

### Questions

A transformation of the data on  $x_i$  and  $y_i$  (like taking their logarithm) changes the interpretation of the slope parameter  $\beta$ .

- (a) Show that in the regression model  $\log(y_i) = \alpha + \beta \log(x_i) + \varepsilon_i$ , the elasticity of  $y$  with respect to  $x$  is equal to  $\beta$  (that is, does not depend on the values of  $x_i$  and  $y_i$ ).
- (b) Determine the elasticity of  $y$  with respect to  $x$  in the model  $y_i = \alpha + \beta \log(x_i) + \varepsilon_i$ .
- (c) Determine the elasticity of  $y$  with respect to  $x$  in the model  $\log(y_i) = \alpha + \beta x_i + \varepsilon_i$ .

### Note

As usual in this MOOC, 'log' denotes the natural logarithm, with base  $e \approx 2.71828$ .

On calculators this is often written as  $\ln(x)$ , but we use the notation  $\log(x)$ .

The derivative of  $\log(x)$ , with base  $e$ , is  $1/x$ .