# Package 'GMMSensitivity'

July 27, 2020
Title Confidence intervals for sensitivity analysis in GMM
Version 0.1.1
<b>Description</b> Construct confidence intervals in generalized method of moments (GMM) models that are valid under local misspecification.
<b>Depends</b> R (>= $4.0.0$ )
License GPL-3
Encoding UTF-8
Suggests spelling, testthat, knitr, CVXR, rmarkdown
Imports stats
RoxygenNote 7.1.1
VignetteBuilder knitr
LazyData true
Language en-US
<pre>URL https://github.com/kolesarm/GMMSensitivity/</pre>
BugReports https://github.com/kolesarm/GMMSensitivity/issues
R topics documented:
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Estimates from Berry, Levinsohn, and Pakes (1995)

## **Description**

This dataset contains estimates of the model in Berry, Levinsohn, and Pakes (1995), as implemented by Andrews, Gentzkow, and Shapiro (2017), and it is used to illustrate the confidence intervals implemented in this package.

## Usage

blp

#### **Format**

A list, consisting 11 objects:

- **G** Matrix with 31 rows and 17 columns, estimate of derivative of the moment condition evaluated at initial estimate of  $\theta$  from Berry, Levinsohn, and Pakes (1995),  $\hat{\theta}$ .
- **H** Vector of length 17, estimate of derivative of average markup  $h(\theta)$  with respect to model parameters  $\theta$ , evaluated at  $\hat{\theta}$ .
- **W** Weight matrix used to obtain the estimate  $\hat{\theta}$ .
- **g\_init** Average moment condition, evaluated at  $\hat{\theta}$ .
- **h\_init** Estimate of the average markup,  $h(\hat{\theta})$ .
- **names** Two lists, one for names of the moment conditions, and one for elements of  $\theta$ .
- **ZZ** Gram matrix Z'Z of the instruments, used to specify the misspecification set C.
- **Sig** Estimate of variance of moment condition.
- sdZ Vector of standard deviations of the instruments.
- **perturb** scaling parameters to give interpretable meaning to violations of supply-side conditions. See vignette vignette("GMMSensitivity", package="GMMSensitivity") for details.
- **n** Sample size, number of model/years.

See Armstrong and Kolesár (2018) for a detailed description of these objects.

### Source

Replication files for Andrews, Gentzkow, and Shapiro (2017), available at https://doi.org/10.7910/DVN/LLARSN

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### References

Andrews, I., M. Gentzkow, and J. M. Shapiro (2017): Measuring the Sensitivity of Parameter Estimates to Sample Statistics, Quarterly Journal of Economics, 132, 1553–1592.

Armstrong, T. B., and M. Kolesár (2018): Sensitivity Analysis Using Approximate Moment Condition Models, Unpublished manuscript

Berry, S. T., J. Levinsohn, and A. Pakes (1995): Automobile Prices in Market Equilibrium, Econometrica, 63, 841–890.

**EffBounds** 

Efficiency bounds under  $\ell_p$  constraints

## **Description**

Computes the asymptotic efficiency of two-sided fixed-length confidence intervals at c=0, as well as the efficiency of one-sided confidence intervals that optimize a given beta quantile of excess length, when the set C is characterized by  $\ell_p$  constraints.

## Usage

```
EffBounds(eo, B, M, p = 2, beta = 0.5, alpha = 0.05, cvx = FALSE)
```

## **Arguments**

В

eo List containing initial estimates with the following components	eo	List containing initial estimates with the following components:
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**Sig** Estimate of variance of the moment condition, matrix with dimension  $d_g$  by  $d_g$ , where  $d_g$  is the number of moments

**G** Estimate of derivative of the moment condition, matrix with dimension  $d_g$  by  $d_{\theta}$ , where  $d_{\theta}$  is the dimension of  $\theta$ 

**H** Estimate of derivative of  $h(\theta)$ . A vector of length  $d_{\theta}$ 

n sample size

**h\_init** Estimate of  $h(\theta)$  **k init** Initial sensitivity

**g\_init** Moment condition evaluated at initial estimate

matrix B with full rank and dimension  $d_g$  by  $d_{\gamma}$  that determines the set C, where  $d_{\gamma}$  is the number of invalid moments, and  $d_g$  is the number of moments

M Bound on the norm of  $\gamma$ 

Parameter determining which  $\ell_p$  norm to use, must equal 1, 2, or Inf.

beta Quantile of excess length that a one-sided confidence interval is optimizing.

alpha determines confidence level, 1-alpha, for constructing/optimizing confidence

intervals.

cvx By default, the efficiency for p=1 and for p=Inf is computed using the homo-

topy algorithm described in Appendix A of Armstrong and Kolesár (2018). If cvx=TRUE is specified, the modulus is computed using the CVX convex optimizer. This option is included mostly just to verify that the homotopy solution

correct.

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## **Details**

The set C takes the form  $B\gamma$  where the  $\ell_p$  norm of  $\gamma$  is bounded by M.

### References

Armstrong, T. B., and M. Kolesár (2018): Sensitivity Analysis Using Approximate Moment Condition Models, Unpublished manuscript

**Jtest** 

J-test of overidentifying restrictions under local misspecification

## **Description**

Computes J-test of overidentifying restrictions with critical value adjusted to allow for local misspecification, when the parameter c takes the form  $c=B\gamma$  with the  $\ell_p$  norm of  $\gamma$  bounded by M. Assumes initial estimator in eo is optimal under correct specification.

## Usage

```
Jtest(eo, B, M, p = 2, alpha = 0.05)
```

## **Arguments**

В

М

eo List containing initial estimates with the following components:

**Sig** Estimate of variance of the moment condition, matrix with dimension  $d_g$  by  $d_g$ , where  $d_g$  is the number of moments

**G** Estimate of derivative of the moment condition, matrix with dimension  $d_g$  by  $d_\theta$ , where  $d_\theta$  is the dimension of  $\theta$ 

**H** Estimate of derivative of  $h(\theta)$ . A vector of length  $d_{\theta}$ 

n sample size

**h\_init** Estimate of  $h(\theta)$ 

**k\_init** Initial sensitivity

g\_init Moment condition evaluated at initial estimate

matrix B with full rank and dimension  $d_g$  by  $d_\gamma$  that determines the set C, where  $d_\gamma$  is the number of invalid moments, and  $d_g$  is the number of moments

Bound on the norm of  $\gamma$ 

Parameter determining which  $\ell_p$  norm to use, must equal 1, 2, or Inf.

alpha determines confidence level, 1-alpha, for constructing/optimizing confidence

intervals.

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## Value

List with three elements:

J Value of J statistic

**p0** P-value of usual J test

pC P-value for J-test that allows for local misspecification

**Mmin** Minimum value of M for which the J-test would not reject

1ph

Compute solution path for  $\ell_{-}\infty$  or  $\ell_{-}1$  constraints

## **Description**

Computes the vector of optimal sensitivities at each knot of the solution path that traces out the optimal bias-variance frontier when the set C takes the form  $c=B\gamma$  with the  $\ell_p$  norm of  $\gamma$  is bounded by a constant, for p=1, or  $p=\infty$ . This path is used as an input to OptEstimator.

## Usage

```
lph(eo, B, p = Inf)
```

## **Arguments**

eo List containing initial estimates with the following components:

**Sig** Estimate of variance of the moment condition, matrix with dimension  $d_g$  by  $d_g$ , where  $d_g$  is the number of moments

**G** Estimate of derivative of the moment condition, matrix with dimension  $d_g$  by  $d_\theta$ , where  $d_\theta$  is the dimension of  $\theta$ 

**H** Estimate of derivative of  $h(\theta)$ . A vector of length  $d_{\theta}$ 

**n** sample size

**h\_init** Estimate of  $h(\theta)$ 

k init Initial sensitivity

**g\_init** Moment condition evaluated at initial estimate

matrix B with full rank and dimension  $d_g$  by  $d_{\gamma}$  that determines the set C, where  $d_{\gamma}$  is the number of invalid moments, and  $d_g$  is the number of moments

p Parameter determining which ell\_p norm to use, one of 1, or Inf.

#### **Details**

В

The algorithm is described in Appendix A of Armstrong and Kolesár (2018)

## References

Armstrong, T. B., and M. Kolesár (2018): Sensitivity Analysis Using Approximate Moment Condition Models, Unpublished manuscript

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OptEstimator

One-step estimator based on optimal sensitivity under  $\ell_p$  constraints

## **Description**

Computes the optimal sensitivity and the optimal estimator when the set C takes the form  $c = B\gamma$  with the  $\ell_p$  norm of  $\gamma$  bounded by M.

## Usage

```
OptEstimator(
  eo,
  B,
  M,
  p = 2,
  spath = NULL,
  alpha = 0.05,
  opt.criterion = "FLCI"
)
```

### **Arguments**

В

eo List containing initial estimates with the following components:

**Sig** Estimate of variance of the moment condition, matrix with dimension  $d_g$  by  $d_g$ , where  $d_g$  is the number of moments

**G** Estimate of derivative of the moment condition, matrix with dimension  $d_g$  by  $d_\theta$ , where  $d_\theta$  is the dimension of  $\theta$ 

**H** Estimate of derivative of  $h(\theta)$ . A vector of length  $d_{\theta}$ 

n sample size

**h\_init** Estimate of  $h(\theta)$ 

**k\_init** Initial sensitivity

**g\_init** Moment condition evaluated at initial estimate

matrix B with full rank and dimension  $d_g$  by  $d_{\gamma}$  that determines the set C, where

 $d_{\gamma}$  is the number of invalid moments, and  $d_g$  is the number of moments

M Bound on the norm of  $\gamma$ 

Parameter determining which  $\ell_p$  norm to use, must equal 1, 2, or Inf.

spath Optionally, the solution path, output of 1ph to speed up computation. For p==1

and p==Inf only.

alpha determines confidence level, 1-alpha, for constructing/optimizing confidence

intervals.

opt.criterion Optimality criterion for choosing optimal bias-variance tradeoff. The options

are:

"MSE" Minimize worst-case mean squared error of the estimator.

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"FLCI" Length of (fixed-length) two-sided confidence intervals.

"Valid" Optimal estimator under valid moments. This returns the original estimator, with confidence intervals adjusted for possible misspecification

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