

$$\begin{aligned}
\mathbf{w}_3^{(1)} &= \mathbf{w}_2^{(1)} - \eta \vec{x}_n^{(0)} (\vec{\delta}^{(1)})^T = \mathbf{w}_2^{(1)} - \eta \begin{pmatrix} 1 \\ x_{n1}^{(0)} \\ x_{n2}^{(0)} \end{pmatrix} (\delta_1^{(1)}, \delta_2^{(1)}) \\
&= \begin{pmatrix} w_{01}^{(1)} & w_{02}^{(1)} \\ w_{11}^{(1)} & w_{12}^{(1)} \\ w_{21}^{(1)} & w_{22}^{(1)} \end{pmatrix} - \eta \begin{pmatrix} \delta_1^{(1)} & \delta_2^{(1)} \\ x_{n1}^{(0)} \delta_1^{(1)} & x_{n1}^{(0)} \delta_2^{(1)} \\ x_{n2}^{(0)} \delta_1^{(1)} & x_{n2}^{(0)} \delta_2^{(1)} \end{pmatrix} \\
&= \begin{pmatrix} -0.17 & -0.17 \\ -0.35 & -0.35 \\ -0.35 & -0.35 \end{pmatrix} - 0.01 \begin{pmatrix} 0 & 0 \\ (-1) * 0 & (-1) * 0 \\ (+1) * 0 & (+1) * 0 \end{pmatrix} \\
&= \begin{pmatrix} -0.17 & -0.17 \\ -0.35 & -0.35 \\ -0.35 & -0.35 \end{pmatrix}
\end{aligned}$$

$$\begin{aligned}
\mathbf{w}_3^{(2)} &= \mathbf{w}_2^{(2)} - \eta \vec{x}_n^{(1)} (\vec{\delta}^{(2)})^T = \mathbf{w}_2^{(2)} - \eta \begin{pmatrix} 1 \\ x_1^{(1)} \\ x_2^{(1)} \end{pmatrix} (\delta_1^{(2)}, \delta_2^{(2)}, \delta_3^{(2)}) \\
&= \begin{pmatrix} w_{01}^{(2)} & w_{02}^{(2)} & w_{03}^{(2)} \\ w_{11}^{(2)} & w_{12}^{(2)} & w_{13}^{(2)} \\ w_{21}^{(2)} & w_{22}^{(2)} & w_{23}^{(2)} \end{pmatrix} - \eta \begin{pmatrix} \delta_1^{(2)} & \delta_2^{(2)} & \delta_3^{(2)} \\ x_1^{(1)} \delta_1^{(2)} & x_1^{(1)} \delta_2^{(2)} & x_1^{(1)} \delta_3^{(2)} \\ x_2^{(1)} \delta_1^{(2)} & x_2^{(1)} \delta_2^{(2)} & x_2^{(1)} \delta_3^{(2)} \end{pmatrix} \\
&= \begin{pmatrix} 0.46 & 0.46 & 0.46 \\ -0.29 & -0.29 & -0.29 \\ -0.29 & -0.29 & -0.29 \end{pmatrix} - 0.01 \begin{pmatrix} 3.82 & 3.82 & 3.82 \\ 0 * 3.82 & 0 * 3.82 & 0 * 3.82 \\ 0 * 3.82 & 0 * 3.82 & 0 * 3.82 \end{pmatrix} \\
&= \begin{pmatrix} 0.42 & 0.42 & 0.42 \\ -0.29 & -0.29 & -0.29 \\ -0.29 & -0.29 & -0.29 \end{pmatrix}
\end{aligned}$$

$$\begin{aligned}
\mathbf{w}_3^{(3)} &= \mathbf{w}_2^{(3)} - \eta \vec{x}_n^{(2)} (\vec{\delta}^{(3)})^T = \mathbf{w}_2^{(3)} - \eta \begin{pmatrix} 1 \\ x_1^{(2)} \\ x_2^{(2)} \\ x_3^{(2)} \end{pmatrix} \delta_1^{(3)} \\
&= \begin{pmatrix} 0.64 \\ -1.91 \\ -1.91 \\ -1.91 \end{pmatrix} - 0.01 \begin{pmatrix} -2.00 \\ 0.46 * (-2.00) \\ 0.46 * (-2.00) \\ 0.46 * (-2.00) \end{pmatrix} = \begin{pmatrix} 0.66 \\ -1.90 \\ -1.90 \\ -1.90 \end{pmatrix}
\end{aligned}$$

t=4, 对于第四个样本 $\vec{x}_2 = (1, -1)^T$, 则第一层神经元的输入为:

$$\begin{pmatrix} s_1^{(1)} \\ s_2^{(1)} \end{pmatrix} = (\mathbf{w}^{(1)})^T \vec{x}_n^{(0)} = \begin{pmatrix} -0.17 & -0.35 & -0.35 \\ -0.17 & -0.35 & -0.35 \end{pmatrix} \begin{pmatrix} 1 \\ 1 \\ -1 \end{pmatrix} = \begin{pmatrix} -0.17 \\ -0.17 \end{pmatrix}$$