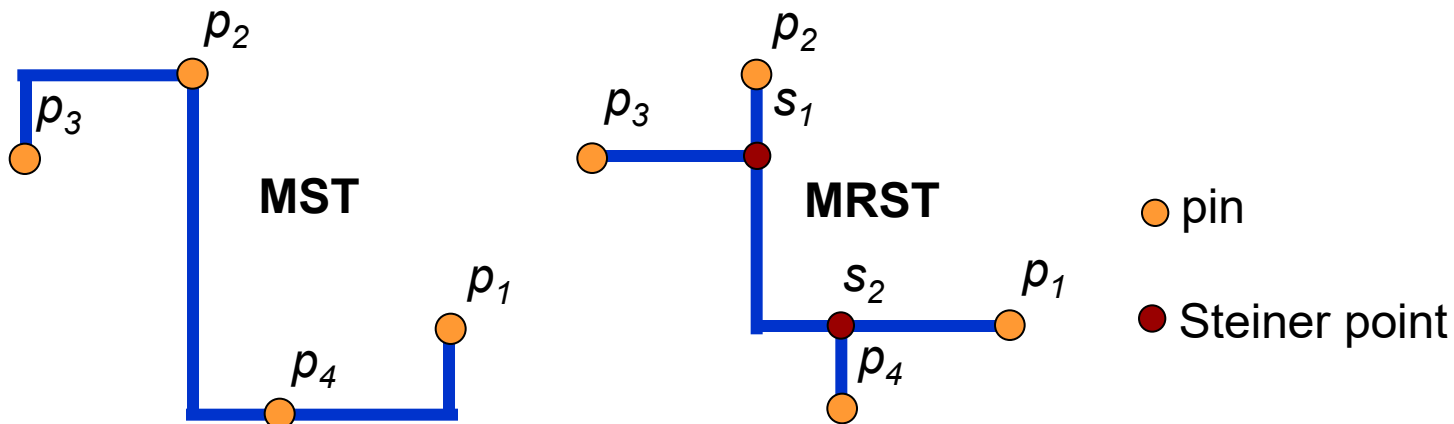


# Routing Tree

- If all nets are two-pin ones, we can apply a general-purpose routing algorithm to handle the problem, such as maze, line-search, and A\*-search routing.
- For three or more multi-pin nets, one approach is to *decompose* each net into a set of two-pin connections, and then routes the connections one-by-one.

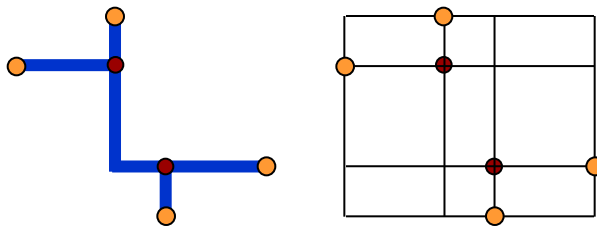
# The Routing-Tree Problem

- **Problem:** Given a set of pins of a net, interconnect the pins by a “routing tree.”
- **Minimum Spanning Tree (MST):** a minimum-length tree of edges connecting all the pins
- **Minimum Rectilinear Steiner Tree (MRST) Problem:** Given  $n$  points in the plane, find a minimum-length tree of rectilinear edges which connects the points. (Very useful in routing of VLSI circuits, but NP-hard)
- $MRST(P) = MST(P \cup S)$ , where  $P$  and  $S$  are the sets of original points and Steiner points, respectively.



# Theoretic Results for the RSMT Problem

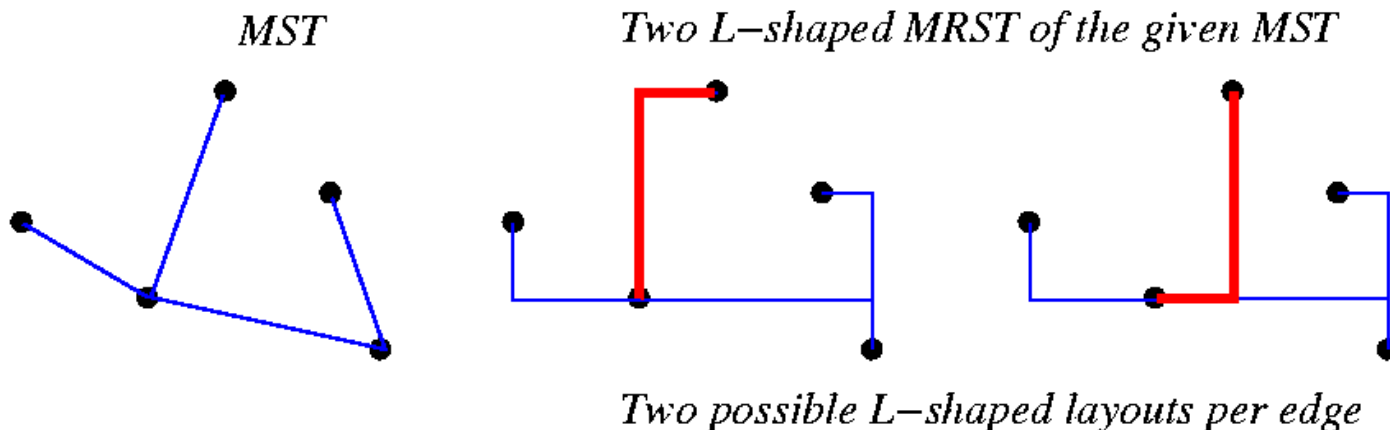
- **Hanan's Thm:** There exists an MRST with all Steiner points (set  $S$ ) chosen from the intersection points of horizontal and vertical lines drawn from points of  $P$ .
  - Hanan, “On Steiner's problem with rectilinear distance,” *SIAM J. Applied Math.*, 1966.



- **Hwang's Theorem:** For any point set  $P$ , 
$$\frac{\text{Cost}(MST(P))}{\text{Cost}(MRST(P))} \leq \frac{3}{2}.$$
  - Hwang, “On Steiner minimal tree with rectilinear distance,” *SIAM J. Applied Math.*, 1976.
- Better approximation algorithm with the performance bound  $61/48$ 
  - Foessmeier *et al*, “Fast approximation algorithm for the rectilinear Steiner problem,” Wilhelm Schickard-Institut für Informatik, TR WSI-93-14, 93.

# Minimum Spanning Tree Based Heuristic

- Ho, Vijayan, and Wong, “New algorithms for the rectilinear Steiner problem,” TCAD-90.
  1. Construct an RST from an MST.
  2. Each edge is straight or L-shaped.
  3. Maximize overlaps by dynamic programming.
- About 8% smaller than  $Cost(MST)$ .



# Repeated 1-Steiner Tree Heuristic

- A. B. Kahng and G. Robins, “A new class of Steiner tree heuristics with good performance: the iterated 1-Steiner approach,” ICCAD, 1990.
- **1-Steiner tree problem**: the minimal Steiner tree problem with the restriction that the tree contains only a single Steiner point.
- The optimal solution of the 1-Steiner tree problem can be found efficiently.
- The **repeated 1-Steiner tree heuristic** gives provably good results (but no optimal solution is guaranteed).

```
(set of struct vertex, set of struct edge)
steiner(set of struct vertex P)
{
    set of struct vertex T;
    set of struct edge E, F;
    int gain;

    E ← prim(P);
    (T, F, gain) ← 1-steiner(P, E);
    while (gain > 0) {
        P ← T;
        E ← F;
        (T, F, gain) ← 1-steiner(P, E);
    }
    return (P, E);
}
```

# 1-Steiner: Try All Hanan Points

(set of struct vertex, set of struct edge, int)  
1-steiner(set of struct vertex V, set of struct edge E)

```
maxgain ← 0;
for each s ∈ "Hanan points of V" {
    (W, F, gain) ← spanning_update(V, E, s);
    if (gain > maxgain) {
        maxgain ← gain;
        maxpoint ← s;
    }
}
if (maxgain > 0) {
    (W, F, gain) ← spanning_update(V, E, s);
    return (W, F, maxgain);
}
else return (V, E, 0);
}
```

# Getting Spanning Tree Incrementally

(set of struct vertex, set of struct edge, int)

spanning\_update(set of struct vertex  $V$ , set of struct edge  $E$ , struct vertex  $s$ )

$\text{delta} \leftarrow 0$ ;

$V \leftarrow V \cup \{s\}$ ;

**for each**  $d \in \{\text{north, east, south, west}\}$  {

$u \leftarrow \text{closest\_point}(V, s, d)$ ;

$\text{delta} \leftarrow \text{delta} - \text{distance}(s, u)$ ;

$E \leftarrow E \cup \{(s, u)\}$ ;

**if** ( $\text{cycle}(V, E)$ ) {

$(v, w) \leftarrow \text{largest\_cycle\_segment}(V, E)$ ;

$E \leftarrow E \setminus \{(v, w)\}$ ;

$\text{delta} \leftarrow \text{delta} + \text{distance}(v, w)$ ;

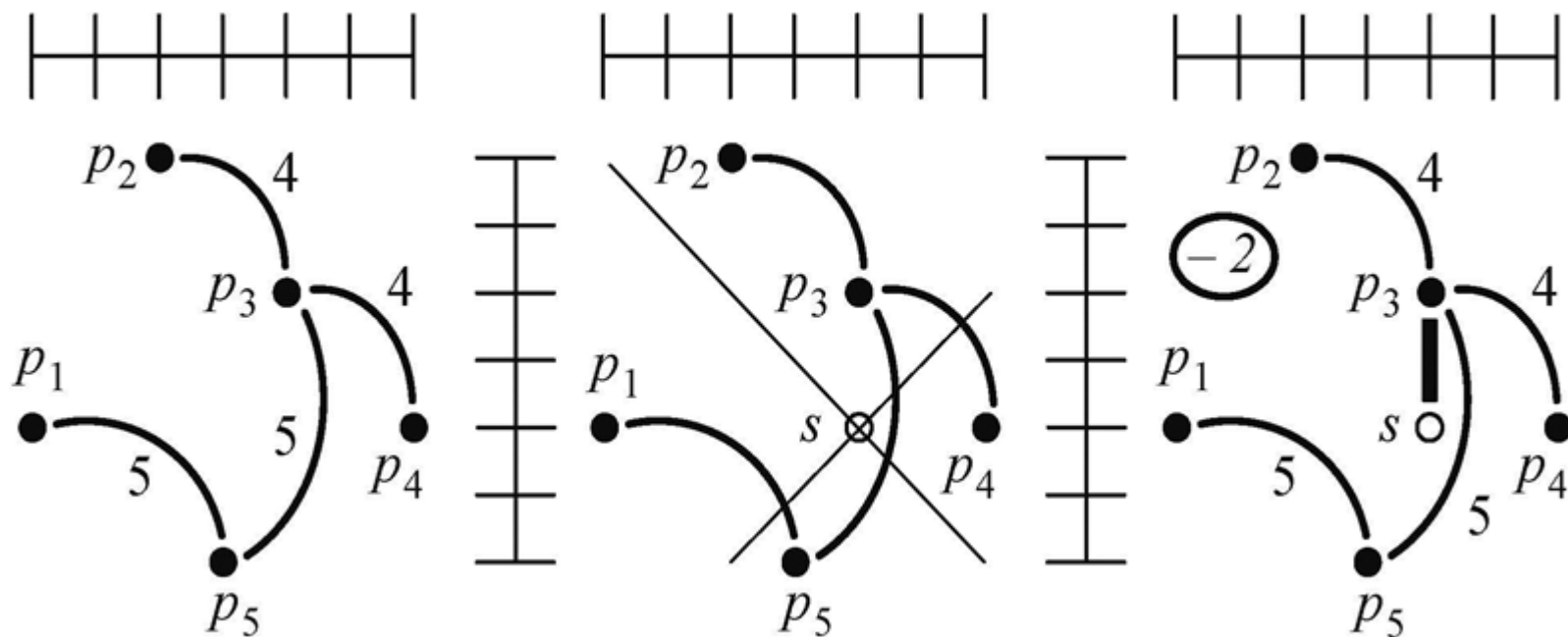
    }

}

**return** ( $V, E, \text{delta}$ );

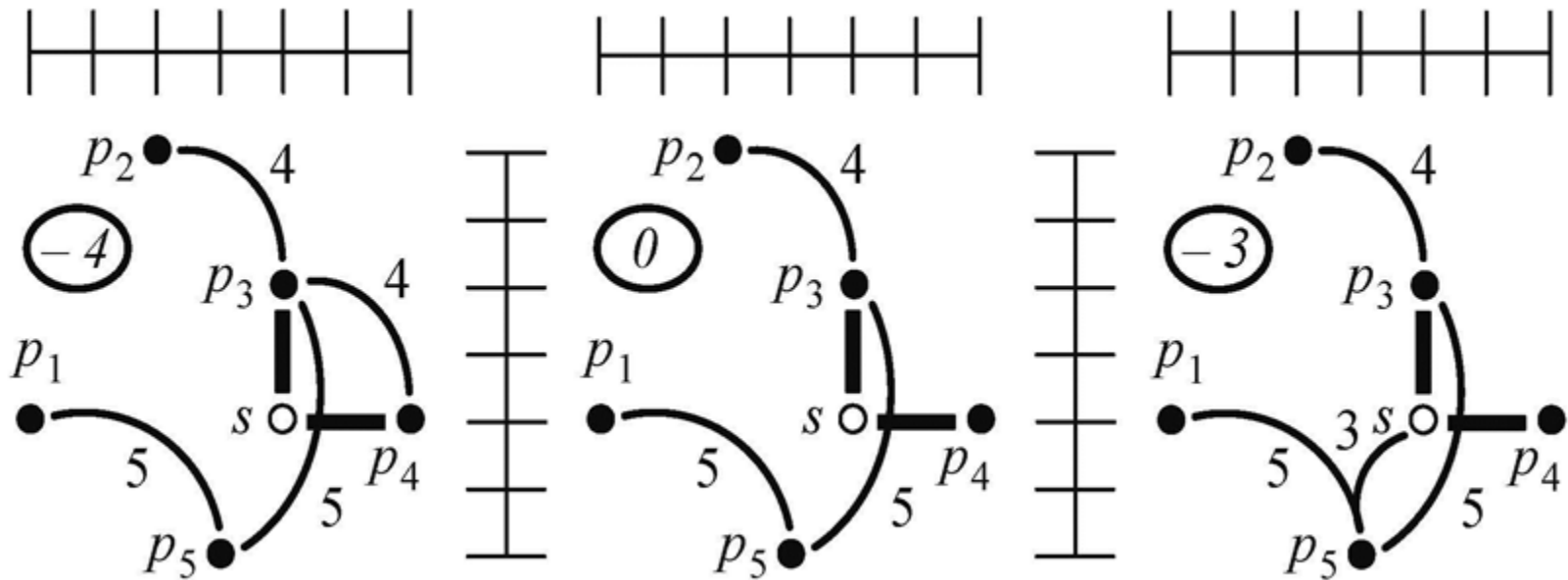
}

# Example

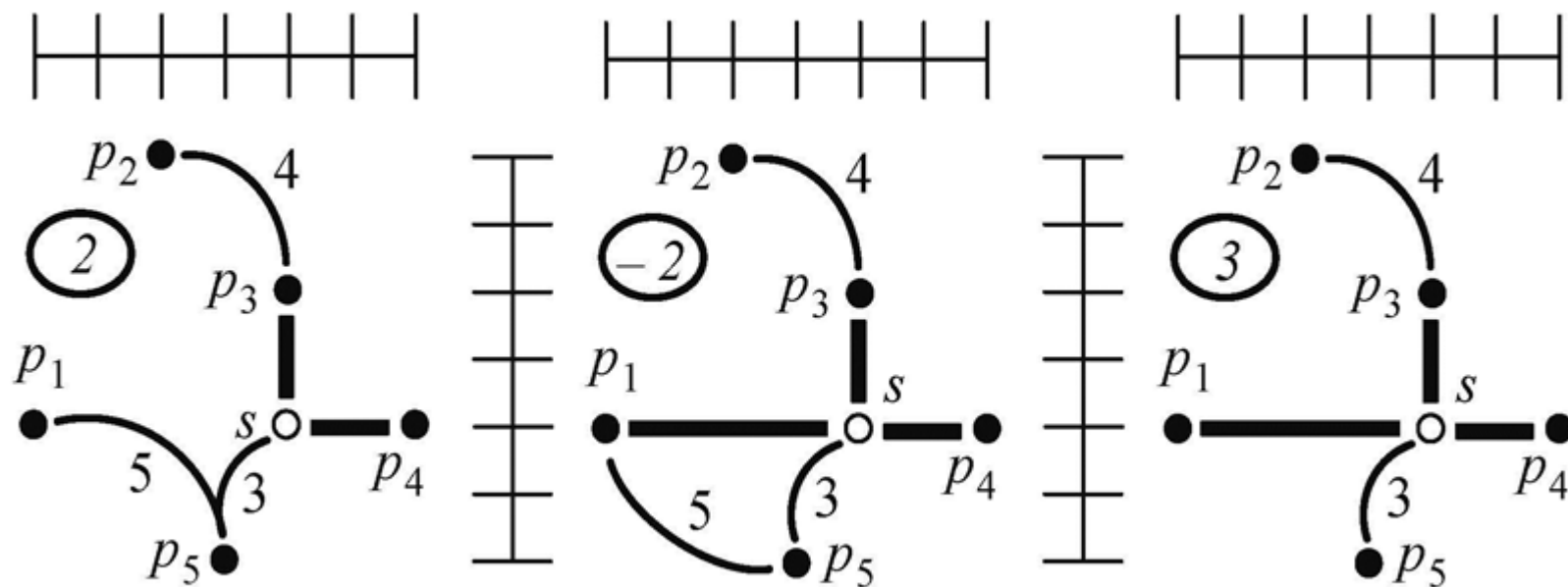




# Example (cont'd)



# Example (cont'd)



# FLUTE: Fast LookUp Table Estimation

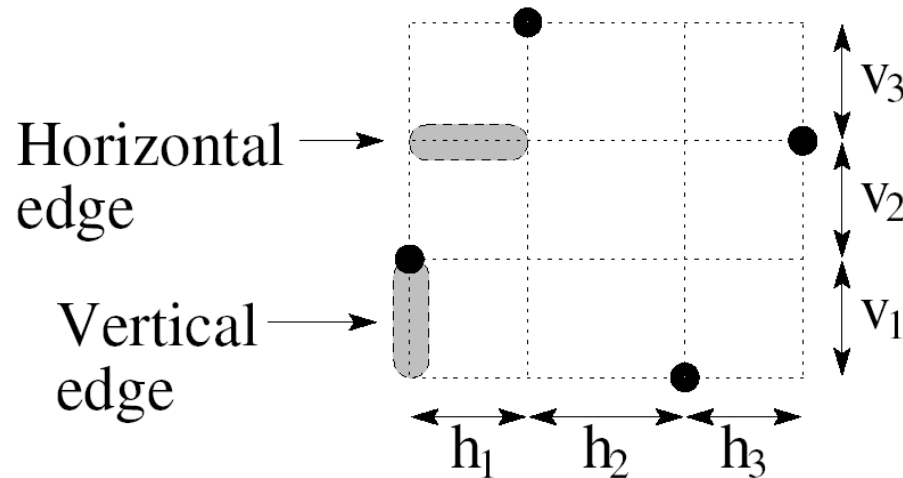
- Related publications
  - C. Chu, “FLUTE: Fast Lookup Table Based Wirelength Estimation Technique”, ICCAD 2004. (FLUTE 1.0)
  - C. Chu and Y.-C. Wong, “Fast and Accurate Rectilinear Steiner Minimal Tree Algorithm for VLSI Design”, ISPD 2005. (FLUTE 2.0)
  - C. Chu and Y.-C. Wong, “FLUTE: Fast Lookup Table Based Rectilinear Steiner Minimal Tree Algorithm for VLSI Design”, TCAD 2008. (FLUTE 2.5)
  - Y.-C. Wong and Chris Chu, “A Scalable and Accurate Rectilinear Steiner Minimal Tree Algorithm”, VLSI-DAT 2008. (FLUTE 3.0)

# Overview

- Basic idea
  - Lookup table to handle nets with a few pins
  - Net breaking technique to recursively break large nets
- Low degree nets are handled extremely well
  - Optimal and extremely efficient for nets up to 9 pins
  - Still very accurate and fast for nets up to 100 pins
- Suitable for VLSI applications
  - Over all 1.57 million nets in 18 IBM circuits [ISPD 98]
    - More accurate than Batched 1-Steiner heuristic
    - Almost as fast as minimum spanning tree construction

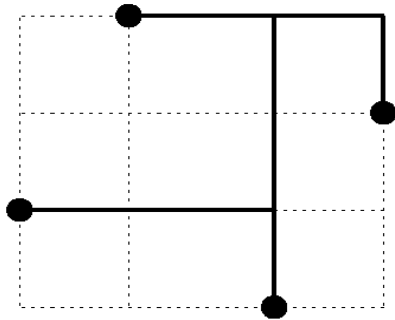
# Preliminaries

- Consider routing along Hanan grid
- **Observation:** An optimal RSMT can always be broken down into a set of horizontal edges and vertical edges
- Define edge lengths  $h_i$  and  $v_i$



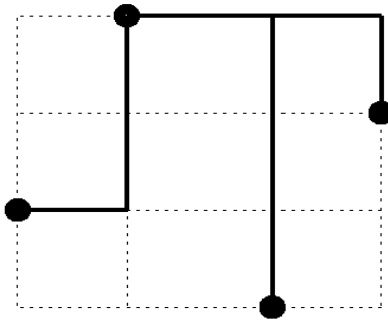
# Wirelength Vector (WV)

- Observation:** WL can be written as a linear combination of edge lengths with positive integral coefficients



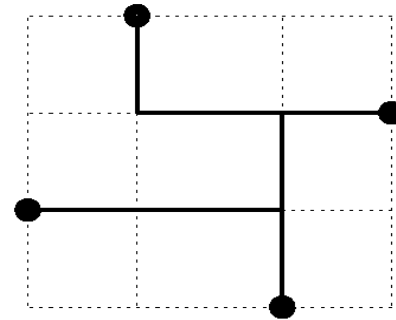
$$WL = h_1 + 2h_2 + h_3 \\ + v_1 + v_2 + 2v_3$$

$$(1, 2, 1, 1, 1, 2)$$



$$WL = h_1 + h_2 + h_3 \\ + v_1 + 2v_2 + 3v_3$$

$$(1, 1, 1, 1, 2, 3)$$



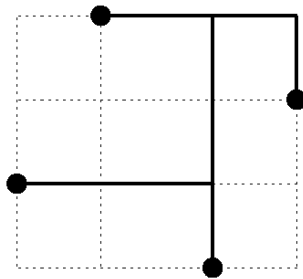
$$WL = h_1 + 2h_2 + h_3 \\ + v_1 + v_2 + v_3$$

$$(1, 2, 1, 1, 1, 1)$$

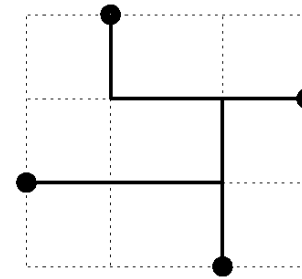
- WL can be expressed as a vector of the coefficients called Wirelength Vector (WV)

# Potentially Optimal WV (POWV)

- Optimal WL can be found by enumerating all WVs
- However, most WVs can never produce optimal WL
  - $(1, 2, 1, 1, 1, \underline{2})$  is redundant as it always produces a larger WL than  $(1, 2, 1, 1, 1, \underline{1})$



$(1, 2, 1, 1, 1, 2)$



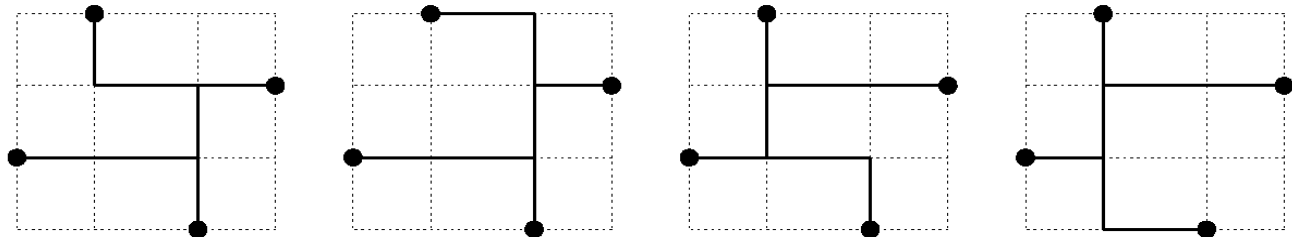
$(1, 2, 1, 1, 1, 1)$

- Potentially Optimal Wirelength Vector (POWV) is a WV that *may* produce optimal WL

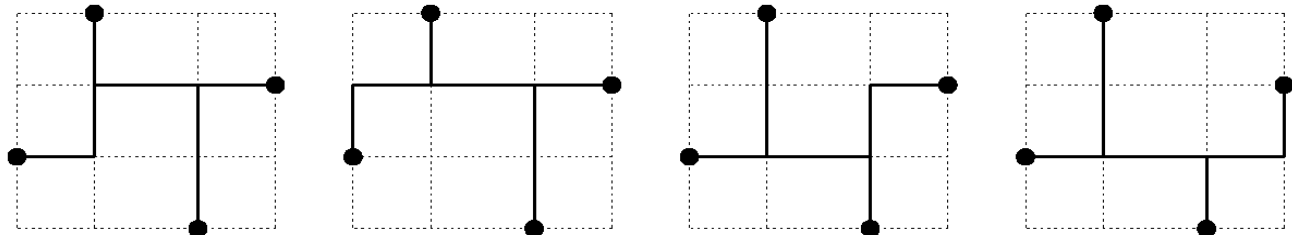
# Number of POWVs

- For any net
  - # of possible routing solutions is huge
  - # of WVs is much less
  - **# of POWVs is very small**
- For example, only 2 POWVs for the net below

POWV  
(1,2,1,1,1,1)



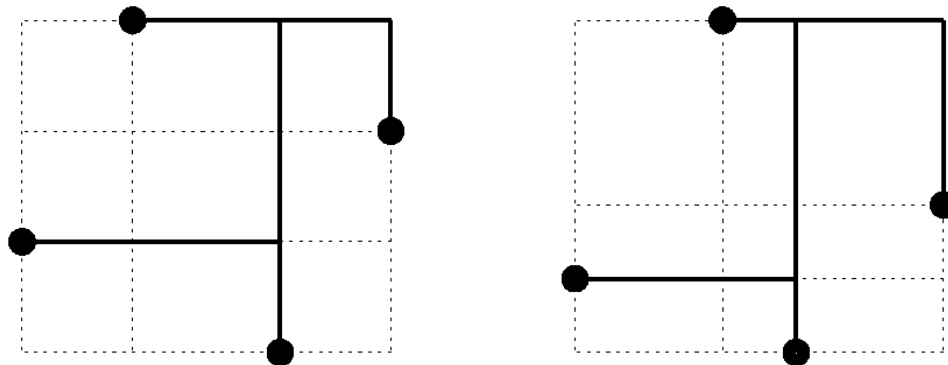
POWV  
(1,1,1,1,2,1)





# Sharing of POWVs Among Nets

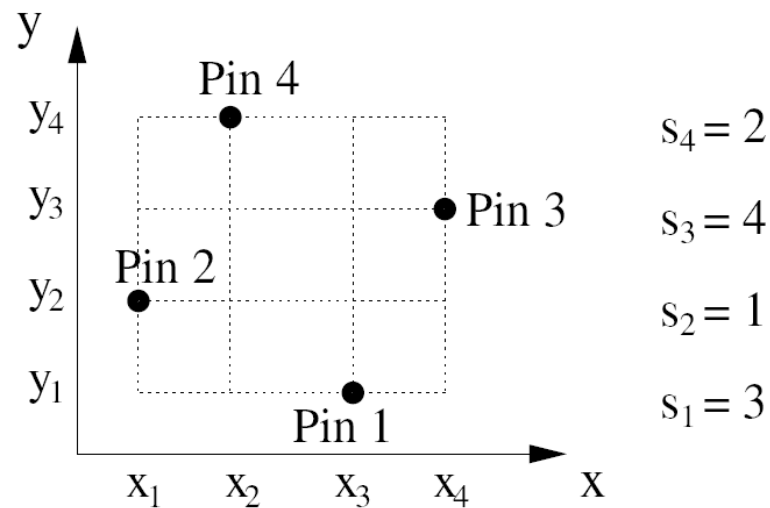
- To find optimal WL, we can pre-compute all POWVs and store them in a lookup table
- However, there are infinite number of different nets
- Try to group together nets that can share the same set of POWVs
- For example, these following two nets share the same set of POWVs:



# Grouping by Position Sequence

- Define position sequence  $s_1 s_2 \dots s_n$  to be the list of ranks of pins in x-coordinate

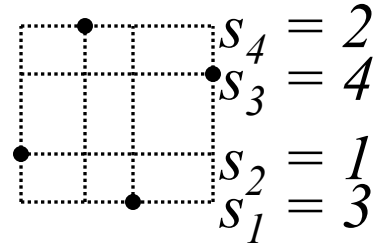
Position sequence  
= 3142



- Lemma:** The set of all degree- $n$  nets can be divided into  $n!$  groups according to the position sequence such that all nets in each group share the same set of POWVs

# Steps for WL Estimation

- Given a net
  - Find the position sequence



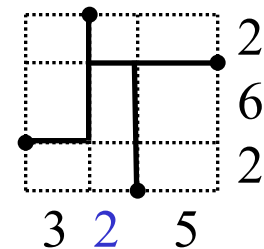
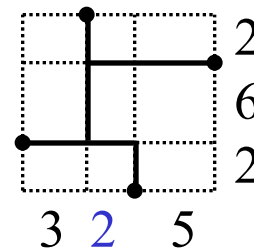
Position  
sequence:  
3142

- Get the POWVs from LUT

POWVs:

(1,2,1,1,1,1)      (1,1,1,1,2,1)

- Find the edge lengths



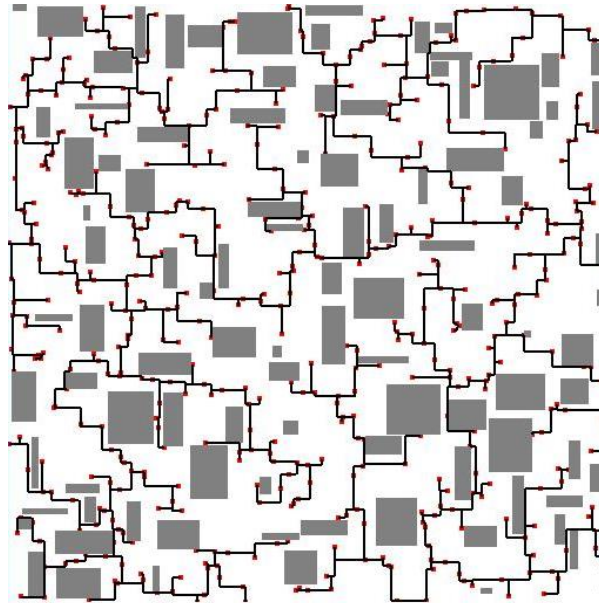
- Find WL for each POWV  
and return the best

HPWL + 2 = 22      HPWL + 6 = 26

Return

# Obstacle-Avoiding Rectilinear Steiner Minimal Tree

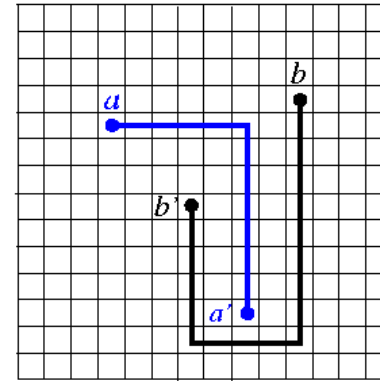
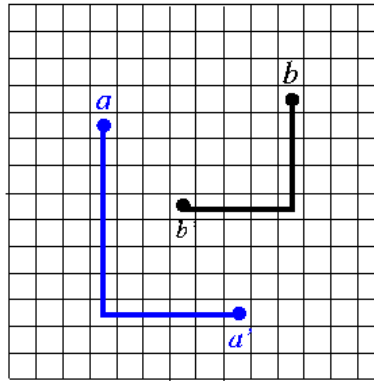
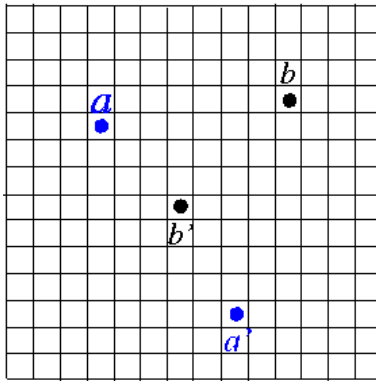
- Obstacles: macro/IP blocks, power/ground network, etc.
  - Rectangular shapes vs. rectilinear shapes
- Single routing layer



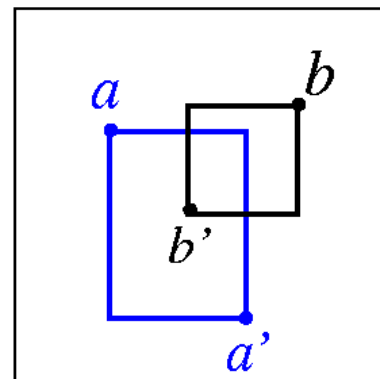
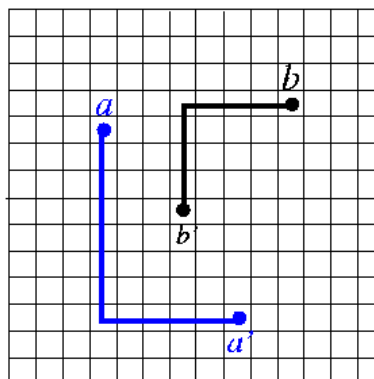
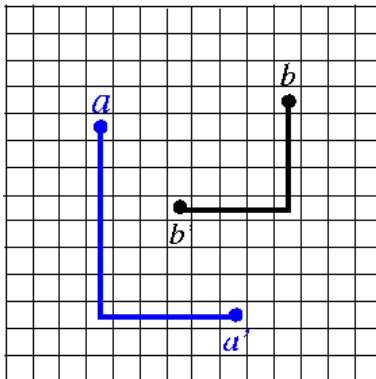
- Multiple routing layers
  - Preferred directions vs. non-preferred directions

# Net Ordering

- Net ordering greatly affects routing solutions.
- In the example, we should route net  $b$  before net  $a$ .



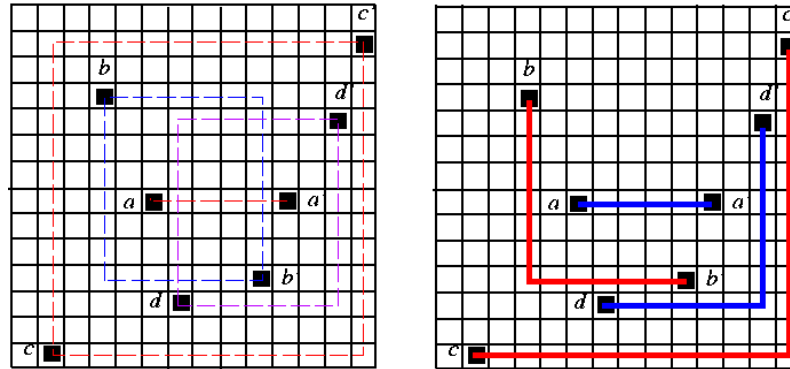
*route net  $a$  before net  $b$*



*route net  $b$  before net  $a$*

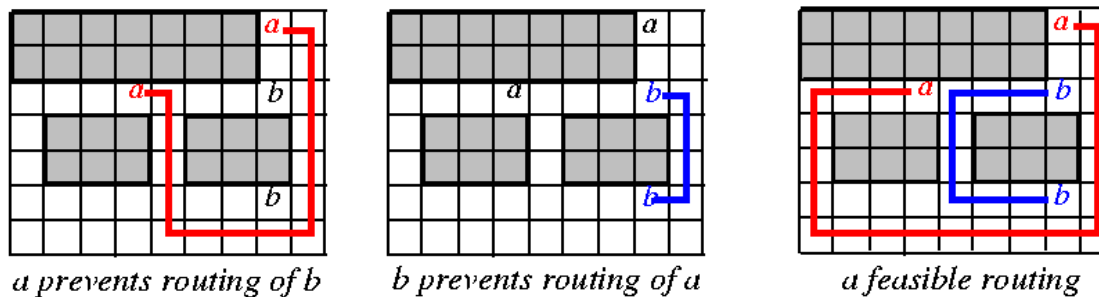
# Net Ordering (cont'd)

- Order the nets in the ascending order of the # of pins within their bounding boxes.



*routing ordering: a (0)  $\rightarrow$  b (1)  $\rightarrow$  d (2)  $\rightarrow$  c (6)*

- Order the nets in the ascending (or descending??) order of their length.
- Order the nets based on their timing criticality.
- A mutually intervening case:

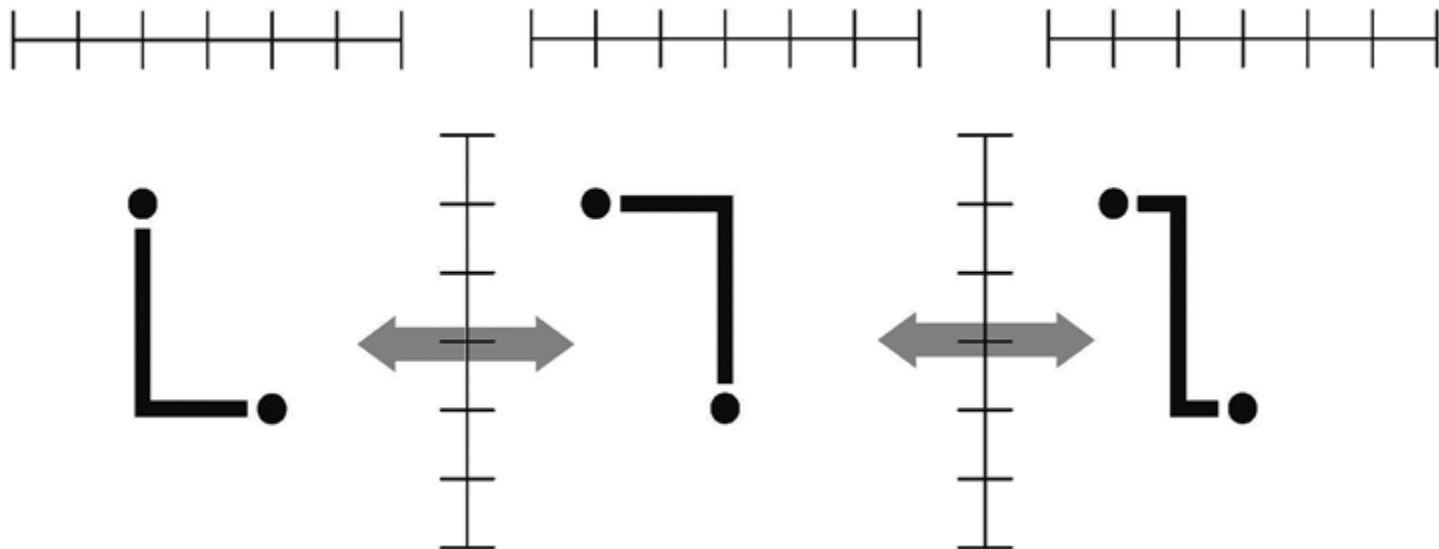


# Rip-Up and Re-routing

- Rip-up and re-routing is required if a global or detailed router fails in routing all nets.
- Two steps in rip-up and re-routing
  1. Identify bottleneck regions, rip off some already routed nets.
  2. Route the blocked connections, and re-route the ripped-up connections.
- Repeat the above steps until all connections are routed or a time limit is exceeded.

# Local Transformations

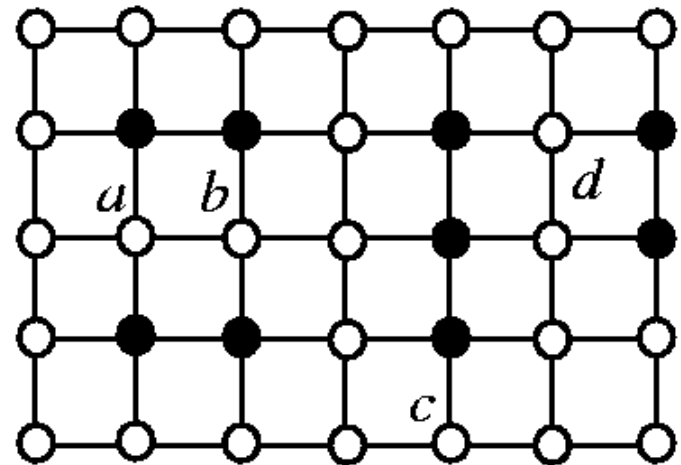
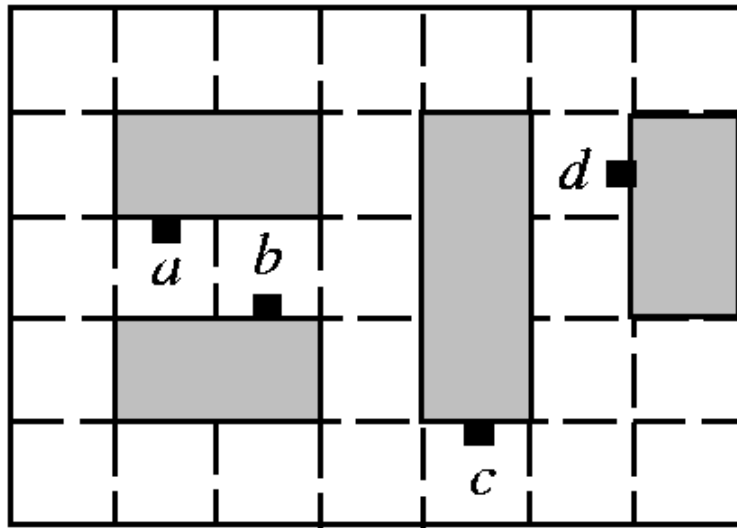
- Over-congestion after net-independent Steiner-tree construction can be eliminated by local transformations (e.g. guided by simulated annealing) or by ripping up a net and rerouting it by maze routing





# Graph Models for Global Routing: Grid Graph

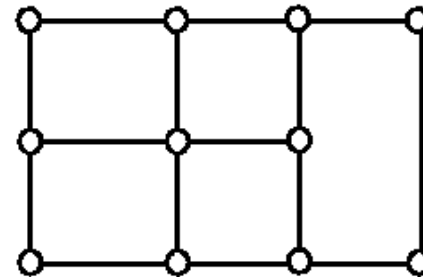
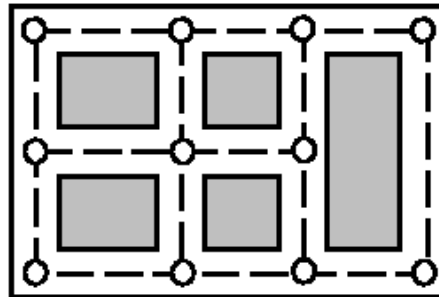
- Each grid cell is represented by a vertex.
- Two vertices are joined by an edge if the corresponding grid cells are adjacent to each other.
- The occupied grid cells are represented as filled circles, whereas the others are as clear circles.



# Graph Model: Channel Intersection Graph

- Channels are represented as edges.
- Channel intersections are represented as vertices.
- Edge weight represents channel capacity.
- Extended channel intersection graph: terminals are also represented as vertices.

*channel  
intersection  
graph*



*extended  
channel  
intersection  
graph*

