

$$\begin{aligned}\vec{\delta}^{(1)} = \begin{pmatrix} \delta_1^{(1)} \\ \delta_2^{(1)} \end{pmatrix} &= \begin{pmatrix} \llbracket s_1^{(1)} \geq 0 \rrbracket & 0 \\ 0 & \llbracket s_2^{(1)} \geq 0 \rrbracket \end{pmatrix} \begin{pmatrix} w_{11}^{(2)} & w_{12}^{(2)} & w_{13}^{(2)} \\ w_{21}^{(2)} & w_{22}^{(2)} & w_{23}^{(2)} \end{pmatrix} \begin{pmatrix} \delta_1^{(2)} \\ \delta_2^{(2)} \\ \delta_3^{(2)} \end{pmatrix} \\ &= \begin{pmatrix} 0 & 0 \\ 0 & 0 \end{pmatrix} \begin{pmatrix} -0.29 & -0.29 & -0.29 \\ -0.29 & -0.29 & -0.29 \end{pmatrix} \begin{pmatrix} 2.77 \\ 2.77 \\ 2.77 \end{pmatrix} = \begin{pmatrix} 0 \\ 0 \end{pmatrix}\end{aligned}$$

令 $\eta = 0.01$ ，利用梯度下降法进行权系数更新：

$$\begin{aligned}\mathbf{w}_4^{(1)} &= \mathbf{w}_3^{(1)} - \eta \vec{x}_n^{(0)} (\vec{\delta}^{(1)})^T = \mathbf{w}_3^{(1)} - \eta \begin{pmatrix} 1 \\ x_{n1}^{(0)} \\ x_{n2}^{(0)} \end{pmatrix} (\delta_1^{(1)}, \delta_2^{(1)}) \\ &= \begin{pmatrix} w_{01}^{(1)} & w_{02}^{(1)} \\ w_{11}^{(1)} & w_{12}^{(1)} \\ w_{21}^{(1)} & w_{22}^{(1)} \end{pmatrix} - \eta \begin{pmatrix} \delta_1^{(1)} & \delta_2^{(1)} \\ x_{n1}^{(0)} \delta_1^{(1)} & x_{n1}^{(0)} \delta_2^{(1)} \\ x_{n2}^{(0)} \delta_1^{(1)} & x_{n2}^{(0)} \delta_2^{(1)} \end{pmatrix} \\ &= \begin{pmatrix} -0.17 & -0.17 \\ -0.35 & -0.35 \\ -0.35 & -0.35 \end{pmatrix} - 0.01 \begin{pmatrix} 0 & 0 \\ (+1) * 0 & (+1) * 0 \\ (-1) * 0 & (-1) * 0 \end{pmatrix} \\ &= \begin{pmatrix} -0.17 & -0.17 \\ -0.35 & -0.35 \\ -0.35 & -0.35 \end{pmatrix} \\ \mathbf{w}_4^{(2)} &= \mathbf{w}_3^{(2)} - \eta \vec{x}_n^{(1)} (\vec{\delta}^{(2)})^T = \mathbf{w}_3^{(2)} - \eta \begin{pmatrix} 1 \\ x_1^{(1)} \\ x_2^{(1)} \end{pmatrix} (\delta_1^{(2)}, \delta_2^{(2)}, \delta_3^{(2)}) \\ &= \begin{pmatrix} w_{01}^{(2)} & w_{02}^{(2)} & w_{03}^{(2)} \\ w_{11}^{(2)} & w_{12}^{(2)} & w_{13}^{(2)} \\ w_{21}^{(2)} & w_{22}^{(2)} & w_{23}^{(2)} \end{pmatrix} - \eta \begin{pmatrix} \delta_1^{(2)} & \delta_2^{(2)} & \delta_3^{(2)} \\ x_1^{(1)} \delta_1^{(2)} & x_1^{(1)} \delta_2^{(2)} & x_1^{(1)} \delta_3^{(2)} \\ x_2^{(1)} \delta_1^{(2)} & x_2^{(1)} \delta_2^{(2)} & x_2^{(1)} \delta_3^{(2)} \end{pmatrix} \\ &= \begin{pmatrix} 0.42 & 0.42 & 0.42 \\ -0.29 & -0.29 & -0.29 \\ -0.29 & -0.29 & -0.29 \end{pmatrix} - 0.01 \begin{pmatrix} 2.77 & 2.77 & 2.77 \\ 0 * 2.77 & 0 * 2.77 & 0 * 2.77 \\ 0 * 2.77 & 0 * 2.77 & 0 * 2.77 \end{pmatrix} \\ &= \begin{pmatrix} 0.39 & 0.39 & 0.39 \\ -0.29 & -0.29 & -0.29 \\ -0.29 & -0.29 & -0.29 \end{pmatrix}\end{aligned}$$