

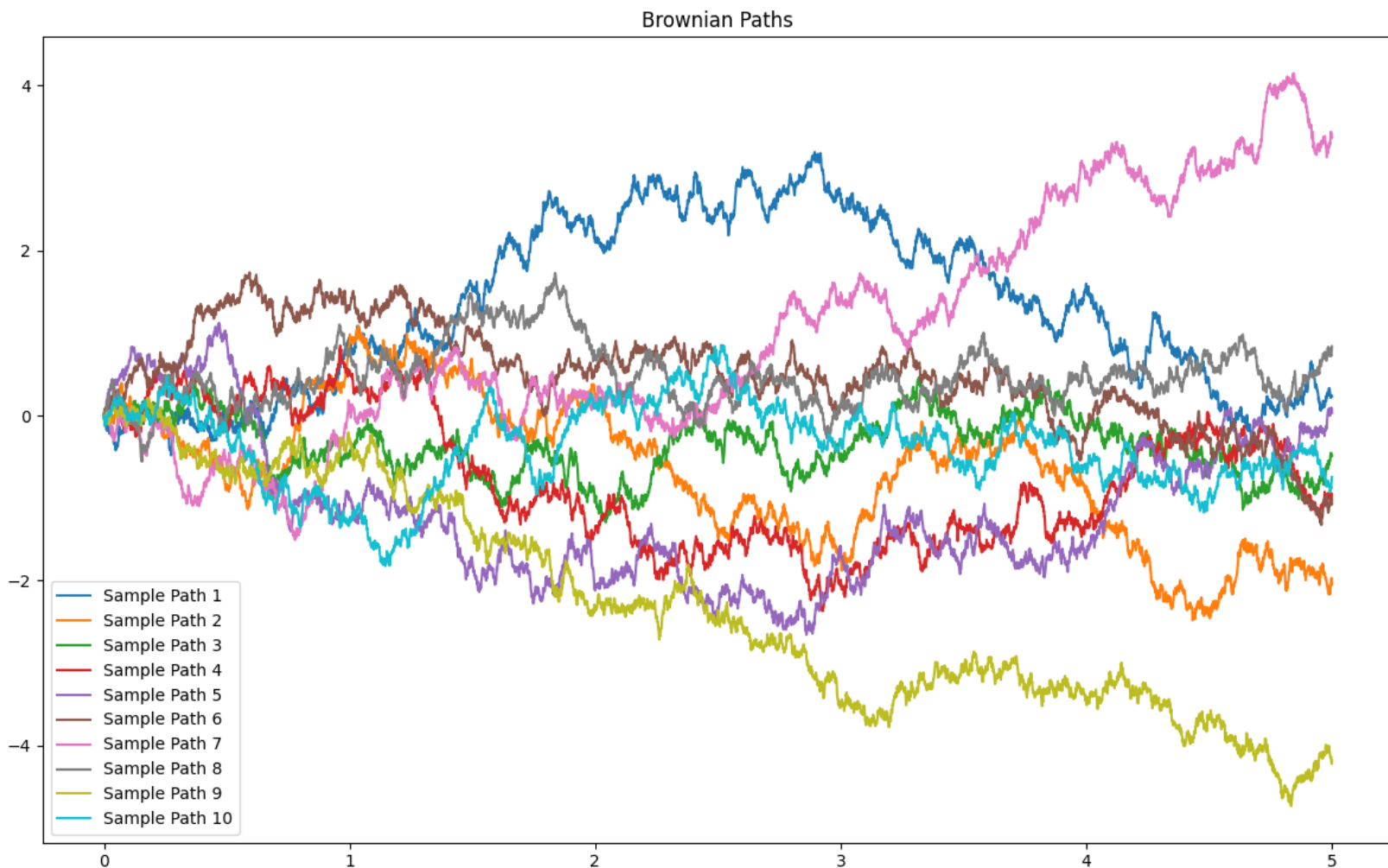
Answer 1.

$$f(x) = \sum_{k=1}^3 \pi_i \frac{1}{\sigma_i} \phi\left(\frac{x - \mu_i}{\sigma_i}\right), \quad x \in \mathbb{R},$$

Each of the above individual functions are $N(\mu_i, \sigma_i^2)$.

So, using the mixed distribution generator, the average of generated random numbers is -0.33196815591573997.

Answer 2.

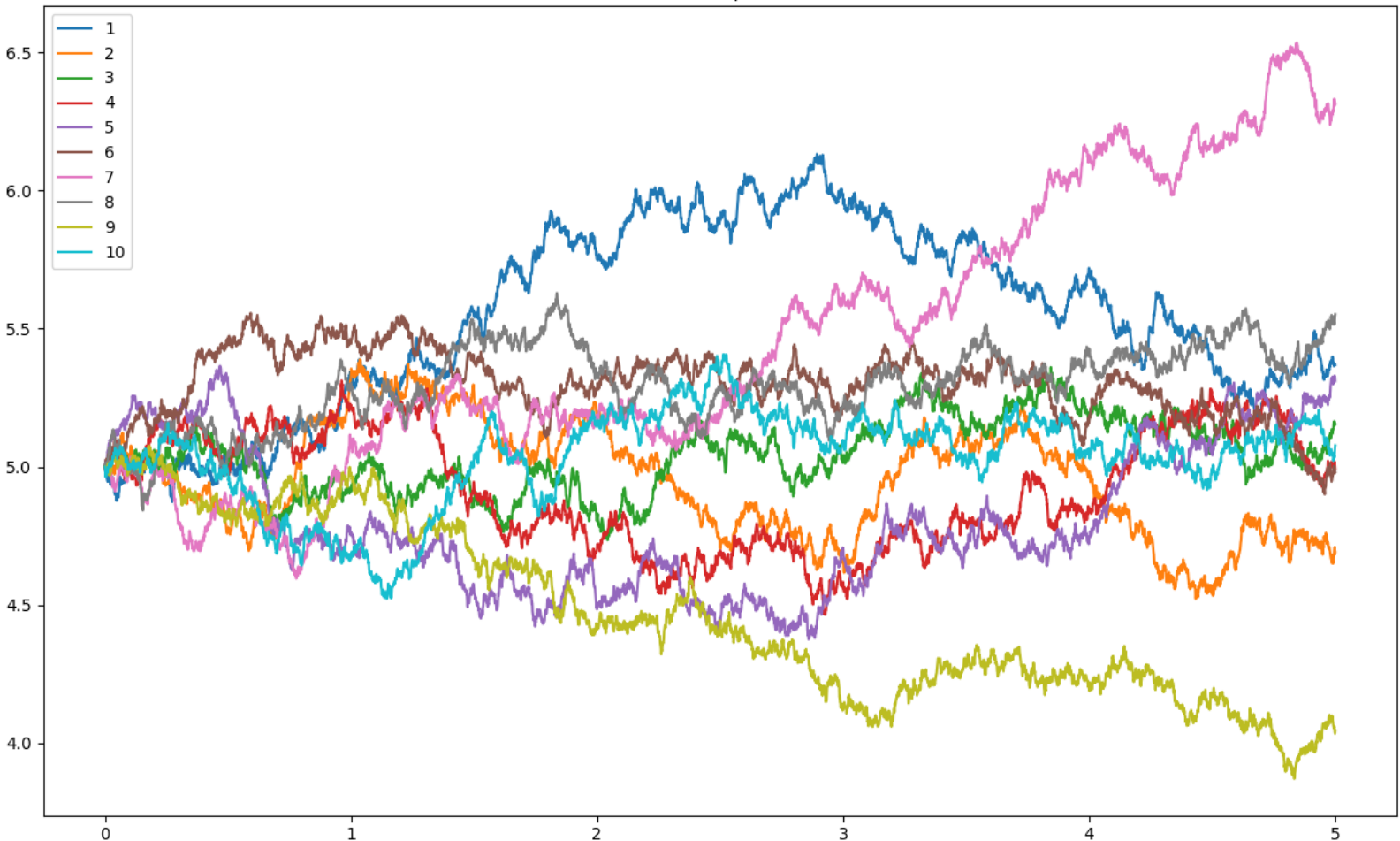


Estimated value of $E[W(2)]$ from the 10 paths that you generated is -0.3085961558649597.

Estimated value of $E[W(5)]$ from the 10 paths that you generated is -0.5048175025828556.

Answer 3.

Brownian motion ($BM(\mu, \sigma^2)$) discretization



Estimated value of $E[X(2)]$ from the 10 paths that you generated is 5.027421153241297.

Estimated value of $E[X(5)]$ from the 10 paths that you generated is 5.148554749227107.

Such an estimated value is evident from the initial value of X i.e $X(0)$ which is 5.