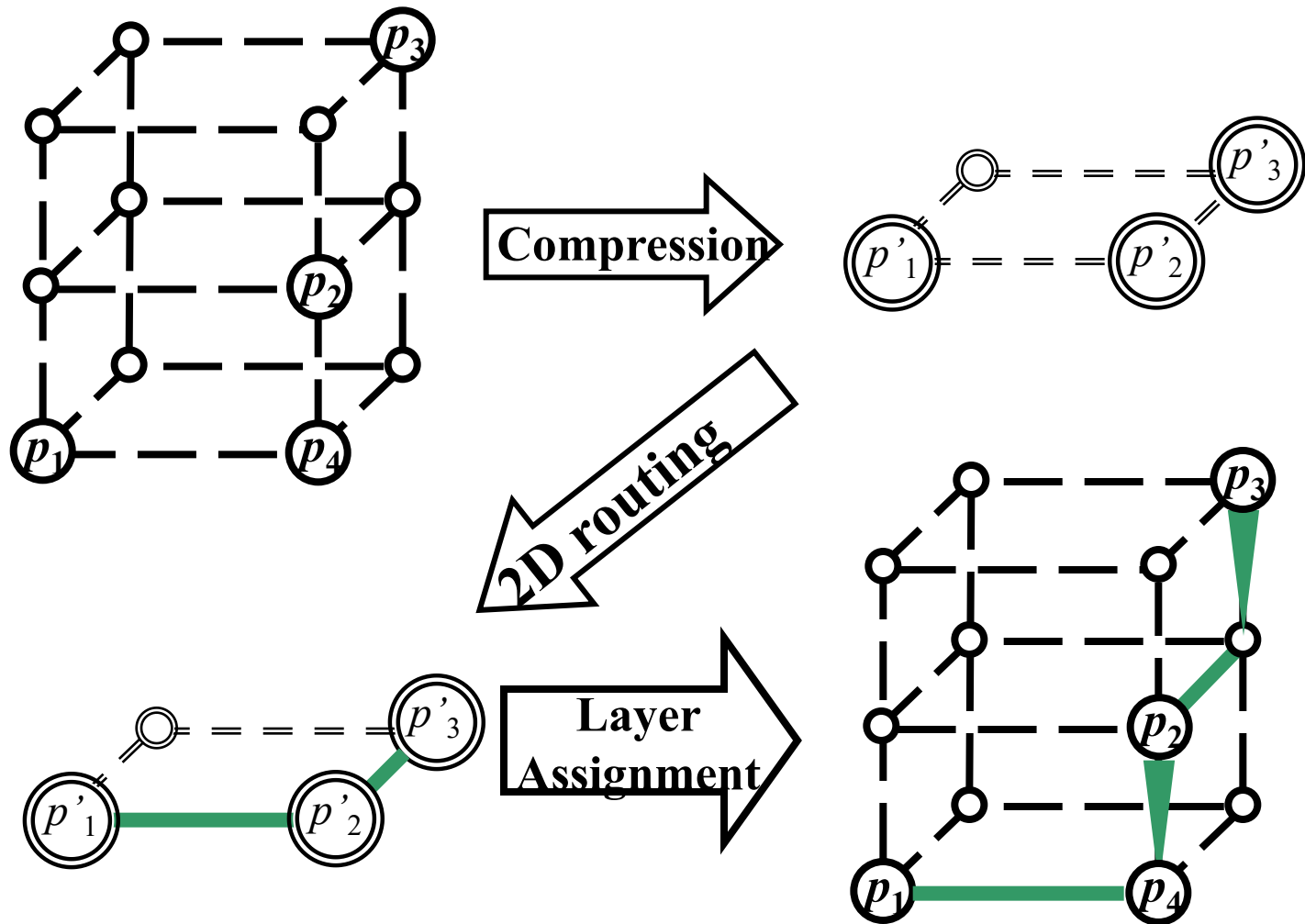


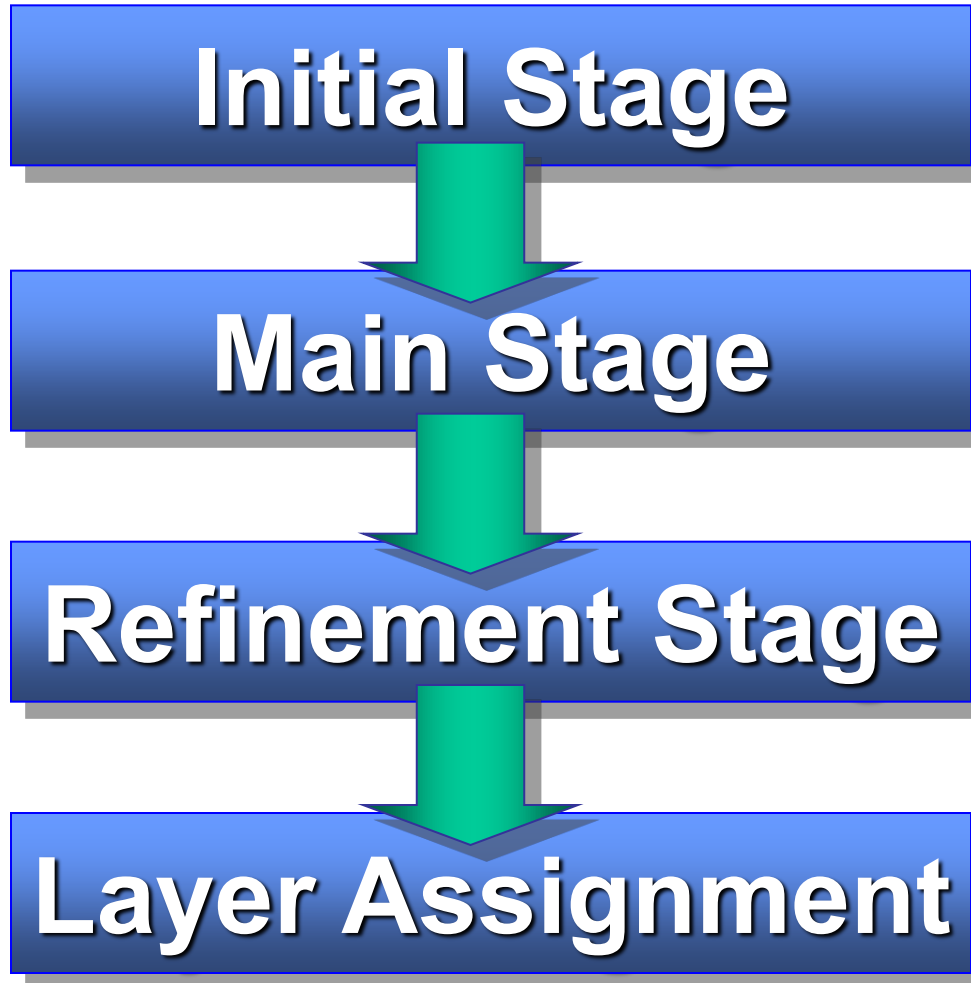
NTHU-Route 2.0

- Related publications:
 - Y.-J. Chang, Y.-T. Lee, J.-R. Gao, P.-C. Wu, and T.-C. Wang, “NTHU-Route 2.0: A Robust Global Router for Modern Designs,” IEEE TCAD 2010.
 - Y.-J. Chang, Y.-T. Lee and T.-C. Wang, “NTHU-Route 2.0: A Fast and Stable Global Router,” ICCAD 2008.
 - J.-R. Gao, P.-C. Wu and T.-C. Wang, “A New Global Router for Modern Designs,” ASP-DAC 2008. (NTHU-Route)
 - T.-H. Lee and T.-C. Wang, “Congestion-Constrained Layer Assignment for Via Minimization in Global Routing,” IEEE TCAD 2008.

Multi-Layer Global Routing



Four Stages



Initial Stage

Decompose using FLUTE

Route with two probabilistic L-shaped patterns

Modify net topology by edge shifting

Reroute with least-cost L-shaped pattern

- First project the design onto a plane
- FLUTE [ISPD05]
 - Generation of a rectilinear Steiner minimal tree
 - A look-up table based method
 - Optimum for net with 9 or fewer pins

Initial Stage (cont'd)

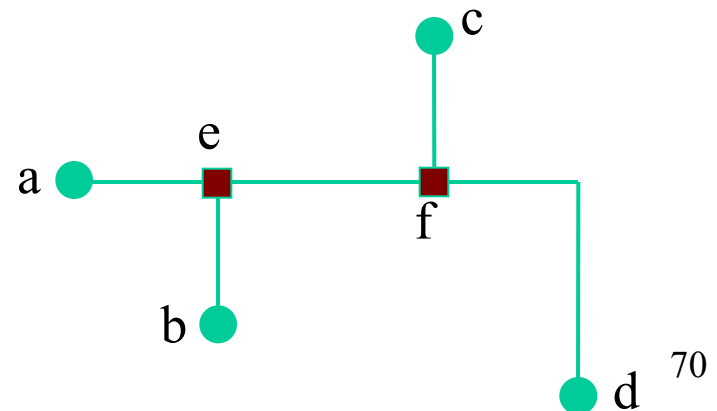
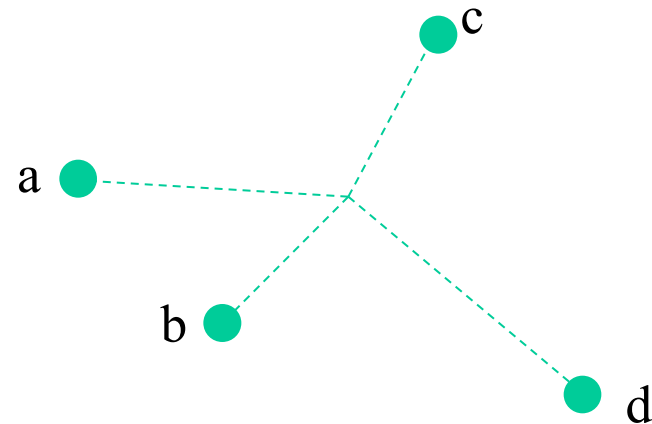
Decompose using FLUTE

Route with two probabilistic L-shaped patterns

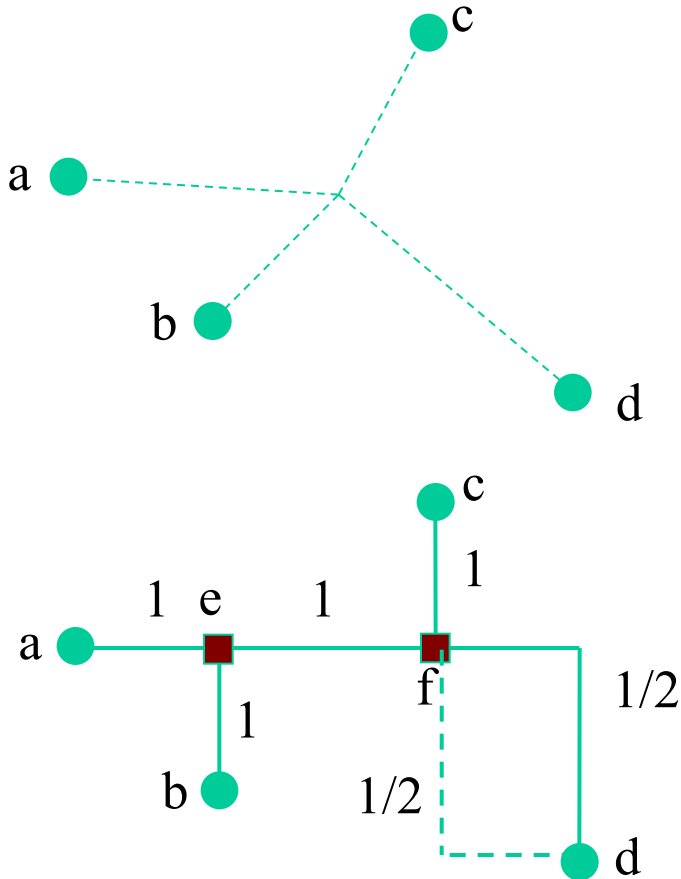
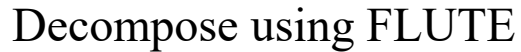
Modify net topology by edge shifting

Reroute with least-cost L-shaped pattern

- Add $\frac{1}{2}$ demand along each edge of an L-shaped path



Initial Stage (cont'd)



Initial Stage (cont'd)

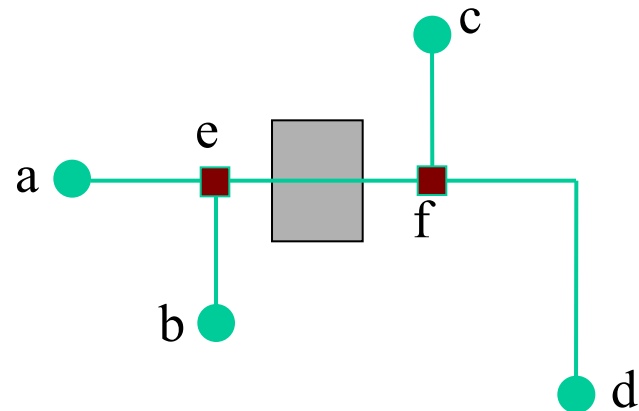
Decompose using FLUTE

Route with two probabilistic L-shaped patterns

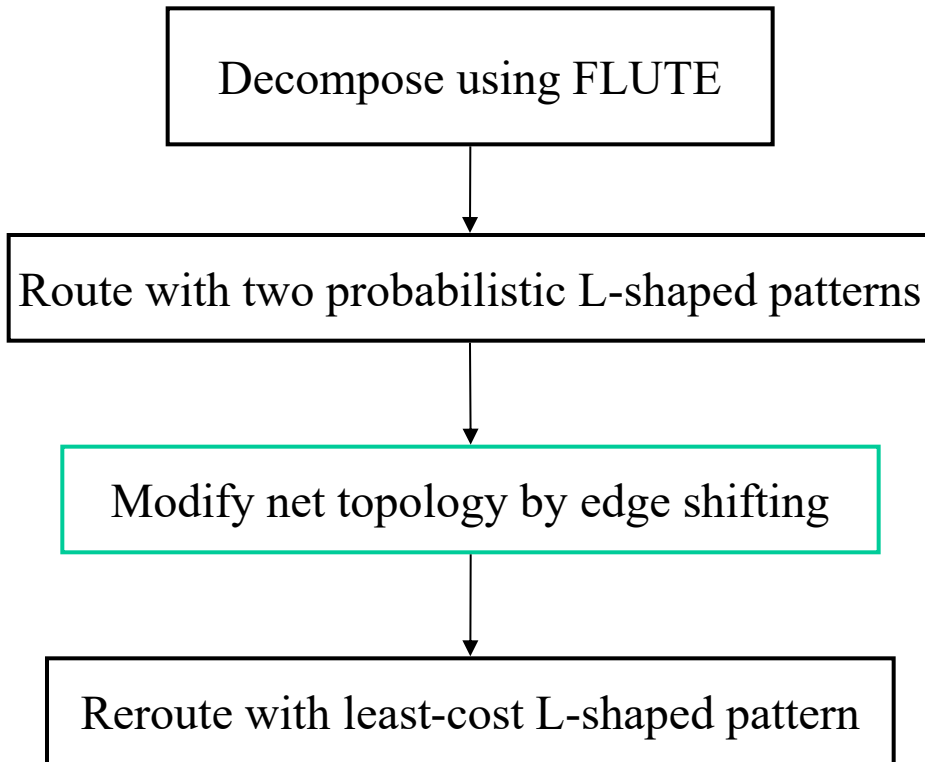
Modify net topology by edge shifting

Reroute with least-cost L-shaped pattern

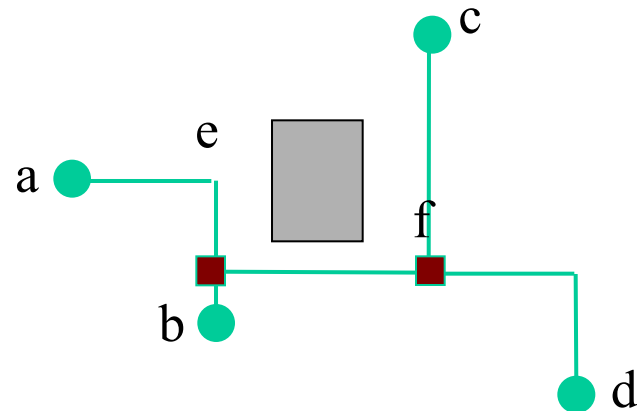
- Edge shifting [ICCAD06]
 - Move edges to less congested regions
 - Does not increase wirelength



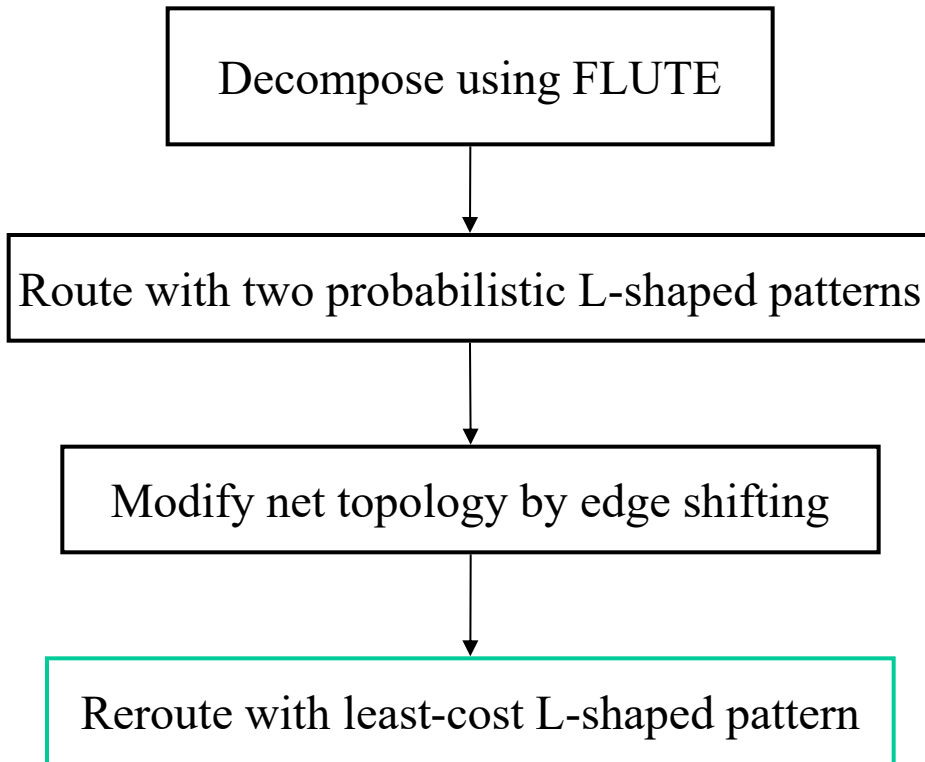
Initial Stage (cont'd)



- Edge Shifting [ICCAD06]
 - Move edges to less congested regions
 - Does not increase wirelength



Initial Stage (cont'd)

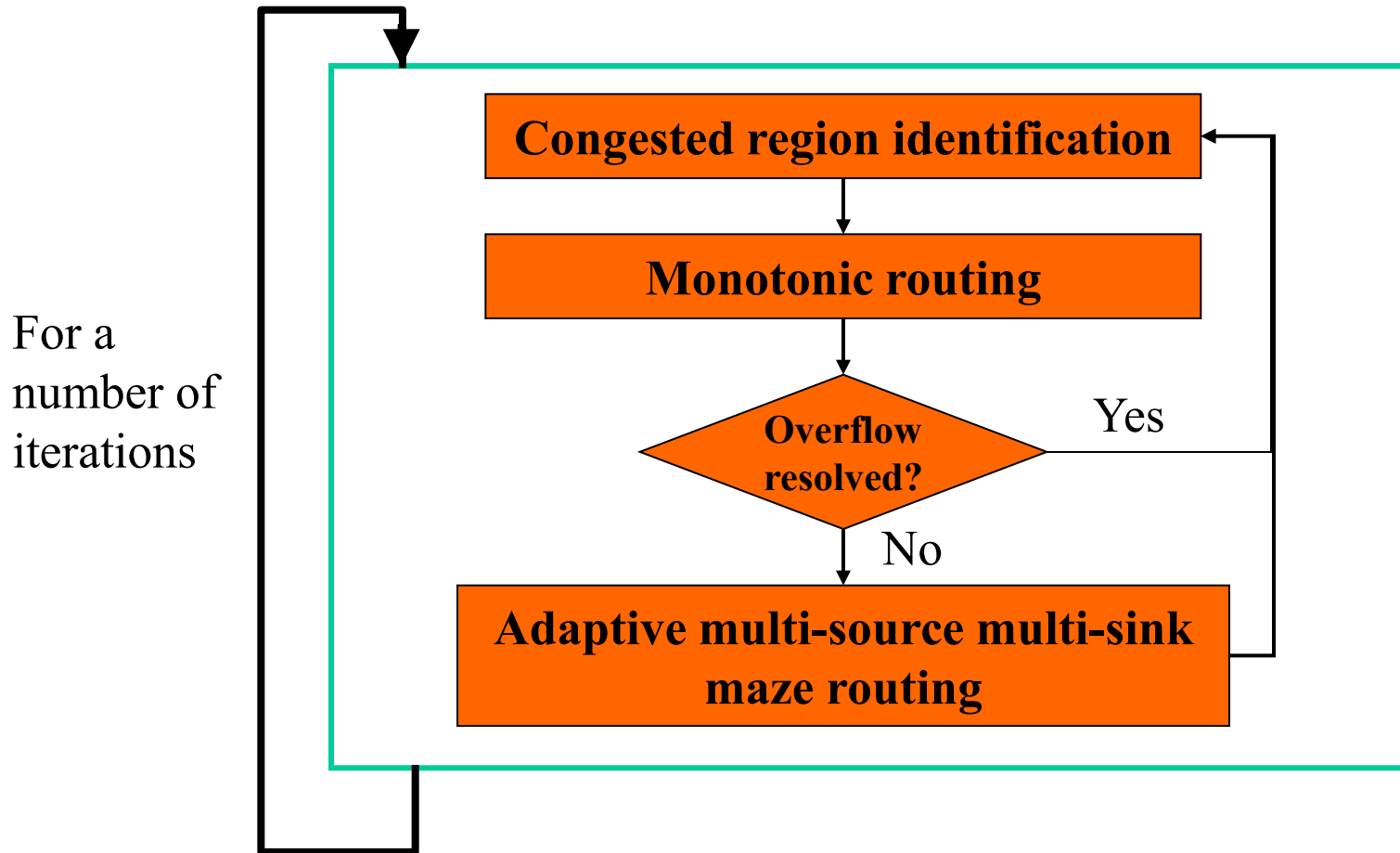


- Reroute all 2-pin nets in increasing order of the size of bounding box
- Add 1 demand to each edge along the chosen L-shaped path

$$cost_e = 1 + \frac{a}{1 + e^{-b*(d(e)-s(e))}}$$

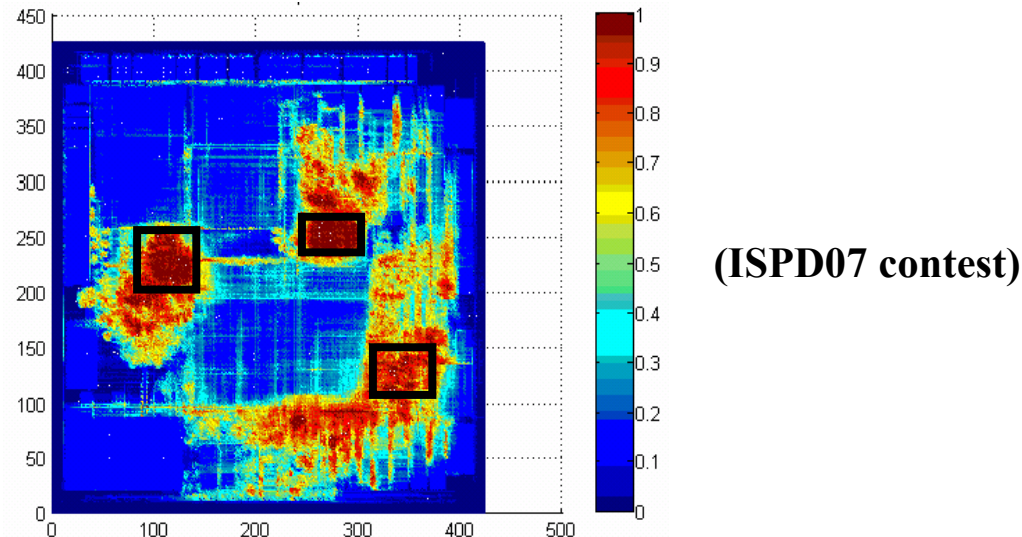
[ICCAD06]

Main Stage



Rip-up and Reroute Based on Congested Region Identification

- The order of nets to be ripped up & rerouted affects the routing quality very much
- An algorithm is proposed to identify congested regions and rip-up & reroute two-pin nets with similar congestion at a time



Congested Region Identification

- Partition the interval between the maximum congestion value and 1 into 10 sub-intervals
 - Each congested edge belongs to a sub-interval
- For each sub-interval I_k
 - Expand a rectangular region r_e from each edge e until $avg_cong(r_e)$ is smaller than the lower bound of I_k

$$avg_cong(r_e) = \frac{\sum d(e)}{\sum s(e)} \quad e_i \text{ is an edge inside } r_e$$

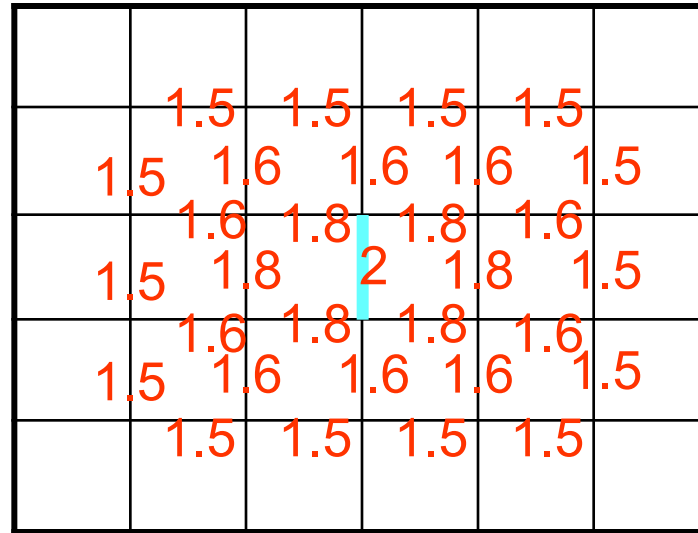
- Find two-pin nets within each region
- For each 2-pin net in non-increasing order of bounding box size
 - Rip-up & reroute using monotonic routing
 - Adaptive multi-source multi-sink maze routing, if necessary

An Example of Region Identification

| | | | | | |
|--|-----|-----|-----|-----|-----|
| | | | | | |
| | 1.5 | 1.5 | 1.5 | 1.5 | |
| | 1.5 | 1.6 | 1.6 | 1.6 | 1.5 |
| | 1.6 | 1.8 | 1.8 | 1.6 | |
| | 1.5 | 1.8 | 2 | 1.8 | 1.5 |
| | 1.6 | 1.8 | 1.8 | 1.6 | |
| | 1.5 | 1.6 | 1.6 | 1.6 | 1.5 |
| | 1.5 | 1.5 | 1.5 | 1.5 | |

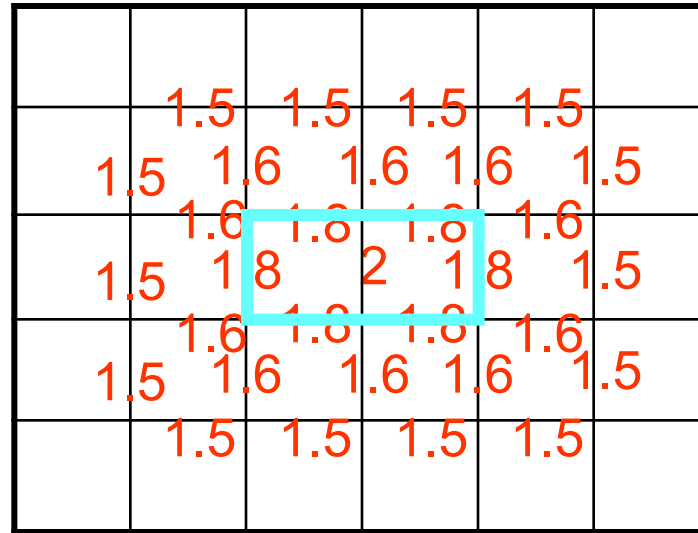
- Partition $[2, 1]$
 $\rightarrow \{[1.1, 1), [1.2, 1.1), \dots, [1.9, 1.8), [2, 1.9)]\}$

An Example of Region Identification



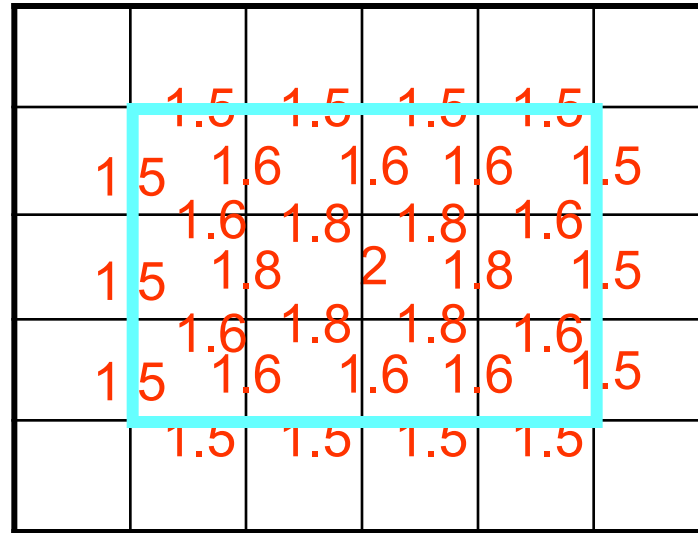
- Partition $[2, 1]$
 $\rightarrow \{[1.1, 1), [1.2, 1.1), \dots, [1.9, 1.8), [2, 1.9)\}$

An Example of Region Identification



- Partition $[2, 1]$
 $\rightarrow \{[1.1, 1), [1.2, 1.1), \dots, [1.9, 1.8), [2, 1.9)\}$

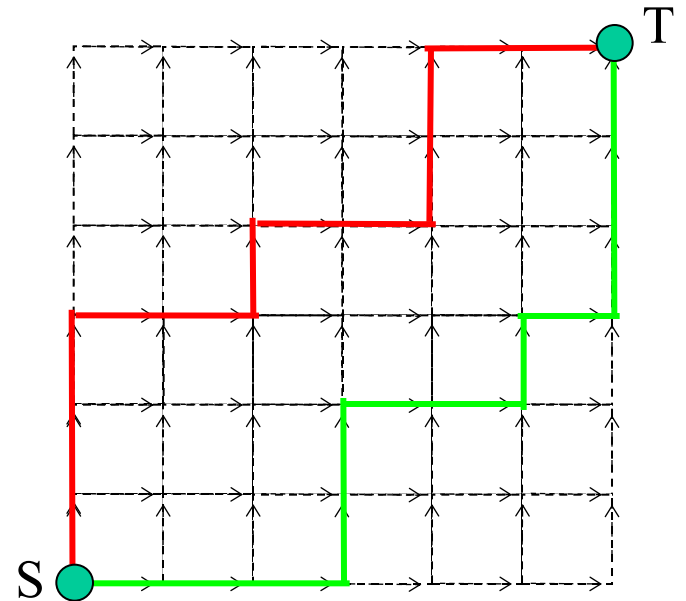
An Example of Region Identification



- Partition $[2, 1]$
 $\rightarrow \{[1.1, 1), [1.2, 1.1), \dots, [1.9, 1.8), [2, 1.9)]\}$

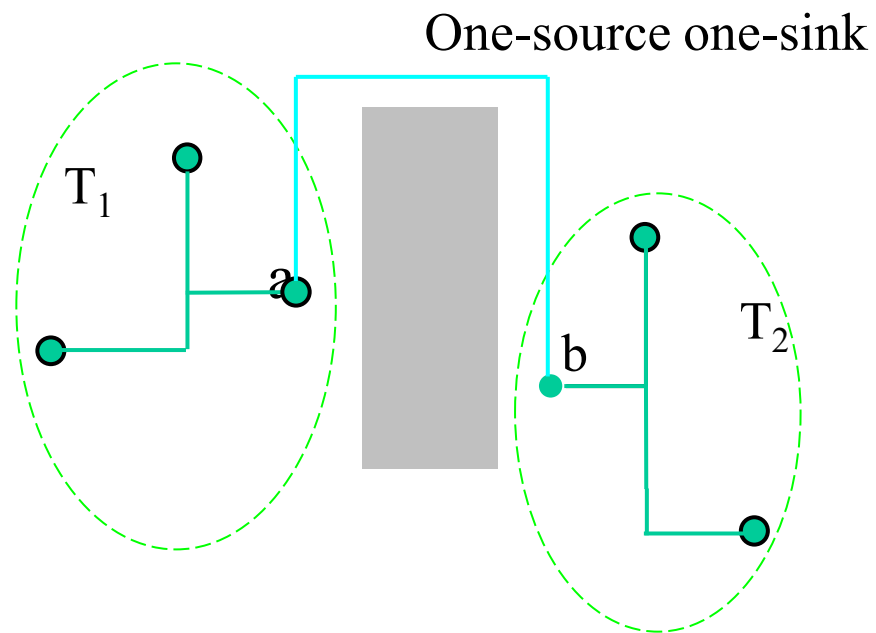
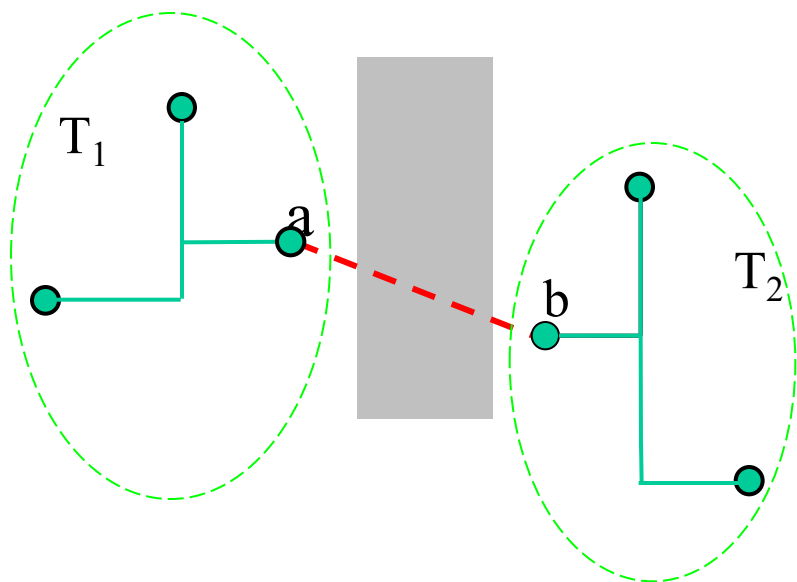
Monotonic Routing

- Proposed in [ASPDAC07]
- Finds the routing path in the direction toward T within the bounding box formed by S and T
- Can be done by dynamic programming with the same complexity as Z-shaped pattern routing

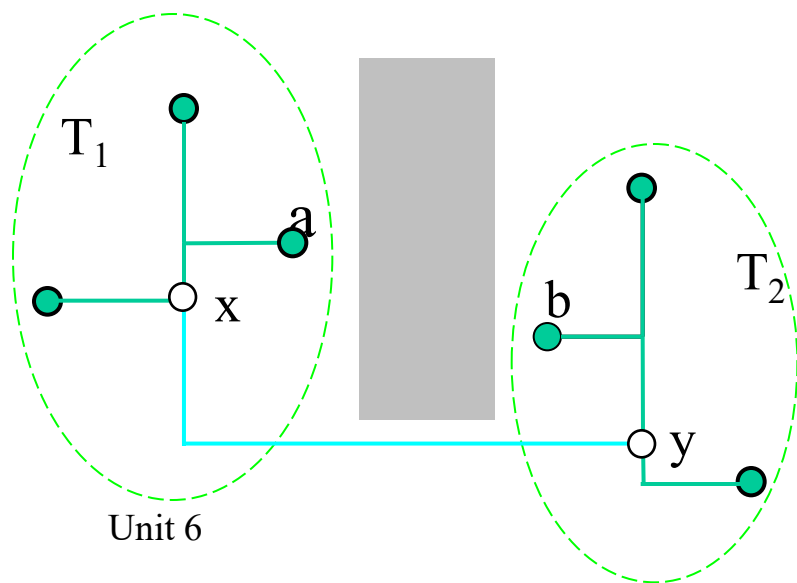


Adaptive Multi-Source Multi-Sink Maze Routing

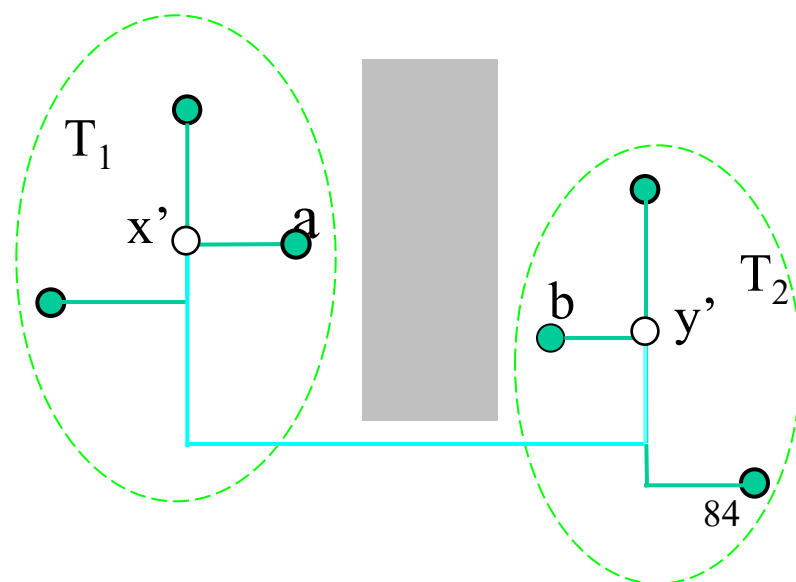
- General maze routing
 - One-source one-sink
- Multi-source multi-sink maze routing
 - Treat all grid points on one subtree as sources
 - Sinks are grid points on another subtree
- Adaptive multi-source multi-sink maze routing
 - Treat only pins or Steiner points as sources and sinks
 - More efficient



Multi-source multi-sink



Adaptive multi-source multi-sink



History Based Cost Function

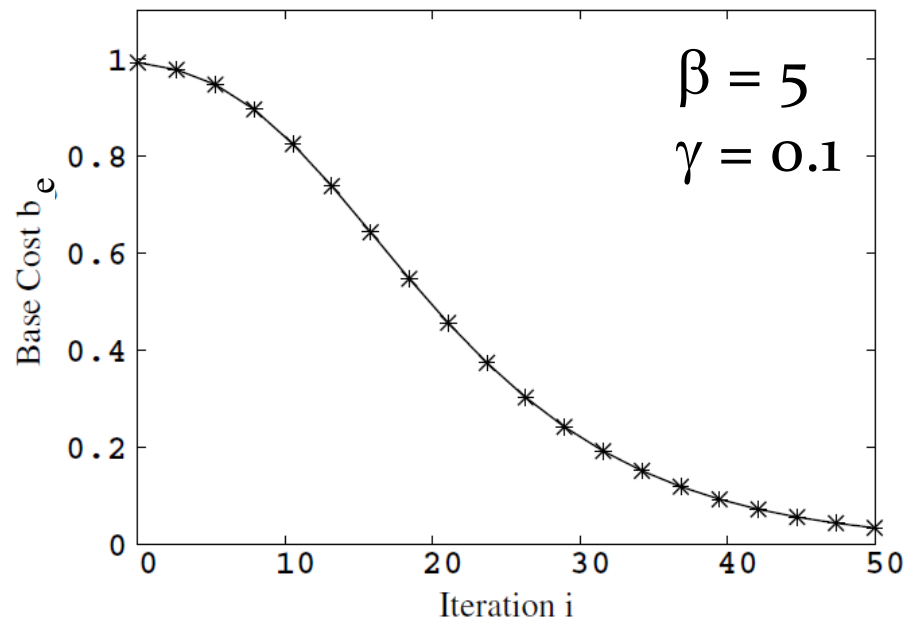
$$cost_e = b_e + h_e \times p_e + vc_e$$

- b_e : adaptive base cost function
- $h_e \times p_e$: congestion cost function with overflow prediction
- vc_e : via cost function for multi-layer design
- Sharing edges does not need additional cost

Adaptive Base Cost Function

- Provides a base cost between 1 to 0 adaptively

$$b_e = 1 - e^{-\beta e^{-\gamma i}}$$



Congestion Cost Function with Overflow Prediction

- $h_e \times p_e$: congestion cost

– h_e : historical term

$$h_e^{i+1} = \begin{cases} h_e^i + 1 & \text{if } e \text{ has overflow} \\ h_e^i & \text{otherwise} \end{cases}$$

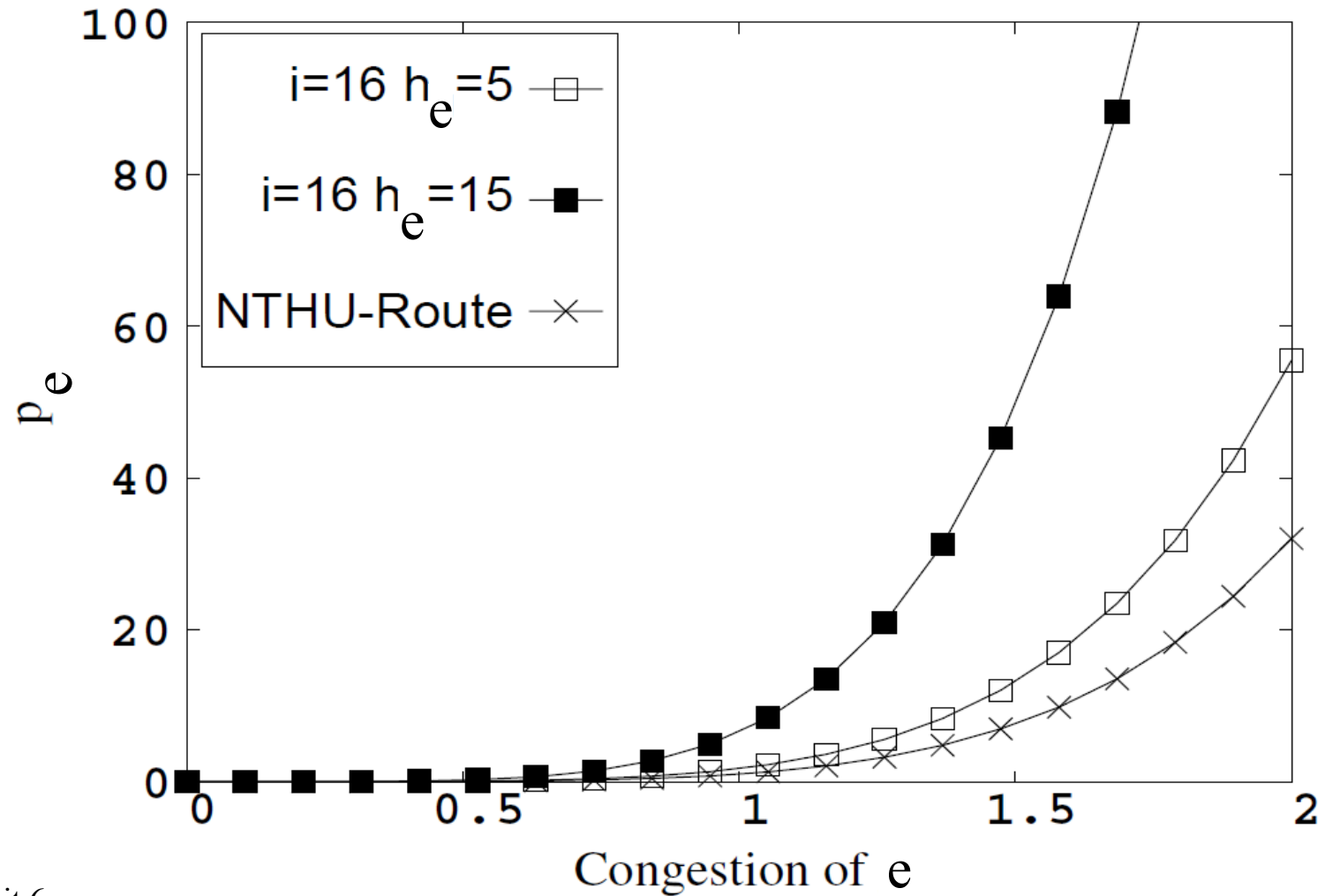
– p_e : current congestion penalty

$$p_e = \left(\frac{d_e + 1}{c_e} \times f(h_e, i) \right)^{k1} \quad f(h_e, i) = \left(\frac{i \times (k_2 + adj(i))}{i \times (k_2 + adj(i)) - (h_e - 1)} \right)$$

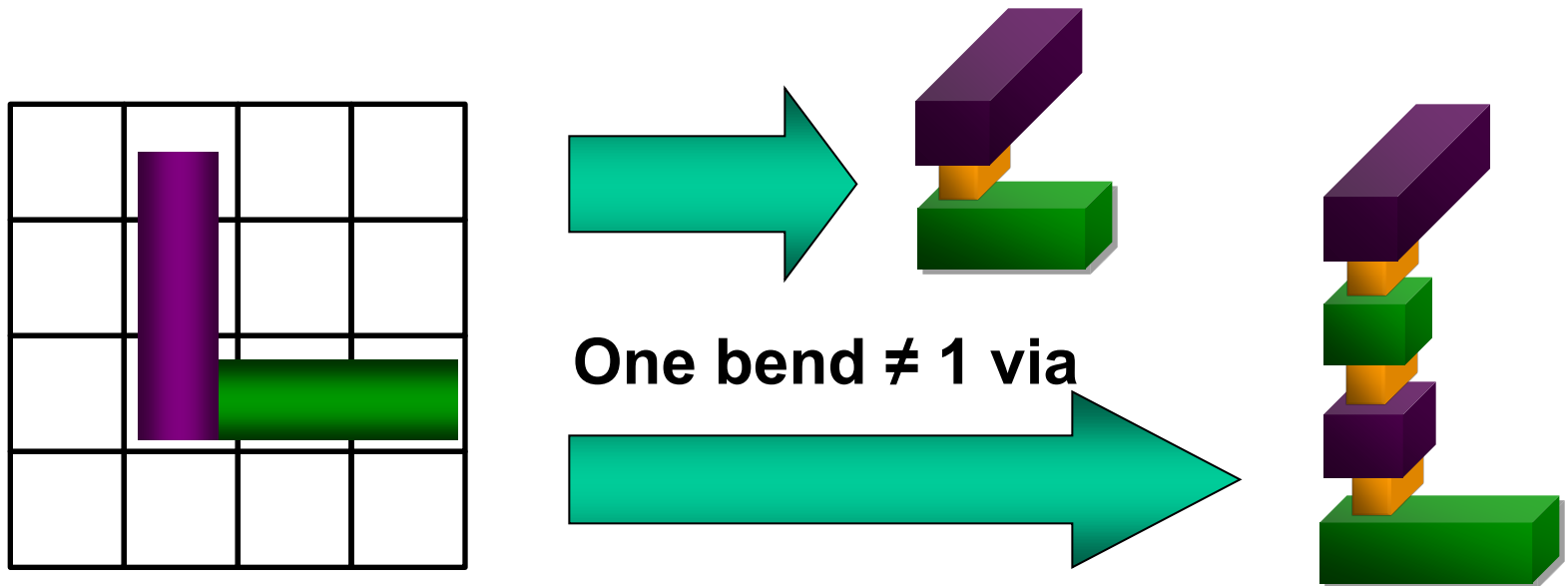
$$adj(i) = k_3 \times (1 - e^{-\beta e^{-\gamma i}})$$

- $f(h_e, i)$: amplify congestion value if e has high probability to have overflow

Curves of Penalty Terms



Via Cost Function for Multi-layer Design



$$v c_e = \begin{cases} v_e \times c_e \times b_e & \text{if passage makes a bend,} \\ 0 & \text{otherwise} \end{cases}$$

- v_e : the expected amount of vias for a bend
- c_e : the wirelength of a via
- b_e : adaptive base cost function