

## 1. (Computer Center Staffing)

**Decision Variables::**  $x_1, x_2, x_3$  : Full time consultants

$y_1, y_2, y_3, y_4$  : Part time consultants

### a. Objective Function:

The objective is to minimize staffing cost therefore the will be the equation

$$Z_{\text{Min}} = 48(y_1 + y_2 + y_3 + y_4) + 112(x_1 + x_2 + x_3)$$

### Constraints:

$$x_1 + y_1 \geq 4$$

$$x_1 + x_2 + y_2 \geq 8$$

$$x_2 + x_3 + y_3 \geq 10$$

$$x_3 + y_4 \geq 6$$

$$x_1=2, x_2=2, x_3=3, y_1=2, y_2=4, y_3=5, y_4=3$$

The min cost is  $Z_{\text{Min}} = 48(y_1 + y_2 + y_3 + y_4) + 112(x_1 + x_2 + x_3)$

$$= 48(14) + 112(7)$$

$$Z_{\text{Min}} = \$1456$$

**b.** since company decided to includes meal break,

The minimum staffing cost is  $Z_{\text{Min}} = 48(y_1 + y_2 + y_3 + y_4) + 112(x_1 + x_2 + x_3)$

### Constraints:

$$x_1 + y_1 \geq 4$$

$$x_1 + x_2 + y_2 \geq 8$$

$$x_2 + x_3 + y_3 \geq 10$$

$$x_3 + y_4 \geq 6$$

To make sure each and every part-time has a full time consultant, I will hire two full time consultants in 12PM-8PM shift.

Hence,  $X_1=2, X_2=5, X_3=3, Y_1=2, Y_2=4, Y_3=5, Y_4=3$

The min cost is  $Z_{\text{Min}}=48(Y_1+Y_2+Y_3+Y_4)+112(X_1+X_2+X_3)$

$$=48(14)+112(10)$$

$$\mathbf{Z_{\text{Min}} = \$1792}$$

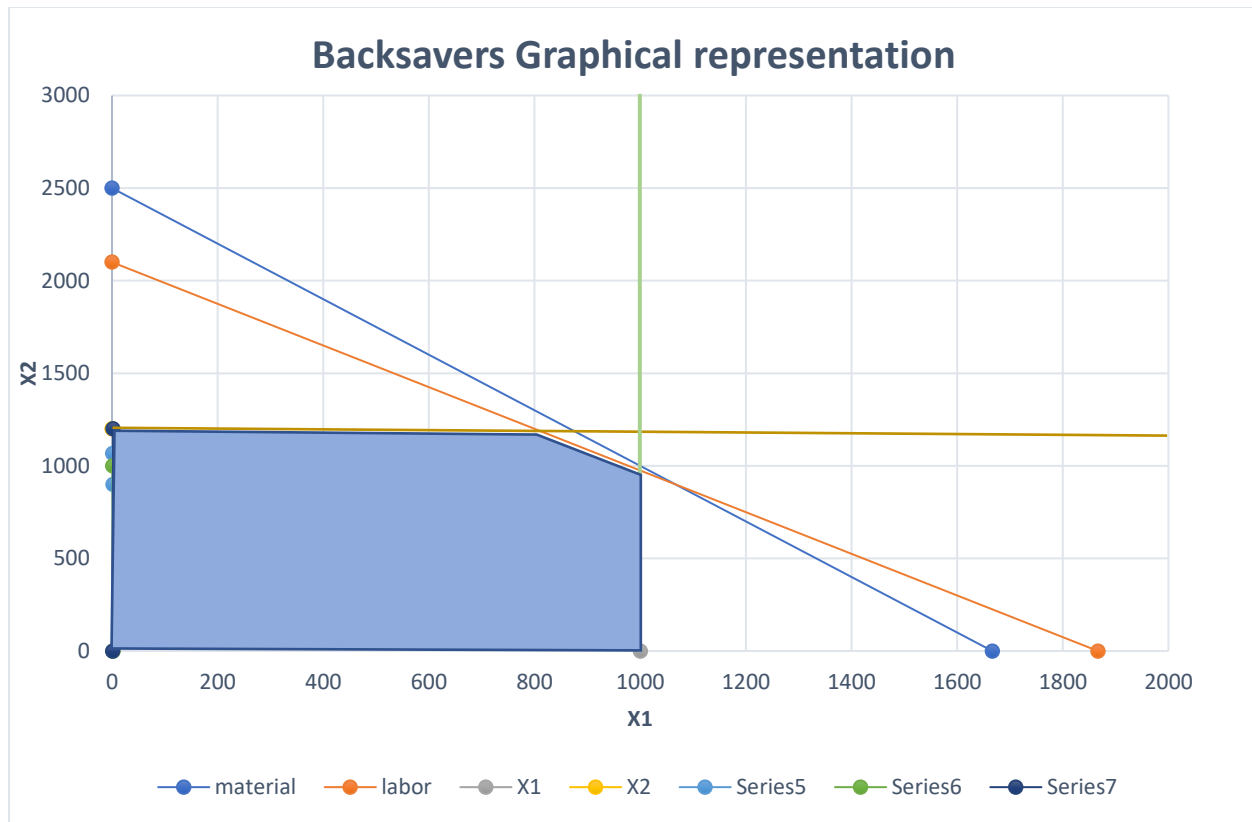
2) Backsavers LP graphical Representation:

	X1	X2	>=	0
Z	32	24		
material	3	2	<=	5000
labor	45	40	<=	84000

intercept	X1	X2	
material	0	2500	5000
	1666.667	0	5000
labor	0	2100	84000
	1866.667	0	84000

X1	≤	1000
X2	≤	1200

In the Graph, we have feasible region at corner points (0,1200) (1000,0)



**3) The decision variables are**

$x_{1L}$  = number of large units produced per day at Plant 1,

$x_{1M}$  = number of medium units produced per day at Plant 1,

$x_{1S}$  = number of small units produced per day at Plant 1,

$x_{2L}$  = number of large units produced per day at Plant 2,

$x_{2M}$  = number of medium units produced per day at Plant 2,

$x_{2S}$  = number of small units produced per day at Plant 2,

$x_{3L}$  = number of large units produced per day at Plant 3,

$x_{3M}$  = number of medium units produced per day at Plant 3,

$x_{3S}$  = number of small units produced per day at Plant 3.

The objective is to maximize

$$Z = 420(x_{1L} + x_{2L} + x_{3L}) + 360(x_{1M} + x_{2M} + x_{3M}) + 300(x_{1S} + x_{2S} + x_{3S})$$

subject to the following constraints.

Capacity constraints:

$$x_{1L} + x_{1M} + x_{1S} \leq 750$$

$$x_{2L} + x_{2M} + x_{2S} \leq 900$$

$$x_{3L} + x_{3M} + x_{3S} \leq 450$$

Storage space constraints:

$$20x_{1L} + 15x_{1M} + 12x_{1S} \leq 13000$$

$$20x_{2L} + 15x_{2M} + 12x_{2S} \leq 12000$$

$$20x_{3L} + 15x_{3M} + 12x_{3S} \leq 5000$$

Sale constraints:

$$x_{1L} + x_{2L} + x_{3L} \leq 900$$

$$x_{1M} + x_{2M} + x_{3M} \leq 1200$$

$$x_{1S} + x_{2S} + x_{3S} \leq 750$$

Same capacity percentage constraints:

$$900(x_{1L} + x_{1M} + x_{1S}) - 750(x_{2L} + x_{2M} + x_{2S}) = 0$$

$$450(x_{2L} + x_{2M} + x_{2S}) - 900(x_{3L} + x_{3M} + x_{3S}) = 0$$

Nonnegativity constraints:

$$x_{1L} \geq 0, x_{1M} \geq 0, x_{1S} \geq 0, x_{2L} \geq 0, x_{2M} \geq 0, x_{2S} \geq 0,$$

$$x_{3L} \geq 0, x_{3M} \geq 0, x_{3S} \geq 0.$$