

1. $\text{Smoke} \Rightarrow \text{Smoke}$

$$\equiv \neg \text{Smoke} \vee \text{Smoke} \quad \equiv \text{True}$$

Valid

2. $\text{Smoke} \Rightarrow \text{Fire}$

$$\equiv \neg \text{Smoke} \vee \text{Fire}$$

Neither

3. $(\text{Smoke} \Rightarrow \text{Fire}) \Rightarrow (\neg \text{Smoke} \Rightarrow \neg \text{Fire})$

$$\equiv (\neg \text{Smoke} \vee \text{Fire}) \Rightarrow (\neg \neg \text{Smoke} \vee \neg \text{Fire})$$

$$\equiv (\neg \text{Smoke} \vee \text{Fire}) \Rightarrow (\text{Smoke} \vee \neg \text{Fire})$$

$$\equiv \neg (\neg \text{Smoke} \vee \text{Fire}) \vee (\text{Smoke} \vee \neg \text{Fire})$$

$$\equiv (\text{Smoke} \wedge \neg \text{Fire}) \vee \text{Smoke} \vee \neg \text{Fire}$$

$$\equiv (\text{Smoke} \vee \text{Smoke} \vee \neg \text{Fire}) \wedge (\neg \text{Fire} \vee \text{Smoke} \vee \neg \text{Fire})$$

$$\equiv (\text{Smoke} \vee \neg \text{Fire}) \wedge (\neg \text{Fire} \vee \text{Smoke})$$

$$\equiv \neg \text{Fire} \vee \text{Smoke}$$

Neither

4. $\text{Smoke} \vee \text{Fire} \vee \neg \text{Fire}$

$$\equiv \text{Smoke} \vee \text{True} \quad \equiv \text{True}$$

Valid

$$\begin{aligned}
 5. & \left((Smoke \wedge Heat) \Rightarrow Fire \right) \Leftrightarrow \left((Smoke \Rightarrow Fire) \vee (Heat \Rightarrow Fire) \right) \\
 & \equiv (\neg Smoke \vee \neg Heat \vee Fire) \Leftrightarrow (\neg Smoke \vee Fire \vee \neg Heat \vee Fire) \\
 & \equiv (\neg Smoke \vee \neg Heat \vee Fire) \Leftrightarrow (\neg Smoke \vee \neg Heat \vee Fire)
 \end{aligned}$$

$$(设 A = \neg Smoke \vee \neg Heat \vee Fire)$$

$$\equiv A \Leftrightarrow A \equiv (A \Rightarrow A) \wedge (A \Rightarrow A) \equiv (\neg A \vee A) \wedge (\neg A \vee A)$$

$$\equiv True \wedge True \equiv True$$

Valid

$$6. Big \vee Dump \vee (Big \Rightarrow Dump)$$

$$\equiv Big \vee Dump \vee \neg Big \vee Dump$$

$$\equiv True \vee Dump \equiv True$$

Valid

$$7. (Big \wedge Dump) \vee \neg Dump$$

$$\equiv (Big \vee \neg Dump) \wedge (Dump \vee \neg Dump)$$

$$\equiv (Big \vee \neg Dump) \wedge True$$

$$\equiv (Big \vee \neg Dump)$$

Neither