

$$\text{sign}(\bar{\mathbf{w}}^{(12)T} \vec{x}_1) = 1 = y_1, \quad \therefore \bar{\mathbf{w}}^{(13)} = \bar{\mathbf{w}}^{(12)} = (-2, 2, 2)^T$$

$$\text{sign}(\bar{\mathbf{w}}^{(13)T} \vec{x}_2) = 1 = y_2, \quad \therefore \bar{\mathbf{w}}^{(14)} = \bar{\mathbf{w}}^{(13)} = (-2, 2, 2)^T$$

$$\text{sign}(\bar{\mathbf{w}}^{(14)T} \vec{x}_3) = 1 \neq y_3, \quad \therefore \bar{\mathbf{w}}^{(15)} = \bar{\mathbf{w}}^{(14)} + y_3 \vec{x}_3 = (-3, 1, 1)^T$$

$$\text{sign}(\bar{\mathbf{w}}^{(15)T} \vec{x}_1) = 1 = y_1, \quad \therefore \bar{\mathbf{w}}^{(16)} = \bar{\mathbf{w}}^{(15)} = (-3, 1, 1)^T$$

$$\text{sign}(\bar{\mathbf{w}}^{(16)T} \vec{x}_2) = 1 = y_2, \quad \therefore \bar{\mathbf{w}}^{(17)} = \bar{\mathbf{w}}^{(16)} = (-3, 1, 1)^T$$

$$\text{sign}(\bar{\mathbf{w}}^{(17)T} \vec{x}_3) = -1 = y_3, \quad \therefore \bar{\mathbf{w}}^{(18)} = \bar{\mathbf{w}}^{(17)} = (-3, 1, 1)^T$$

$$\therefore \bar{\mathbf{w}} = (-3, 1, 1)^T, \text{ 分类面为: } x_1 + x_2 - 3 = 0$$

对测试样本进行增广, $\vec{x} = (1, 0, 1)^T$,

$$\text{sign}(\bar{\mathbf{w}}^T \vec{x}) = \text{sign}((-3, 1, 1)(1, 0, 1)^T) = -1, \quad \therefore \vec{x} \in -1 \text{ 类}$$

2, 对于感知器算法 (PLA), 假设第 t 次迭代时, 选择的是第 n 个样

本: $\text{sign}(\mathbf{w}_t^T \mathbf{x}_n) \neq y_n$, $\mathbf{w}_{t+1} \leftarrow \mathbf{w}_t + y_n \mathbf{x}_n$, 下述那个式子正确?

(a) $\mathbf{w}_{t+1}^T \mathbf{x}_n = y_n$

(b) $\text{sign}(\mathbf{w}_{t+1}^T \mathbf{x}_n) = y_n$

(c) $y_n \mathbf{w}_{t+1}^T \mathbf{x}_n \geq y_n \mathbf{w}_t^T \mathbf{x}_n$

(d) $y_n \mathbf{w}_{t+1}^T \mathbf{x}_n < y_n \mathbf{w}_t^T \mathbf{x}_n$

3, 证明: 针对线性可分训练样本集, PLA 算法中, 当 $\mathbf{w}_0 = \mathbf{0}$, 在对分

错样本进行了 T 次纠正后, 下式成立: $\frac{\mathbf{w}_f^T}{\|\mathbf{w}_f\|} \frac{\mathbf{w}_T}{\|\mathbf{w}_T\|} \geq \sqrt{T} \cdot \text{constant}$

证明: 由于