

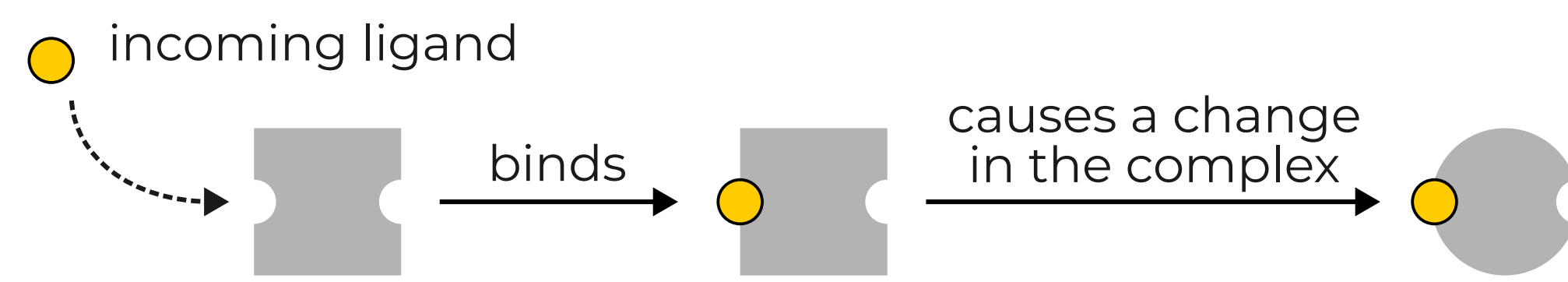
Functional dynamics in out-of-equilibrium allosteric assemblies

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Allostery is the communication between distant sites of a macromolecule, such as binding sites on a protein



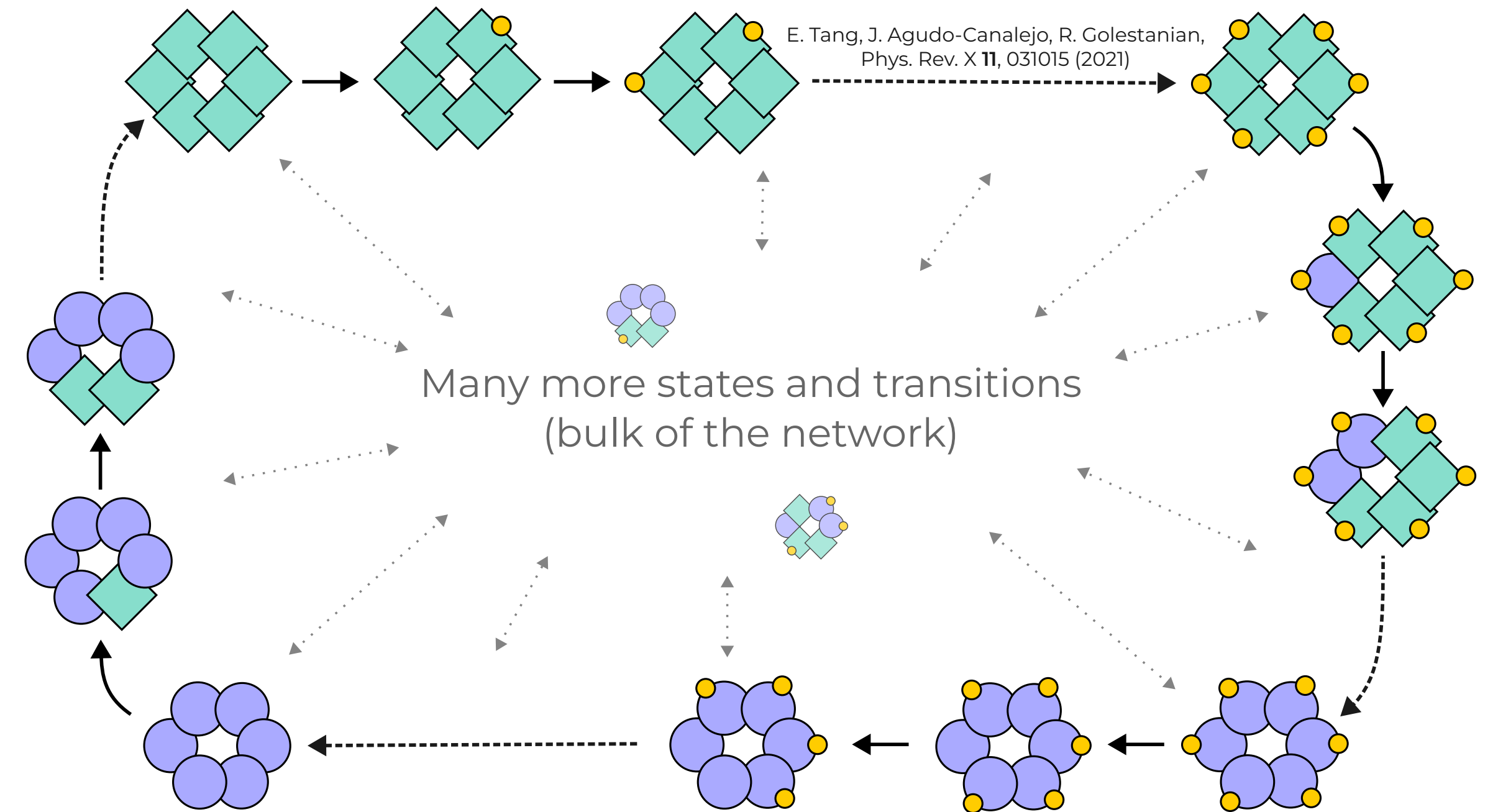
Equilibrium allostery

- MWC, KNF and the comprehensive Ensemble Allostery Model
- Cooperative binding, allosteric regulation/signalling

But there are **out-of-equilibrium** allosteric complexes such as AAA ATPases (e.g. cyanobacterial circadian clock KaiC or the DNA clamp loader)

What new behaviour is possible out of equilibrium?

- Dynamic steady states
- Oscillations (such as in KaiC or other circadian clocks)
- Sensitivity to initial conditions (memory/spontaneous symmetry breaking)
- Dimensionality reduction (constraining the dynamics to part of the state space)
- Topologically protected states
- Modified cooperative binding



We build models to identify classes of behaviour in biology and guide synthetic designs

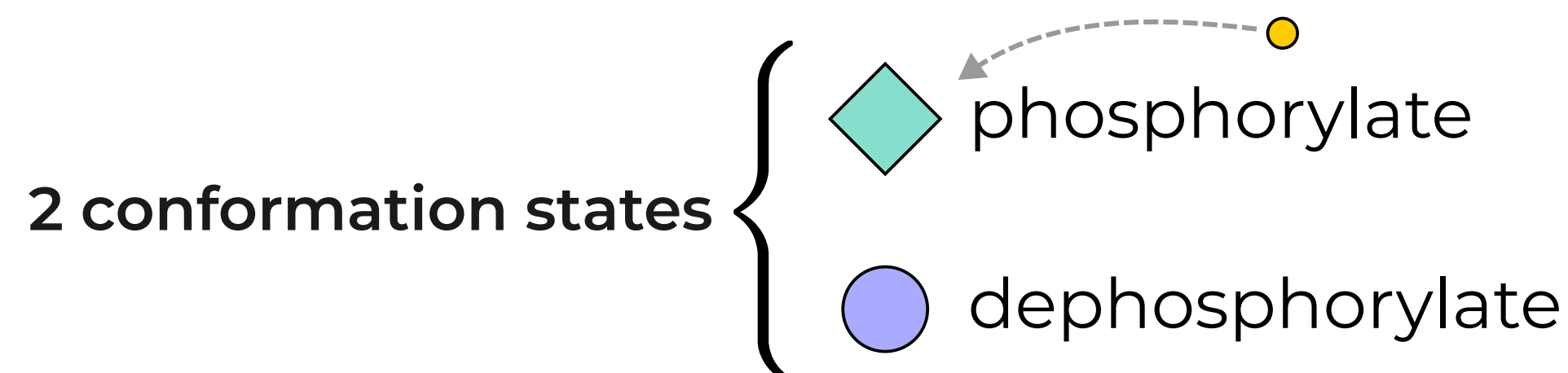
- Models with **identical subunits** (polymer like)
- Statistical physics and graph theory methods
- **Local (nearest-neighbour) interactions**
- **Thermodynamically consistent** transitions between system states (satisfying local detailed balance)

$$\text{system} + R_1 + \dots \xrightleftharpoons[r_b]{r_f} \text{changed system} + P_1 + \dots$$

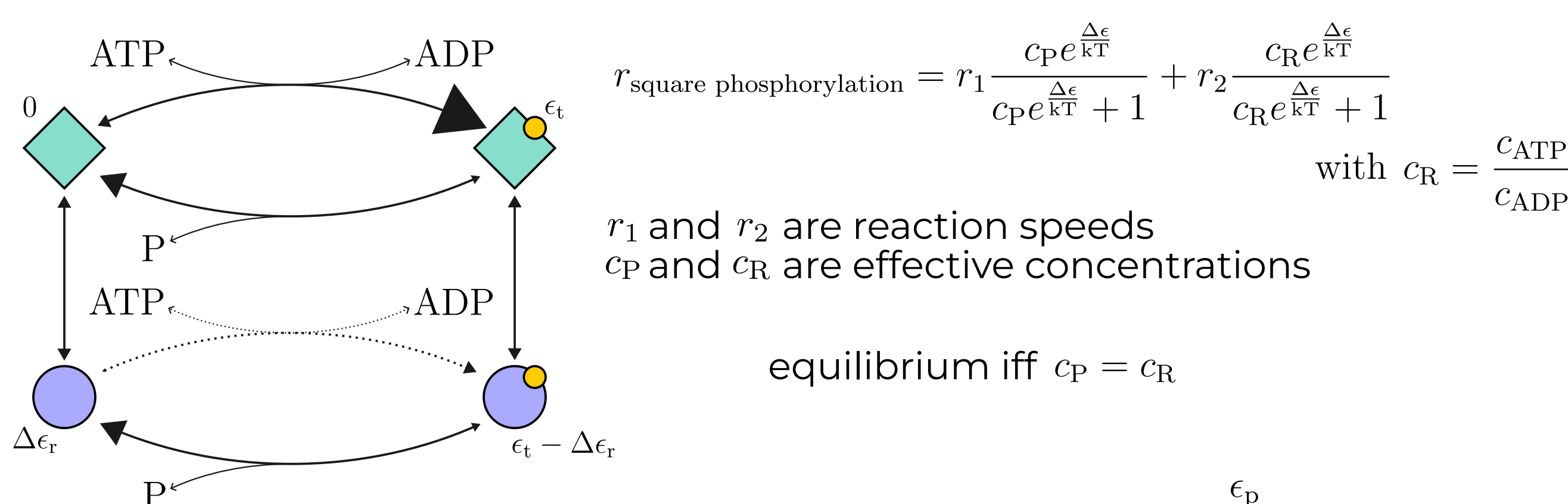
$$\frac{r_f}{r_b} = \exp((\Delta\epsilon + \mu_{R_1} + \dots - \mu_{P_1} - \dots)/kT)$$

change in system energy chemical potentials of all reactants and products

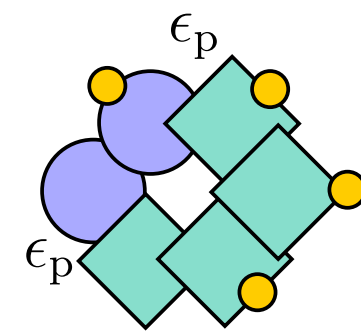
Towards topological edge currents in non-equilibrium assemblies



Including two different reactions brings the system out of equilibrium and allows individual subunits to perform **futile cycles**

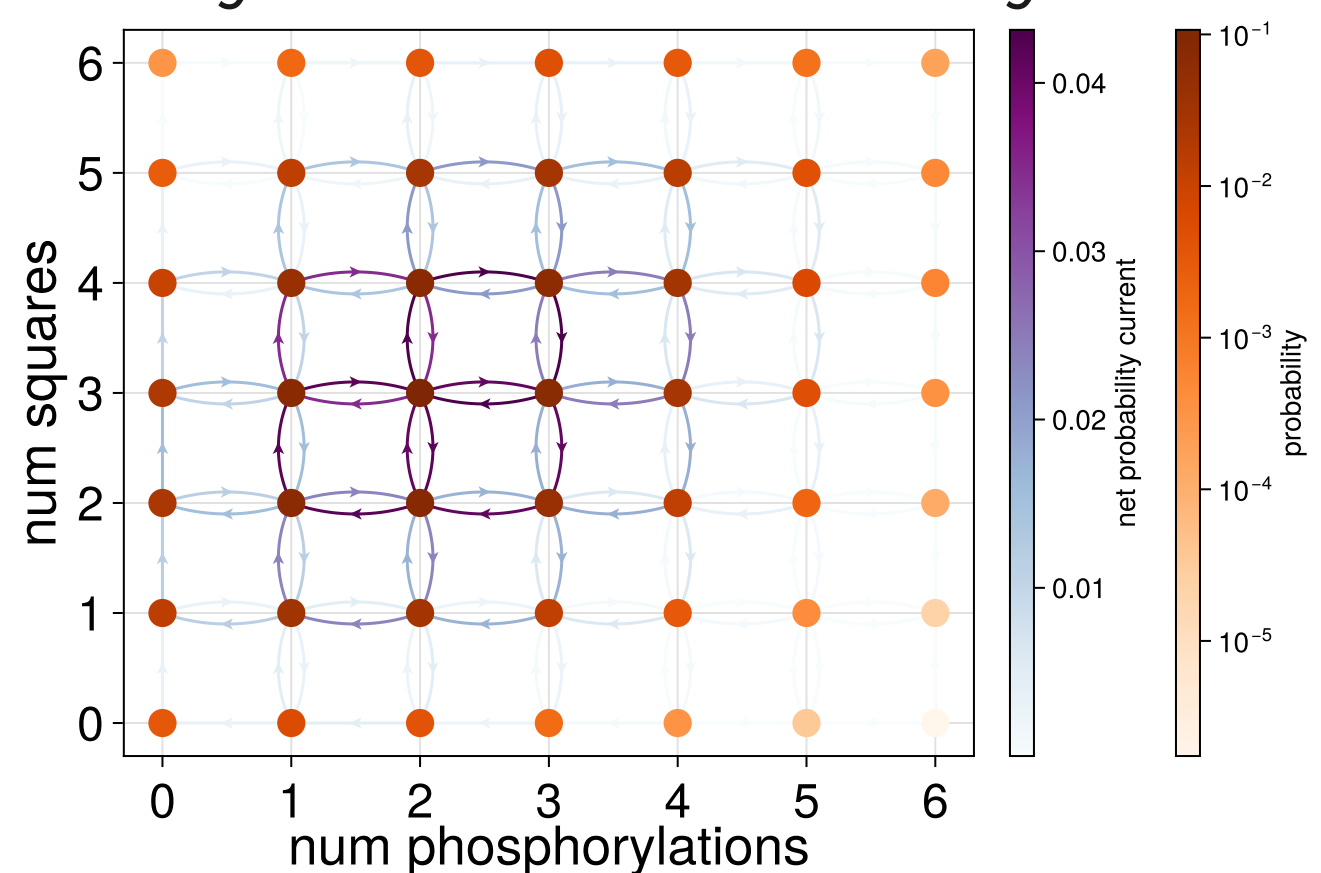


Subunits then interact in an equilibrium manner through an energy penalty of ϵ_p for each square-circle boundary

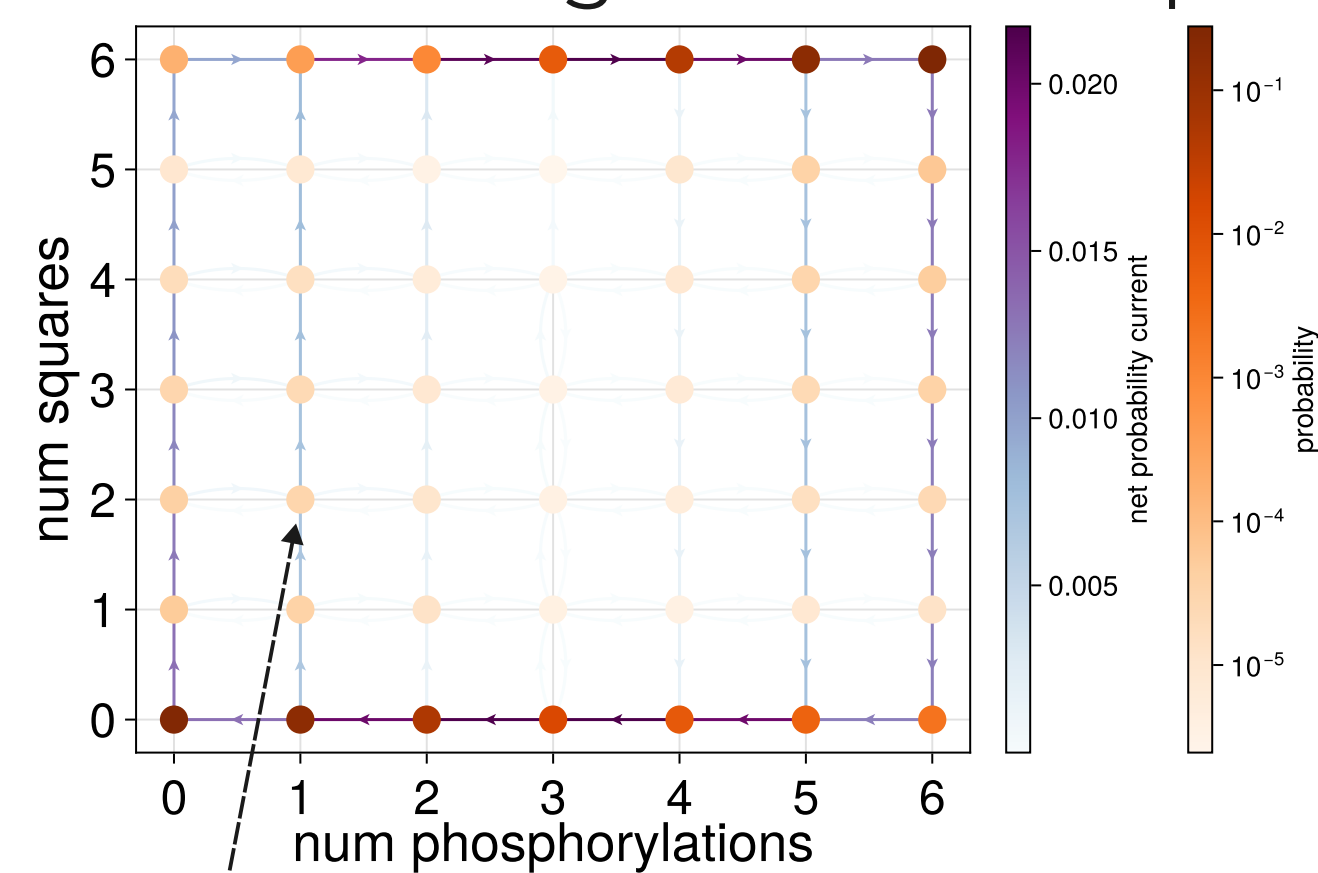


What types of dynamical steady states can we get?

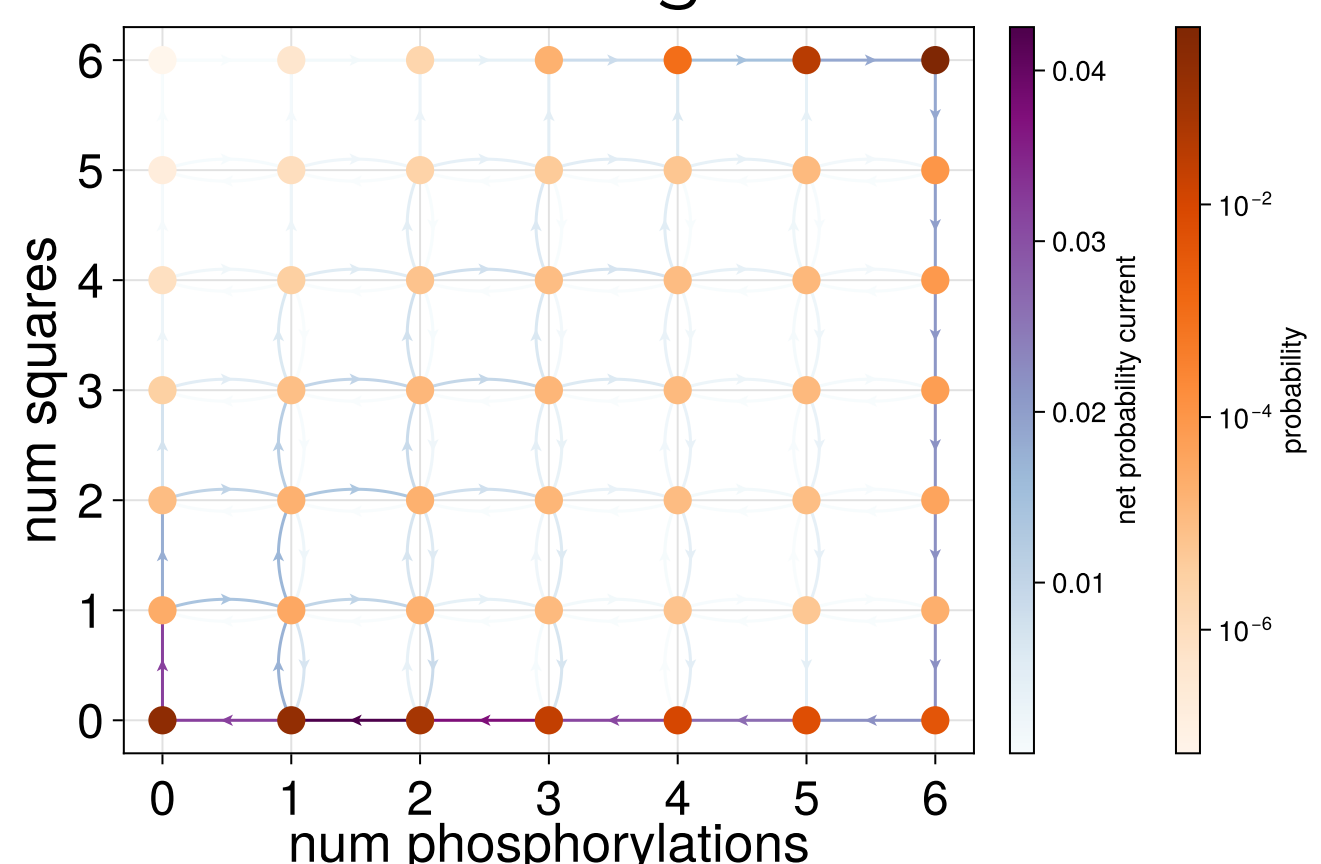
Asynchronous bulk cycles



Closed edge current loop



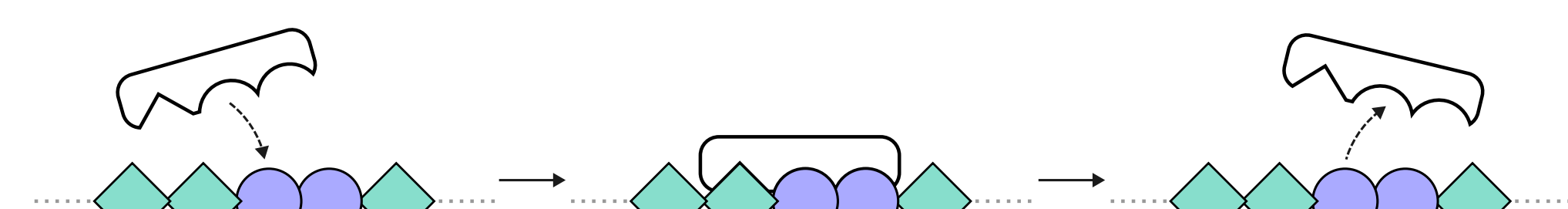
Partial edge current



each node is a group of system states with the same number of bound ligands and the same number of squares/circles

Realizing molecular automata with site-specific enzymes

- Bring out-of-equilibrium drive directly into the nearest-neighbour interactions
- Equivalent to stochastic dynamics on **binary strings**
- Potential implementation: context dependent enzymes



$$\text{enzyme } E + \dots i0j \dots \xrightleftharpoons[r_{E,1 \rightarrow 0,ij}]{r_{E,0 \rightarrow 1,ij}} \text{changed } E + \dots i1j \dots$$

$$r_{E,0 \rightarrow 1,ij} = K_{E,ij} \frac{\exp(\beta\mu_E)}{\exp(\beta\mu_E) + 1}$$

$$r_{E,1 \rightarrow 0,ij} = K_{E,ij} \frac{1}{\exp(\beta\mu_E) + 1}$$

- For each enzyme μ_E determines its bias toward 0s or 1s and K_E which combination of neighbours it may act on

Maximally driven case: $\mu_E \rightarrow \pm\infty$

- Fully specified by the presence of **up to 8 different enzymes**
- Can be **mapped to a cellular automata rule**

