

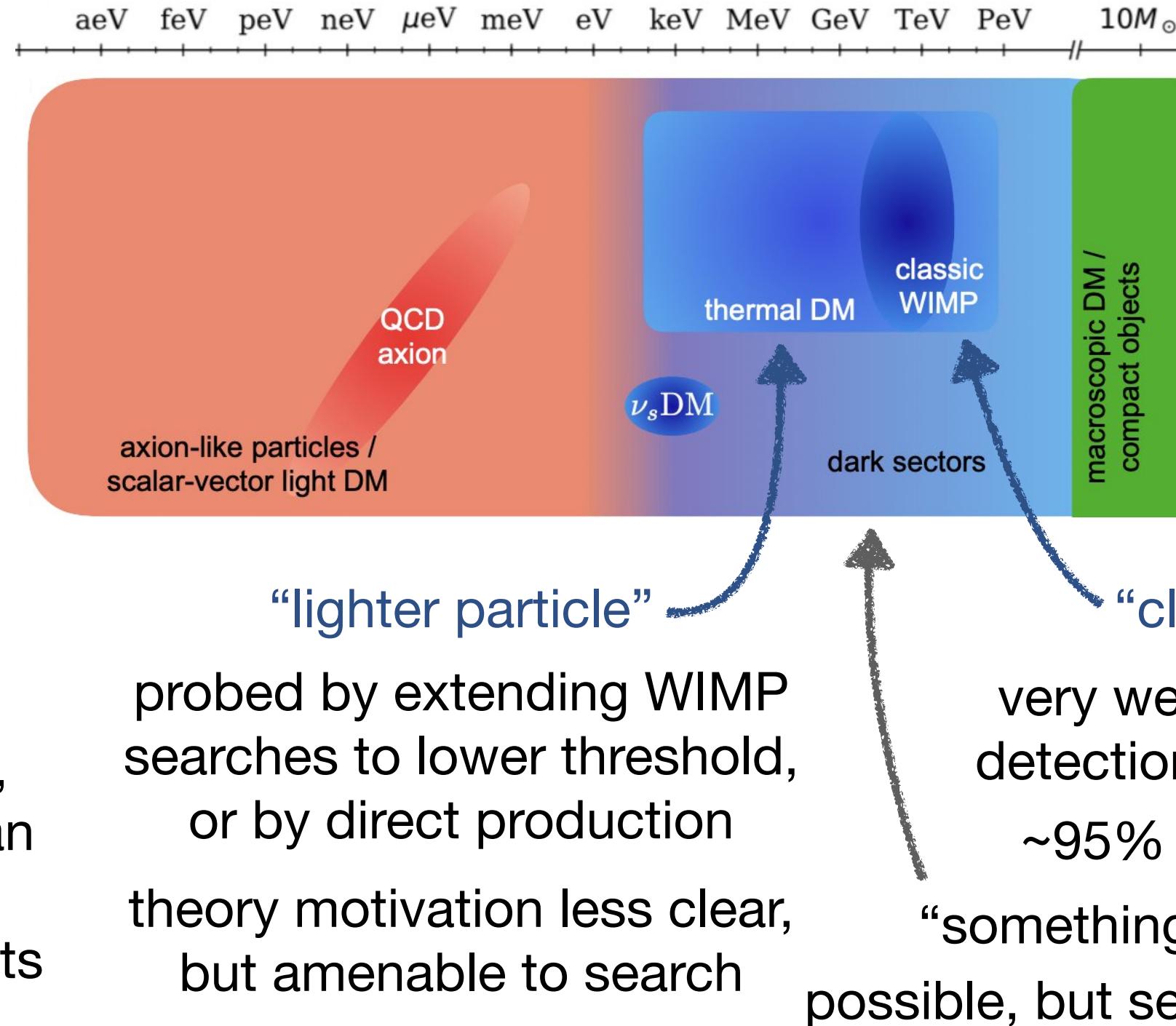
How (Not) to Probe The Axion-Electron Coupling

Kevin Zhou



Peking University Seminar — July 17, 2025

Dark Matter Candidates



macroscopic object

well-tested by astrophysical observation

ultralight field

acts like oscillating classical field

$$\frac{f}{\text{GHz}} \sim \frac{m_{\text{DM}}}{\mu\text{eV}}$$

field's weak forces, torques, currents can be probed by new precision experiments

"lighter particle"

probed by extending WIMP searches to lower threshold, or by direct production

theory motivation less clear, but amenable to search

"classic WIMP"

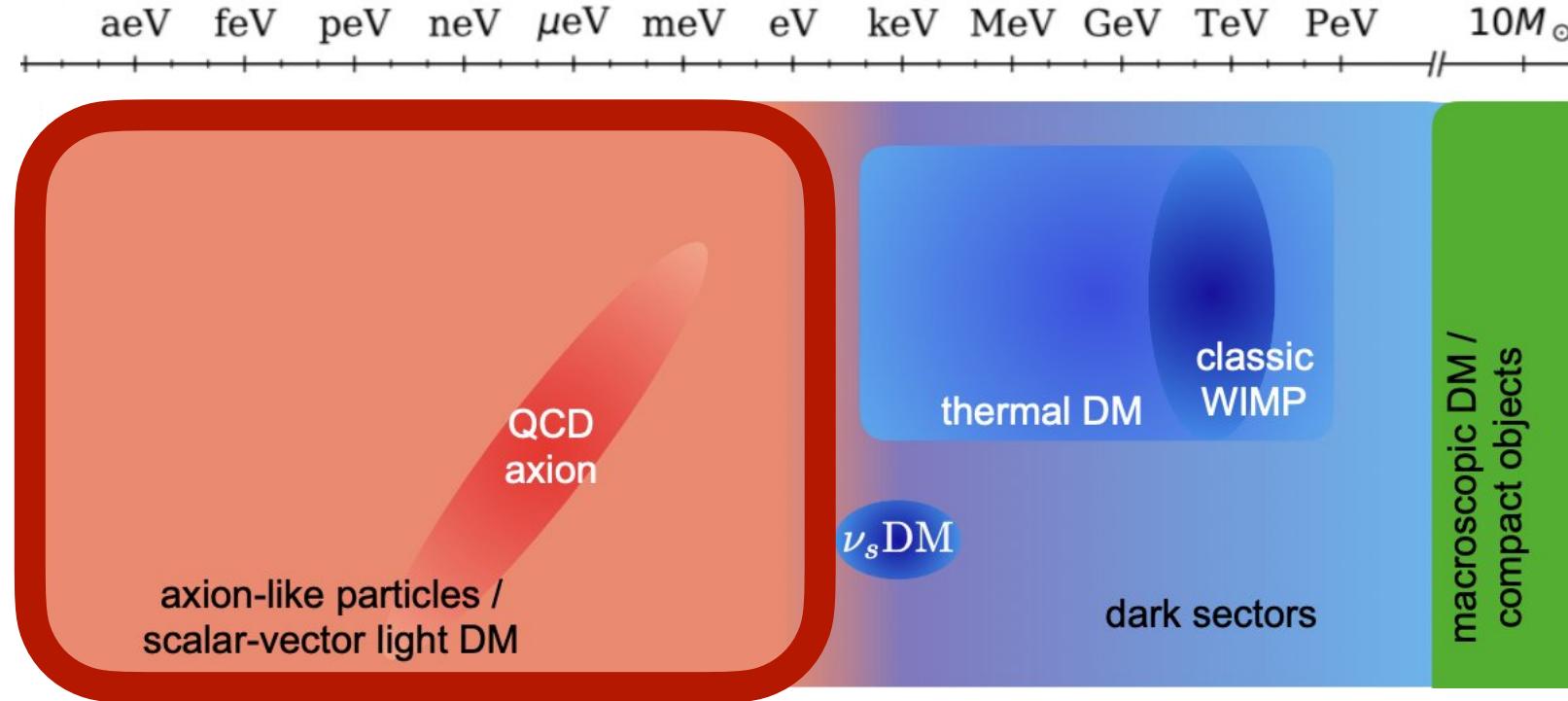
very well-tested by direct detection and astrophysics

~95% of funding, effort

"something more complex"

possible, but search strategy unclear

Why Search for Ultralight Dark Matter?



- Simply produced: gives right amount of dark matter with minimal cosmology
- Generic: required ultralight fields automatically appear in many models
- Minimal: requires introduction of only a single new field at low energies
- Low-hanging fruit: new experiments are needed, inexpensive, and very effective
- Bounded: only a few interactions are natural and leading in effective field theory

Ultralight Dark Matter Candidates

In field theory, only a few candidates are possible!

pseudoscalar a

naturally light with
leading coupling

arises in high
energy theories

solves tuning
problems

simply produced

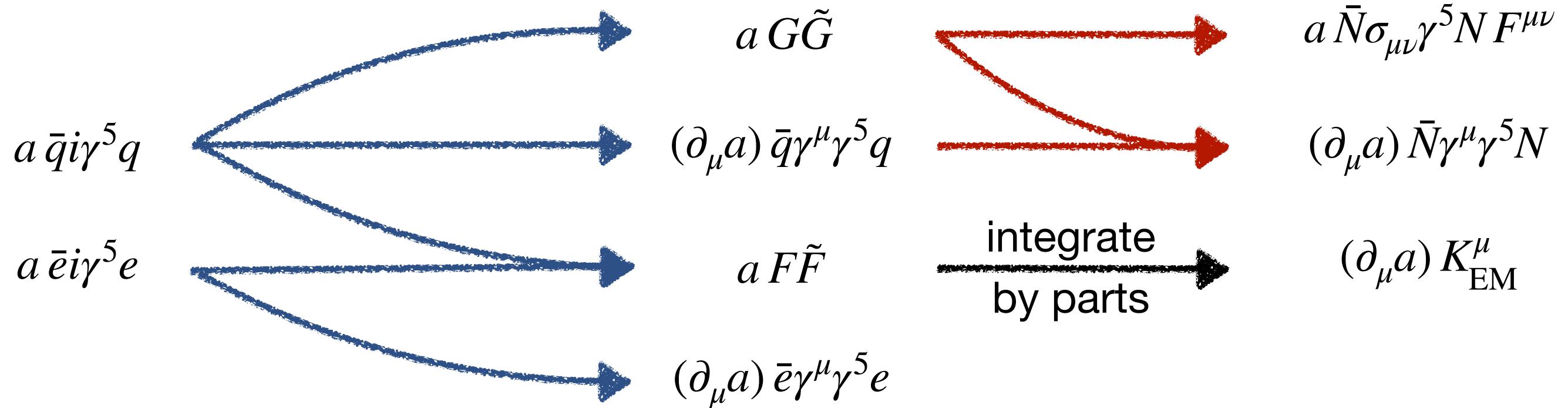
scalar ϕ

vector A'_μ

tensor $h'_{\mu\nu}$



Couplings of a Field Theory Axion

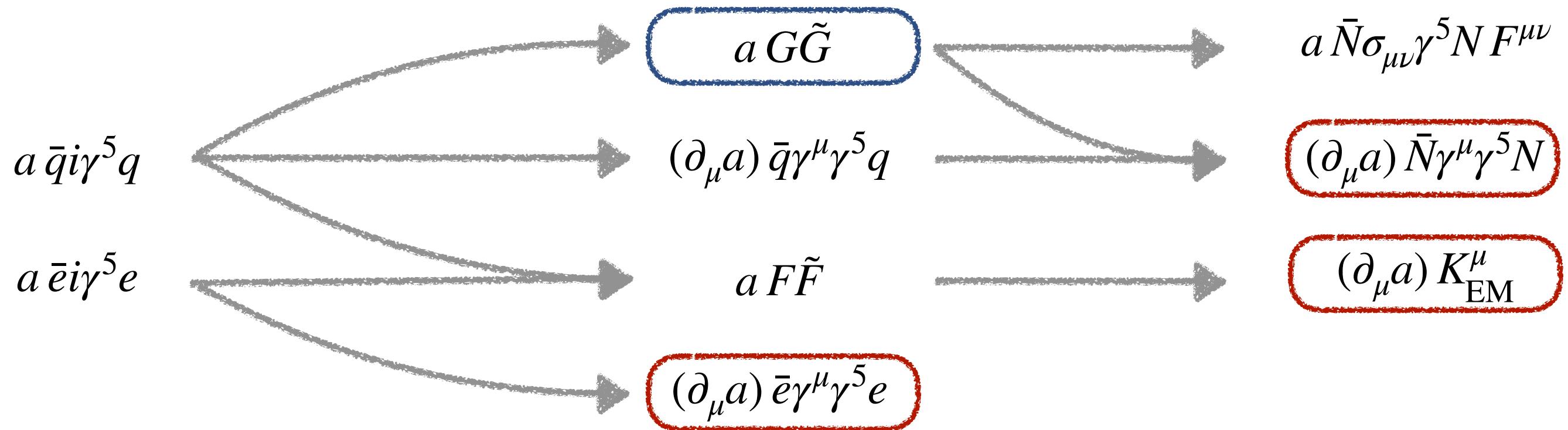


arises from spontaneous breaking of chiral symmetry at high energies

axion is Goldstone boson, so recast most interactions in derivative form by **chiral field redefinitions**, inducing couplings to gauge bosons by anomaly

take **low-energy limit** to find effects on nucleons

Couplings of a Field Theory Axion



Only a few **dimension 5 operators** possible, and generically all exist

These operators depend only on the axion derivative $\partial_\mu a$

(many proposals claim sensitivity even as $\partial_\mu a \rightarrow 0$, but are all incorrect)

However, a **QCD axion** can have signatures proportional to a

$$(\partial_\mu a) K_{\text{EM}}^\mu$$

axion-photon

$$(\partial_\mu a) \bar{N} \gamma^\mu \gamma^5 N$$

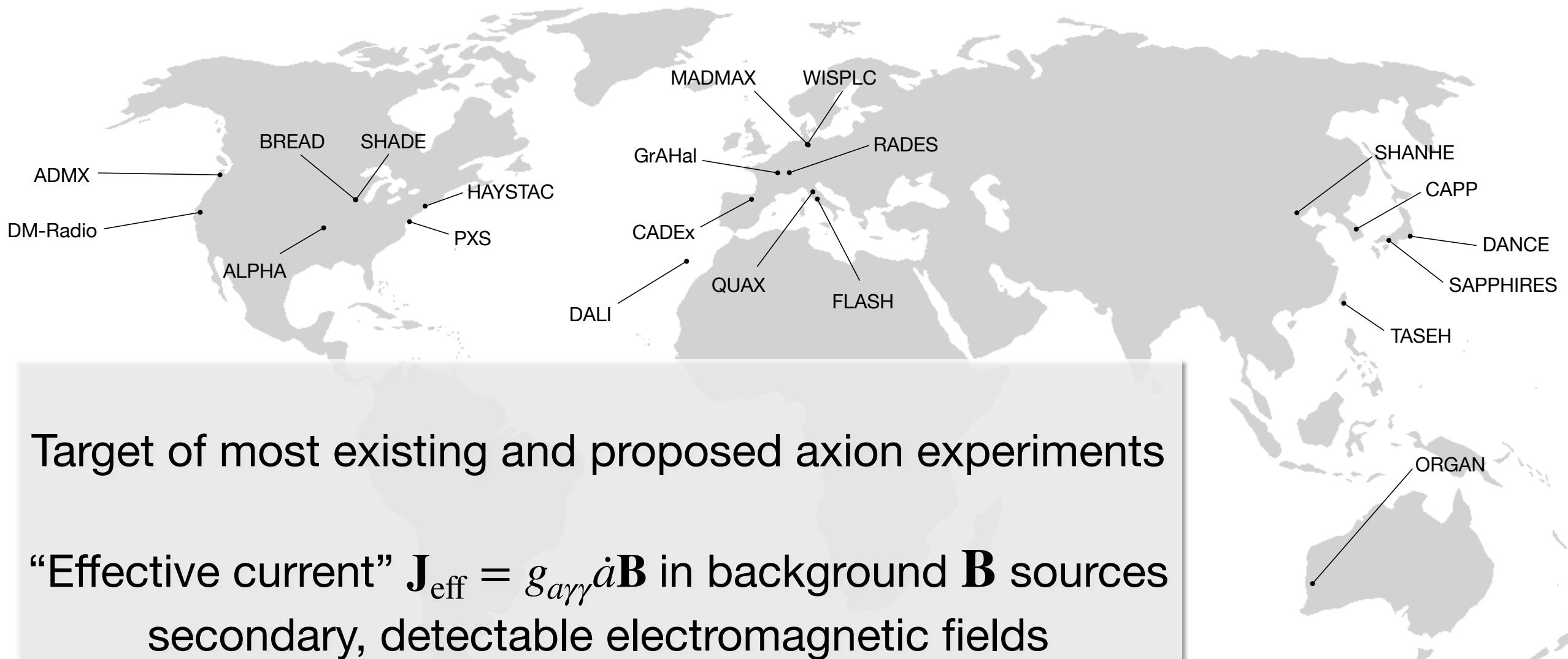
axion-nucleon

$$(\partial_\mu a) \bar{e} \gamma^\mu \gamma^5 e$$

axion-electron

$$a \bar{N} \sigma_{\mu\nu} \gamma^5 N F^{\mu\nu}$$

axion-EDM



$$(\partial_\mu a) K_{\text{EM}}^\mu$$

axion-photon

$$(\partial_\mu a) \bar{N} \gamma^\mu \gamma^5 N$$

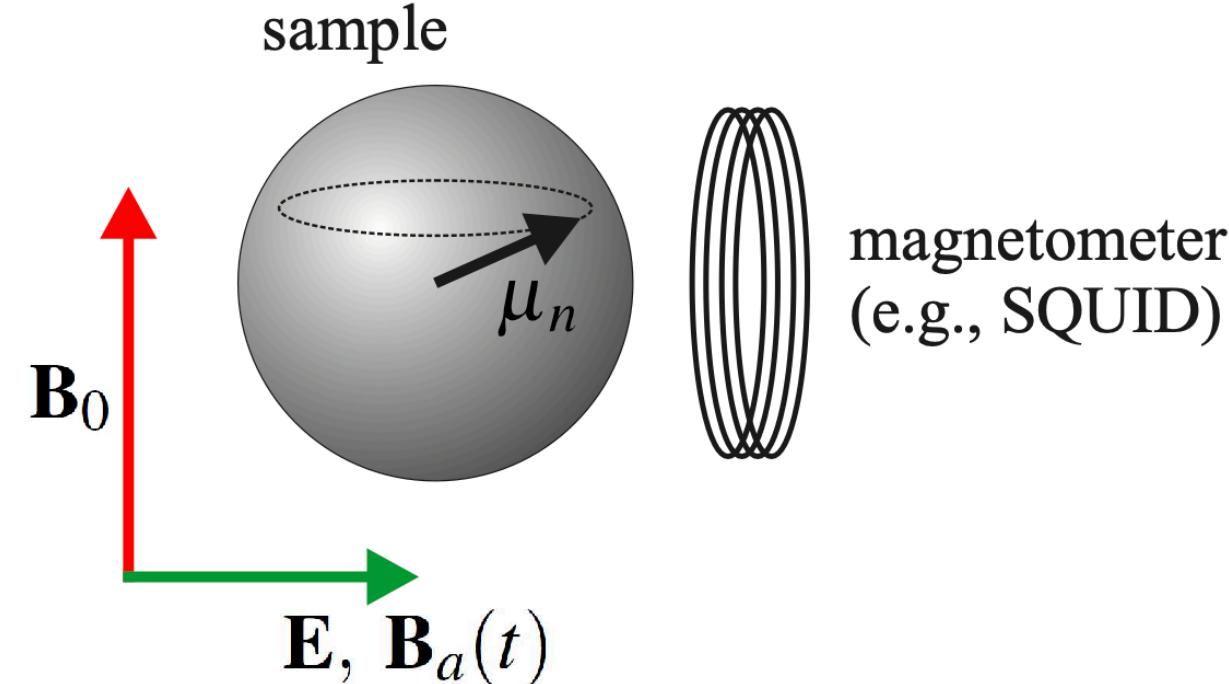
axion-nucleon

$$(\partial_\mu a) \bar{e} \gamma^\mu \gamma^5 e$$

axion-electron

$$a \bar{N} \sigma_{\mu\nu} \gamma^5 N F^{\mu\nu}$$

axion-EDM



Exerts nuclear spin torque $\tau = \hat{s} \times \mathbf{B}$ through effective magnetic field $\mathbf{B}_{\text{eff}} = g_{aN} \nabla a$

Field is very weak; need to amplify signal with nuclear magnetic resonance

Detection remains very challenging, due to weakness of nuclear spin polarization, smallness of nuclear magnetic moment

$$(\partial_\mu a) K_{\text{EM}}^\mu$$

axion-photon

$$(\partial_\mu a) \bar{N} \gamma^\mu \gamma^5 N$$

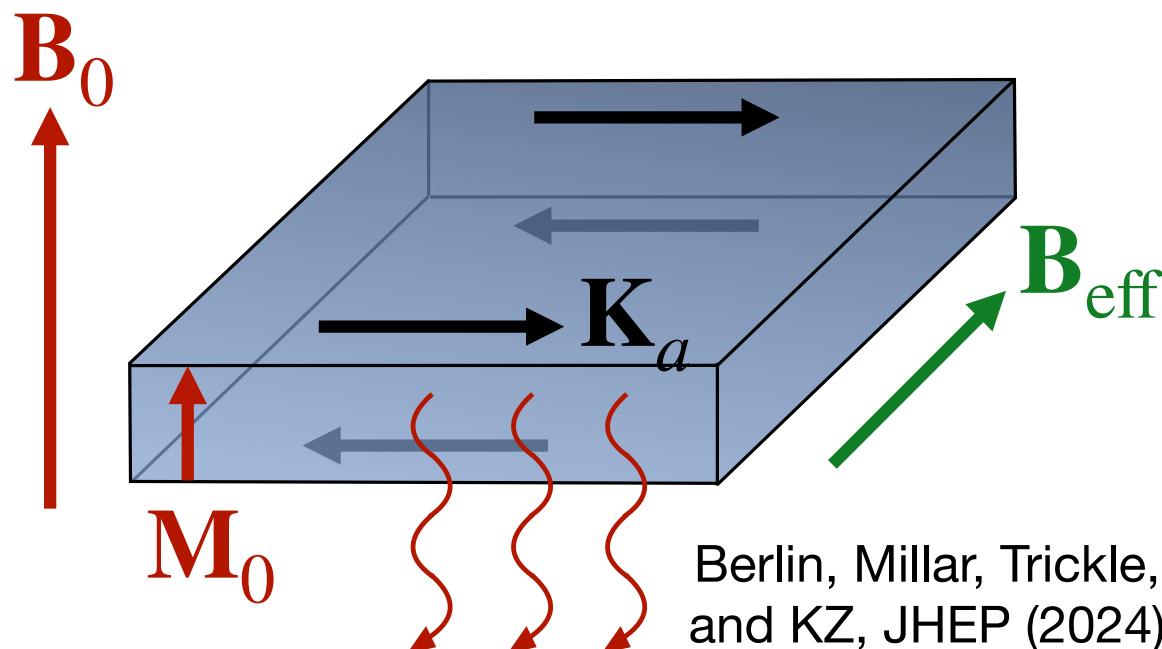
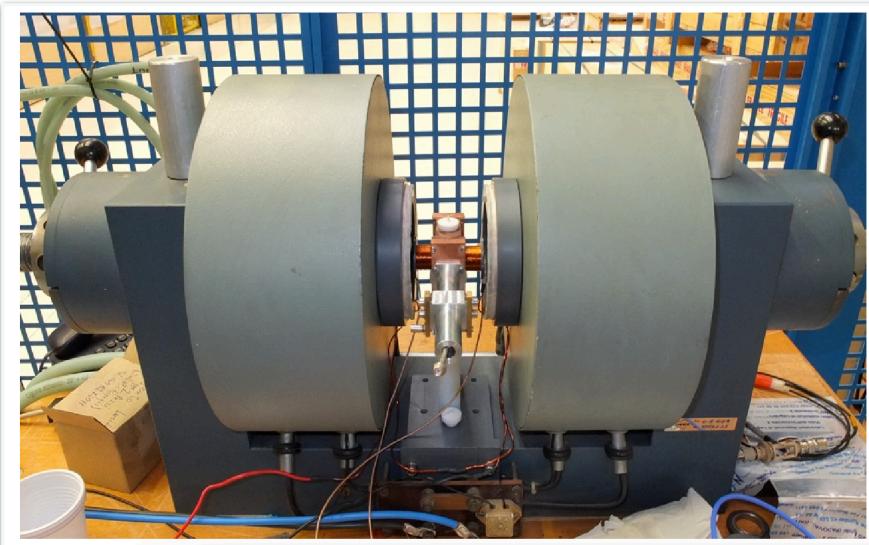
axion-nucleon

$$(\partial_\mu a) \bar{e} \gamma^\mu \gamma^5 e$$

axion-electron

$$a \bar{N} \sigma_{\mu\nu} \gamma^5 N F^{\mu\nu}$$

axion-EDM



Exerts electron spin torque $\tau = \hat{s} \times \mathbf{B}$ through effective magnetic field $\mathbf{B}_{\text{eff}} = g_{ae} \nabla a$

Stronger signals than nuclear case, but electron spins are “messier”

Most experiments amplify with ferromagnetic resonance, so sample excites a microwave cavity

New concept: emit radiation from “magnetic multilayer”, substituting scale for resonance

$$(\partial_\mu a) K_{\text{EM}}^\mu$$

axion-photon

$$(\partial_\mu a) \bar{N} \gamma^\mu \gamma^5 N$$

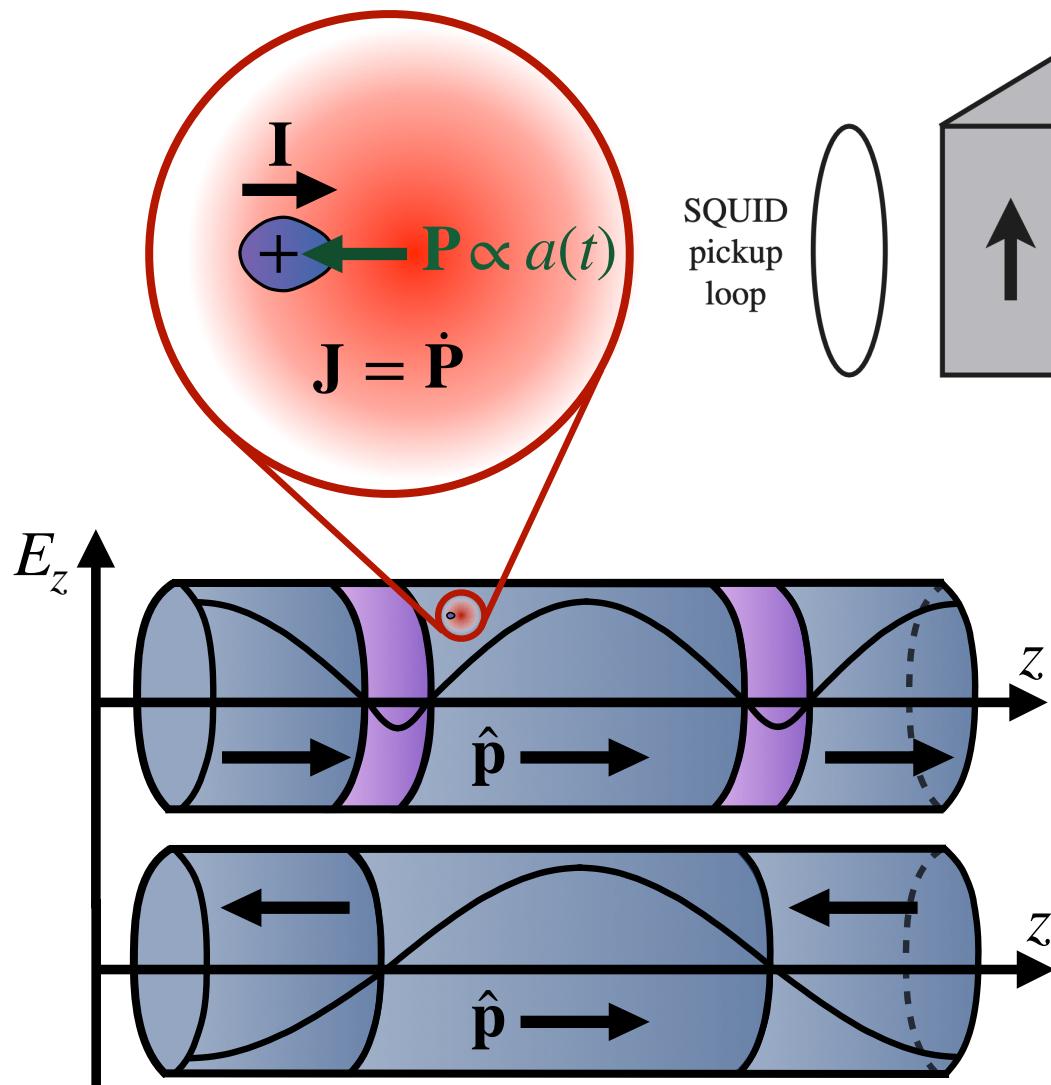
axion-nucleon

$$(\partial_\mu a) \bar{e} \gamma^\mu \gamma^5 e$$

axion-electron

$$a \bar{N} \sigma_{\mu\nu} \gamma^5 N F^{\mu\nu}$$

axion-EDM



Berlin and KZ, PRD (2023)

Leads to time-dependent nuclear and atomic electric dipole moments

Traditional EDM experiments don't work, as the EDM oscillates rapidly in time

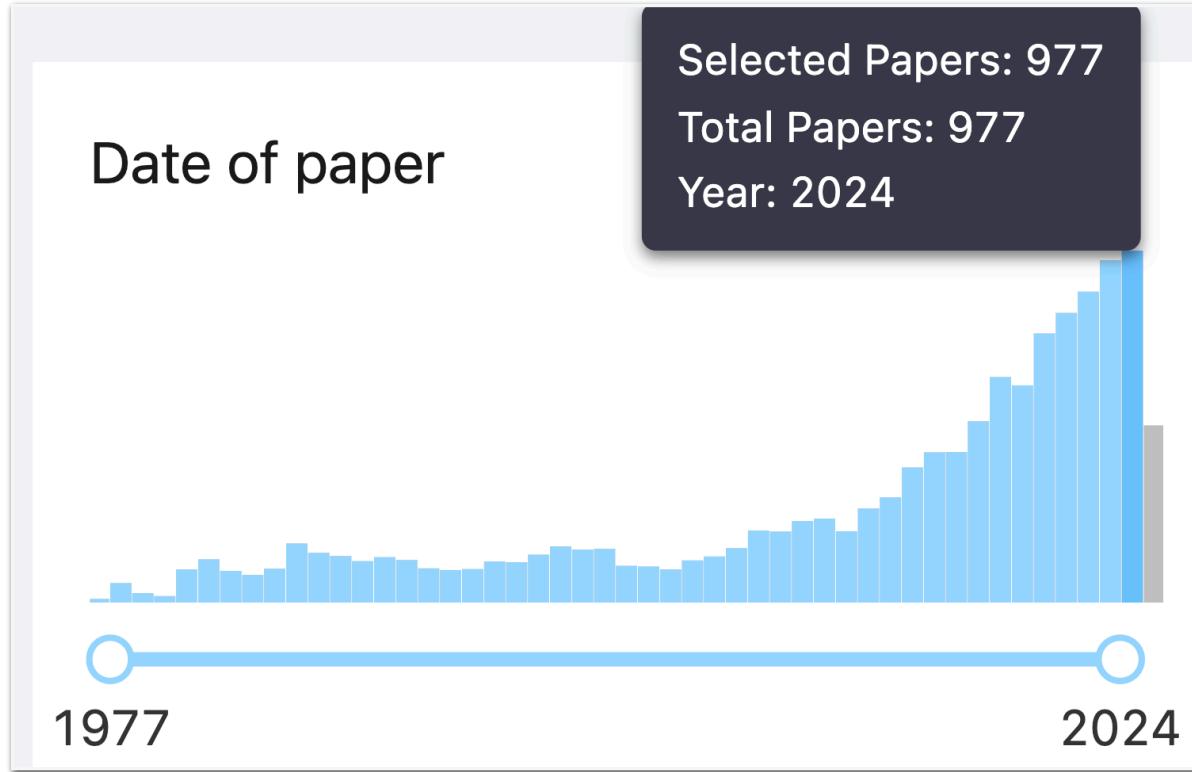
Below GHz: in sample with background \mathbf{E} , amplify with nuclear magnetic resonance

Above GHz: use oscillating current $\mathbf{J} = d\mathbf{P}/dt$ to excite a resonant microwave cavity

Both quite difficult, better for “post discovery”

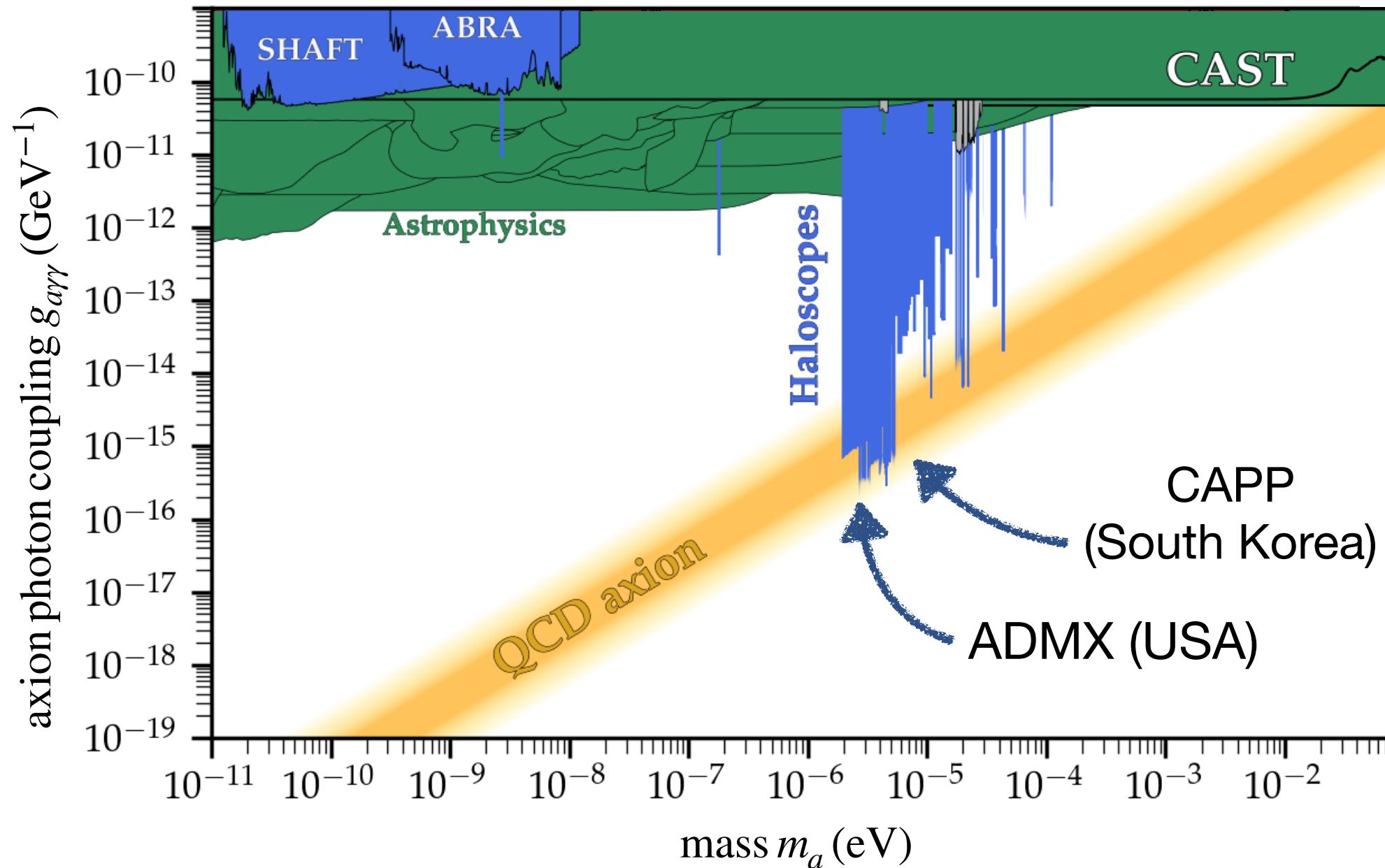
Axion Searches: Theory and Practice

Many papers have been written, and many experimental collaborations formed



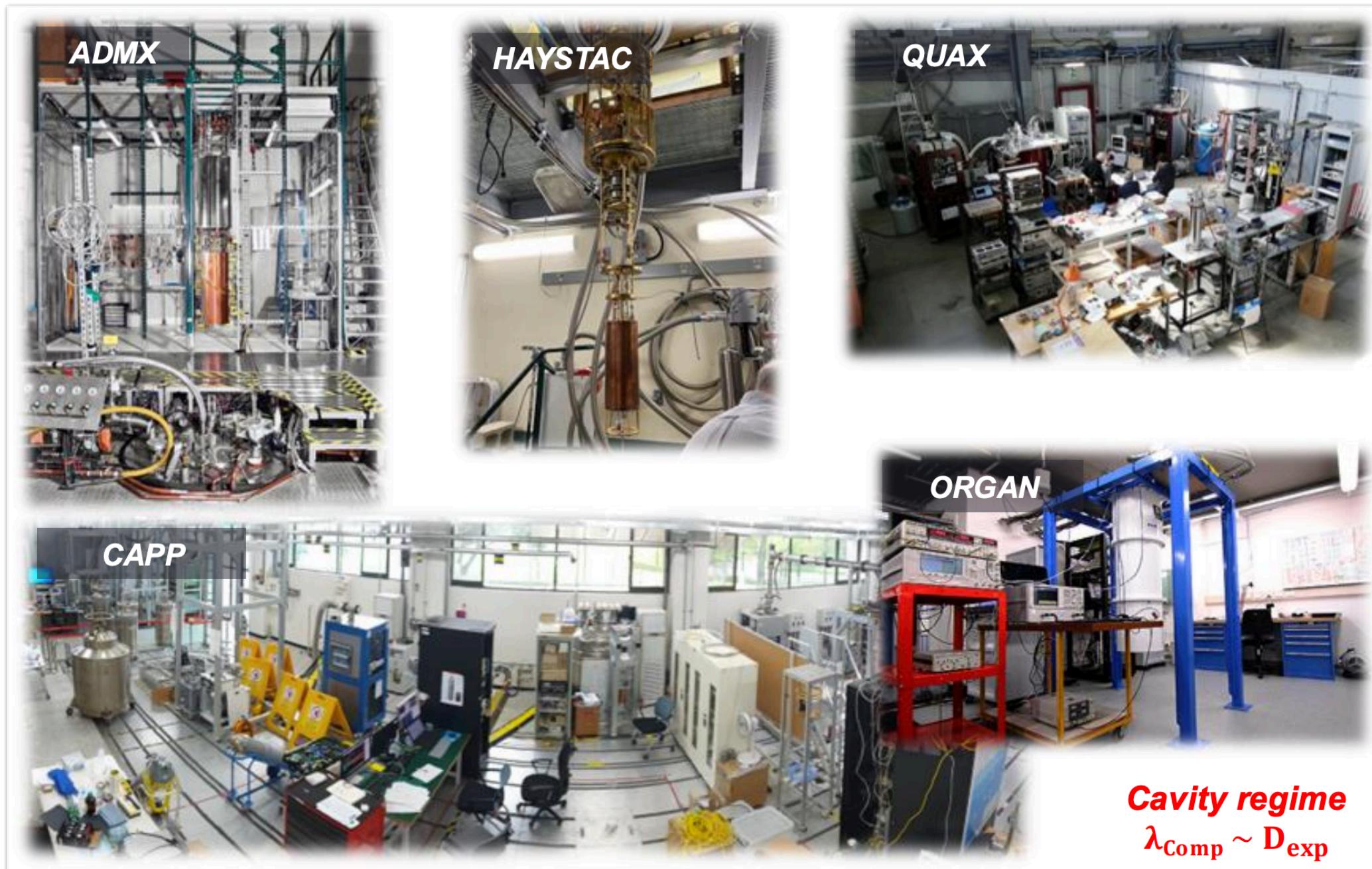
But many sensitivity projections from theorists are overly optimistic,
and many experiments only aim for very low sensitivity

Axion Searches: Theory and Practice



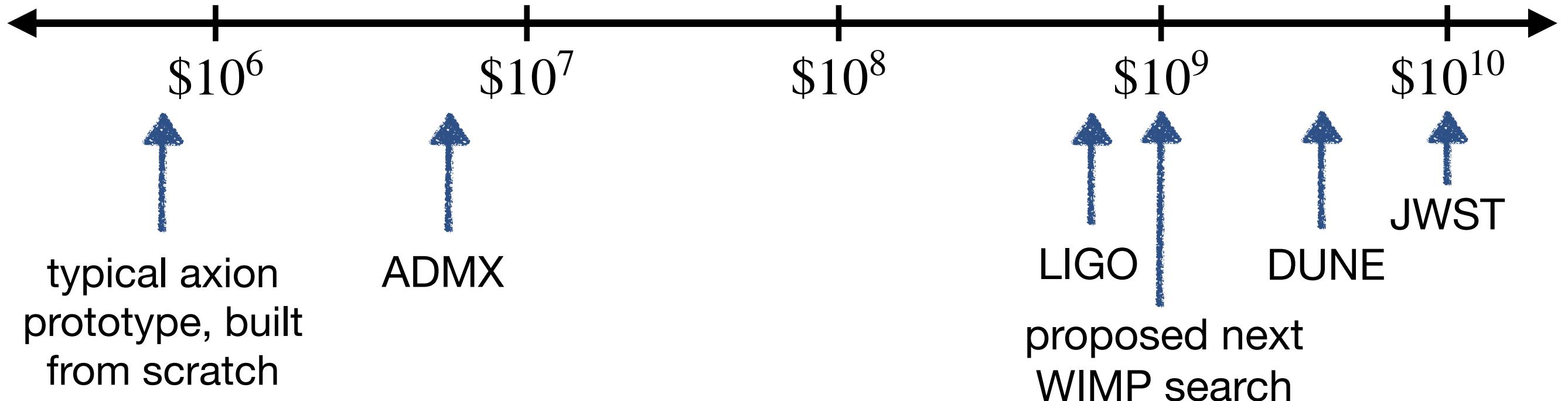
Currently, only the axion-photon coupling has been probed significantly, and largely by just two experiments, both cavity haloscopes

Cavity Haloscopes in the Lab



(slide by Sungwoo Youn, present director of CAPP)

Axion Searches: Theory and Practice



Axion experiments are “small scale” science

Achieving strong sensitivity costs more than an average graduate student, but fits within the scale of a university lab

A decisive next-generation axion experiment would still be a very small fraction of a national particle physics budget

$$(\partial_\mu a) K_{\text{EM}}^\mu$$

axion-photon

$$(\partial_\mu a) \bar{N} \gamma^\mu \gamma^5 N$$

axion-nucleon

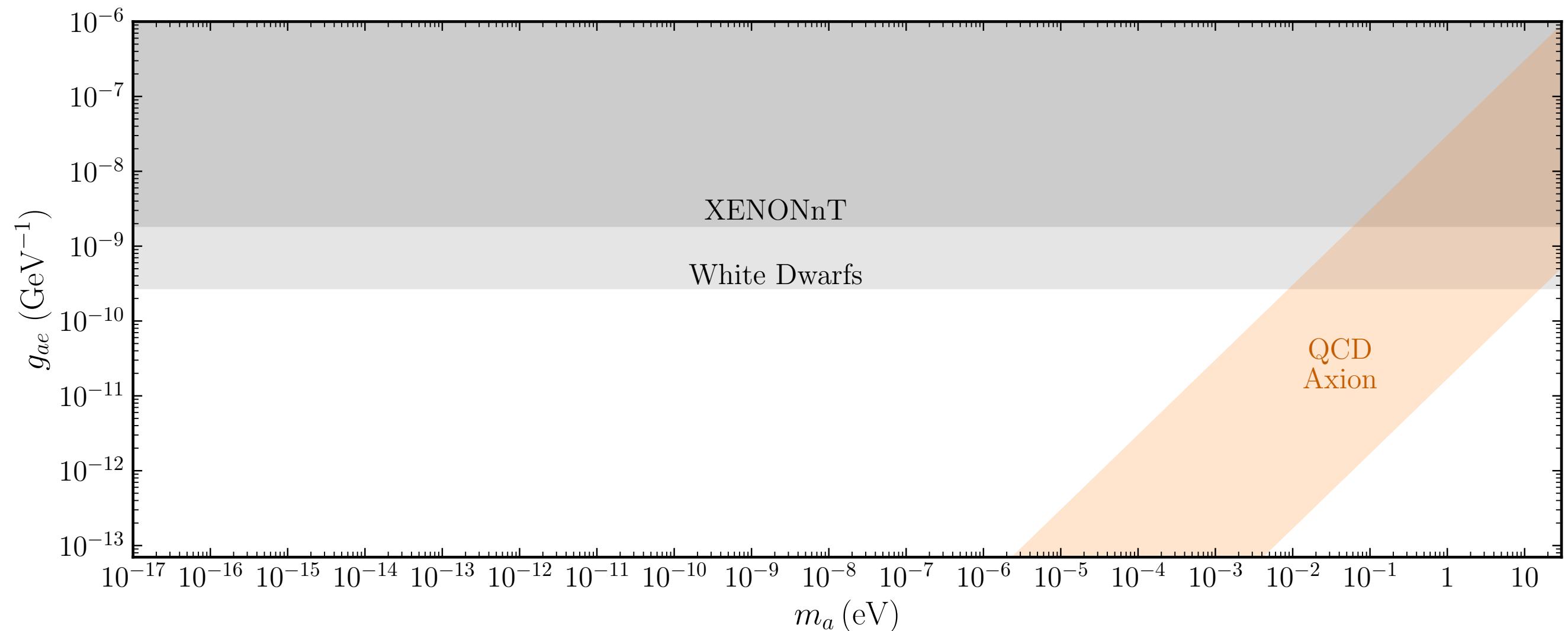
$$(\partial_\mu a) \bar{e} \gamma^\mu \gamma^5 e$$

axion-electron

$$a \bar{N} \sigma_{\mu\nu} \gamma^5 N F^{\mu\nu}$$

axion-EDM

This talk explains: what will and won't work to probe the axion-electron coupling



The Axion-Electron Coupling

Lagrangian has axial vector current:

$$\mathcal{L} \supset g(\partial_\mu a) \bar{e} \gamma^\mu \gamma^5 e$$

Which is a classical particle's spin 4-vector:

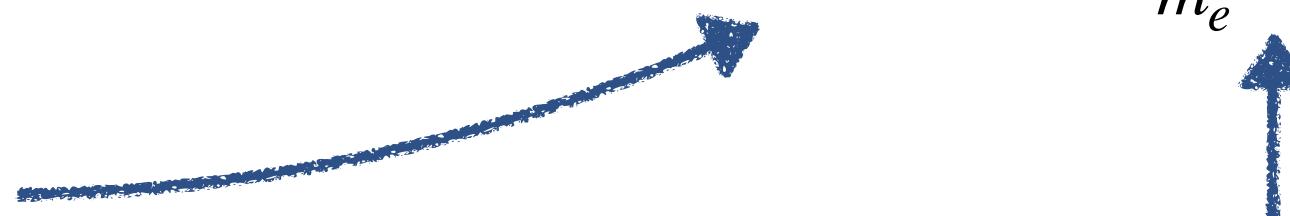
$$\int d^3x \bar{e} \gamma^\mu \gamma^5 e \rightarrow s^\mu \simeq (\mathbf{v} \cdot \hat{\mathbf{s}}, \hat{\mathbf{s}})^\mu$$

So for a nonrelativistic quantum particle:

$$H \supset -g(\nabla a) \cdot \sigma - \frac{g}{m_e} \dot{a} \sigma \cdot (\mathbf{p} - q\mathbf{A})$$

“axion wind” spin torque

$$\tau = g \hat{\mathbf{s}} \times \nabla a$$



“axioelectric” term

both terms oscillate with the axion field, at $f \sim (m_a/\mu\text{eV})$ GHz

$$|\nabla a| \sim v_{\text{DM}} \dot{a} \text{ where } v_{\text{DM}} \sim 10^{-3}$$

axioelectric term seems larger, but subject to traps!

Axioelectric Pitfalls

For simplicity, set $\nabla a = \mathbf{B} = 0$ and work in gauge $\mathbf{E} = -\dot{\mathbf{A}}$

$$H \simeq \frac{(\mathbf{p} - q\mathbf{A})^2}{2m_e} - \frac{g}{m_e} \dot{a} \sigma \cdot (\mathbf{p} - q\mathbf{A})$$

Idea #1: this implies $\mathcal{H} \supset -\mathbf{J}_{\text{eff}} \cdot \mathbf{A}$ where $\mathbf{J}_{\text{eff}} = (g\dot{a}q/m_e) \langle n_e \sigma \rangle$, a large current!

However, it would be more transparent to write: $H \simeq \frac{(\mathbf{p} - q\mathbf{A} - g\dot{a}\sigma)^2}{2m_e}$

No extra contribution to the current, but a new force: $\mathbf{A}_{\text{eff}} = (g/q) \dot{a}\sigma$ $\mathbf{F} = -g \frac{d}{dt} \langle \dot{a}\sigma \rangle$

Generally very small, because it is suppressed by two time derivatives

Idea #2: integrating the force over time yields $\mathbf{J} = (g\dot{a}q/m_e) \langle n_e \sigma \rangle$, a large current!

(For DFSZ axion, would be $\sim 10^3$ larger than \mathbf{J}_{eff} from axion-photon coupling)

Estimating the Axioelectric Current

How large of a current can we really get from $\mathbf{E}_{\text{eff}} = (g/q) \ddot{a} \sigma$?

In a spin-polarized dielectric, we have: $\mathbf{J}_a = \dot{\mathbf{P}}_a = (\epsilon - 1) \dot{\mathbf{E}}_{\text{eff}}$

But material also creates electric field: ~~$\nabla \times \nabla \times \mathbf{E} + \epsilon \ddot{\mathbf{E}} = -\dot{\mathbf{J}}_a$~~

Total polarization current:

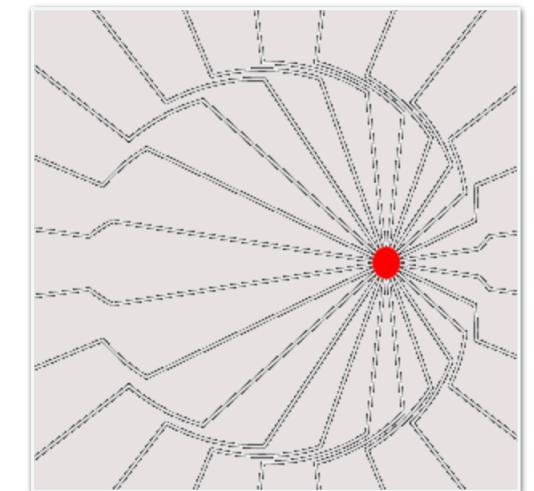
$$\mathbf{J}_{\text{tot}} = (\epsilon - 1)(\dot{\mathbf{E}} + \dot{\mathbf{E}}_{\text{eff}}) = \frac{\epsilon - 1}{\epsilon} \dot{\mathbf{E}}_{\text{eff}}$$

Result suppressed by **three** time derivatives! But what if charges can move?

$$\epsilon(\omega) \sim \begin{cases} 1 + i\sigma/\omega & \text{ideal conductor} \\ 1 - \omega_p^2/\omega^2 & \text{ideal superconductor} \end{cases}$$

Above result holds, and implies $\mathbf{J}_{\text{tot}} \sim \dot{\mathbf{E}}_{\text{eff}}$ even when $|\epsilon| \gg 1$!

Physically, better conductors shield \mathbf{E}_{eff} more



Estimating the Axioelectric Current

How large of a current can we really get from $\mathbf{E}_{\text{eff}} = (g/q) \ddot{a} \sigma$?

In a spin-polarized dielectric, we have: $\mathbf{J}_a = \dot{\mathbf{P}}_a = (\epsilon - 1) \dot{\mathbf{E}}_{\text{eff}}$

But material also creates electric field:

$$\nabla \times \nabla \times \mathbf{E} + \epsilon \ddot{\mathbf{E}} = -\dot{\mathbf{J}}_a$$

Takeaway: can't just treat electrons as free.

Total polarization current:

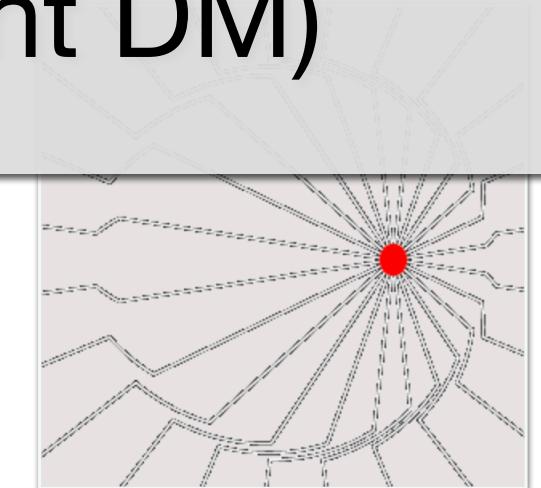
$$\mathbf{J}_{\text{tot}} = (\epsilon - 1)(\dot{\mathbf{E}} + \dot{\mathbf{E}}_{\text{eff}}) = \frac{\epsilon - 1}{\epsilon} \dot{\mathbf{E}}_{\text{eff}}$$

Material shielding effects can be very important.
(also applies to other forms of ultralight DM)

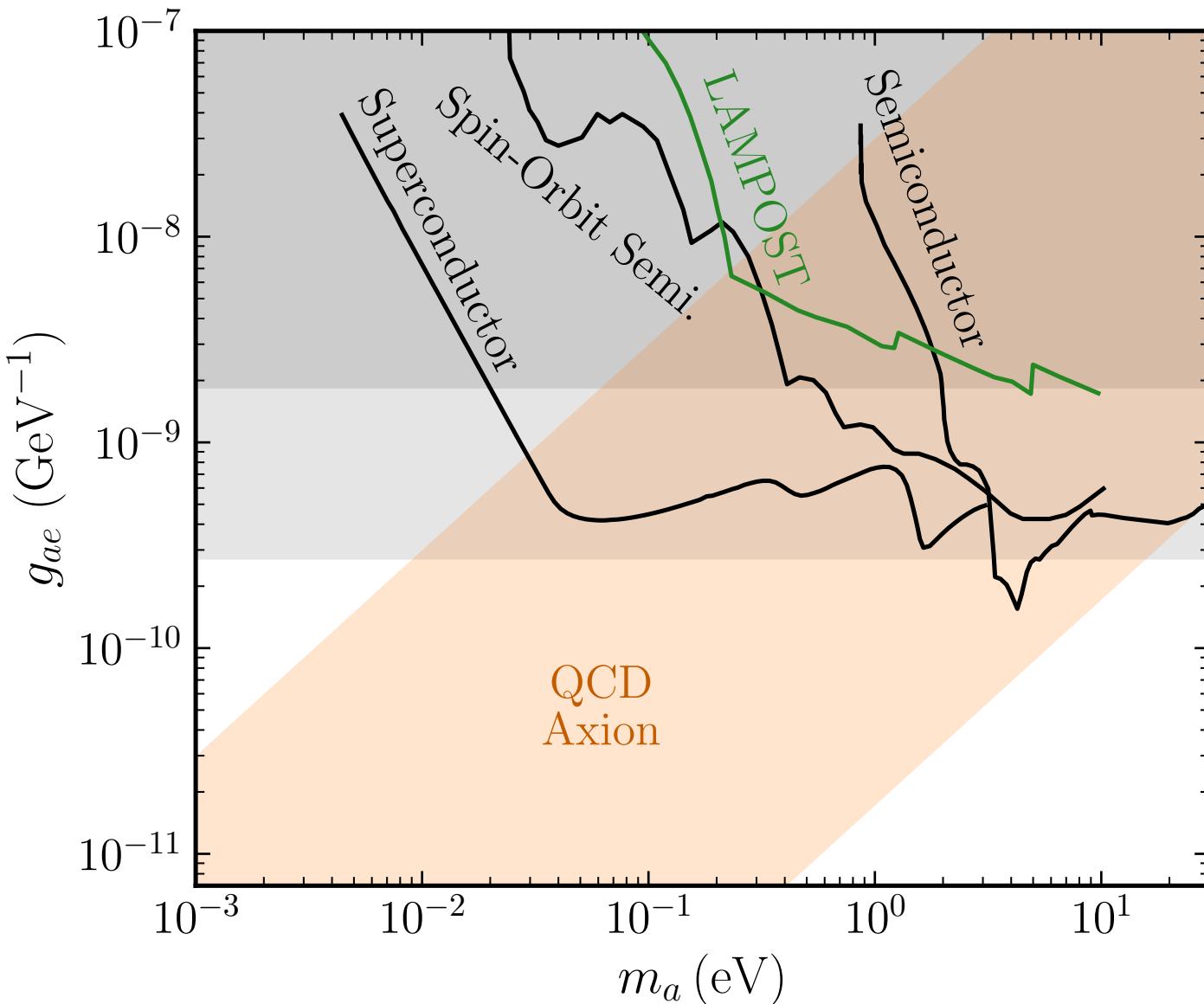
$$\epsilon(\omega) \sim \begin{cases} 1 & \text{ideal conductor} \\ 1 - \omega_p^2/\omega^2 & \text{ideal superconductor} \end{cases}$$

Above result holds, and implies $\mathbf{J}_{\text{tot}} \sim \dot{\mathbf{E}}_{\text{eff}}$ even when $|\epsilon| \gg 1$!

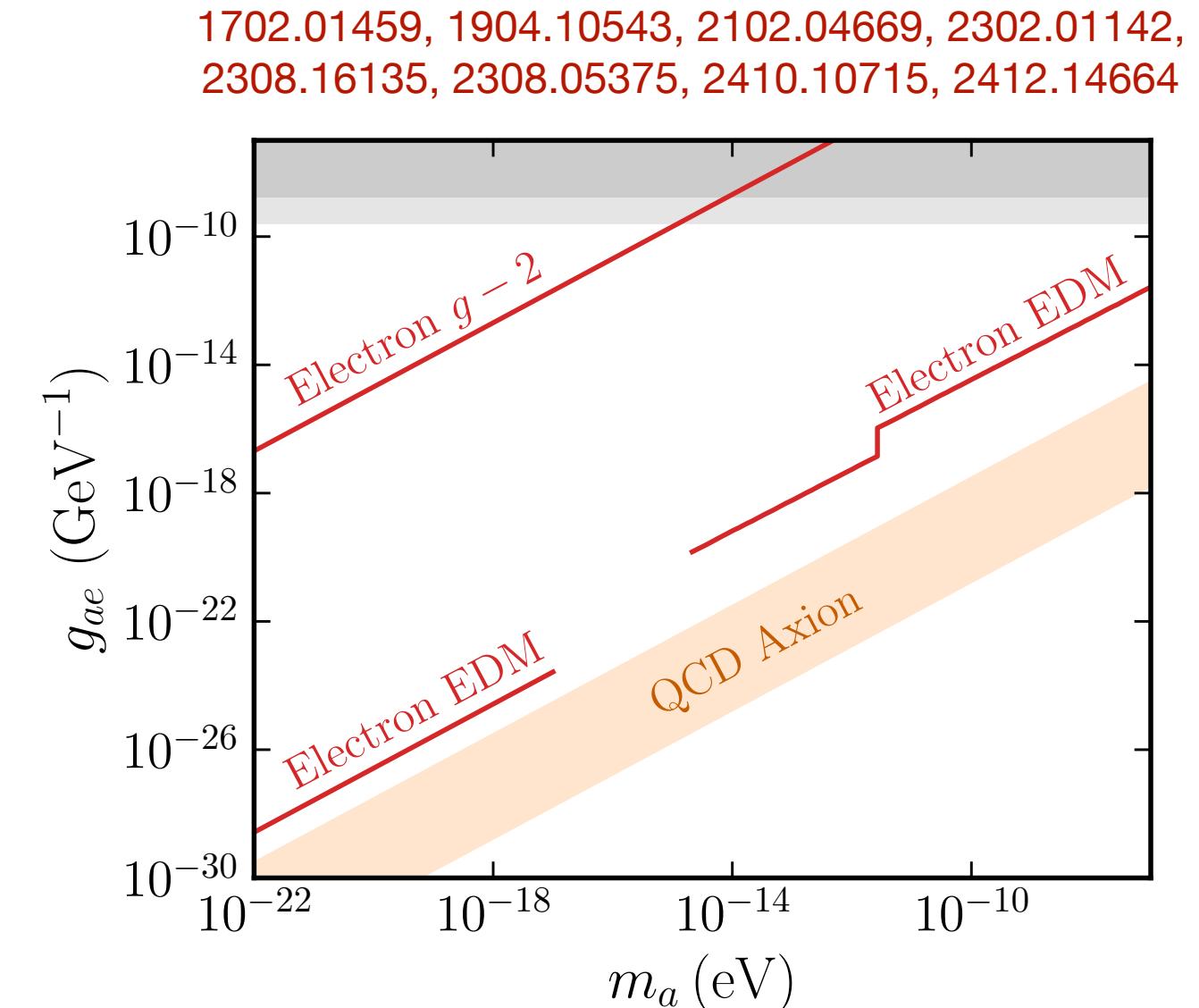
Physically, better conductors shield \mathbf{E}_{eff} more



Axioelectric Reach vs. Other Projections



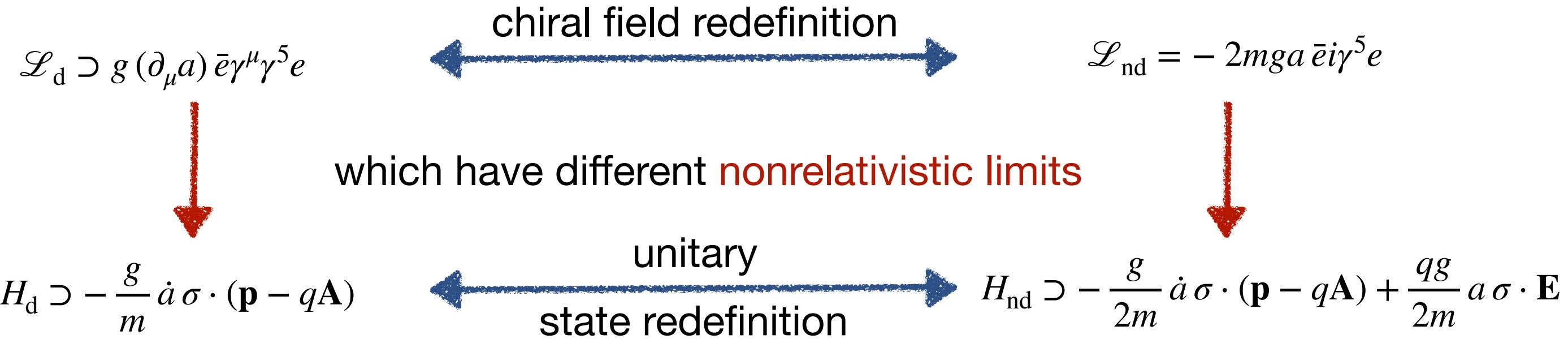
Since $\mathbf{J} \propto d^3a/dt^3$, best probes are at high m_a , and still not very strong...



...but many recent papers claimed **vastly** stronger effects proportional to a !

The EDM Controversy

The axion-electron coupling has two equivalent forms



which are related by redefining states, $|\psi'\rangle = U|\psi\rangle$, so that all observables same

$$U \simeq \exp \left(-\frac{iga}{2m} (\mathbf{p} - q\mathbf{A}) \cdot \boldsymbol{\sigma} \right)$$

Already noted for pion-nucleon interactions in 1950s – but not obvious how!

Coefficient of the Axioelectric Term

For simplicity take $q = 0$, where only difference is axioelectric coefficient:

$$H_d \supset -\frac{g\dot{a}}{m} \boldsymbol{\sigma} \cdot \mathbf{p}$$

$$H_{nd} \supset -\frac{g\dot{a}}{2m} \boldsymbol{\sigma} \cdot \mathbf{p}$$

Puzzle: why can the coefficient of a force be freely adjusted?

Resolution: **any** force can be removed from a single particle Hamiltonian by working in the particle's reference frame; only relative accelerations physical

$$H_d \supset V(\mathbf{x}_1 - \mathbf{x}_2) - \frac{g\dot{a}}{m} (\boldsymbol{\sigma}_1 \cdot \mathbf{p}_1 + \boldsymbol{\sigma}_2 \cdot \mathbf{p}_2)$$

$$H_{nd} \supset V(\mathbf{x}_1 - \mathbf{x}_2) - \frac{g\dot{a}}{2m} (\boldsymbol{\sigma}_1 \cdot \mathbf{p}_1 + \boldsymbol{\sigma}_2 \cdot \mathbf{p}_2) - \frac{ga}{2m} (\boldsymbol{\sigma}_1 - \boldsymbol{\sigma}_2) \cdot \nabla_1 V(\mathbf{x}_1 - \mathbf{x}_2)$$

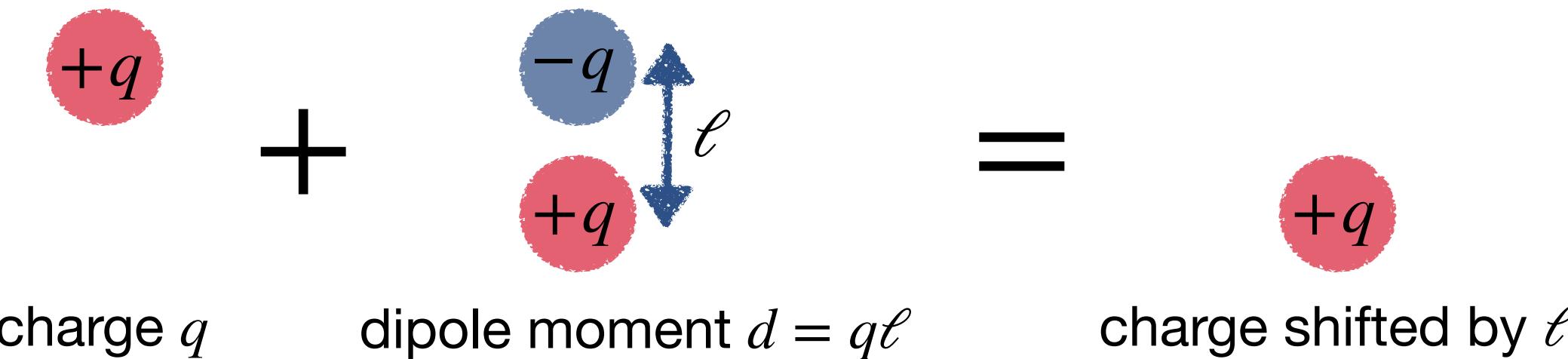
Shifting the axioelectric coefficient adds other terms with same physical effect

True and Spurious EDMs

The new term is the nonrelativistic limit of a genuine EDM:

$$H_{\text{nd}} \supset \frac{qga}{2m} \sigma \cdot \mathbf{E} \quad H_{\text{EDM}} = \frac{d}{2} \Psi \gamma^5 \sigma^{\mu\nu} \Psi F_{\mu\nu} = -d \sigma \cdot \mathbf{E} + (\text{relativistic corrections})$$

But for charged nonrelativistic particles, a constant EDM has no physical effects!



In this limit, just equivalent to unobservable shift in definition of position!
(key intuition behind “Schiff screening”)

True and Spurious EDMs

The new term is the nonrelativistic limit of a genuine EDM:

$$H_{\text{nd}} \supset \frac{qga}{2m} \boldsymbol{\sigma} \cdot \mathbf{E} \quad H_{\text{EDM}} = \frac{d}{2} \Psi \gamma^5 \sigma^{\mu\nu} \Psi F_{\mu\nu} = -d \boldsymbol{\sigma} \cdot \mathbf{E} + (\text{relativistic corrections})$$

But for charged nonrelativistic particles, a constant EDM has no physical effects!

The effects of a true EDM probed in experiments are from relativistic corrections:

$O(v/c)$ magnetic dipole, $O(v^2/c^2)$ length contraction

Commins, Jackson, DeMille (2007)

so H_{nd} contains **only** the part of H_{EDM} with no physical effect!

(time-varying $a(t)$ does have effect, but highly suppressed by $\sim (m_a/\text{eV})^2$)

Stadnik and Flambaum (2014)

True and Spurious EDMs

The new term is the nonrelativistic limit of a genuine EDM:

Takeaway: large terms in H or \mathcal{L} don't always imply large physical effects.

But for charged nonrelativistic particles, a constant EDM has no physical effects!

Can be artifacts of using wrong “reference frame”

The effects of a true EDM probed in experiments are from relativistic corrections:

$O(v/c)$ magnetic dipole, $O(v^2/c^2)$ length contraction

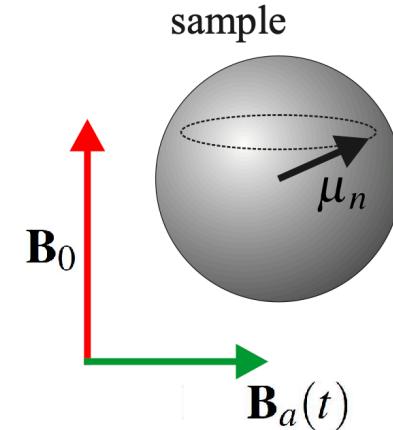
Takeaway: for derivatively coupled axion, beware of any claimed effect that persists as $m_a \rightarrow 0$

Almost always results from unphysical assumption!

Stadnik and Flambaum (2014)

Probing the Axion Wind Torque

The axion wind spin torque tilts spins, yielding oscillating transverse magnetic field



Naively seems easier for electrons, as $\mu_e/\mu_n \sim m_p/m_e \sim 10^3$
But typical quality factors much lower!

Solid magnetic material

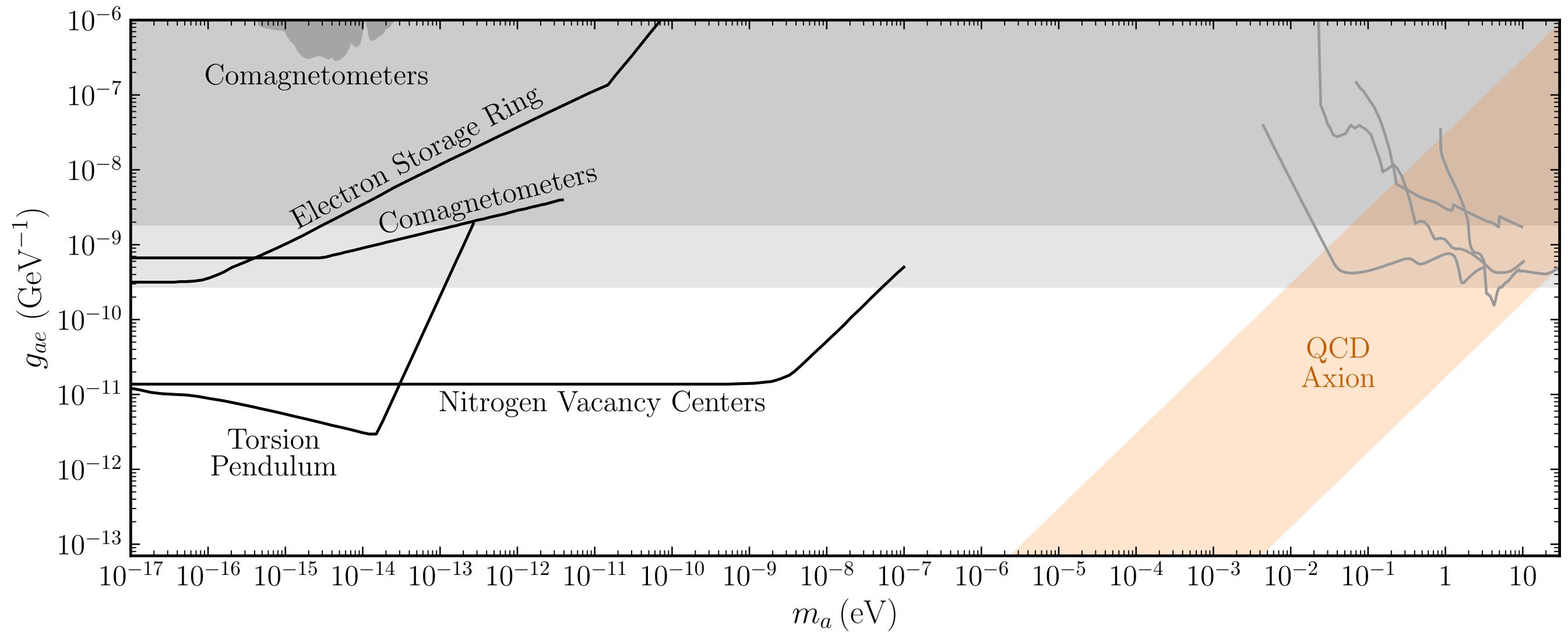
Naturally probes $m_a \sim \text{meV}$ but interactions prevent very high Q

Signal is emitted meV radiation

"Separated" or "locked" electrons

Much higher Q and lower resonant frequencies possible

Signal is quasistatic magnetic field, detected by magnetometer

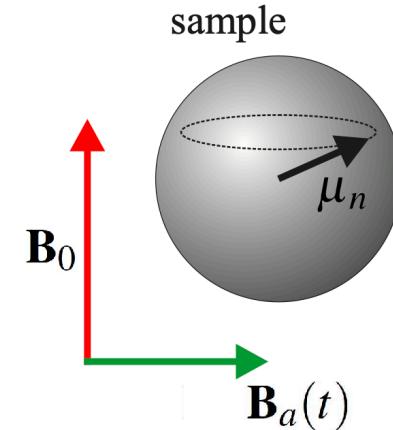


Separated electrons: comagnetometer vapor, storage ring bunch, NV centers
 (but much lower number density results in limited sensitivity)

Locked electrons: align spins to crystal, so spin torque becomes mechanical
 (but suppressed by inertia of nuclei, doesn't benefit from electron being light)

Probing the Axion Wind Torque

The axion wind spin torque tilts spins, yielding oscillating transverse magnetic field



Naively seems easier for electrons, as $\mu_e/\mu_n \sim m_p/m_e \sim 10^3$
But typical quality factors much lower!

Solid magnetic material

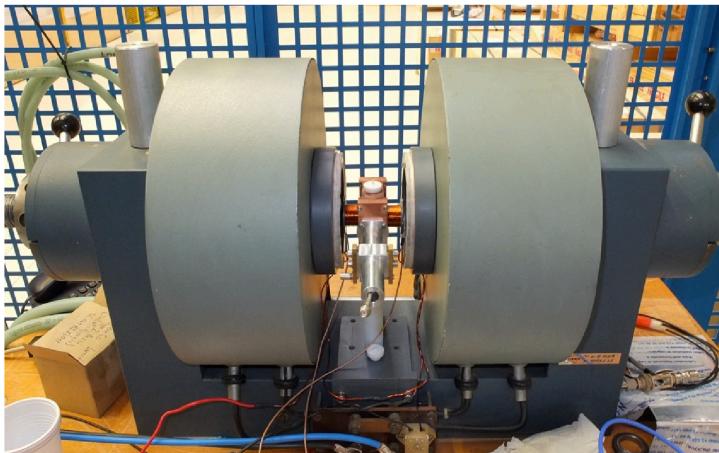
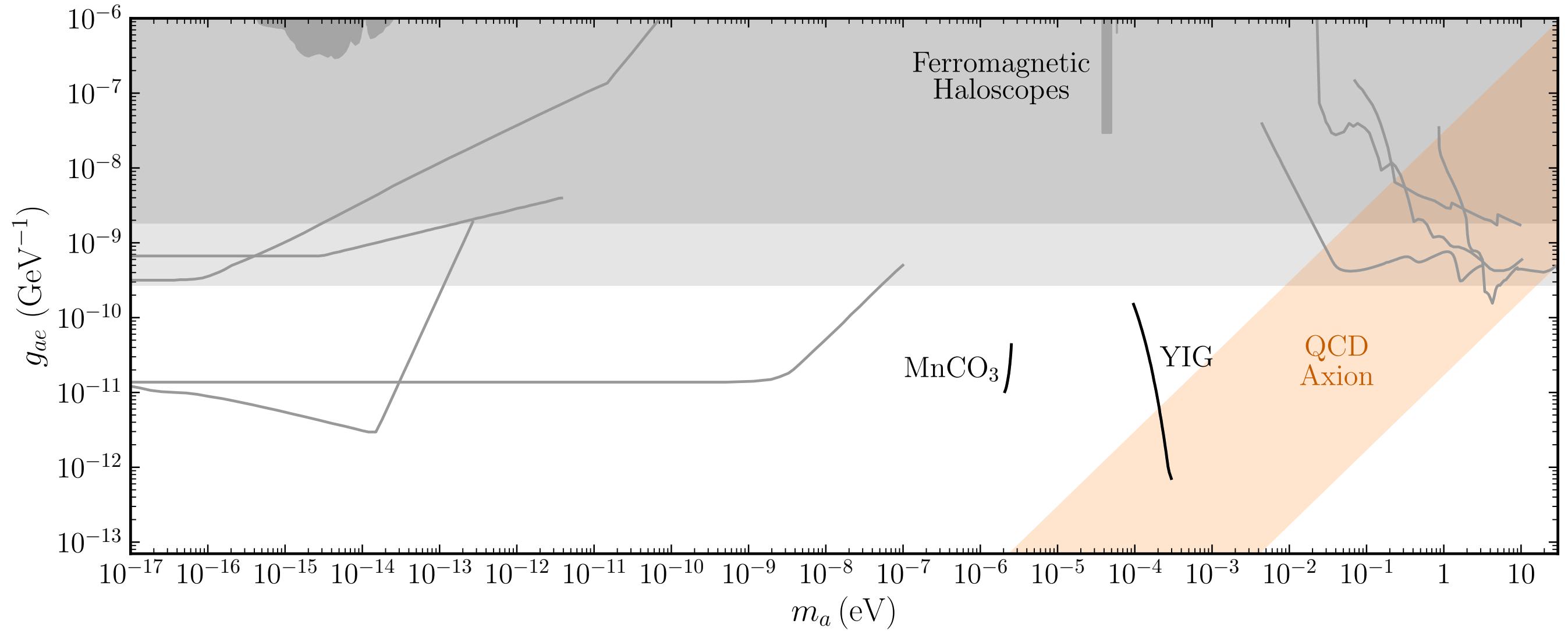
Naturally probes $m_a \sim \text{meV}$ but interactions prevent very high Q

Signal is emitted meV radiation

“Separated” or “locked” electrons

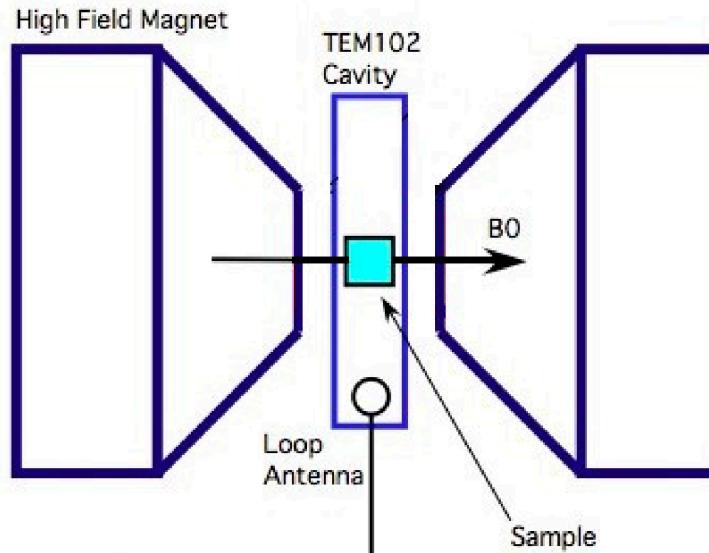
Much higher Q and lower resonant frequencies possible

Signal is quasistatic magnetic field, detected by magnetometer



Before our work, all existing and proposed experiments used the “ferromagnetic haloscope” concept

The Ferromagnetic Haloscope



effective magnetic field

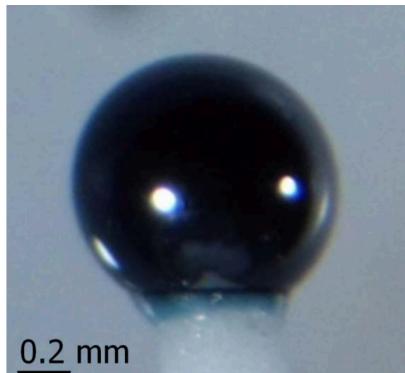
$$\mathbf{B}_{\text{eff}} = \frac{g_{ae}}{\mu_B} \nabla a$$

magnetic quality factor

$$Q_m \sim 10^4$$

sample magnetization

$$\omega_m = 2\mu_B M_0 \sim 0.03 \text{ meV}$$



$$V \sim \begin{cases} 0.005 \text{ cm}^3 & \text{QUAX (2018)} \\ 0.01 \text{ cm}^3 & \text{Flower et al. (2019)} \\ 0.1 \text{ cm}^3 & \text{QUAX (2020)} \\ 100 \text{ cm}^3 & \text{QUAX target} \end{cases}$$

Main issue: scaling sample volume

Single crystal YIG made very slowly, in mm spheres, at cost of over \$10⁷/kg

The Ferromagnetic Haloscope

High Field Magnet

TEM102
Cavity

Alternative idea: replace strong resonant enhancement with overall scale

Ferromagnet spin precesses on resonance
with axion, driving a cavity mode

Polycrystalline spinel ferrites are cheap and mass produced



Ferrite Blocks Ceramic Magnets, 1 7/8" x 7/8" x 3/8" Rectangular Magnets, Ceramic Rectangular Square Magnets, Grade-8 Hard Ferrite Magnets for Crafts, Science and Hobbies (8 Pieces)

★★★★★ ~33

\$14⁹⁸

✓prime One-Day
FREE delivery Tomorrow, Nov 18

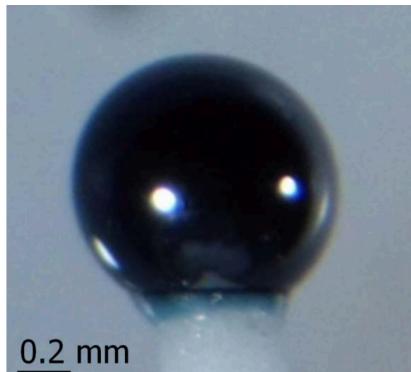
Lower carbon delivery ~

Add to Cart

M_0 double that of YIG

$$Q_m \sim 10^2$$

$$\omega_m = 2\mu_B M_0 \sim 0.03 \text{ meV}$$

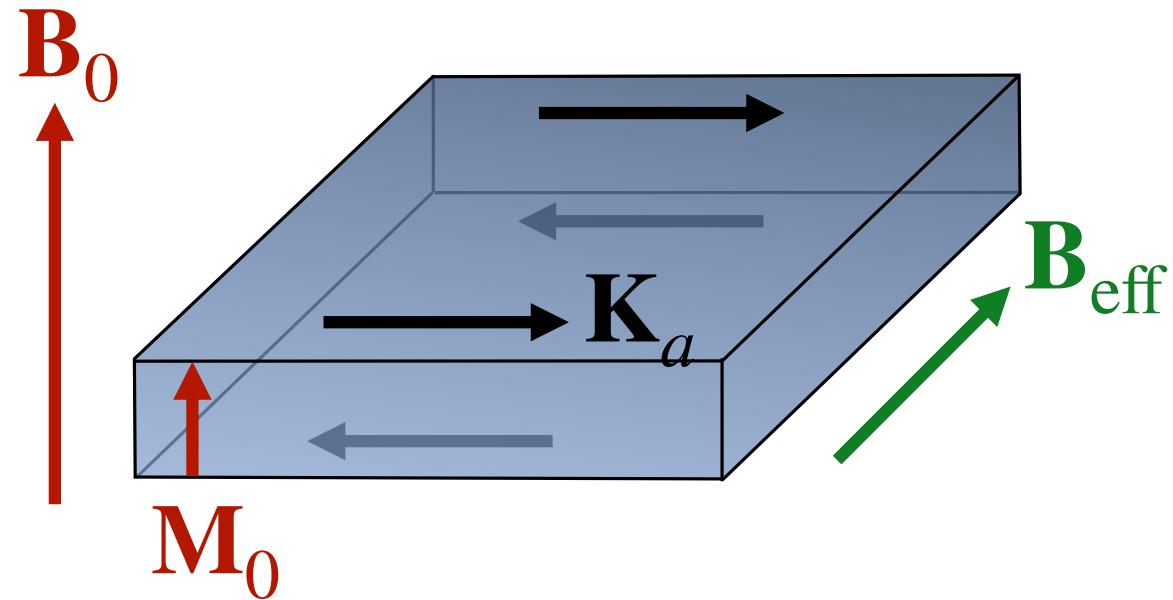


$$V \sim \begin{cases} 0.005 \text{ cm}^3 & \text{QUAX (2018)} \\ 0.01 \text{ cm}^3 & \text{Flower et al. (2019)} \\ 0.1 \text{ cm}^3 & \text{QUAX (2020)} \\ 100 \text{ cm}^3 & \text{QUAX target} \end{cases}$$

Main issue: scaling sample volume

Single crystal YIG made very slowly, in mm spheres, at cost of over \$10⁷/kg

Radiation From a Slab



Solving spin equation of motion:

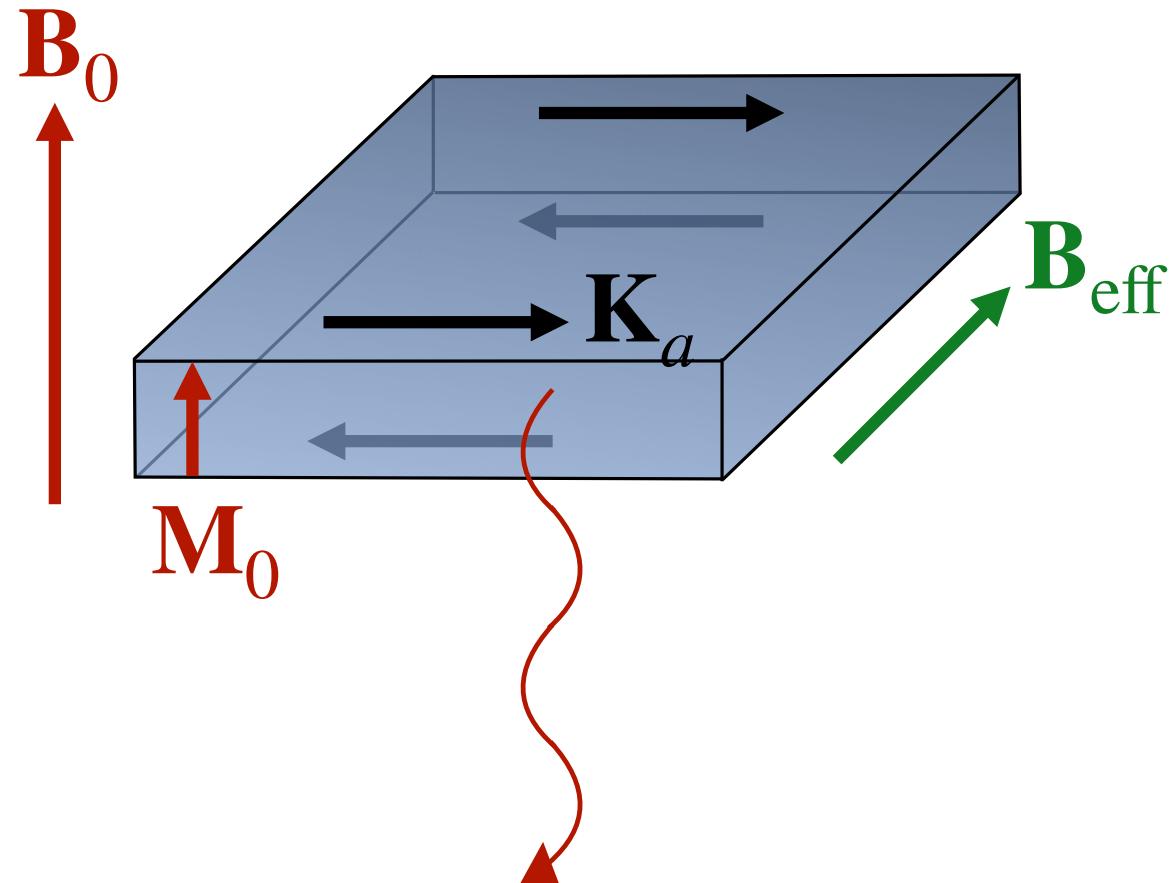
$$\mathbf{J}_a = \nabla \times ((1 - \mu^{-1}) \mathbf{B}_{\text{eff}})$$

Magnetized slab carries surface currents

$$1 - \mu^{-1} \simeq \frac{M_0}{B_0 - (m_a/2\mu_B) - iB_0/2Q_m}$$

(for clockwise polarization)

Radiation From a Slab



much of this power is converted to outgoing radiation

$$\mathbf{J}_a = \nabla \times ((1 - \mu^{-1}) \mathbf{B}_{\text{eff}})$$

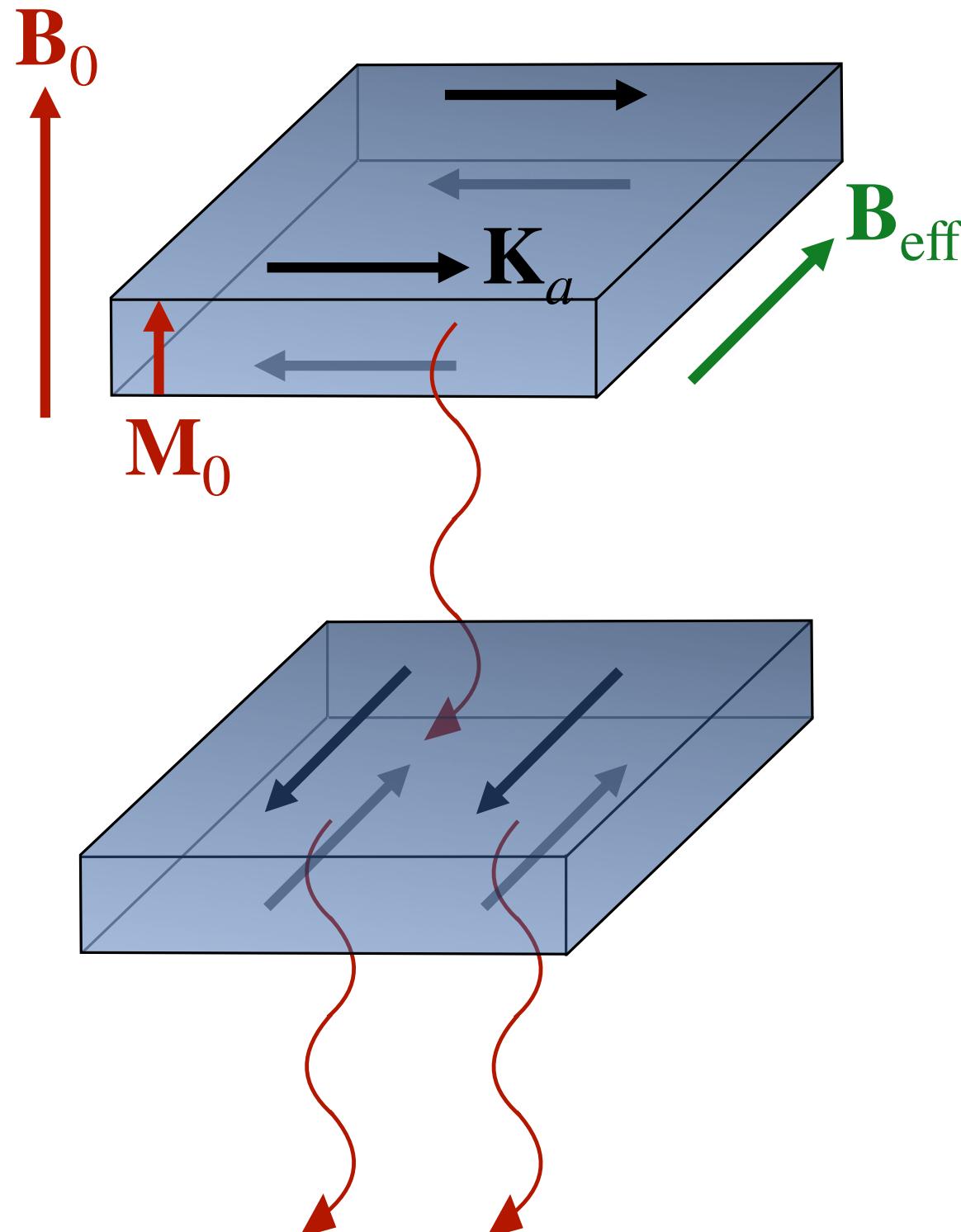
Magnetized slab carries surface currents

$$1 - \mu^{-1} \simeq \frac{M_0}{B_0 - (m_a/2\mu_B) - iB_0/2Q_m}$$

Power deposited in slab maximized on resonance, at tunable frequency

$$(B_0 \leq 10 \text{ T} \text{ implies } m_a \leq 10^{-3} \text{ eV})$$

Radiation From a Slab



$$\mathbf{J}_a = \nabla \times ((1 - \mu^{-1}) \mathbf{B}_{\text{eff}})$$

Magnetized slab carries surface currents

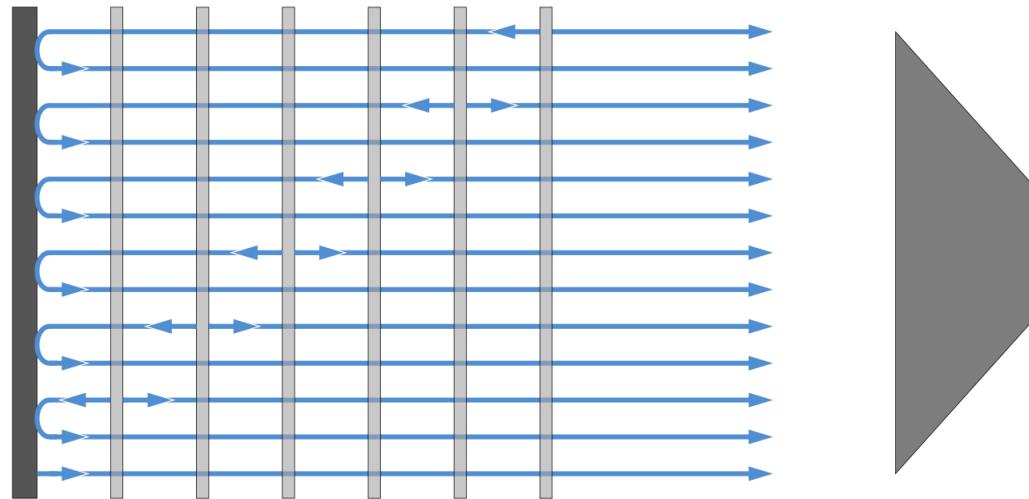
$$1 - \mu^{-1} \simeq \frac{M_0}{B_0 - (m_a/2\mu_B) - iB_0/2Q_m}$$

Power deposited in slab maximized on resonance, at tunable frequency

$$(B_0 \leq 10 \text{ T} \text{ implies } m_a \leq 10^{-3} \text{ eV})$$

Place layers, with tunable separation, so emitted radiation interferes constructively

Magnetized Multilayers



Like the MADMAX experiment, radiation emitted from layers is focused on a detector

For simplicity, we consider the “transparent mode” setup:

slab spacing π/m_a , slab thickness $\pi/(\text{Re}(n) m_a)$

$$P_{\text{sig}} \sim \mathcal{F}^2 N^2 |B_{\text{eff}}|^2 A$$

slab form factor

$$\mathcal{F} \sim 1 - \mu^{-1}$$

(+ material loss effects)

slab area

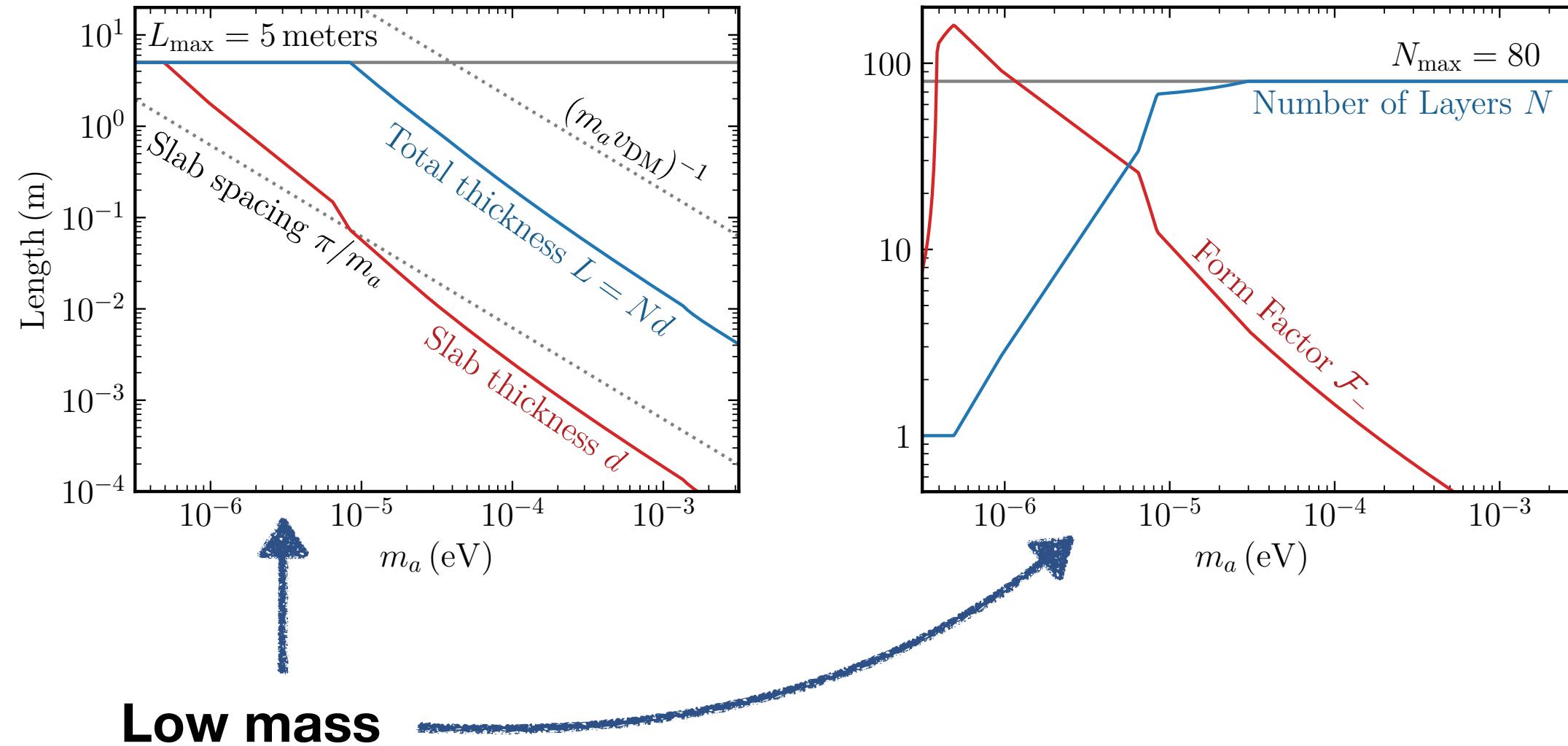
$$A = 1 \text{ m}^2$$

number of layers

$$N \leq 80$$

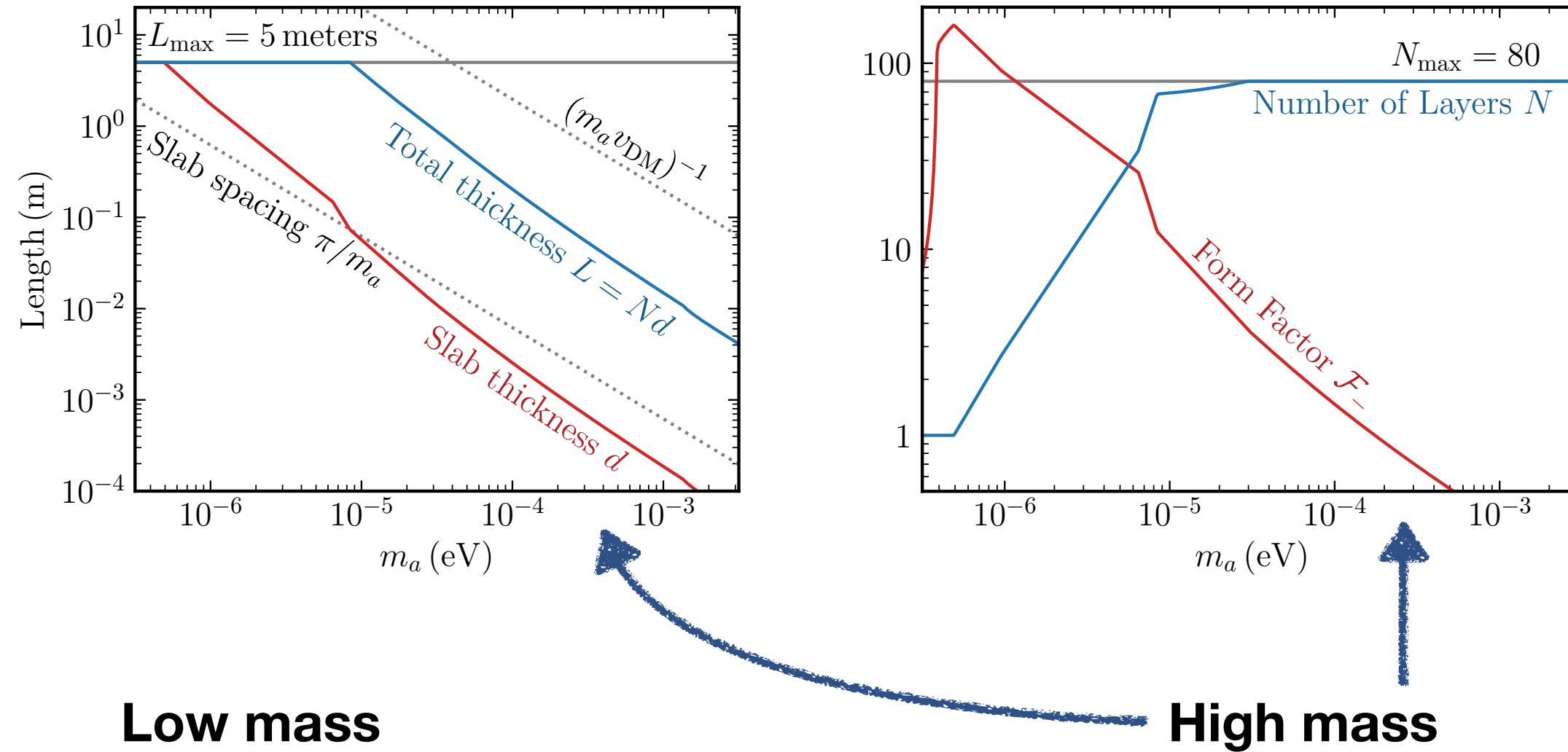
$$N \leq \text{Re}(n)/(\pi \text{Im}(n))$$

Optimizing a Magnetized Multilayer



A few thick slabs tuned close to resonance; large volume needed, but only low magnetic field

Optimizing a Magnetized Multilayer



A few thick slabs tuned close to resonance; large volume needed, but only low magnetic field

Many thin slabs, which must be well off resonance to avoid absorption; high field but only in small volume

Benchmark Reach

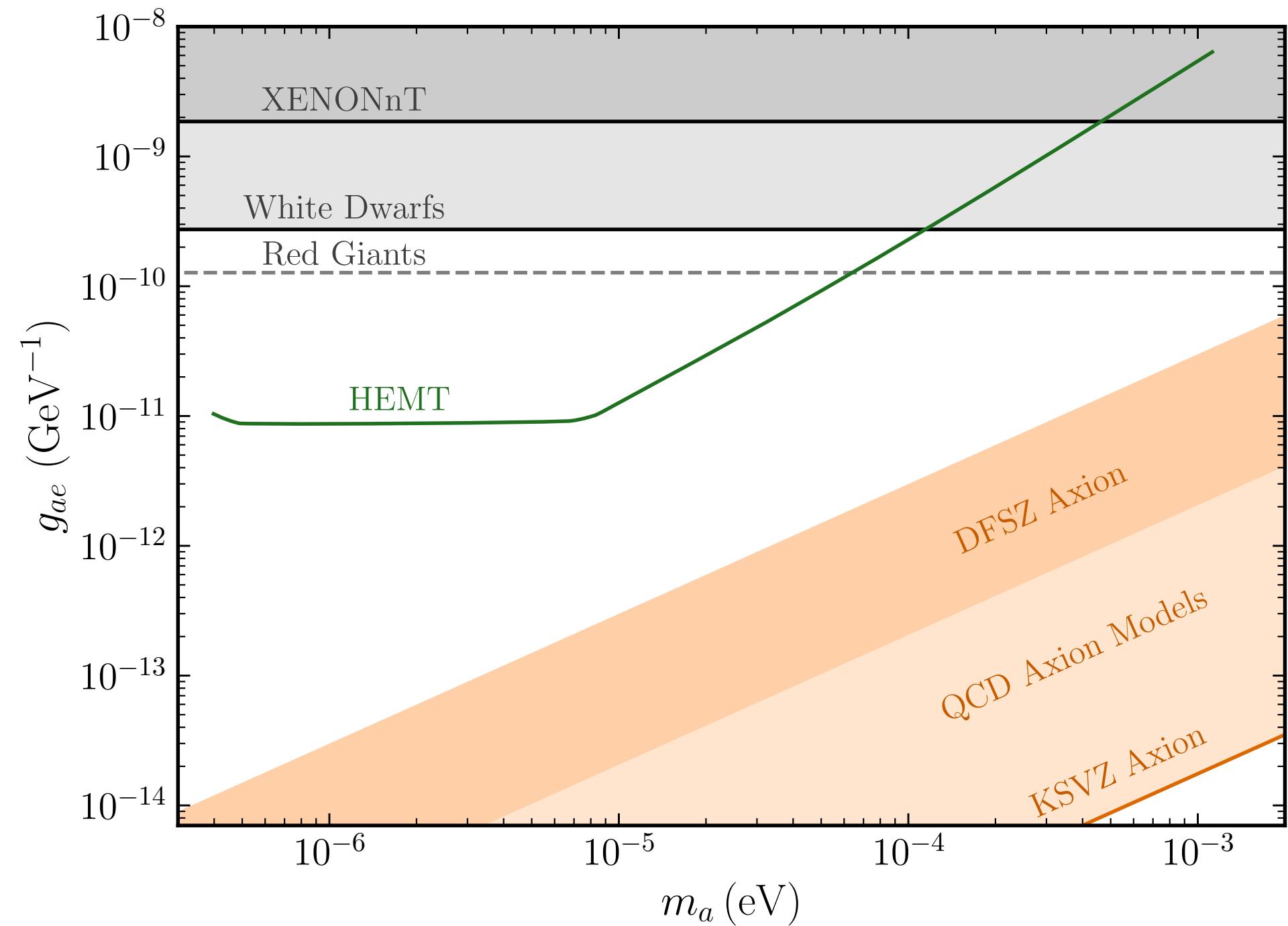
$$\text{SNR} \simeq \frac{P_{\text{sig}}}{T_n} \sqrt{\frac{t_{\text{int}}}{\Delta\nu_a}}$$

Standard HEMT amplifier



Helium cryostat cooling

$$T_n = 4 \text{ K} + T_{\text{amp}}$$



Benchmark Reach

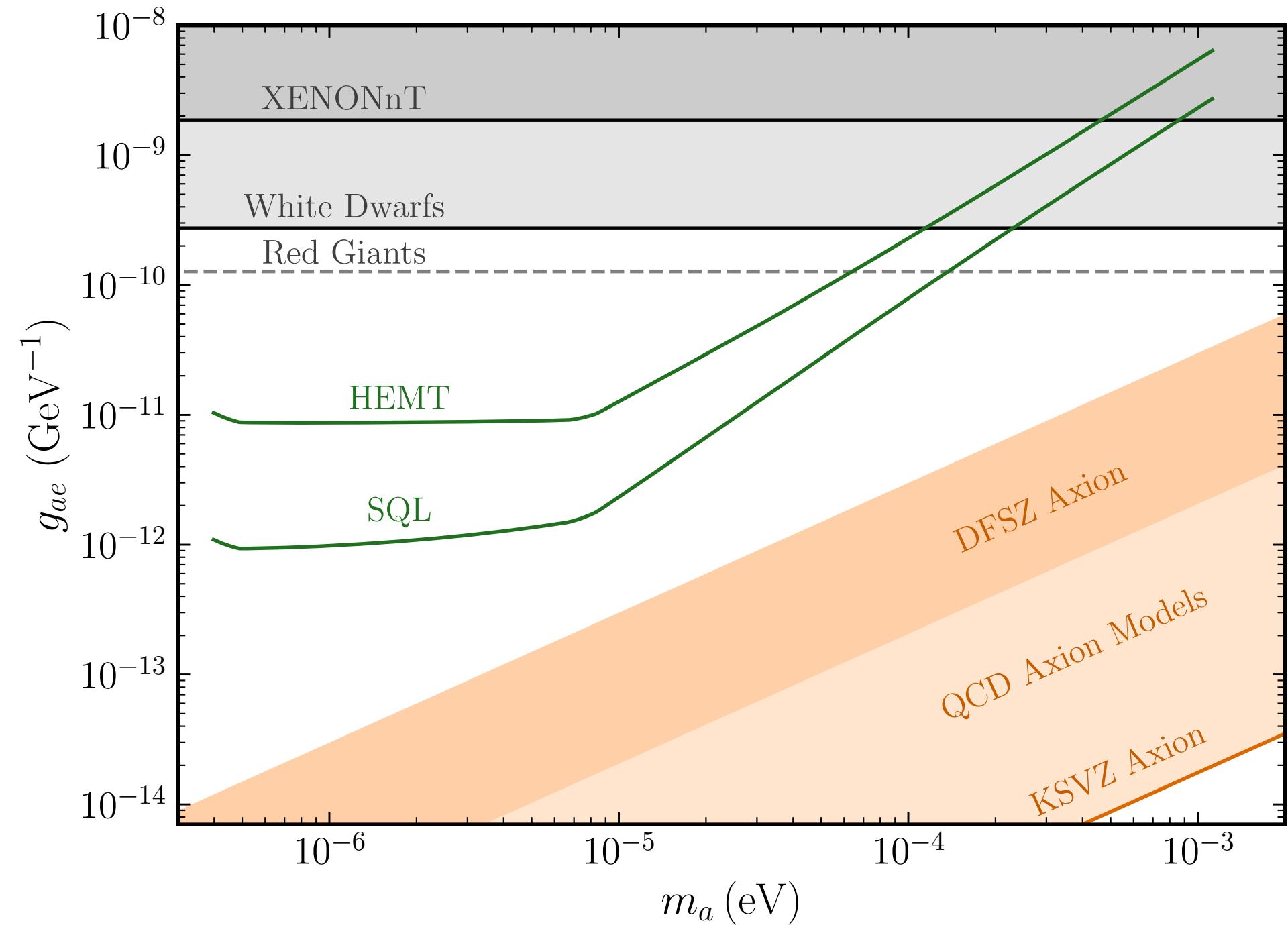
$$\text{SNR} \simeq \frac{P_{\text{sig}}}{T_n} \sqrt{\frac{t_{\text{int}}}{\Delta\nu_a}}$$

Standard quantum limited amplification

Dilution fridge cooling

$$T_n = 40 \text{ mK} + T_{\text{amp}}$$

More challenging, but realized in several expts



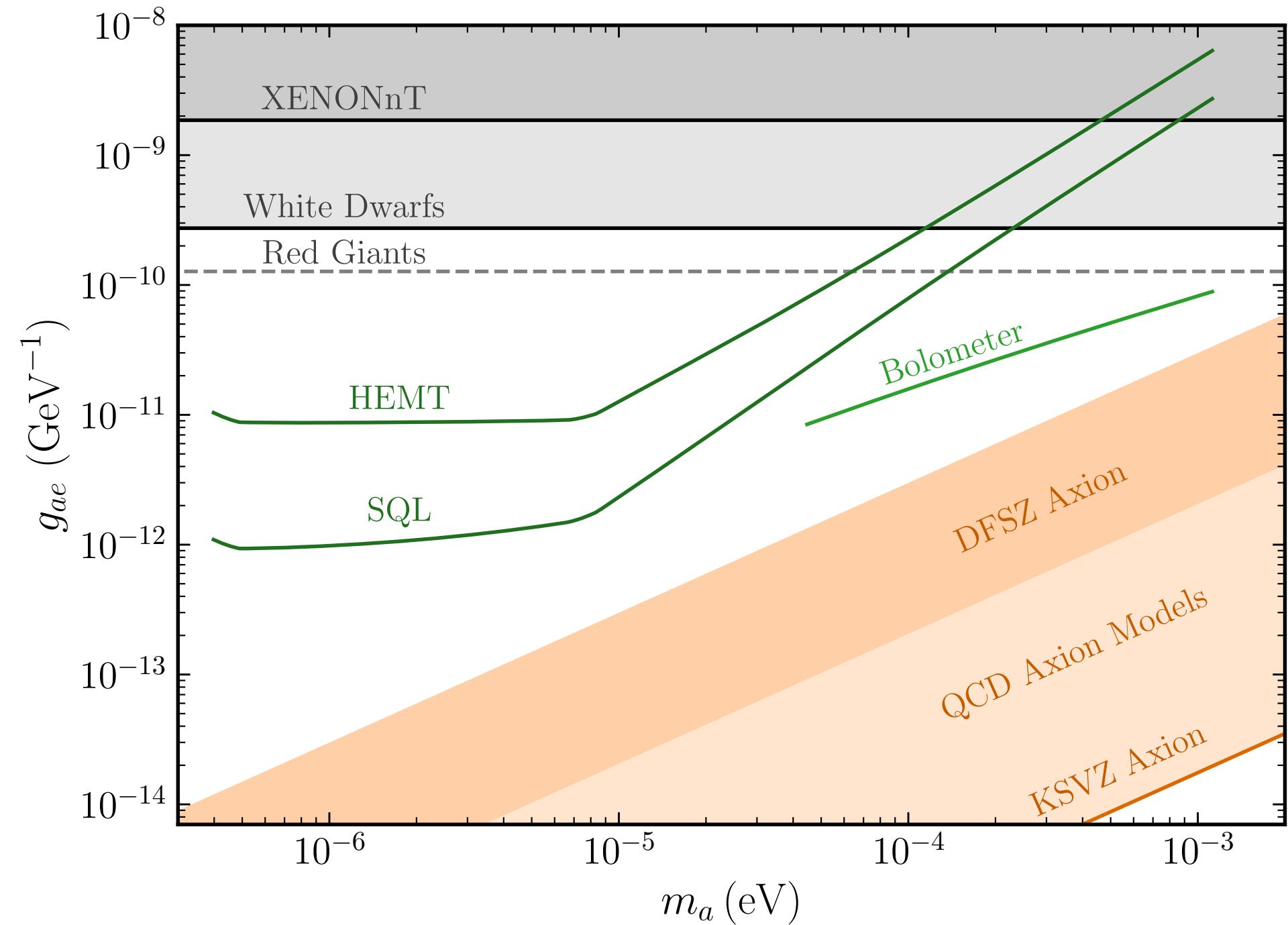
Benchmark Reach

$$\text{SNR} \simeq \frac{P_{\text{sig}} \sqrt{t_{\text{int}}}}{\text{NEP}}$$

Frequency insensitive
bolometer

$$\text{NEP} = 10^{-22} \text{ W}/\sqrt{\text{Hz}}$$

About 10x improvement
over state of the art;
target for BREAD



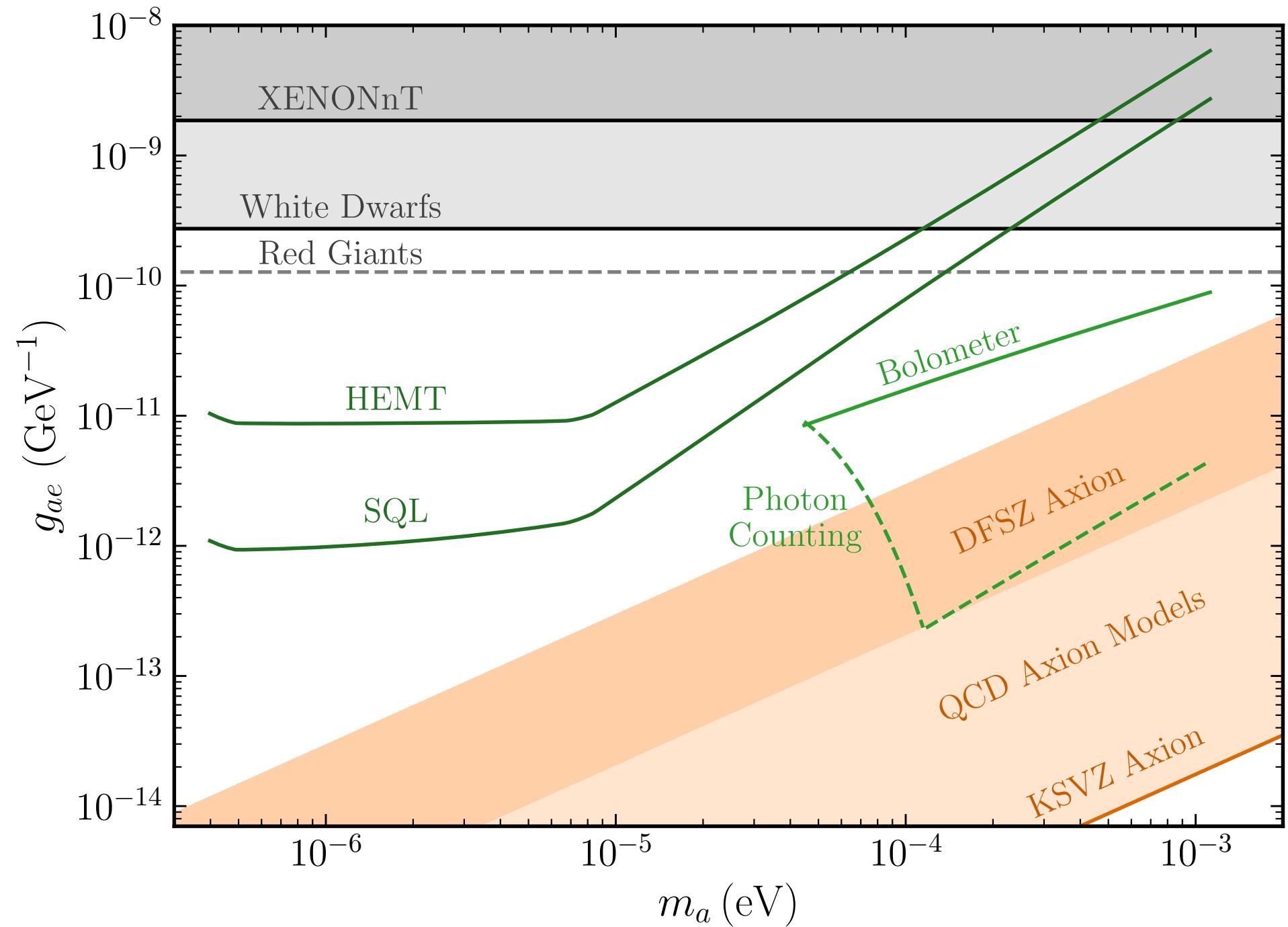
Benchmark Reach

$$\text{SNR} \simeq \frac{P_{\text{sig}}}{m_a} \sqrt{\frac{t_{\text{int}}}{\text{DCR}}}$$

Thermal limited
photon counting

$$\text{DCR} \sim \frac{\Delta\nu_s}{e^{m_a/T} - 1}$$

Challenging, but some
prototypes at meV,
with improving dark
count rates



Conclusion

- The axion is minimal and generic: promising search target
- Its physical effects are simple, but can be subtle to compute
- Experiments are moving forward with proven concepts, while new ideas may allow even stronger sensitivity

