## BINOMIAL IDENTITIES

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## 1. BINOMIAL IDENTITIES

Identity for negative r in binomial coefficients

$$\binom{r}{k} = (-1)^k \binom{k-r-1}{k}$$

$$\binom{-r}{k} = (-1)^k \binom{k+r-1}{k}$$

Thus, the generating function follows

$$\frac{1}{(1+z)^r} = \sum_{k} (-1)^k \binom{k+r-1}{k} z^k = 1 - \binom{r}{1} x + \binom{r+1}{2} x^2 - \binom{r+2}{3} x^3 \cdots$$

$$\frac{1}{(1-z)^r} = \sum_{k} \binom{k+r-1}{k} z^k = 1 + \binom{r}{1} x + \binom{r+1}{2} x^2 + \binom{r+2}{3} x^3 \cdots$$