## CS204: Homework #7

Due on November 17, 2016 at 11:59pm

 $Prof. \ Sungwon \ Kang \ -- \ Section \ A$ 

20160051 Ohjun Kwon

C5204 HW#7 20160051 OhJun knon Pg 1/3 62 61 B(e) d(n) d(n2) X(U1) and X(n)=(e) NZ 1 1/2 di 7/2 63 53 Xe S 7/3 0/2 4, 74 43 0/2 02 24 715 45 05 43 45 715 7/5/ ab 451 7/3 4,  $\propto(\alpha)=1$ X(b) = 3 B((1)=51 d(()=5 B(d')=7' 2(d)=7 G1=62 B(e')=2' d(e) = 2 X(f)=4 B141=4 B(5') = 6 Edge of 62 Edge of 6270 Ining d(u,) 61 d(n) d(n2) Jothin x(n) and & (n) = B(e) 2 2 NZ NI a 3 d 5 19 2 ti If we make an undirected graph 3 and teams represent the played games, the games 11x6/2=33 edges, and this graph can : 37 games will be played. continued on next page

(SWY HWHT 20160051 objunktuon Pg 2/3 3(cont.) (b) No. If we try to make a graph with conditions that I have stated on prob 3 (a), the graph's edge should be 11x5/2= 55/2, which cannot be happened. Interons of the Fuler's theorem, the sum of the degrees of the vertices should be twice the number of edges, TP, the sum of the gumes that have been played by each teams should be even, which is not the case in the problem Mathematical Induction T(n): a tree with n vertices.

1) n=1

E(T) Titree

+ of edges in T. TT) N=K E(T(K)) = K-1: Induction hypothesis. 111) u=(c+1 We can pick a terminal node (= a vertex with the degree 1) since there is no simple circuits In the tree. If we remove the edge that 75 connected to the terminal node, we can get a T(K) and T(1). The # of edges of each tree are k-1 and 0. If we put the edge we have deleted back, the total humber of edge is (K-1)+0+1=(E) Mathematical Induction on P 1) p=0 L=(a,1) -> 5um(L)=a, by part B. V 17) p= v Induction hypothesis; sum(L)=a,+a2+...+a2n L= ((a, az, ..., azn), (azn+1, azn+z, ..., azn+1)) Sum(L) = Sum((a, (az, -, azn)) + Sum ((azn+1, -, azn+1)) by powt R = (a1+a2+ ... + an) + (a2n+1+ ... + a2n+1) by I.H = a, ta2+ - + an+1

CS204 HW41 2016005/ objun (anon pg 3/3 G-2: (b) faces; 4 e. 6, d C.b.d. 6, C, a d,b,e d,6,0 baje e b, c ad aef Cha def Carfid a vertices edges: (2+2+2+3+3+3+4+4+5)/2=14 (Enler's thin on dequees) 1 taces = e-V+2=14-9+2= 9. 1) Tis a full binary free w/ i internal vertices -> Thas it I terminal vertices, 21+1 total vertices 13:0 Internal vertex ; I terminal vertices, I total vertices. I(T) : # of Strong mentlymation Induction. I for ick intunal vertex - it I terminal vertices 21+1 total R: For I(T)=K+1 o root; Land R; not empty (: full binary tree) Tot(T) I(T) = I(L)+I(R) fotal K=I(L)+I(R) K+1 =) T(L)= I(L)+1 YI(L) =| K) Tot(L)= 2I(L)+1 (:I.H) T(R)= I(R)+1 Tot(R) = 2 1(2)+1 => T(T)= T(L)+T(R)=I(L)+I(R)+Z= K+2= (K+1)+1 Tot(T)=Tot(C)+Tot(R)+1=2(I(L)+I(R)+3=2(+3=2(1c+1)+1)