

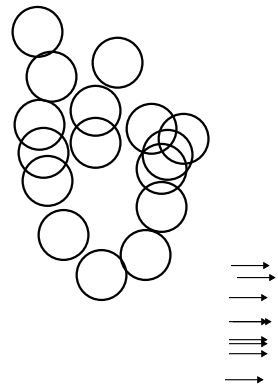
determines the byproduct of each reaction, specifically if strain i consumes resource β then $D_{i\alpha\beta}$ is the fraction of the leaked energy of that reaction that produces resource α

Resource abundance

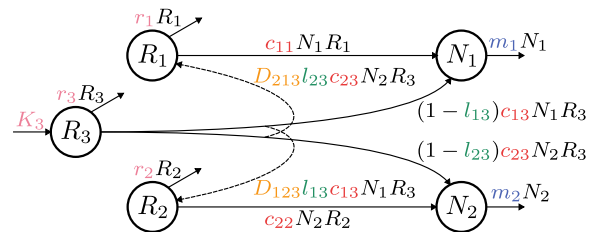
$$\frac{\partial R_\alpha}{\partial t} = \overset{\text{external supply rate}}{K_\alpha} - \overset{\text{dilution rate}}{r_\alpha} R_\alpha - \sum_i \underbrace{\frac{N_i c_{i\alpha} R_\alpha}{\text{total consumption of } \alpha \text{ by species } i}}_{\text{consumption rate by an } i \text{ individual per unit of } \alpha} + \sum_{i,\beta} \underbrace{\frac{w_\beta}{w_\alpha} D_{i\alpha\beta}}_{\substack{\text{conversion from } \alpha \text{ to } \beta \\ \text{from } \alpha \text{ to } \beta \\ \text{of } \beta \text{ to } \alpha \text{ by } i}} \underbrace{\frac{N_i c_{i\beta} R_\beta}{\text{total consumption of } \beta \text{ by species } i}}_{\text{leakage of } \beta \text{ by } i} + \underbrace{D_{R_\alpha}}_{\substack{\text{contribution to } \alpha \text{ due to} \\ \text{conversion from leaked resources}}} \nabla^2 R_\alpha$$

Species abundance

$$\frac{\partial N_i}{\partial t} = N_i \left(\underbrace{g_i}_{\substack{\text{conversion from} \\ \text{energy to cell}}} \underbrace{\sum_\alpha \frac{w_\alpha (1 - l_{i\alpha}) c_{i\alpha} R_\alpha}{\text{energy/fmole}}}_{\substack{\text{retained} \\ \text{energy/cell/hr}}} - \underbrace{m_i}_{\substack{\text{cell upkeep energy} \\ \text{consumption - in E/T/cell}}} \right) + \underbrace{D_{N_i}}_{\text{diffusion constants}} \nabla^2 N_i$$



Simple example showing crossfeeding (cosmo)



General diagram

