

Electromagnetism and Gravity with Continuous Spin

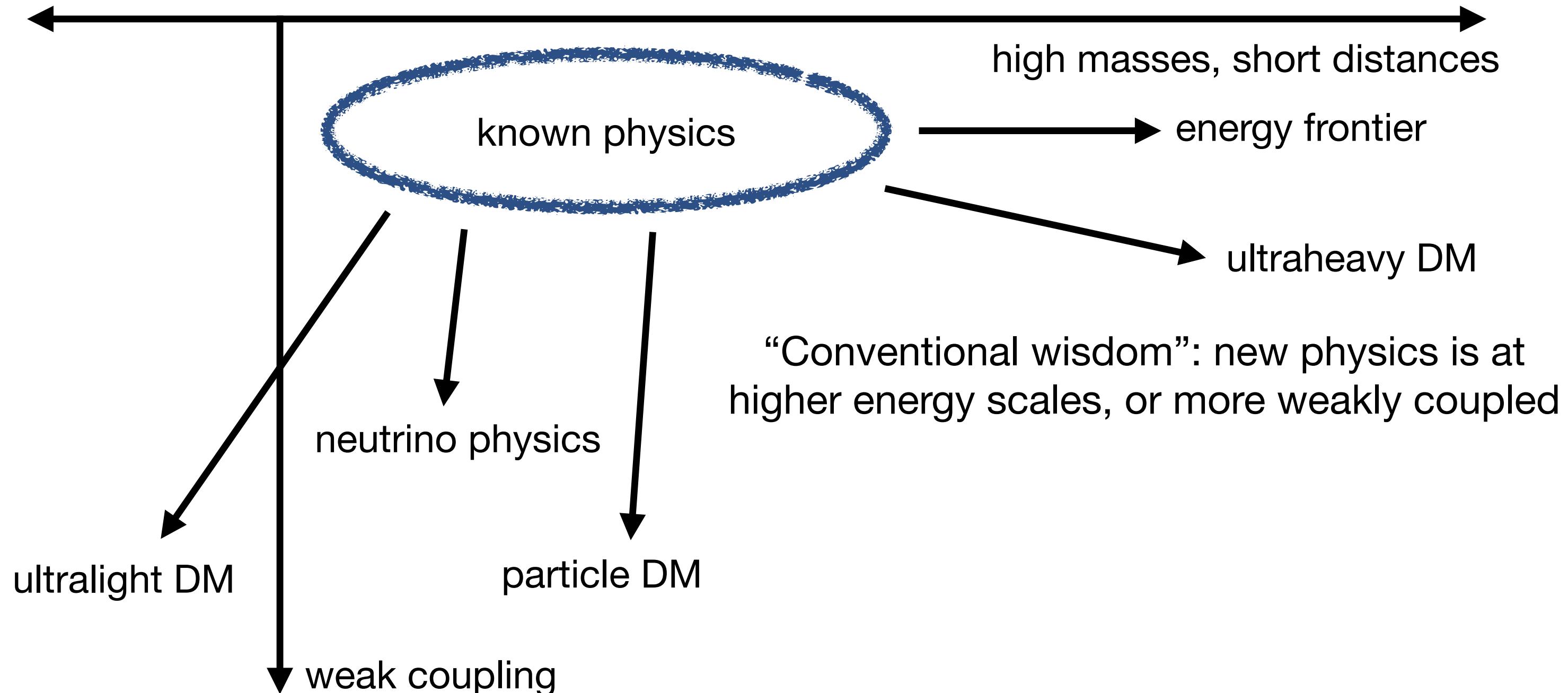
Kevin Zhou

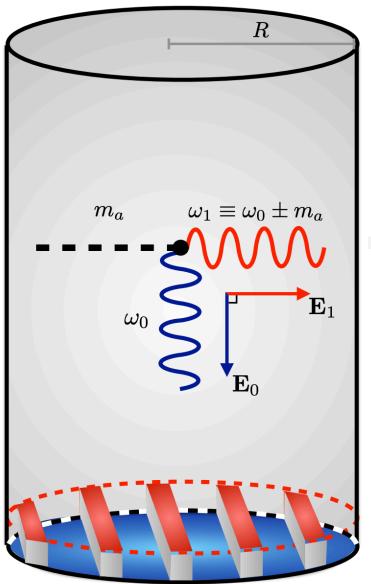


Tsinghua University Physics Seminar — July 21, 2025

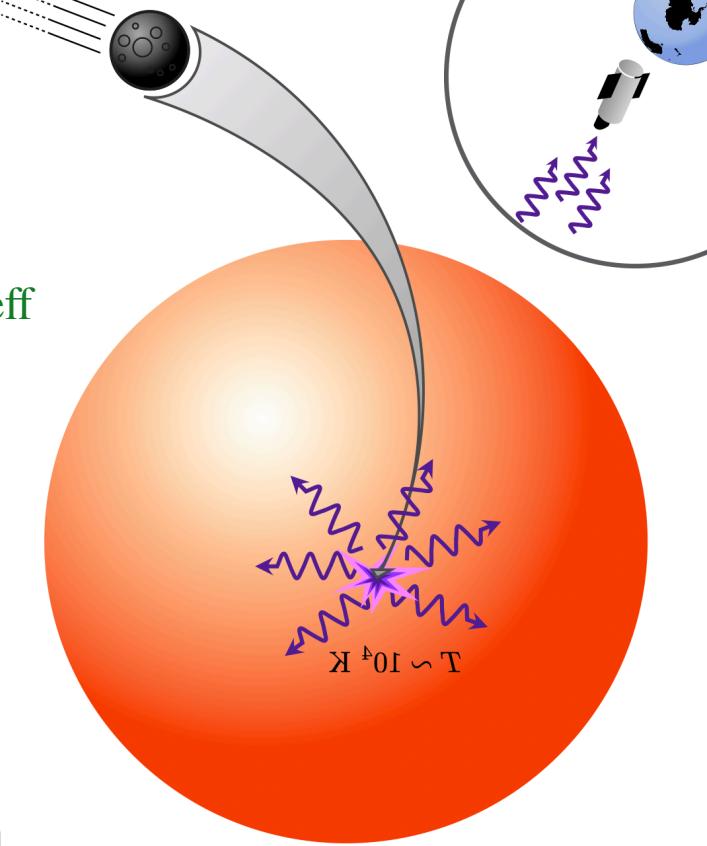
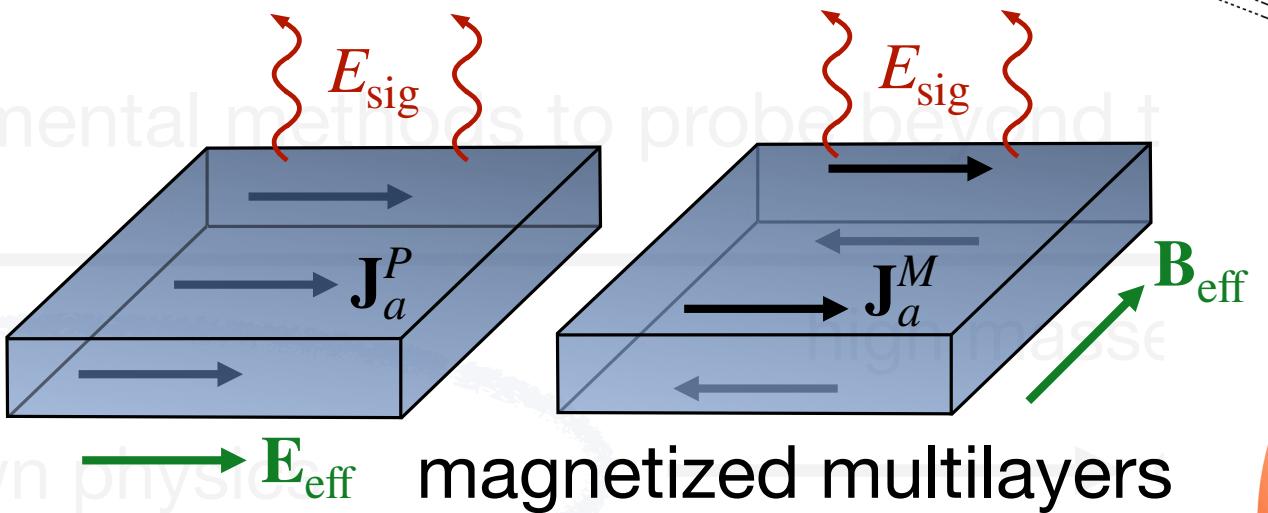
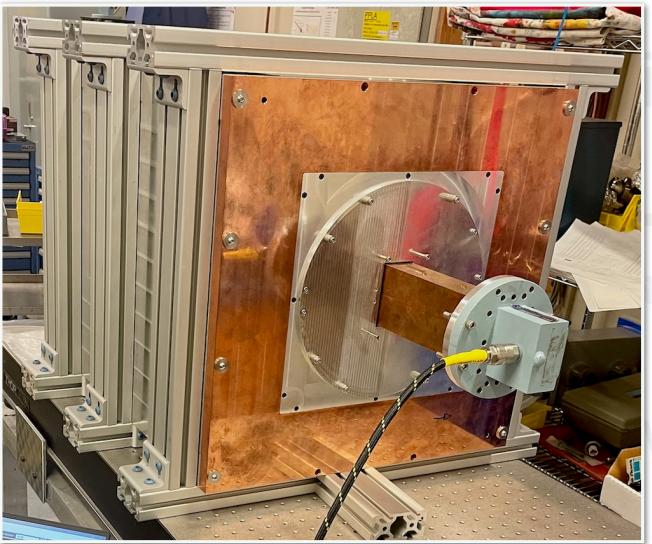
arXiv:2303.04816 (JHEP), with Philip Schuster and Natalia Toro

My focus is finding new experimental methods to probe beyond the Standard Model.



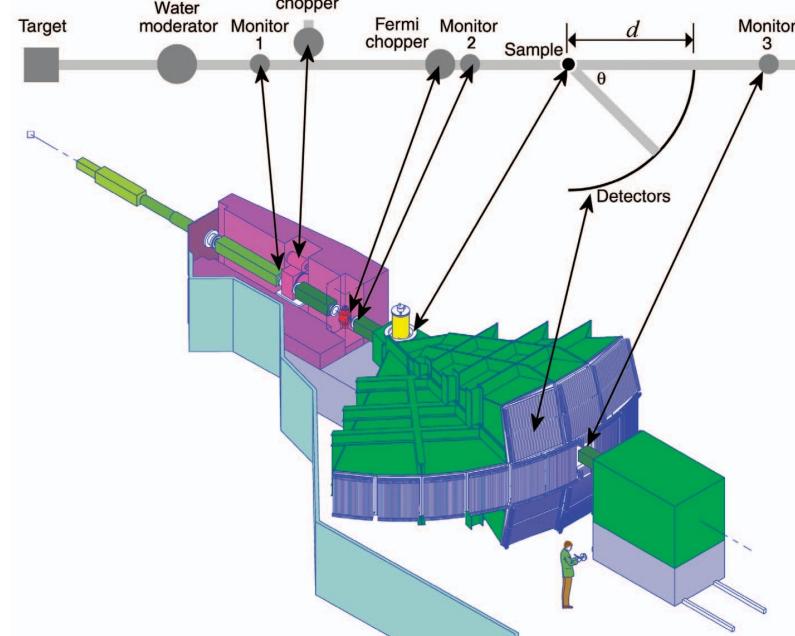


superconducting heterodyne

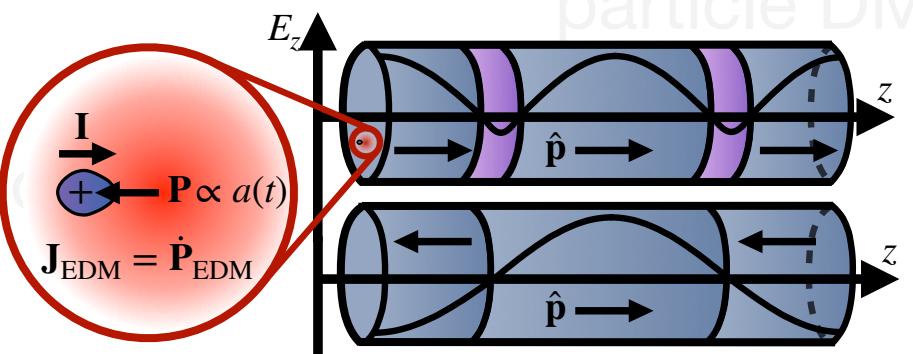


(accordingly, much of my work has been proposing new ways to search for dark matter, at a variety of mass scales)

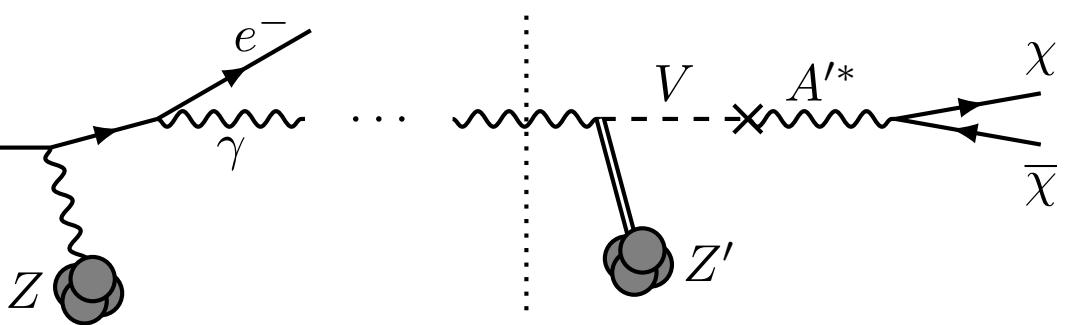
neutron scattering



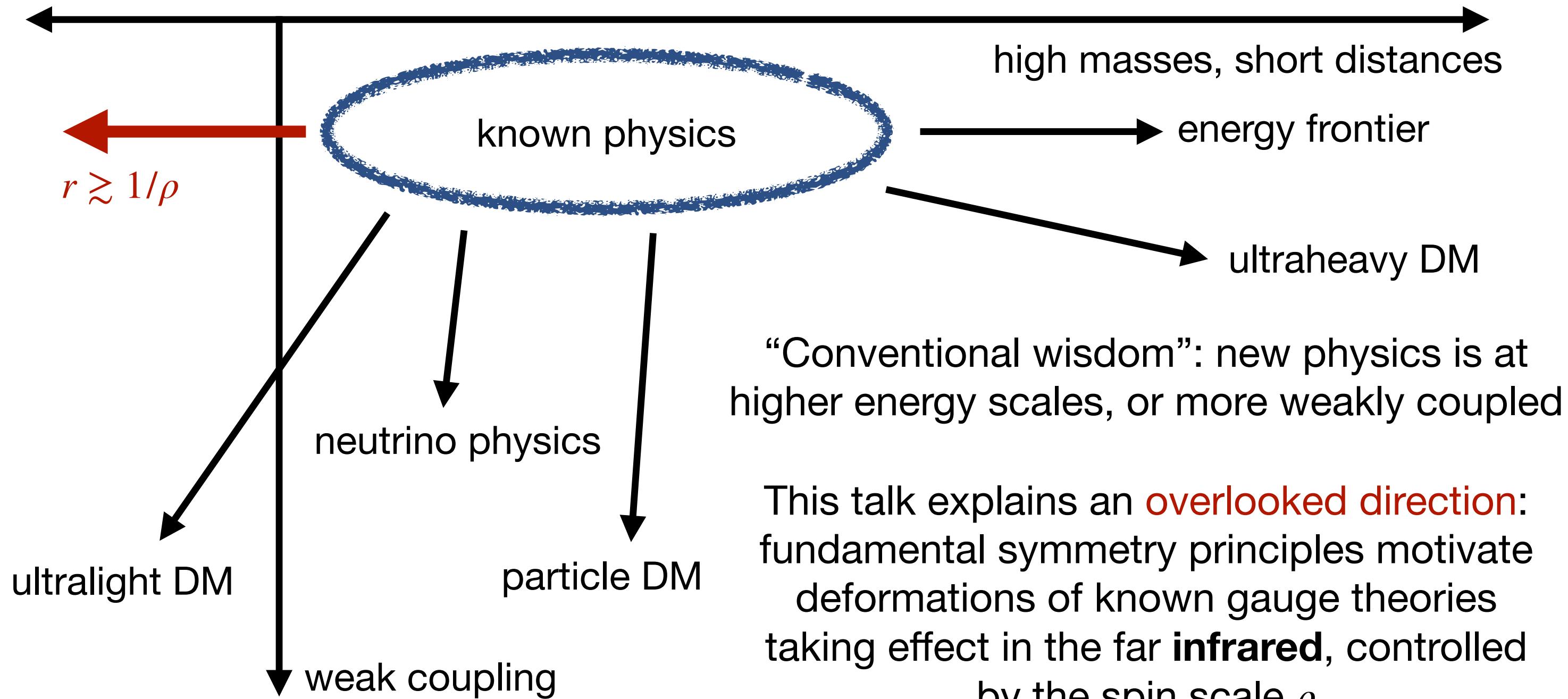
polarization haloscopes



invisible meson decays



My focus is finding new experimental methods to probe beyond the Standard Model.



Classifying Particles by Mass and Spin Scale

States transform under translations P^μ and rotations/boosts $J^{\mu\nu}$

Particle states with definite momentum obey $P^\mu |k, \sigma\rangle = k^\mu |k, \sigma\rangle$

Little group transformations $W^\mu = \frac{1}{2}\epsilon^{\mu\nu\rho\sigma}J_{\nu\rho}k_\sigma$ affect only internal state σ

Different types of particles classified by $P^2 = m^2$ and $W^2 = -\rho^2$

What is the physical meaning of the spin scale ρ ?

Classifying Particles by Mass and Spin Scale

For $m^2 > 0$, representations are spin S massive particles

States are $|k, h\rangle$ for helicity $h = -S, \dots, S$, which is not Lorentz invariant

Boosts mix helicities by amount determined by $\rho = m\sqrt{S(S+1)}$

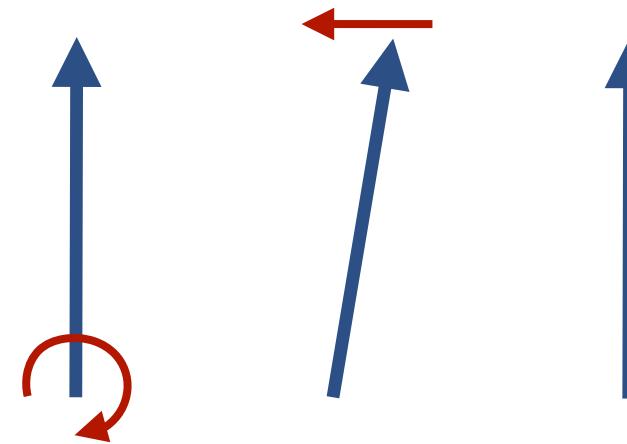
For $m^2 = 0$, states are still indexed by helicity $|k, h\rangle$

Spin scale again determines how helicity varies under boosts

The Massless Little Group

For a massless particle, $k^\mu = (\omega, 0, 0, \omega)$, little group generators are

$$R = J_z$$
$$R | k, h \rangle = h | k, h \rangle$$



$$T_1 \propto J_x + K_y$$
$$T_2 \propto J_y - K_x$$

Defining $T_\pm = T_1 \pm iT_2$, commutation relations imply

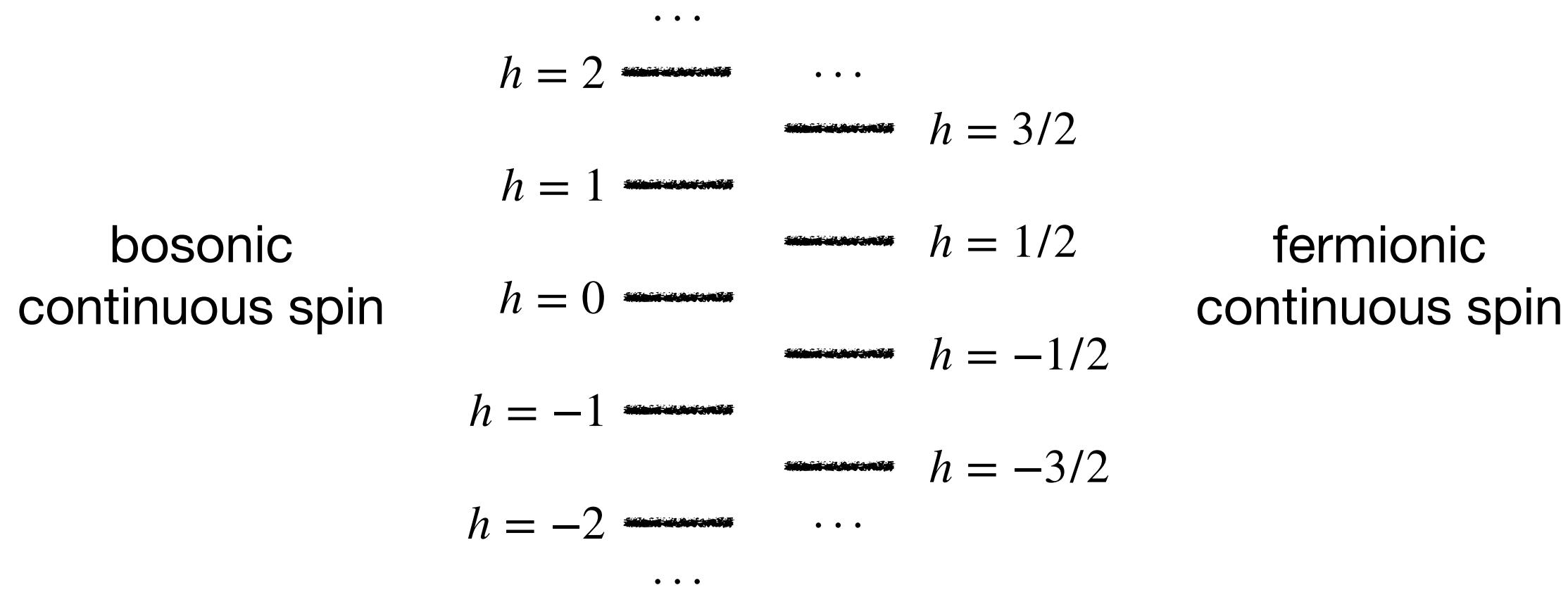
$$T_\pm | k, h \rangle = \rho | k, h \pm 1 \rangle$$

Generic result is an **infinite** ladder of integer-spaced helicities!

Allowed Helicities for Massless Particles

Generic massless particle representation has continuous-valued spin scale ρ

Since h is always integer or half-integer, gives two options, known since 1930s:



(plus supersymmetric, (A)dS, higher/lower dimension variants)

Allowed Helicities for Massless Particles

If we set $\rho = 0$, recover a single helicity h (related to $-h$ by CPT symmetry)

Focus on bosonic case, which can mediate long-range $1/r^2$ forces

- $h = 0$ massless scalar (requires fine-tuning)
- $|h| = 1$ photon (minimal coupling to conserved charge)
- $|h| = 2$ graviton (minimal coupling to stress-energy)
- $|h| = 3$ higher spin (no minimal couplings allowed)
- ...

Role of each $|h|$ in nature well-understood from general arguments from 1960s

Why Not Consider Continuous Spin?

~~Ruled out by Weinberg soft theorems?~~

Theorems rely on Lorentz invariant h
Generalize to good soft factors for $\rho \neq 0$

Schuster and Toro, JHEP (2013) 104/105

~~Incompatible with field theory?~~

Simple free gauge theory found
Schuster and Toro, PRD (2015)

~~Can't interact with anything?~~

Addressed in our paper!
Schuster, Toro, Zhou, JHEP (2023)

~~Just way too complicated?~~

Addressed in our paper!
Schuster, Toro, Zhou, JHEP (2023)

Infinite set of h 's leads to infinities in scattering/cosmology/astrophysics/...?

All but one $|h|$ decouples in the $\rho \rightarrow 0$ limit!

$h = 0$ scalar-like (recovers Yukawa theory)

$|h| = 1$ vector-like (recovers electromagnetism)

$|h| = 2$ tensor-like (recovers linearized gravity)

Why Consider Continuous Spin?

For the field theorist: “because it’s there”

Simple and directly motivated by the postulates of relativity and quantum mechanics, but still not fully understood

For the experimentalist: “because it might really be there”

Theory predicts ρ -dependent deviations from electromagnetism and general relativity
The value of ρ is unknown, and only experiment can determine it

Force in a radiation background:
$$\frac{\mathbf{F}}{q} = \mathbf{E} + \mathbf{v} \times \mathbf{B} - \left(\frac{\rho v_{\perp}}{2\omega} \right)^2 \left(\mathbf{E}_{\perp} + \frac{\mathbf{E}}{2} \right) + \dots$$

Significant correction when particles travel distance $\gtrsim 1/\rho$, total result always well-behaved

Why Consider Continuous Spin?

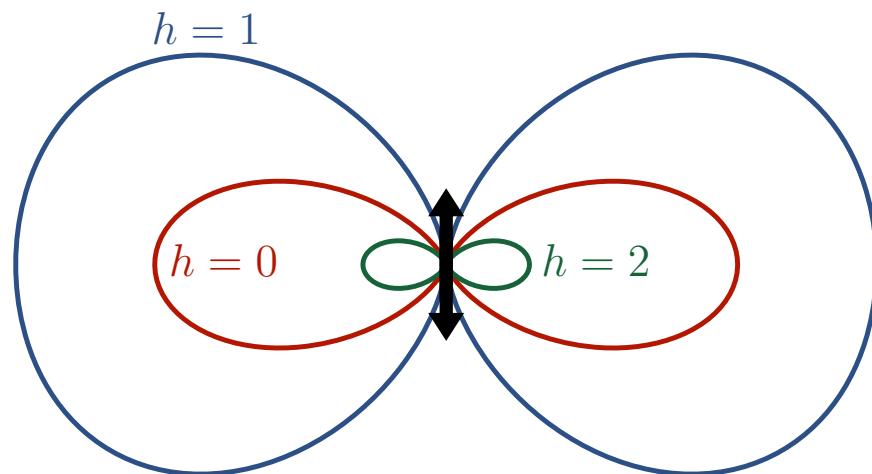
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Radiation from an oscillating particle:



$$P = P_{\text{Larmor}} \times \begin{cases} (\rho\ell)^2/40 + \dots & h = 0 \\ 1 - 3(\rho\ell)^2/20 + \dots & h = \pm 1 \\ (\rho\ell)^2/80 + \dots & h = \pm 2 \end{cases}$$

Significant correction when particles travel distance $\gtrsim 1/\rho$, total result always well-behaved

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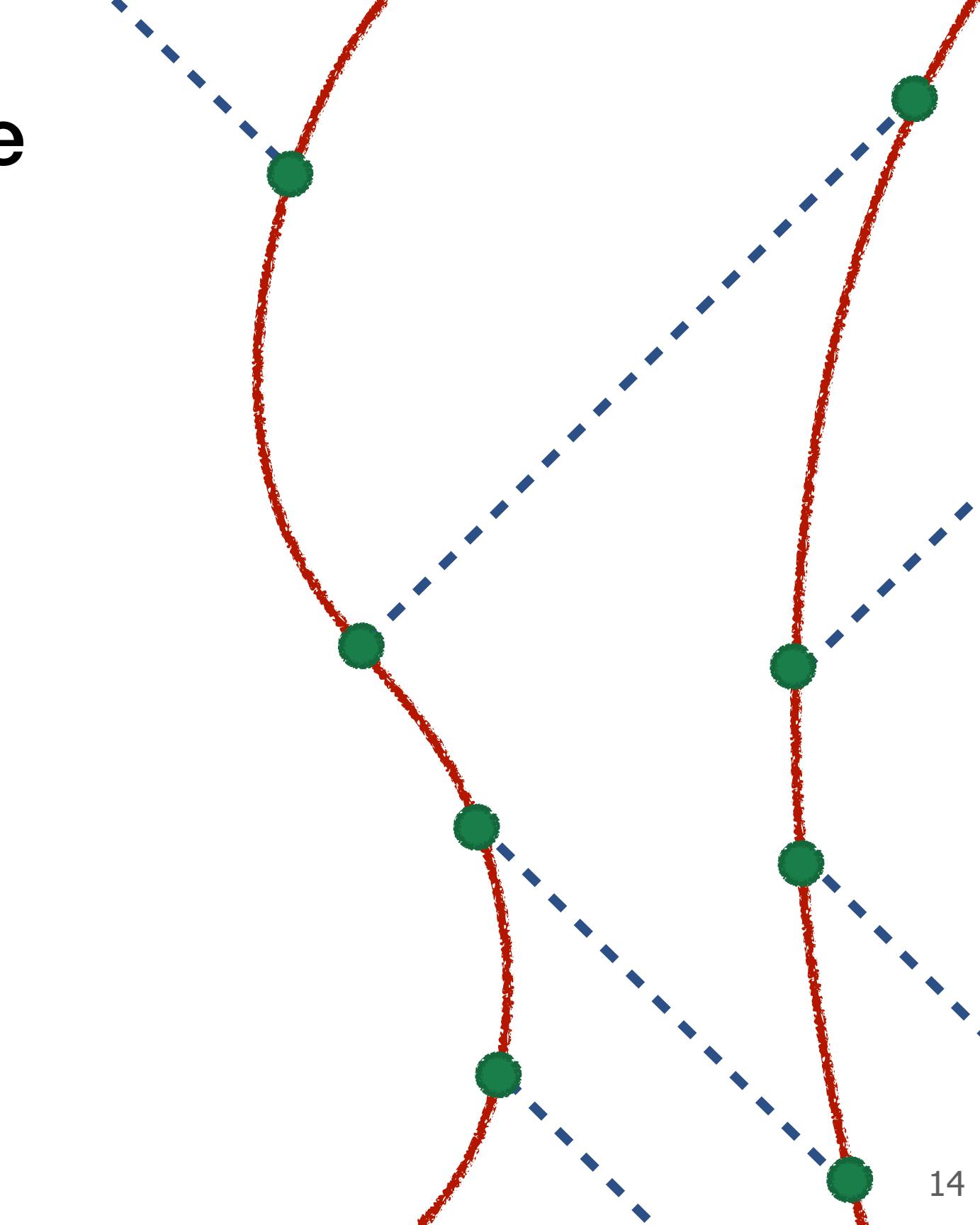
For the model builder: “because it’s novel”

A new infrared deformation of gauge theories, which may shed light on long-distance physics (dark matter, cosmic acceleration)

A new type of spacetime symmetry based on a bosonic superspace, possibly relevant for tuning problems (hierarchy, cosmological constant)

Outline

- Free continuous spin fields
- Coupling to matter particles
- Physics with continuous spin



Free Fields for Massless Particles

Tricky even for $\rho = 0$, by mismatch of field and particle degrees of freedom

scalar $h = 0$

scalar field ϕ , no extra components

photon $h = \pm 1$

vector field A_μ , $4 - 2 = 2$ extra components

must use action with gauge symmetry $\delta A_\mu = \partial_\mu \alpha$

graviton $h = \pm 2$

sym. tensor field $h_{\mu\nu}$, $10 - 2 = 8$ extra components

must use action with gauge symmetry $\delta h_{\mu\nu} = \partial_{(\mu} \xi_{\nu)}$

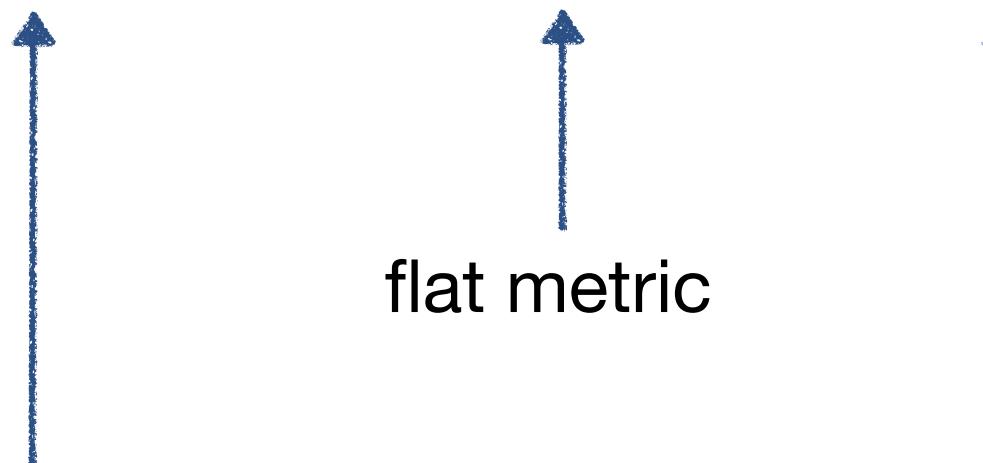
higher spin $|h| > 2$ sym. tensor field $\phi_{\mu_1 \dots \mu_h}$, many extra components

Given complexity of higher h , constructing a continuous spin field seems intractable!

Introducing Vector Superspace

A field in “vector superspace” (x^μ, η^μ) has tensor components of all ranks

$$\Psi(\eta, x) = \phi(x) + \sqrt{2} \eta^\mu A_\mu(x) + (2\eta^\mu \eta^\nu - g^{\mu\nu}(\eta^2 + 1)) h_{\mu\nu}(x) + \dots .$$



just suggestive notation: these components not necessarily related to electromagnetic potential or metric perturbation

Introducing Vector Superspace

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$$\Psi(\eta, x) = \phi(x) + \sqrt{2} \eta^\mu A_\mu(x) + (2\eta^\mu \eta^\nu - g^{\mu\nu}(\eta^2 + 1)) h_{\mu\nu}(x) + \dots$$

Simple expression has free Lagrangian for each tensor field simultaneously!

$$\mathcal{L}[\Psi] = \frac{1}{2} \int_\eta \delta'(\eta^2 + 1)(\partial_x \Psi)^2 + \frac{1}{2} \delta(\eta^2 + 1)(\Delta \Psi)^2 \quad \Delta = \partial_x \cdot \partial_\eta$$

Integration measure normalized by

$$\int_\eta \delta(\eta^2 + 1) \equiv 1$$

Symmetry and basic integration properties fix all other integrals, e.g.

$$\int_\eta \delta'(\eta^2 + 1) = 1, \int_\eta \delta'(\eta^2 + 1) \eta^\mu \eta^\nu = -\frac{1}{2} g^{\mu\nu}, \dots$$

Recovering Familiar Actions

$$\mathcal{L}[\phi] = \frac{1}{2} \int_{\eta} \underbrace{\delta'(\eta^2 + 1)(\partial_x \Psi)^2}_{\text{gives } 1 - \partial_x \phi} + \underbrace{\frac{1}{2} \delta(\eta^2 + 1)(\partial_x \cdot \partial_{\eta} \Psi)^2}_{\partial_{\eta} \phi = 0} \Big|_{\Psi=\phi} = \frac{1}{2} (\partial_x \phi)^2$$

$$\mathcal{L}[A_{\mu}] = \frac{1}{2} \int_{\eta} \underbrace{\delta'(\eta^2 + 1)(\partial_x \Psi)^2}_{(\sqrt{2} \eta_{\mu} \partial_x A^{\mu})^2} + \underbrace{\frac{1}{2} \delta(\eta^2 + 1)(\partial_x \cdot \partial_{\eta} \Psi)^2}_{(\sqrt{2} \partial_{\mu} A^{\mu})^2} \Big|_{\Psi=\sqrt{2}\eta^{\mu}A_{\mu}} = -\frac{1}{2} (\partial_{\mu} A_{\nu})^2 + \frac{1}{2} (\partial_{\mu} A^{\mu})^2$$

More generally, we recover the linearized Einstein-Hilbert action, and higher-rank Fronsdal actions, with no mixing

Recovering Familiar Dynamics

One equation of motion for all helicities:

$$\delta'(\eta^2 + 1) \partial_x^2 \Psi - \frac{1}{2} \Delta (\delta(\eta^2 + 1) \Delta \Psi) = 0 \quad \left\{ \begin{array}{l} \partial^2 \phi = 0 \\ \partial^2 A^\mu - \partial^\mu (\partial \cdot A) = 0 \\ \dots \end{array} \right.$$

One gauge transformation for all helicities:

$$\delta \Psi = (\eta \cdot \partial_x - \frac{1}{2}(\eta^2 + 1)\Delta) \alpha(\eta, x) \quad \left\{ \begin{array}{l} \delta A^\mu = \partial^\mu \alpha \\ \delta h^{\mu\nu} = \partial^{(\mu} \alpha^{\nu)} \\ \dots \end{array} \right.$$

One mode expansion for all helicities:

$$\Psi_{k,h} = e^{-ik \cdot x} (\eta \cdot \epsilon_\pm)^{|h|} \quad \left\{ \begin{array}{l} \phi_k = e^{-ik \cdot x} \\ A_k^\mu = e^{-ik \cdot x} \epsilon_\pm^\mu \\ \dots \end{array} \right.$$

Turning on the Spin Scale

All previous results can be generalized to arbitrary ρ by taking $\Delta = \partial_x \cdot \partial_\eta + \rho$

Still get one mode of each helicity, but now the action, equation of motion, gauge transformations, and plane waves all mix tensor ranks, e.g.

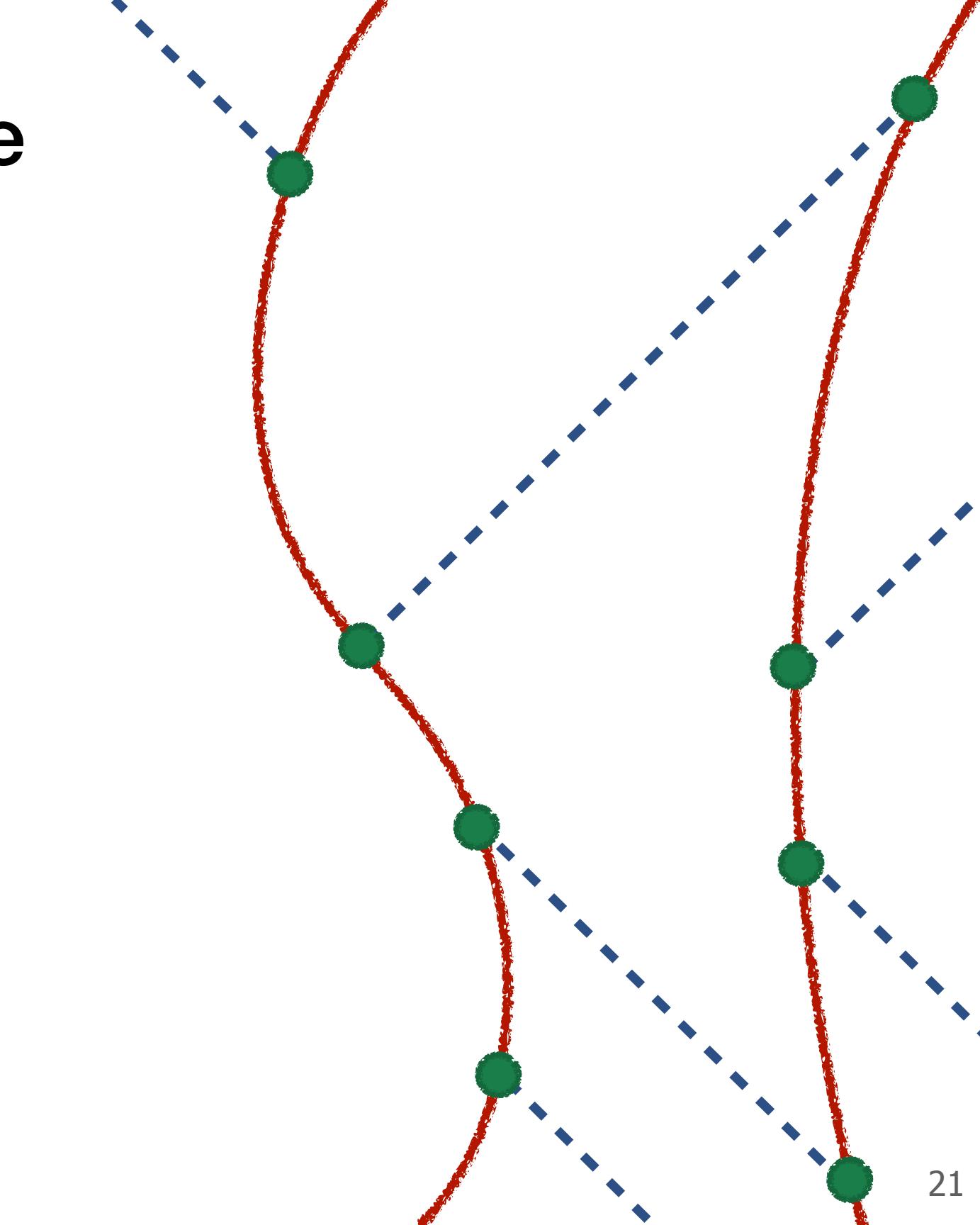
$$\mathcal{L} \supset \rho \left(\frac{1}{\sqrt{2}} \phi \partial_\mu A^\mu + \dots \right) + \rho^2 \left(-\frac{1}{4} \phi h^\mu_{\mu} + \dots \right)$$

$$\Psi_{k,h} = e^{-ik \cdot x} e^{-i\rho \eta \cdot q} (\eta \cdot \epsilon_{\pm})^{|h|} \quad q \cdot k = 1$$

Because of the infinite tower of mixing terms, tensor expansion is complicated and physically opaque, while vector superspace description remains simple

Outline

- Free continuous spin fields
- **Coupling to matter particles**
- Physics with continuous spin



Coupling Currents to Fields

Couple the continuous spin field to a current by

$$\mathcal{L}_{\text{int}} = \int_{\eta} \delta'(\eta^2 + 1) J(\eta, x) \Psi(\eta, x) = \phi J - A_\mu J^\mu + h_{\mu\nu} J^{\mu\nu} + \dots$$

Recover familiar results by tensor decomposition

$$J(\eta, x) = J(x) - \sqrt{2} \eta^\mu J_\mu(x) + (2\eta^\mu \eta^\nu + g^{\mu\nu}) J_{\mu\nu}(x) + \dots$$

Preserving continuous spin gauge symmetry implies relations between $J, J_\mu, J_{\mu\nu}, \dots$

Tensors are **not** conserved! Instead, nonzero divergence related to other tensors

Digression: Connecting to the Hierarchy Problem

A simplified framing: minimally coupled scalars are not naturally light



Minimally coupled massless scalar receives large mass corrections $\delta m^2 \sim \Lambda_{\text{UV}}^2$



Goldstone bosons like axions have mass protected by shift symmetry – but require derivative couplings

Continuous spin fields achieve both at once: a minimal coupling $\mathcal{L} \supset \phi J$, and a gauge symmetry that sets the mass to zero!

Protecting Massless Scalars: Bottom Up

Try imposing a gauge shift symmetry on a minimally coupled massless scalar:

$$\mathcal{L}_0 = \frac{1}{2} (\partial_\mu \phi)^2 + \phi J \quad \delta\phi = \bar{\rho}\epsilon$$

At order $\bar{\rho}$, gauge variation of this term cancelled by adding

$$\mathcal{L}_1 = \frac{1}{4} F_{\mu\nu} F^{\mu\nu} + \bar{\rho} \phi (\partial^\mu A_\mu) - A^\mu J_\mu \quad \delta A_\mu = \partial_\mu \epsilon \quad \partial_\mu J^\mu = \bar{\rho} J \neq 0$$

This isn't gauge invariant at order $\bar{\rho}^2$! But adding $\bar{\rho}^2 A^\mu A_\mu / 2$ just gives vector of mass $\bar{\rho}$.

To preserve gauge invariance while keeping all particles **massless**, must add tensor field $h_{\mu\nu}$, coupled to current $J_{\mu\nu}$, with more mixing terms...

Performing this to all orders gives CSP theory with $\rho = \sqrt{2} \bar{\rho}$

A leading conserved current comes with an infinite tower of nonconserved currents!

Protecting Massless Scalars: Top Down

A deeper perspective: the full action, with coupling to $J(\eta, x)$, is invariant under the bosonic superspace translation $\delta x^\mu = \omega^{\mu\nu}\eta_\nu$

Corresponds to tensorial conserved charge $i\eta^{[\mu}\partial_x^{\nu]}$ which mixes modes separated by **integer** helicity – a new exception to Coleman-Mandula

Transfers the protection of massless vectors, tensors, etc. to massless scalars

Of course, much more work needed to see if something like this can protect the mass of the Higgs at the quantum level

Currents From Matter Particles

In familiar theories, the current from a matter particle is local to its worldline $z^\mu(\tau)$

For spinless particles, the minimal couplings are:

$$\left. \begin{aligned} J(x) &= g \int d\tau \delta^4(x - z(\tau)) \\ J^\mu(x) &= e \int d\tau \delta^4(x - z(\tau)) \frac{dz^\mu}{d\tau} \\ T^{\mu\nu}(x) &= m \int d\tau \delta^4(x - z(\tau)) \frac{dz^\mu}{d\tau} \frac{dz^\nu}{d\tau} \end{aligned} \right\} \text{should be } \rho \rightarrow 0 \text{ limit of } \left\{ \begin{array}{l} \text{scalar-like current} \\ \text{vector-like current} \\ \text{tensor-like current} \end{array} \right.$$

Must be incorporated into full current $J(\eta, x)$ satisfying $\delta(\eta^2 + 1)(\partial_x \cdot \partial_\eta + \rho) J(\eta, x) = 0$

Locality and Causality

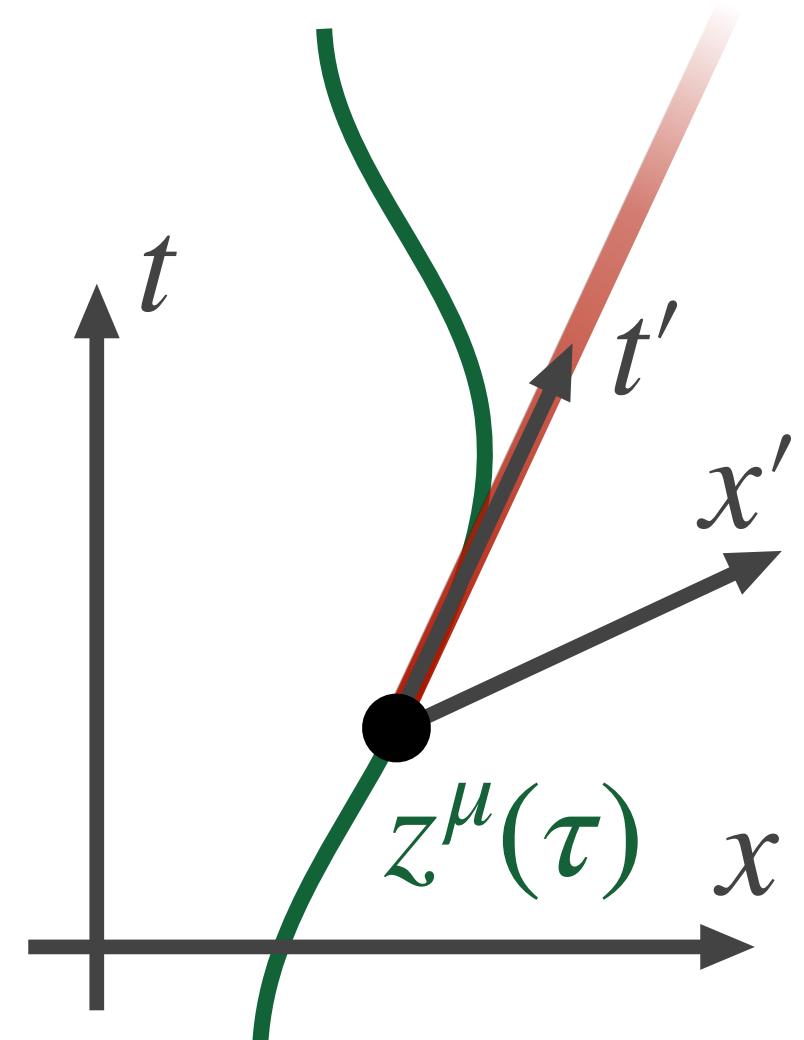
In Fourier space, current and gauge invariance condition are

$$J(\eta, k) = \int d\tau e^{ik \cdot z(\tau)} f(\dot{z}, k, \eta) \quad (-ik \cdot \partial_\eta + \rho)f \approx 0$$

Our currents are generically **not** localized to the worldline!

For example, $f = e^{-i\rho\eta \cdot \dot{z}/k \cdot \dot{z}}$ produces a scalar-like current with “wake” confined in future (or past) light cone

This can yield causal particle dynamics; could emerge from integrating out fields in a manifestly local description



A Universality Result

Key technical result: all currents can be decomposed as

$$f = e^{-i\rho\eta \cdot \dot{z}/k \cdot \dot{z}} \hat{g}(k \cdot \dot{z}) + \mathcal{D}X$$

First term contains the key physics of nonzero spin scale ρ

“Shape” terms are proportional to equation of motion operator \mathcal{D}

Many physical observables are **universal**: determined by only ρ and \hat{g} , where

$$\hat{g} = \begin{cases} g & \text{scalar-like current} \\ e k \cdot \dot{z} & \text{vector-like current} \\ m(k \cdot \dot{z})^2 + \dots & \text{tensor-like current} \end{cases}$$

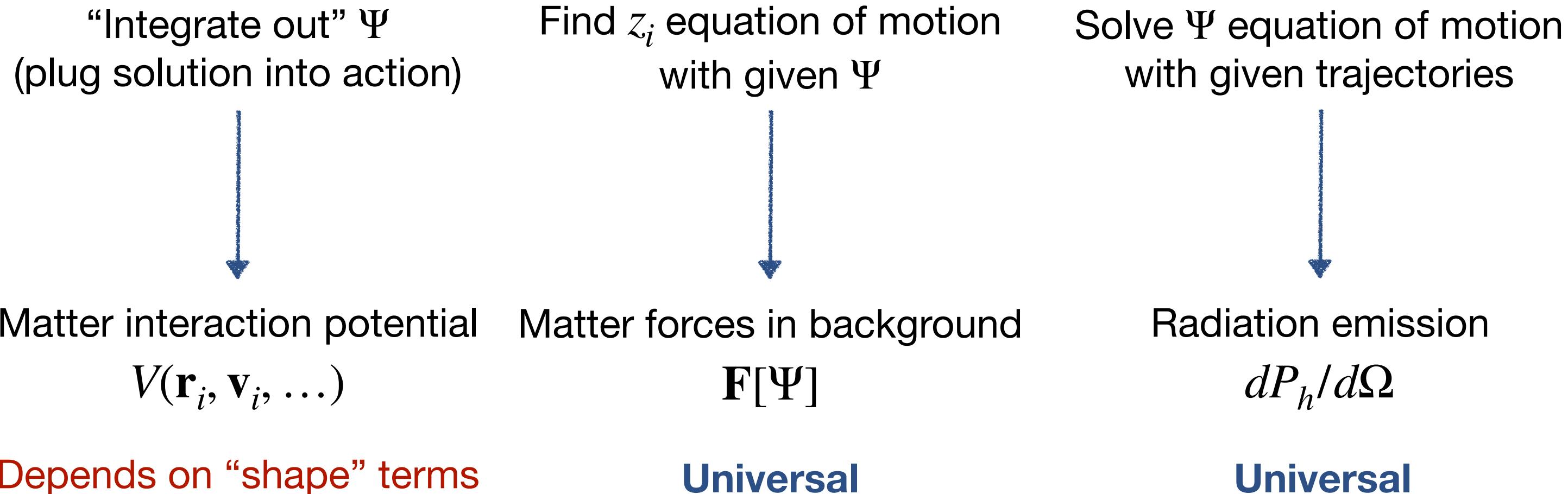
Like familiar contact terms, these couplings can be completely removed by field redefinition

All valid currents found in earlier works were pure shape terms, with $\hat{g} = 0$

[2505.14770](#): similar results for spin 1/2 matter particles (via worldline SUSY)

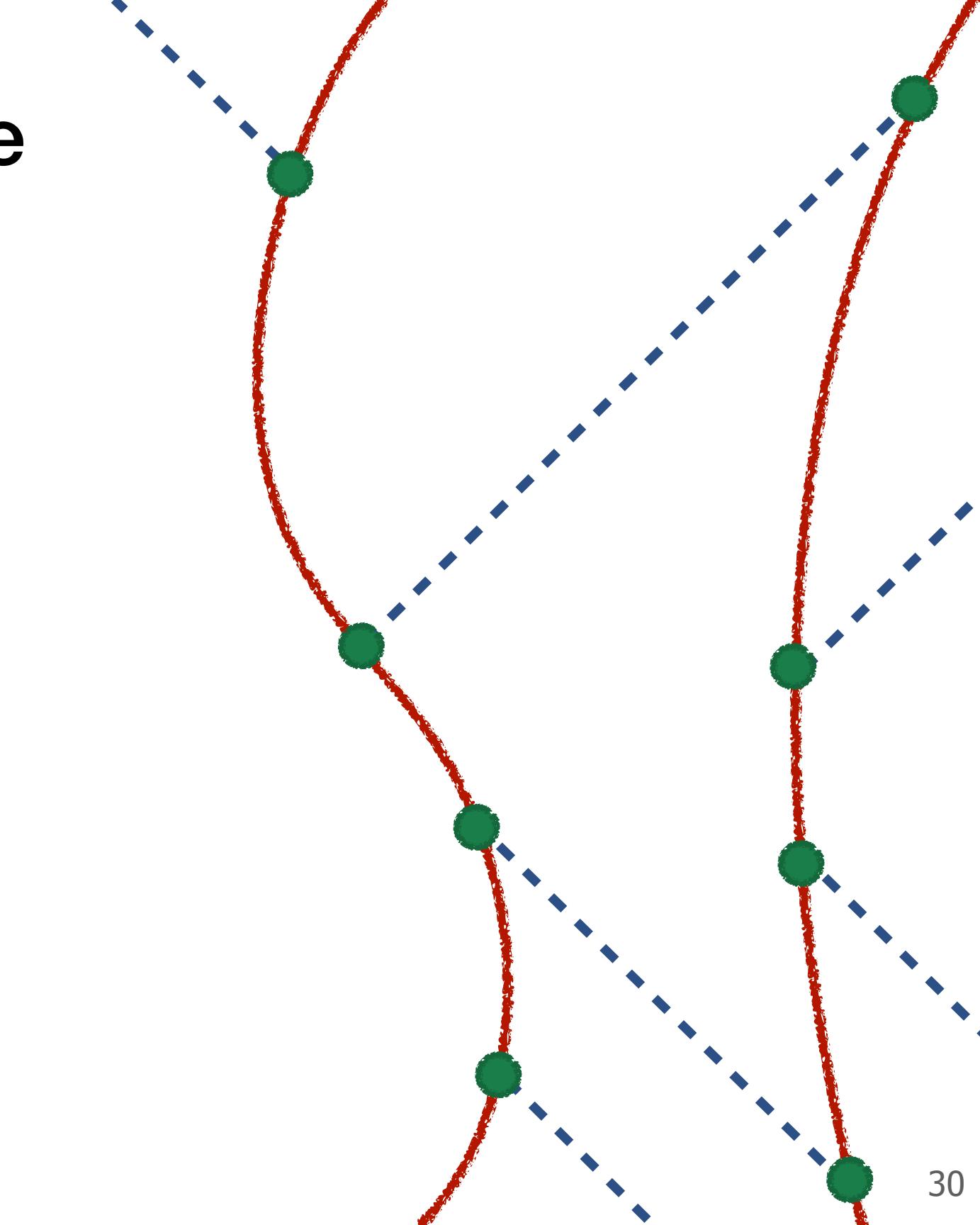
Extracting the Physics

From the action $S[\Psi, z_i^\mu(\tau)]$ we can compute any desired classical observable:



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- Free continuous spin fields
- Coupling to matter particles
- **Physics with continuous spin**



Forces in Background Fields

Force on particle with vector-like current in background of frequency ω , helicity h :

$$\frac{\mathbf{F}_{h=0}}{q} = \frac{\rho}{\omega} \frac{\dot{\phi} \mathbf{v}_\perp}{2} + \dots$$

$$\frac{\mathbf{F}_{h=\pm 1}}{q} = \mathbf{E} + \mathbf{v} \times \mathbf{B} - \left(\frac{\rho}{\omega} \right)^2 \left(\frac{\mathbf{v}_\perp (\mathbf{v}_\perp \cdot \mathbf{E})}{4} + \frac{\nu_\perp^2 \mathbf{E}}{8} \right) + \dots$$

$$\frac{\mathbf{F}_{h=\pm 2}}{q} = \frac{\rho}{\omega} \frac{\dot{h}_+ (\nu_x \hat{\mathbf{x}} - \nu_y \hat{\mathbf{y}})}{4} + \dots$$

Corrections controlled by $\rho v/\omega$, and as $\rho \rightarrow 0$ other helicities decouple

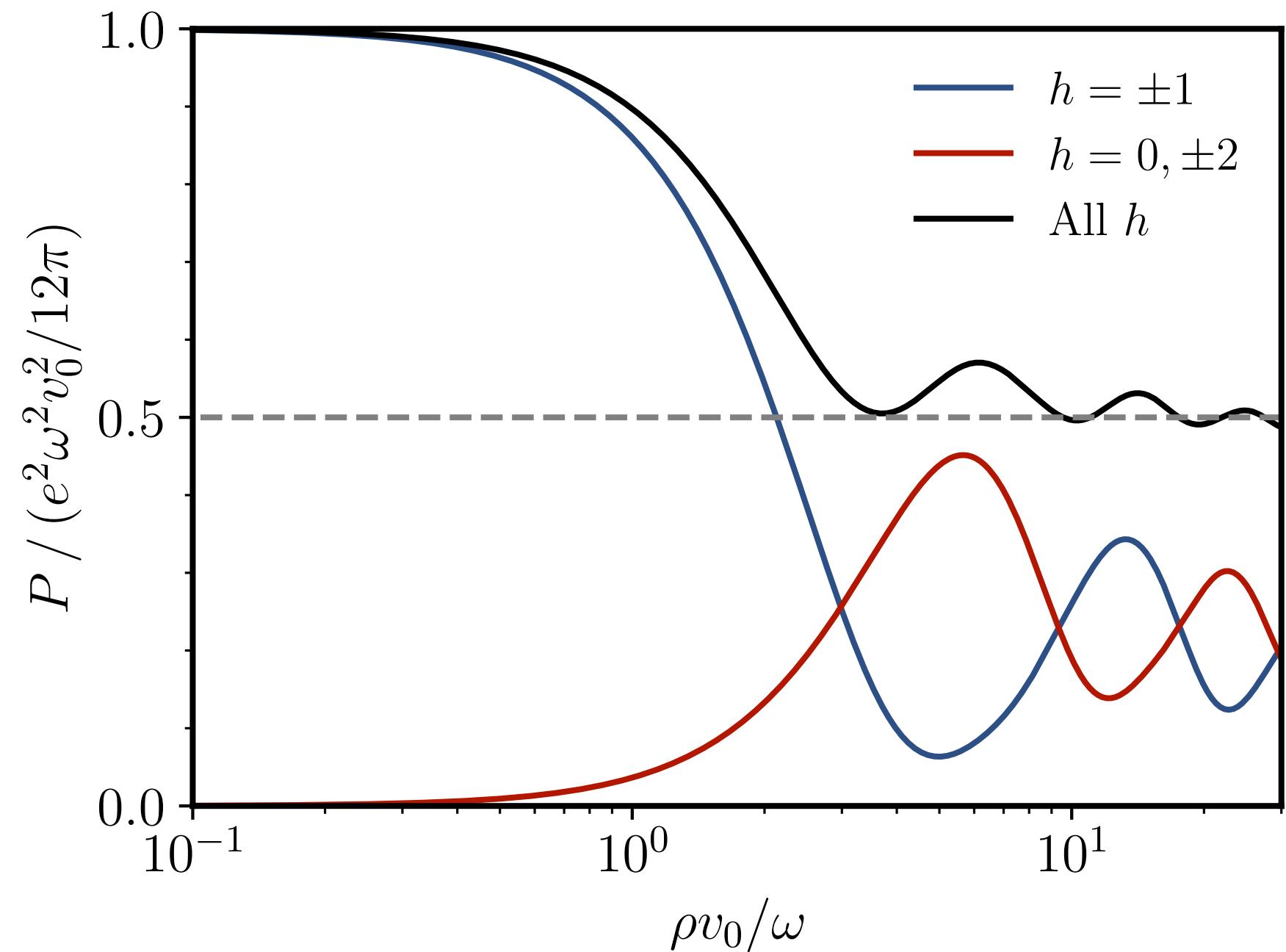
Full expressions have Bessel functions, convergent at large arguments

Radiation From Oscillating Particle

Consider motion with amplitude $\ell = v_0/\omega$, and vector-like current

Radiation emitted in all helicities, and at large $\rho\ell$ many helicities contribute, but total power radiated is finite!

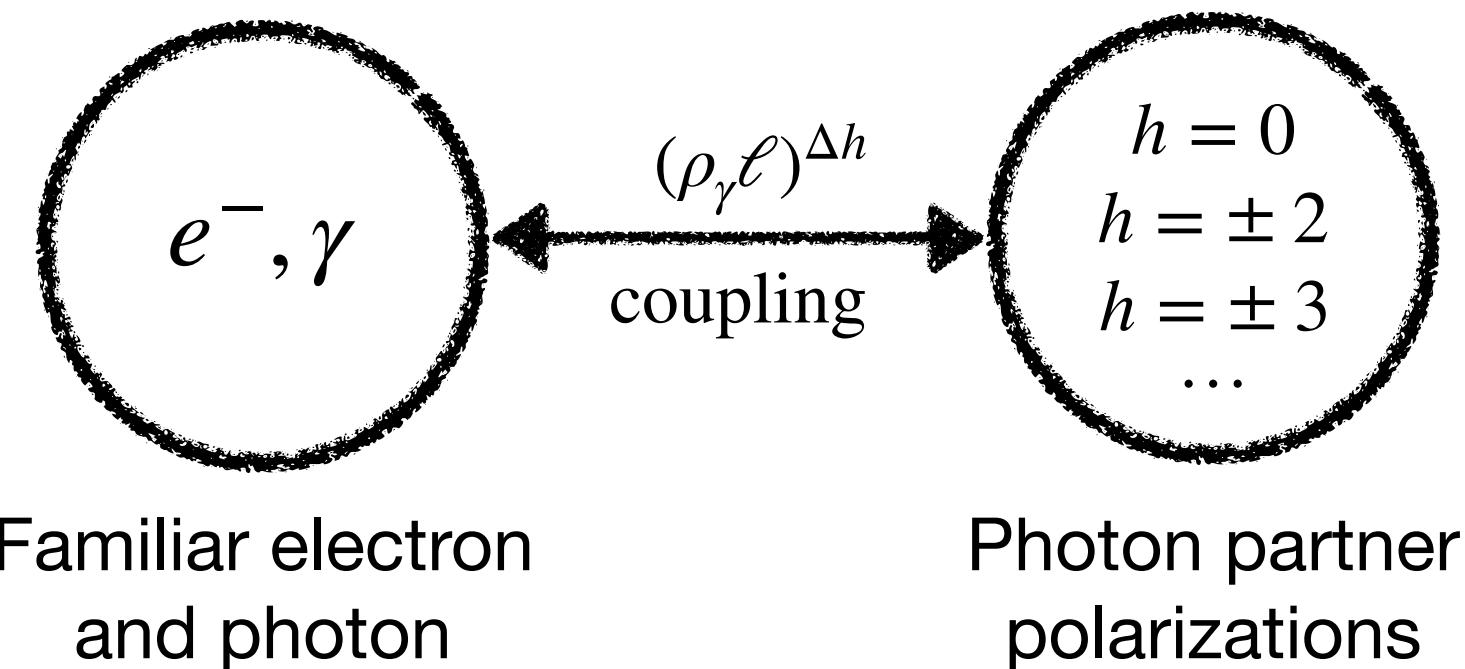
Variant of this calculation recovers previously known soft emission amplitudes



Probing The Spin Scale of the Photon

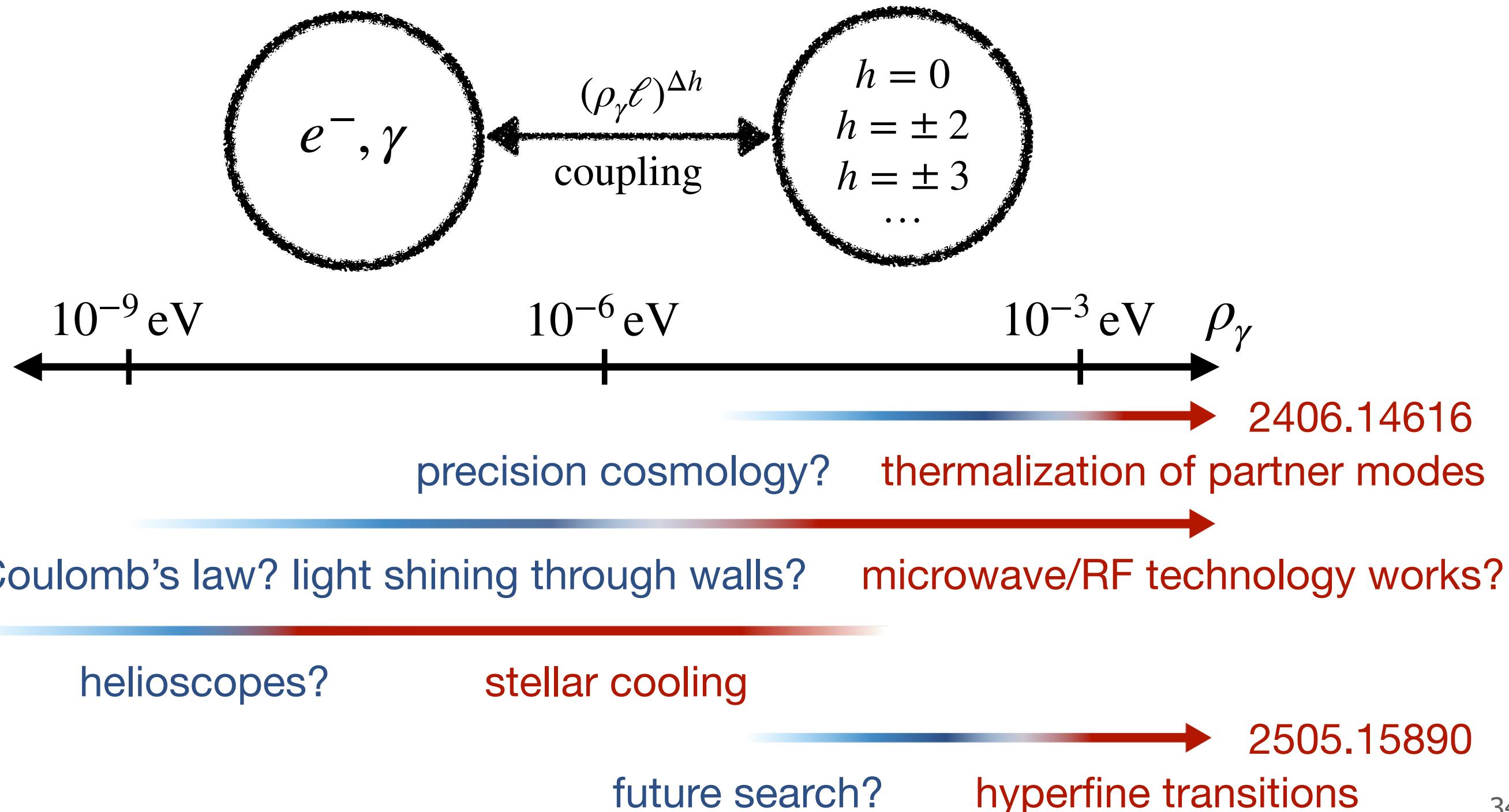
For vector-like currents, $h = \pm 1$ could be observed photon

Other helicities are weakly coupled “dark radiation”



Sensitivity of various probes can be readily calculated

Probing The Spin Scale of the Photon



Continuous Spin and Gravity?

We need to distinguish two distinct possibilities



The graviton is the $|h| = 2$ part of a continuous spin particle, which implies infrared modifications of GR

“continuous spin gravity”

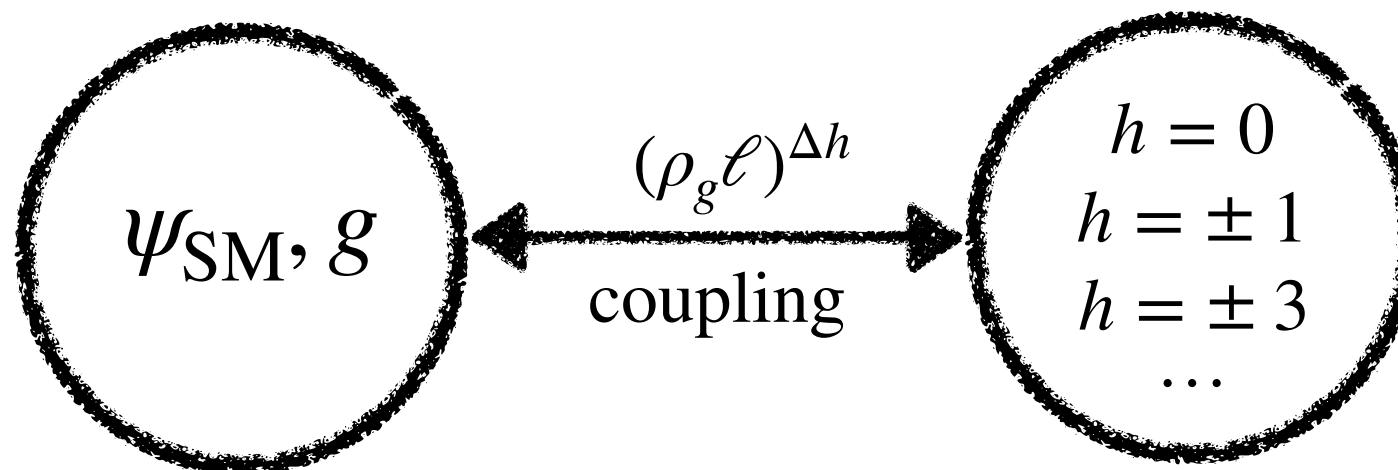


The photon is the $|h| = 1$ part of a continuous spin particle, which is coupled to standard GR

“continuous spin in curved spacetime”

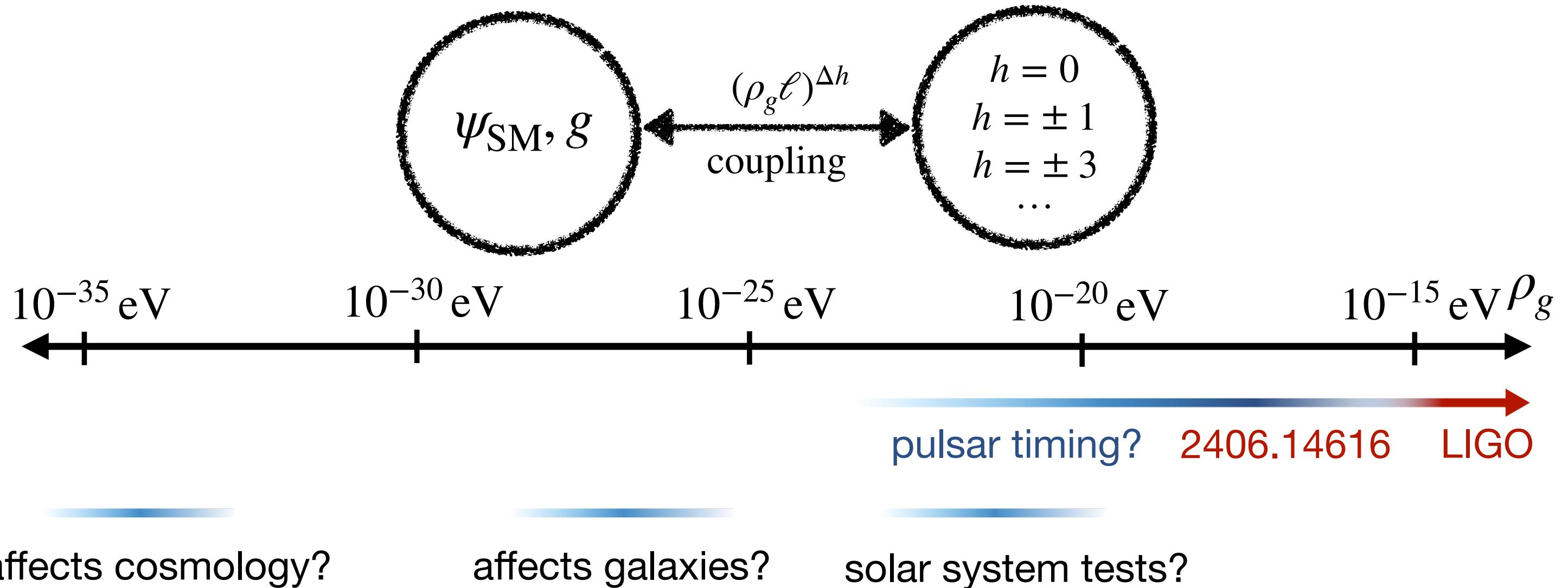
Probing The Spin Scale of the Graviton

A tensor-like current yields linearized gravity with ρ -dependent corrections



Linearized theory enough for many observables, though strong field effects require understanding self-interactions of continuous spin fields, and nonlinear generalization of their gauge symmetry

Probing The Spin Scale of the Graviton



Pushed towards galactic and cosmology scales, where gravitational force may change

Continuous Spin Fields in Curved Spacetime

To couple Ψ to gravity, start with its conserved stress-energy tensor:

$$T^{\mu\nu} = -g^{\mu\nu}\mathcal{L} + \int_{\eta} \delta'(\eta^2 + 1) \partial^{\mu}\Psi \partial^{\nu}\Psi - \frac{1}{2} \partial_{\eta}^{\mu} (\delta(\eta^2 + 1) \Delta\Psi) \partial^{\nu}\Psi$$

By itself, this breaks Ψ 's gauge symmetry – need to find consistent completion

Aren't gravitational observables like Hawking radiation infinite?



No, because of falling greybody factors for higher h modes

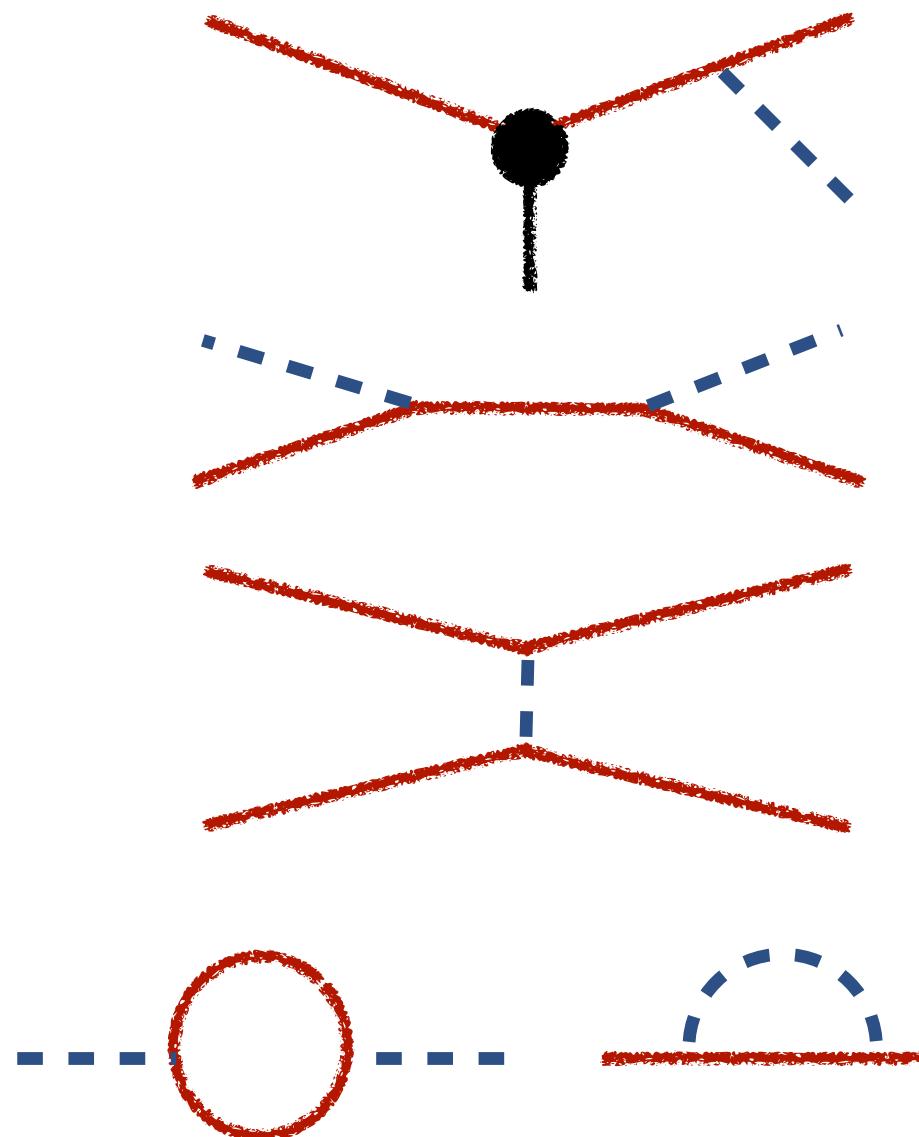


No, because CSPs don't have to obey the equivalence principle

For photon-like CSP, only $|h| = 1$ should couple to gravity as $\rho \rightarrow 0$

Scattering Amplitudes

Scattering amplitudes computable with path integral or on-shell methods



CSP emission straightforward, recovers soft factors

CSP-matter scattering only involves external CSPs, so is universal

CSP exchange not universal, but obeys tree-level unitarity

Unitarity at loop level unknown, may place constraints on current (key next step)

Amplitudes in the Worldline Formalism

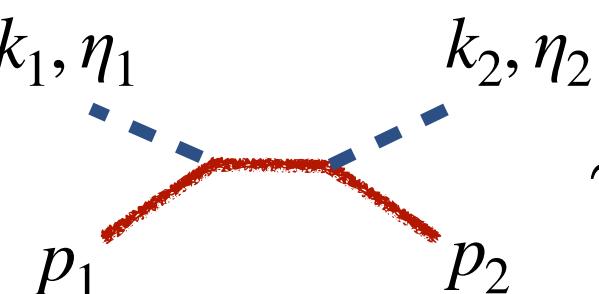
$$\mathcal{M} \sim \int \mathcal{D}[z(\tau)] \left(\prod_i \int dt_i V(k_i, t_i) \right) \exp \left(i \int d\tau \dot{z}^2 / 4 \right)$$

scalar massless matter particle

$$V(\eta, k, t) \sim q e^{ik \cdot z(t)} \frac{e^{-i\rho \eta \cdot \dot{z}/k \cdot \dot{z}}}{-i\rho/k \cdot \dot{z}}$$

vertex operator of vector-like CSP

2308.16218: defining $P_i = p_1 + p_2 + xk_i$, Compton scattering amplitude is



$$\sim \int_{-1}^1 dx \left(\eta_1 - \frac{\eta_1 \cdot P_1}{k_1 \cdot P_1} k_1 \right) \cdot \left(\eta_2 - \frac{\eta_2 \cdot P_2}{k_2 \cdot P_2} k_2 \right) \exp \left(i\rho \left(\frac{\eta_1 \cdot P_1}{k_1 \cdot P_1} - \frac{\eta_2 \cdot P_2}{k_2 \cdot P_2} \right) \right)$$

Reduces to scalar QED result as $\rho \rightarrow 0$, contains benign essential singularities for $\rho \neq 0$

General rule: ρ must be in numerator, so momenta must be in denominator

Nonrelativistic Atomic Transition Amplitudes

$$\mathcal{M} \sim \int \mathcal{D}[z(\tau)] \left(\prod_i \int dt_i V(k_i, t_i) \right) \exp \left(i \int d\tau \dot{z}^2 / 4 \right)$$

scalar massless matter particle

$$V(\eta, k, t) \sim q e^{ik \cdot z(t)} \frac{e^{-i\rho\eta \cdot \dot{z}/k \cdot \dot{z}}}{-i\rho/k \cdot \dot{z}}$$

vertex operator of vector-like CSP

2505.01500: for electronic states $|i\rangle, |f\rangle$, amplitude to emit CSP with (h, \mathbf{k}, ω) is

$$\mathcal{M}_h = \langle f | \mathcal{O}_h | i \rangle \quad \mathcal{O}_h \sim q \int_0^{2\pi} d\theta e^{ih\theta} \frac{\omega}{\rho} \exp \left(\frac{i\rho}{\omega m} \hat{\mathbf{p}} \cdot \mathbf{e}_\theta \right) \quad \mathbf{e}_\theta \perp \mathbf{k}$$

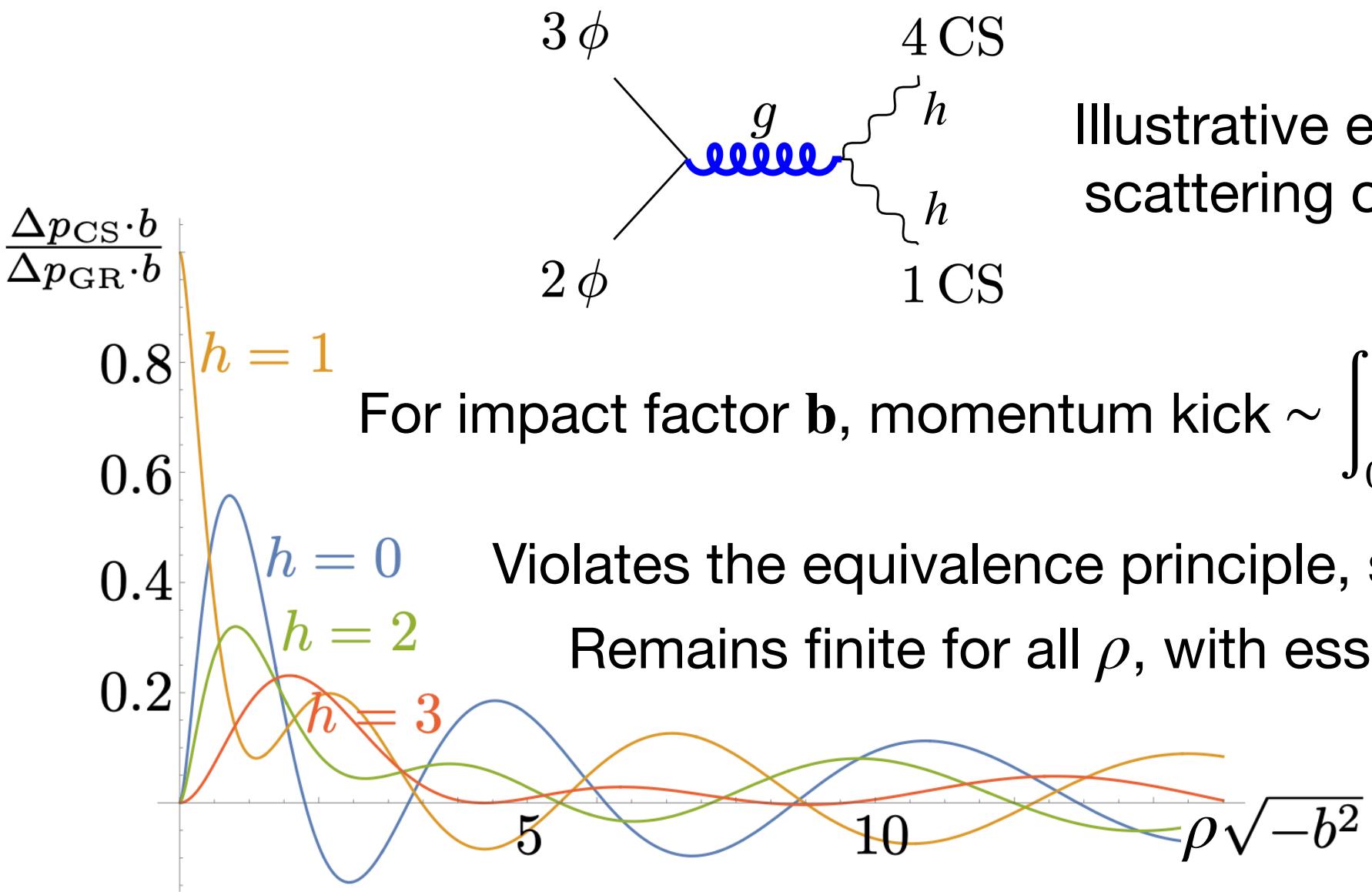
As $\rho \rightarrow 0$, recover $\mathcal{O}_{\pm 1} \rightarrow (q/m) \hat{\mathbf{p}} \cdot \mathbf{A}_\pm$, while other $\mathcal{O}_h \rightarrow 0$

Essential singularity at $\rho/\omega \rightarrow \infty$, but still well-behaved

Amplitudes From the On-Shell Approach

2406.17017: studied on-shell scattering amplitudes, bootstrapped four-point amplitudes

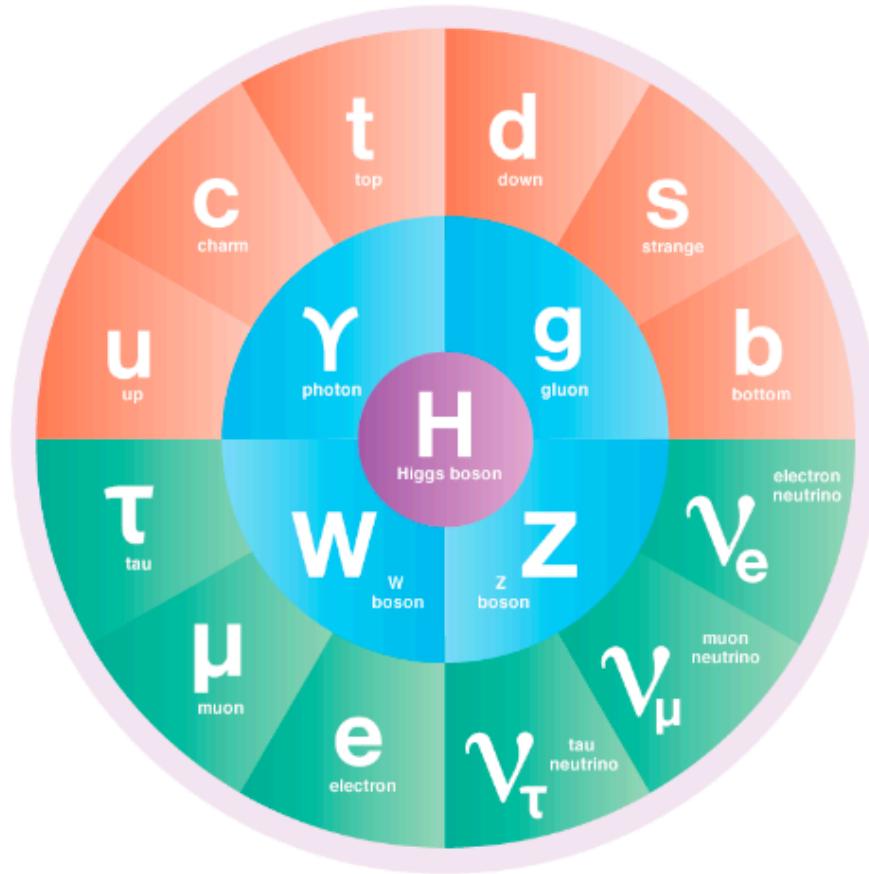
Bellazzini, de Angelis, Romano, JHEP (2025)



Illustrative example: CSP photon scattering off scalar via graviton

$$\int_0^\infty dq (J_{h-1}(\rho/q)^2 + J_{h+1}(\rho/q)^2) J_1(4|\mathbf{b}|q)$$

A Continuous Spin Standard Model?



Would ultimately want to embed a continuous spin photon within the electroweak sector

Need to give continuous
spin fields mass

Need nonabelian continuous
spin gauge symmetry

Using massive CSPs could help regulate infrared behavior

But naive mass term $m^2\Psi^2/2$ doesn't work: results in ghosts

Open question: find appropriate mass term from dimensional reduction

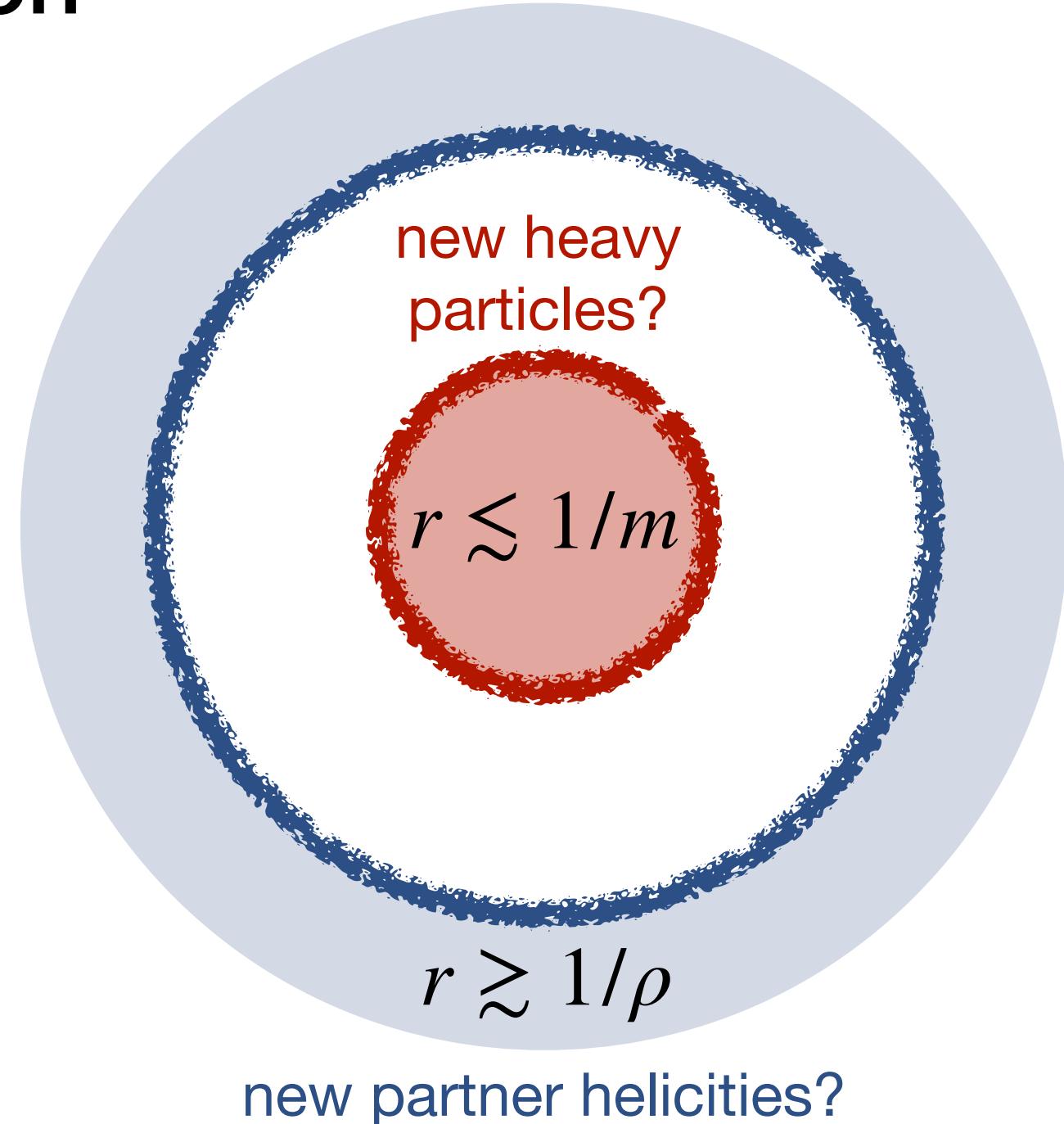
Conclusion

Lorentz symmetry implies massless particles have a spin scale ρ — **is it zero or not?**

For nonzero ρ , there are calculable, universal predictions which can be immediately tested!

Grand theory question: are there fully consistent analogues of the full Standard Model and/or general relativity at nonzero ρ ?

If so, they are effective theories at both long and short distances — which can shed light on a variety of fundamental problems



Extra Slides

CSP Lagrangian in Component Form

In component form, the Lagrangian is physically opaque:

$$\begin{aligned}\mathcal{L} = \mathcal{L}_0 + \frac{\rho}{\sqrt{2}} & \left(\phi (\partial^\mu A_\mu) + A^\mu (\partial_\mu h' - \partial^\nu h_{\mu\nu}) + \dots \right) \\ & + \frac{\rho^2}{4} \left(\phi^2 - \frac{1}{2} A_\mu A^\mu - \phi h' + \frac{1}{6} (h')^2 - \frac{1}{3} h_{\mu\nu} h^{\mu\nu} + \dots \right)\end{aligned}$$

Infinite towers of mixing and apparent mass terms!

Mixing can't be eliminated, and prevents a simple approximate description in terms of a few tensor components

CSP corrections enter as an infinite tower of **relevant** interactions, which conspire to give good behavior in the infrared

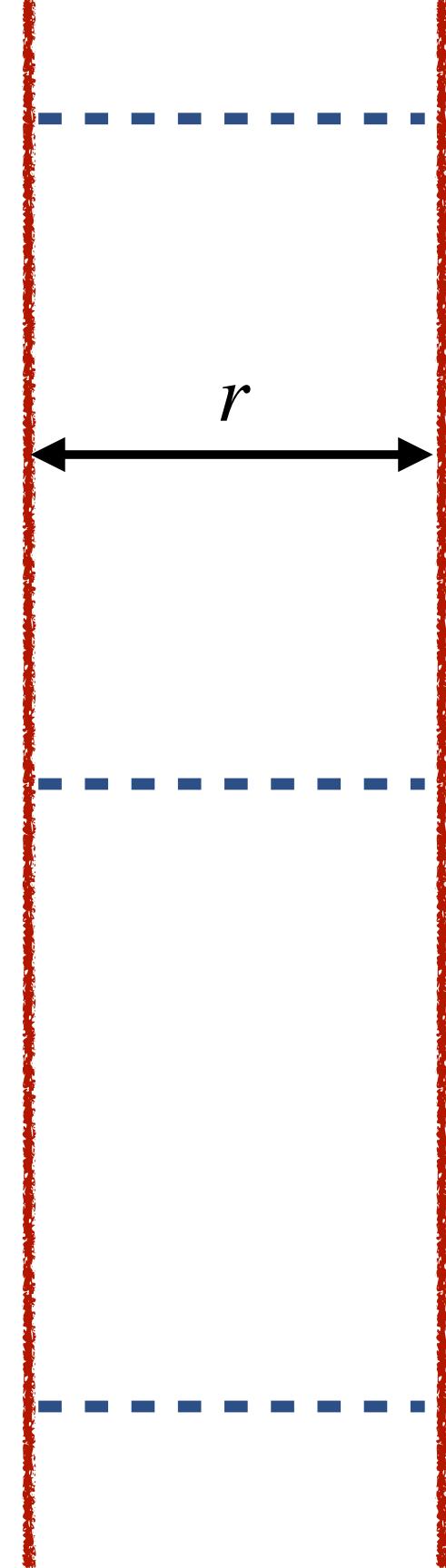
Static Potentials

Static potentials can exhibit deviations at long distances:

$$V(r) = \frac{g^2}{4\pi r} \left(1 - c_1 \rho r + c_2 (\rho r)^2 + \dots \right)$$

Coefficients depend on current: vanish for simplest currents, but for general currents can cause force to flip sign at large distances

Similar results for vector-like currents; can also find velocity-dependent potentials (e.g. corrections to magnetic interaction)



Radiation From Kicked Particle

For any scalar-like current, radiation amplitude from a kicked particle is

$$a_{h,k} \propto g \left(\frac{\tilde{J}_h(\rho |\epsilon_- \cdot p/k \cdot p|)}{k \cdot p} - \frac{\tilde{J}_h(\rho |\epsilon_- \cdot p'/k \cdot p'|)}{k \cdot p'} \right)$$

which exactly matches soft emission amplitudes fixed by general arguments

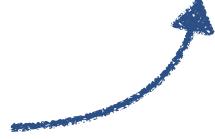
Same agreement for vector-like currents; in both cases other helicities decouple as $\rho \rightarrow 0$

CSP Mass Terms

Using the naive mass term gives a ghost at rank 2, even for $\rho = 0$

$$\mathcal{L}_m = -\frac{1}{2} \int_{\eta} \delta'(\eta^2 + 1) m^2 \Psi^2 = -\frac{1}{2} m^2 \phi^2 + \frac{1}{2} m^2 A_\mu A^\mu - \frac{1}{2} m^2 \left(h_{\mu\nu} h^{\mu\nu} - \frac{1}{2} h^2 \right)$$

allows ghost mode associated with traceful $h_{\mu\nu}$



Hard to guess a better term; instead proceed systematically by reduction from 5D

$$\mathcal{L}_5 = \frac{1}{2} \int_{\bar{\eta}} \delta'(\bar{\eta}^2 + 1) (\partial_{\bar{x}} \bar{\Psi})^2 + \frac{1}{2} \delta(\bar{\eta}^2 + 1) (\bar{\Delta} \bar{\Psi})^2 \quad \bar{\eta} = (\eta^\mu, \eta^5) \quad \bar{x} = (x^\mu, x^5)$$

Guaranteed to avoid ghosts; expect one mass m particle of every integer spin

But resulting 4D action is complicated; needs clever choice of 5D gauge