Machine Learning for Computer Vision

Exercise 5

Kodai Matsuoka, Yuyan Li 26 May, 2017

1 Features

Our unary and Potts features are computed with the code in Listing 1.

Listing 1: Feature functions (lines 30 - 63) in StructLearn.py

```
def get_unary_features(raw):
   features = []
   # ADD YOUR CODE HERE
   raw = norm01(raw)
   sigmas = [0.5, 1.0, 1.5, 2.0, 3.0]
   for sigma in sigmas:
      feat = skimage.filters.gaussian(raw, sigma=sigma)
      features.append(feat[:,:,None])
   features.append(numpy.ones(raw.shape)[:,:,None])
   return numpy.concatenate(features, axis=2)
def get_potts_features(raw):
   features = []
   # ADD YOUR CODE HERE
   raw = norm01(raw)
   sigmas = [0.5, 1.0, 1.5, 2.0, 3.0]
   for sigma in sigmas:
      smooth = skimage.filters.gaussian(raw, sigma=sigma)
      edge = skimage.filters.laplace(smooth)
      feat = numpy.exp(-1.0*numpy.abs(edge))
```

```
features.append(feat[:,:,None])

# a constant feature is needed
features.append(numpy.ones(raw.shape)[:,:,None])
return numpy.concatenate(features, axis=2)
```

2 Test set performance with GraphCut

The full code is at the bottom in Listing 3. We have a variable mode for the different exercises.

For this part we chose mode='gp' to use graph cut.

The computed loss values for different noises and regularizers are:

```
[[[ 7 15
          1 10
                8]
  [ 7 13
          2
             8
                8]
  [ 7 13
         2 9
                9]
  [ 7 14
                9]
         1 10
         1 10
  [ 7 14
                9]]
 [[16 14 17 15 19]
  [15 15 17 19 20]
  [16 15 12 19 20]
  [16 16 13 20 20]
  [16 15 13 20 20]]
 [[10 12 16 10 11]
  [17 14 22 10 15]
  [17 14 23 10 15]
  [17 14 22 10 15]
  [19 14 22 10 15]]
 [[22 18 16 21 15]
  [20 21 19 24 16]
  [20 23 19 22 18]
  [20 23 19 24 18]
  [20 23 19 24 18]]
 [[40 25 18 32 22]
  [40 30 18 41 32]
  [37 28 18 40 38]
  [41 30 17 42 43]
  [41 30 17 42 43]]]
```

The content of this list structure is:

- every row is the loss of the five test images of a certain regularizer C and noise
- every list of five rows belong to a certain noise

The noises and regularizer values are sorted as given in the exercise.

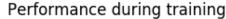
As expected, a bigger noise leads to worse predictions and therefore higher losses.

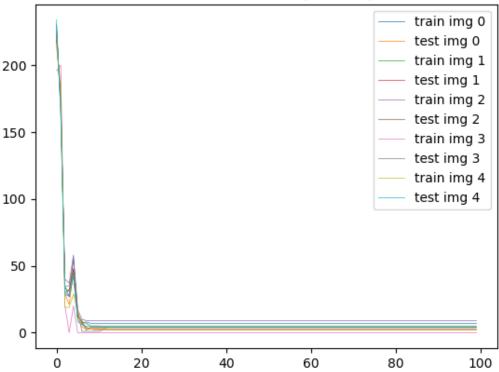
3 Test set performance with ICM

The same is done using an ICM solver instead of GraphCut by setting mode='icm'.

```
[[[5
       5
          6
             9
                 5]
  [ 5
       5
             9
                 5]
          6
  [ 5
       5
          6
             8
                5]
  [ 5
       5
          6
             8
                5]
  [ 5
       5
                5]]
          6
             8
 [[ 1 10 12 14
                 0]
  [ 5 11 12 15
                 0]
  [ 4 12 11 14
                 0]
  [ 5 11 13 15
                 0]
  [ 5 11 13 14
                0]]
 [[16 12 12 17 15]
  [17 13 22 18 14]
  [17 13 21 19 14]
  [17 13 22 20 14]
  [17 13 22 20 14]]
 [[21 22 22 17 16]
  [22 25 20 22 17]
  [23 27 20 22 16]
  [22 24 19 22 16]
  [22 24 18 22 16]]
 [[56 46 21 26 34]
  [40 24 34 14 60]
  [46 24 43 17 60]
  [46 24 55 19 60]
  [44 26 44 21 60]]]
```

Qualitatively, there does not seem to be a difference to the GraphCut results.





4 Bonus: show performance during training

With the code in Listing 2 (part of subgradient_ssvm)the training and test set performances are show after every iteration during training.

If mode='bonus' then after every training a plot with the losses is shown. One exemplary plot can be seen in Section 4.

Listing 2: Code to show performance after every iteration during training (lines 243 - 273 in StrucLearn.py).

```
losses = []
    for gm,_,loss_function in dataset.models_test:
        gm.change_weights(weights)
        graphcut = GraphCut(model=gm)
        y_pred = graphcut.optimize()
        losses.append(loss_function(y_pred))
    loss_test.append(losses)
    print('test set performance', losses)
# in bonus mode: make a plot of performance
if mode=='bonus':
    plottrain = numpy.array(loss_train).T
    plottest = numpy.array(loss_test).T
    for i in range(plottrain.shape[0]):
        plt.plot(range(n_iter), plottrain[i], lw=0.5, label=f'train img
            { i } ')
        plt.plot(range(n_iter), plottest[i], lw=0.5, label=f'test img {
           i } ')
    plt.title('Performance during training')
    plt.legend()
```

```
# Structured Learning:
1
2
   # =
3
   #
4
   \# In this exercise we will implement a structured learning system for
   \#\ foreground\ background\ segmentation .
6
   # We will learn the weights of a CRF Potts model.
7
   # The first step is to import all needed modules
8
9
10
   \# misc
   import numpy
11
   import sys
12
13
   # visualization
14
15
   import matplotlib.pyplot as plt
16
   import pylab
17
18
   # features
   import skimage. filters
19
20
21
   \#\ discrete\ graphical\ model\ package
  from dgm. models import *
22
23
   from dgm.solvers import *
24
   from dgm.value_tables import *
25
   \# misc. tools
26
   from tools import make_toy_dataset, norm01
27
28
   from skimage.morphology import disk
29
30
   def get_unary_features(raw):
31
       features = []
32
33
       34
       # ADD YOUR CODE HERE
35
       36
37
       raw = norm01(raw)
38
       sigmas = [0.5, 1.0, 1.5, 2.0, 3.0]
39
       for sigma in sigmas:
40
           feat = skimage.filters.gaussian(raw, sigma=sigma)
41
           features.append(feat[:,:,None])
42
       features.append(numpy.ones(raw.shape)[:,:,None])
43
44
       return numpy.concatenate(features, axis=2)
45
46
47
   def get_potts_features (raw):
       features = []
48
49
50
       ╫╫╫╫╫╫╫╫╫╫╫╫╫╫╫╫╫╫╫╫╫
51
       # ADD YOUR CODE HERE
```

```
52
        53
        raw = norm01(raw)
        sigmas = [0.5, 1.0, 1.5, 2.0, 3.0]
54
55
        for sigma in sigmas:
56
            smooth = skimage.filters.gaussian(raw, sigma=sigma)
57
            edge = skimage.filters.laplace(smooth)
            feat = numpy.exp(-1.0*numpy.abs(edge))
58
59
            features.append(feat[:,:,None])
60
61
        # a constant feature is needed
        features.append(numpy.ones(raw.shape)[:,:,None])
62
63
        return numpy.concatenate(features, axis=2)
64
65
66
    class HammingLoss(object):
        def __init__(self , y_true):
67
68
            self.y_true = y_true.copy()
69
        def __call__(self , y_pred):
70
            """ total loss"""
71
72
            return numpy.sum(self.y_true!=y_pred)
73
74
75
    def build_model(raw_data, gt_image, weights):
        shape = raw_data.shape
76
77
        n_{\text{var}} = \text{shape}[0] * \text{shape}[1]
78
        n_labels = 2
79
        variable_space = numpy.ones(n_var)*n_labels
80
        # lets compute some filters for the uanry features
81
82
        unary_features = get_unary_features(raw_data)
83
        # lets compute some filters for the potts features
84
85
        potts_features = get_potts_features (raw_data)
86
        n_weights = potts_features.shape[2] + unary_features.shape[2]
87
88
        \#assert \ n_-weights == len(weights)
89
90
91
        \# both graphical models
        gm = WeightedDiscreteGraphicalModel(variable_space=variable_space,
92
            weights=weights)
        loss_augmented_gm = WeightedDiscreteGraphicalModel(variable_space=
93
            variable_space , weights=weights)
94
        # convert coordinates to scalar
95
        \mathbf{def} vi(x0,x1):
96
97
            return x1 + x0*shape[1]
98
99
        # weight ids for the unaries (just plain numbers to remeter which
            weights are associated with the unary features)
100
        weight_ids = numpy.arange(unary_features.shape[2])
```

```
101
         for x0 in range(shape [0]):
102
             for x1 in range(shape [1]):
103
104
                 pixel_val = raw_data[x0, x1]
105
                 gt_label = gt_limage[x0, x1]
106
                 features = unary_features[x0, x1, :]
107
                 unary_function = WeightedTwoClassUnary(features=features,
108
                     weight_ids=weight_ids,
109
                                                         weights=weights)
110
111
                 if gt_label == 0:
112
                     loss = numpy.array([0,1])
113
                 else:
                     loss = numpy.array([1,0])
114
115
                 loss\_augmented\_unary\_function \ = \ WeightedTwoClassUnary ( \ features
116
                     =features, weight_ids=weight_ids,
117
                                                           weights=weights,
                                                               const_terms = -1.0*
                                                               loss)
118
119
                 variables = vi(x0, x1)
                 gm.\ add\_factor(\ variables=variables\ ,\ \ value\_table=unary\_function)
120
121
                 loss_augmented_gm.add_factor(variables=variables, value_table=
                     loss_augmented_unary_function)
122
123
        # average over 2 coordinates to extract feature vectors for potts
            functins
124
         def get_potts_feature_vec(coord_a, coord_b):
125
126
             fa = potts_features [coord_a [0], coord_a [1],:]
127
             fb = potts_features [coord_b[0], coord_b[1],:]
128
             return (fa+fb)/2.0
129
130
        # weight ids for the potts functions (just plain numbers to remeber
            which weights are associated with the potts features)
131
         weight_ids = numpy.arange(potts_features.shape[2]) + unary_features.
            shape [2]
132
133
         for x0 in range(shape [0]):
134
             for x1 in range(shape[1]):
135
136
                 # horizontal edge
                 if x0 + 1 < shape [0]:
137
                     variables = [vi(x0,x1),vi(x0+1,x1)]
138
139
                     features = get_potts_feature_vec((x0,x1), (x0+1,x1))
140
                     # the weighted potts function
141
                     potts_function = WeightedPottsFunction(shape=[2,2],
142
                                                                features=features,
143
                                                                weight_ids=
                                                                   weight_ids,
```

```
144
                                                              weights=weights)
145
                     \# add factors to both models
                     gm.add_factor(variables=variables, value_table=
146
                         potts_function)
                     loss_augmented_gm.add_factor(variables=variables,
147
                         value_table=potts_function)
148
149
                 # vertical edge
150
                 if x1 + 1 < shape[1]:
                     variables = [vi(x0,x1),vi(x0, x1+1)]
151
152
                     features = get_potts_feature_vec((x0,x1), (x0,x1+1))
153
                     # the weighted potts function
                     potts_function = WeightedPottsFunction(shape=[2,2],
154
155
                                                              features=features,
156
                                                              w eight_i ds =
                                                                  weight_ids,
157
                                                              weights=weights)
                     # add factors to both models
158
159
                     gm.add_factor(variables=variables, value_table=
                         potts_function)
160
                     loss_augmented_gm.add_factor(variables=variables,
                         value_table=potts_function)
161
162
        # gm, loss augmented and the loss
163
        return gm, loss_augmented_gm, HammingLoss(gt_image.ravel())
164
165
    # very simple helper class to combine things
    class Dataset(object):
166
        def __init__(self , models_train , models_test , weights):
167
             self.models_train = models_train
168
169
             self.models_test = models_test
170
             self.weights = weights
171
172
    # Subgradient SSVM
173
174
175
    # Instead of a cutting plane approach, we use a subgradient decent to find
         the optimal weights
176
177
    def subgradient_ssvm(dataset, mode='gp', n_iter=20, learning_rate=1.0, c
178
        =0.5, lower_bounds=None, upper_bounds=None, convergence=0.001):
179
180
        loss_train = []
        loss_test = []
181
182
        weights = dataset.weights
183
184
        n = len(dataset.models_train)
185
186
        if lower_bounds is None:
             lower_bounds = numpy.ones(len(weights))*-1.0*float('inf')
187
188
```

```
189
         if upper_bounds is None:
190
             upper_bounds = numpy.ones(len(weights))*float('inf')
191
192
         do_{-}opt = True
193
         for iteration in range(n_iter):
194
             effective_learning_rate = learning_rate*float(learning_rate)/(1.0+
195
                iteration)
196
197
             # compute gradient
             diff = numpy.zeros(weights.shape)
198
199
             for gm, gm_loss_augmented, loss_function in dataset.models_train:
200
201
                 \# update the weights to the current weight vector
202
                 gm. change_weights (weights)
203
                 gm_loss_augmented.change_weights(weights)
204
205
                 # the gt vector
206
                 y_true = loss_function.y_true
207
208
                 # optimize loss augmented / find most violated constraint
209
                 if mode == 'icm':
210
211
                     icm = IteratedConditionalModes(model=gm_loss_augmented)
212
                     y_hat = icm.optimize()
                 else:
213
214
                     graphcut = GraphCut(model=gm_loss_augmented)
                     y_hat = graphcut.optimize()
215
216
217
                 # compute joint feature vector
218
                 phi_y_hat = gm. phi(y_hat)
219
                 phi_y_true = gm.phi(y_true)
220
221
                 diff += phi_y_true - phi_y_hat
222
223
224
225
             new_weights = weights - effective_learning_rate*(c/n)*diff
226
227
             # project new weights
228
             where_to_large = numpy.where(new_weights>upper_bounds)
229
             new_weights [where_to_large] = upper_bounds [where_to_large]
             where\_to\_small = numpy.where(new\_weights < lower\_bounds)
230
231
             new_weights[where_to_small] = lower_bounds[where_to_small]
232
233
234
             delta = numpy.abs(new_weights-weights).sum()
             if ( delta < convergence ) :</pre>
235
236
                 print("converged")
237
             print('iter', iteration, 'delta', delta', delta', numpy.round(new_weights
238
                , 3))
```

```
239
240
             weights = new_weights
241
242
243
244
             # show performance during training
245
246
247
             losses = []
248
             for gm,_,loss_function in dataset.models_train:
249
                 gm. change_weights (weights)
250
                 graphcut = GraphCut (model=gm)
251
                 y_pred = graphcut.optimize()
252
                 losses.append(loss_function(y_pred))
             loss_train.append(losses)
253
254
             print('training set performance', losses)
255
256
             losses = []
             for gm,_,loss_function in dataset.models_test:
257
258
                 gm. change_weights (weights)
259
                 graphcut = GraphCut (model=gm)
260
                 y_pred = graphcut.optimize()
261
                 losses.append(loss_function(y_pred))
262
             loss_test.append(losses)
263
             print('test set performance', losses)
264
265
        # in bonus mode: make a plot of performance
266
         if mode='bonus':
267
             plottrain = numpy.array(loss_train).T
268
             plottest = numpy.array(loss_test).T
269
             for i in range(plottrain.shape[0]):
270
                 plt.plot(range(n_iter), plottrain[i], lw=0.5, label=f'train img
                      { i } ')
                 plt.plot(range(n_iter), plottest[i], lw=0.5, label=f'test img {
271
                     i } ')
             plt.title('Performance during training')
272
273
             plt.legend()
274
             plt.show()
275
276
277
        return weights
278
    noises = [1.5, 2.0, 2.5, 3.0, 3.5]
279
    regularizers = [0.1, 0.5, 0.9, 5., 10.]
280
    shape = (20, 20)
281
    \# noise = 2.0
282
283
284
    loss_train = []
285
    loss_test = []
286
287
288 # CHOOSE MODE
```

```
289 \mid \# gp: use graph cut
290
   \# icm: use icm
291
   # bonus: show a plot of the loss at every step of learning phase
292
    modes = ['gp', 'icm', 'bonus']
293
294
    mode = modes[2]
295
    for noise in noises:
296
297
298
        l_noises = []
299
300
        # The Dataset
301
        # =====
302
        x_train, y_train = make_toy_dataset(shape=shape, n_images=5, noise=
303
            noise)
304
        x_{test}, y_{test} = make_{toy_{dataset}}(shape=shape, n_{images}=5, noise=
            noise)
305
306
        # Build the weighted models:
307
        # _____
308
309
        unary_features_0 = get_unary_features(x_train[0])
310
        potts_features_0 = get_potts_features(x_train[0])
        n_unary_features = unary_features_0.shape[2]
311
312
        n_potts_features = potts_features_0.shape[2]
313
314
        n_weights = n_unary_features + n_potts_features
315
316
        for c in regularizers:
317
             weights = numpy.zeros(n_weights)
318
319
             # build the graphical models
             models\_train = [build\_model(x,y, weights) for x,y in zip(x\_train, y)]
320
                 y_train)]
                           = [build_model(x,y, weights) for x,y in zip(x_test,
321
             models\_test
                y_test)]
322
323
324
             # combine things in a dataset
325
             dset = Dataset (models_train, models_test, weights)
326
327
328
            # we want the regularizer 'beta' to be positive
             lower_bounds = numpy.ones(n_weights)*(-1.0*float('inf'))
329
330
             lower_bounds[n_unary_features:n_unary_features+n_potts_features] =
                 0
331
332
             weights = subgradient_ssvm (dset, mode=mode, c=c, learning_rate=1.0,
                lower_bounds=lower_bounds, n_iter=100)
333
334
```

```
335
             \# Training Set Performance:
336
337
             print("learned weights", weights)
338
339
340
             for i,(gm,_,loss_function) in enumerate(models_train):
341
                 gm. change_weights (weights)
342
343
                 if \mod = 'icm':
344
                     icm = IteratedConditionalModes(model=gm)
                     y_pred = icm.optimize()
345
346
                 else:
                      graphcut = GraphCut(model=gm)
347
                      y_pred = graphcut.optimize()
348
                 print('loss of train img ', i, ':', loss_function(y_pred))
349
350
351
352
             # Test set performance:
353
354
355
             \#\ losses\ for\ this\ c
             1_{-c} = []
356
357
             for i,(gm,_,loss_function) in enumerate(models_test):
358
359
                 gm.change_weights(weights)
360
361
                 if \mod = 'icm':
362
                     icm = IteratedConditionalModes(model=gm)
363
                     y_pred = icm.optimize()
364
                 else:
365
                      graphcut = GraphCut (model=gm)
366
                      y_pred = graphcut.optimize()
367
                 print('loss of test img', i, '=', loss_function(y_pred))
368
369
                 l_c.append(loss_function(y_pred))
370
             l_noises.append(l_c)
371
372
373
         loss_test.append(l_noises)
374
    print(numpy.array(loss_test))
375
```