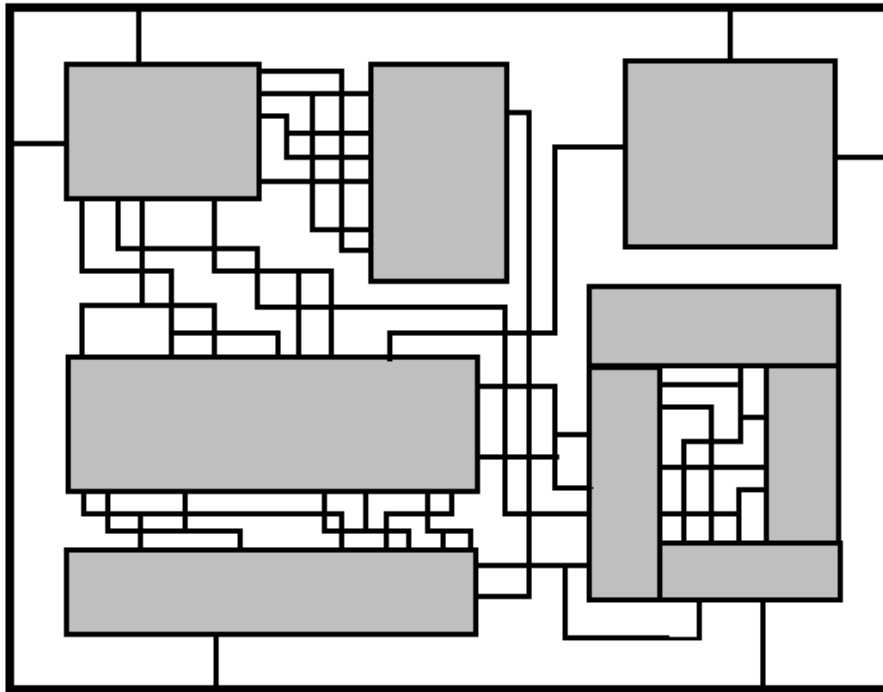
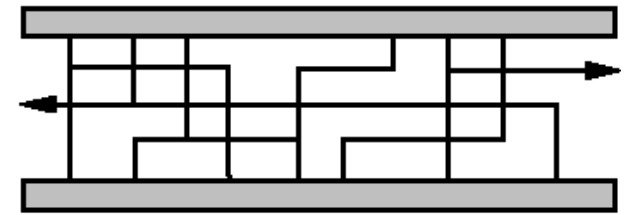


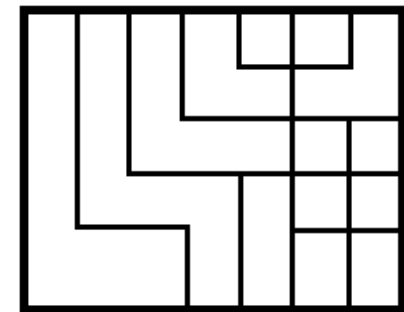
# Detailed Routing



Detailed routing



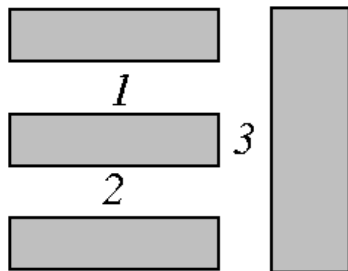
channel routing



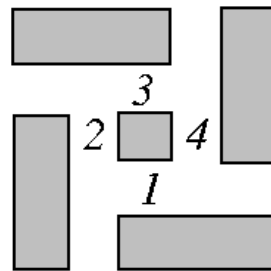
switchbox routing

# Order of Routing Regions

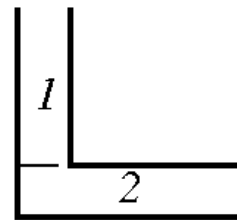
- (a) No conflicts in case of routing in the order of 1,2, and 3.
- (b) No ordering is possible to avoid conflicts.
- (c) The situation of (b) can be resolved by using L-channels.
- (d) An L-channel can be decomposed into two channels and a switchbox.



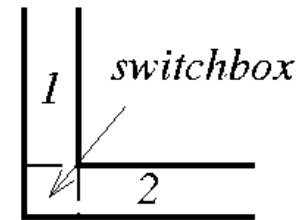
(a)



(b)



(c)



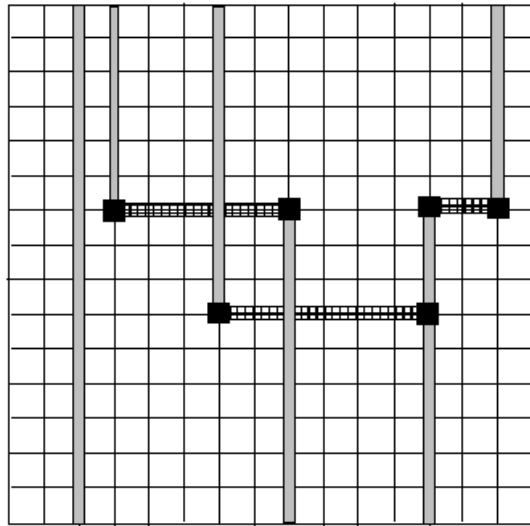
(d)

# Routing Considerations

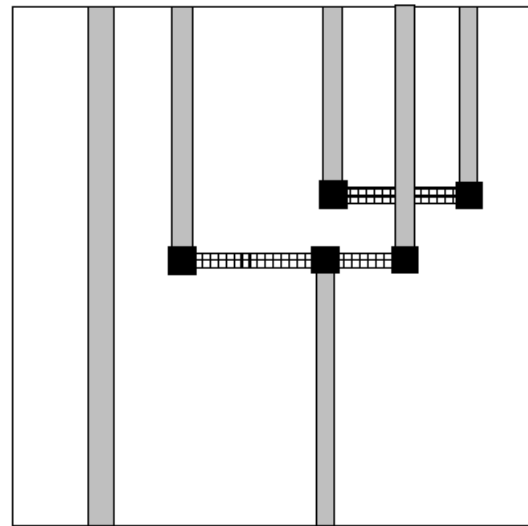
- Number of terminals (two-terminal vs. multi-terminal nets)
- Net widths (power and ground vs. signal nets)
- Via restrictions (stacked vs. conventional vias)
- Boundary types (regular vs. irregular)
- Number of layers (two vs. three, more layers?)
- Net types (critical vs. non-critical nets)

# Routing Models

- **Grid-based model:**
  - A grid is super-imposed on the routing region.
  - Wires follow paths along the grid lines.
- **Gridless model:**



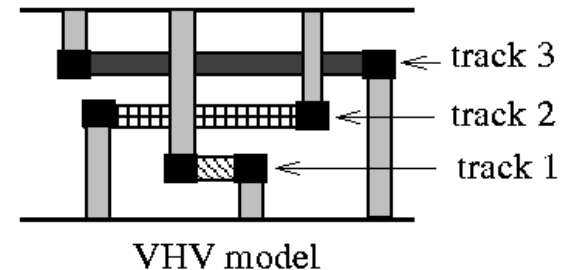
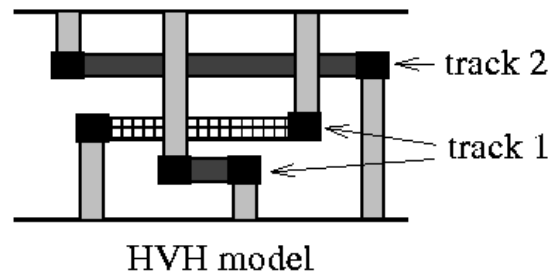
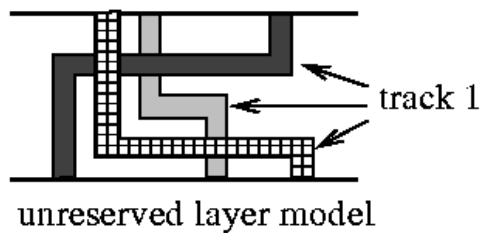
grid-based



gridless

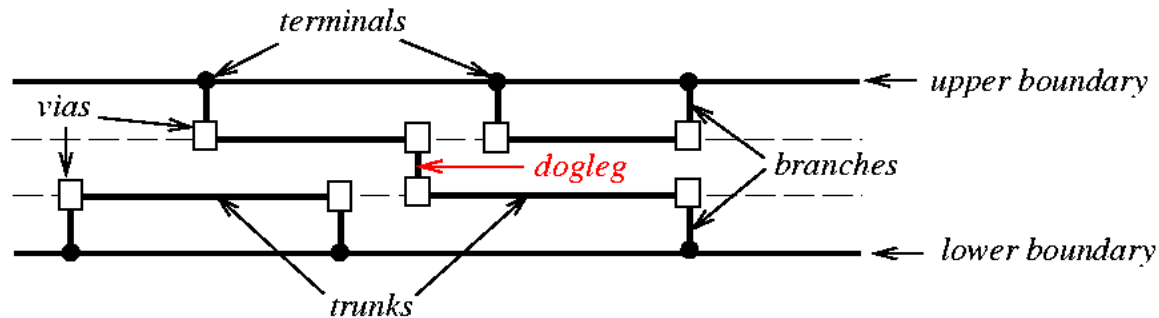
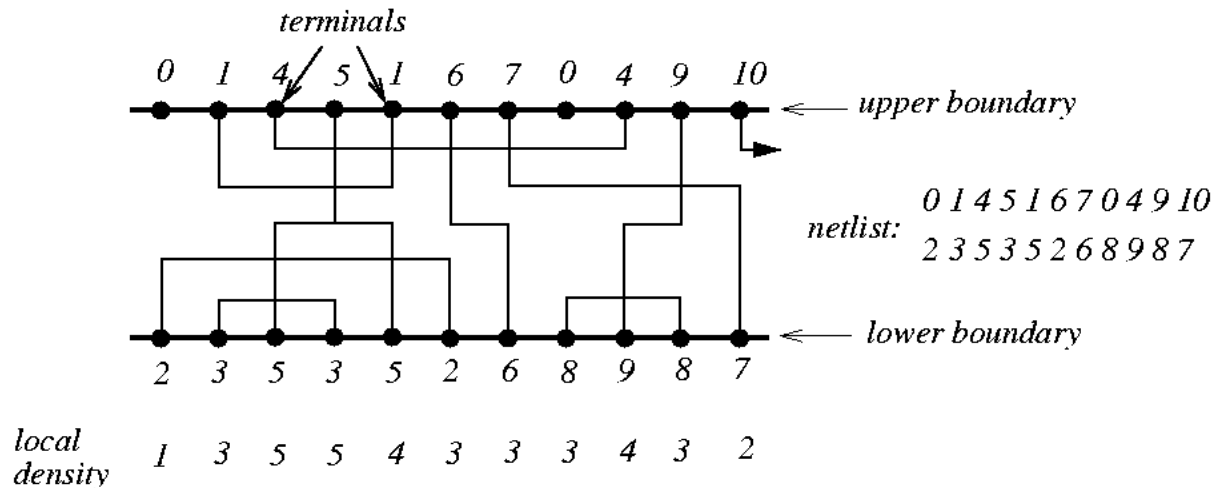
# Models for Multi-Layer Routing

- **Unreserved layer model:** Any net segment is allowed to be placed in any layer.
- **Reserved layer model:** Certain type of segments are restricted to particular layer(s).
  - Two-layer: HV (horizontal-vertical), VH
  - Three-layer: HVH, VHV



*3 types of 3-layer models*

# Terminology for Channel Routing



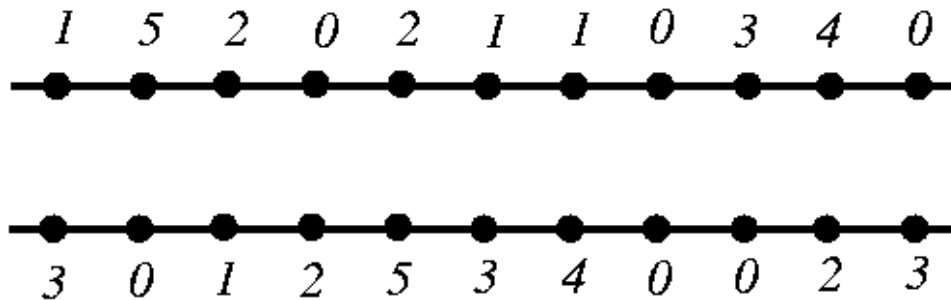
- Local density at column  $i$ : total # of nets that crosses column  $i$ .
- Channel density: maximum local density; # of horizontal tracks required  $\geq$  channel density.

# Channel Routing

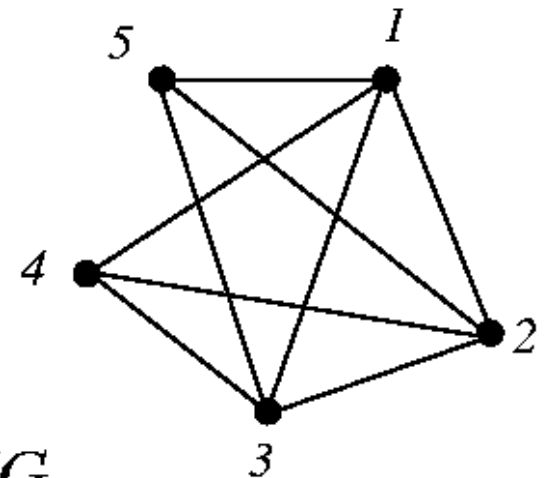
- **Assignments of horizontal segments of nets to tracks.**
- **Assignments of vertical segments to connect**
  - horizontal segments of the same net in different tracks, and
  - the terminals of the net to horizontal segments of the net.
- **Horizontal and vertical constraints must not be violated.**
  - Horizontal constraints between two nets: The horizontal span of two nets overlaps each other.
  - Vertical constraints between two nets: There exists a column such that the terminal on top of the column belongs to one net and the terminal on bottom of the column belongs to the other net.
- **Objective: Channel height is minimized** (i.e., channel area is minimized).

# Horizontal Constraint Graph (HCG)

- HCG  $G = (V, E)$  is an **undirected** graph where
  - $V = \{v_i | v_i \text{ represents a net } n_i\}$
  - $E = \{(v_i, v_j) | \text{a horizontal constraint exists between } n_i \text{ and } n_j\}$ .
- For graph  $G$ : vertices  $\Leftrightarrow$  nets; edge  $(i, j) \Leftrightarrow$  net  $i$  overlaps net  $j$ .



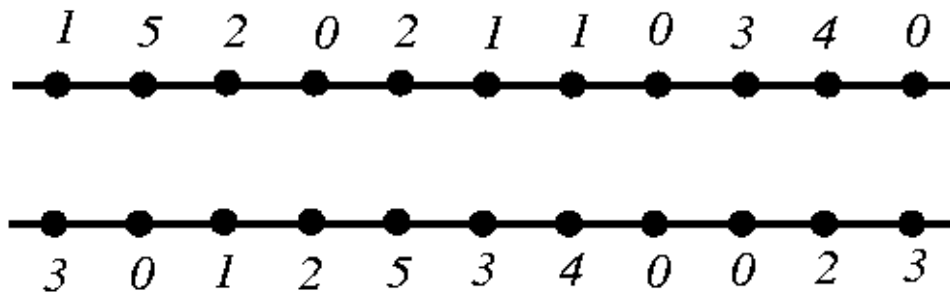
*A routing problem and its HCG.*



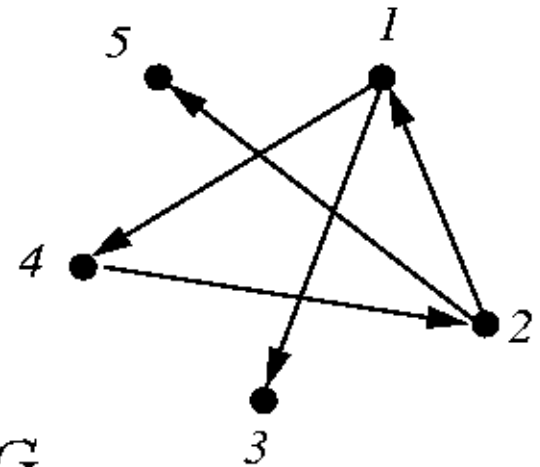


# Vertical Constraint Graph (VCG)

- VCG  $G = (V, E)$  is a **directed** graph where
  - $V = \{v_i | v_i \text{ represents a net } n_i\}$
  - $E = \{(v_i, v_j) | \text{a vertical constraint exists between } n_i \text{ and } n_j\}$ .
- For graph  $G$ : vertices  $\Leftrightarrow$  nets; edge  $i \rightarrow j \Leftrightarrow$  net  $i$  must be above net  $j$ .



*A routing problem and its VCG.*



## 2-L Channel Routing: Basic Left-Edge Algorithm

- Hashimoto & Stevens, “Wire routing by optimizing channel assignment within large apertures,” DAC, 1971.
- **No vertical constraint.**
- HV-layer model is used.
- **Doglegs are not allowed.**
- Treat each net as an interval.
- Intervals are sorted according to their left-end x-coordinates.
- Intervals (nets) are routed one-by-one according to the order.
- For a net, tracks are scanned from top to bottom, and the first track that can accommodate the net is assigned to the net.
- Optimality: produces a routing solution with the minimum # of tracks (if no vertical constraint).

# Basic Left-Edge Algorithm

**Algorithm: Basic\_Left-Edge( $U, track[j]$ )**

$U$ : set of unassigned intervals (nets)  $I_1, \dots, I_n$ ;

$I_j = [s_j, e_j]$ : interval  $j$  with left-end  $x$ -coordinate  $s_j$  and right-end  $e_j$ ;

$track[j]$ : track to which net  $j$  is assigned.

**1 begin**

**2**  $U \leftarrow \{I_1, I_2, \dots, I_n\}$ ;

**3**  $t \leftarrow 0$ ;

**4 while** ( $U \neq \emptyset$ ) **do**

**5**    $t \leftarrow t + 1$ ;

**6**    $watermark \leftarrow 0$ ;

**7**   **while** (there is an  $I_j \in U$  s.t.  $s_j > watermark$ ) **do**

**8**       Pick the interval  $I_j \in U$  with  $s_j > watermark$ ,  
          nearest  $watermark$ ;

**9**        $track[j] \leftarrow t$ ;

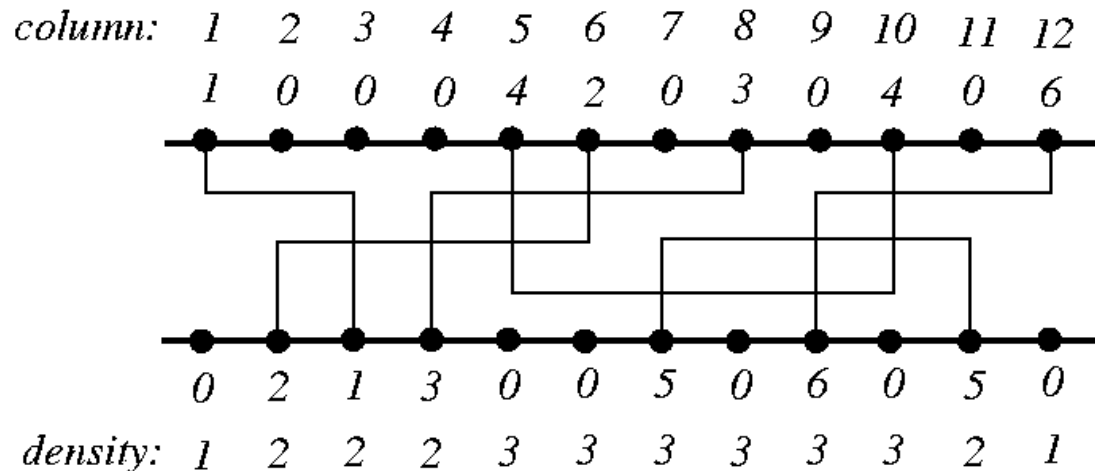
**10**       $watermark \leftarrow e_j$ ;

**11**       $U \leftarrow U - \{I_j\}$ ;

**12 end**

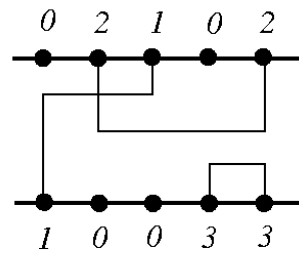
# Example

- $U = \{I_1, I_2, \dots, I_6\}$ ;  $I_1 = [1,3]$ ,  $I_2 = [2,6]$ ,  $I_3 = [4,8]$ ,  $I_4 = [5,10]$ ,  $I_5 = [7,11]$ ,  $I_6 = [9,12]$ .
- $t = 1$ :
  - Route  $I_1$ : watermark = 3;
  - Route  $I_3$ : watermark = 8;
  - Route  $I_6$ : watermark = 12;
- $t = 2$ :
  - Route  $I_2$ : watermark = 6;
  - Route  $I_5$ : watermark = 11;
- $t = 3$ : Route  $I_4$

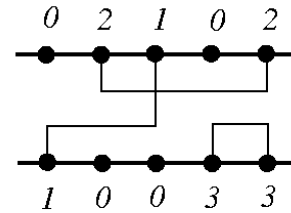


# Basic Left-Edge Algorithm

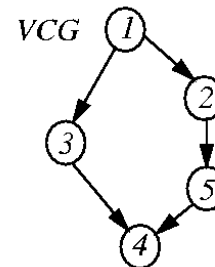
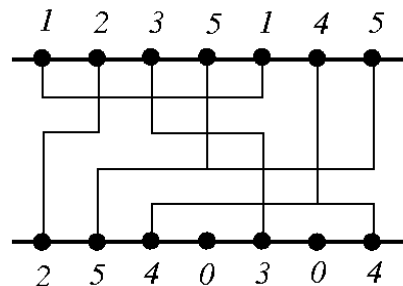
- If there is no vertical constraint, the basic left-edge algorithm is optimal.
- If there is any vertical constraint, the algorithm no longer guarantees optimal solution.



*result from basic  
left-edge algorithm  
3 tracks*



*optimal routing: 2 tracks*



# Constrained Left-Edge Algorithm

**Algorithm: Constrained\_Left-Edge( $U, track[j]$ )**

$U$ : set of unassigned intervals (nets)  $I_1, \dots, I_n$ ;

$I_j = [s_j, e_j]$ : interval  $j$  with left-end  $x$ -coordinate  $s_j$  and right-end  $e_j$ ;

$track[j]$ : track to which net  $j$  is assigned.

1 **begin**

2  $U \leftarrow \{I_1, I_2, \dots, I_n\}$ ;

3  $t \leftarrow 0$ ;

4 **while** ( $U \neq \emptyset$ ) **do**

5      $t \leftarrow t + 1$ ;

6      $watermark \leftarrow 0$ ;

7     **while** (there is an **unconstrained**  $I_j \in U$  s.t.  $s_j > watermark$ ) **do**

8         Pick the interval  $I_j \in U$  that is unconstrained,  
with  $s_j > watermark$ , nearest  $watermark$ ;

9          $track[j] \leftarrow t$ ;

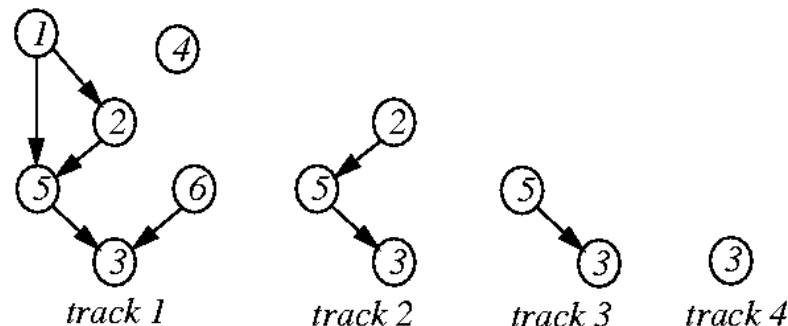
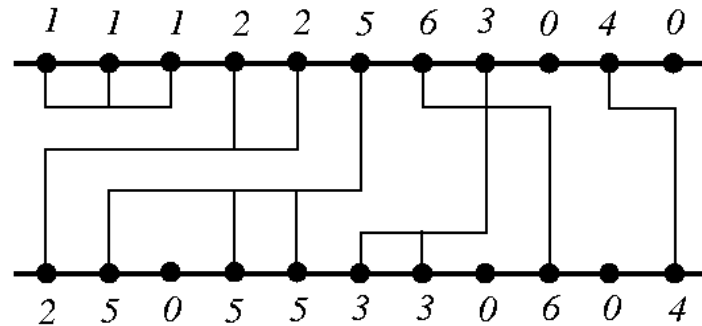
10         $watermark \leftarrow e_j$ ;

11         $U \leftarrow U - \{I_j\}$ ;

12 **end**

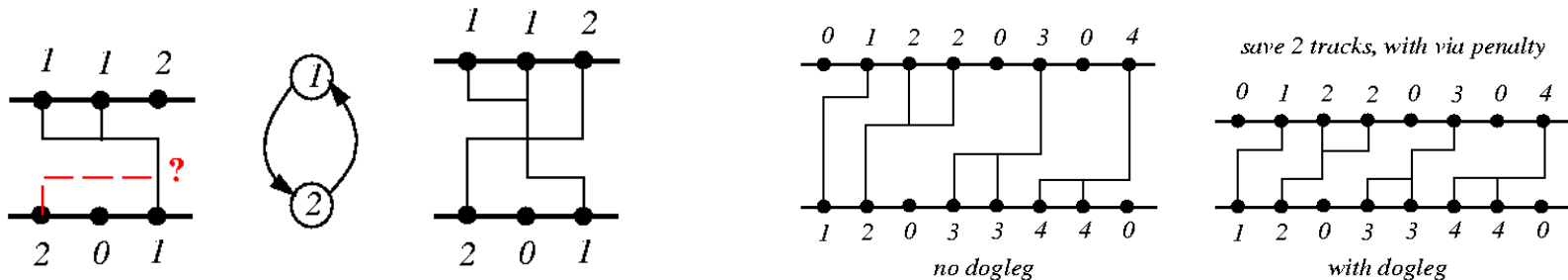
# Constrained Left-Edge Example

- $I_1 = [1,3]$ ,  $I_2 = [1,5]$ ,  $I_3 = [6,8]$ ,  $I_4 = [10,11]$ ,  $I_5 = [2,6]$ ,  $I_6 = [7,9]$ .
- Track 1: Route  $I_1$  (cannot route  $I_3$ ); Route  $I_6$ ; Route  $I_4$ .
- Track 2: Route  $I_2$ ; cannot route  $I_3$ .
- Track 3: Route  $I_5$ .
- Track 4: Route  $I_3$ .



# Dogleg Channel Router

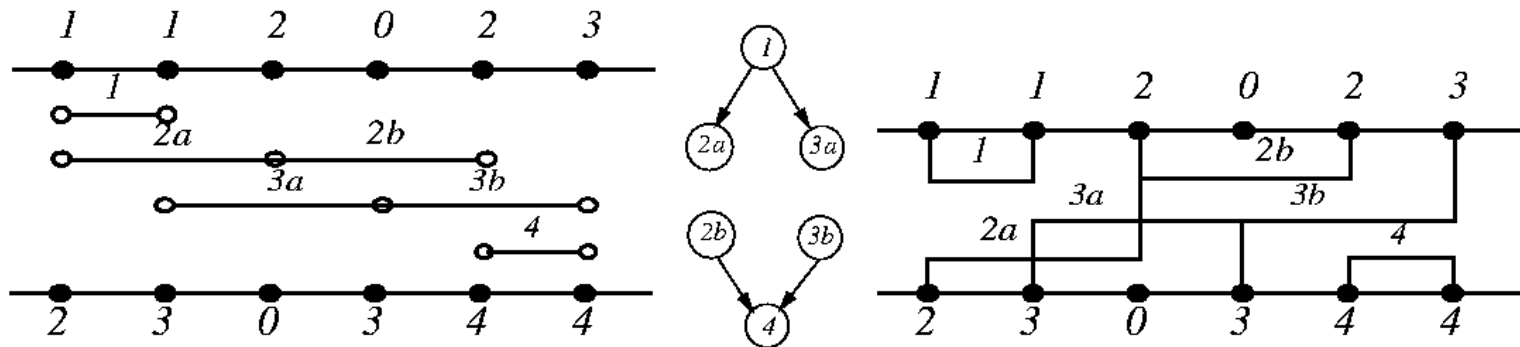
- Deutsch, “A dogleg channel router,” DAC, 1976.
- **Drawback of Left-Edge: cannot handle the cases with constraint cycles.**
  - **Doglegs** are used to resolve constraint cycle.
- **Drawback of Left-Edge: the entire net is on a single track.**
  - **Doglegs** are used to place parts of a net on different tracks to minimize channel height.
  - Might incur penalty for additional vias.





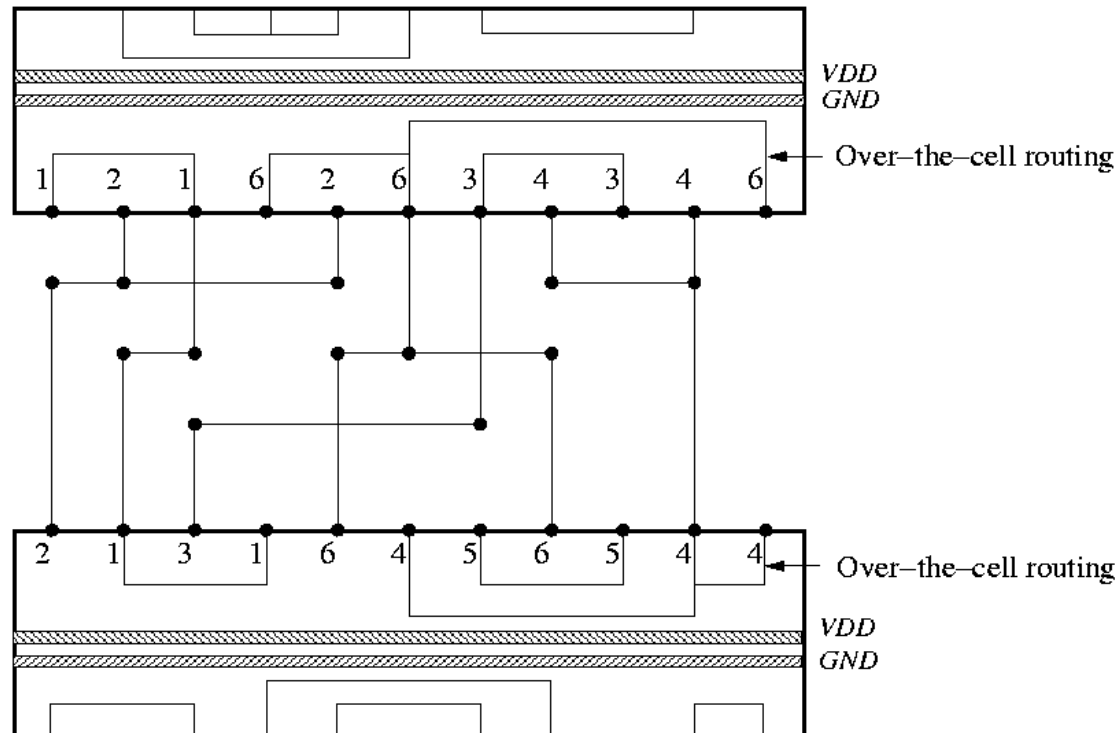
# Dogleg Channel Router

- Each multi-terminal net is broken into a set of 2-terminal nets.
- Two parameters are used to control routing:
  - Range: Determine the # of consecutive 2-terminal subnets of the same net that can be placed on the same track.
  - Routing sequence: Specifies the starting position and the direction of routing along the channel.
- Modified Left-Edge Algorithm is applied to each subnet.



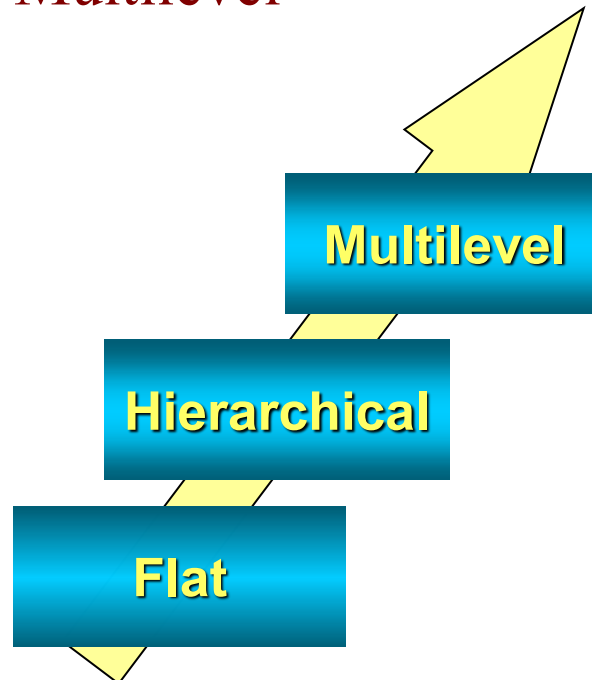
# Over-the-Cell Routing

- Routing over the cell rows is possible due to the limited use of the 2nd (M2) metal layers within the cells.
- Divide the over-the-cell routing problem into 3 steps: (1) routing over the cell, (2) choosing the net segments, and (3) routing within the channel.



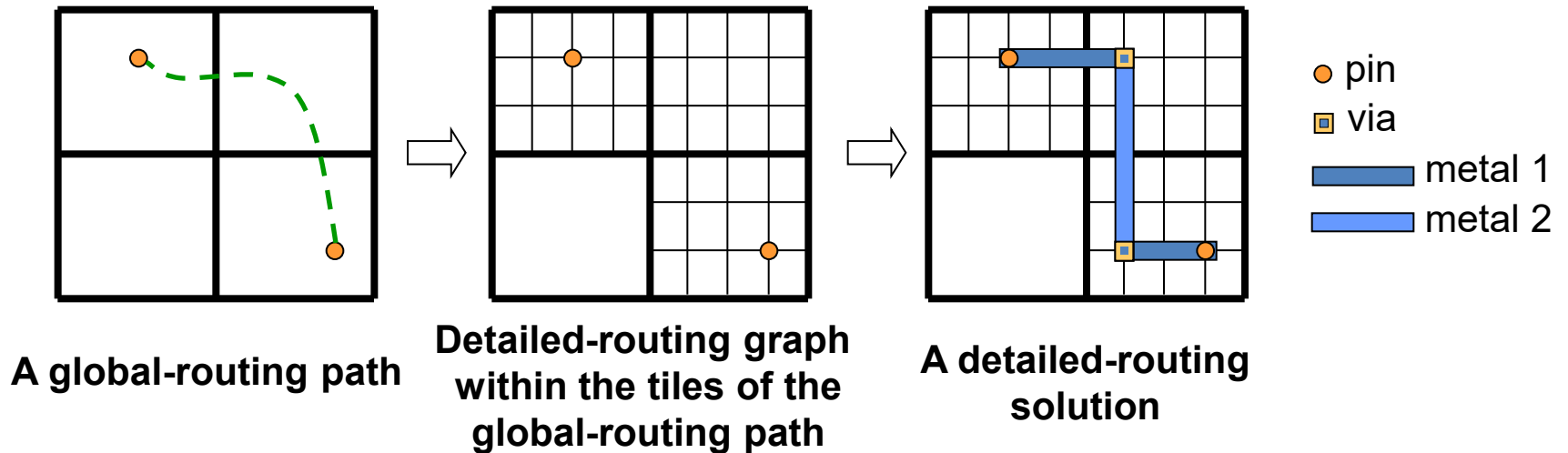
# Routing Framework Evolution

- Billions of transistors may be fabricated in a single chip for nanometer technology.
- Need frameworks for very large-scale designs.
- Framework evolution for EDA tools:  
**Flat → Hierarchical → Multilevel**



# Flat Routing Framework

- Global routing followed by detailed routing.
  - Maze searching, line searching, and/or A\*-searching



- Drawback: hard to handle larger problems