

1. Consider this propositional logic. Assume that  $\sim$  is negation.

$$\sim y \vee \sim u \vee \sim s \vee q$$

Select all true statements.

- a) The statement is a Horn clause **T**
- b) The statement is a definite clause **T**
- c) The statement is logically equivalent to  $\sim y \vee \sim u \vee \sim s \rightarrow q$  **F**
- d) The statement is logically equivalent to  $\sim y \wedge \sim u \wedge \sim s \rightarrow q$  **F**
- e) The statement is logically equivalent to  $y \wedge u \wedge s \rightarrow q$  **T**
- f) The statement is logically equivalent to  $\sim q \wedge u \wedge s \rightarrow \sim y$  **T**

2. Select all inferences that are valid logical inferences. That is, the clause below the line logically follows from (i.e.,  $\vdash$  *or*  $\models$ ) the clause(s) above the line.

F a) 
$$\frac{p \vee \sim q \vee s, \sim p \vee q \vee \sim s}{\{ \}}$$

T b) 
$$\frac{p, \sim p \vee q \vee r}{q \vee r}$$

T c) 
$$\frac{p \wedge \sim q \rightarrow s, p \wedge \sim q}{s \vee r}$$

T d) 
$$\frac{p \wedge \sim q \rightarrow s, p \wedge \sim q}{s}$$

T e) 
$$\frac{p \vee q \vee s, \sim p \vee q \vee r}{q \vee s \vee r}$$

T f) 
$$\frac{p \wedge \sim q \wedge r}{p \wedge r}$$

3. Consider the propositional knowledge base, KB. Prove  $(t \wedge p)$  by contradiction using resolution (resolution refutation) with a set-of-support strategy.

$$p \vee \sim q \vee \sim r$$

$$\sim y \vee \sim u \vee \sim s \vee q$$

$$\sim x \vee r$$

$$\sim q \vee t \vee \sim x$$

$$u \vee \sim w$$

$$z \vee \sim m$$

$$\sim w \vee y \vee \sim x$$

s

w

x

AI

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② Prove  $\vdash \neg P$ .

Apply Resolution

$$\boxed{p \vee \neg q \vee \neg r} \quad \text{① } \neg r \vee t$$

$$\begin{aligned} & \neg y \vee \neg u \vee \neg s \vee q \quad \text{② } \neg y \vee \neg u \vee \neg s \\ & \neg x \vee r \quad \text{③ } \neg r \vee t \quad \text{④ } \neg x \vee t \end{aligned}$$

$$\boxed{\neg q \vee t \vee \neg x}$$

$$\begin{aligned} & u \vee \neg w \quad \text{⑤ } \neg y \vee \neg u \vee \neg s \quad \text{⑥ } \neg y \vee \neg s \\ & z \vee \neg m \end{aligned}$$

$$\boxed{\neg w \vee y \vee \neg x} \quad \text{⑦ } \neg y \vee \neg x$$

$$\begin{aligned} & s \quad \text{⑧ } \neg y \vee \neg s \quad \text{⑨ } \neg y \\ & \boxed{w} \end{aligned}$$

$$X \quad \text{⑩ } \neg y \quad \equiv \quad \neg(\neg t \vee \neg p)$$

is false

Therefore  $\vdash \neg P$   
is True

#### 4. Select all statements that are true.

- F**a) Creating a machine that thinks like a human is definitional of the field of artificial intelligence
- T**b) Anytime search continues to search for solutions after finding the first solution
- F**c) The most challenging task environments for AI are fully observable, single agent, deterministic, episodic, and discrete.
- T**d) The runtime cost of a depth-bounded depth-first search is  $O(B \cdot D)$ , where  $B$  is the branching factor and  $D$  is the depth bound
- F**e) Macro operators are guaranteed of reducing search costs because their use reduces the effective depth of search.
- T**f) Increased heuristic accuracy effects search costs by reducing the effective branching factor of search.
- T**g) Logical state estimation is the process of updating the belief state as new percepts arrive

## 5. Select all statements that are true.

- F**a) WalkSAT conducts an iterative deepening depth first search in pursuit of a proof of satisfiability
- F**b) Modus Ponens is the sole basis of a complete inference algorithm when paired with iterative deepening
- T**c) The path between a start state and a descendant state M can be recovered through M's SearchNode parent link, and subsequent ancestor links -- this mitigates redundancy in path storage
- T**d) Nondeterministic algorithms can be slow due to search, but they can be elegant and simply stated too, and machine learning can speed them up
- F**e) Heuristic admissibility applies straightforwardly to utility-driven search
- F**f) The generalized arc consistency (GAC) procedure is guaranteed to find one or more solutions to any n-ary constraint satisfaction problems
- T**g) In contrast to offline search, online search interleaves computation and action