

Calculator Program Notes

Pohlig-Hellman on calculator:

- First, factor the group order yourself!
- Then start the program, and input your h , g (generator) and modulus
- Now QS is the number of factors
- Now input the factors, and after that, input the powers of the factors

Fermat test.

TRIVIAAL. Gebruik programma ervoor niet! (doet namelijk iets raars met square and multiply).

Take an a , and check if:

$$a^{n-1} \equiv 1 \pmod{n}$$

Example, $a = 2$ and $n = 4891$:

$$2^{4890} \equiv 3950 \not\equiv 1 \pmod{4891}$$

```
Mod(2^4890,4891)
```

```
Mod(3950, 4891)
```

Since $2^{4890} \not\equiv 1 \pmod{4891}$, thus n is not prime.

Calculate lcm of multiple numbers

$$\text{lcm}(\{1, 2, 3, 4\}) = \text{lcm}(\text{lcm}(1, 2), \text{lcm}(3, 4))$$

```
lcm([1,2,3,4])
```

```
lcm(lcm(1,2), lcm(3,4))
```

```
12
```

```
12
```

Inverse of a number modulo n

Inverse of g , modulo n . First calculate the XGCD, with $xg + yn = 1$ (otherwise it is not invertible). Then, x is the inverse. If x is negative, do modulo n to obtain positive.

Example: $g = 7, n = 34567$. Calculate $g^{-1} \bmod n$. First calculate the XGCD, which gives $-4938 \cdot 7 + 1 \cdot 34567 = 1$ $g^{-1} \equiv -4938 \equiv 29629 \bmod 34567$

```
gcdext(7, 34567)
```

```
Mod(-4938, 34567)
```

```
Mod(7^-1, 34567)
```

```
[-4938, 1, 1]
```

```
Mod(29629, 34567)
```

```
Mod(29629, 34567)
```

Order of a point in Edwards curve

Given a point P , calculate $2P, 3P, 4P, \dots$ until $n \cdot P = P$ with $n \in \mathbb{N}$.

The order of P is the smallest $n \in \mathbb{N}, n \neq 1$ such that $n \cdot P = P$