

1. Consider the expectation  $I = E[\exp(\sqrt{U})]$  where,  $U \sim U(0, 1)$ . Use the following antithetic method to approximate  $I$ :

$$\hat{I}_M = \frac{1}{M} \sum_{i=1}^{M/2} \hat{Y}_i \text{ where } \hat{Y}_i = \exp(\sqrt{U_i}) + \exp(\sqrt{1 - U_i}) \text{ with } U_i \sim U(0, 1).$$

Take the values of  $M$  to be  $10^2, 10^3, 10^4$  and  $10^5$ . Determine the 95% confidence interval for  $I_M$  for all the four values of  $M$  that you have taken.

2. Present the results that you have obtained in Question 1 of Lab 06 and Question 1 of Lab 07 in a tabular form. Your table must consist of the values of  $\hat{I}_M$  (using two methods), 95% confidence intervals for  $I$  (from two methods), and the ratio of widths of both the intervals. How do the values of  $I_M$  and  $\hat{I}_M$  compare with the actual value of  $I$ ?
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***Submission Deadline: October 11, 2023, 11:50 PM***