

ECE4122: Advanced Electromagnetics  
Assignment S2 2018

**Q1. Plan wave (marks 75)**

An  $x$  Hz ground penetration radar obliquely incidents a randomly polarized UPW at the Brewster's angle from air ( $z < 0$ ) onto the soil. Assume the soil is lossless, nonmagnetic material with  $\epsilon_r = 20$  ( $z > 0$ ). The wave can be decomposed into equal TE and TM parts, each with an incident electric field amplitude of  $A$  (V/m).

Calculate (i) the Brewster's angle; (5 marks) (ii) the phase constants  $\beta_1$  and  $\beta_2$  in (rad/m) for air and soil, respectively, (5 marks) (iii) the intrinsic wave impedances  $\eta_1$  and  $\eta_2$  for air and soil, respectively, (5 marks) (iv) the angle of transmission,  $\theta_t$  in (deg), (5 marks) (v) the TE polarised reflection coefficient,  $\Gamma_{TE}$ ; (5 marks) (vi) the time domain expressions of TE polarised incident, reflected and transmitted electric fields in (V/m), (15 marks) (vii) the reflection coefficient for TM polarised oblique incidence fields, (5 marks) (viii) the incident, reflected and transmitted electric fields for TM polarisation, (15 marks) and finally, (ix) find the time domain expressions of the incident, reflected and transmitted randomly polarized electric fields. (15 marks)

Rule:  $x = \text{your student number in Hz}$ ;

$A = 1^{st} \text{ two digits of your student number,}$

*if 1<sup>st</sup> digit is zero then  $A = 2^{nd}$  two digits of your student number*

Hints: Calculate the Brewster's angle first. Then calculate incident, reflected and transmitted electric fields for both TE and TM. Finally combine the respective fields to get resultant field expressions.

**Q2. Terminated transmission line and impedance matching (marks 75)**

A microstrip patch is to be designed at 2.2 GHz for PCS (personal **communications** service) digital cellular system for better mobility than conventional mobilephones. The input impedance of the patch antenna is  $Z_A = R_A + jX_A(\Omega)$  at 2.2 GHz. The antenna needs to be matched to a  $50 \Omega$  impedance T-Line.

(a) Calculate the complex reflection coefficient of the antenna (15 marks)

(b) Design an open circuit stub matching network to match the antenna with the T-line on FR4 board with  $\epsilon_r = 4.2$ . Choose the solutions that minimise: (i) the length of the through line and (ii) the length of the open circuited stub

(i) Through line length in (mm) and Open circuit stub length (mm) (30 marks)

(ii) Through line length in (mm) and Open circuit stub length (mm) (30 marks)

Rule:  $R_A = 1^{st}3 - \text{digit of your student number} \div 2 \ (\Omega)$ ; if first digit is zero, select next 3-digit of your student number  $(\Omega)$ ;

$X_A = 1^{st}3 - \text{digit of your student number} \div 1.5 \ (\Omega)$ ; if first digit is zero, select next 3-digit of your student number  $\div 1.5 \ (\Omega)$ ;