继续运用反向传播法,于是: $\delta_j^{(1)} = \sum_k (\delta_k^{(2)})(w_{jk}^{(2)})(x_j^{(1)})'$,所以:

$$\delta_j^{(1)} = \sum_{k} (\delta_k^{(2)})(w_{jk}^{(2)}) \left[s_j^{(1)} \ge 0 \right] = (\delta_1^{(2)} w_{j1}^{(2)} + \delta_2^{(2)} w_{j2}^{(2)} + \delta_3^{(2)} w_{j3}^{(2)}) \left[s_j^{(1)} \ge 0 \right]$$

由此可以得到:

$$\vec{\delta}^{(1)} = \begin{pmatrix} \delta_1^{(1)} \\ \delta_2^{(1)} \end{pmatrix} = \begin{pmatrix} \begin{bmatrix} s_1^{(1)} \ge 0 \end{bmatrix} & 0 \\ 0 & \begin{bmatrix} s_2^{(1)} \ge 0 \end{bmatrix} \end{pmatrix} \begin{pmatrix} w_{11}^{(2)} & w_{12}^{(2)} & w_{13}^{(2)} \\ w_{21}^{(2)} & w_{22}^{(2)} & w_{23}^{(2)} \end{pmatrix} \begin{pmatrix} \delta_1^{(2)} \\ \delta_2^{(2)} \\ \delta_3^{(2)} \end{pmatrix}$$
$$= \begin{pmatrix} 1 & 0 \\ 0 & 1 \end{pmatrix} \begin{pmatrix} 1 & 1 & 1 \\ 1 & 1 & 1 \end{pmatrix} \begin{pmatrix} 42 \\ 42 \\ 42 \end{pmatrix} = \begin{pmatrix} 126 \\ 126 \end{pmatrix}$$

$$\begin{split} \mathbf{w}_{1}^{(1)} &= \mathbf{w}_{0}^{(1)} - \eta \vec{x}_{n}^{(0)} (\overrightarrow{\delta}^{(1)})^{T} = \mathbf{w}_{t}^{(1)} - \eta \begin{pmatrix} 1 \\ x_{n1}^{(0)} \\ x_{n2}^{(0)} \end{pmatrix} \left(\delta_{1}^{(1)}, \delta_{2}^{(1)} \right) \\ &= \begin{pmatrix} w_{01}^{(1)} & w_{02}^{(1)} \\ w_{11}^{(1)} & w_{12}^{(1)} \\ w_{21}^{(1)} & w_{22}^{(1)} \end{pmatrix} - \eta \begin{pmatrix} \delta_{1}^{(1)} & \delta_{2}^{(1)} \\ x_{n1}^{(0)} \delta_{1}^{(1)} & x_{n1}^{(0)} \delta_{2}^{(1)} \\ x_{n2}^{(0)} \delta_{1}^{(1)} & x_{n2}^{(0)} \delta_{2}^{(1)} \end{pmatrix} \\ &= \begin{pmatrix} 1 & 1 \\ 1 & 1 \\ 1 & 1 \end{pmatrix} - 0.01 \begin{pmatrix} 126 & 126 \\ 1*126 & 1*126 \end{pmatrix} = \begin{pmatrix} -0.26 & -0.26 \\ -0.26 & -0.26 \\ -0.26 & -0.26 \end{pmatrix} \\ &= \begin{pmatrix} w_{01}^{(2)} & w_{02}^{(2)} & w_{03}^{(2)} \\ w_{11}^{(2)} & w_{12}^{(2)} & w_{13}^{(2)} \\ w_{21}^{(2)} & w_{22}^{(2)} & w_{23}^{(2)} \end{pmatrix} - \eta \begin{pmatrix} \delta_{1}^{(2)} & \delta_{2}^{(2)} & \delta_{3}^{(2)} \\ x_{1}^{(1)} \delta_{1}^{(2)} & x_{1}^{(1)} \delta_{2}^{(2)} & x_{1}^{(1)} \delta_{3}^{(2)} \\ x_{2}^{(1)} \delta_{2}^{(2)} & x_{2}^{(1)} \delta_{2}^{(2)} & x_{2}^{(1)} \delta_{3}^{(2)} \end{pmatrix} \\ &= \begin{pmatrix} 1 & 1 & 1 \\ 1 & 1 & 1 \end{pmatrix} - 0.01 \begin{pmatrix} 42 & 42 & 42 \\ 3*42 & 3*42 & 3*42 \\ 3*42 & 3*42 & 3*42 \end{pmatrix} \\ &= \begin{pmatrix} 0.58 & 0.58 & 0.58 \\ -0.26 & -0.26 & -0.26 \\ -0.26 & -0.26 & -0.26 \end{pmatrix} \\ &= 0.26 & -0.26 & -0.26 \\ &= 0.26 & -0.26 & -0.26 \end{pmatrix} \end{split}$$