Variable Importance Plots: An Introduction to the vip Package

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Abstract In the era of "big data", it is becoming more of a challenge to not only build state-of-the-art predictive models, but also gain an understanding of whats really going on in the data. For example, it is often of interest to know which, if any, of the predictors in a fitted model are relatively influential on the predicted outcome. Some modern algorithmslike random forests and gradient boosted decision treeshave a natural way of quantifying the importance or relative influence of each feature. Other algorithmslike naive Bayes classifiers and support vector machinesare not capable of doing so and model-agnostic approaches are generally used to measure each predictors importance. Enter **vip**, an R package for constructing variable importance scores/plots for many types of supervised learning algorithms using model-based and novel model-agnostic approaches. We'll also discuss a novel way to display both feature importance and feature effects together using sparklines.

TODO:

- Discuss layout of the package (e.g., vi() vs. vip() and workhorse functions like vi_permute().
- Discuss strengths/weaknesses of different approaches.
- Discuss other packages (like DALEX and iml).
- Discuss how PDP and ICE curve info is stored as an attribute whenever method = "pdp" or method = "ice", respectively.
- Should we discuss interaction detection? Probably...(the *H*-statistic example, if correct, is motivation enough).
- Need a good motivating example (e.g., airfoil example from arXiv paper using the SuperLearner package).
- Better discussion of function arguments, especially for permutation approach.
- Parallel examples for PDP-, ICE-, and permuataion-based approaches.
- Example showing how to supply your own custom metric function.
- Add note about permuting features in the train vs. test/new data and a reference to the IML book chapter where this is discussed further.

Introduction

Computing variable importance (VI) and communicating them through variable importance plots (VIPs) is fundamental to the problem of *interpretable machine learning*. TBD.

VI scores and VIPs are available in a number of packages. The **iml** package (Molnar et al., 2018) provides the FeatureImp() function which computes variable importance for general prediction models using the permutation approach. It is written in R6 (FIXME: Add refrence) and allows the user to specify a generic loss function or select from a pre-defined list (e.g., loss = "mse" for mean squared error). It also allows the user to specify whether importance is measures ad the difference or as the ratio of the original model error and the model error after permutation. The user can also specify the number of repitionions used when permuting each feature to help stabilize the variability in the procedure.

The DALEX package (Biecek, 2018) also provides permutation-based variable importance scores through the variable_importance() function. Similar to iml::FeatureImp(), this function allows the user to specify a loss function and how the importance scores are computed (e.g., using the difference or ratio). It also provides an option to sample the training data before shuffling the data to compute importance (the default is to use n_sample = 1000. This can help speed up computation.

The caret package (Kuhn, 2017b) includes a general varImp() function for computing model-specific and filter-based variable importance scores. Filter-based approaches, which are described in Kuhn and Johnson (2013), do not make use of the fitted model to measure VI. They also do not take into account the other predictors in the model. For regression problems, a popular approach to measuring the VI of a numeric predictor x is to first fit a flexible nonparametric model between x and the target Y; for example, the locally-weighted polynomial regression (LOWESS) method developed by Cleveland (1979). From this fit, a pseudo- R^2 measure can be obtained from the resulting residuals and used as a measure of VI. For categorical predictors, a different method based on standard statistical tests (e.g., t-tests and ANOVAs) can be employed; see Kuhn and Johnson (2013) for details. For

classification problems, an area under the ROC curve (AUC) statistic can be used to quantify predictor importance. The AUC statistic is computed by using the predictor x as input to the ROC curve. If x can reasonably separate the classes of Y, that is a clear indicator that x is an important predictor (in terms of class separation) and this is captured in the corresponding AUC statistic. For problems with more than two classes, extensions of the ROC curve or a one-vs-all approach can be used.

While the iml and DALEX packages provide model-agnostic approaces to computing variable importance, caret provides model-specific approaches (e.g., using the absolute value of the t-statistic for linear models) as well less accurate filter-based appraoches . Furthermore, each package has a completely different interface (e.g., iml is written in R6). The vip package (?) strives to provide a consistent interface to both model-specific and model-agnostic approaches to feature importance that is simple to use with three main functions:

- vi() computes VI scores using model-specific or model-agnostic approaces (the results are always returned as a tibble (Müller and Wickham, 2019));
- vip() computes VI scores using model-specific or model-agnostic approaces and allow flexible plotting of the results with ggplot2-type graphics (Wickham, 2016);
- add_sparklines() adds a novel sparkline representation of feature effects (e.g., partial dependence plots) to any VI table produced by vi().

There's also a function called vint() (for variable interactions) but is experimental and will not be discussed here. The interested reader is pointed to Greenwell et al. (2018).

Conbstructing VIPs in R

We'll illustrate major concepts using one of the regression problems described in Friedman (1991) and Breiman (1996):

$$Y_i = 10\sin(\pi X_{1i}X_{2i}) + 20(X_{3i} - 0.5)^2 + 10X_{4i} + 5X_{5i} + \epsilon_i, \quad i = 1, 2, \dots, n,$$
(1)

where $\epsilon_i \stackrel{iid}{\sim} N\left(0,\sigma^2\right)$. Data from this model can be generated using the mlbench.friedman1() function available in the mlbench package (Leisch and Dimitriadou, 2012). The inputs consist of 10 independent variables uniformly distributed on the interval [0,1]; however, only 5 out of these 10 are actually used in the true model. Outputs are created according to the formula described in ?mlbench.friedman1. The code chunk below simulates 500 observations from the model default standard deviation.

```
# Simulate training data
set.seed(101) # for reproducibility
trn <- as.data.frame(mlbench::mlbench.friedman1(500)) # ?mlbench.friedman1</pre>
# Inspect data
tibble::as_tibble(trn)
#> Warning: `as.tibble()` is deprecated, use `as_tibble()` (but mind the new semantics).
#> This warning is displayed once per session.
#> # A tibble: 500 x 11
#>
        x.1 x.2 x.3 x.4
                             x.5
                                      x.6 x.7 x.8 x.9 x.10
#>
      1 0.372 0.406 0.102 0.322 0.693 0.758 0.518 0.530 0.878 0.763 14.9
   2 0.0438 0.602 0.602 0.999 0.776 0.533 0.509 0.487 0.118 0.176 15.3
   3 0.710 0.362 0.254 0.548 0.0180 0.765 0.715 0.844 0.334 0.118 15.1
   4 0.658 0.291 0.542 0.327 0.230 0.301
                                         0.177 0.346 0.474 0.283 10.7
  5 0.250 0.794 0.383 0.947 0.462 0.00487 0.270 0.114 0.489 0.311 17.6
   6 0.300
           0.701 0.992 0.386 0.666 0.198 0.924 0.775 0.736 0.974 18.3
   7 0.585 0.365 0.283 0.488 0.845 0.466 0.715 0.202 0.905 0.640 14.6
#> 8 0.333 0.552 0.858 0.509 0.697 0.388 0.260 0.355 0.517 0.165 17.0
#> 9 0.622 0.118 0.490 0.390 0.468 0.360 0.572 0.891 0.682 0.717 8.54
#> 10 0.546 0.150 0.476 0.706 0.829 0.373 0.192 0.873 0.456 0.694 15.0
#> # with 490 more rows
```

For these data, it should be clear that features X_1 – X_5 are the most important! (The others don't influence Y at all.)

Model-specific VI

Some machine learning algorithms have their own way of quantifying variable Importance. We describe some of these in the subsection that follow. The issue with model-specific VI scores is that they are not necessarily comparable across different types of models. For example, directly computing the impurity-based VI scores from tree-based models to the -statistic from linear models.

Trees and tree ensembles

Decision trees probably offer the most natural model-based approach to quantifying the importance of each feature. In a binary decision tree, at each node, a single predictor is used to partition the data into two homogeneous groups. The chosen predictor is the one that maximizes some measure of improvement. The relative importance of predictor is the sum of the squared improvements over all internal nodes of the tree for which was chosen as the partitioning variable; see Breiman, Friedman, and Charles J. Stone (1984) for details. This idea also extends to ensembles of decision trees, such as RFs and GBMs. In ensembles, the improvement score for each predictor is averaged across all the trees in the ensemble. Fortunately, due to the stabilizing effect of averaging, the improvement-based VI metric is often more reliable in large ensembles (see Hastie, Tibshirani, and Friedman 2009, pg. 368). RFs offer an additional method for computing VI scores. The idea is to use the leftover out-of-bag (OOB) data to construct validation-set errors for each tree. Then, each predictor is randomly shuffled in the OOB data and the error is computed again. The idea is that if variable is important, then the validation error will go up when is perturbed in the OOB data. The difference in the two errors is recorded for the OOB data then averaged across all trees in the forest.

To illustrate, we fit a CART-like regression tree, RF, and GBM to the simulated training data. (Note: there are a number of different packages available for fitting these types of models, we just picked popular and efficient implementations for illustration.)

```
# Load required packages
library(rpart) # for fitting CART-like decision trees
library(randomForest) # for fitting random forests
library(xgboost)
                   # for fitting GBMs
# Fit a single regression tree
tree <- rpart(y \sim ., data = trn)
# Fit a random forest
set.seed(101)
rfo <- randomForest(y ~ ., data = trn, importance = TRUE)</pre>
# Fit a GBM
set.seed(102)
bst <- xgboost(</pre>
  data = data.matrix(subset(trn, select = -y)),
  label = trn$y,
  objective = "reg:linear",
  nrounds = 100,
  max_depth = 5,
  eta = 0.3,
  verbose = 0 # suppress printing
)
```

Each of the above packages include the ability to compute VI scores for all the features in the model; however, the implementation is rather package specific, as shown in the code chunk below. The results are displayed in Figure 1.

```
# Extract VI scores from each model
vi_tree <- tree$variable.importance
vi_rfo <- rfo$variable.importance
vi_bst <- xgb.importance(model = bst)</pre>
```

As we would expect, all three methods rank the variables x.1-x.5 as more important than the others. While this is good news, it is unfortunate that we have to remember the different functions and ways of extracting and plotting VI scores from various model fitting functions. This is where vip (?) can help...one function to rule them all! Once vip is loaded, we can use vi() to extract a tibble of VI scores.

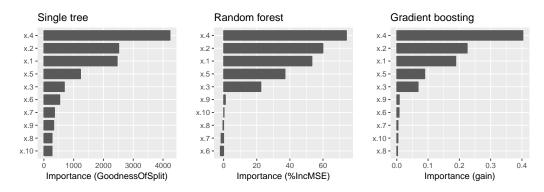


Figure 1: Model-based VIPs for the three different tree-based models fit to the simulated Friedman data..

library(vip)

```
vi(tree) # CART-like decision tree
#> # A tibble: 10 x 2
#>
      Variable Importance
#>
      <chr>
                    <dbl>
#>
   1 x.4
                    4234.
#>
                    2513.
   2 x.2
#>
   3 x.1
                    2461.
#>
   4 x.5
                    1230.
#>
   5 x.3
                     688.
#>
                     533.
    6 x.6
#>
   7 x.7
                     357.
#>
   8 x.9
                     331.
#> 9 x.8
                     276.
#> 10 x.10
                     275.
vi(rfo) # RF
#> # A tibble: 10 x 2
#>
      Variable Importance
#>
      <chr>
                   <dbl>
                   74.2
  1 x.4
#> 2 x.2
                   59.9
#> 3 x.1
                   53.3
#> 4 x.5
                   37.1
#> 5 x.3
                   22.5
#> 6 x.9
                    1.05
#> 7 x.10
                    0.254
#> 8 x.8
                   -0.408
#> 9 x.7
                   -1.56
#> 10 x.6
                   -2.00
vi(bst) # GBM
#> # A tibble: 10 x 2
#>
      Variable Importance
#>
      <chr>
                   <dbl>
  1 x.4
#>
                  0.403
  2 x.2
                  0.225
#>
#>
   3 x.1
                  0.189
#>
  4 x.5
                  0.0894
#> 5 x.3
                  0.0682
#> 6 x.9
                  0.00802
#> 7 x.6
                  0.00746
#> 8 x.7
                  0.00400
#> 9 x.10
                  0.00377
#> 10 x.8
                  0.00262
```

Notice how the vi() function always returns a tibble with two columns: Variable and Importance.

Also, by default, vi() always orders the VI scores from highest to lowest; this, among other options, can be controlled by the user (see ?vip::vi for details). Plotting VI scores with vip() is just as straightforward. For example, the following code can be used to reproduce Figure 1.

```
p1 <- vip(tree) + ggtitle("Single tree")
p2 <- vip(rfo) + ggtitle("Random forest")
p3 <- vip(bst) + ggtitle("Gradient boosting")
# Figure 1
grid.arrange(p1, p2, p3, nrow = 1)</pre>
```

Notice how the vip() function always returns a "ggplot" object (by default, this will be a bar plot). For large models with many features, a dot plot is more effective (in fact, a number of useful plotting options can be fiddles with). Below we call vip() and change a few useful options (the resulting plot is displayed in Figure 2).

```
# Load required packages
library(ggplot2) # for theme_light() function

vip(bst, num_features = 5, bar = FALSE, color, horizontal = FALSE,
    color = "red", shape = 17, size = 4) +
   theme_light()
```

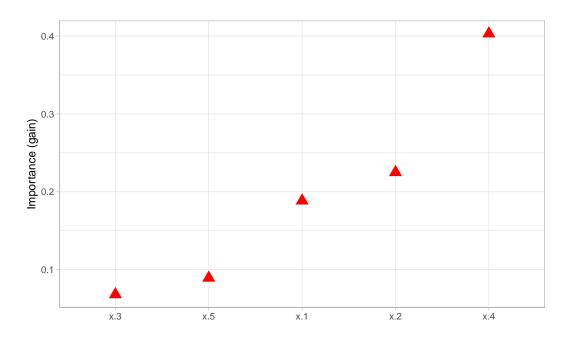


Figure 2: Illustrating various options available in vip().

Linear models

In multiple linear regression, or linear models (LMs), the absolute value of the t-statistic (or some other scaled variant of the estimated coefficients) is commonly used as a measure of VI. The same idea also extends to generalized linear models (GLMs). In the code chunk below, we fit an LM to the simulated trn data set allowing for all main and two-way interaction effects, then use the step() function to perform backward elimination. The resulting VIP is displayed in Figure 3.

```
# Fit a LM
linmod <- lm(y ~ .^2, data = trn)
backward <- step(linmod, direction = "backward", trace = 0)
# Extract VI scores
vi(backward)
#> # A tibble: 21 x 3
```

```
#>
     Variable Importance Sign
#>
     <chr>
                   <dbl> <chr>
                   14.2 POS
  1 x.4
#>
#> 2 x.2
                   7.31 POS
#> 3 x.1
                   5.63 POS
#> 4 x.5
                   5.21 POS
#> 5 x.3:x.5
                   2.46 POS
#> 6 x.1:x.10
                   2.41 NEG
  7 x.2:x.6
                    2.41 NEG
#> 8 x.1:x.5
                    2.37 NEG
#> 9 x.10
                    2.21 POS
#> 10 x.3:x.4
                    2.01 NEG
#> # with 11 more rows
# Plot VI scores
vip(backward, num_features = length(coef(backward)),
   bar = FALSE, horizontal = FALSE)
```

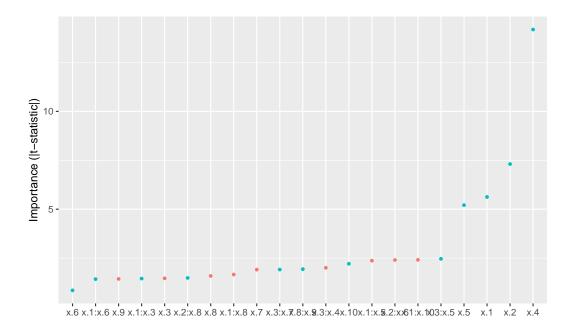


Figure 3: Example VIP from a linear model fit to the simulated Friedman data.

One issue with computing VI scores for LMs using the *t*-statistic approach is that a score is assigned to each term in the model, rather than to just each feature! We can solve this problem using one of the model-agnostic approaches discussed later.

Multivariate adaptive regression splines (MARS), which were introduced in Friedman (1991), is an automatic regression technique which can be seen as a generalization of multiple linear regression and generalized linear models. In the MARS algorithm, the contribution (or VI score) for each predictor is determined using a generalized cross-validation (GCV) statistic. An example using the earth package (Milborrow, 2017) is given below (the results are plotted in Figure 5):

```
#> 1 x.4
                    100
#>
   2 x.1
                     83.2
#>
                     83.2
  3 x.2
#> 4 x.5
                     59.3
#> 5 x.3
                     43.5
#> 6 x.6
                      0
#> 7 x.7
                      0
#> 8 x.8
                      0
#> 9 x.9
                      0
#> 10 x.10
# Plot VI scores
vip(mars)
```

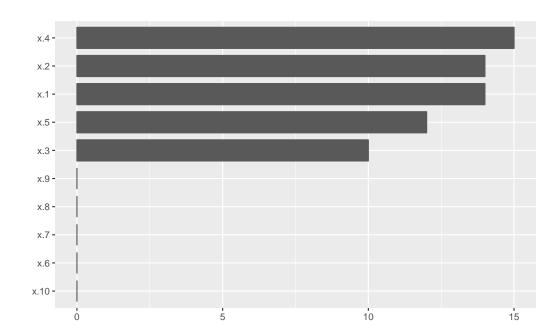


Figure 4: Example VIP from a MARS model fit to the simulated Friedman data.

Importance (nsubsets)

Neural networks

For neural netwroks (NNs), two popular methods for constructing VI scores are the Garson algorithm (Garson, 1991), later modified by Goh (1995), and the Olden algorithm (Olden et al., 2004). For both algorithms, the basis of these importance scores is the networks connection weights. The Garson algorithm determines VI by identifying all weighted connections between the nodes of interest. Oldens algorithm, on the other hand, uses the product of the raw connection weights between each input and output neuron and sums the product across all hidden neurons. This has been shown to outperform the Garson method in various simulations. For DNNs, a similar method due to Gedeon (1997) considers the weights connecting the input features to the first two hidden layers (for simplicity and speed); but this method can be slow for large networks. We illustrate these two methods below using vip() with the nnet package (Venables and Ripley, 2002) (see the results in Figure ??).

```
# Load required packages
library(nnet)

# Fit a neural network
set.seed(0803)
nn <- nnet(y ~ ., data = trn, size = 7, decay = 0.1, linout = TRUE)

# VIPs
p1 <- vip(nn, method = "garson")
p2 <- vip(nn, method = "olsen")</pre>
```

```
# Figure X
grid.arrange(p1, p2, nrow = 1)
```

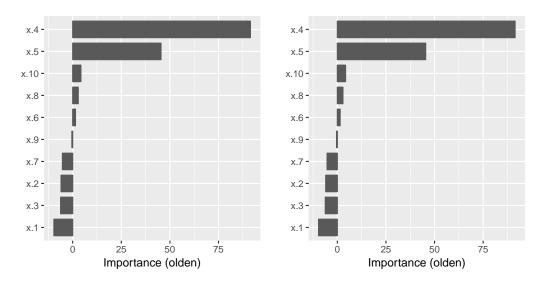


Figure 5: Example VIPs from a single-hidden-layer NN fit to the simulated Friedman data.

Model-agnostic VI

Model-agnostic interpredibility separates interpretation from the model. Compared to model-specific approaches, model-agnostic VI methods are more flexible (since they can be applied to any supervised learning algorithm). In this section, we discuss model-agnostic methods for quantifying global feature importance using three different approaches: 1) partial dependence plots (PDPs), 2) individual conditional expectation (ICE) curves, and 3) permutation-based feature importance. For details on approaches 1)–2), see Greenwell et al. (2018).

Our first model-agnostic approach is based on quantifying the "flatness" of the PDPs of each feature. PDPs help visualize the effect of low cardinality subsets of the feature space on the estimated prediction surface (e.g., main effects and two/three-way interaction effects.). PDPs provide model-agnostic interpretations and can be constructed in the same way for any supervised learning algorithm; for an overview, see Greenwell (2017). Below, we fit a projection pursuit regression (PPR) model and construct PDPs for each feature using the pdp package Greenwell (2017). The results are displayed in Figure 6. Notice how the PDPs for the uninformative features are relatively flat compared to the PDPs for features x . 1–x . 2!

```
# Load required packages
library(pdp)

# Fit a PPR model (nterms was chosen using the caret package with 5 repeats of
# 5-fold cross-validation)
pp <- ppr(y ~ ., data = trn, nterms = 11)

# PDPs for all 10 features
features <- paste0("x.", 1:10)
pdps <- lapply(features, FUN = function(feature) {
   pd <- partial(pp, pred.var = feature)
    autoplot(pd) +
     ylim(range(trn$y)) +
     theme_light()
})
grid.arrange(grobs = pdps, ncol = 5)</pre>
```

Next, we compute PDP-based VI scores for the PPR and NN models. The PDP method constructs VI scores that quantify the "flatness" of each PDP (by default, this is defined by computing the standard deviation of the y-axis values for each PDP). To use the PDP method, specify method = "pdp" in the call to vi() or vip():

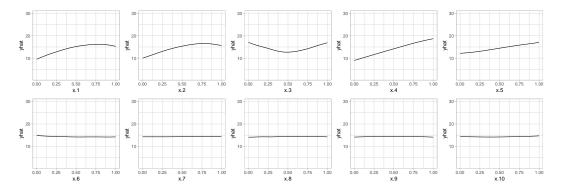


Figure 6: PDPs of main effects in the PPR model fit to the simulated Friedman data..

```
# Fit a PPR model (nterms was chosen using the caret package with 5 repeats of
# 5-fold cross-validation)
pp <- ppr(y ~ ., data = trn, nterms = 11)

# Plot VI scores
p1 <- vip(pp, method = "pdp") + ggtitle("PPR")
p2 <- vip(nn, method = "pdp") + ggtitle("NN")

# Figure X
grid.arrange(p1, p2, ncol = 2)</pre>
```

In Figure ?? we display the PDP-based feature improtance for the previously obtained PPR and NN models. These VI scores essentially capture the variability in the partial dependence values for each main effect.

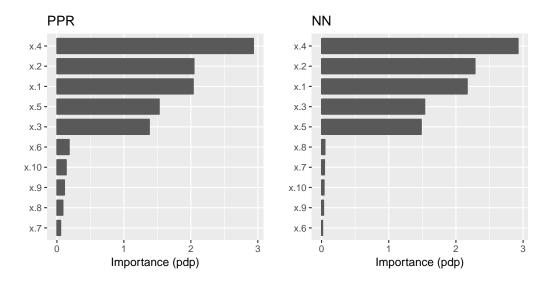


Figure 7: PDP-based feature importance for the PPR and NN models fit to the simulated Friedman data..

ICE curve method

The ICE curve method is similar to the PDP method. The only difference is that we measure the "flatness" of each ICE curve and then aggregate the results (e.g., by averaging). If there are no (substantial) interaction effects, using method = "ice" will produce results similar to using method = "pdp". However, if strong interaction effects are present, they can obfuscate the main effects and render the PDP-based approach less useful (since the PDPs for important features can be relatively flat when certain interactions are present; see Goldstein et al. (2015) for details). In fact, it is probably safest to always use method = "ice".

Below, we display the ICE curves for each feature in the PP model using the same y-axis scale; see

Figure 8. Again, there is a clear difference between the ICE curves for features x.1-x.5 and x.6-x.10; the later being relatively flat by comparison. Also, notice how the ICE curves within each feature are relatively parallel (if the ICE curves within each feature were perfectly parallel, the standard deviation for each curve would be the same and the results will be identical to the PDP method). In this example, the interaction term between x.1 and x.2 does not obfuscate the PDPs for the main effects and the results are not much different.

```
# ICE curves for all 10 features
ice_curves <- lapply(features, FUN = function(feature) {
  ice <- partial(pp, pred.var = feature, ice = TRUE)
  autoplot(ice, alpha = 0.1) +
    ylim(range(trn$y)) +
    theme_light()
})

# Figure X
grid.arrange(grobs = ice_curves, ncol = 5)</pre>
```

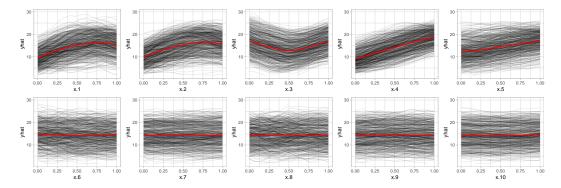


Figure 8: ICE curves for each feature in the PPR model fit to the simulated Friedman data. The red curve represents the PDP (i.e., the averaged ICE curves).

Obtaining the ICE-based feature importance scores is also straightforward. The results in Figure 9 are similar to those obtained using the PDP method.

```
# Plot VI scores
p1 <- vip(pp, method = "ice") + ggtitle("PPR")
p2 <- vip(nn, method = "ice") + ggtitle("NN")
# Figure X
grid.arrange(p1, p2, ncol = 2)</pre>
```

Permutation method

The permutation method exists in various forms and was made popular in Breiman (2001) for random forests. The permutation approach used in **vip** is quite simple. The idea is that if we randomly permute thse values of an important feature in the training data, the training performance would degrade (since permuting the values of a feature effectively destroys any relationship between that feature and the target variable). This of course assumes that the model has been properly tuned (e.g., using cross-validation) and is not over fitting. The permutation approach uses the difference between some baseline performance measure (e.g., training R^2 , AUC, or RMSE) and the same performance measure obtained after permuting the values of a particular feature in the training data (**Note:** the model is NOT refit to the training data after randomly permuting the values of a feature). To use the permutation approach, specify method = "permute" in the call to vi() or vip(). Note that using method = "permute" requires specifying a few additional arguments; see ?vi_permute for details.

An example is given below for the previously fitted PPR and NN models. The result, which are displayed in Figure 10, agree with those obtained using the PDP- and ICE-based methods.

```
# Plot VI scores
set.seed(2021) # for reproducibility
p1 <- vip(pp, method = "permute", target = "y", metric = "rsquared",</pre>
```

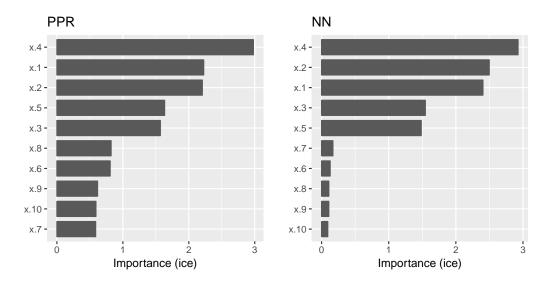


Figure 9: ICE-based feature importance for the PPR and NN models fit to the simulated Friedman data..

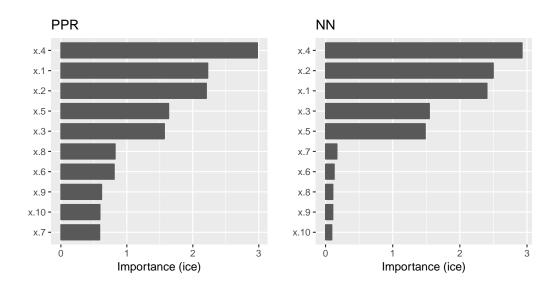


Figure 10: Permutation-based feature importance for the PPR and NN models fit to the simulated Friedman data...

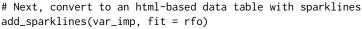
The permutation approach introduces randomness into the procedure and therefore should be run more than once if computationally feasible. Fortunately, this also allows us to compute standard errors for the estimated feature importance, as illustrated in the example below where we specify 'nsim = 10' to request that each feature be permuted 10 times and the results averaged together.

```
# A tibble: 10 x 3
#>
     Variable Importance
                            StDev
#>
      <chr>
                   <dbl>
                            <dbl>
#>
  1 x.4
                   0.586 0.0188
#> 2 x.2
                  0.416 0.0184
                  0.377
#>
   3 x.1
                         0.0162
                   0.222 0.0155
   4 x.5
```

Use sparklines to characterize feature effects

Starting with **vip** 0.1.3, we have included a new function add_sparklines() for constructing HTML-based feature importance tables. The primary difference between vi() and add_sparklines() is that the latter includes an Effect column that displays a sparkline representation of the partial dependence function for each feature. This is a concise way to display both feature importance and feature effect information in a single table. See ?vip::add_sparklines for details. We illustrate the basic use of add_sparklines() in the code chunks below.

```
# First, compute a tibble of variable importance scores using any method
var_imp <- vi(rfo, method = "permute", metric = "rmse", target = "y")
# Next convert to an html-based data table with sparklines</pre>
```



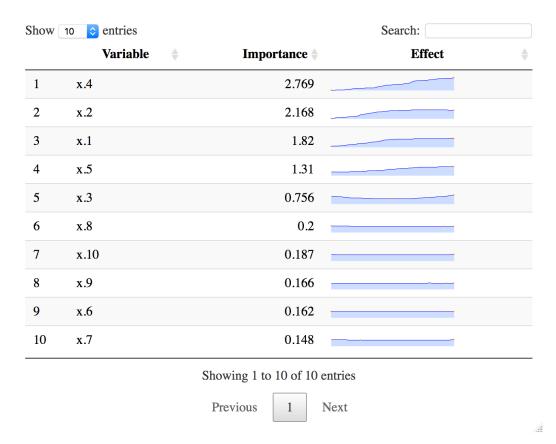


Figure 11: VIP with sparkline representation of feature effects fit to the simulated Friedman data.

Predict the sale price for a home

For illustration, we'll use the Ames housing data set—a more contemporary version of the often cited Boston Housing data set. These data are available in the **AmesHousing** package (Kuhn, 2017a).

To speed up the process, we perform the computations in parallel using...

```
# Load the Ames housing data
ames <- AmesHousing::make_ames()</pre>
```

```
X <- subset(ames, select = -Sale_Price)</pre>
y <- ames$Sale_Price
# Load required packages
library(SuperLearner)
# Stack models
set.seed(840)
ctrl <- SuperLearner.CV.control(V = 5L, shuffle = TRUE)</pre>
sl <- SuperLearner(Y = y, X = X, SL.library = learners, verbose = TRUE,</pre>
                    cvControl = ctrl)
sl
# Prediction wrapper functions
imp_fun <- function(object, newdata) {</pre>
  predict(object, newdata = newdata)$pred
par_fun <- function(object, newdata) {</pre>
  mean(predict(object, newdata = newdata)$pred)
# Setup parallel backend
library(doParallel) # load the parallel backend
cl <- makeCluster(5) # use 5 workers</pre>
registerDoParallel(cl) # register the parallel backend
# Permutation-based feature importance
set.seed(278)
var_imp <- vi(sl, method = "permute", train = X, target = y, metric = "rmse",</pre>
              pred_wrapper = imp_fun, nsim = 5, parallel = TRUE)
# Add sparline representation of feature effects
add_sparklines(var_imp[1L:10L, ], fit = sl, pred.fun = par_fun, train = X,
               digits = 2, verbose = TRUE, trim.outliers = TRUE,
               grid.resolution = 20, parallel = TRUE)
```

Summary

TBD.

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Show (10 \$ entries		Search:	
	Variable	♦ Importance	♦ StDev	Effect
1	Gr_Liv_Area	24746.03	558.96	
2	Total_Bsmt_SF	14196.22	218.70	
3	Year_Built	12140.76	236.92	
4	Overall_Qual	9111.40	118.94	
5	Year_Remod_Add	7481.20	238.79	
6	Garage_Cars	5716.48	320.30	
7	Lot_Area	4842.86	171.66	
8	Mas_Vnr_Type	4246.83	412.73	=
9	Bsmt_Unf_SF	3722.94	156.61	
10	Latitude	3195.60	213.94	



Figure 12: VIP with sparkline representation of feature effects for the top ten features from a Super Learner fit to the Ames housing data.

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