

# SUMS OF POWERS VIA CENTRAL FINITE DIFFERENCES AND NEWTON'S FORMULA

PETRO KOLOSOV

ABSTRACT. In this manuscript we derive formula for multifold sums of powers using Newton's formula in central differences. Furthermore, we show that famous Knuth's formula for multifold sums of odd powers originates from Newton's interpolation formula in central differences.

## CONTENTS

1. Introduction	1
Conclusions	10
References	10
2. Mathematica programs	12

## 1. INTRODUCTION

In this manuscript we derive formula for multifold sums of powers using Newton's formula and central differences.

---

*Date:* January 18, 2026.

*2010 Mathematics Subject Classification.* 05A19, 05A10, 11B73, 11B83.

*Key words and phrases.* Sums of powers, Newton's interpolation formula, Finite differences, Binomial coefficients, Faulhaber's formula, Bernoulli numbers, Bernoulli polynomials, Interpolation, Discrete convolution, Combinatorics, Polynomial identities, Central factorial numbers, Stirling numbers, Eulerian numbers, Worpitzky identity, Pascal's triangle, OEIS.

DOI: <https://doi.org/10.5281/zenodo.18096789>

The idea to derive sums of powers using difference operator and Newton's series is quite generic. Thus, formulas for sums of powers using forward and backward differences can be found in the works [1, 2].

We define the recurrence for multifold sums of powers introduced by Donald Knuth in [3], which we utilize throughout the paper.

**Proposition 1.1** (Multifold sums of powers recurrence). *For non-negative integers  $r, n, m$*

$$\Sigma^0 n^m = n^m$$

$$\Sigma^1 n^m = \Sigma^0 1^m + \Sigma^0 2^m + \cdots + \Sigma^0 n^m$$

$$\Sigma^{r+1} n^m = \Sigma^r 1^m + \Sigma^r 2^m + \cdots + \Sigma^r n^m$$

**Proposition 1.2** (Central factorials). *For integers  $n, k$*

$$n^{[k]} = \begin{cases} 0, & \text{if } k < 0 \\ 1, & \text{if } k = 0 \\ n \left(n + \frac{k}{2} - 1\right) \left(n + \frac{k}{2} - 2\right) \cdots \left(n - \frac{k}{2} + 1\right) = n \prod_{j=1}^{k-1} \left(n + \frac{k}{2} - j\right), & \text{if } k > 0 \end{cases}$$

Consider Newton's interpolation formula [4, 5] in central differences evaluated in zero

**Proposition 1.3** (Newton's formula in central differences in zero).

$$f(x) = \sum_{k=0}^{\infty} \frac{x^{[k]}}{k!} \delta^k f(0)$$

where  $\delta^k f(0) = \sum_{j=0}^k (-1)^j \binom{k}{j} f\left(\frac{k}{2} - j\right)$  are central finite differences in zero, and  $x^{[k]}$  are central factorials, with  $x^{[0]} = 1$  for every  $x$ .

We observe that central factorials are closely related to falling factorials  $(x)_n = x(x-1)(x-2)(x-3)\cdots(x-n+1) = \prod_{k=0}^{n-1} (x-k)$ . Therefore,

**Proposition 1.4** (Central factorials in terms of falling). *For integers  $n, k$*

$$n^{[k]} = \begin{cases} 0, & \text{if } k < 0 \\ 1, & \text{if } k = 0 \\ n \left( n + \frac{k}{2} - 1 \right)_{k-1}, & \text{if } k > 0 \end{cases}$$

where  $\left( n + \frac{k}{2} - 1 \right)_{k-1}$  are falling factorials.

To derive formula for multifold sums of powers, we follow the strategy to express the Newton's formula (1.3) in terms of binomial coefficients, then to reach closed forms of column sum of binomial coefficients by means of hockey stick identity. Therefore,

**Proposition 1.5** (Binomial form of central factorials). *For integers  $n$  and  $k \geq 1$*

$$\frac{n^{[k]}}{k!} = \frac{n}{k} \binom{n + \frac{k}{2} - 1}{k-1}$$

*Proof.* We have

$$\frac{n^{[k]}}{k!} = \frac{n}{k!} \left( n + \frac{k}{2} - 1 \right)_{k-1} = \frac{n}{k(k-1)!} \left( n + \frac{k}{2} - 1 \right)_{k-1} = \frac{n}{k} \binom{n + \frac{k}{2} - 1}{k-1}$$

because of the identity in falling factorial  $\frac{(x)_n}{n!} = \binom{x}{n}$  and (1.4).  $\square$

Which yields Newton's formula for powers, in terms of central differences.

**Proposition 1.6** (Newton's formula for powers in zero). *For positive integers  $n \geq 1$  and  $m \geq 1$*

$$n^m = \sum_{k=1}^m \frac{n}{k} \binom{n + \frac{k}{2} - 1}{k-1} \delta^k 0^m$$

Although based on Newton's interpolation formula (1.3), the proposition (1.6) iterates starting from  $k = 1$  to avoid division by zero in  $\frac{n}{k}$ . This is a valid trick, because the central difference  $\delta^k 0^n$  is zero for all  $n \geq 1$  and  $k = 0$ .

By factoring out and simplifying the term  $n$ , we get

$$n^{m-1} = \sum_{k=1}^m \frac{1}{k} \binom{n + \frac{k}{2} - 1}{k-1} \delta^k 0^m$$

We may observe that the operator of central finite difference  $\delta^k 0^m$  requires the parity of its arguments  $m$  and  $k$  meaning that both  $m$  and  $k$  required to be:  $m \pmod{2} = k \pmod{2}$ , such that finite differences  $\delta^k 0^m$  are non-zero

$$\delta^k 0^m \neq 0, \quad \text{whether} \quad m \pmod{2} = k \pmod{2},$$

$$\delta^k 0^m = 0, \quad \text{whether} \quad m \pmod{2} \neq k \pmod{2}.$$

By setting  $m \rightarrow 2m$  we get

$$n^{2m-1} = \sum_{k=1}^{2m} \frac{1}{k} \binom{n + \frac{k}{2} - 1}{k-1} \delta^k 0^{2m}$$

Thus, the central differences  $\delta^k 0^{2m}$  are zero for all odd  $k$ .

Since that  $k$  runs over all integers in the range  $0 \leq k \leq 2m$ , we can omit odd values of  $k$

$$n^{2m-1} = \sum_{k=1}^m \frac{1}{2k} \binom{n + k - 1}{2k-1} \delta^{2k} 0^{2m}$$

Hence, formula for ordinary sums of odd powers yields

**Proposition 1.7** (Ordinary sums of odd powers in central differences). *For integers  $n \geq 1, m \geq 1$*

$$\Sigma^1 n^{2m-1} = \sum_{k=1}^m \frac{1}{2k} \binom{n+k}{2k} \delta^{2k} 0^{2m}$$

*Proof.* We have  $\Sigma^1 n^{2m-1} = \sum_{k=1}^m \frac{1}{2k} \delta^{2k} 0^{2m} \sum_{j=1}^n \binom{j+k-1}{k-1}$ .

By hockey stick identity  $\sum_{j=1}^n \binom{j+k-1}{k-1} = \binom{n+k}{k}$ , thus the statement follows.  $\square$

Therefore,

**Theorem 1.8** (Multifold sums of odd powers in central differences). *For integers  $n \geq 1$ ,  $m \geq 1$  and  $r \geq 0$*

$$\Sigma^r n^{2m-1} = \sum_{k=1}^m \frac{1}{2k} \binom{n+k-1+r}{2k-1+r} \delta^{2k} 0^{2m}.$$

*Proof.* We have  $\Sigma^1 n^{2m-1} = \sum_{k=1}^m \frac{1}{2k} \delta^{2k} 0^{2m} \sum_{j=1}^n \binom{j+k-1}{2k-1}$ .

By hockey stick identity  $\sum_{j=1}^n \binom{j+k-1}{k-1} = \binom{n+k}{k}$ . By induction the claim follows.  $\square$

It is quite interesting to notice that theorem (1.8) is a central difference form of the formula of sums of odd-powers given by Donald Knuth in *Johann Faulhaber and sums of powers*, see [3].

The reason is straightforward, instead of using Central factorial numbers of the second kind  $T(n, k)$ , the theorem (1.8) utilizes central differences explicitly, because

**Lemma 1.9** (Central factorial numbers of the second kind).

$$k!T(n, k) = \delta^k 0^n$$

Meaning that the Knuth's formula

**Proposition 1.10** (Multifold sums of odd powers in central factorial numbers). *For integers  $n \geq 1$ ,  $m \geq 1$  and  $r \geq 0$*

$$\Sigma^r n^{2m-1} = \sum_{k=1}^m (2k-1)! \binom{n+k-1+r}{2k-1+r} T(2m, 2k).$$

originates from Newton's interpolation formula in central differences (1.3).

The lemma (1.9) is well discussed in [6, 7, 8].

The non-zero central factorial numbers  $T(2m, 2k)$  is the sequence [A008957](#) in the OEIS [9].

For example,

$$\Sigma^1 n^1 = \binom{n+1}{2}$$

$$\Sigma^1 n^3 = 6\binom{n+2}{4} + \binom{n+1}{2}$$

$$\Sigma^1 n^5 = 120\binom{n+3}{6} + 30\binom{n+2}{4} + \binom{n+1}{2}$$

$$\Sigma^1 n^7 = 5040\binom{n+4}{8} + 1680\binom{n+3}{6} + 126\binom{n+2}{4} + \binom{n+1}{2}$$

While multifold sums of odd powers are

$$\Sigma^r n^1 = \binom{n+1+r}{2+r}$$

$$\Sigma^r n^3 = 6\binom{n+2+r}{4+r} + \binom{n+1+r}{2+r}$$

$$\Sigma^r n^5 = 120\binom{n+3+r}{6+r} + 30\binom{n+2+r}{4+r} + \binom{n+1+r}{2+r}$$

$$\Sigma^r n^7 = 5040\binom{n+4+r}{8+r} + 1680\binom{n+3+r}{6+r} + 126\binom{n+2+r}{4+r} + \binom{n+1+r}{2+r}$$

The coefficients 1, 6, 1, 120, 30, 1, ... is the sequence [A303675](#) in the OEIS [9].

This approach can be generalized even further. Consider Newton's interpolation formula around arbitrary integer  $t$

**Proposition 1.11** (Newton's interpolation formula in central differences).

$$f(x+t) = \sum_{k=0}^{\infty} \frac{x^{[k]}}{k!} \delta^k f(t)$$

*Proof.* See [5, p. 462]. □

Thus, for powers we have identity

**Proposition 1.12** (Newton's formula for powers). *For integers  $n, t$  and  $m \geq 0$*

$$n^m = \sum_{k=0}^m \frac{(n-t)^{[k]}}{k!} \delta^k t^m$$

Thus,

**Proposition 1.13** (Powers in central binomial form). *For integers  $n, t$  and  $m \geq 0$*

$$\begin{aligned} n^m &= \frac{(n-t)^{[0]}}{0!} \delta^0 t^m + \sum_{k=1}^m \frac{n-t}{k} \binom{n+t+\frac{k}{2}-1}{k-1} \delta^k t^m \\ &= t^m + \sum_{k=1}^m (n-t) \binom{n-t+\frac{k}{2}-1}{k-1} \frac{\delta^k t^m}{k} \end{aligned}$$

Now we expand the brackets in central binomial form above

$$n^m = t^m + \sum_{k=1}^m \frac{\delta^k t^m}{k} \left[ n \binom{n-t+\frac{k}{2}-1}{k-1} - t \binom{n-t+\frac{k}{2}-1}{k-1} \right]$$

Hence, we get ordinary sum of powers

**Corollary 1.14** (Centered ordinary sums of powers). *For integers  $t, m \geq 0, n \geq 0$*

$$\Sigma^1 n^m = \sum_{j=1}^n t^m + \sum_{k=1}^m \frac{\delta^k t^m}{k} \left[ \sum_{j=1}^n j \binom{j-t+\frac{k}{2}-1}{k-1} - t \sum_{j=1}^n \binom{j-t+\frac{k}{2}-1}{k-1} \right]$$

Now we notice that

**Proposition 1.15** (Binomial re-factorization). *For integers  $n \geq 0, r \geq 0, m \geq 0$*

$$n \binom{n+r}{m} = (m+1) \binom{n+r}{m+1} - (r-m) \binom{n+r}{m}$$

Thus, by setting  $n = j$  and  $r = -t + \frac{k}{2} - 1$  and  $m = k - 1$  yields

**Proposition 1.16** (Central binomial re-factorization). *For integers  $j \geq 0, t \geq 0, k \geq 0$*

$$\begin{aligned} j \binom{j-t+\frac{k}{2}-1}{k-1} &= (k-1+1) \binom{j-t+\frac{k}{2}-1}{k-1+1} - \left[ -t + \frac{k}{2} - 1 - (k-1) \right] \binom{j-t+\frac{k}{2}-1}{k-1} \\ &= k \binom{j-t+\frac{k}{2}-1}{k} - \left[ -t - \frac{k}{2} \right] \binom{j-t+\frac{k}{2}-1}{k-1} \\ &= k \binom{j-t+\frac{k}{2}-1}{k} + \left[ t + \frac{k}{2} \right] \binom{j-t+\frac{k}{2}-1}{k-1} \end{aligned}$$

Thus, formula for sums of powers yields

$$\begin{aligned}
\Sigma^1 n^m &= \sum_{j=1}^n t^m + \sum_{k=1}^m \frac{\delta^k t^m}{k} \left[ \sum_{j=1}^n \left\{ k \binom{j-t+\frac{k}{2}-1}{k} + \left[ t + \frac{k}{2} \right] \binom{j-t+\frac{k}{2}-1}{k-1} \right\} \right. \\
&\quad \left. - t \sum_{j=1}^n \binom{j-t+\frac{k}{2}-1}{k-1} \right] \\
&= \sum_{j=1}^n t^m + \sum_{k=1}^m \frac{\delta^k t^m}{k} \left[ \left\{ k \sum_{j=1}^n \binom{j-t+\frac{k}{2}-1}{k} + \left[ t + \frac{k}{2} \right] \sum_{j=1}^n \binom{j-t+\frac{k}{2}-1}{k-1} \right\} \right. \\
&\quad \left. - t \sum_{j=1}^n \binom{j-t+\frac{k}{2}-1}{k-1} \right] \\
&= \sum_{j=1}^n t^m + \sum_{k=1}^m \frac{\delta^k t^m}{k} \left[ k \sum_{j=1}^n \binom{j-t+\frac{k}{2}-1}{k} + \frac{k}{2} \sum_{j=1}^n \binom{j-t+\frac{k}{2}-1}{k-1} \right]
\end{aligned}$$

Therefore,

**Proposition 1.17** (Centered decomposition of power sums). *For integers  $t, m \geq 0, n \geq 0$*

$$\Sigma^1 n^m = \sum_{j=1}^n t^m + \sum_{k=1}^m \frac{\delta^k t^m}{k} \left[ k \sum_{j=1}^n \binom{j-t+\frac{k}{2}-1}{k} + \frac{k}{2} \sum_{j=1}^n \binom{j-t+\frac{k}{2}-1}{k-1} \right]$$

Let be generalized hockey stick identity

**Proposition 1.18** (Generalized hockey-stick identity). *For integers  $a, b$  and  $j$*

$$\sum_{k=a}^b \binom{k}{j} = \binom{b+1}{j+1} - \binom{a}{j+1}$$

*Proof.* We have  $\sum_{k=a}^b \binom{k}{j} = \binom{a}{j} + \binom{a+1}{j} + \cdots + \binom{b}{j}$ , which means that  $\sum_{k=a}^b \binom{k}{j} = \left( \sum_{k=0}^b \binom{k}{j} \right) - \left( \sum_{k=0}^{a-1} \binom{k}{j} \right)$ . By hockey stick identity  $\sum_{k=0}^n \binom{k}{j} = \binom{n+1}{j+1}$  yields  $\sum_{k=a}^b \binom{k}{j} = \left( \sum_{k=0}^b \binom{k}{j} \right) - \left( \sum_{k=0}^{a-1} \binom{k}{j} \right) = \binom{b+1}{j+1} - \binom{a}{j+1}$ .  $\square$

Therefore, by setting  $a = -t + \frac{k}{2}$  and  $b = n - t - \frac{k}{2} - 1$  yields

**Proposition 1.19** (Centered hockey stick identity). *For integers  $n, j, t, k$*

$$\sum_{j=1}^n \binom{j-t+\frac{k}{2}-1}{k} = \sum_{a=-t+\frac{k}{2}}^{n-t-\frac{k}{2}-1} \binom{a}{k} = \binom{n-t+\frac{k}{2}}{k+1} - \binom{-t+\frac{k}{2}}{k+1}$$



Thus, closed form of centered sums of powers yields

**Theorem 1.20** (Closed form of centered sums of powers). *For integers  $n \geq 0$ ,  $m \geq 0$  and arbitrary integer  $t$*

$$\Sigma^1 n^m = \sum_{j=1}^n t^m + \sum_{k=1}^m \frac{\delta^k t^m}{k} \left[ k \left( \binom{n-t+\frac{k}{2}}{k+1} - \binom{-t+\frac{k}{2}}{k+1} \right) + \frac{k}{2} \left( \binom{n-t+\frac{k}{2}}{k} - \binom{-t+\frac{k}{2}}{k} \right) \right].$$

Let  $a = n - t + \frac{k}{2}$ , then

$$\begin{aligned} & k \left( \binom{n-t+\frac{k}{2}}{k+1} - \binom{-t+\frac{k}{2}}{k+1} \right) + \frac{k}{2} \left( \binom{n-t+\frac{k}{2}}{k} - \binom{-t+\frac{k}{2}}{k} \right) \\ &= k \left( \binom{a}{k+1} - \binom{a-n}{k+1} \right) + \frac{k}{2} \left( \binom{a}{k} - \binom{a-n}{k} \right) \\ &= k \left( \binom{a}{k+1} - \binom{a-n}{k+1} + \frac{1}{2} \binom{a}{k} - \frac{1}{2} \binom{a-n}{k} \right) \\ &= \frac{k}{2} \left( 2 \binom{a}{k+1} - 2 \binom{a-n}{k+1} + \binom{a}{k} - \binom{a-n}{k} \right) \\ &= \frac{k}{2} \left( \binom{a}{k+1} + \binom{a}{k+1} - \binom{a-n}{k+1} - \binom{a-n}{k+1} + \binom{a}{k} - \binom{a-n}{k} \right) \end{aligned}$$

By binomial recurrence  $\binom{a+1}{k+1} = \binom{a}{k} + \binom{a}{k+1}$

$$\begin{aligned} & \frac{k}{2} \left( \binom{a}{k+1} + \binom{a}{k+1} - \binom{a-n}{k+1} - \binom{a-n}{k+1} + \binom{a}{k} - \binom{a-n}{k} \right) \\ &= \frac{k}{2} \left( \left[ \binom{a}{k+1} + \binom{a}{k} \right] + \binom{a}{k+1} - \binom{a-n}{k+1} - \left[ \binom{a-n}{k+1} - \binom{a-n}{k} \right] \right) \\ &= \frac{k}{2} \left( \binom{a+1}{k+1} + \binom{a}{k+1} - \binom{a-n}{k+1} - \binom{a-n+1}{k+1} \right) \\ &= \frac{k}{2} \left( \left[ \binom{a+1}{k+1} + \binom{a}{k+1} \right] - \left[ \binom{a-n}{k+1} + \binom{a-n+1}{k+1} \right] \right) \end{aligned}$$

Therefore,

**Proposition 1.21** (Simplified centered sums of powers). *For integers  $n \geq 0$ ,  $m \geq 0$  and arbitrary integer  $t$*

$$\Sigma^1 n^m = \sum_{j=1}^n t^m + \sum_{k=1}^m \frac{\delta^k t^m}{2} \left[ \left( \binom{n-t+\frac{k}{2}+1}{k+1} + \binom{n-t+\frac{k}{2}}{k+1} \right) - \left( \binom{-t+\frac{k}{2}}{k+1} + \binom{-t+\frac{k}{2}+1}{k+1} \right) \right]$$

Continuing similarly, we can derive formula for multifold sums of powers by using centered hockey stick identity (1.19) repeatedly.

## CONCLUSIONS

In this manuscript, we derived formula for multifold sums of powers using Newton's formula in central differences, combined with hockey-stick identity for binomial coefficients. Additionally, we shown that the famous Knuth's formula for multifold sums of powers [3] originates from Newton's formula in central differences. All results of this manuscript are validated using programs in Wolfram Mathematica, see section (2).

## REFERENCES

- [1] Petro Kolosov. Newton's interpolation formula and sums of powers, January 2026. <https://doi.org/10.5281/zenodo.18040979>.
- [2] Petro Kolosov. Sums of powers via backward finite differences and newton's formula, January 2026. <https://doi.org/10.5281/zenodo.18118011>.
- [3] Knuth, Donald E. Johann Faulhaber and sums of powers. *Mathematics of Computation*, 61(203):277–294, 1993. <https://arxiv.org/abs/math/9207222>.
- [4] Newton, Isaac and Chittenden, N.W. *Newton's Principia: the mathematical principles of natural philosophy*. New-York, D. Adee, 1850. [https://archive.org/details/bub\\_gb\\_KaAIAAAIAAJ/page/466/mode/2up](https://archive.org/details/bub_gb_KaAIAAAIAAJ/page/466/mode/2up).
- [5] Paul Leo Butzer, K. Schmidt, E.L. Stark, and L. Vogt. Central factorial numbers; their main properties and some applications. *Numerical Functional Analysis and Optimization*, 10(5-6):419–488, 1989. <https://doi.org/10.1080/01630568908816313>.
- [6] Steffensen, Johan Frederik. *Interpolation*. Williams & Wilkins, 1927. <https://www.amazon.com/-/de/Interpolation-Second-Dover-Books-Mathematics-ebook/dp/B00GHQVON8>.
- [7] L. Carlitz and John Riordan. The divided central differences of zero. *Canadian Journal of Mathematics*, 15:94–100, 1963. <https://doi.org/10.4153/CJM-1963-010-8>.
- [8] John Riordan. *Combinatorial identities*, volume 217. Wiley New York, 1968. <https://www.amazon.com/-/de/Combinatorial-Identities-Probability-Mathematical-Statistics/dp/0471722758>.
- [9] Sloane, Neil J.A. and others. The on-line encyclopedia of integer sequences. <https://oeis.org/>, 2003.

- [10] Kolosov, Petro. Source code for Central Finite Differences and Newton Formula manuscript. <https://github.com/kolosovpetro/SumsOfPowersViaCentralFiniteDifferencesAndNewtonFormula>, 2025.

## 2. MATHEMATICA PROGRAMS

Use the *Mathematica* package [10] to validate the results

Mathematica Function	Validates / Prints
MultifoldSumOfPowersRecurrence[r, n, m]	Computes $\sum^r n^m$
ValidateCentralFactorialsInTermsOfFalling[10]	Validates Proposition (1.4)
ValidateBinomialFormOfCentralFactorials[10]	Validates Proposition (1.5)
ValidateNewtonsFormulaForPowersInZero[20]	Validates Proposition (1.6)
ValidateOrdinarySumsOfOddPowersInCentralDifferences[20]	Validates Prop. (1.7)
ValidateMultifoldSumsOfOddPowersInCentralDifferences[5]	Validates Thm. (1.8)
ValidateNewtonsFormulaForPowers[10]	Validates Prop. (1.12)
ValidatePowersInCentralBinomialForm[10]	Validates Prop. (1.13)
ValidateCenteredOrdinarySumsOfPowers[10]	Validates Cor. (1.14)
ValidateBinomialRefactorization[5]	Validates Prop. (1.15)
ValidateCentralBinomialRefactorization[5]	Validates Prop. (1.16)
ValidateCenteredDecompositionOfPowerSums[10]	Validates Prop. (1.17)
ValidateCenteredHockeyStickIdentity[10]	Validates Prop. (1.19)
ValidateCenteredHockeyStickIdentity[10]	Validates Prop. (1.19)
ValidateClosedFormOfCenteredSumsOfPowers[10]	Validates Thm. (1.20)
ValidateSimplifiedCenteredSumsOfPowers[10]	Validates Prop. (1.21)

## Metadata

- **Initial release date:** January 3, 2026.
- **Current release date:** January 18, 2026.
- **Version:** Local-0.1.0 .
- **MSC2010:** 05A19, 05A10, 11B73, 11B83 .
- **Keywords:** Sums of powers, Newton's interpolation formula, Finite differences, Binomial coefficients, Faulhaber's formula, Bernoulli numbers, Bernoulli polynomials, Interpolation, Discrete convolution, Combinatorics, Polynomial identities, Central factorial numbers, Stirling numbers, Eulerian numbers, Worpitzky identity, Pascal's triangle, OEIS
- **License:** This work is licensed under a [CC BY 4.0 License](#).
- **DOI:** <https://doi.org/10.5281/zenodo.18096789>
- **Web Version:** [kolosovpetro.github.io/sums-of-powers-central-differences/](https://kolosovpetro.github.io/sums-of-powers-central-differences/)
- **Sources:** [github.com/kolosovpetro/SumsOfPowersViaCentralFiniteDifferencesAndNewtonF](https://github.com/kolosovpetro/SumsOfPowersViaCentralFiniteDifferencesAndNewtonF)
- **ORCID:** [0000-0002-6544-8880](#)
- **Email:** [kolosovp94@gmail.com](mailto:kolosovp94@gmail.com)

DEVOPS ENGINEER

*Email address:* [kolosovp94@gmail.com](mailto:kolosovp94@gmail.com)

*URL:* <https://kolosovpetro.github.io>