

Free-energy bound on surprise

$$F = -\langle \ln p(\tilde{s}, \vartheta | m) \rangle_q + \langle \ln q(\vartheta | \mu) \rangle_q$$

Action minimizes prediction errors

$$F = D(q(\vartheta | \mu) \parallel p(\vartheta)) - \langle \ln p(\tilde{s}(a) | \vartheta, m) \rangle_q$$

$$a = \arg \max \text{Accuracy}$$

Perception optimizes predictions

$$F = D(q(\vartheta | \mu) \parallel p(\vartheta | \tilde{s})) - \ln p(\tilde{s} | m)$$

$$\mu = \arg \max \text{Divergence}$$