
Analyzing the Weekly S&P Stock Market Data using Logistic Regression

CMSC 6950 - COMPUTER BASED RESEARCH TOOLS AND APPLICATIONS

TERM PROJECT

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SUBMITTED BY

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Abstract

1 Introduction

The S&P 500, or basically the S&P, is a stock exchange index that evaluates the stock performance of 500 huge companies recorded on stock trades in the United States. It is one of the most usually followed equity indicators, and many believe it to be probably the best depictions of the U.S. stock exchange. The normal yearly aggregate return of the index, including profits, since beginning in 1926 has been 9.8%; be that as it may, there were more than a few years where the index dropped over 30%. The index has posted yearly increases 70% of the time (Wikipedia contributors (2020)) .

The index is one of the components in calculation of the Conference Board Leading Economic Index, used to predict the course of the economy. The index is related with numerous ticker images, including: $\hat{\text{GSPC}}$, INX , and $\text{\$SPX}$, dependent on marketplace or internet site. The index value is revised each 15 seconds, or 1,559 times per business day, with price upgrade circulated by Reuters (Duggan, Wayne (2019)).

2 Materials and Methods

2.1 Logistic Regression

Let attempt to comprehend logistic regression by thinking about a logistic model with given parameters, at that point perceiving how the coefficients can be assessed from data. Think about a model with two forecasters, x_1 and x_2 , and single binary (Bernoulli) response variable Y , which we represent $p = P(Y = 1)$. We believe a linear correlation sandwiched between the predictor variables and the log-odds of the outcome that $Y = 1$. This linear correlation* can be written in the ensuing mathematical structure (where ℓ is the log-odds, b is the base of the logarithm, and β_i are parameters of the model):

$$\ell = \log_b \frac{p}{1-p} = \beta_0 + \beta_1 x_1 + \beta_2 x_2 \quad (1)$$

We can retrieve the log-odds:

$$\frac{p}{1-p} = b^{\beta_0 + \beta_1 x_1 + \beta_2 x_2}. \quad (2)$$

By straightforward algebraic manipulation, the likelihood that $Y = 1$ is

$$p = \frac{b^{\beta_0 + \beta_1 x_1 + \beta_2 x_2}}{b^{\beta_0 + \beta_1 x_1 + \beta_2 x_2} + 1} = \frac{1}{1 + b^{-(\beta_0 + \beta_1 x_1 + \beta_2 x_2)}}. \quad (3)$$

The equation above reveals that as soon as β_i are fixed, we can effortlessly calculate either the log-odds that $Y = 1$ for a given observation, or the likelihood that $Y = 1$ for

a given observation. The main usage of a logistic model is to be provided an observation (x_1, x_2) , and calculate the likelihood p that $Y = 1$. In many applications, the base b of the logarithm is generally taken to be e . Nevertheless, in some cases it can be simpler to convey results by working in base 2, or base 10 (Wikipedia contributors (2020)).

2.2 Data Collection and Description

In this project, the dataset used was downloaded or collected online from <https://www.picostat.com/dataset/r-dataset-package-islr-weekly> by executing a pandas python code.

This dataset consists of percentage returns for the stock index over 1089 weeks for 21 years, from the beginning of 1990 to the end of 2010. For each data, we have the percentage returns for each of the first previous trading weeks, Lag1 through Lag5. We have also Volume (the number of shares traded on the previous day, in billions), Today (the percentage return on the date in question) and Direction (whether the market was Up or Down on this date).

2.3 Python-Software Packages Used

The dataset downloaded was then analyzed mainly using three open source python packages. These packages are Pingouin, Statsmodels and PyCM packages.

The Pingouin package was used to determine the structure, summary, correlation, normality of variables in the dataset and also analyze the dataset with the logistic regression model (Vallat, R. (2018)). The Statsmodel was then used to determine the Confusion matrix of the logistic regression output derived. Lastly, the PyCM package was used to check the performance or accuracy or predictions of these models (Haghighi et al., (2018)).

3 Analysis and Results

3.1 Numerical and Graphical Summaries of Data

3.1.1 Structure of Data

The Table ?? below shows the structure of the dataset used. This data consists of percentage returns for the stock index over 1089 weeks for 21 years, from the beginning of 1990 to the end of 2010. For each column, we have the percentage returns for each of the first previous trading weeks, Lag1 through Lag5. We have also Volume, Today and Direction.

Year	Lag1	Lag2	Lag3	Lag4	Lag5	Volume	Today	Direction
1990	0.816	1.572	-3.936	-0.229	-3.484	0.154976	-0.270	Down
1990	-0.270	0.816	1.572	-3.936	-0.229	0.148574	-2.576	Down
1990	-2.576	-0.270	0.816	1.572	-3.936	0.159837	3.514	Up
1990	3.514	-2.576	-0.270	0.816	1.572	0.161630	0.712	Up
1990	0.712	3.514	-2.576	-0.270	0.816	0.153728	1.178	Up

Table 1: Structure of Data

3.1.2 Descriptive Statistics of Data

From Table ??, we can see the statistics of the variables employed for this study. This includes the count, minimum, maximum, mean, median (50%), 1st quartile (25%) and 3rd quartile (75%).

It can be observed that Lag 5 has the highest standard deviation value of 2.361285 indicating that Lag 5 had the highest level of impact on Direction. Also, Volume had the least level of impact due to its low standard deviation value (1.686636)

	Year	Lag1	Lag2	Lag3	Lag4	Lag5	Volume	Today
count	1089.000000	1089.000000	1089.000000	1089.000000	1089.000000	1089.000000	1089.000000	1089.000000
mean	2000.048669	0.150585	0.151079	0.147205	0.145818	0.139893	1.574618	0.149899
std	6.033182	2.357013	2.357254	2.360502	2.360279	2.361285	1.686636	2.356927
min	1990.000000	-18.195000	-18.195000	-18.195000	-18.195000	-18.195000	0.087465	-18.195000
25%	1995.000000	-1.154000	-1.154000	-1.158000	-1.158000	-1.166000	0.332022	-1.154000
50%	2000.000000	0.241000	0.241000	0.241000	0.238000	0.234000	1.002680	0.241000
75%	2005.000000	1.405000	1.409000	1.409000	1.409000	1.405000	2.053727	1.405000
max	2010.000000	12.026000	12.026000	12.026000	12.026000	12.026000	9.328214	12.026000

Table 2: Descriptive Statistics of Data

3.1.3 Normality Test of Variables

Here, the Pingouin python package was used to check for normality in the variables. The normal distribution fit of the independent variables (Lag 1, Lag 2, Lag 3, Lag 4, Lag 5, Volume, Today) is seen in the Table ??.

It can be seen from the table that none of the independent variables was normal. In other words, they all showed signs of skewness.

3.2 Correlation Analysis

3.2.1 Graphical Summary of Data

From Table ??, Table ?? and Figure ??, some years seem to have more or less variations than others. Looking at the shape of the various Lag features and the Year. There does

	W	pval	normal
Year	0.950223	9.951609e-19	False
Lag 1	0.948756	5.232496e-19	False
Lag 2	0.948813	5.364750e-19	False
Lag 3	0.949282	6.578534e-19	False
Lag 4	0.949279	6.570206e-19	False
Lag 5	0.949428	7.011749e-19	False
Volume	0.787729	2.101803e-35	False
Today	0.948765	5.252924e-19	False

Table 3: Normality Test of Variables

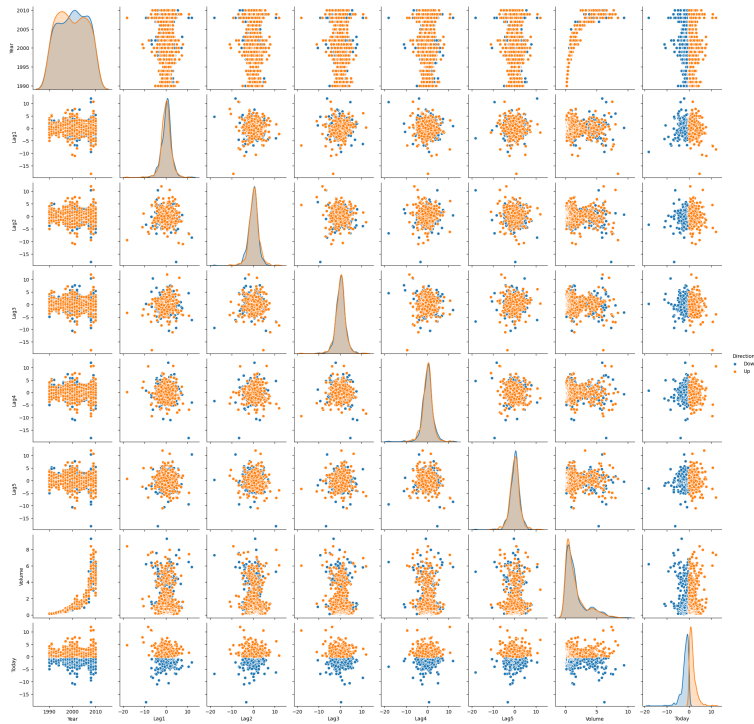


Figure 1: Graphical Summary of Correlation between Variables

seem to be some autocorrelation in the variability of the Lags and the year. Perhaps some years, people are more skittish than other years, and this takes a while to wear off. There appears to be very little if any correlation between Lag and other lags. Direction appears slightly skewed by a few of the lags, perhaps Lag5, and Lag1.

Also, there is no obvious pattern aside that of Volume of shares and years. Looking closely at plot of volume and time, we can see that the Volume of shares has grown exponentially over time.

3.2.2 Graphical Correlation Analysis between Volume and Year

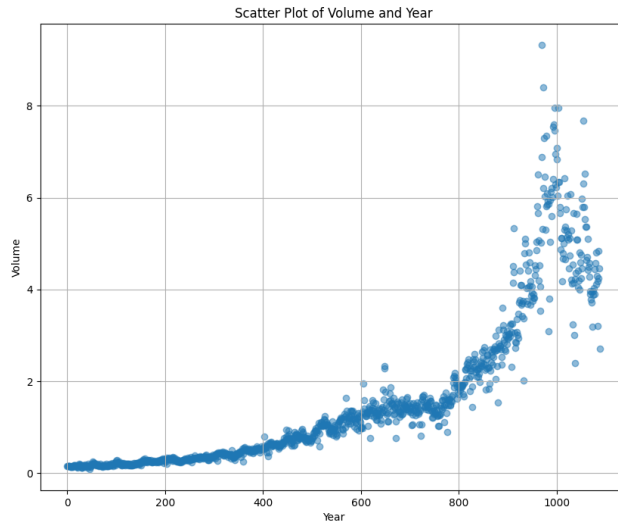


Figure 2: Graphical Summary of Correlation between Variables

From Figure ??, there is relation between the variables in question. From visualization, it is clear that there is high correlation between Volume and Year. This appears to be an exponential relationship where volume increases exponentially as a function of year.

Further verification was done with Pingouin correlation package as seen in Table ?? and it was seen that the R^2 and Adjusted R^2 were quite large hence indicating a high correlation between Volume and Year.

	n	r	CI95%	r2	adj_r2	p-val	BF10	power
pearson	1089	0.841942	[0.82, 0.86]	0.708866	0.70833	1.559688e-293	2.042e+289	1.0

Table 4: Pearson Correlation between Volume and Year

4 Conclusion

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