- 1. Consider the multivariate normal distribution  $\boldsymbol{X} \sim N_2(\boldsymbol{\mu}, \, \boldsymbol{\Sigma}).$ 
  - (a) Taking  $\boldsymbol{\mu} = \begin{pmatrix} 5 \\ 8 \end{pmatrix}$  and  $\boldsymbol{\Sigma} = \begin{pmatrix} 1 & 2a \\ 2a & 4 \end{pmatrix}$  and for each of the four values of a = -0.5, 0, 0.5, 1, generate 10,000 sample from the distribution of  $\boldsymbol{X} = \begin{pmatrix} X_1 \\ X_2 \end{pmatrix} \sim N_2(\boldsymbol{\mu}, \boldsymbol{\Sigma}).$
  - (b) For the cases a, plot the 2-dimensional histogram (please see https://plotly.com/python/2D-Histogram/) based on 10,000 simulated values of X.
  - (c) Also, draw the contour plots of the actual densities on the histograms.

Submission Deadline: September 06, 2023, 11:50 PM