

# CMSC389R

## Cryptography II



**COMPUTER SCIENCE**  
UNIVERSITY OF MARYLAND



## homework ix recap

- Hash cracking
- Hash and submit challenge
- Questions?

# agenda

- Some theory
  - Private key vs public key cryptography
- Heavy emphasis on applications
  - Focus on PGP
  - Message signing/verification
  - Attack on hash-based signatures

# hashing

- Last week, we covered popular hashing algorithms
  - What they look like
  - How they can be cracked
  - Their weaknesses
- How does this tie into the course?

# encryption

- Private key cryptography
  - Also known as symmetric cryptography
  - One key for encryption/decryption
  - Need to keep this *private*
- Public key cryptography
  - Also known as asymmetric cryptography
  - Public key -> encrypt, known to all
  - Private key -> decrypt, kept secret

# symmetric key cryptography

- Meet your two new best friends:
  - Alice and Bob
- Alice wants to send Bob a message
  - Expectation: channel in which message is sent is actively wiretapped
  - Goal: send Bob a secret message without eavesdropper (Eve) recovering the message

## symmetric key cryptography

- Alice generates a private key  $K$  and meets with Bob in person
  - Alice assures that Bob is *really* Bob
  - Alice give Bob  $K$
- Alice and Bob part ways
  - Alice and Bob encrypt/decrypt messages with the *shared* key  $K$ .

# symmetric key cryptography

- Examples:
  - Vigenere Cipher
  - One-time pad (OTP)
  - Data Encryption Standard (DES)
  - Advanced Encryption Standard (AES)

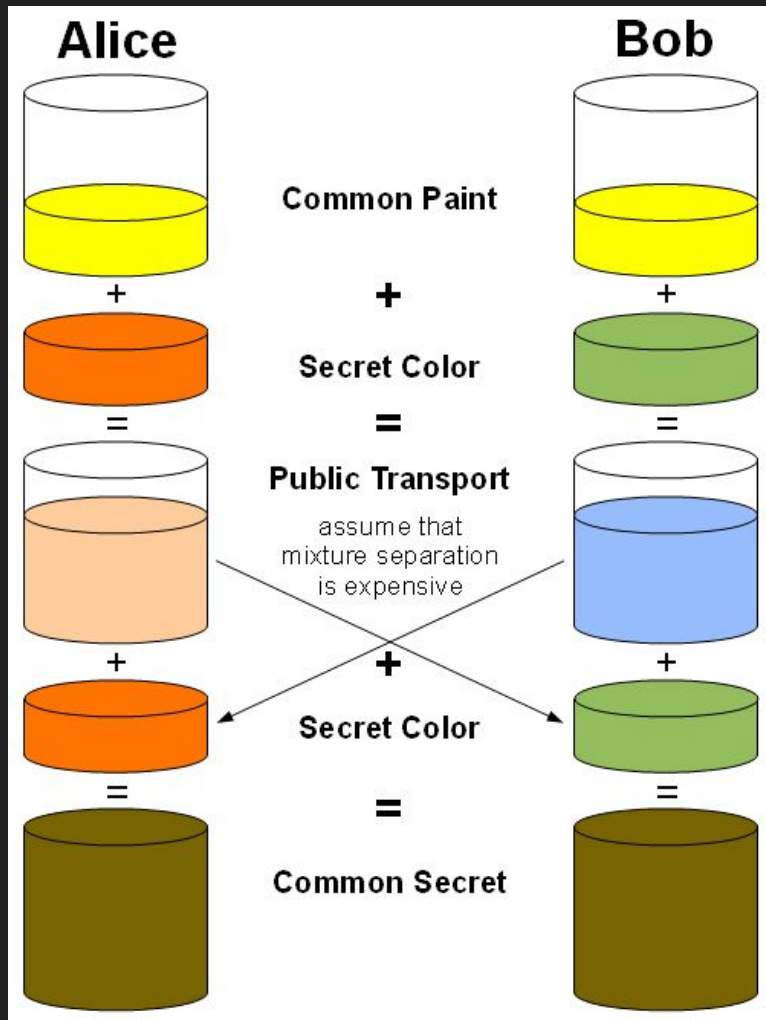


# symmetric key cryptography

- Advantages
  - Very secure with small key length
  - Relatively fast (vs asymmetric)
- Disadvantages
  - Difficult to share key
  - Both parties vulnerable if key is compromised

## symmetric key cryptography

- Protocols exist for safe generation and sharing of symmetric keys
- e.g. Diffie-Hellman
  - Alice and Bob each pick their own secret
  - Each person transforms their secret based on a publicly agreed upon rule and exchange their transformations
  - Each person applies their secret to the other's transformation to get the same key



- Diffie-Hellman
- Uses modular arithmetic
- Security provable based on mathematically hard problem
  - Discrete log

$$(g^a \bmod p)^b \bmod p = (g^b \bmod p)^a \bmod p$$

## asymmetric key cryptography

- Alice and Bob each generate a public and private key pair
- Each exchange their public keys, keep private keys secret
- Alice applies Bob's public key to her message and sends to Bob, encrypted
- Bob and ONLY Bob can apply his private key to Alice's encryption to recover the message

# asymmetric key cryptography

- Examples:
  - RSA (*HTTPS*, DRM)
  - PGP (Commonly used in email, ACH)
  - ElGamal (Discrete Logarithm problem)
  - Elliptic-Curve (shorter keys than RSA)

## Pretty Good Privacy (PGP)

- Pretty Good Privacy (PGP): Developed in 1991 by Phil Zimmermann. Allows for
  - Encryption/Decryption
  - Signing
- Frequently used in email, files, full disk encryption, etc.

## Pretty Good Privacy (PGP)

- Use gpg command line tool to generate public key/private key pair
- Can then share public key with the world
  - MIT PGP Key server
  - Email (ie. enigmail)
  - Keybase
  - ...
- Decrypt messages using PGP private key

# Pretty Good Privacy (PGP)

- `gpg --gen-key`
  - Generate key -- ID based on name/email
- `gpg --list-secret-keys`
- `gpg --export --armor you@email.com > pubkey.asc`
  - Create a key to send to friends
- `gpg --import pubkey.asc`
  - Import a friend's key
- `gpg -e -u "Your name" -r "Their name" msg.txt`
  - Generates `msg.txt.gpg`
- `gpg --decrypt msg.txt.gpg`
  - Display decrypted message



# Pretty Good Privacy (PGP)

- Can sign documents too
  - Analogous to “encrypting” with private key
  - Anyone can then use your public key to verify the signature
- `gpg --output myfile.sig --sign myfile`
  - “Encrypts” file, can’t see message without “decrypting”
- `gpg --output myfile --decrypt myfile.sig`
- `gpg --clearsign myfile`
  - Generates `myfile.asc`
  - Wraps file in signature rather than “encrypting” it
  - Useful for sending/posting publicly as it provides the message/signature in ASCII

# Pretty Good Privacy (PGP)

```
-----BEGIN PGP PUBLIC KEY BLOCK-----
```

```
mQENBFrHpXsBCADeJrGA5Rwaj4GvAwzGtKt6PFC  
oaXj7uJTK13h2IR2YTFSbyQV2...
```

```
-----END PGP PUBLIC KEY BLOCK-----
```

```
-----BEGIN PGP PRIVATE KEY BLOCK-----
```

```
02I1BJm5AQ0EWse1ewEIALahcUsgcJTUyUb+yWka  
+cN2Tsh3oItAAndhXUR0/zsEN...
```

```
-----END PGP PRIVATE KEY BLOCK-----
```

# Merkle-Damgard Construction

- Recall from last week
- Can be used to make hash functions
  - Take a fixed-length block cipher or function
  - Split message into blocks
  - Pipe output of one block into input of next
  - Pad last block to be the right size
  - Final output = internal state of hash

# Merkle-Damgard Construction

- Used by MD5 and SHA family of hashes
- Note: final output = final internal state
  - What if we initialize a hash with a given internal state?
  - Can add more message blocks to continue hashing from last state

## Hash-based signatures

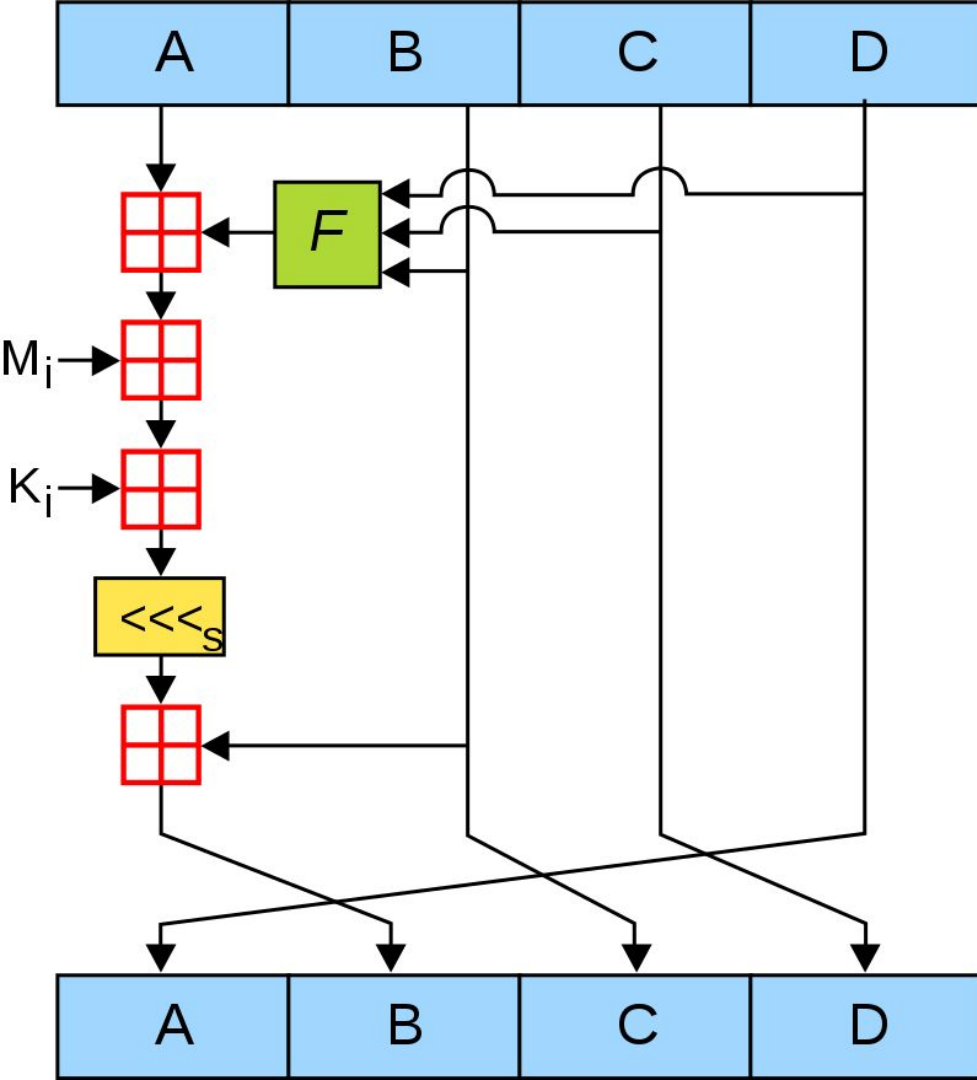
- Can use hashes to verify integrity of data
- Could use hashes to “sign” data
  - Signature: proof of authenticity by owner
  - $\text{hash}(\text{secret} + \text{data}) = \text{signature}$
- Safe?

## an attack on hash-based signatures

- `hash(secret + data)` signature is NOT safe for Merkle-Damgard-based hashes
  - Compute output = `hash(secret + data)`
  - Initialize another hash with state being the “output” of another hash
  - Update hash with payload
    - becomes `hash(secret + data + payload)`
  - Can forge signatures w/o secret!

## MD5 state

- Example: MD5
- Output = final state
  - State variables A, B, C, D corresponding to 1/4 of final hash
  - e.g. 6057f13c496ecf7fd777ceb9e79ae285
  - A = 6057f13c, ..., D = e79ae285



MD5

- Output =  $A+B+C+D$



## MD5 padding

- MD5 is padded to a multiple of 512-bits
  - If message is a multiple of 512-bits, just make a new block containing only padding
- '1' bit appended to message
- '0' bits appended until block length is 64-bits less than a multiple of 512
- Last 64 bits filled with  $\text{len}(\text{msg})$  in **bits**, modulo  $2^{64}$

## MD5 padding

- Want to pad msg = “CMSC389R Rocks!”
  - $\text{len}(\text{msg}) = 15 \text{ bytes} = 120 \text{ bits}$
  - $512 - 64 = 448 \text{ bits of msg} + \text{pad}$
  - $448 - 120 = 328 \text{ bits of pad} = 41 \text{ bytes}$ 
    - 1 ‘1’ bit, 327 ‘0’ bits
    - or one ‘0x80’ and 40 ‘0x00’
  - Message length 15 bytes  $\Rightarrow 120 \text{ bits} = 0x78$ 
    - Bit length stored in little endian
    - i.e. 78 00 00 00 00 00 00 00

# MD5 padding

```
'CMSC389R Rocks!\x80\x00\x00\x00\x00\x00\x00\x00
\x00\x00\x00\x00\x00\x00\x00\x00\x00\x00\x00\x00
\x00\x00\x00\x00\x00\x00\x00\x00\x00\x00\x00\x00
\x00\x00\x00\x00\x00\x00\x00\x00\x00\x78\x00\x00
\x00\x00\x00\x00'
```

- use `\x` escape sequence in python for hex literals

## attack on MD5 signatures

- Query w/ **data**:  $h = \text{hash}(\text{secret} + \text{data})$
- Initialize local state:  $A, B, C, D = h_1, h_2, h_3, h_4$ 
  - Now have hash function  $\text{hash}_{ABCD}()$
- Craft **padding** to match **data**
  - **data** + **padding** should be multiple of 512-bit
- Combine **data** + **padding** and arbitrary **payload**
- Perform  $\text{hash}_{ABCD}(\text{payload}) = h'$
- $h' = \text{hash}(\text{secret} + \text{data} + \text{padding} + \text{payload})$
- Valid signature forged on **data** + **padding** + **payload**!

## attack in python

- hashlib provides NO access to internal states of any algorithm, MD5 or SHA
- use separate module that opens access
  - We'll be using one called md5py.py, supplied on Github

## Homework #9

Will be posted soon.

Let us know if you have any questions!

This assignment has 2 parts.