

$$\begin{aligned}
\mathbf{w}_2^{(2)} &= \mathbf{w}_1^{(2)} - \eta \vec{x}_n^{(1)} (\vec{\delta}^{(2)})^T = \mathbf{w}_1^{(2)} - \eta \begin{pmatrix} 1 \\ x_1^{(1)} \\ x_2^{(1)} \end{pmatrix} (\delta_1^{(2)}, \delta_2^{(2)}, \delta_3^{(2)}) \\
&= \begin{pmatrix} w_{01}^{(2)} & w_{02}^{(2)} & w_{03}^{(2)} \\ w_{11}^{(2)} & w_{12}^{(2)} & w_{13}^{(2)} \\ w_{21}^{(2)} & w_{22}^{(2)} & w_{23}^{(2)} \end{pmatrix} - \eta \begin{pmatrix} \delta_1^{(2)} & \delta_2^{(2)} & \delta_3^{(2)} \\ x_1^{(1)} \delta_1^{(2)} & x_1^{(1)} \delta_2^{(2)} & x_1^{(1)} \delta_3^{(2)} \\ x_2^{(1)} \delta_1^{(2)} & x_2^{(1)} \delta_2^{(2)} & x_2^{(1)} \delta_3^{(2)} \end{pmatrix} \\
&= \begin{pmatrix} 0.58 & 0.58 & 0.58 \\ -0.26 & -0.26 & -0.26 \\ -0.26 & -0.26 & -0.26 \end{pmatrix} \\
&\quad - 0.01 \begin{pmatrix} 11.56 & 11.56 & 11.56 \\ 0.26 * 11.56 & 0.26 * 11.56 & 0.26 * 11.56 \\ 0.26 * 11.56 & 0.26 * 11.56 & 0.26 * 11.56 \end{pmatrix} \\
&= \begin{pmatrix} 0.46 & 0.46 & 0.46 \\ -0.29 & -0.29 & -0.29 \\ -0.29 & -0.29 & -0.29 \end{pmatrix}
\end{aligned}$$

$$\begin{aligned}
\mathbf{w}_2^{(3)} &= \mathbf{w}_1^{(3)} - \eta \vec{x}_n^{(2)} (\vec{\delta}^{(3)})^T = \mathbf{w}_1^{(3)} - \eta \begin{pmatrix} 1 \\ x_1^{(2)} \\ x_2^{(2)} \\ x_3^{(2)} \end{pmatrix} \delta_1^{(3)} \\
&= \begin{pmatrix} 0.58 \\ -1.94 \\ -1.94 \\ -1.94 \end{pmatrix} - 0.01 \begin{pmatrix} -5.96 \\ 0.44 * (-5.96) \\ 0.44 * (-5.96) \\ 0.44 * (-5.96) \end{pmatrix} = \begin{pmatrix} 0.64 \\ -1.91 \\ -1.91 \\ -1.91 \end{pmatrix}
\end{aligned}$$

t=3, 对于第三个样本 $\vec{x}_3 = (-1, 1)^T$, 则第一层神经元的输入为:

$$\begin{pmatrix} s_1^{(1)} \\ s_2^{(1)} \end{pmatrix} = (\mathbf{w}^{(1)})^T \vec{x}_n^{(0)} = \begin{pmatrix} -0.17 & -0.35 & -0.35 \\ -0.17 & -0.35 & -0.35 \end{pmatrix} \begin{pmatrix} 1 \\ -1 \\ 1 \end{pmatrix} = \begin{pmatrix} -0.17 \\ -0.17 \end{pmatrix}$$

$$\text{则: } \begin{pmatrix} x_1^{(1)} \\ x_2^{(1)} \end{pmatrix} = \begin{pmatrix} \max(0, s_1^{(1)}) \\ \max(0, s_2^{(1)}) \end{pmatrix} = \begin{pmatrix} 0 \\ 0 \end{pmatrix}$$

第二层神经元的输入为:

$$\begin{pmatrix} s_1^{(2)} \\ s_2^{(2)} \\ s_3^{(2)} \end{pmatrix} = (\mathbf{w}^{(2)})^T \begin{pmatrix} 1 \\ x_1^{(1)} \\ x_2^{(1)} \end{pmatrix} = \begin{pmatrix} 0.46 & -0.29 & -0.29 \\ 0.46 & -0.29 & -0.29 \\ 0.46 & -0.29 & -0.29 \end{pmatrix} \begin{pmatrix} 1 \\ 0 \\ 0 \end{pmatrix} = \begin{pmatrix} 0.46 \\ 0.46 \\ 0.46 \end{pmatrix}$$

$$\text{则: } \begin{pmatrix} x_1^{(2)} \\ x_2^{(2)} \\ x_3^{(2)} \end{pmatrix} = \begin{pmatrix} 0.46 \\ 0.46 \\ 0.46 \end{pmatrix}$$