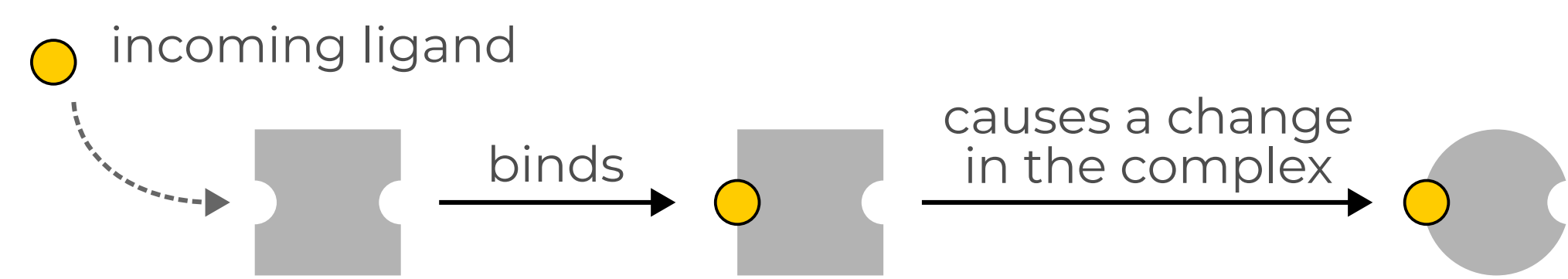


Functional dynamics in out-of-equilibrium allosteric assemblies



Allostery is the communication between distant sites of a macromolecule, such as binding sites on a protein



Equilibrium allostery

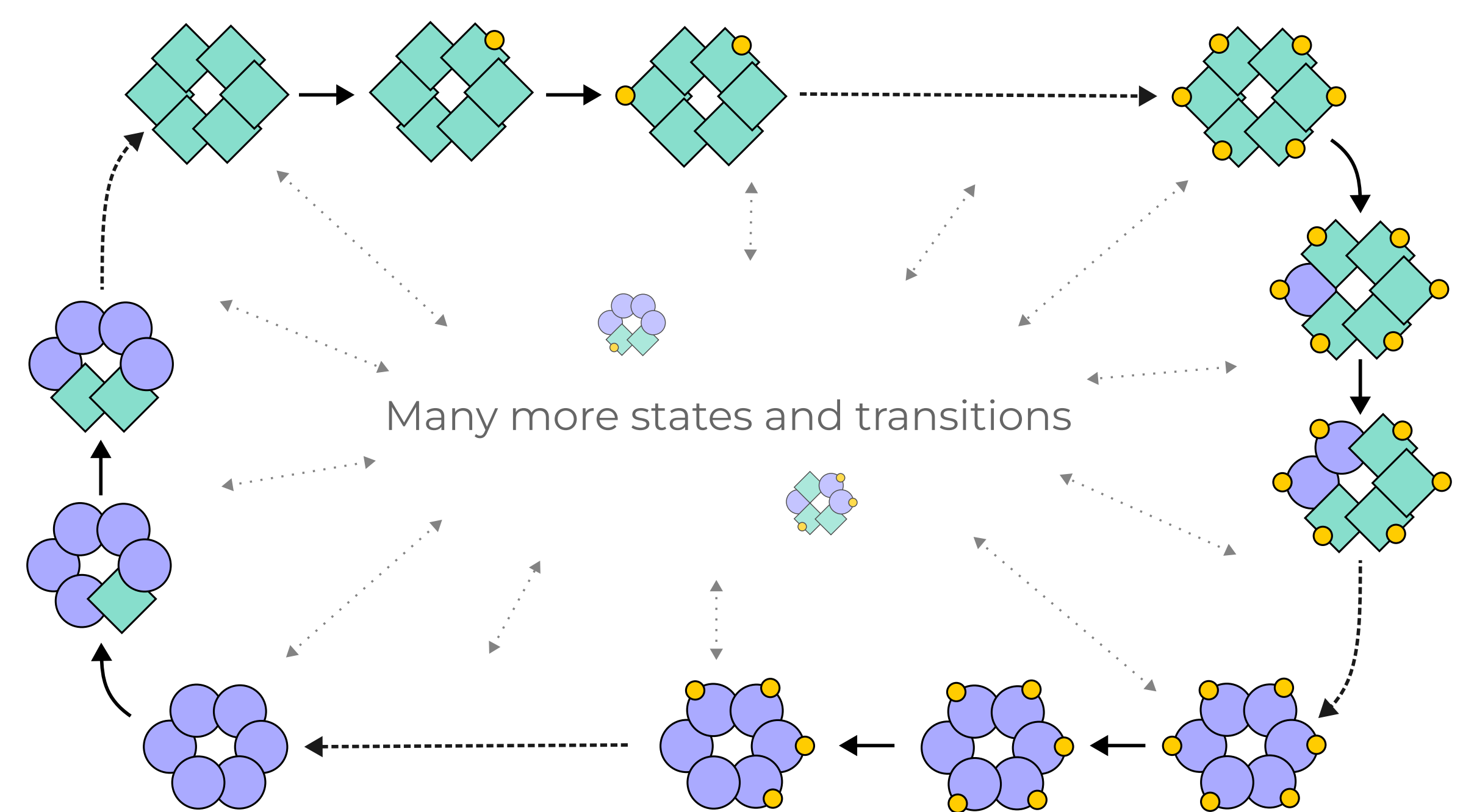
- MWC, KNF and the comprehensive Ensemble Allostery Model
- Cooperative binding, allosteric regulation/signalling

But there are out-of-equilibrium allosteric systems like KaiC or DNA clamps

What new behaviour is possible out of equilibrium?

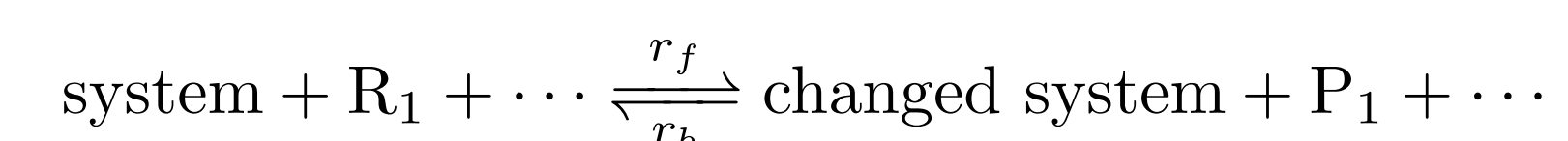
- Dynamic steady states
- Oscillations (such as in KaiC or other circadian clocks)
- Sensitivity to initial conditions (memory/spontaneous symmetry breaking)
- Dimensionality reduction (constraining the dynamics to part of the state space)
- Topologically protected states
- Modified cooperative binding

Outline of an allosteric interaction



Our approach

- Model of **identical subunits** (polymer like)
- Statistical physics and graph theory methods
- **Nearest neighbour interactions**
- **Thermodynamically consistent** transitions between system states (satisfying local detailed balance)

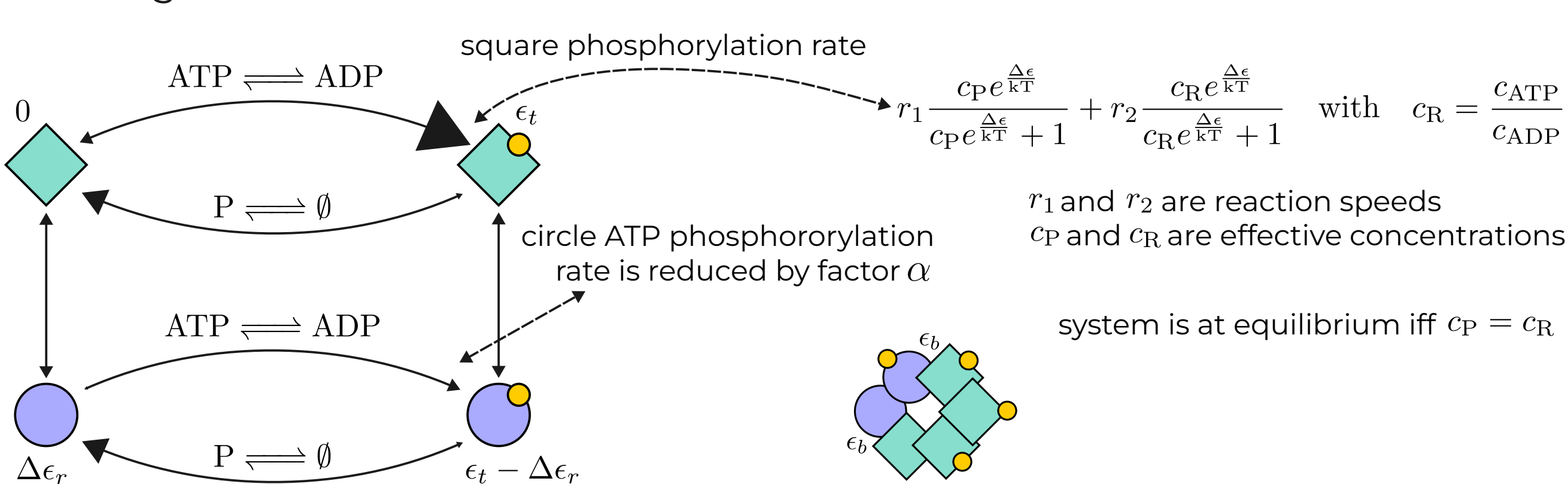


$$\frac{r_f}{r_b} = \exp(\beta(\Delta\epsilon + \mu_{R_1} + \dots - \mu_{P_1} - \dots))$$

change in system energy chemical potentials of all reactants and products

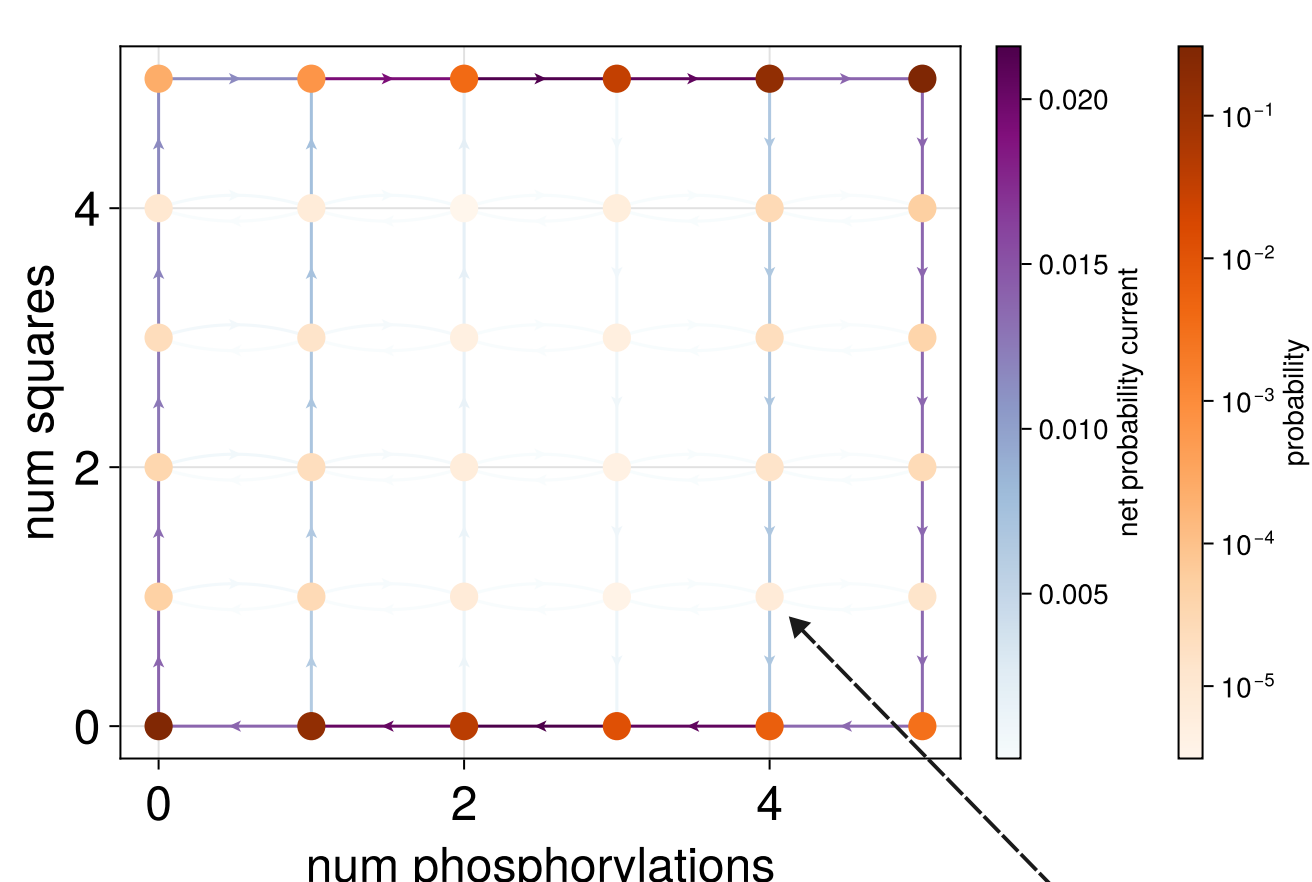
Biological model with out-of-equilibrium drive within subunits

- Each subunit can be in one of **2 conformational states** (squares and circles) and **phosphorylate**
- Subunits interact through their conformations only, and in an equilibrium manner by an energy penalty of ϵ_b per square-circle boundary
- Drive the system out of equilibrium by allowing **two different phosphorylation reactions** which couple differently to each conformation
- Through that we implement **futile cycles** of phosphorylation and conformation change within monomers

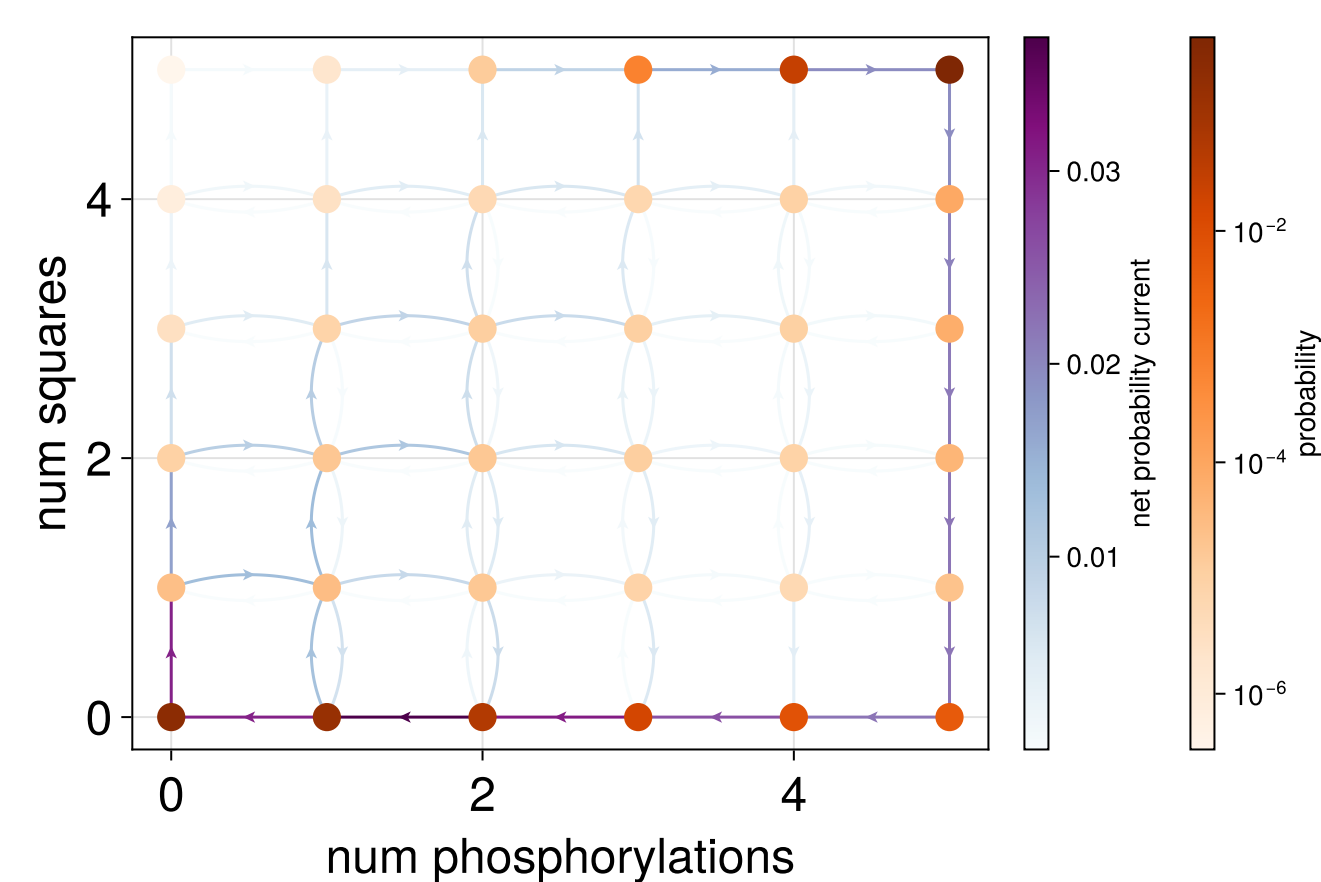


What types of dynamical steady states can we get?

Closed current loops



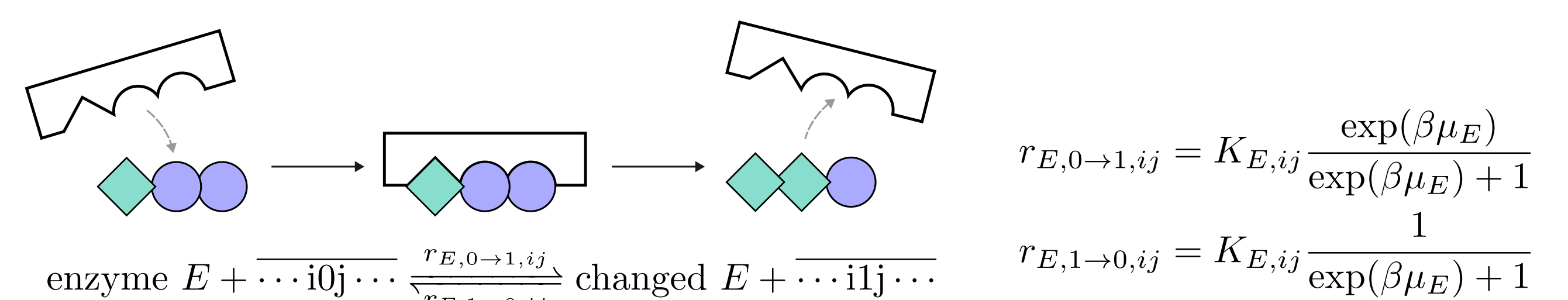
Open, streamlined currents



each node is a group of system states with the same number of bound ligands and the same number of squares/circles

Simple model allowing out-of-equilibrium subunit interactions

- **Bring out-of-equilibrium drive directly into the nearest neighbour interactions**
- Stochastic dynamics on **binary strings** (or general digit strings)
- Adding transitions reactions that differ based on neighbours leads to



- For each enzyme K_E **determines how it discriminates based on neighbours** and a μ_E **whether it is biased towards 0s or 1s**
- Out-of-equilibrium drive requires at least 2 reaction mechanisms

Minimal, maximally driven model has two enzymes, one for 0 to 1 transitions the one for the inverse

- This is the limit of one μ going to $+\infty$ and the other to $-\infty$
- A model is then fully specified by the two K
- This model can be seen as a stochastic version of 1D cellular automata and we can map any combination of K to a CA rule number
- Accounting for the symmetries of exchanging 0s and 1s and reversal we have 88 distinct rules

