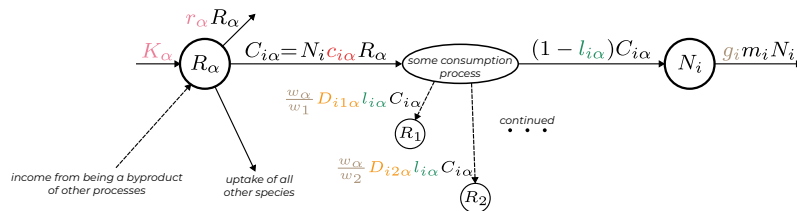


**i** always refers to different species  
**a** and **b** to resources

$$\begin{aligned}
 \text{resource concentrations } \frac{\partial R_\alpha}{\partial t} &= \underbrace{K_\alpha}_{\text{external supply}} - \underbrace{r_\alpha R_\alpha}_{\text{dilution rates}} - \underbrace{\sum_i \frac{N_i c_{i\alpha} R_\alpha}{\text{total consumption of a by i}}}_{\text{consumption rate of a by i, per unit concentrations of both}} + \sum_{i,\beta} \frac{w_\beta}{w_\alpha} \underbrace{D_{i\alpha\beta}}_{\text{determines the byproducts created when i consumes b}} \underbrace{l_{i\beta}}_{\text{total leakage of b when consumed by i}} \underbrace{N_i c_{i\beta} R_\beta}_{\text{total leakage of b when consumed by i}} + \underbrace{D_{R_\alpha}}_{\text{diffusion constants}} \nabla^2 R_\alpha \\
 \text{species concentrations } \frac{\partial N_i}{\partial t} &= \underbrace{g_i}_{\text{unit conversion factors}} N_i \left( \sum_\alpha (1 - l_{i\alpha}) \underbrace{w_\alpha c_{i\alpha} R_\alpha}_{\text{cell upkeep energy consumption}} - \underbrace{m_i}_{\text{diffusion constants}} \right) + \underbrace{D_{N_i}}_{\text{diffusion constants}} \nabla^2 N_i
 \end{aligned}$$

## Consumption with byproducts diagram



Note for Wenying: should I instead replace the bigger expressions above with  $\sum_\alpha D_{i1\alpha} l_{i\alpha} C_{i\alpha}$