

SymPy Cheat Sheet

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Notebook (and commandline)

Sympy Packages: `from sympy import`

Declare Symbols: `x = symbol('x')`

Declare Variables: `x = var('x')`

Substituting Symbols: `expression.subs(old,new)`

e.g. `x+x.subs(x,1)=x+1`

Sympy Help: `help()`

Numerical types

Integers: $\mathbb{Z} = \text{integer}(x)$ e.g. `-2 0 1 10^100`

Decimals: $\mathbb{R} \approx \text{float}(x)$ e.g. `2.58`

Rationals: $\mathbb{Q} = \text{rational}(x,y)$ e.g. `1/2`

Complex: $\mathbb{C} \approx \text{complex}(expr)$ e.g. `1+i 2.5-3*i`

Arithmetic

`ab = a*b` $\frac{a}{b} = a/b$ `a^b = a**b` $\sqrt{x} = \text{sqrt}(x)$

$\sqrt[n]{x} = x^{(1/n)}$ or `mpmath.root(x,n)` $|x| = \text{abs}(x)$

$\log_b(x) = \text{log}(x,b)$ $\log_1 0(x) = \text{log10}(x)$

`x!=factorial(x)` $\gamma(x) = \text{gamma}(x)$

Constants: $\pi = \text{mpmath.pi}$ $e = \text{mpmath.e}$

$i = j$ $\infty = \text{inf}$ $\phi = \text{mpmath.phi}$

Approximate to n digits: `mpmath.dps=n`

Basic Functions

Rationalizing the denominator: `radsimp(expr)`

Common Denominator: `ratsimp(expr)`

Trigonometry: `sin cos tan sec csc cot`

Inverse Trigonometric: `asin acos atan asec acsc acot`

Radians to Degrees: `degrees(x)`

Degrees to Radians: `radians(x)` Exponential Function:

`e^x = mpmath.exp(x)`

Algebraic Expressions

Expanding: `(expression).expand()`

Simplifying: `simplify(expression)`

Solving Polynomials: `solve(f(x),x)`

Solving Systems: `solve([f(x,y),g(x,y)],[x,y])`

e.g. `solve([x + 5*y - 2, -3*x + 6*y], [x, y])`

Sum: `a + b = a._add_(b)=Add(a,b)`

$$\sum_{x=k}^n f(x) = \text{nsum}(\text{lambda } x: f(x), [k, n])$$

Calculus

$\lim_{x \rightarrow a} f(x) = \text{limit}(f(x), x, a)$

$\lim_{x \rightarrow a^-} f(x) = \text{limit}(f(x), x=a, \text{dir}='-')$

$\lim_{x \rightarrow a^+} f(x) = \text{limit}(f(x), x=a, \text{dir}='+')$

$\frac{d}{dx}(f(x)) = \text{diff}(f(x), x)$

$\frac{\partial}{\partial x}(f(x,y)) = \text{diff}(f(x,y), x)$

$\int f(x)dx = \text{integrate}(f(x), x)$

$\int_a^b f(x)dx = \text{integrate}(f(x), (x,a,b))$

Taylor polynomial, deg n about a : `f(x).series(x,n,a)`

Geometry

from `sympy.geometry import *`

Point: `a = Point(0, 0)` `Point.is_collinear(a, b, c)`

`l=line([Point(x1,y1), Point(x2,y2)])`

`t=triangle(a,b,c)`

`c=circle((x,y),r)`

`t.area, t.medians[a]`

`c.is_tangent(l), intersection(c,l)`

Graphing

2D Plot from a to b: `mpmath.plot([f(x),g(x)], [a,b])`

3D Plot (pylab only): `mpmath.splot(f(x), [a,b], [a,b])`

Zoom: `R` and `F`, Page Up and Down, Numpad `+` and `-`

Rotate View X,Y axis: Arrow Keys, `A,S,D,W`

Rotate View Z axis: `Q` and `E`, Numpad `7` and `9`

Rotate Ordinate Z axis: `Z` and `C`, Numpad `1` and `3`

View XY: `F1` View XZ: `F2` View YZ: `F3`

View Perspective: `F4` Reset: `X`, Numpad `5`

Toggle Axes Visible: `F5` Axes Colors: `F6`

Close Window: `ESCAPE` Screenshot: `F8`

Discrete math

`n! = factorial(n)` $\binom{x}{m} = \text{binomial}(x,m)$

Strings: e.g. `s = 'Hello' = "Hello" = ""+"He"+"llo"`

`s[0]='H' s[-1]='o' s[1:3]='el' s[3:]='lo'`

Lists: e.g. `[1,'Hello',x] = []+[1,'Hello']+x`

Tuples: e.g. `(1,'Hello',x)` (immutable)

Sets: e.g. `{1,2,1,a} = Set([1,2,1,'a']) (= {1,2,a})`

Linear algebra

from `sympy.matrices import *`

$\begin{pmatrix} 1 \\ 2 \end{pmatrix} = \text{Matrix} ([[1],[2]])$

$\begin{pmatrix} 1 & 2 \\ 3 & 4 \end{pmatrix} = \text{Matrix} ([[1,2],[3,4]])$

$\begin{vmatrix} 1 & 2 \\ 3 & 4 \end{vmatrix} = \text{M.det}() \quad \begin{vmatrix} 1 & 2 \\ 3 & 4 \end{vmatrix}^{-1} = \text{M.inv}()$

Dot Product: `v1.dot(v2)` Cross Product: `v1.cross(v2)`

Combining Matrices: `M1.row_join(M2), M1.col_join(M2)`

For an nxn matrix, Identity: `eye(n)`

Zeroes: `zeros(n)` Ones: `ones(n)`

Statistics

from `sympy.statistics import *`

Normal distribution: `N=Normal(mu,sigma)`

`N.mean, N.median, N.variance, N.stdev, N.pdf(), N.cdf()`

Random number generator: `N.random()`

Probability on an interval: `N.probability(a,b)`

Confidence interval for x confidence level: `N.confidence(x)`

Printing

LaTeX: `latex()`

MathML: `mathml()`

Python: `print python()`

Unicode: `pprint()`