

<u>Help</u>

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<u>Course</u> **Discussion** <u>Progress</u> <u>Dates</u>



Problem Sets due Jul 6, 2022 21:22 PKT Completed

Problems 1-2 correspond to "The generative approach to classification"

Problem 1

1/1 point (graded)

Which of the following accurately describes the generative approach to classification, in the case where there are just two labels?

Fit a	a model	to the	boundary	between	the two	classes.
	a iiioaci	to the	Dodinadi y	20011	CITO CVVO	Classes.

• Fit a probability distribution to each class separately.



Submit

Problem 2

1/1 point (graded)

In a generative model with k classes, the class probabilities are $\pi_1, ..., \pi_k$ (summing to 1) and the individual class distributions are $P_1(x), ..., P_k(x)$. In order to classify a new point x, we should pick the label j that maximizes which of the following quantities?

 $\bigcap \pi_j$

 $\bigcap P_j(x)$

 $\bigcap \pi_j + P_j(x)$





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Problems 3-8 correspond to "Probability review I: probability spaces, events, conditioning"

Problem 3

3/3 points (graded)

What is the size of the sample space in each of the following experiments?

a) A fair coin is tossed.

2

Answer

Correct: The possible outcomes are 0 and 1.

b) A fair die is rolled.
6
Answer Correct: The possible outcomes are 1,2,3,4,5,6.
c) A fair coin is tossed ten times in a row.
1024
Answer Correct: For each of the coins, there are two possible outcomes. For all ten coins together, there are $2\times 2\times \cdots \times 2=1024$ outcomes.
Submit
Problem 5
3/3 points (graded) Two fair dice are rolled. What is the probability that:
a) Their sum is 10, given that the first roll is a 6?
1/6
Answer Correct: If the first roll is a 6, the second needs to be a 4, which happens with probability 1/6.
b) Their sum is 10, given that the first roll is an even number?
1/9
Answer Correct: The probability that the sum is 10 <i>given that</i> the first roll is even is, by the basic conditioning formula, equal to Pr(sum is 10 AND first roll is even) divided by Pr(first roll is even). Let's compute these two separately. Pr(sum is 10 AND first roll is even) correspond to just two possible outcomes, (4,6) and (6,4); the probability that one of these occurs is 2/36 = 1/18. Meanwhile, Pr(first roll is even) is 1/2. Now divide.
c) They have the same value?
1/6
Answer Correct: Whatever the first roll is, the probability that the second roll is exactly that number is 1/6.
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1/1 point (graded)

A certain genetic disease occurs in 5% of men but just 1% of women. Let's say there are an equal number of men and women in the world. A person is picked at random and found to possess the disease. What is the probability, given this information, that the person is male?

0.83

Submit

Problem 7

2/2 points (graded)

The TryMe smartphone company has three factories making its phones. They are all fairly unreliable: 10% of the phones from factory 1 are defective, 20% of the phones from factory 2 are defective, and 24% of the phones from factory 3 are defective. The factories do not produce the same numbers of phones: factory 1 produces 1/2 of TryMe's phones, while factories 2 and 3 each produce 1/4.

a) What is the probability that a TryMe phone chosen at random is defective?

0.16

Answer

Correct:

For a phone chosen at random, let D denote the event that it is defective, F_1 that it comes from factory 1, F_2 that it comes from factory 2, and F_3 that it comes from factory 3. Then $Pr(D) = Pr(D \cap F_1) + Pr(D \cap F_2) + Pr(D \cap F_3)$. Applying the formula for conditional probability, we then have $Pr(D) = Pr(F_1)Pr(D|F_1) + Pr(F_2)Pr(D|F_2) + Pr(F_3)Pr(D|F_3)$. We have all the information we need for the right-hand side; plugging in, $Pr(D) = \frac{1}{2} \times 0.1 + \frac{1}{4} \times 0.2 + \frac{1}{4} \times 0.24 = 0.16$.

b) Given that a TryMe phone is defective, what is the probability that it came from factory 1?

0.3125

Answer

Correct: By Bayes' rule, $Pr(F_1|D) = Pr(F_1) \times \frac{Pr(D|F_1)}{Pr(D)} = \frac{1}{2} \times \frac{0.1}{0.16} = \frac{5}{16}$.

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Problem 8

1/1 point (graded)

Here are some statistics collected by a doctor about patients who walk into her office.

- · 25% of the patients have the flu.
- · Among patients with the flu, 75% have a fever.
- · Among patients who don't have the flu, 50% have a fever.

A new person walks into the doctor's office and turns out to have a fever. What is the probability that

he has the flu?

0.33

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Problems 9-12 correspond to "Generative modeling in one dimension"

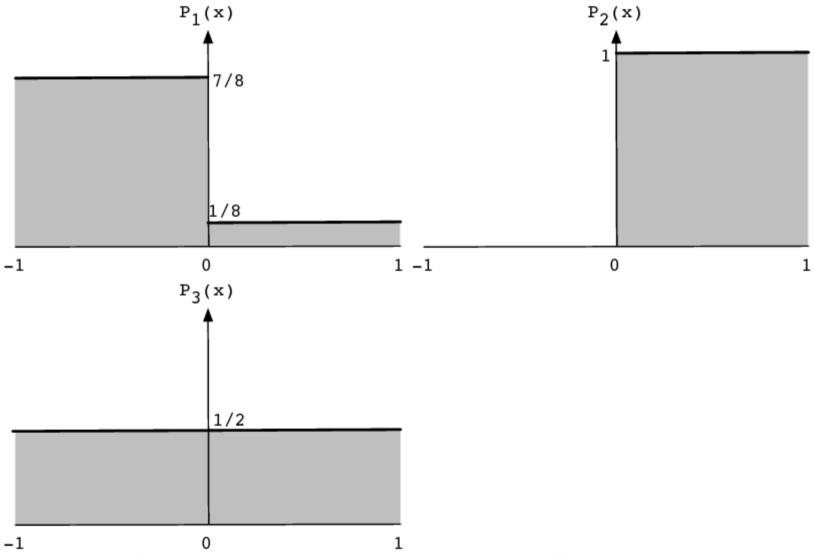
Problem 9

2/2 points (graded)

Suppose we have one-dimensional data points lying in X = [-1, 1], that have associated labels in $Y = \{1, 2, 3\}$. The individual classes have weights

$$\pi_1 = \frac{1}{3}, \quad \pi_2 = \frac{1}{6}, \quad \pi_3 = \frac{1}{2}$$

and densities P_1, P_2, P_3 as shown below. (For instance, P_1 is the density of the points whose label is 1; in particular, this means that P_1 integrates to 1.)



Based on this information, what labels should be assigned to the following points?

a)
$$-1/2$$

1

b) 1/2

3

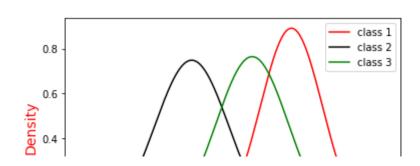
Submit Problem 10 2/2 points (graded) A set of 100 data points in R have mean of 20 and standard deviation of 10. We want to fit a Gaussian $N(\mu, \sigma^2)$ to this data. What μ and σ^2 should we pick? a) μ = 20 b) $\sigma^2 =$ 100 Submit Problem 11 1/1 point (graded) A generative approach is used for a binary classification problem and it turns out that the resulting classifier predicts + at all points x in the input space. What can we conclude for sure? Check all that apply. There are no – points in the training set. The + points are spread out over the space, while the - points are concentrated in a small region. ✓ There are fewer – points than + points in the training set. The density of + points is greater than the density of - points everywhere in the space.

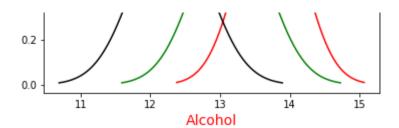
Problem 12

Submit

5/5 points (graded)

For the winery example from lecture, the densities obtained are reproduced here:





The class probabilities are $\pi_1=0.33, \pi_2=0.39, \pi_3=0.28.$ What labels would be assigned to the following points?

a) 12.0

2	~
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b) 12.5



c) 13.0



d) 13.5



e) 14.0



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Problems 13-15 correspond to "Probability review II: random variables, expected value, and variance"

Problem 13

4/4 points (graded)

A fair die is rolled twice. Let X_1 and X_2 denote the outcomes, and define random variable X to be the minimum of X_1 and X_2 .

a) How many possible values are there for *X*?



Answer

Correct: The minimum of the two rolls could be any number from 1 to 6.

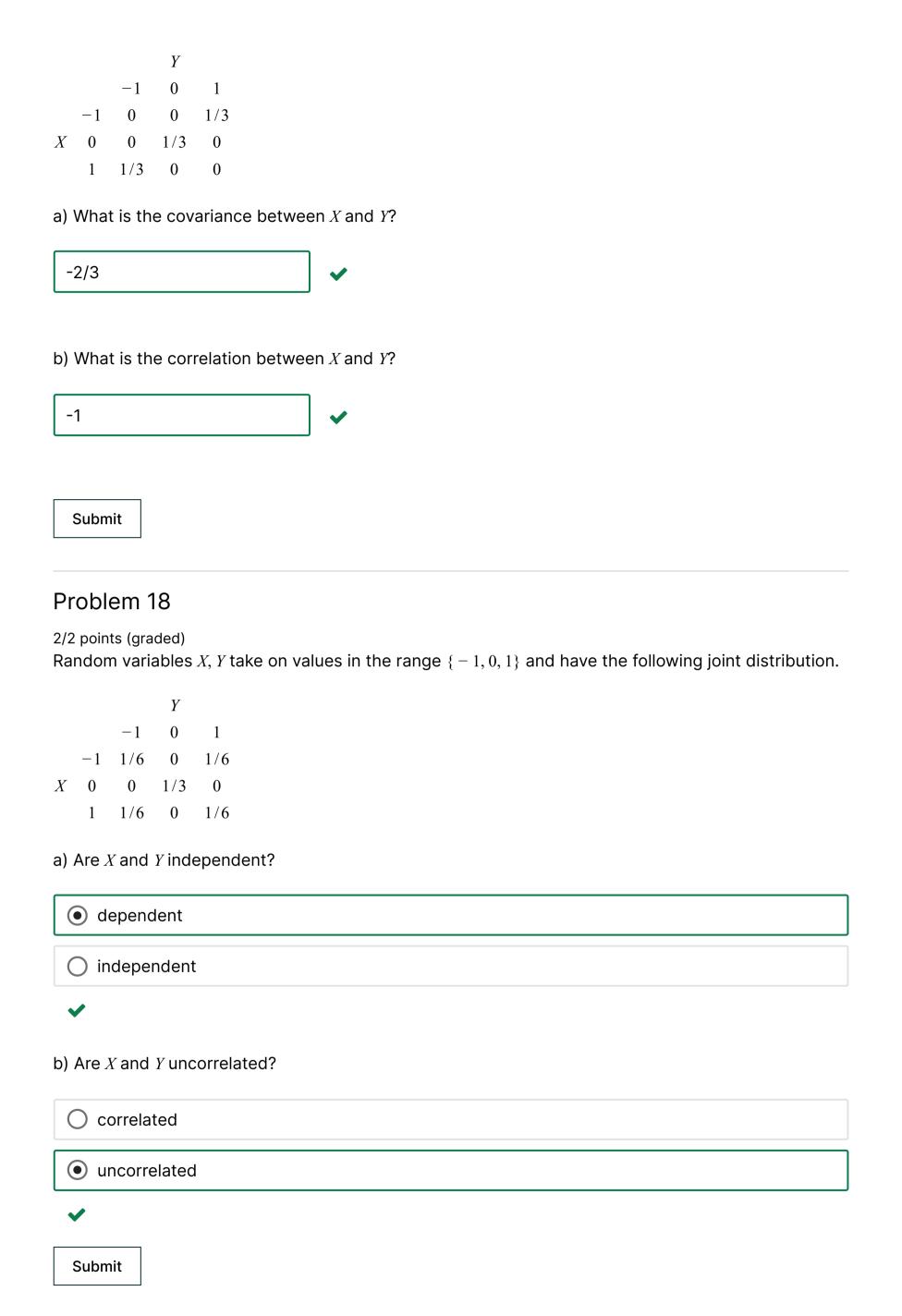
ω_I which is the probability that A	— 1:
11/36	
Answer Correct: This is the probability tl	hat at least one of the two rolls is a 1.
c) What is $E(X)$?	
2.52	
d) What is var(X)?	
1.96	
Submit	
Problem 14	
2/2 points (graded) n a series of ten independent ex	operiments, a random variable X takes on values
	1, 1, 2, 5, 0, 1, 2, 2, 1, 1.
a) Give an estimate of $E(X)$.	
1.6	
o) Give an estimate of $var(X)$.	
1.64	
1.04	
Submit	
Problem 15	
/1 point (graded)	ariables has zero variance? Check all that apply.
\square X takes on values -1 and 1	
	man oqual probability.
✓ X always takes on value 1.	
\square X is always equal to X^2 .	
\checkmark X is always zero.	

✓
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Problems 16-18 correspond to "Probability review III: modeling dependence"
Problem 16
4/4 points (graded) In each of the following cases, say whether X and Y are dependent or independent.
a) Randomly pick a card from a pack of 52 cards. Define X to be 1 if the card is a Jack, and 0 otherwise. Define Y to be 1 if the card is a spade, and 0 otherwise.
Odependent
independent
✓
b) Randomly pick two cards from a pack of 52 cards. X is 1 if the first card is a spade, and 0 otherwise. Y is 1 if the second card is a spade, and 0 otherwise.
dependent
independent
c) Toss a coin ten times. X is the number of heads and Y is the number of tails.
dependent
Oindependent
✓
d) Roll a fair die. X is 1 if the outcome is even, and 0 otherwise. Y is 1 if the outcome is \geq 3, and zero otherwise.
Odependent
independent
✓
Submit
Droblem 17

Problem 17

2/2 points (graded)

Random variables X, Y take on values in the range $\{-1, 0, 1\}$ and have the following joint distribution.



Problems 19-20 correspond to "Two-dimensional generative modeling with the bivariate Gaussian"

2/2 points (graded)

Each of the following scenarios describes a joint distribution (x, y). In each case, give the parameters of the (unique) bivariate Gaussian that satisfies these properties.

a) x has mean 2 and standard deviation 1, y has mean 2 and standard deviation 0.5, and the correlation between x and y is -0.5.

$$\mu = \begin{pmatrix} 1 \\ 1 \end{pmatrix}, \Sigma = \begin{pmatrix} 1 & -\frac{1}{2} \\ -\frac{1}{2} & \frac{1}{2} \end{pmatrix}$$

$$\Omega$$
 $\mu = \begin{pmatrix} 2 \\ -1 \end{pmatrix}$, $\Sigma = \begin{pmatrix} 1 & -1 \\ -1 & \frac{1}{2} \end{pmatrix}$

$$\mu = \begin{pmatrix} 2 \\ 2 \end{pmatrix}$$
 , $\Sigma = \begin{pmatrix} 1 & -\frac{1}{4} \\ -\frac{1}{4} & \frac{1}{4} \end{pmatrix}$

b) x has mean 1 and standard deviation 1, and y is equal to x.

$$\bigcap$$
 $\mu=\left(egin{array}{cc} 0 \ 0 \end{array}
ight)$, $\Sigma=\left(egin{array}{cc} 1 & 0 \ 0 & 1 \end{array}
ight)$

$$\mu = \begin{pmatrix} 1 \\ 1 \end{pmatrix}$$
 , $\Sigma = \begin{pmatrix} 1 & 1 \\ 1 & 1 \end{pmatrix}$

$$\mu = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$
 , $\Sigma = \begin{pmatrix} 1 & -1 \\ -1 & 1 \end{pmatrix}$

$$\mu = \begin{pmatrix} 1 \\ -1 \end{pmatrix}$$
, $\Sigma = \begin{pmatrix} 0 & 0 \\ 0 & 0 \end{pmatrix}$



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Problem 20

3/3 points (graded)

Here are four possible shapes of Gaussian distributions:











For each of the following Gaussians $N(\mu, \Sigma)$, indicate which of these shapes (1,2,3,4) is the best approximation.

a)
$$\mu = \begin{pmatrix} 0 \\ 0 \end{pmatrix}$$
 and $\Sigma = \begin{pmatrix} 9 & 0 \\ 0 & 1 \end{pmatrix}$

b)
$$\mu = \begin{pmatrix} 0 \\ 0 \end{pmatrix}$$
 and $\Sigma = \begin{pmatrix} 9 & 2 \\ 2 & 1 \end{pmatrix}$

c)
$$\mu = \begin{pmatrix} 0 \\ 0 \end{pmatrix}$$
 and $\Sigma = \begin{pmatrix} 1 & -0.75 \\ -0.75 & 1 \end{pmatrix}$

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