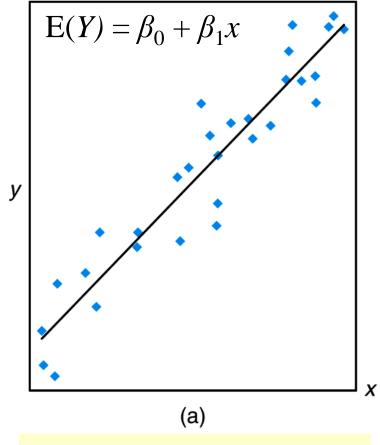
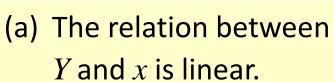
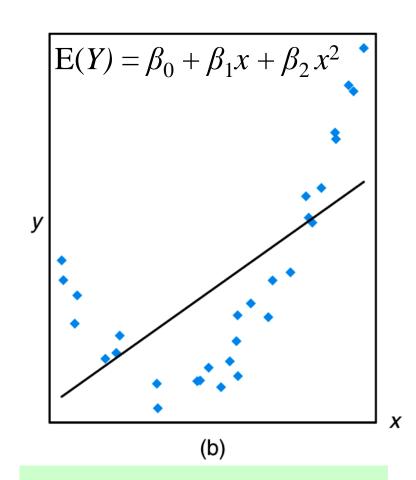
The Problem of Overfitting

Solving the Problem of Overfitting Regularization







(b) There is a second order relation between *Y* and *x*.

Housing prices prediction

$$h_{\theta}(x) = \theta_0 + \theta_1 \times frontage + \theta_2 \times depth$$

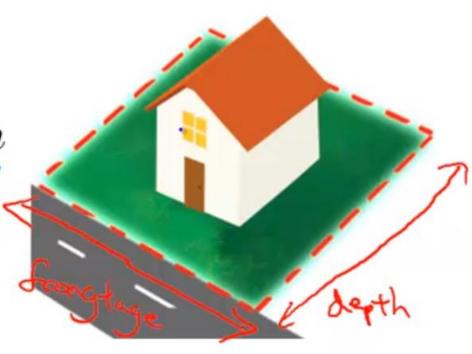


Housing prices prediction

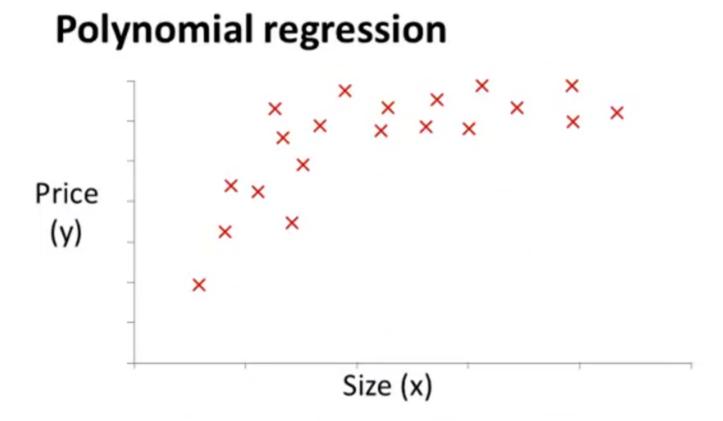
$$h_{\theta}(x) = \theta_0 + \theta_1 \times \underbrace{frontage}_{X} + \theta_2 \times \underbrace{depth}_{X}$$



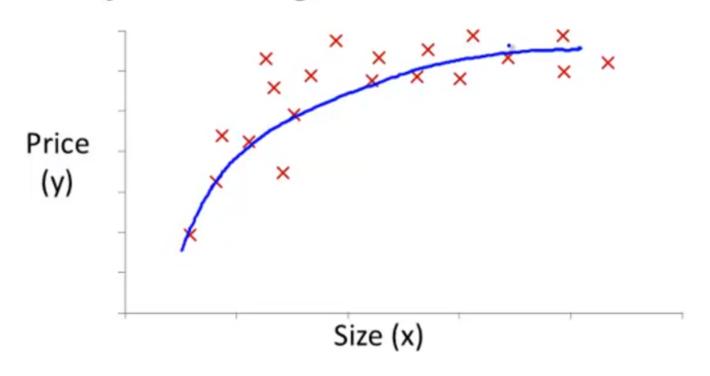
cland are



Polynomial regression

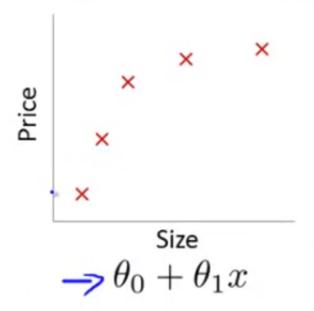


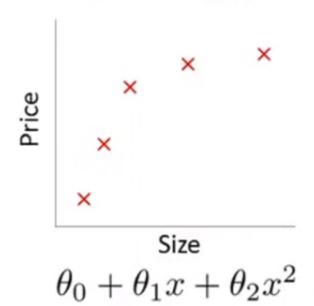
Polynomial regression

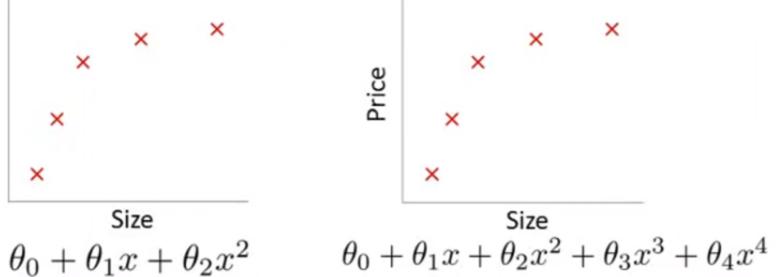


$$\rightarrow \theta_0 + \theta_1 x + \theta_2 x^2$$

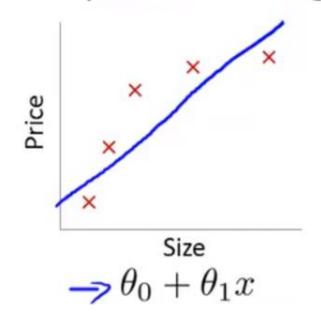
Example: Linear regression (housing prices)

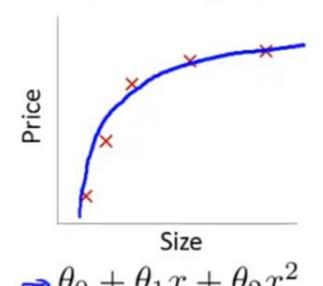


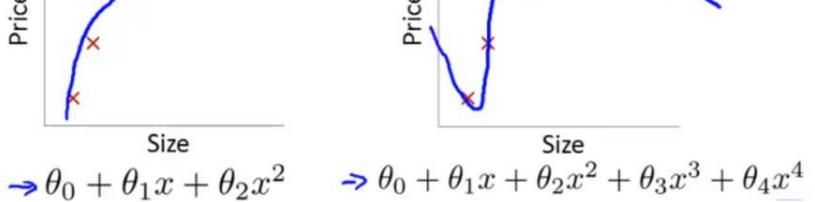




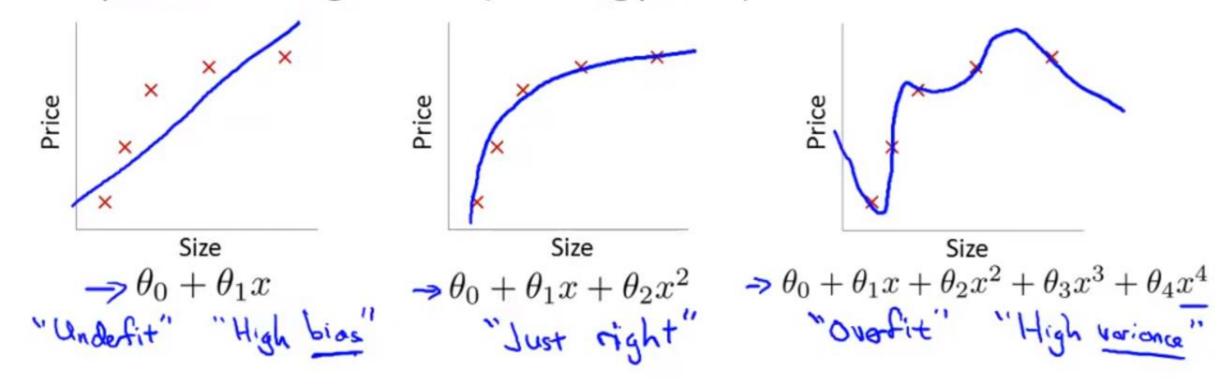
Example: Linear regression (housing prices)





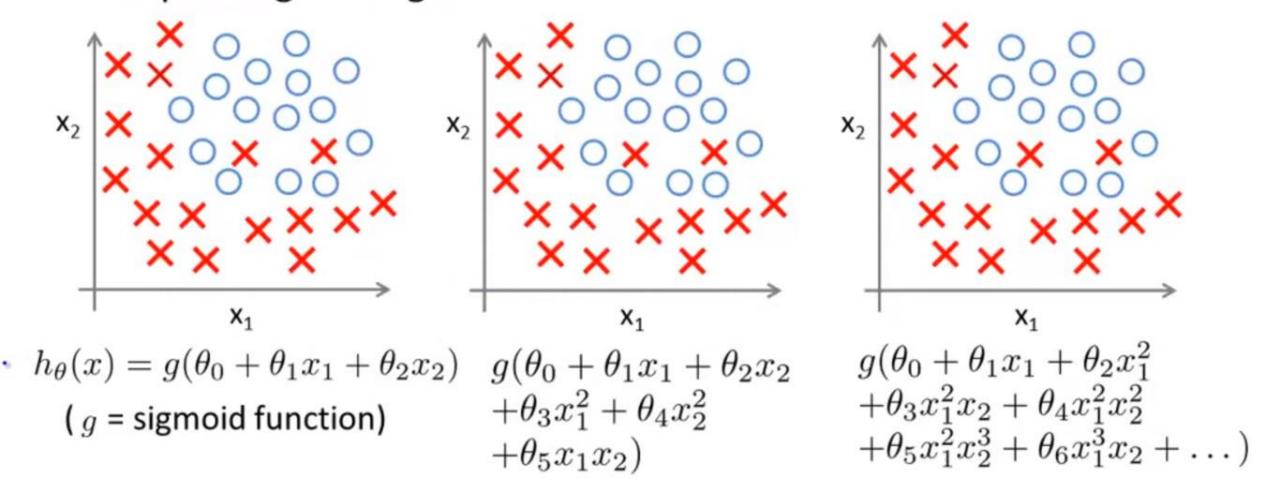


Example: Linear regression (housing prices)

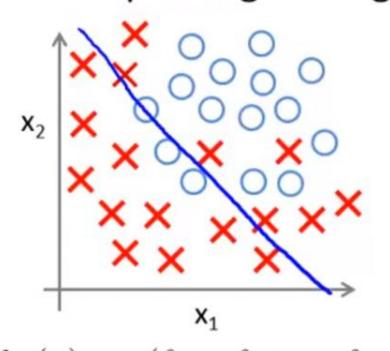


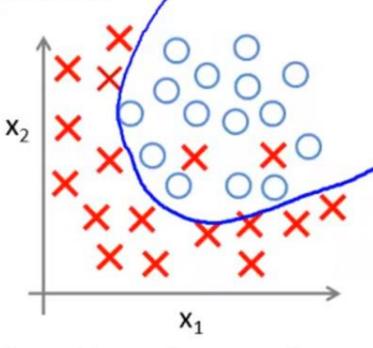
Overfitting: If we have too many features, the learned hypothesis may fit the training set very well $(J(\theta) = \frac{1}{2m} \sum_{i=1}^{m} (h_{\theta}(x^{(i)}) - y^{(i)})^2 \approx 0)$, but fail to generalize to new examples (predict prices on new examples).

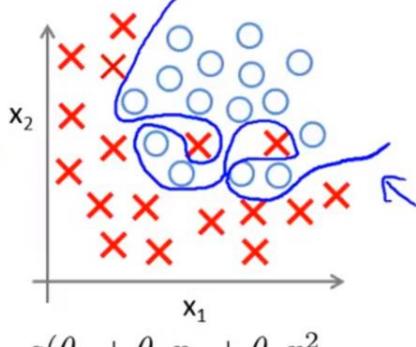
Example: Logistic regression



Example: Logistic regression







$$h_{\theta}(x) = g(\theta_0 + \theta_1 x_1 + \theta_2 x_2)$$
(g = sigmoid function)

$$g(\theta_{0} + \theta_{1}x_{1} + \theta_{2}x_{2} + \theta_{3}x_{1}^{2} + \theta_{4}x_{2}^{2} + \theta_{5}\overline{x_{1}}x_{2})$$

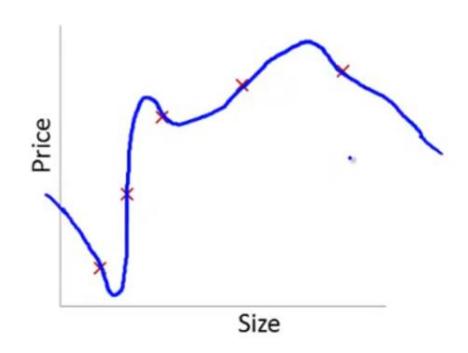
$$g(\theta_{0} + \theta_{1}x_{1} + \theta_{2}x_{1}^{2} + \theta_{3}x_{1}^{2}x_{2} + \theta_{4}x_{1}^{2}x_{2}^{2} + \theta_{5}x_{1}^{2}x_{2}^{3} + \theta_{6}x_{1}^{3}x_{2} + \dots)$$

Exercise

- Consider the medical diagnosis problem of classifying tumors as malignant or benign. If a hypothesis h(x) has overfit the training set, it means that:
 - It makes accurate predictions for examples in the training set and generalizes well to make accurate predictions on new, previously unseen examples.
 - It does not make accurate predictions for examples in the training set, but it does generalize well to make accurate predictions on new, previously unseen examples.
 - It makes accurate predictions for examples in the training set, but it does not generalize well to make accurate predictions on new, previously unseen examples.
 - It does not make accurate predictions for examples in the training set and does not generalize well to make accurate predictions on new, previously unseen examples.

Addressing overfitting:

```
x_1 = \text{ size of house}
x_2 = \text{ no. of bedrooms}
x_3 = \text{ no. of floors}
x_4 = age of house
x_5 = \text{average income in neighborhood}
x_6 = \text{kitchen size}
x_{100}
```



Addressing overfitting:

Options:

- Reduce number of features.
 - Manually select which features to keep.
 - Model selection algorithm (later in course).

Andrew Ng

Addressing overfitting:

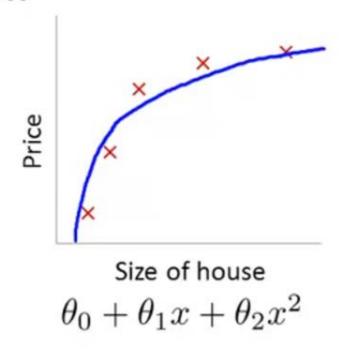
Options:

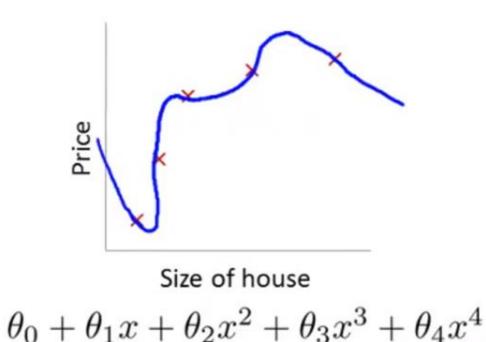
- Reduce number of features.
- Manually select which features to keep.
- Model selection algorithm (later in course).
- Regularization.
 - \rightarrow Keep all the features, but reduce magnitude/values of parameters θ_j .
 - Works well when we have a lot of features, each of which contributes a bit to predicting y.

Cost Function

Solving the Problem of Overfitting Regularization

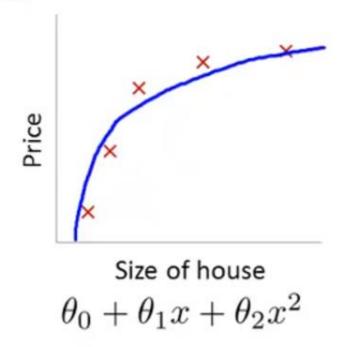
Intuition

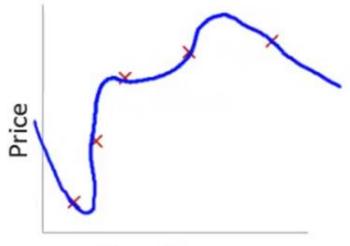




Windows'u Etkinleştir Windows'u etkinleştirmek için Ayarlar'a gidin.

Intuition





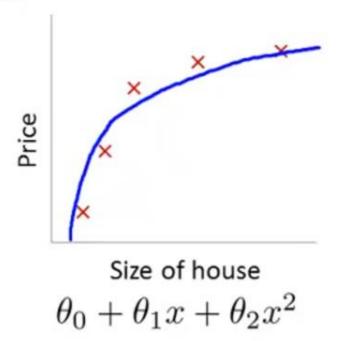
Size of house

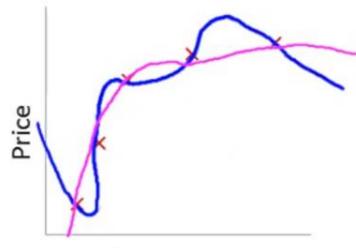
$$\theta_0 + \theta_1 x + \theta_2 x^2 + \theta_3 x^3 + \theta_4 x^4$$

Suppose we penalize and make θ_3 , θ_4 really small.

Windows'u Etkinleştir Windows'u etkinleştirmek için Ayarlar'a gidin.

Intuition

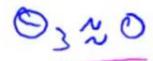




Size of house

$$\theta_0 + \theta_1 x + \theta_2 x^2 + \theta_3 x^3 + \theta_4 x^4$$

Suppose we penalize and make θ_3 , θ_4 really small.





Windows'u Etkinleştir Windows'u etkinleştirmek için Ayarlar'a gidin.

Small values for parameters $\theta_0, \theta_1, \dots, \theta_n \in$

- "Simpler" hypothesis
- Less prone to overfitting <

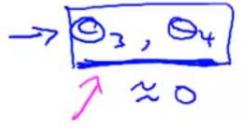
~ O4

Housing:

- Features: $x_1, x_2, \ldots, x_{100}$
- Parameters: $\theta_0, \theta_1, \theta_2, \dots, \theta_{100}$
- Which one to minimize???

Small values for parameters $\theta_0, \theta_1, \dots, \theta_n \leftarrow$

- "Simpler" hypothesis
- Less prone to overfitting <



Housing:

- Features: $x_1, x_2, \ldots, x_{100}$
- Parameters: $\theta_0, \theta_1, \theta_2, \dots, \theta_{100}$

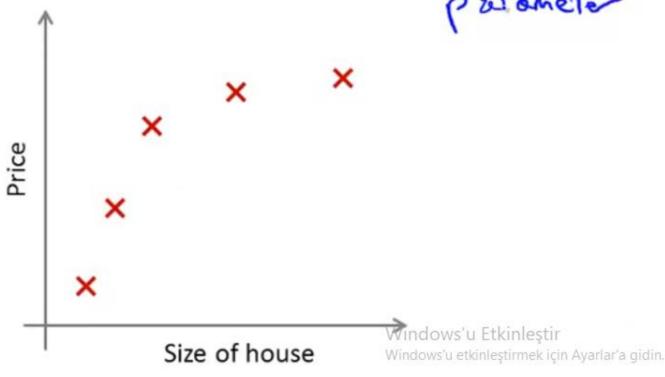
$$J(\theta) = \frac{1}{2m} \left[\sum_{i=1}^{m} (h_{\theta}(x^{(i)}) - y^{(i)})^2 + \lambda_{\text{pirity}} \right]$$



 $\min_{\theta} J(\theta)$

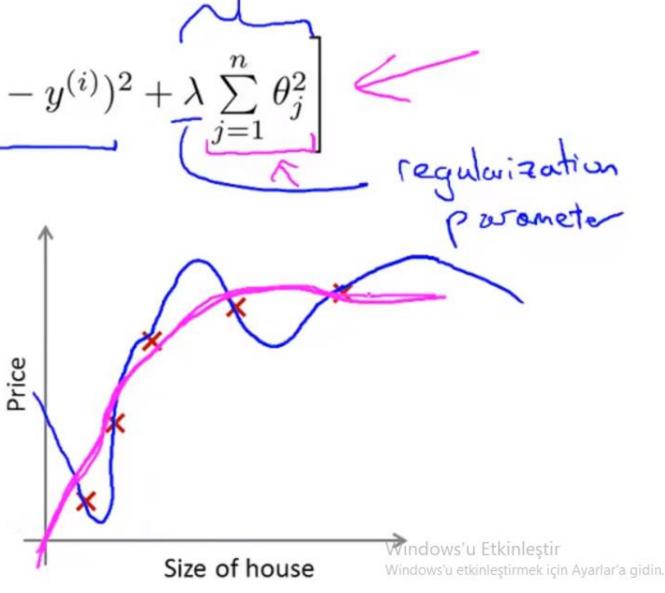
This is also called the Ridge regression.

regularization



$$J(\theta) = \frac{1}{2m} \left[\sum_{i=1}^{m} (h_{\theta}(x^{(i)}) - y^{(i)})^2 + \lambda \sum_{j=1}^{n} \theta_j^2 \right]$$

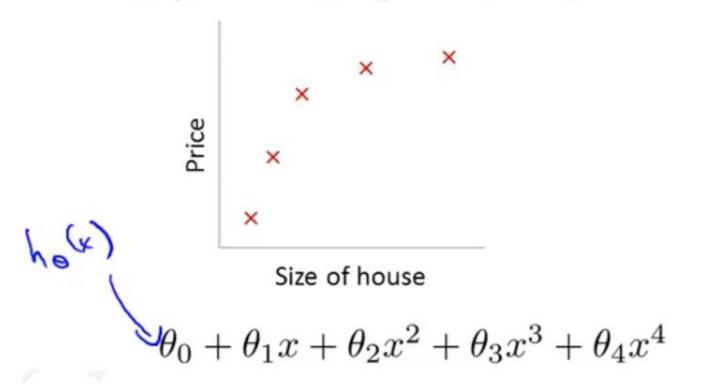
$$\min_{\theta} J(\theta)$$



In regularized linear regression, we choose θ to minimize

$$J(\theta) = \frac{1}{2m} \left[\sum_{i=1}^{m} (h_{\theta}(x^{(i)}) - y^{(i)})^2 + \underline{\lambda} \sum_{j=1}^{n} \theta_j^2 \right]$$

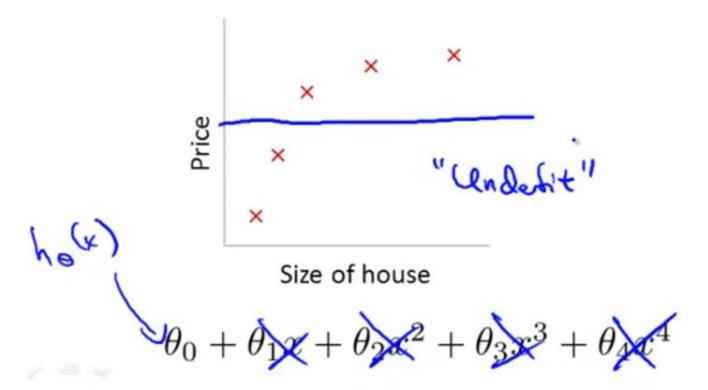
What if λ is set to an extremely large value (perhaps for too large for our problem, say $\lambda = 10^{10}$)?

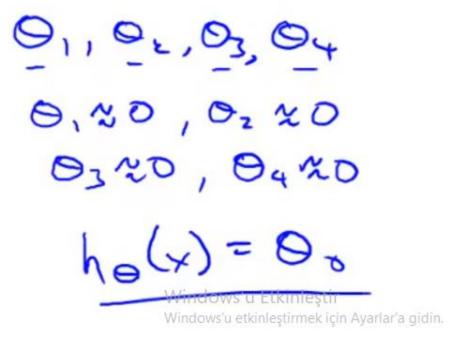


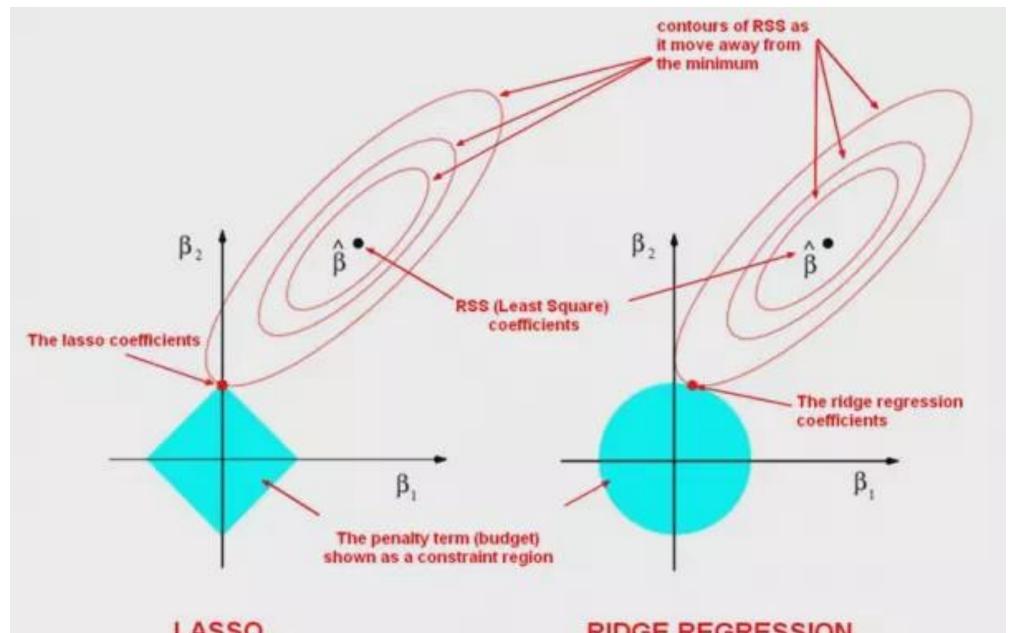
Windows'u Etkinleştir Windows'u etkinleştirmek için Ayarlar'a gidin. In regularized linear regression, we choose θ to minimize

$$J(\theta) = \frac{1}{2m} \left[\sum_{i=1}^{m} (h_{\theta}(x^{(i)}) - y^{(i)})^2 + \underline{\lambda} \sum_{j=1}^{n} \theta_j^2 \right]$$

What if λ is set to an extremely large value (perhaps for too large for our problem, say $\lambda = 10^{10}$)?







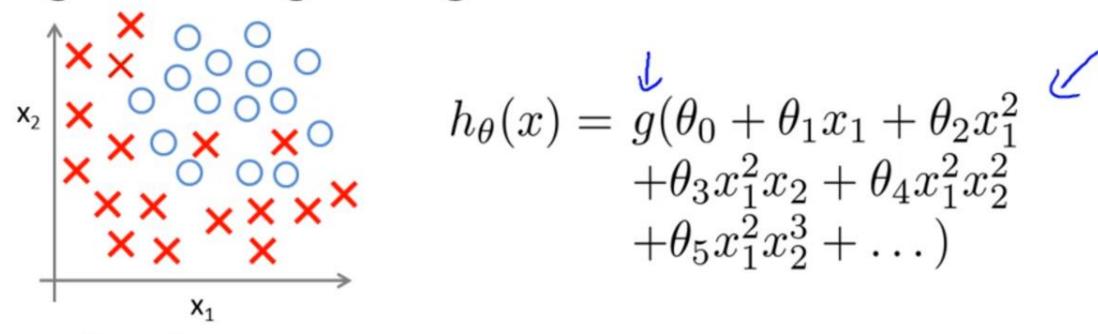
LASSO

RIDGE REGRESSION

Regularized Logistic Regression

Solving the Problem of Overfitting Regularization

Regularized logistic regression.

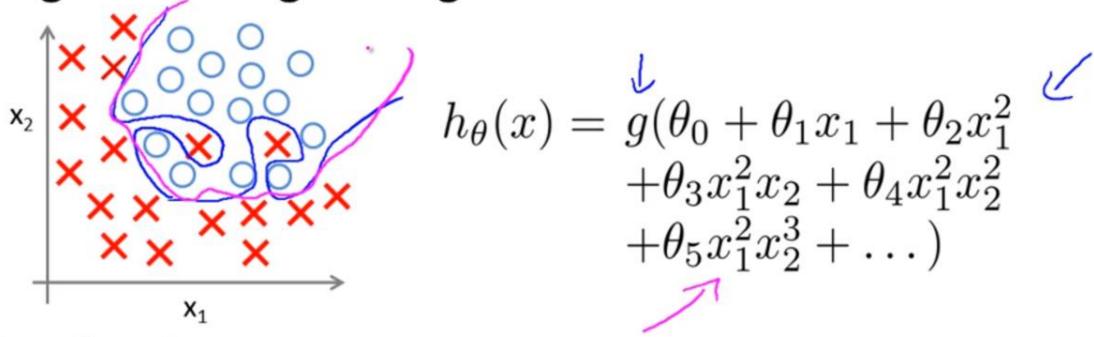


Cost function:

$$J(\theta) = -\left[\frac{1}{m} \sum_{i=1}^{m} y^{(i)} \log h_{\theta}(x^{(i)}) + (1 - y^{(i)}) \log (1 - h_{\theta}(x^{(i)}))\right]$$

Windows'u Etkinleştir Windows'u etkinleştirmek için Ayarlar'a gidin.

Regularized logistic regression.



Cost function:

$$J(\theta) = -\left[\frac{1}{m} \sum_{i=1}^{m} y^{(i)} \log h_{\theta}(x^{(i)}) + (1 - y^{(i)}) \log (1 - h_{\theta}(x^{(i)}))\right]$$

$$+ \frac{\lambda}{2m} \sum_{j=1}^{m} \mathcal{O}_{j}^{2}$$

$$\downarrow \mathcal{O}_{i}, \mathcal{O}_{i} \text{ indows'u Ethics stirm Avariar'a gidin.}$$