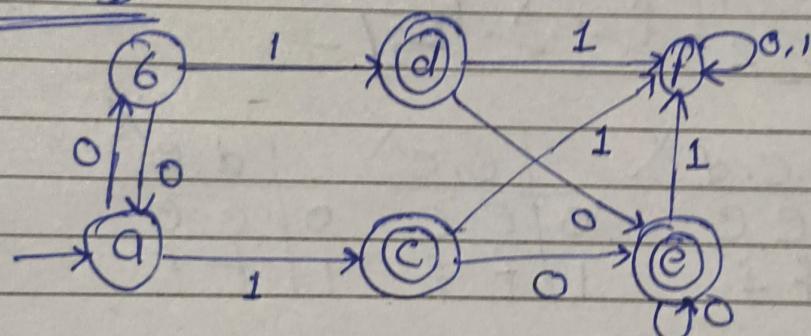
$L_1 \cup L_2 \rightarrow$ So jaha bhi q ya p be vo accept state
 $p_0q_0, p_1q_1, p_1q_2, p_0q_0$ (final)

$L_1 \cap L_2 \rightarrow$ Dono q p_0q_0 be vo final state

$L_1 - L_2 = L_1$ ki final state and L_2 ki non final state
 p_1q_1, p_1q_2

$L_2 - L_1 = p_0q_0$, J_1 - final ka non final viswariya

$L_1, L_2 = L_1$ ki sare final state se L_2 ki starting state jad le,

T-4 Q-5

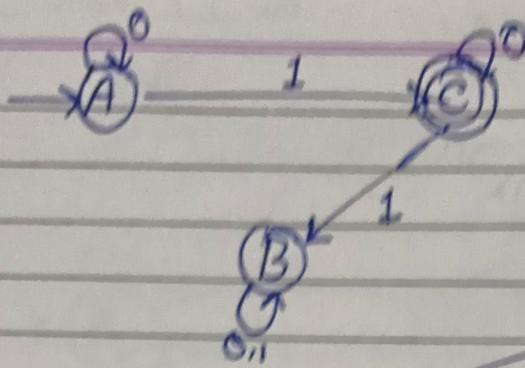
$$\pi_0 = \{ \underbrace{\{a, b, f\}}_A, \underbrace{\{c, d, e\}}_B \}$$

	a	b	f	c	d	e
0	A	A	A	B	B	B
1	B	B	A	A	A	A

$$\pi_1 = \{ \underbrace{\{a, b\}}_A, \underbrace{\{f\}}_B, \underbrace{\{c, d, e\}}_C \}$$

	a	b	f	c	d	e
0	A	A	B	C	C	C
1	B	B	B	B	B	B

$$\pi_2 = \{ \{a, b\}, \{f\}, \{c, d, e\} \} \quad \boxed{\pi_1 = \pi_2}$$



Iteration

①st state me ek final
and ek non-final pe
tak legana hai

Now by table filling ↴

	a.	b	c	d	e	f
a	X	-	-	-	-	-
b	X	-	-	-	-	-
c	-1	-1	-	-	-	-
d	-1	-1	X	-	-	-
e	-1	-1	X	-	-	-
f	=2	=2	1	1	1	-

2nd Iteration

Q, G remain go to 3 rd iteration		C, d X	C, e X	d e X
0	c g	0 c c	0 c e	0 e e
1	c d	1 f f	1 f f	1 f f

a, f ↴		G f ↴	
0	6 f	0	a f
1	c f	1	d f

a, c

third

g, b X	
0	6 g
1	c b

Unmarked = $(a, g), (c, d) \}^{cde}$
 $(c, e), (e, d) \}^{cde}$

So both gaya na akela