

# TASS: A Toolkit for Aircraft Sizing and Synthesis

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## Abstract

A Toolkit for Aircraft Sizing and Synthesis (TASS), capable of performing sizing and synthesis calculations in the context of conceptual design of aircraft is developed in Matlab.<sup>3</sup> TASS implements energy-based constraint and weight-fraction approach for the mission sizing analyses, and provides the user with a design point that is a function of *thrust-weight ratio* and *wing-loading*. The performance of TASS is benchmarked against the known metrics of a transonic jet fighter aircraft F-86L Sabre (Sabrejet).

## 1 Introduction and Motivation

Design of aircraft is subject to tens of thousands of constraints that span across a variety of disciplines such as aerodynamics, structures, controls and performance.<sup>1,2,7,8</sup> Examples of such constraints, to name a few are: achieving a long cruise range, minimizing the take-off distance, fuel-efficient engines, stealth capabilities for reconnaissance, lift-constrained-drag-minimization, stress and strain requirements, and so on. These constraints are indeed the ones that drive the design and play a pivotal role in shaping the end-design. There has been an increased interest in exploring more at initial stages of design to identify conventional as well as non-conventional configurations – a strategy that helps one to get a better insight of potential configurations that can meet the design requirements and eliminate retrospective changes that may be due at later stages of the design process, that are known to be prohibitively expensive.

Similar motivations have led to development of tools that ably perform conceptual analysis in various platforms.<sup>6,9</sup> To this end, this work too aims to develop a toolkit in Matlab<sup>3</sup> known as TASS, that performs an analysis of the early phases of aircraft design *i.e.*, the sizing and synthesis. The scope of current work is limited to the conceptual design phase of aircraft design; more advanced phases in aircraft design (e.g. preliminary, detailed design *etc.*) fall beyond the scope of current work. Nevertheless, modularity is a key consideration in the development of the toolkit, which enables further advancements a function of time.

Energy based constraint analyses encompass an attractive way to start with aircraft design. The main advantage of energy-based approach over conventional approaches is that it employs Lagrangian paradigm of mechanics, as opposed to Newton's world of vector mechanics. The key idea is that aircraft is treated as a system that converts energy from one form to another as the mission progresses. For example, combustion in the engines convert the chemical energy of the fuel into thermal energy, which in-turn accelerates the gases to rotate the turbines to provide mechanical energy to sustain motion. It is easier to think in terms of scalars such as potential energy (depends on position) and kinetic energy (depends on rate of change of position), compared to resolving forces (e.g. lift, thrust) along different directions (e.g. vertical, horizontal) and invoking force and moment balances. Due to such advantages, TASS preferably employs energy based constraint

analyses. The mathematical and physical models used in various stages of the mission are explained as and when they are introduced in later sections and are not explained here for brevity.

This report is organized as follows. Section 4 outlines the mathematical models behind the aircraft sizing and synthesis procedure. Section 3.1 outlines the functionality that is expected from the toolkit. Section ?? contains detailed step-by-step instructions on the working of the tool with the help of an example. Section 6 concludes the report highlighting the key aspects of the tool and lays-out scope for further improvements to the toolkit.

## 2 Getting Started

This section is devoted to provide a high-level overview of the of the software.

### 2.1 Installation

TASS uses native Matlab code for all of its functionality – including initialization, iterative calculations and graphics, therefore a working version of Matlab<sup>3</sup> is sufficient. The software is tested to work on both UNIX and Windows based workstations. The source code can be obtained by using `git clone https://github.com/komahanb/tass.git` from a *terminal* or *shell* program or by downloading `tass-master.zip` file and extracting it in a working folder of convenience.

### 2.2 Input Layout

A Graphical User Interface (GUI) is designed to collect all the mission-specific inputs that the user supplies to the software. From an user-standpoint these input parameters are decided based on the complete break-down of mission requirements (e.g. humanitarian, rescue, military missions). Table ?? presents the typical inputs that the user is expected to provide to the software.

### 2.3 Output Layout

Output layout contains a collection of information interms of values and plots that the user can get from the software. TASS provides a constraint analysis plot and enables the user to directly identify a design point in terms of thrust to weight ratio and wing loading. It also provides a mission analysis for the sizing of the system indicating the converged estimated weight and weight contributions from the different weight groups. The following is a comprehensive list of values, tables and plots that TASS is able to present to the user.

## 3 Benchmarking TASS

A brief introduction of the concept under study and a summary of the mission and requirements are outlined next.<sup>5</sup> The design produced by TASS will be compared to the design of the actual aircraft.

### **3.1 Aircraft Requirements**

The conceptual design process begins with a defined set of requirements. These requirements lay-out specific constraints and design goals that the end-system must be capable of achieving. These goals and constraints are often presented the form of Request for Proposal (RFP).

#### **3.1.1 Functional Requirements**

The functional requirement of the aircraft is to carryout a military mission, which is:

- to carry a crew member weighing 210 *lbs*
- to carry a payload of 432 *lb*

#### **3.1.2 Mission Profile**

Table 1 breaks-down the performance requirements of the aircraft to be designed using the TASS.

### **3.2 Performance Requirements**

The elemets in mission profile are decomposed into performance requirements that are tabulated in Table ??.

Table 1: Requirements of the fighter aircraft and for different stages in the mission profile

Segment	Phase	Performance Requirements
0-1	Takeoff	Distance 4400 <i>ft</i> Clear obstacle at 50 <i>ft</i> Maximum power with afterburners Air speed 1200 <i>ft/s</i> Sea level runway at 90 <i>F</i> Maximum rate of climb 90 <i>ft/s</i>
1-2	Climb	Altitude 35400 ft Full military power without afterburners Maximum rate of climb 90 <i>ft/s</i>
2-3	Cruise climb	Altitude 38700 ft Distance 550 nautical miles Cruise speed 458 knots Normal power
3-4	Loiter	Altitude 38700 ft 10 minutes loiter normal power
4-5	Climb	Altitude 47550 ft
5-6	Combat	Maximum power with afterburners Duration 5 minutes Speed 536 knots
6-7	Cruise	Altitude 37000 ft Distance 550 nautical miles Normal power
7-8	Loiter	10 minutes Altitude 35000 ft Maximum endurance conditions
8-9	Landing	Distance 5000 ft Without highlift devices 10% fuel reserve

Table 2: Performance requirements of the desired aircraft

Item	Performance Requirements
Takeoff distance	4400 <i>ft</i>
Landing distance	5000 <i>ft</i>
Maximum air speed	1200 <i>ft/s</i>
Maximum rate of climb	90 <i>ft/s</i>
Altitude	47550 ft
Turn	5g sustained turn <sup>1</sup>

## 4 Architecture of the Toolkit

This section provides an outline of the theory, physical and mathematical models used in TASS. A rather comprehensive discussion on these topics can be found in the literature.<sup>1,2,4,7,8</sup> Figure 4.1 provides a generic overview of the elements involved in the sizing and synthesis process. As it can be seen, *constraint analyses* and *weight estimations* are pivotal in producing the design. All the discussions in this section are organized in terms of the benchmarking test case Sabrejet F-86 L described in Section 3.1.

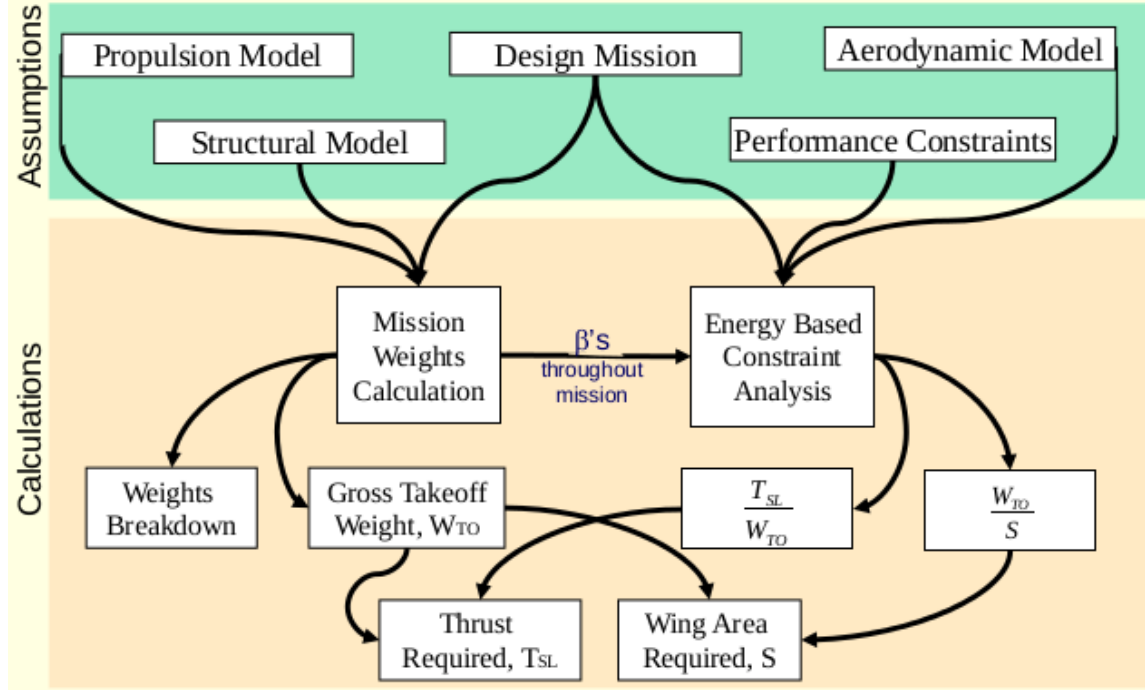


Figure 4.1: A top level overview of sizing and synthesis process implemented in TASS.<sup>5</sup>

### 4.1 Standard Atmosphere Model

TASS has offers the flexibility to choose between two popular standard atmosphere models to the users:

- (a) U.S. Standard Atmosphere model<sup>10</sup>
- (b) Committee on Extension to the Standard Atmosphere (COESA) model<sup>10</sup>

These models are used to obtain the temperature, speed of sound (Mach number), pressure and density as a function of height in the calculations. The default model used in the tool is the U.S. Standard Atmosphere model.

### 4.2 Mattingly Energy Equation

The performance constraints and requirements are set as functions of *thrust loading* (thrust-to-weight ratio) and *wing loading*, the two sizing parameters that contain key information about the

top level characteristics of the system.<sup>4</sup> The Mattingly Master Energy equation is:

$$\frac{T_{SL}}{W_{TO}} = \frac{\beta}{\alpha} \left\{ \frac{qS}{\beta W_{TO}} \left[ K_1 \left( \frac{n\beta W_{TO}}{qS} \right)^2 + K_2 \left( \frac{n\beta W_{TO}}{qS} \right) + C_{D_0} + \frac{R}{qS} \right] + \frac{1}{V} \frac{d}{dt} \left( h + \frac{V^2}{2g_0} \right) \right\} \quad (4.1)$$

Table 3 contains a short definition of the parameters in Eq. 4.1.

Table 3: Parameters in Mattingly Energy Equation

Parameter	Description	English Unit	SI Unit
$T_{SL}$	sea-level thrust	lb	N
$W_{TO}$	take-off gross weight	lb	N
$q$	dynamic pressure	$lb/ft^2$	$N/m^2$
$S$	wing planform area	$ft^2$	$m^2$
$C_{D_0}$	drag at zero lift	no unit	no unit
$K_1$			
$K_2$			
$q$	load factor	no unit	no unit
$R$			
$V$	velocity(speed)	$ft/s$	$m/s$
$h$	altitude from sea level	$ft$	$m$
$g_0$	gravity at sea level	$ft/s^2$	$m/s^2$
$\alpha$			
$\beta$	instantaneous weight fraction		

### 4.3 Constraint Analysis

By manipulating Eq. 4.1 various constraints pertaining to the mission can be derived. Detailed derivation and treatment of such constraints can be found in Mattingly *et al.*<sup>4</sup>

#### 4.3.1 Constant Altitude/Speed Cruise

#### 4.3.2 Constant Speed Climb

#### 4.3.3 Constant Altitude/Speed Turn

#### 4.3.4 Horizontal Acceleration

#### 4.3.5 Takeoff Ground Roll (lots of Thrust)

#### 4.3.6 Takeoff Ground Roll (not so much Thrust)

#### 4.3.7 Braking Roll

#### 4.3.8 Service Ceiling

### 4.4 Weight Estimation

The takeoff gross weight  $W_{TO}$  can be estimated using

$$W_{TO} = W_C + W_P + W_E + W_F \quad (4.2)$$

where  $W_C$  is the crew weight,  $W_P$  is the payload weight,  $W_E$  is the empty weight and  $W_F$  is the fuel weight. The design is to be done to carry a crew member who weighs 210 *lbs* and a payload of 432 *lbs*. It is rather difficult to estimate the empty and fuel weight compared to the other counterparts.

## 5 Conceptual Design of the Benchmark Fighter

The comparison of the design obtained using the tool with known configuration of the aircraft follows next. Table ?? presents the performance parameters that are calculated using the tool with that of the existing data. A good agreement between values demonstrate the accuracy of the tool.

### 5.1 Perturbations of Constraints

A good end-result of the conceptual design phase is to identify answers to the following questions?

1. Will it work?
2. What does it look like?
3. What requirements drive the design?
4. What tradeoffs should be considered?
5. What should it weigh and cost?

## 6 Summary

This work presented a generic toolkit that performs sizing and synthesis of the aircraft configurations at the conceptual design level. The toolkit is provided with a graphical user-interface that helps non-expert users to simulate different requirements at the same time. It is validated against a known configuration of F-86 Sabrejet.

## References

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## **A RFP for Benchmarking Test Case**

## **B Flexibility of the Tool**

### **B.1 Versatility of the Tool**

1. The Graphical User Interface (GUI) takes the set of inputs and perform the analyses. As long as the inputs specified are within the validity of the underlying mathematical models, the tool will work for any set of requirements as explained in Section ??.
2. TASS can operate with both English and SI units
3. TASS employs interpolations and extrapolations whenever it encounters data that are be rather difficult to supply or unavailable (e.g.)

### **B.2 Challenges and Cons**

1. Since it is extremely laborious to implement sanity checks on the user-supplied values, it is recommended that the users proactively consider the physical meaning of the values supplied (e.g. range, rate of climb)