

# **A Spatio-Temporal Betweenness Centrality Measure for the Micro-Scale Estimation of Pedestrian Traffic**

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# Context

## Spatio-Temporal Analysis of Terrorism Vulnerability: A Case Study of Central Tokyo, Japan

A Dissertation Submitted to  
the Graduate School of Life and Environmental Sciences,  
the University of Tsukuba

in Partial Fulfillment of the Requirements  
for the Degree of Doctor of Philosophy in Science  
(Doctoral Program in Geoenvironmental Sciences)

Konstantin GREGER

# Stationary Building Population

中央東口  
Central East Exit  
直進 中央西口  
Straight ahead Central West Exit

14 山手線

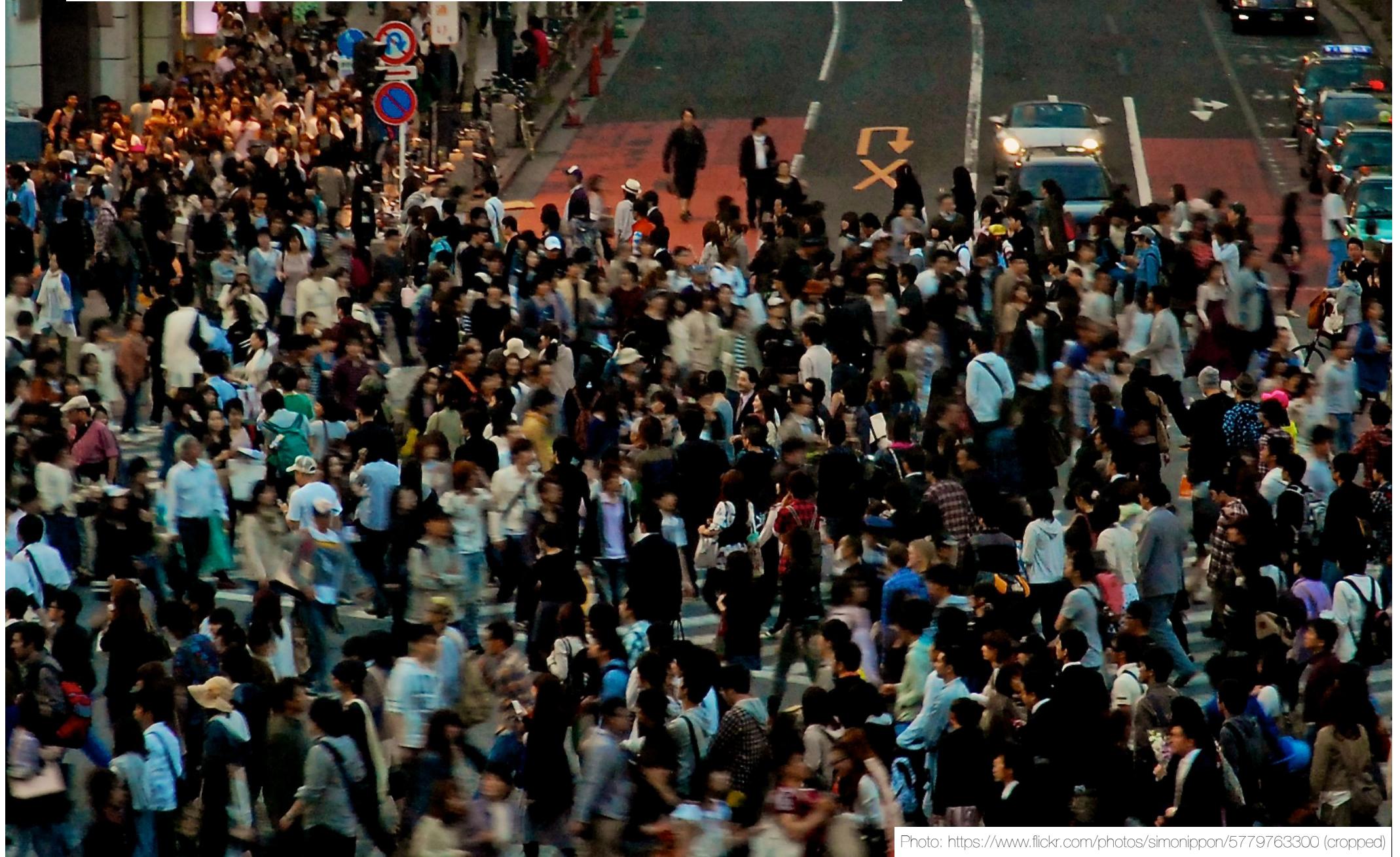
原宿・渋谷・品川方面

Harajuku, Shibuya & Shinagawa

# Mobile Railway Population



# Mobile Pedestrian Population



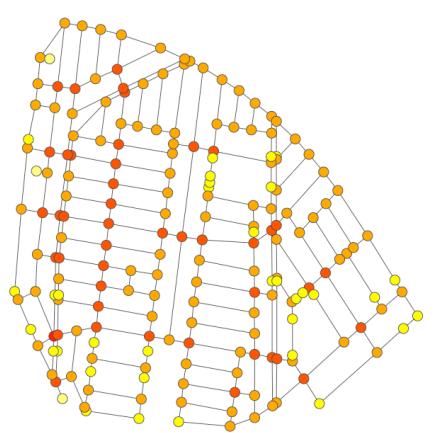
# **Part 1:**

## Spatial Graph Centrality Analysis

# Graph Centrality Measures

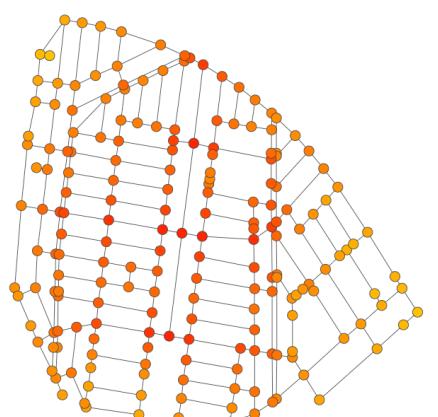
Degree  
centrality

$$C_D(v) = \deg(v)$$



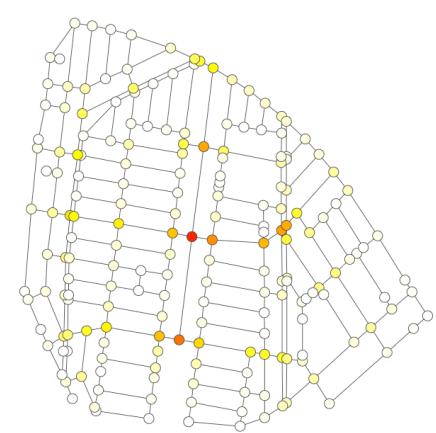
Closeness  
centrality

$$C_C(v) = \sum_{t \in V \setminus v} 2^{-d_G(v,t)}$$



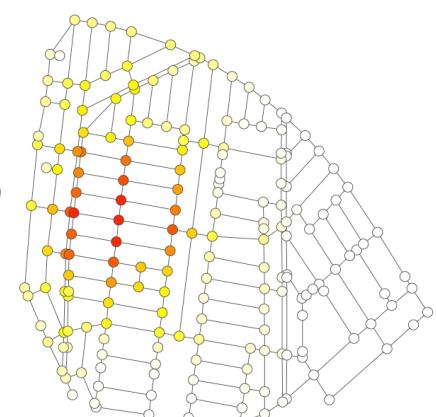
Betweenness  
centrality

$$C_B(v) = \sum_{s \neq v \neq t \in V} \frac{\sigma_{st}(v)}{\sigma_{st}}$$



Eigenvector  
centrality

$$C_E(v) = \frac{1}{\lambda} \sum_{t \in G} a_{v,t} C_E(t)$$



# Betweenness Centrality Measure

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Number of shortest paths from all vertices to all other vertices that pass through that node

Originated in social network analysis (BAVELAS 1948; SABIDUSSI 1966; ANTHONISSE 1971; FREEMAN 1977, 1979)

Original implementations suffered from  $\mathcal{O}(n^3)$

Improved algorithm by BRANDES (2001) reduced complexity to  $\mathcal{O}(nm + n^2 \log n)$  and  $\mathcal{O}(n+m)$

Does not account for topological and spatial impedance (e.g. distance, angularity, ...)

# Spatial Weighted Betweenness Centrality Measure

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Implementation by SEVTSUK & MEKONNEN (2012) in  
*Urban Network Analysis Toolbox* (for Esri ArcGIS)

Building on previous efforts in the area of spatial network analysis (MARTIN & MARCH 1971; HILLIER & HANSON 1984; PORTA, CRUCITTI ET AL., 2005)

Allows vertices to be weighted according to particular characteristics (e.g. volume, population, importance)

Does not account for temporal differences in real-world applications

# Spatio-Temporal Betweenness Centrality Measure

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Introducing the spatio-temporal betweenness centrality measure as

$$C_{STB}^r(i,t) = \sum_{j \neq k \in \{G \setminus i | \delta_{jk} \leq r\}} \frac{\sigma_{jk}(i)}{\sigma_{jk}} \cdot w(j,t) ,$$

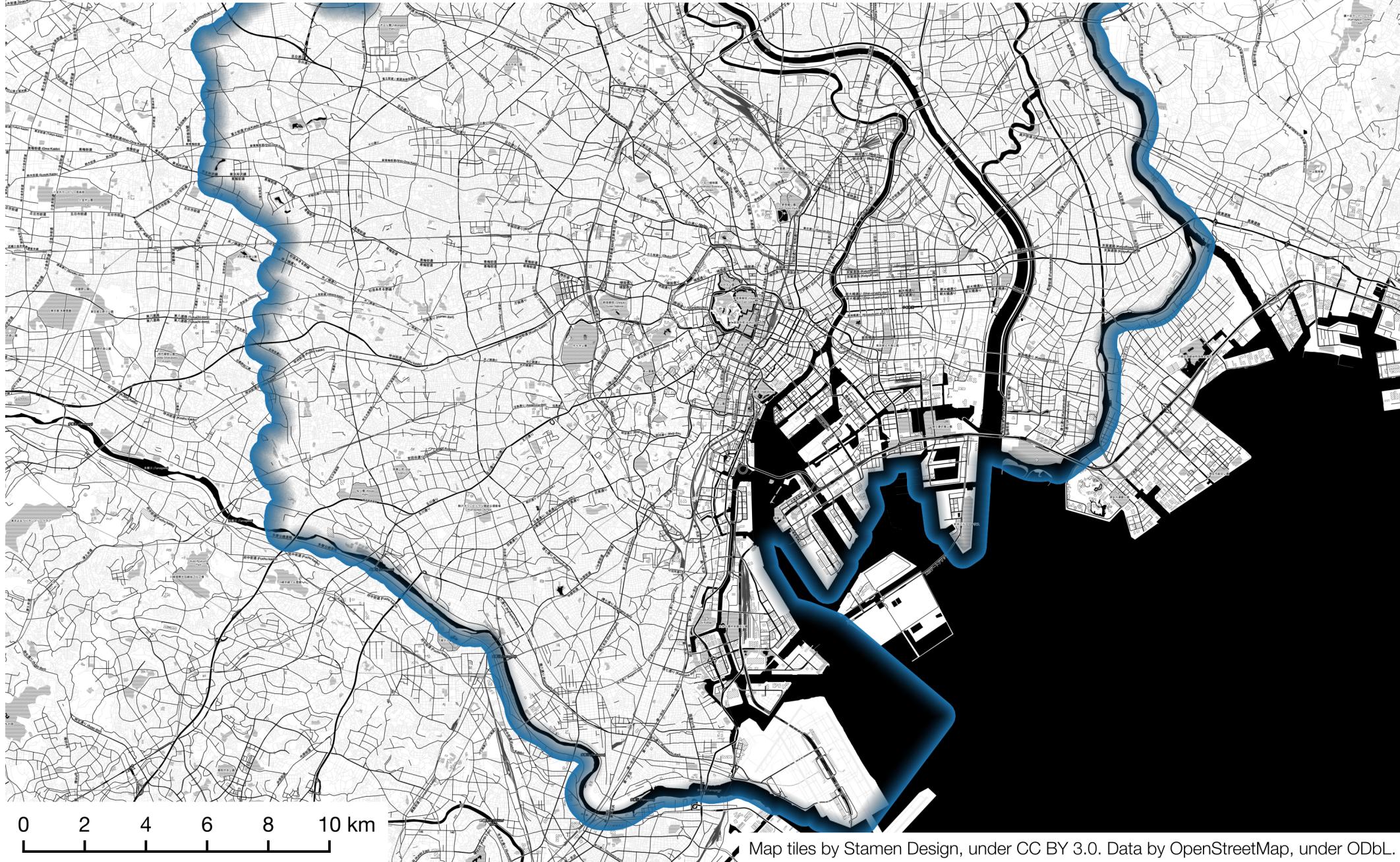
where  $\sigma_{jk}(i)$  is the number of shortest paths between vertices  $j$  and  $k$  passing through vertex  $i$ ,  $\sigma_{jk}$  is the total number of shortest paths between vertices  $j$  and  $k$ ,  $w_{j,t}$  is the weight of vertex  $j$  at time  $t$ , with network distance  $\delta_{jk}$  between vertices  $j$  and  $k$  within network radius  $r$

## **Part 2:**

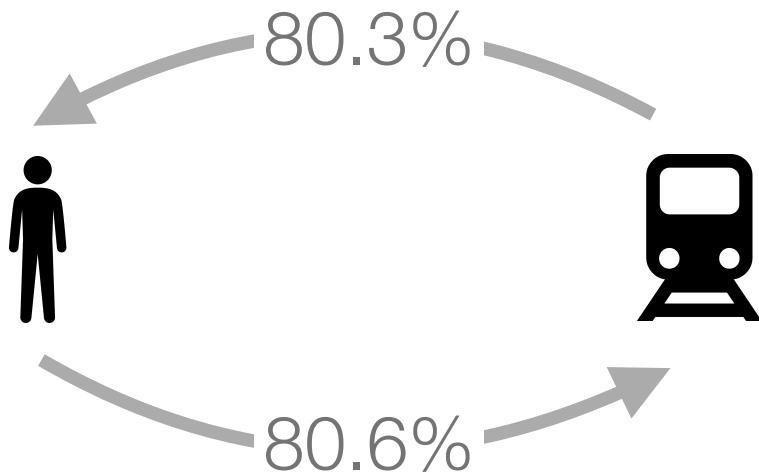
### Case Study



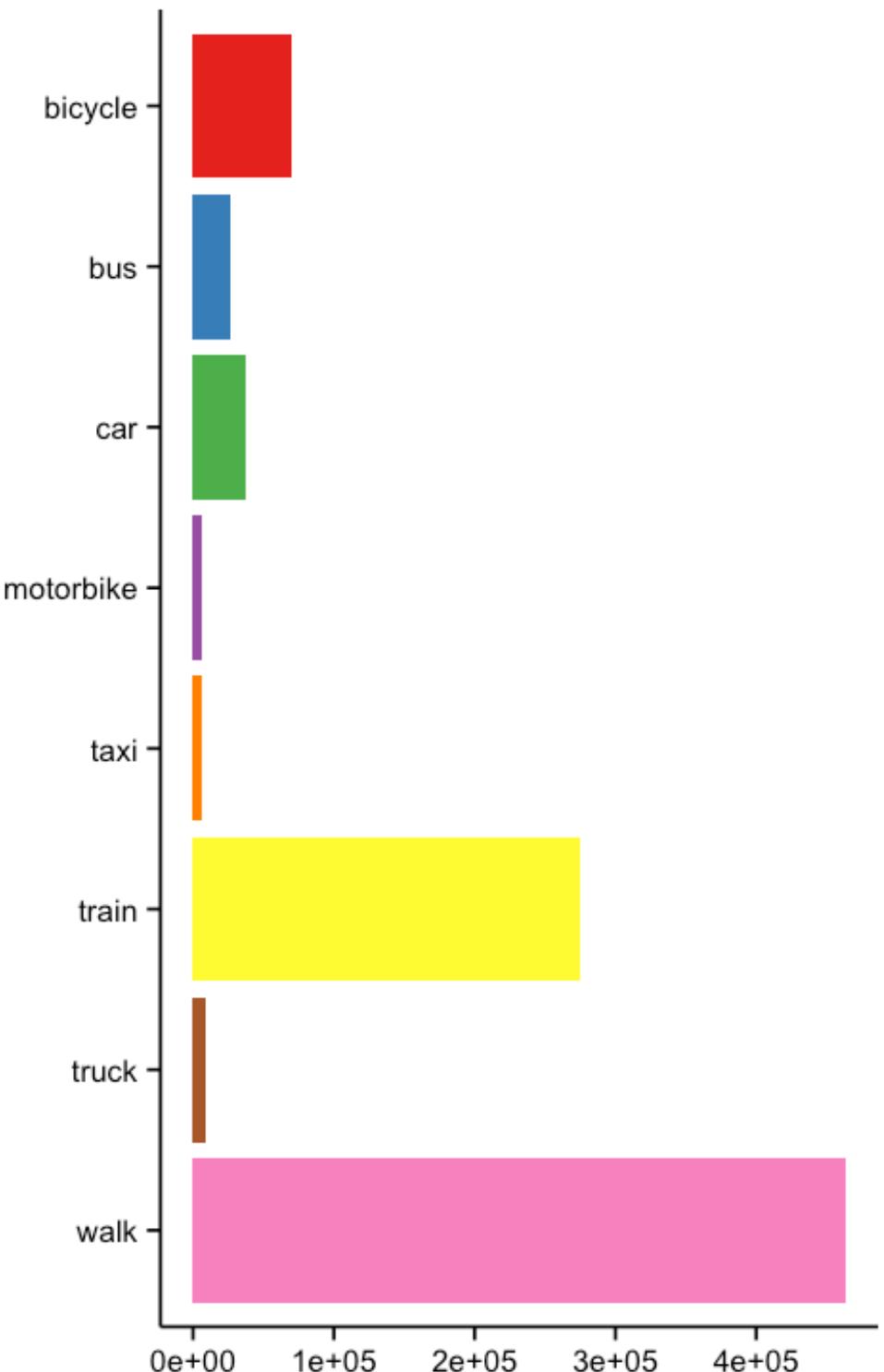
# Study Area: The 23 Special Wards of Tokyo



# Use Case: Pedestrian Traffic



Datasource:  
*PersonFlow* data by CSIS at the  
University of Tokyo



# Calculation Process

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- 1) Calculation of building population at each time  $t_i$
- 2) Determination of building access
- 3) Calculation of train station usage at each time  $t_i$
- 4) Calculation of road network betweenness centrality at each time  $t_i$

# Building Population and Building Access

Stationary building population algorithm explained in GREGER (2015)

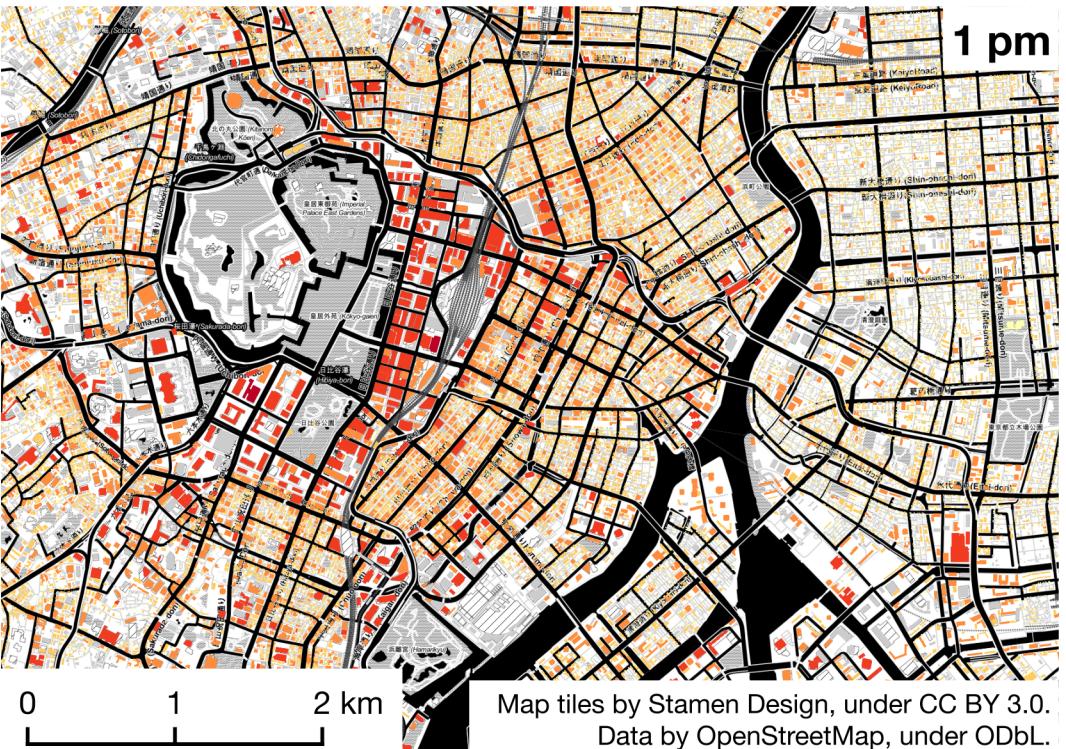
Building access from closest road segment



## Building Population

(simulated)

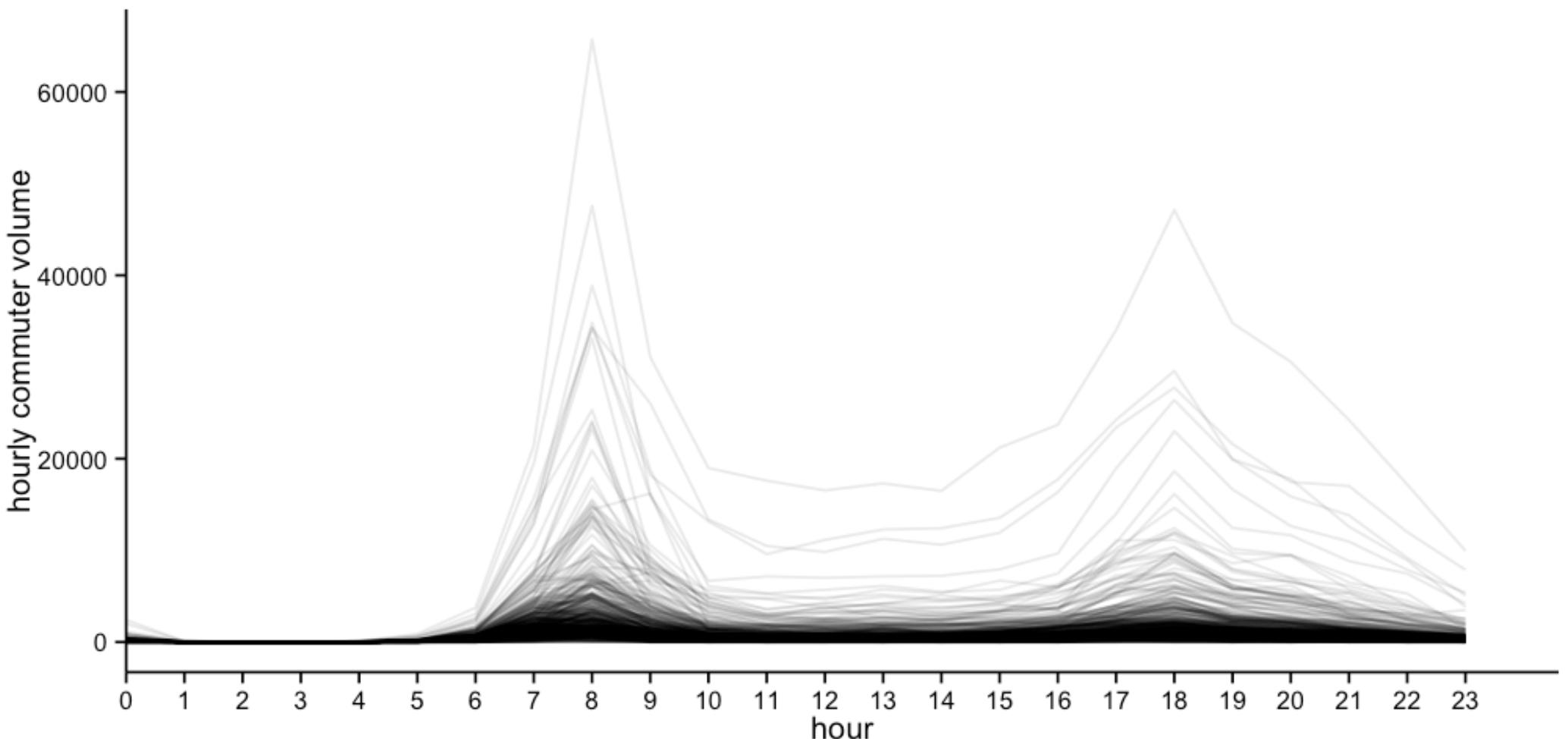
- no data
- < 10 ppl.
- < 100 ppl.
- < 1,000 ppl.
- < 10,000 ppl.
- > 10,000 ppl.



# Train Station Usage

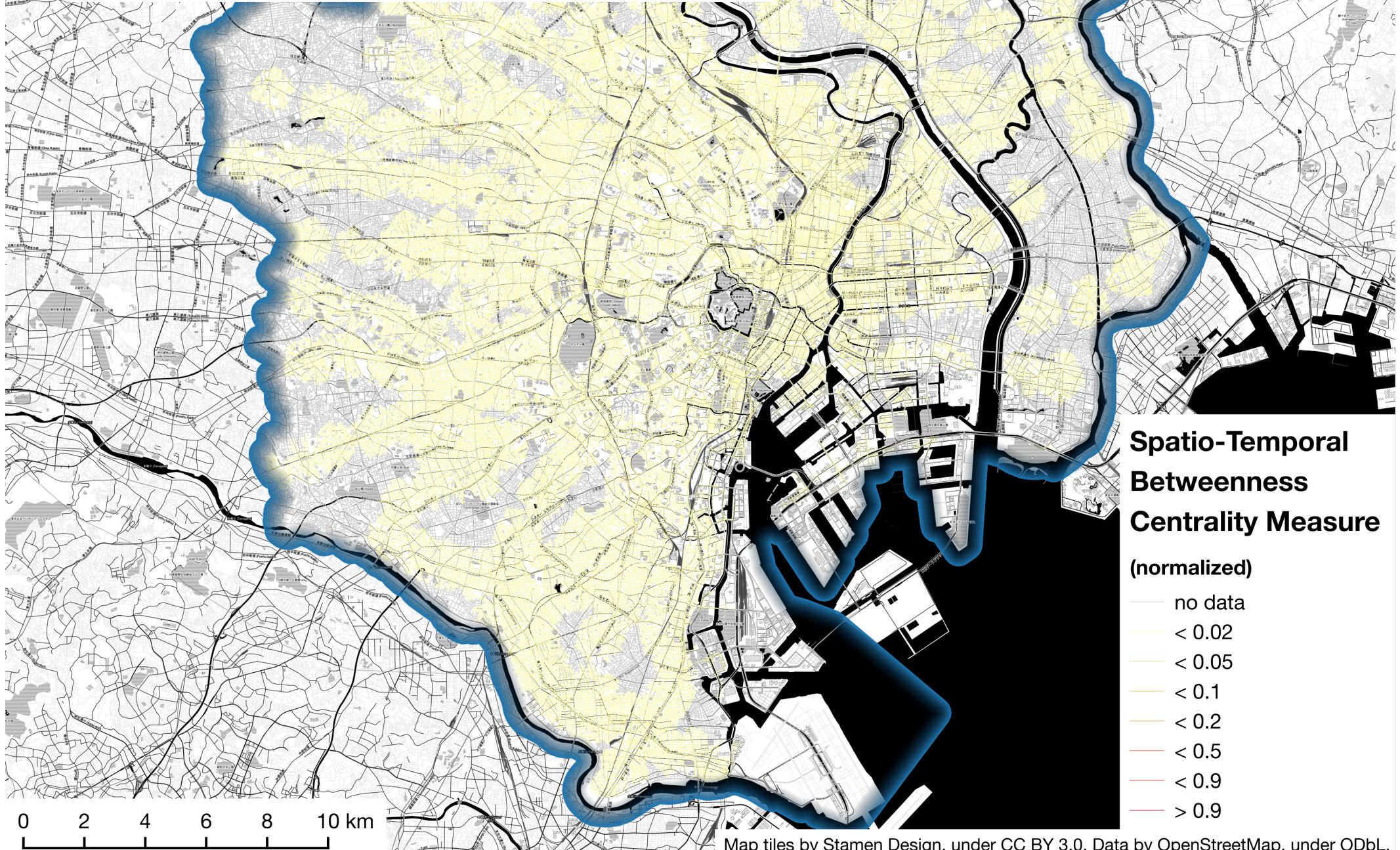
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Derivation of hourly number of passengers using daily train station passenger volumes and *PersonFlow* data



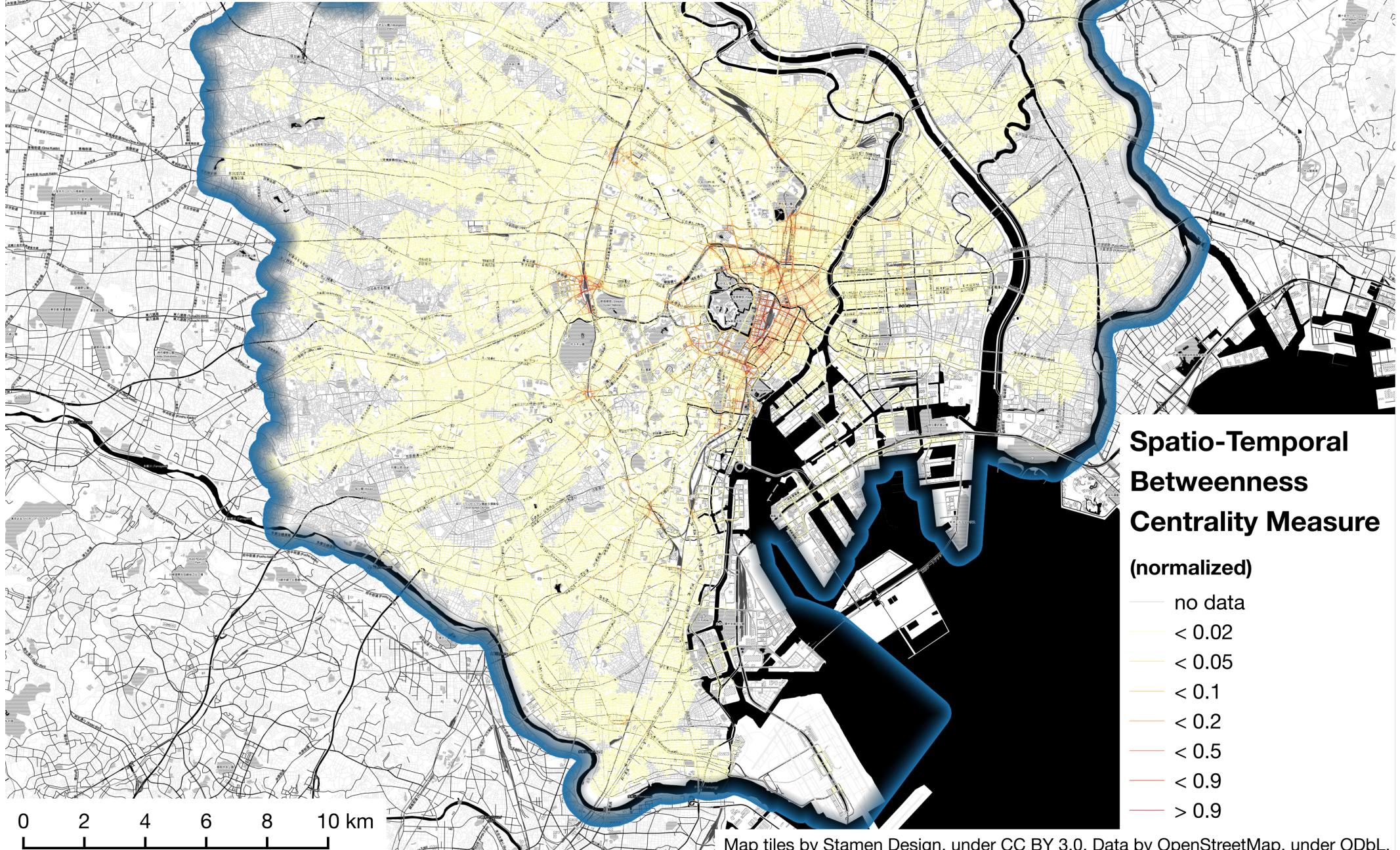
4 am

# Spatio-Temporal Network Betweenness Centrality

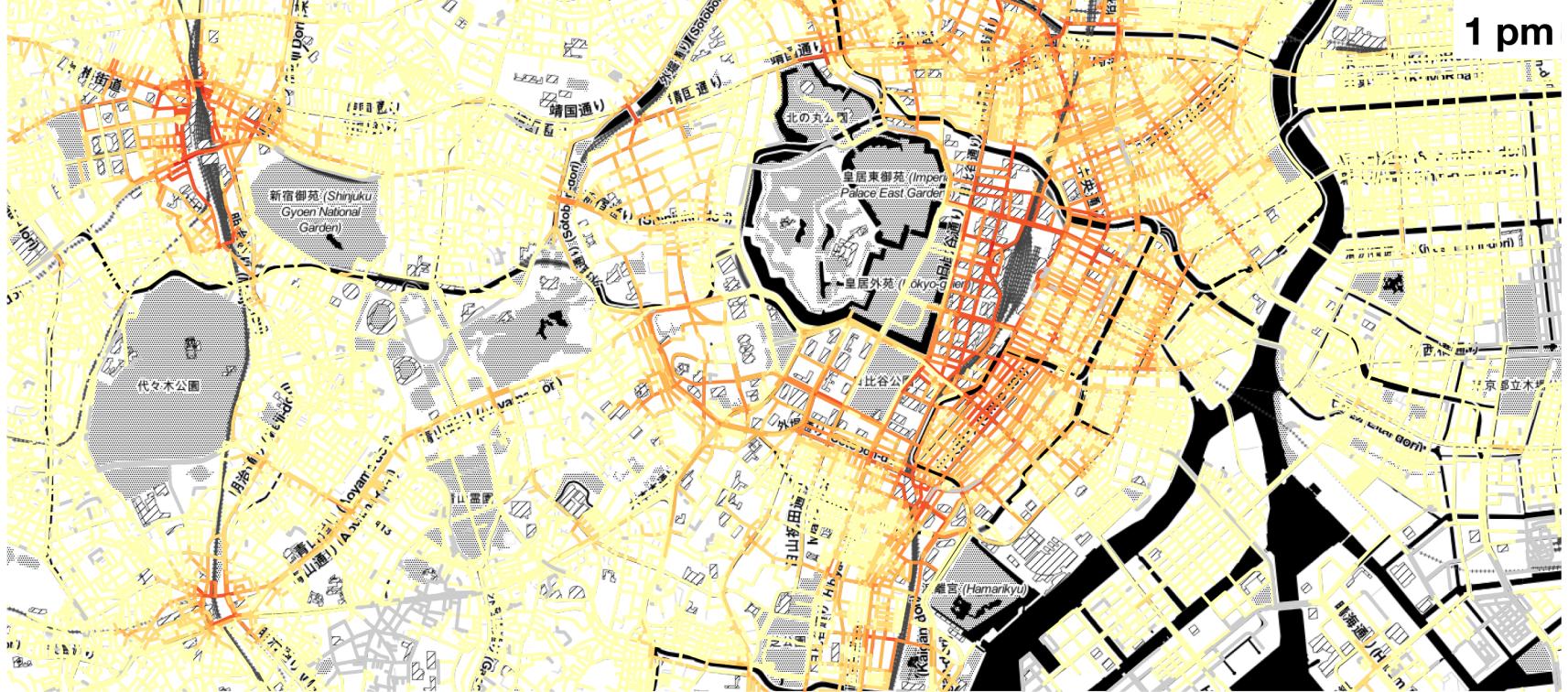


9 am

# Spatio-Temporal Network Betweenness Centrality



# STBC Details

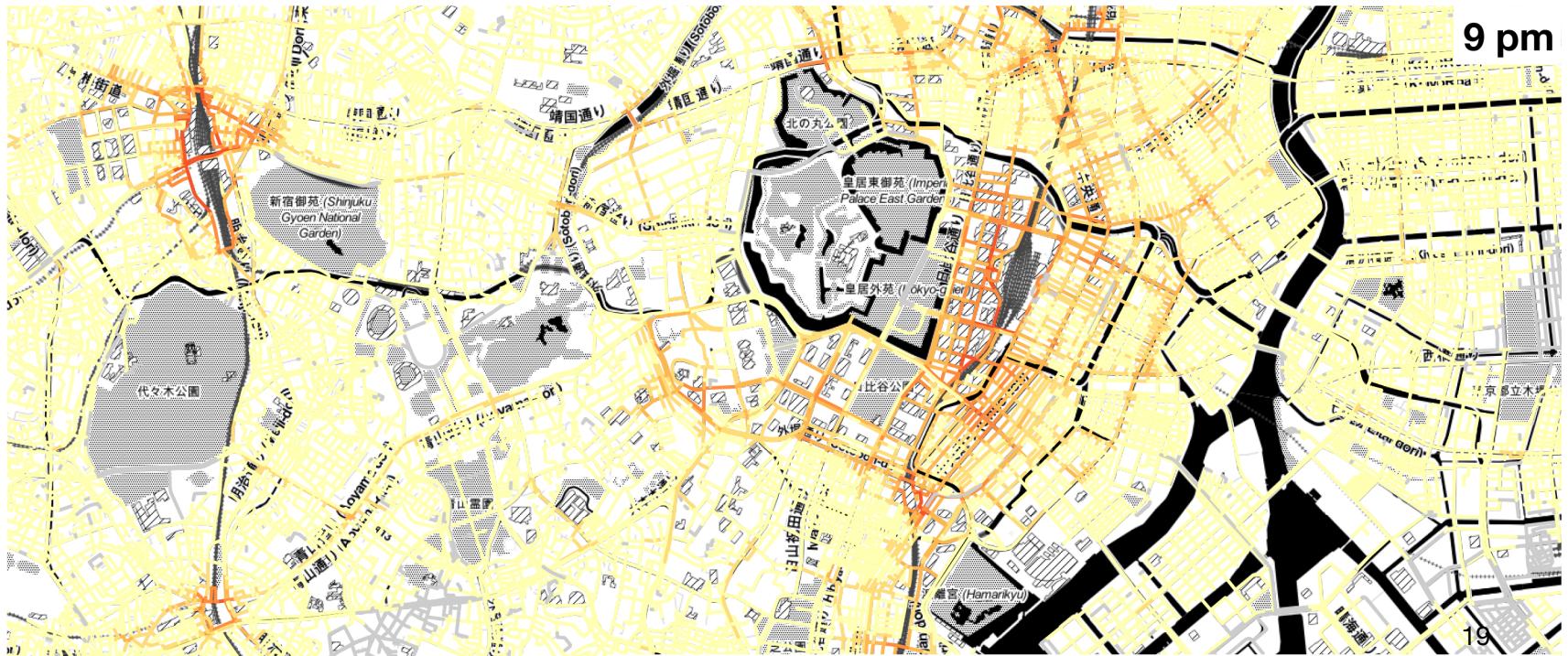


## Spatio-Temporal Betweenness Centrality Measure

(normalized)

- no data
- < 0.02
- < 0.05
- < 0.1
- < 0.2
- < 0.5
- < 0.9
- > 0.9

0 1 2 km



Map tiles by Stamen Design, under CC BY 3.0. Data by OpenStreetMap, under ODbL.

# Summary

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Extension of existing betweenness centrality measures

Allows for fine-grained micro-scale spatio-temporal analysis of centrality of transportation networks

Results useful for city planning, retail management and emergency preparedness

# Shortcomings & Outlook

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Rather data intensive

→ Use of OSM and other open data sources

Proprietary implementation for Esri ArcGIS

→ Implementations in Python (for use in QGIS) and R

Error-prone assignment of buildings' network access

→ ? (entrance data)

# References

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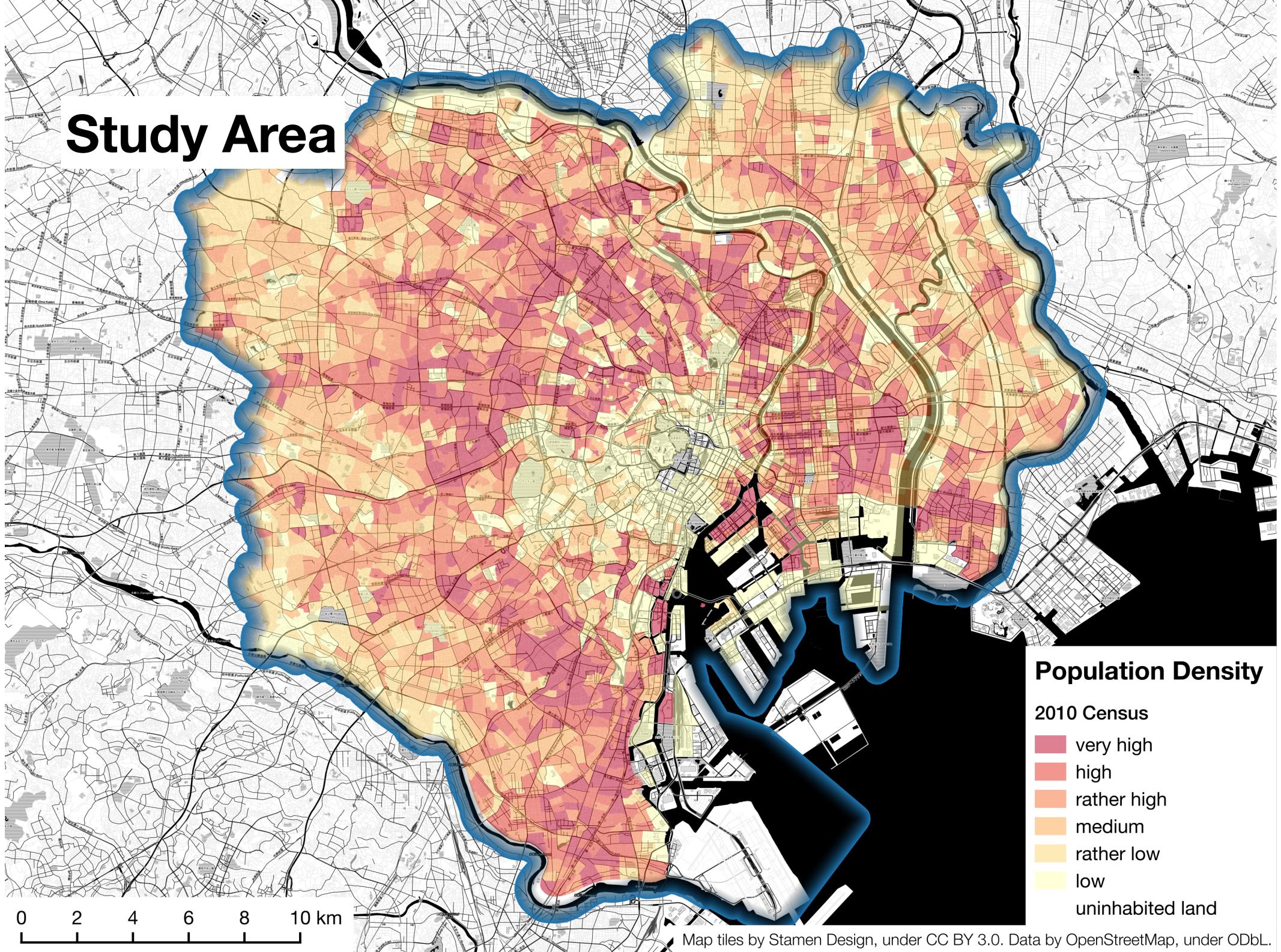
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# **Thank you for your attention**

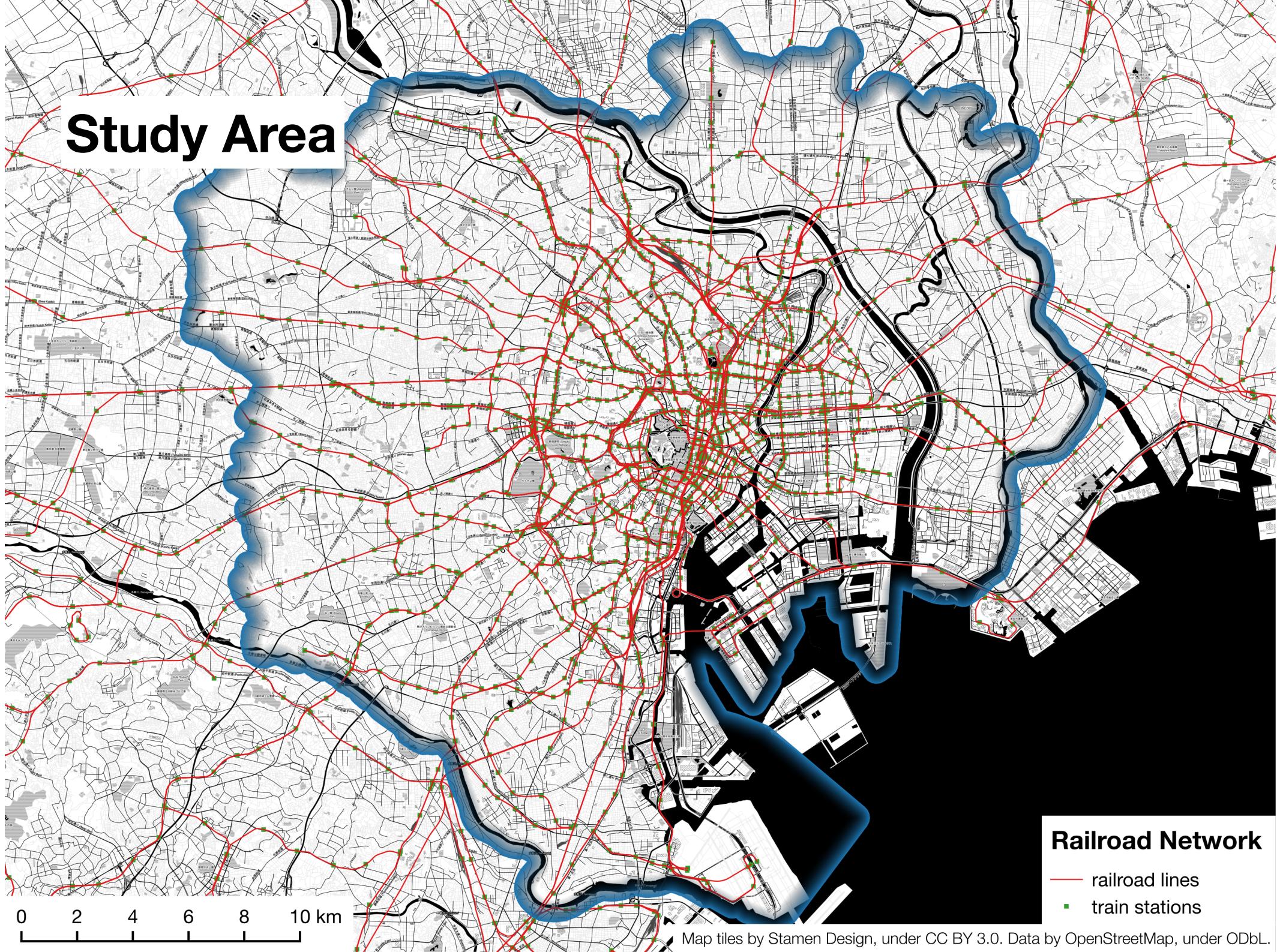
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@kogreger  
[www.konstantingreger.net](http://www.konstantingreger.net)  
[github.com/kogreger/stbc](https://github.com/kogreger/stbc)

# Study Area



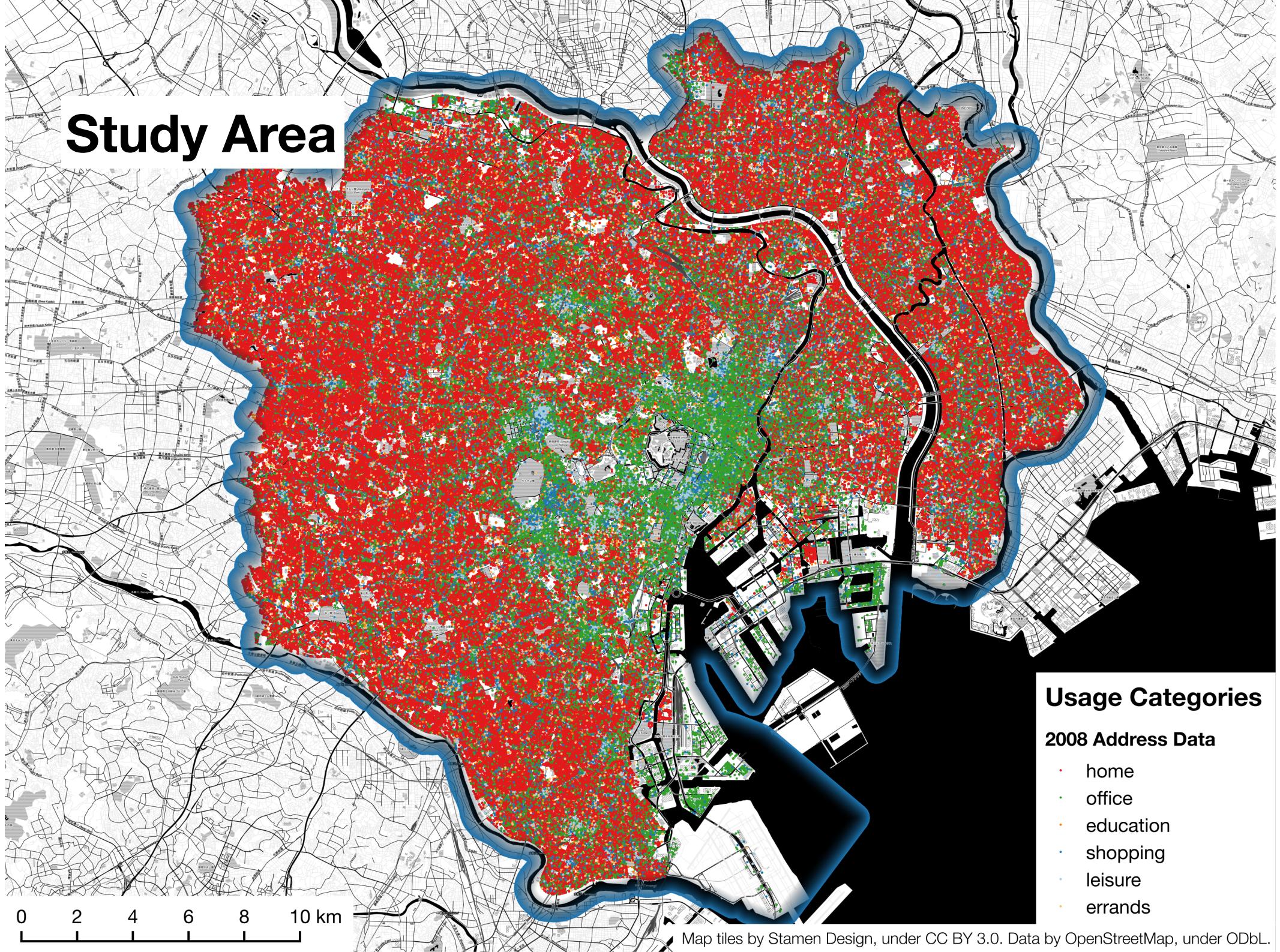
# Study Area



0 2 4 6 8 10 km

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# Study Area



## Usage Categories

### 2008 Address Data

- home
- office
- education
- shopping
- leisure
- errands

0 2 4 6 8 10 km

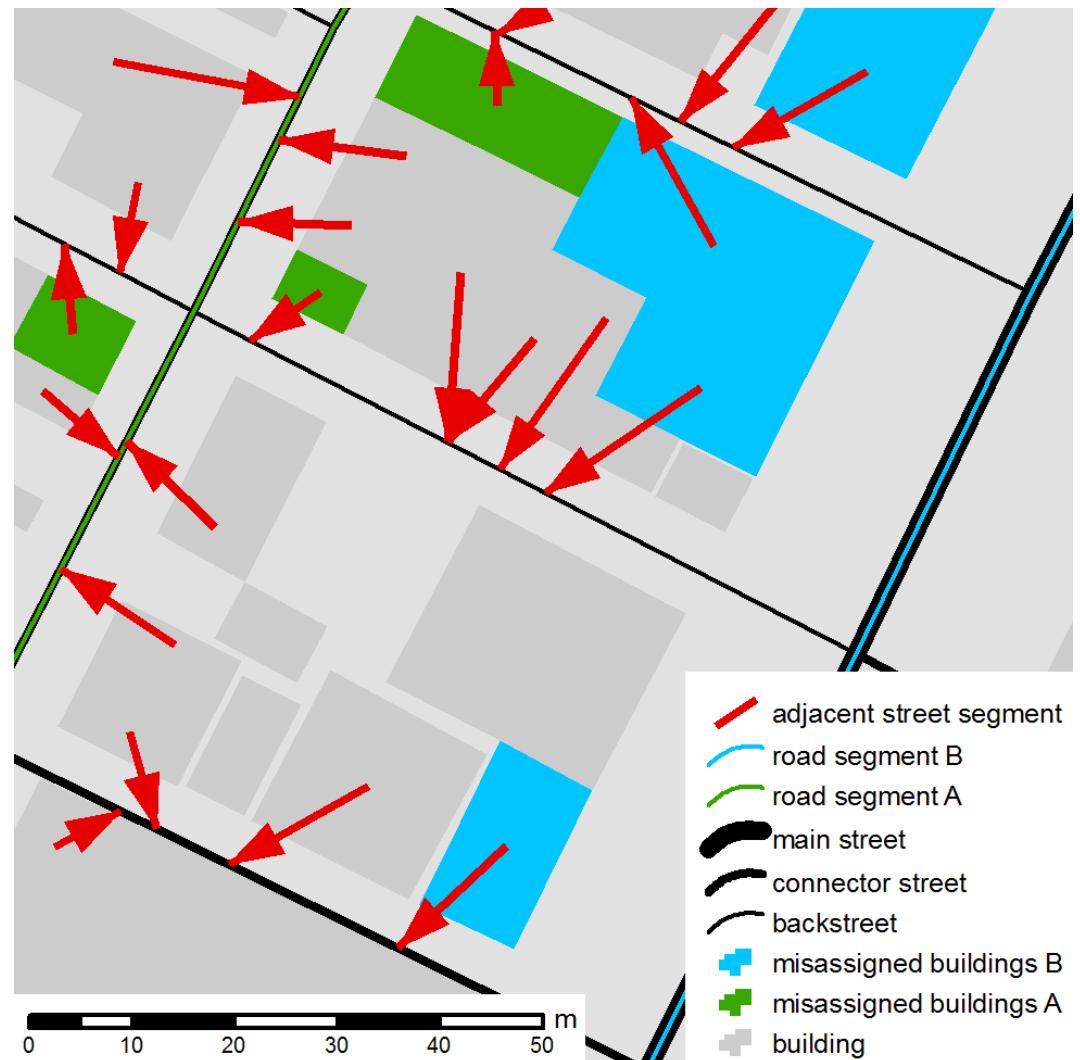
Map tiles by Stamen Design, under CC BY 3.0. Data by OpenStreetMap, under ODbL.

# Building Access

Building access from closest road segment

Introduces errors:

- misassignments
- multiple entrances



# Data Dimensions

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## Study area

627 km<sup>2</sup>

## Train stations

~ 3,656 platforms

~ 457 separate stations

## Buildings

~ 260,000 buildings

19 attributes per building  
usage per building known  
hourly population known

## *PersonFlow* data

~ 600,000 people

24 h \* 60 min = 1,440 min

~  $834 \times 10^6$  in total

~  $217 \times 10^6$  in study area

12 attributes per point

## Road network

~240,000 vertices

29 attributes per vertex

~ 350,000 edges

69 attributes per edge