

Homework Week 11

1. Give a valid interpretation in first-order logic of

"Every martian can fool some of the people all of the time (and these can be different subsets of people for each martian)"

Use both ForAll (\forall) and Exists (\exists) quantifiers, and assume predicates Martian($?v$), Person($?v$), Time($?v$), and Fools($?v_1, ?v_2, ?v_3$), where the first three are probably clear, and the latter is $?v_1$ fools $?v_2$ at time $?v_3$.

ForAll(x), [Martian(x) \rightarrow Exists(y)[Person(y) AND ForAll(t)[Time(t) \rightarrow Fools(x,y,t)]]]

ForAll(x), Exists(y) ForAll(t) [Martian(x) \rightarrow Person(y) AND Time(t) \rightarrow Fools(x,y,t)]

2. Consider the following propositional KB

- | | | |
|----------------------------------------------|----------------------------------------------|-----------------------------------------|
| 1. handEmpty \rightarrow \sim holding-A; | 4. holding-A \rightarrow \sim handEmpty; | 7. on-A-B \rightarrow \sim clear-B; |
| 2. handEmpty \rightarrow \sim holding-B; | 5. holding-B \rightarrow \sim handEmpty; | 8. on-B-C \rightarrow \sim clear-C; |
| 3. handEmpty \rightarrow \sim holding-C; | 6. holding-C \rightarrow \sim handEmpty; | 9. on-C-D \rightarrow \sim clear-D |

(a) Give a single first-order rule to replace propositional rules 1-3. Show quantifiers. You can use “Exists” and “ForAll” (as in problem 1) instead of the usual symbols.

ForAllx, (handEmpty \rightarrow \sim holding(x))

(b) Give a single first-order rule that replaces propositional rules 4-6.

ForAllx, (holding(x) \rightarrow \sim handEmpty(x))

(c) Give a single first-order rule that replaces propositional rules 7-9. Show quantifiers.

ForAllx, ForAlly, (on(x, y) \rightarrow \sim clear(y))
ForAllx, ForAlly, (\sim on(x, y) \vee \sim clear(y))
ForAllx, ForAlly, (\sim (on(x, y) \wedge clear(y)))
 \sim (Existsx, Existsy, (on(x, y) \wedge clear(y)))

3. Given the axioms:

ontable(A)

\sim clear(A)

\sim above(?x1, ?y1) or below(?y1, ?x1)

\sim below(?x2, ?y2) or above(?y2, ?x2)

\sim on(?x3, ?y3) or above(?x3, ?y3)

\sim on(?x4, ?y4) or \sim above(?y4, ?z4) or above(?x4, ?z4)

clear(?x5) or on(B, ?x5)

\sim ontable(?x6) or \sim holding(?x6)

\sim ontable(?x7) or \sim on(?x7, ?y7)

A,B are constants

?x's, ?y's, and ?z's are (universally-quantified) variables

Give a *refutation resolution* proof of **below(A, B)**.

See next page

3. Given the axioms:

A, B are constants

?x's, ?y's, and ?z's are (universally-quantified) variables

$\text{ontable}(A)$
 $\sim \text{clear}(A)$
 $\sim \text{above}(\text{?x1}, \text{?y1}) \text{ or } \text{below}(\text{?y1}, \text{?x1})$
 $\sim \text{below}(\text{?x2}, \text{?y2}) \text{ or } \text{above}(\text{?y2}, \text{?x2})$
 $\sim \text{on}(\text{?x3}, \text{?y3}) \text{ or } \text{above}(\text{?x3}, \text{?y3})$
 $\sim \text{on}(\text{?x4}, \text{?y4}) \text{ or } \sim \text{above}(\text{?y4}, \text{?z4}) \text{ or } \text{above}(\text{?x4}, \text{?z4})$
 $\text{clear}(\text{?x5}) \text{ or } \text{on}(B, \text{?x5})$
 $\sim \text{ontable}(\text{?x6}) \text{ or } \sim \text{holding}(\text{?x6})$
 $\sim \text{ontable}(\text{?x7}) \text{ or } \sim \text{on}(\text{?x7}, \text{?y7})$

Give a *refutation resolution* proof of **below(A, B)**.

$[-\text{below}(A, B)] \quad [-\text{above}(\text{?x1}, \text{?y1}) \text{ or } \text{below}(\text{?y1}, \text{?x1})]$

$\{A/x1, B/y1\}$
 $-\text{above}(B, A) \quad [-\text{below}(\text{?x2}, \text{?y2}) \text{ or } \text{above}(\text{?y2}, \text{?x2})]$

$\{B/y2, A/x2\}$
 $-\text{below}(A, B) = [\text{ontable}(-\text{below}(A, B))] \quad [-\text{ontable}(\text{?x6}) \text{ or } -\text{holding}(\text{?x6})]$

$-\text{holding}(-\text{below}(A, B)) = -\text{holding}(-\text{below}(-\text{clear}(-\text{below}(A, B)))) \quad [\text{clear}(\text{?x5}) \text{ or } \text{on}(B, \text{?x5})]$

$-\text{holding}(-\text{below}(\text{on}(B, -\text{below}(A, B)))) \quad [-\text{on}(\text{?x4}, \text{?y4}) \text{ or } -\text{above}(\text{?y4}, \text{?z4}) \text{ or } \text{above}(\text{?x4}, \text{?z4})]$

$-\text{holding}(-\text{below}(-\text{above}(\text{on}(B, -\text{below}(A, B)))) \text{ or } \text{above}(\text{on}(B, -\text{below}(A, B)))) \quad [-\text{on}(\text{?x3}, \text{?y3}) \text{ or } \text{above}(\text{?x3}, \text{?y3})]$

$-\text{holding}(-\text{below}(\{\}\))$

4. Show the result of resolving $P(?y, ?x, B, ?y)$ or $Q(?x, ?y, ?x, A)$ with $\sim P(?z, ?z, ?w, A)$.

$Q(A, A, A, A)$

$\{z/y, y/A, w/B, x/A\}$