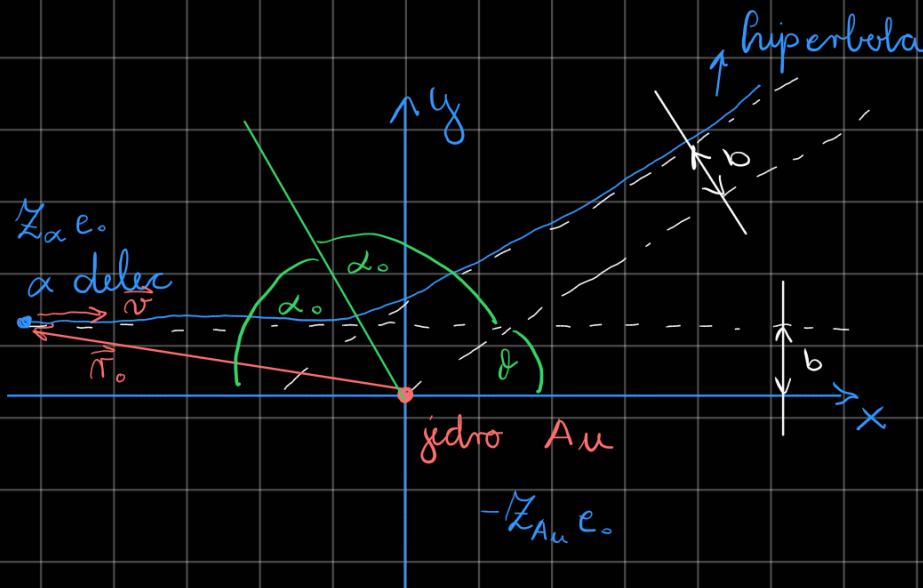


Rutherfordovo zjedanje



Tekūšām sistēmā
reducirāmo masu
vai velja

$$m_\alpha \ll m_{Au}$$

$$\Rightarrow \mu = m_{Au} // \text{reducirāma masa}$$

$$\vec{v} = (v_0, 0)$$

Zaujima masas virzītība uz zjedājumiem (izpējāl komo zjedājumi pāri)

1) Ģibājība uz centruļum potenciālu

$$\vec{F} \parallel \vec{r} \Rightarrow \vec{M} = \emptyset // \text{mavor}$$

$$\vec{M} = \emptyset \Rightarrow \vec{r} = \text{konst.} \quad \frac{d\vec{r}}{dt} = \vec{v} // \text{konst. ģibājība}$$

$$\vec{r} = \vec{r}_0 \times \vec{p}$$

$$\vec{p} = m \vec{v} = m \dot{\vec{r}}$$

$$\text{Definējam } \vec{v} = (-r \cos \varphi, r \sin \varphi, 0)$$

Velja $r = r(t)$ un $\varphi = \varphi(t)$ un tāls je

$$\dot{\vec{r}} = (-\dot{r} \cos \varphi + r \sin \varphi \dot{\varphi}, \dot{r} \sin \varphi + r \cos \varphi \dot{\varphi}, 0)$$

$$\Rightarrow \vec{\nabla} = m \begin{vmatrix} i & j & k \\ r_x & r_y & r_z \\ v_x & v_y & v_z \end{vmatrix} = m (0, 0, r_x v_y - r_y v_x)$$

$$\begin{aligned} \vec{\nabla}_x &= m \left[-r \dot{\varphi} \sin \varphi \cos \varphi - r^2 \cos^2 \varphi \ddot{\varphi} + r \dot{r} \sin \varphi \cos \varphi - r^2 \sin^2 \varphi \ddot{\varphi} \right] \\ &= -m r^2 \ddot{\varphi} \end{aligned}$$

Zelimo povzati $\propto b$ in v_0 (∇):

$$\nabla(t = \emptyset) = \vec{r}(t = \emptyset) \times \vec{p}(t = \emptyset) = m v_0 b \quad // \vec{r} \times \vec{p} = 0$$

$$\vec{r} = \vec{r}_{\perp} + \vec{r}_{\parallel} \quad |\vec{r}_{\perp}| = b$$

$$\text{Tako velja } m v_0 b = -m r^2 \ddot{\varphi} \Rightarrow \ddot{\varphi} = -\frac{v_0 b}{r^2}$$

2) Newtonov zakon v y -meri

$$m \frac{dy}{dt} = F_y \quad // \text{poznamo } \ddot{\varphi}, \text{ tako uravno odvajamo}$$

$$m \frac{d v_{yx}}{d \varphi} \frac{d \dot{\varphi}}{d t} = \frac{\chi_{\alpha} \chi_{Au} e_0^2}{4 \pi \epsilon_0 r^2} \cdot \sin \varphi$$

$$\ddot{\varphi} = \frac{v_0 b}{r^2}$$

$$\frac{d v_{yx}}{d \varphi} = \frac{\chi_{\alpha} \chi_{Au} e_0^2}{4 \pi \epsilon_0 v_0 b m} \sin \varphi$$

// xamima mas koton spreminjanje hitrosti \Rightarrow integracija

$$\int_0^{\omega_y} d\omega_y = \frac{\chi_\alpha \chi_{Au} \epsilon_0^2}{4\pi \epsilon_0 n_0 b m} \int_0^\varphi \sin \varphi d\varphi$$

$$\omega_y(\varphi) = \frac{\chi_\alpha \chi_{Au} \epsilon_0^2}{4\pi \epsilon_0 n_0 b m} [1 - \cos \varphi]$$

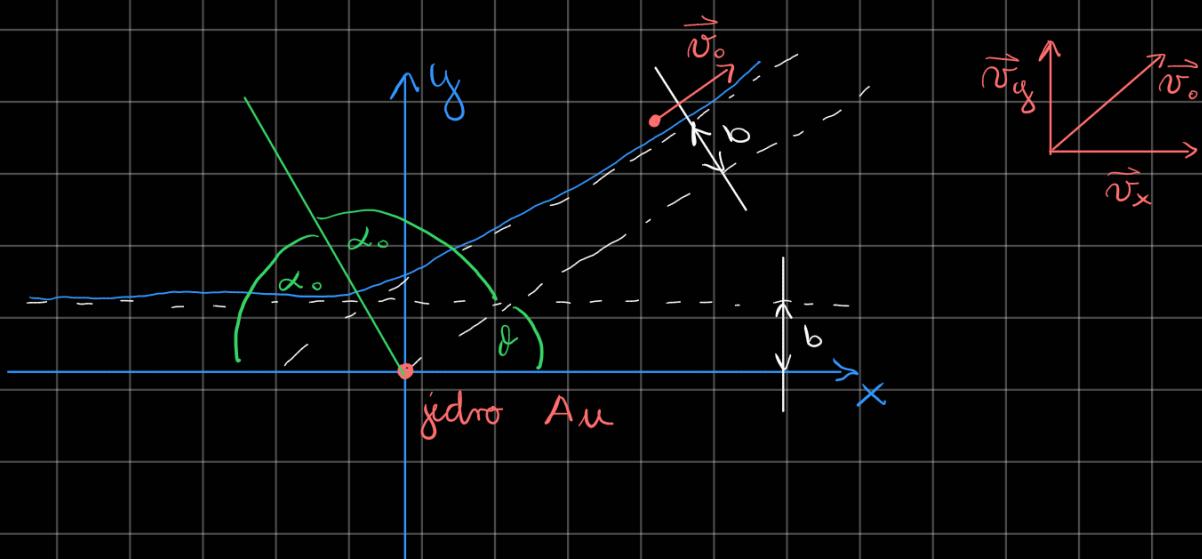
// preidimo iš φ ma θ , kur mas žauima kai ripauja

Po ripauju: $\varphi \rightarrow \varphi = \pi - \theta$

$$\Rightarrow \cos(\pi - \theta) = -\cos(\theta)$$

$$\omega_y(\theta) = \frac{\chi_\alpha \chi_{Au} \epsilon_0^2}{4\pi \epsilon_0 n_0 b m} [1 + \cos \theta]$$

// mahajamo se demo



$$\omega_y = \omega_0 \sin \theta$$

K

Žauima mas parameter b: $b =$

$$b = \frac{\chi_\alpha \chi_{Au} \epsilon_0^2}{4\pi \epsilon_0 m \omega_0^2} \frac{1 + \cos \theta}{\sin \theta}$$

$$\text{dvojini koti: } \cos \vartheta = \cos\left(2 \frac{\vartheta}{2}\right) = \cos^2\left(\frac{\vartheta}{2}\right) - \sin^2\left(\frac{\vartheta}{2}\right)$$

$$\sin \vartheta = 2 \sin\left(\frac{\vartheta}{2}\right) \cos\left(\frac{\vartheta}{2}\right)$$

$$1 = \cos^2 \frac{\vartheta}{2} + \sin^2 \frac{\vartheta}{2}$$

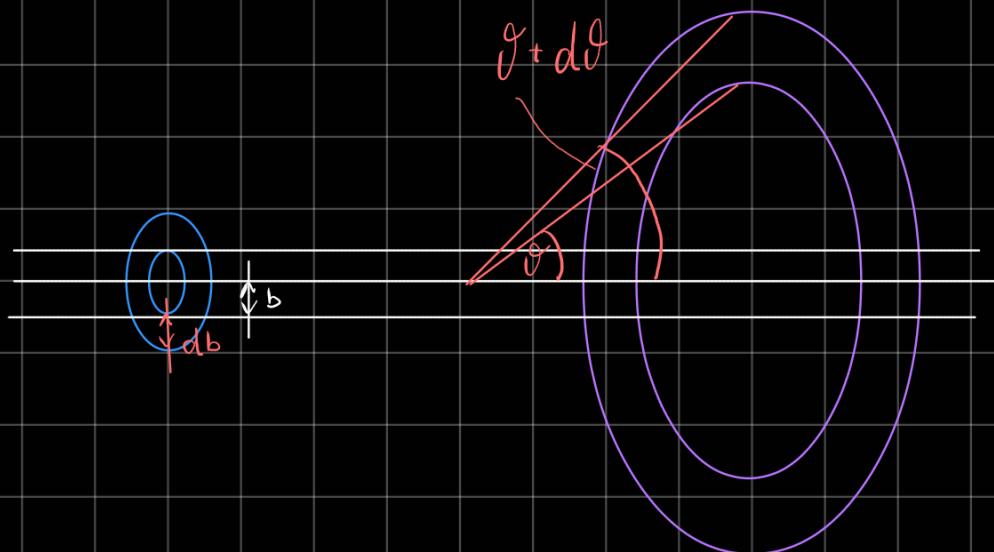
$$b = K \frac{\cos\left(\frac{\vartheta}{2}\right)}{\sin\left(\frac{\vartheta}{2}\right)} = \frac{K}{\tan\left(\frac{\vartheta}{2}\right)}$$

π^α

$$K = \frac{Z_\alpha Z_{Au} e^z}{4\pi \epsilon_0 m v_0^2} = Z_\alpha Z_{Au} \frac{e^z}{4\pi \epsilon_0 \hbar c} \hbar c \frac{1}{\frac{mv_0^2}{2} \cdot 2} = \frac{Z_\alpha Z_{Au} \alpha \hbar c}{2 E_{kin}}$$

3) Porovnateliv po kotech

$$\frac{d\lambda}{d\omega} = \frac{\text{# xipauh preuk}}{\text{ma casovno ceto}} \quad \begin{matrix} \text{xipauh delav v intervalu } [\omega, \omega + d\omega] \\ \text{vhodno intervaleto/tok} \end{matrix}$$



Obranitec # delaw

$$Z = \frac{dN}{dS} \Rightarrow Z dS = I 2\pi b db \quad // \# \text{ vpaduih delaw} \quad \left. \begin{array}{l} E \\ N \\ A \\ K \\ A \end{array} \right\}$$

$$Z \frac{d\beta}{d\Omega} d\Omega \quad // \# \text{ po supauju} \\ \hookrightarrow d(\cos \theta) d\phi = 2\pi \sin \theta d\theta$$

Upostevamo enakost

~~$$Z db 2\pi b = Z \frac{d\beta}{d\Omega} 2\pi \sin \theta d\theta$$~~

$$\frac{d\beta}{d\Omega} = \frac{b}{\sin \theta} \quad \frac{db}{d\theta} = K \frac{\cos \frac{\theta}{2}}{\sin \frac{\theta}{2}} \cdot \frac{1}{2 \sin \theta \cos \frac{\theta}{2}}$$

$$\frac{db}{d\theta} = K \frac{\sin \frac{\theta}{2} \left(-\sin \frac{\theta}{2} \right) \cdot \frac{1}{2} - \cos \frac{\theta}{2} \cos \frac{\theta}{2} \cdot \frac{1}{2}}{\sin^2 \frac{\theta}{2}} = -\frac{K}{2} \frac{1}{\sin^2 \frac{\theta}{2}}$$

$$\frac{d\beta}{d\Omega} \propto \frac{1}{\sin^2 \frac{\theta}{2}}$$

Teoretična mama formula

Masa jedra $m(A, Z) c^2 = N m_n c^2 + Z m_p c^2 + E_v(A, Z) < 0$

Masa atoma $M(A, Z) c^2 = N m_n c^2 + Z m_e c^2 + E_v(A, Z)$

The dudes in the past so xi izmisili: model jedra kot "kapljevino" nukleonov, ki jih drži skupaj - jedrska sila

Vzorna en. je nastavljena s

$$E_v(A, Z) = -w_0 A + w_1 A^{\frac{2}{3}} + w_2 \frac{Z^2}{A^{\frac{1}{3}}} \quad \rightarrow \text{priznani vpeljavi, el. potencial}$$

\hookrightarrow površinska napetost

$$+ w_3 \frac{(A - 2Z)^2}{A}$$

\hookrightarrow posledica KM

$$+ w_4 \frac{\delta_{ZN}}{A^{\frac{3}{4}}}$$

$$V\text{reduvosti } \delta_{ZN} = \begin{cases} 1; & (Z \text{ lih}, N \text{ lih}) \\ 0; & (Z \text{ rod/lih}, N \text{ lih/rod}) \\ -1; & (Z \text{ rod/lih}, N \text{ rod}, \text{lith}) \end{cases}$$

Za spletoma jedra (reduje težka jedra):

$$w_0 = 15'6 \text{ MeV}$$

$$w_4 = 33'5 \text{ MeV}$$

$$w_1 = 17'3 \text{ MeV}$$

Ver: Gtmad

$$w_2 = 0'70 \text{ MeV}$$

$$w_3 = 23'3 \text{ MeV}$$

Zorko 5.2

$$M\left({}_{7}^{15}N\right) = 15'000108 \mu$$

$$M\left({}_{8}^{15}O\right) = 15'003605 \mu$$

$$M_H = 1,007825 \mu$$

$$m_m = 1'008655 \mu$$

$$\mu = 931,494 \text{ MeV}/c^2$$

Kinik: $M\left({}_{8}^{15}O\right)c^2 = 7m_m c^2 + 8M_H c^2 + E_v(15,8)$

Duxik: $M\left({}_{7}^{15}N\right)c^2 = 8m_m c^2 + 7M_H c^2 + E_v(15,7)$

$$E_v: -\omega_0 A \xrightarrow{A_0 = A_\omega} E_{v_0}(O) = E_{v_0}(N)$$

$$\omega_1 A^{\frac{2}{3}} \rightarrow E_{v_1}(O) = E_{v_1}(N)$$

$$\omega_2 \frac{Z^2}{A^{\frac{1}{3}}} \rightarrow E_{v_2}(O) \neq E_{v_2}(N)$$

$$\omega_3 \frac{(A-2Z)^2}{A} \rightarrow E_{v_3}(O) = E_{v_3}(N)$$

$$\begin{array}{ccc} & \swarrow & \searrow \\ (-1)^2 & & (1)^2 \end{array}$$

$$\omega_4 \frac{\delta_{ZN}}{A^{\frac{3}{4}}} \xrightarrow[\text{komb.}]{\text{liha-soda}} \delta_{ZN}(O) = \delta_{ZN}(N) = 0$$

$$\Rightarrow E_{v4}(O) = E_{v4}(N) = \emptyset$$

$$\left(M\left(^{15}_8 O\right) - M\left(^{15}_7 N\right) \right) C^2 = M_H C^2 - m_m C^2 + \frac{\omega^2}{(A^{\frac{1}{3}})} \left(Z_o^2 - Z_N^2 \right)$$

$$\Rightarrow \omega_2 = \frac{[C^2 M\left(^{15}_8 O\right) - C^2 M\left(^{15}_7 N\right) - M_H C^2 + m_m C^2]}{Z_o^2 - Z_N^2} A^{\frac{1}{3}} = 0.58 \text{ MeV}$$

Zórko 5.8 //stabilnost' jader na α -razpad

$$A = 2Z$$



Stabilnostui kriterij

$$E_v(A, Z) \leq \underbrace{E_v(A-4, Z-2)}_{\text{rozwijali gorno to}} + E_v(4, 2)$$

Predpostavius $A, Z \gg 4$

$$E_v(A-4, Z-2) = \frac{\partial E_v}{\partial A} \Big|_{A, Z}^{(-4)} dA + \frac{\partial E_v}{\partial Z} \Big|_{A, Z}^{(-2)} dZ + E_v(4, 2)$$

//rozwoj

//vstatvius v menučbo

$$\mathcal{O} \leq \frac{\partial E_v}{\partial A} \Big|_{A=2Z}^{(-4)} + \frac{\partial E_v}{\partial Z} \Big|_{A=2Z}^{(-2)} + E_v(4, 2)$$

