

1.

$$\begin{pmatrix} -7 & -1 & -2 & 5 \\ -6 & -1 & -2 & 5 \\ 4 & 1 & 3 & -7 \end{pmatrix}$$

$$\begin{aligned} & \xrightarrow{\text{line2} \leftarrow \text{line1}} \begin{pmatrix} -7 & -1 & -2 & 5 \\ 1 & 0 & 0 & 0 \\ 4 & 1 & 3 & -7 \end{pmatrix} \xrightarrow{\text{line1} \leftrightarrow \text{line2}} \begin{pmatrix} 1 & 0 & 0 & 0 \\ -7 & -1 & -2 & 5 \\ 4 & 1 & 3 & -7 \end{pmatrix} \\ & \xrightarrow{\text{line2} \leftarrow \text{line1} \times (7)} \begin{pmatrix} 1 & 0 & 0 & 0 \\ 0 & -1 & -2 & 5 \\ 4 & 1 & 3 & -7 \end{pmatrix} \xrightarrow{\text{line3} \leftarrow \text{line1} \times (4)} \begin{pmatrix} 1 & 0 & 0 & 0 \\ 0 & -1 & -2 & 5 \\ 0 & 1 & 3 & -7 \end{pmatrix} \\ & \xrightarrow{\text{line2} \leftrightarrow \text{line3}} \begin{pmatrix} 1 & 0 & 0 & 0 \\ 0 & 1 & 3 & -7 \\ 0 & -1 & -2 & 5 \end{pmatrix} \xrightarrow{\text{line3} \leftarrow \text{line2}} \begin{pmatrix} 1 & 0 & 0 & 0 \\ 0 & 1 & 3 & -7 \\ 0 & 0 & 1 & -2 \end{pmatrix} \\ & \xrightarrow{\text{line2} \leftarrow \text{line3} \times (3)} \begin{pmatrix} 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & -1 \\ 0 & 0 & 1 & -2 \end{pmatrix} \end{aligned}$$

したがって,  $(x, y, z) = (0, -1, -2)$

2.

$$\begin{pmatrix} 1 & -1 & 2 & -6 \\ -1 & 3 & -5 & 9 \\ 2 & 1 & -1 & -7 \end{pmatrix}$$

$$\begin{aligned} & \xrightarrow{\text{line2} \leftarrow \text{line1}} \begin{pmatrix} 1 & -1 & 2 & -6 \\ 0 & 2 & -3 & 3 \\ 2 & 1 & -1 & -7 \end{pmatrix} \xrightarrow{\text{line3} \leftarrow \text{line1} \times (2)} \begin{pmatrix} 1 & -1 & 2 & -6 \\ 0 & 2 & -3 & 3 \\ 0 & 3 & -5 & 5 \end{pmatrix} \\ & \xrightarrow{\text{line3} \leftarrow \text{line2}} \begin{pmatrix} 1 & -1 & 2 & -6 \\ 0 & 2 & -3 & 3 \\ 0 & 1 & -2 & 2 \end{pmatrix} \xrightarrow{\text{line2} \leftrightarrow \text{line3}} \begin{pmatrix} 1 & -1 & 2 & -6 \\ 0 & 1 & -2 & 2 \\ 0 & 2 & -3 & 3 \end{pmatrix} \\ & \xrightarrow{\text{line1} \leftarrow \text{line2}} \begin{pmatrix} 1 & 0 & 0 & -4 \\ 0 & 1 & -2 & 2 \\ 0 & 2 & -3 & 3 \end{pmatrix} \xrightarrow{\text{line3} \leftarrow \text{line2} \times (2)} \begin{pmatrix} 1 & 0 & 0 & -4 \\ 0 & 1 & -2 & 2 \\ 0 & 0 & 1 & -1 \end{pmatrix} \\ & \xrightarrow{\text{line2} \leftarrow \text{line3} \times (2)} \begin{pmatrix} 1 & 0 & 0 & -4 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & 1 & -1 \end{pmatrix} \end{aligned}$$

したがって,  $(x, y, z) = (-4, 0, -1)$

3.

$$\begin{pmatrix} -1 & 1 & -1 & 1 \\ 8 & -7 & 6 & -3 \\ -5 & 5 & -6 & 7 \end{pmatrix}$$

$$\begin{aligned} & \xrightarrow{\text{line1} \times (-1)} \begin{pmatrix} 1 & -1 & 1 & -1 \\ 8 & -7 & 6 & -3 \\ -5 & 5 & -6 & 7 \end{pmatrix} \xrightarrow{\text{line2} \leftarrow \text{line1} \times (8)} \begin{pmatrix} 1 & -1 & 1 & -1 \\ 0 & 1 & -2 & 5 \\ -5 & 5 & -6 & 7 \end{pmatrix} \\ & \xrightarrow{\text{line3} \leftarrow \text{line1} \times (5)} \begin{pmatrix} 1 & -1 & 1 & -1 \\ 0 & 1 & -2 & 5 \\ 0 & 0 & -1 & 2 \end{pmatrix} \xrightarrow{\text{line1} \leftarrow \text{line2}} \begin{pmatrix} 1 & 0 & -1 & 4 \\ 0 & 1 & -2 & 5 \\ 0 & 0 & -1 & 2 \end{pmatrix} \end{aligned}$$

$$\begin{aligned}
& \xrightarrow{\text{line3} \times (-1)} \begin{pmatrix} 1 & 0 & -1 & 4 \\ 0 & 1 & -2 & 5 \\ 0 & 0 & 1 & -2 \end{pmatrix} \xrightarrow{\text{line1} += \text{line3}} \begin{pmatrix} 1 & 0 & 0 & 2 \\ 0 & 1 & -2 & 5 \\ 0 & 0 & 1 & -2 \end{pmatrix} \\
& \xrightarrow{\text{line2} += \text{line3} \times (2)} \begin{pmatrix} 1 & 0 & 0 & 2 \\ 0 & 1 & 0 & 1 \\ 0 & 0 & 1 & -2 \end{pmatrix}
\end{aligned}$$

したがって,  $(x, y, z) = (2, 1, -2)$

4.

$$\begin{pmatrix} 1 & 1 & -1 & 3 \\ -3 & -2 & 3 & -9 \\ -3 & -1 & 2 & -8 \end{pmatrix}$$

$$\begin{aligned}
& \xrightarrow{\text{line2} += \text{line1} \times (3)} \begin{pmatrix} 1 & 1 & -1 & 3 \\ 0 & 1 & 0 & 0 \\ -3 & -1 & 2 & -8 \end{pmatrix} \xrightarrow{\text{line3} += \text{line1} \times (3)} \begin{pmatrix} 1 & 1 & -1 & 3 \\ 0 & 1 & 0 & 0 \\ 0 & 2 & -1 & 1 \end{pmatrix} \\
& \xrightarrow{\text{line1} -= \text{line2}} \begin{pmatrix} 1 & 0 & -1 & 3 \\ 0 & 1 & 0 & 0 \\ 0 & 2 & -1 & 1 \end{pmatrix} \xrightarrow{\text{line3} -= \text{line2} \times (2)} \begin{pmatrix} 1 & 0 & -1 & 3 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & -1 & 1 \end{pmatrix} \\
& \xrightarrow{\text{line3} \times (-1)} \begin{pmatrix} 1 & 0 & -1 & 3 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & 1 & -1 \end{pmatrix} \xrightarrow{\text{line1} += \text{line3}} \begin{pmatrix} 1 & 0 & 0 & 2 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & 1 & -1 \end{pmatrix}
\end{aligned}$$

したがって,  $(x, y, z) = (2, 0, -1)$

6.

$$\begin{pmatrix} 1 & -2 & -1 & -2 \\ -2 & 4 & 1 & 2 \\ -3 & 5 & 3 & 7 \end{pmatrix}$$

$$\begin{aligned}
& \xrightarrow{\text{line2} += \text{line1} \times (2)} \begin{pmatrix} 1 & -2 & -1 & -2 \\ 0 & 0 & -1 & -2 \\ -3 & 5 & 3 & 7 \end{pmatrix} \xrightarrow{\text{line3} += \text{line1} \times (3)} \begin{pmatrix} 1 & -2 & -1 & -2 \\ 0 & 0 & -1 & -2 \\ 0 & -1 & 0 & 1 \end{pmatrix} \\
& \xrightarrow{\text{line2} \leftrightarrow \text{line3}} \begin{pmatrix} 1 & -2 & -1 & -2 \\ 0 & -1 & 0 & 1 \\ 0 & 0 & -1 & -2 \end{pmatrix} \xrightarrow{\text{line2} \times (-1)} \begin{pmatrix} 1 & -2 & -1 & -2 \\ 0 & 1 & 0 & -1 \\ 0 & 0 & -1 & -2 \end{pmatrix} \\
& \xrightarrow{\text{line1} += \text{line2} \times (2)} \begin{pmatrix} 1 & 0 & -1 & -4 \\ 0 & 1 & 0 & -1 \\ 0 & 0 & -1 & -2 \end{pmatrix} \xrightarrow{\text{line3} \times (-1)} \begin{pmatrix} 1 & 0 & -1 & -4 \\ 0 & 1 & 0 & -1 \\ 0 & 0 & 1 & 2 \end{pmatrix} \\
& \xrightarrow{\text{line1} += \text{line3}} \begin{pmatrix} 1 & 0 & 0 & -2 \\ 0 & 1 & 0 & -1 \\ 0 & 0 & 1 & 2 \end{pmatrix}
\end{aligned}$$

したがって,  $(x, y, z) = (-2, -1, 2)$