

深度神经网络

与神经网络的区别在隐藏层数量变多了(即网络变深了)

从宏观来说，机器学习有两个高潮的发展：浅层学习 (Shallow Learning) 和深度学习 (Deep Learning, DL)

(1) 第一个是在20世纪80年代末期，BP算法的发明，掀起了一波机器学习的热潮。因为这种算法可以让模型从大量训练样本中学习到一定的规律，这比基于人工规则的系统效果好。当时的人工网络基本上只含有一层隐含层，是浅层网络。20世纪90年代，SVM、Boost等各种浅层机器学习模型相继出现。

(2) 2006年，加拿大多伦多大学的Geoffrey Hinton教授和他的学生发表了一篇文章，其主要观点是：多隐藏层的神经网络具有更好的特征学习能力，从此开启深度学习的浪潮。

► 表示深度神经网络 (Deep Neural Network, DNN) 的元素

□ 深度神经网络的层数： $L = 4$

□ 第1层的神经元数： $n^{[1]}$

□ 第1层的激活函数： $a^{[1]}$

□ 第1层的权重与偏置： $w^{[1]}, b^{[1]}$

► 参数与超参数

□ 参数指与预测函数相关的 $w^{[l]}, b^{[l]}$

□ 超参数指控制最终参数 $w^{[l]}, b^{[l]}$ 取值的其他参数，如隐含层数量与每层神经元数、激活函数、学习率、梯度下降的迭代次数等

从黑白模型到多层次每层神经元在理解和提取什么特征

只能通过超参数调控其大致行为 \rightarrow Inception 模块降低模型参数



卷积神经网络

计算机视觉：让机器理解图片/视频中的内容

全连接神经网络处理图像面临问题

$3 \times 100 \times 100$ 图像 \rightarrow NNN \rightarrow N 类分类向量 ($n \times 1$ 维)

若采用全连接神经网络输入维度 $3 \times 100 \times 100 \Rightarrow$ 输入维度大，权值多，易过拟合

图像平铺失去掉像素点的空间联系

对图像移位、缩放和其它形式的退化不敏感

仅卷积神经网络

工作原理 \Rightarrow 提取图像局部特征进行比对

Receptive field (感受野)



二维卷积运算：将输入或卷积核做互相关运算，从最左上方开始，按从左往右、从上往下的顺序，二阶核窗口一次在输入或卷积核上滑动，当窗口滑到某一位置时，窗口中的输入数据组与核数据组按元素乘积并求和，得到输出矩阵中相对应位置的元素。

padding: 在输入图像四周填充元素以方便推测输出形状

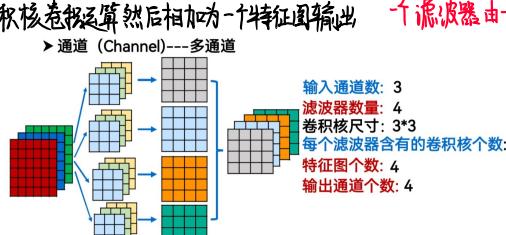
$P=1$ 时输出大小相同

每个卷积核只与输入数据的局部区域连接 \Rightarrow 大大减少网络参数，可以提取局部特征
更深的网络可使特征图单元感受野更加广阔，从而捕捉更大尺寸的特征

通道 channel 彩色图像三通道 双向通道卷积 \rightarrow 输入层 单通道：三通道

输入通道数为上层输出通道数，输出通道数取决于滤波器数目 逐层计算渐进通道

和一个卷积核卷积运算然后相加为一个特征图输出 一个滤波器由一组卷积核组成



需训练参数数量由卷积核个数和大小决定而与图片大小无关 每个滤波器还有个偏置量

例：假设输入的图像的尺寸是 $100 \times 100 \times 3$ ，卷积层使用 10 个 $3 \times 3 \times 3$ 的卷积核，这一层需要训练的参数是多少？

$10 \times (3 \times 3 \times 3 + 1) = 280$

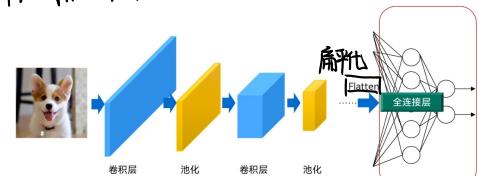
偏置 全连接神经网络

参数共享/权值共享 控制参数数量因渐进滤波器与上一层局部连接且所有局部连接都使用同样的参数，有效减少参数数目

池化 \Rightarrow 下采样，采样不改变图像中的物体；可缩小图像尺寸，减少最后连接层参数量，加快

最底层平坦池化计算防止过拟合

卷积神经网络的结构



卷积神经网络的反向传播 更新连接层/卷积层的权值；对池化操作

CNN与全连接神经网络的反向传播：

► 最后的输出层到最后一个卷积层或池化层的误差计算方式是基本相同

► 池化层到卷积层，卷积层到输出层 (or 池化层)

的误差传播方式与全连接网络是大不相同

池化层：上层为卷积层，下层为池化层，当前置梯度一样，卷积层激活函数梯度

$$\frac{\partial J}{\partial z^M} = \frac{\partial J}{\partial z^L} \cdot \frac{\partial z^L}{\partial z^M} \cdot \frac{\partial a^L}{\partial z^M} = (\text{upsamplec}) \frac{\partial J}{\partial z^L} \cdot \frac{\partial a^L}{\partial z^M}$$

平均池化反向传播：将当前位置的梯度均分

记录前向传播最大值位置索引，将当前位置梯度填入对应位置

卷积层：为 L 层，上层往该池化层间倒至 L 层梯度为 $\frac{\partial J}{\partial z^{L-1}}$ ，记为 $\frac{\partial J}{\partial z^L}$

卷积层反向传播：将当前位置梯度均分

记录前向传播最大值位置索引，将当前位置梯度填入对应位置

正向传播

$Z_{11}, Z_{12}, Z_{13}, Z_{21}, Z_{22}$ = 卷积 $\left(\begin{array}{ccc} X_{11}, X_{12}, X_{13} \\ X_{21}, X_{22}, X_{23} \\ X_{31}, X_{32}, X_{33} \end{array} \right) \cdot \left(\begin{array}{cc} F_{11}, F_{12} \\ F_{21}, F_{22} \end{array} \right)$

$X(\text{输入})$ $F(\text{卷积核})$

$$z_{11} = X_{11}F_{11} + X_{12}F_{12} + X_{21}F_{21} + X_{22}F_{22}$$

$$z_{12} = X_{12}F_{11} + X_{13}F_{12} + X_{22}F_{21} + X_{23}F_{22}$$

$$z_{21} = X_{21}F_{11} + X_{22}F_{12} + X_{31}F_{21} + X_{32}F_{22}$$

$$z_{22} = X_{22}F_{11} + X_{23}F_{12} + X_{32}F_{21} + X_{33}F_{22}$$

求解 $\frac{\partial J}{\partial z} = \frac{\partial J}{\partial z} \cdot \frac{\partial z}{\partial F}$ ，即求解 $\frac{\partial z}{\partial F}$

$$\frac{\partial J}{\partial F} = \sum_{k=1}^K \frac{\partial J}{\partial z_k} \cdot \frac{\partial z_k}{\partial F} = \frac{\partial J}{\partial z_{11}} \cdot \frac{\partial z_{11}}{\partial F_{11}} + \frac{\partial J}{\partial z_{12}} \cdot \frac{\partial z_{12}}{\partial F_{12}} + \frac{\partial J}{\partial z_{21}} \cdot \frac{\partial z_{21}}{\partial F_{21}} + \frac{\partial J}{\partial z_{22}} \cdot \frac{\partial z_{22}}{\partial F_{22}}$$

$$\frac{\partial z_{11}}{\partial F_{11}} = \frac{\partial z_{11}}{\partial X_{11}} \cdot \frac{\partial X_{11}}{\partial F_{11}} + \frac{\partial z_{11}}{\partial X_{12}} \cdot \frac{\partial X_{12}}{\partial F_{11}} + \frac{\partial z_{11}}{\partial X_{21}} \cdot \frac{\partial X_{21}}{\partial F_{11}} + \frac{\partial z_{11}}{\partial X_{22}} \cdot \frac{\partial X_{22}}{\partial F_{11}}$$

$$\frac{\partial z_{12}}{\partial F_{12}} = \frac{\partial z_{12}}{\partial X_{11}} \cdot \frac{\partial X_{11}}{\partial F_{12}} + \frac{\partial z_{12}}{\partial X_{12}} \cdot \frac{\partial X_{12}}{\partial F_{12}} + \frac{\partial z_{12}}{\partial X_{21}} \cdot \frac{\partial X_{21}}{\partial F_{12}} + \frac{\partial z_{12}}{\partial X_{22}} \cdot \frac{\partial X_{22}}{\partial F_{12}}$$

$$\frac{\partial z_{21}}{\partial F_{21}} = \frac{\partial z_{21}}{\partial X_{11}} \cdot \frac{\partial X_{11}}{\partial F_{21}} + \frac{\partial z_{21}}{\partial X_{12}} \cdot \frac{\partial X_{12}}{\partial F_{21}} + \frac{\partial z_{21}}{\partial X_{21}} \cdot \frac{\partial X_{21}}{\partial F_{21}} + \frac{\partial z_{21}}{\partial X_{22}} \cdot \frac{\partial X_{22}}{\partial F_{21}}$$

$$\frac{\partial z_{22}}{\partial F_{22}} = \frac{\partial z_{22}}{\partial X_{11}} \cdot \frac{\partial X_{11}}{\partial F_{22}} + \frac{\partial z_{22}}{\partial X_{12}} \cdot \frac{\partial X_{12}}{\partial F_{22}} + \frac{\partial z_{22}}{\partial X_{21}} \cdot \frac{\partial X_{21}}{\partial F_{22}} + \frac{\partial z_{22}}{\partial X_{22}} \cdot \frac{\partial X_{22}}{\partial F_{22}}$$

$$\frac{\partial z_{11}}{\partial X_{11}} = \frac{\partial z_{11}}{\partial F_{11}} \cdot \frac{\partial F_{11}}{\partial X_{11}} + \frac{\partial z_{11}}{\partial F_{21}} \cdot \frac{\partial F_{21}}{\partial X_{11}} + \frac{\partial z_{11}}{\partial F_{12}} \cdot \frac{\partial F_{12}}{\partial X_{11}} + \frac{\partial z_{11}}{\partial F_{22}} \cdot \frac{\partial F_{22}}{\partial X_{11}}$$

$$\frac{\partial z_{12}}{\partial X_{12}} = \frac{\partial z_{12}}{\partial F_{11}} \cdot \frac{\partial F_{11}}{\partial X_{12}} + \frac{\partial z_{12}}{\partial F_{21}} \cdot \frac{\partial F_{21}}{\partial X_{12}} + \frac{\partial z_{12}}{\partial F_{12}} \cdot \frac{\partial F_{12}}{\partial X_{12}} + \frac{\partial z_{12}}{\partial F_{22}} \cdot \frac{\partial F_{22}}{\partial X_{12}}$$

$$\frac{\partial z_{21}}{\partial X_{21}} = \frac{\partial z_{21}}{\partial F_{11}} \cdot \frac{\partial F_{11}}{\partial X_{21}} + \frac{\partial z_{21}}{\partial F_{21}} \cdot \frac{\partial F_{21}}{\partial X_{21}} + \frac{\partial z_{21}}{\partial F_{12}} \cdot \frac{\partial F_{12}}{\partial X_{21}} + \frac{\partial z_{21}}{\partial F_{22}} \cdot \frac{\partial F_{22}}{\partial X_{21}}$$

$$\frac{\partial z_{22}}{\partial X_{22}} = \frac{\partial z_{22}}{\partial F_{11}} \cdot \frac{\partial F_{11}}{\partial X_{22}} + \frac{\partial z_{22}}{\partial F_{21}} \cdot \frac{\partial F_{21}}{\partial X_{22}} + \frac{\partial z_{22}}{\partial F_{12}} \cdot \frac{\partial F_{12}}{\partial X_{22}} + \frac{\partial z_{22}}{\partial F_{22}} \cdot \frac{\partial F_{22}}{\partial X_{22}}$$

$$\frac{\partial z_{11}}{\partial F_{11}} = \frac{\partial z_{11}}{\partial X_{11}} \cdot \frac{\partial X_{11}}{\partial F_{11}} + \frac{\partial z_{11}}{\partial X_{12}} \cdot \frac{\partial X_{12}}{\partial F_{11}} + \frac{\partial z_{11}}{\partial X_{21}} \cdot \frac{\partial X_{21}}{\partial F_{11}} + \frac{\partial z_{11}}{\partial X_{22}} \cdot \frac{\partial X_{22}}{\partial F_{11}}$$

$$\frac{\partial z_{12}}{\partial F_{12}} = \frac{\partial z_{12}}{\partial X_{11}} \cdot \frac{\partial X_{11}}{\partial F_{12}} + \frac{\partial z_{12}}{\partial X_{12}} \cdot \frac{\partial X_{12}}{\partial F_{12}} + \frac{\partial z_{12}}{\partial X_{21}} \cdot \frac{\partial X_{21}}{\partial F_{12}} + \frac{\partial z_{12}}{\partial X_{22}} \cdot \frac{\partial X_{22}}{\partial F_{12}}$$

$$\frac{\partial z_{21}}{\partial F_{21}} = \frac{\partial z_{21}}{\partial X_{11}} \cdot \frac{\partial X_{11}}{\partial F_{21}} + \frac{\partial z_{21}}{\partial X_{12}} \cdot \frac{\partial X_{12}}{\partial F_{21}} + \frac{\partial z_{21}}{\partial X_{21}} \cdot \frac{\partial X_{21}}{\partial F_{21}} + \frac{\partial z_{21}}{\partial X_{22}} \cdot \frac{\partial X_{22}}{\partial F_{21}}$$

$$\frac{\partial z_{22}}{\partial F_{22}} = \frac{\partial z_{22}}{\partial X_{11}} \cdot \frac{\partial X_{11}}{\partial F_{22}} + \frac{\partial z_{22}}{\partial X_{12}} \cdot \frac{\partial X_{12}}{\partial F_{22}} + \frac{\partial z_{22}}{\partial X_{21}} \cdot \frac{\partial X_{21}}{\partial F_{22}} + \frac{\partial z_{22}}{\partial X_{22}} \cdot \frac{\partial X_{22}}{\partial F_{22}}$$

卷积神经网络经典结构 PPT P50-P78

$\frac{\partial z}{\partial F} = \text{卷积} \left\{ \begin{array}{l} X(\text{输入}), \text{回传的梯度} \\ F(\text{卷积核}), \text{旋转} 180^\circ \end{array} \right\}$

$\frac{\partial X}{\partial x} = \text{卷积} \left\{ \begin{array}{l} X(\text{输入}), \text{回传的梯度} \\ F(\text{卷积核}), \text{旋转} 180^\circ \end{array} \right\}$

$\frac{\partial z}{\partial x} = \text{卷积} \left\{ \begin{array}{l} X(\text{输入}), \text{回传的梯度} \\ F(\text{卷积核}), \text{旋转} 180^\circ \end{array} \right\}$