

FRE-6971 Final Part 2 of 2, Spring 2023 (due 5/11/2023 by 8pm)

Your work for this final must be independent. Incomplete work is not a failure, but copying somebody else's work is.

Data:

'Constant_Maturity_ED.csv' in the 'Class Materials' folder contains constant-maturity Eurodollar rates produced to mitigate the impact of futures roll. There are 20 time series in the file: 3m future, 6m future.... 5y future rate on 3M LIBOR (ED8=2y, ED12=3y, ED16=4y, ED20=5y)

Historical samples:

1/1/2010 through 1/1/2014, Estimation Sample (A)

1/1/2014 through 1/1/2016 Signal Building Sample (B)

1/1/2016 through 1/1/2018, Testing Sample (C)

1. Use Sample A to compute 3 cointegrated butterflies of ED futures rates: [2y,3y,5y], [3y,4y,5y], [2y,3y,4y]. Weight on the belly of a butterfly is 1 for all combinations.
2. Let's define $z(t, \lambda)$ as $\{x(t) - \text{EMA}(x(t), \lambda)\}$ where $x(t)$ is a cointegrated butterfly at t . Use Sample B to construct the following forecasting models:
 - a. AR(1) model fitted to $z(t, \lambda = 0)$ (Signal 1), this is a constant mean case
 - b. AR(1) model fitted to $z(t, \lambda = 0.05)$ (Signal 2)
 - c. AR(1) model fitted to $z(t, \lambda = 0.1)$ (Signal 3)

Each model is estimated in a rolling 6m window, and forecast, $E[z(t+H)|t]$, is produced for $H=5$ days. Note that your forecast for the cointegrated butterfly at $t+H$ will be $E[z(t+H)|t] + \text{EMA}(t, \lambda)$ (we assume that EMA value won't change in H days).

IF YOU NEED TO SIMPLIFY: Carry out the estimation in the first 6m of Sample B, and keep forecasting model parameters unchanged.

3. EXTRA CREDIT: Can you suggest a method of combining Signals 1, 2 & 3? Call the combination (or mixture of signals) Signal 4.
4. Define one or two signal quality metrics, and explain clearly what you are implementing.
 - a. Apply signal quality metrics to Signals 1-3 (or Signals 1-4) in the last year of Sample B
 - b. Apply signal quality metrics to Signals 1-3 (or Signals 1-4) in Sample C
 - c. Compare and analyze your results across signals & samples