education_data

February 20, 2021

```
[2]: library(ISLR)
    library(dplyr)
    library(lmridge)
    library(leaps)
    library(glmnet)
    library(DAAG)
    library(lmvar)
    library(MASS)
```

Importing GEORGIA education data...

```
[3]: # Import
k_read = read.csv("kread.csv")

[4]: #convert Farm to binary
k_read = cbind(k_read, 'FARM_BIN' = as.integer(k_read[,'FARM']=='Y'))
k_read = subset(k_read, select = -c(FARM))
```

0.1 Fill in missing values somehow

We need to fill in missing values, so let's clean the NA values from the data first.

```
[5]: cleaned_read = k_read[complete.cases(k_read),]
    cleaned_read = subset(cleaned_read, select = -c(ID.))

##get rows which correspond to NA vals

R_na = subset(k_read,is.na(R.SCORE))
L_na = subset(k_read,is.na(L.SCORE))

#drop columsn with NAs to create test set

R_test = subset(R_na, select= -c(R.SCORE,ID.))
L_test = subset(L_na, select = -c(L.SCORE,ID.))

##Use R Score, DIEBLS, INP, FARM_BIN to predict L Score
##Use L Score, DIEBLS, INP, FARM_BIN to predict R score
```

Create a train/test set since we want to figure out if an lm model will be any good in predicting

L.SCORE/R.SCORE. We are doing this since we don't have any actualy groundtruth labels for the NA values, and want to see how good this model is.

```
num_rows = c(1:nrow(cleaned_read)) ##CONSTANT
set.seed(0)
sampled = sample(num_rows)
test_size = .20*nrow(cleaned_read) ##CONSTANT
train_size = nrow(cleaned_read)-test_size ##CONSTANT
train_index = sampled[1:train_size] ##CONSTANT
test_index = sampled[(train_size + 1): nrow(cleaned_read)] ##CONSTANT

train_set = cleaned_read[train_index,]
test_set = cleaned_read[test_index,]
```

```
[7]: train_set
```

		R.SCORE	L.SCORE	DIEBLS	INP	$FARM_BIN$
		<int></int>	<int $>$	<int $>$	<int $>$	<int></int>
_	157	14	18	33	0	1
	78	17	18	16	0	0
	182	20	21	42	0	0
	144	18	20	30	0	1
	177	20	20	38	0	0
	50	14	10	8	1	1
	15	9	11	0	1	0
	61	14	9	12	1	0
	97	16	21	20	0	0
	22	16	13	0	1	0
	118	15	19	24	0	1
	85	12	13	18	0	0
	8	14	8	0	1	1
	84	19	21	17	0	0
	90	15	17	19	0	1
	44	16	14	6	1	1
	117	21	17	24	0	0
	124	17	16	26	0	0
	41	16	17	4	1	0
	175	20	16	38	0	0
	141	17	16	30	0	1
	101	20	19	21	0	0
	40	12	14	4	1	1
	96	20	20	20	0	0
	81	15	16	17	0	1
	174	20	20	37	0	0
	49	13	8	8	1	1
	125	16	17	26	0	1
	21	13	13	0	1	1
A data.frame: 136×5	51	11	11	8	1	1
					•••	
	183	19	19	44	0	0
	168	20	20	35	0	1
	7	19	7	0	1	1
	110	19	21	22	0	1
	62	16	13	12	1	0
	48	12	16	7	1	0
	170	18	20	36	0	0
	53	14	13	8	1	0
	58	14	18	10	1	1
	3	7	5	0	1	1
	73	15	13	15	0	0
	184	19	20	50	0	0
	173	19	19	37	0	1
	67	15	14	13	1	0
	134	15	19	28	0	0
	156	20	21	32	0	0
	92	16	18 3	19	0	0
	55	0	16	8	1	1
	28	18	20	0	1	1
	98	10	13	21	0	1

Fit the models on the train set using all variables other than R.Score/L.Score. This is probably not best practice because were are trying to predict DIEBELS with R.Score/L.Score

```
[8]: model_R = lm(R.SCORE~.,train_set, x = TRUE,y= TRUE)
model_L =lm(L.SCORE~.,train_set, x= TRUE, y= TRUE)
```

Creating custom scoring metrics for the cross validations

```
[9]: rsqd = function(object, y, X){
    preds = predict(object, as.data.frame(X))
    tss = sum((y-mean(y))%*%(y-mean(y)))
    rss = sum((y-preds)%*%(y-preds))
    rsq = 1 - (rss/tss)
    return(rsq)
    }
    rse = function(object,y,X){
        preds = predict(object, as.data.frame(X))
        rss = sum((y-preds)%*%(y-preds))
        rse = sqrt(rss/(length(y)-(length(coefficients(object)-1))))
        return(rse)
}
```

Run 5 fold CV on built-in metrics as well as rsqd custom metric

```
[10]: cv_R_rsq = cv.lm(object = model_R, k = 5, fun = rsqd, seed = 24)
cv_L_rsq = cv.lm(object = model_L, k = 5, fun = rsqd, seed = 24)
```

[11]: cv_R_rsq

Mean absolute error : 2.335835 Sample standard deviation : 0.3632365

Mean squared error : 10.20601 Sample standard deviation : 3.343929

Root mean squared error : 3.159387 Sample standard deviation : 0.5294868

User supplied function : 0.3890505 Sample standard deviation : 0.197561

[12]: cv_L_rsq

Mean absolute error : 2.369548 Sample standard deviation : 0.3360425

Mean squared error : 9.654316 Sample standard deviation : 3.038032 Root mean squared error : 3.073806 Sample standard deviation : 0.507485

User supplied function : 0.4191553 Sample standard deviation : 0.1789954

Rsquard test statistic is around .4 for all models. Rsquared is low, so there isn't too much of a linear relationship here. Shouldn't expect much during testing. Figure out rse below.

```
[13]: cv_R_rse = cv.lm(object = model_R, k = 5, fun = rsqd, seed = 24) cv_L_rse = cv.lm(object = model_L, k = 5, fun = rse, seed = 24)
```

Below, RSE is around 3 for both models, which isn't that bad.

[14]: cv_R_rse

Mean absolute error : 2.335835 Sample standard deviation : 0.3632365

Mean squared error : 10.20601 Sample standard deviation : 3.343929

Root mean squared error : 3.159387 Sample standard deviation : 0.5294868

User supplied function : 0.3890505 Sample standard deviation : 0.197561

[15]: cv_L_rse

Mean absolute error : 2.369548 Sample standard deviation : 0.3360425

Mean squared error : 9.654316 Sample standard deviation : 3.038032

Root mean squared error : 3.073806 Sample standard deviation : 0.507485

User supplied function : 3.405234 Sample standard deviation : 0.5622038

```
[16]: test_preds_R = predict(model_R, subset(test_set,select = -c(R.SCORE)))
test_preds_L = predict(model_L, subset(test_set,select = -c(L.SCORE)))
```

Compute the RSE and R² statistics.

```
[17]: y_R = test_set[,'R.SCORE']
y_L = test_set[,'L.SCORE']
rss_R = sum((test_preds_R -y_R)%*%(test_preds_R-y_R))
rss_L = sum((test_preds_L-y_L)%*%(test_preds_L-y_L))
tss_R = sum((y_R -mean(y_R))%*%(y_R-mean(y_R)))
tss_L = sum((y_L-mean(y_L))%*%(y_L-mean(y_L)))

rsq_R = 1 - rss_R/tss_R
rsq_L = 1 - rss_L/tss_L

rse_R = sqrt(rss_R/(length(y_L)-2))
rse_L = sqrt(rss_L/(length(y_L)-2))
```

[18]: c(rsq_R,rsq_L,rse_R,rse_L)

 $1. \ 0.358059616325482 \ 2. \ 0.637019820218491 \ 3. \ 4.10994481278894 \ 4. \ 2.71121416750214$ We replace NA values with our predictions.

```
[19]: R_score_pred = predict(model_R, subset(R_na, select = -c(R.SCORE, ID.)) )
L_score_pred = predict(model_L, subset(L_na, select = -c(L.SCORE, ID.)))

##insert predicted values
R_na[,'R.SCORE'] = round(R_score_pred)
L_na[,'L.SCORE'] = round(L_score_pred)
#reset cleaned data variable
cleaned_read = k_read[complete.cases(k_read),]
#combine data frames
filled_read = rbind(cleaned_read, R_na)
filled_read = rbind(filled_read, L_na)
```

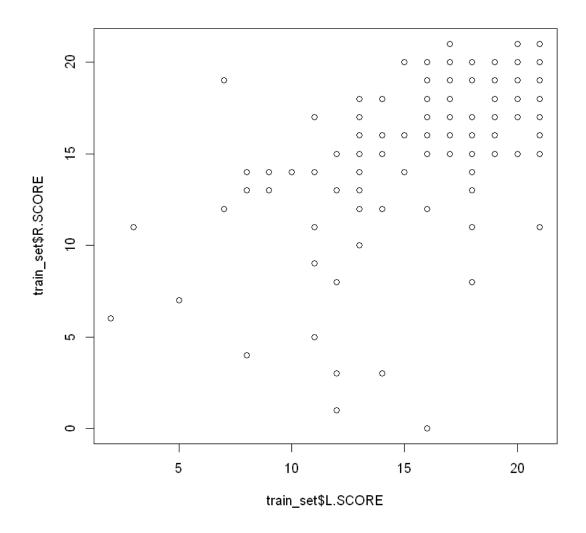
[20]: filled_read

$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$	N
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	
3 3 7 5 0 1 1 4 4 10 5 0 1 1 6 6 0 7 0 1 1 7 7 19 7 0 1 1 8 8 14 8 0 1 1 9 9 14 8 0 1 1 10 10 12 9 0 1 1 11 11 13 9 0 1 1 12 12 13 9 0 1 0 13 13 0 10 0 1 1 14 14 5 11 0 1 1 15 15 9 11 0 1 1 17 17 17 11 0 1 1 17 17 17 11 0 1 1 18 18 1	
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20 20 8 12 0 1 0 21 21 13 13 0 1 1 22 22 16 13 0 1 0 23 23 16 13 0 1 0 24 24 17 13 0 1 0 25 25 3 14 0 1 1	
21 21 13 13 0 1 1 22 22 16 13 0 1 0 23 23 16 13 0 1 0 24 24 17 13 0 1 0 25 25 3 14 0 1 1	
22 22 16 13 0 1 0 23 23 16 13 0 1 0 24 24 17 13 0 1 0 25 25 3 14 0 1 1	
23 23 16 13 0 1 0 24 24 17 13 0 1 0 25 25 3 14 0 1 1	
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A data.frame: $185 \times 6 \ 36 \ 36 \ 21 \ 15 \ 3 \ 1 \ 1$	
$171 \mid 171 20 20 36 0 0$	
$172 \mid 172 16 19 37 0 1$	
$173 \mid 173 19 19 37 0 1$	
$174 \mid 174 20 20 37 0 0$	
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177 177 20 20 38 0 0 170 170 21 20 20 20 20 20 20 2	
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180 180 19 18 41 0 1	
$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$	
182 182 20 21 42 0 0 183 183 19 19 44 0 0	
184 184 19 20 50 0	
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	
$119 \ \ 119 \ \ 19 \ \ 21 \ \ 24 \ \ 0 \ \ 0$	

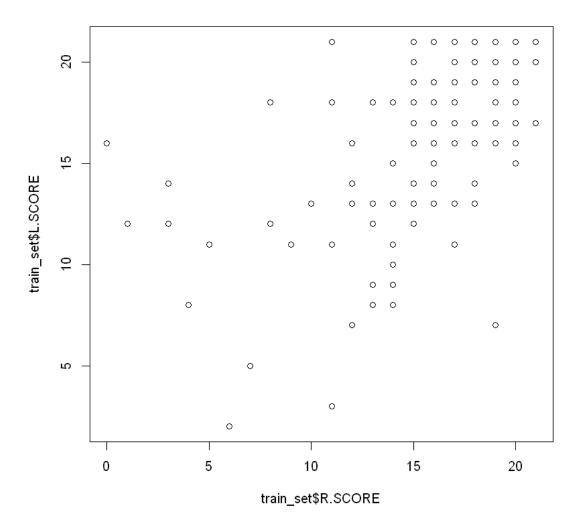
```
[21]: #reset row names
rownames(filled_read) <- 1:nrow(filled_read)</pre>
```

This isn't good practice though, maybe a better thing to do would just be to regress R.Score on L.Score. Let's see if there is some natural relationship between R.Score and L.Score. The graph below is less than exciting, but still shows a linear trend. Let's use R.Score to predict L.Score, and throug this relationship, we can determine R.Score through the coefficients by working backwards.

```
[22]: plot(train_set$L.SCORE, train_set$R.SCORE)
```



```
[23]: plot(train_set$R.SCORE, train_set$L.SCORE)
```



Fit the model and run CV validation on model_R_new

```
[24]: model_R_new =lm(R.SCORE~L.SCORE, train_set, x = TRUE,y= TRUE)
model_L_new = lm(L.SCORE~R.SCORE, train_set, x = TRUE, y= TRUE)
```

```
[25]: cv_R_new_rsqd = cv.lm(object = model_R_new, k = 5, fun = rsqd, seed = 24) cv_R_new_rse = cv.lm(object = model_R_new, k = 5, fun = rse, seed = 24)
```

[26]: cv_R_new_rsqd ##considerably worse than before

Mean absolute error : 2.476237Sample standard deviation : 0.3516305

Mean squared error : 12.37

Sample standard deviation : 4.007563 Root mean squared error : 3.476131 Sample standard deviation : 0.5984562 User supplied function : 0.2781961 Sample standard deviation : 0.1640992 [27]: cv_R_new_rse Mean absolute error 2.476237 Sample standard deviation : 0.3516305 Mean squared error : 12.37 Sample standard deviation : 4.007563 Root mean squared error : 3.476131 Sample standard deviation : 0.5984562 User supplied function : 3.612501 Sample standard deviation : 0.6219339 [28]: model R new\$coefficients model_L_new\$coefficients ##qet coefficients, since it is probably better to use_□ →a model whose covariate does not include diebls (Intercept) 5.50149566257854 L.SCORE 0.626034499950144 7.14186792869685 **R.SCORE** (Intercept) 0.584053302945383[29]: test_preds_R new = predict(model R_new, subset(test_set,select = -c(R.SCORE))) Test scores [30]: rss_R_new = sum((test_preds_R_new -y_R)%*%(test_preds_R_new-y_R)) $tss_R_new = sum((y_R - mean(y_R))\%*\%(y_R - mean(y_R)))$ rsq_R_new = 1 - rss_R_new/tss_R_new rse_R_new = sqrt(rss_R_new/(length(y_R)-2)) [31]: c(rss_R_new,tss_R_new,rsq_R_new,rse_R_new) $1.\ 505.14149615482\ 2.\ 842.029411764706\ 3.\ 0.400090437344515\ 4.\ 3.97311864343844$ Get rss R for comparison [32]: RSS_r_new = sum((model_R_new\$residuals)^2) RSS_r = sum((model_R\$residuals)^2)

[33]: RSS_r_new

1604.54526872071

[34]: RSS_r

1263.21423558875

Let's quickly do a model comparison between model_R_new and model_R. We have $\frac{(RSS_0-RSS_1)/(p-p_0)}{RSS_1/(n-p-1)} \sim F_{p-p_0,n-p-1}$, where the 0 subscripts refer to model_R_new.

We have rss_R_new = RSS_0 = 1604.54526872071 and rss_R =1263.21423558875 = RSS_1 . We also have p_0 = 1, p = 4 and n = 136. Computing our test stat, we have $\frac{(1604.54526872071-1263.21423558875)/(3)}{1263.21423558875/(136-4-1)}$ = -.6328. We have $F_{3,29}$, so we compute the test stat with $\alpha = 0.05$.

```
[35]: f_stat = ((RSS_r_new - RSS_r)/3)/(RSS_r/131)
```

[36]: f_stat

11.7990979097978

```
[37]: pf(11.799,3,29,lower = FALSE)
```

3.17290704084422e-05

We therefore reject the null, and believe that the relationship is better explained with the alternative model. Of course, I don't think we should use the alternative model. We will use the other one.

Let's get our predictions and replace the NA vals with them.

```
[38]: R_new_preds = predict(model_R_new, subset(R_na, select = -c(R.SCORE, ID.)) )
L_new_preds = predict(model_L_new, subset(L_na, select = -c(L.SCORE, ID.)))

##insert predicted values
R_na[,'R.SCORE'] = round(R_new_preds)
L_na[,'L.SCORE'] = round(L_new_preds)
#reset cleaned data variable
cleaned_read = k_read[complete.cases(k_read),]
#combine data frames
filled_read = rbind(cleaned_read, R_na)
filled_read = rbind(filled_read, L_na)
rownames(filled_read) <- 1:nrow(filled_read)</pre>
```

Alright, we'll use this one. I don't know how bad of practice it is to regress two variables on eachother, but this is better I believe than attempting to use DIEBLS to predict R.SCORE/L.SCORE."filled_read" is our new data frame with non-na values.

```
[39]: head(filled_read)
```

```
R.SCORE L.SCORE
                       ID.
                                                      DIEBLS INP
                                                                         FARM BIN
                        <int>
                               <dbl>
                                           <dbl>
                                                       <int>
                                                                 <int>
                                                                         <int>
                                           2
                                                       0
                                                                 1
                                                                         1
                       1
                               6
                       2
                                           3
                                                       0
                                                                 1
                               11
                                                                         1
A data.frame: 6 \times 6
                       3
                               7
                                                                         1
                                           5
                                                       0
                                                                 1
                    4
                       4
                               10
                                           5
                                                      0
                                                                 1
                                                                         1
                    5
                       6
                               0
                                           7
                                                      0
                                                                 1
                                                                         1
                    6 7
                               19
                                           7
                                                       0
                                                                 1
                                                                         1
```

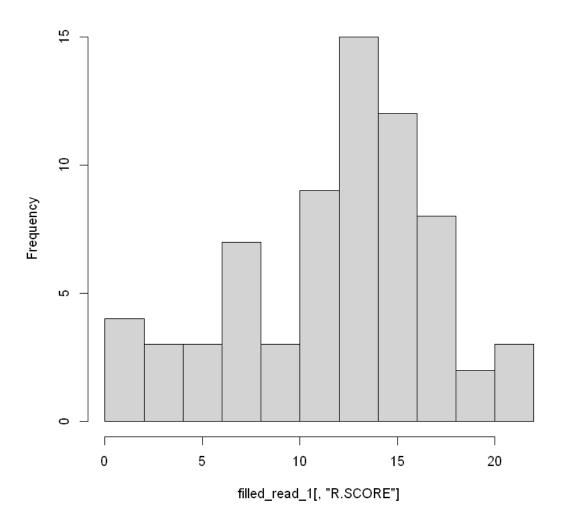
0.2 Check if there is any statistical difference between RScore LScore by group

```
[40]: ##using filled_read
filled_read_1 = filled_read[filled_read['INP']==1,]
filled_read_0 = filled_read[filled_read['INP']==0,]

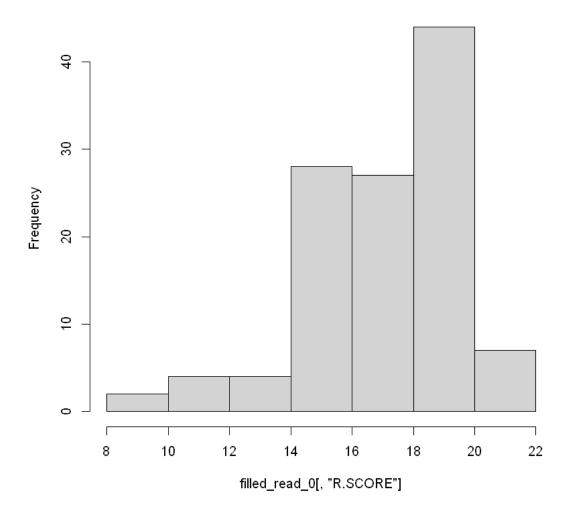
##check normality

hist(filled_read_1[,'R.SCORE'])
hist(filled_read_0[,'R.SCORE'])
hist(filled_read_1[,'L.SCORE'])
hist(filled_read_0[,'L.SCORE'])
```

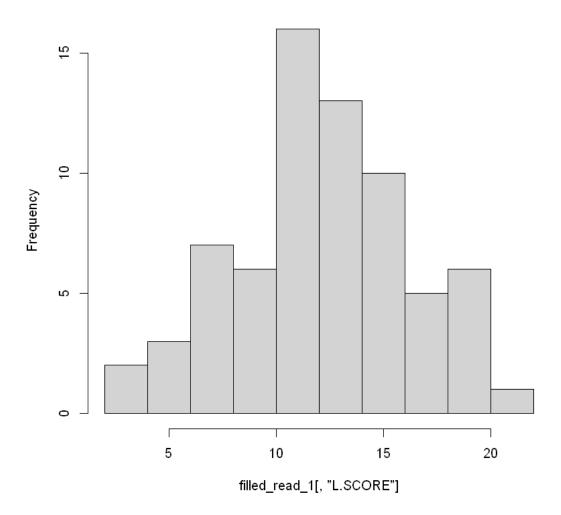
Histogram of filled_read_1[, "R.SCORE"]



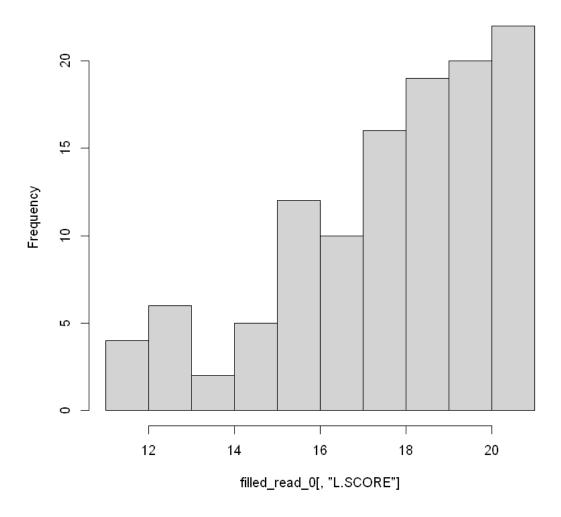
Histogram of filled_read_0[, "R.SCORE"]



Histogram of filled_read_1[, "L.SCORE"]



Histogram of filled_read_0[, "L.SCORE"]



All of these look approximately normal, except the last histogram. While it might be bad practice to run t-tests on the last one it's not a crazy assumption to believe that the reading scores of a pre-kindergarten population will be asymptotically normal

For the t-tests below, we have natural assumption that those with greater reading score belong in the group that don't find placement

```
[41]: t.test(filled_read_0[,'R.SCORE'],filled_read_1[,'R.SCORE'], alternative = 

→'greater')

t.test(filled_read_0[,'L.SCORE'], filled_read_1[,'L.SCORE'], alternative = 

→'greater')
```

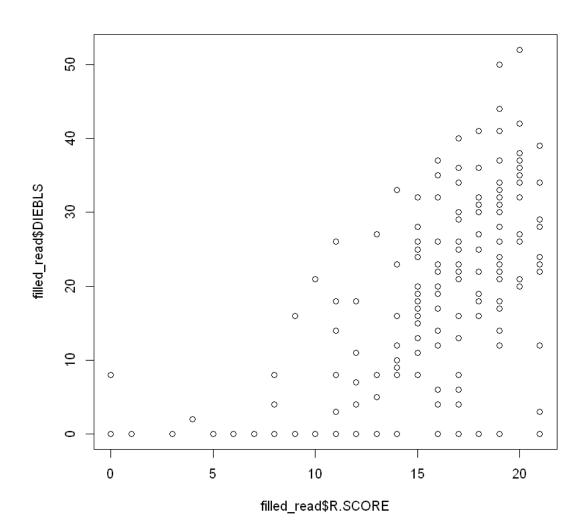
Welch Two Sample t-test

```
data: filled_read_0[, "R.SCORE"] and filled_read_1[, "R.SCORE"]
     t = 7.9135, df = 87.474, p-value = 3.597e-12
     alternative hypothesis: true difference in means is greater than 0
     95 percent confidence interval:
      4.136328
                    Tnf
     sample estimates:
     mean of x mean of y
      17.48276 12.24638
             Welch Two Sample t-test
     data: filled_read_0[, "L.SCORE"] and filled_read_1[, "L.SCORE"]
     t = 9.8546, df = 97.967, p-value < 2.2e-16
     alternative hypothesis: true difference in means is greater than 0
     95 percent confidence interval:
      4.563974
                    Tnf
     sample estimates:
     mean of x mean of y
      18.11207 12.62319
     With a 95% confidence level, in both, we have p-values which are significantly less than 0.05. We
     should expect good predictive power using R.SCORE and L.SCORE to predict DIEBLS.
[42]: wilcox.test(filled_read_0[,'R.SCORE'], y = filled_read_1[,'R.SCORE'],__
       →alternative = 'greater')
             Wilcoxon rank sum test with continuity correction
     data: filled_read_0[, "R.SCORE"] and filled_read_1[, "R.SCORE"]
     W = 6671.5, p-value = 1.332e-14
     alternative hypothesis: true location shift is greater than 0
[43]: wilcox.test(filled_read_0[,'L.SCORE'], filled_read_1[,'L.SCORE'], alternative = [
       Wilcoxon rank sum test with continuity correction
     data: filled_read_0[, "L.SCORE"] and filled_read_1[, "L.SCORE"]
     W = 6933.5, p-value < 2.2e-16
     alternative hypothesis: true location shift is greater than 0
```

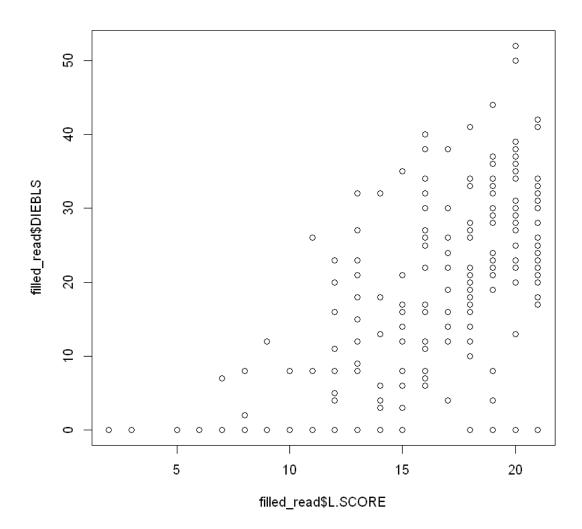
0.3 Model Selection

[46]: plot(filled_read\$R.SCORE, filled_read\$DIEBLS) #weak positive linear trend

→except for all the 0's



[47]: plot(filled_read\$L.SCORE, filled_read\$DIEBLS) #weak positive linear trend_
→except for the Os



0.3.1 Full model

Let's fit the full model first, using R.SCORE, L.SCORE, INP, and FARM_BIN, and see how good of covariates these are. Here, we are using "filled_read". First, remove the ID column and call this "features_full".

```
[48]: features_full= subset(filled_read, select = -c(ID.,INP)) ##create features_

→ matrix from filled_read

[49]: INP = filled_read$INP
```

We use the constants from earlier for the indices/sizes. We'll set a different seed though.

```
[50]: invisible(num_rows) ##CONSTANT
      set.seed(1) #different seed
      sampled_fill = sample(num_rows)
      invisible(test_size) ##CONSTANT
      invisible(train_size) ##CONSTANT
      train_index_fill = sampled_fill[1:train_size]
      test_index_fill = sampled_fill[(train_size + 1): nrow(cleaned_read)] ##CONSTANT
      train set fill = features full[train index fill,] #train and test sets
      test_set_fill = features_full[test_index_fill,]
[51]: filled_read[test_index_fill,]$INP
      1. \ 0 \ 2. \ 0 \ 3. \ 0 \ 4. \ 0 \ 5. \ 1 \ 6. \ 1 \ 7. \ 0 \ 8. \ 0 \ 9. \ 0 \ 10. \ 0 \ 11. \ 1 \ 12. \ 0 \ 13. \ 1 \ 14. \ 1 \ 15. \ 0 \ 16. \ 0 \ 17. \ 0 \ 18. \ 1 \ 19. \ 0
      20. \ 1\ 21.\ 0\ 22.\ 1\ 23.\ 1\ 24.\ 0\ 25.\ 1\ 26.\ 0\ 27.\ 1\ 28.\ 0\ 29.\ 1\ 30.\ 0\ 31.\ 0\ 32.\ 0\ 33.\ 0\ 34.\ 0
[53]: INP_train = filled_read[train_index_fill,]$INP
      INP_test = filled_read[test_index_fill,]$INP
      We have separated our train/test sets, so let's use CV to determine the validation errors of a full
      model first. We'll feed in both RSS and RSE as scoring metrics, setting a seed to maintain that
      we're getting the same folds.
[54]: full fit = lm(DIEBLS^{-}., train set fill, x = TRUE, y = TRUE)
[55]: cv_full_rsqd = cv.lm(full_fit, k = 5, fun = rsqd, seed = 23) ##set different_
       \hookrightarrow seed
[56]: cv_full_rse = cv.lm(full_fit, k = 5, fun = rse, seed = 23)
[57]: ##Mean R^2 is 45%! Not much variance explained.
      cv_full_rsqd
      Mean absolute error
                                        7.717329
      Sample standard deviation :
                                        0.8457575
      Mean squared error
                                        91.45073
      Sample standard deviation :
                                        18.81876
      Root mean squared error
                                        9.522736
      Sample standard deviation :
                                        0.9799461
```

: 0.4528572

User supplied function

Sample standard deviation : 0.112877

```
[58]: ##Mean RS is 9. Note great.
       cv_full_rse
      Mean absolute error
                                   : 7.717329
      Sample standard deviation :
                                      0.8457575
      Mean squared error
                                   : 91.45073
      Sample standard deviation : 18.81876
      Root mean squared error : 9.522736
      Sample standard deviation :
                                      0.9799461
      User supplied function
                                  : 10.31762
      Sample standard deviation :
                                      1.061745
      Let's predict on our test test, compute R<sup>2</sup>, RSS, RSE, MSE, and TSS.
[59]: preds full = predict(full_fit, subset(test_set_fill, select = -c(DIEBLS)))
       RSS_full = (preds_full -_
        →test_set_fill$DIEBLS)%*%(preds_full-test_set_fill$DIEBLS)
       TSS_full = (test_set_fill$DIEBLS -_
        →mean(test set fill$DIEBLS))%*%(test set fill$DIEBLS-___
        →mean(test_set_fill$DIEBLS))
       R2 \text{ full} = 1 - RSS \text{ full}/TSS \text{ full}
       RSE_full = sqrt(RSS_full/(length(preds_full) -__
        →length(coefficients(full_fit)-1)))
       MSE_full = RSS_full/length(preds_full)
[60]: full_fit_coef = coef(full_fit)
[61]: full_fit_coef
      (Intercept) -18.9131905525481 R.SCORE 1.15634799931682 L.SCORE 1.23235286333114
      FARM\_BIN
                                                 0.0171337679086991
[62]: full_stats = c(RSS_full, TSS_full, R2_full, RSE_full, MSE_full)
[63]: full stats ##R^2 on test set is 50%
      1.\,\,2860.47471980569\,\, 2.\,\,5824.5\,\, 3.\,\, 0.50888922314264\,\, 4.\,\, 9.76468931030867\,\, 5.\,\, 84.1316094060498
      After making our predictions, we now check if we accurately predicted the INP for students.
[151]: sum(as.integer(preds_full <= 13)) #how many did we enroll in extra help
[160]: inp_pred = as.integer(preds full <= 13) ##assign the binary vector of INP
```

```
[161]: INP_test #check the actual INP assignments
       1. \ 0 \ 2. \ 0 \ 3. \ 0 \ 4. \ 0 \ 5. \ 1 \ 6. \ 1 \ 7. \ 0 \ 8. \ 0 \ 9. \ 0 \ 10. \ 0 \ 11. \ 1 \ 12. \ 0 \ 13. \ 1 \ 14. \ 1 \ 15. \ 0 \ 16. \ 0 \ 17. \ 0 \ 18. \ 1 \ 19. \ 0
       20.\ 1\ 21.\ 0\ 22.\ 1\ 23.\ 1\ 24.\ 0\ 25.\ 1\ 26.\ 0\ 27.\ 1\ 28.\ 0\ 29.\ 1\ 30.\ 0\ 31.\ 0\ 32.\ 0\ 33.\ 0\ 34.\ 0
[162]: sum(as.integer(inp_pred == INP_test)) #how many did we assign correctly?
       29
[163]: 29/34 #what is our percentage?
       0.852941176470588
[136]: preds_full
                                                                                25.2569067423406 11
       92 24.0245538790094 146 26.4132547416574 112
                                                         24.0245538790094 62
                                                                                27.7216124690029 97
       7.21050920855075 57
                               15.6849695238401 66
                                                       22.8682058796926 130
       26.565264469686 91
                               22.7750672477696 30
                                                       23.8725441509808 114
                                                                                 28.9368315644253 8
       7.15163811244513 9
                             6.07129497714263 128
                                                      25.3329116063549 155
                                                                              26.5481307017773 157
       23.0202156077213 5
                              -10.2695867413215 95
                                                       24.1765636070381 32
                                                                                15.5500935637201 96
       28.8019556043054 50
                                9.76835356713604 12
                                                        -6.57252815132806 88
                                                                                 22.9442107437069 4
                                23.0202156077213 38
                                                        19.2300183858048 63
       -1.17081247481555 94
                                                                                14.4526166605089 56
       21.7878627443901 170
                               28.8779604683197 117
                                                       21.6358530163615 71
                                                                              19.3060232498192 136
                                                        18.0908041543967
       16.8413175231569 152
       0.3.2 Ridge
       Next, let's use lasso and ridge models to penalize some of the covariates. First, ridge.
[166]: lambdas = 10^seq(6, -6, by = -.1)
       set.seed(0)
       ridge_cv = cv.glmnet(as.matrix(subset(train_set_fill, select = -c(DIEBLS))), as.
         →matrix(train_set_fill$DIEBLS), alpha = 0, lambda = lambdas)
[167]: ridge_cv$lambda.min
       1
[168]: set.seed(0)
       ridge_fit <- glmnet(as.matrix(subset(train_set_fill, select = -c(DIEBLS))),as.
         →matrix(train_set_fill$DIEBLS), alpha = 0, lambda = ridge_cv$lambda.min)
[169]: #Get RSS
[170]: rid_fit_coef = coef(ridge_fit)
       Let's compute R^2, RSS, RSE, MSE, TSS.
[171]: preds ridge = predict(ridge_fit, as.matrix(subset(test_set_fill, select = ___
```

```
RSS_rid = (as.vector(preds_ridge) - test_set_fill$DIEBLS)%*%(as.
        →vector(preds_ridge)-test_set_fill$DIEBLS)
       TSS_rid = (test_set_fill$DIEBLS -_
        →mean(test set fill$DIEBLS))%*%(test set fill$DIEBLS-___
        →mean(test_set_fill$DIEBLS))
       R2_rid = 1 - RSS_rid/TSS_rid
       RSE_rid = sqrt(RSS_rid/(length(preds_ridge)-length(coefficients(ridge_fit)-1)))
       MSE_rid = RSS_rid/length(preds_ridge)
[172]: ridge_stats = c(RSS rid, TSS rid, R2 rid, RSE rid, MSE rid)
[173]: ridge_stats ##R^2 51%
      1.\,\, 2853.04153276127\,\, 2.\,\, 5824.5\,\, 3.\,\, 0.510165416299893\,\, 4.\,\, 9.75199386922366\,\, 5.\,\, 83.9129862576845
[178]: sum(as.integer(preds ridge <= 13))
      7
[180]: inp_pred_ridge = as.integer(preds_ridge <= 13) #assign binary vector for INP
[183]: sum(as.integer(inp_pred_ridge == INP_test)) #how many did we get correct
      29
[182]: 29/34 #correct percentage
      0.852941176470588
[184]: as.integer(preds_ridge <= 13) == as.integer(preds_full <= 13) ##same_u
        \rightarrowpredictions as the full model
      1. TRUE 2. TRUE 3. TRUE 4. TRUE 5. TRUE 6. TRUE 7. TRUE 8. TRUE 9. TRUE 10. TRUE
      11. TRUE 12. TRUE 13. TRUE 14. TRUE 15. TRUE 16. TRUE 17. TRUE 18. TRUE 19. TRUE
      20. TRUE 21. TRUE 22. TRUE 23. TRUE 24. TRUE 25. TRUE 26. TRUE 27. TRUE 28. TRUE
      29. TRUE 30. TRUE 31. TRUE 32. TRUE 33. TRUE 34. TRUE
[186]: preds_ridge #our DIEBLS predictions
```

```
s0
                                    23.6559324
                               92
                              146
                                    25.9229901
                              112
                                    23.6559324
                               62
                                    24.8271193
                                    7.9730247
                               11
                               57
                                    16.0207005
                               66
                                    22.5600617
                              130
                                    27.1694930
                               97
                                    26.0736223
                               91
                                    22.7465573
                               30
                                    23.5053002
                              114
                                    28.6024916
                                8
                                    7.6358969
                                9
                                    6.6153422
                              128
                                    24.9024354
                              155
                                    26.3354340
A matrix: 34 \times 1 of type dbl
                              157
                                    22.7106939
                                    -8.8774806
                                5
                               95
                                    23.8065646
                               32
                                    15.6082566
                               96
                                    28.1900477
                               50
                                    10.1289028
                               12
                                    -5.3639201
                               88
                                    22.6353778
                                4
                                    -0.2611468
                               94
                                    22.7106939
                               38
                                    19.3836289
                               63
                                    14.8495137
                               56
                                    21.5395070
                                    28.2653638
                              170
                              117
                                    21.3888748
                               71
                                    19.4589450
                              136
                                    17.1165713
                              152
                                    18.0259464
```

0.3.3 LASSO

Let's run a LASSO model. It will be interesting to see if it reduces FARM to 0 for later analysis when we do model accuracy tests.

```
[187]: lambdas = 10^seq(6, -6, by = -.1) ##same lambdas
set.seed(0) ##same seed
lasso_cv = cv.glmnet(as.matrix(subset(train_set_fill, select = -c(DIEBLS))), as.

-matrix(train_set_fill$DIEBLS), alpha = 1, lambda = lambdas)
```

0.398107170553497

[188]: lasso_cv\$lambda.min

```
[189]: set.seed(0)
       lasso_fit = glmnet(as.matrix(subset(train_set_fill, select = -c(DIEBLS))),as.
        →matrix(train_set_fill$DIEBLS), alpha = 1, lambda = lasso_cv$lambda.min)
[190]: ## GEt RSS/RSE
[191]: lass_fit_coef = coef(lasso_fit)
[192]: lass_fit_coef #FARM reduced to 0
      4 x 1 sparse Matrix of class "dgCMatrix"
      (Intercept) -17.022647
      R.SCORE
                     1.098742
      L.SCORE
                     1.172488
      FARM_BIN
[193]: preds_lasso = predict(lasso_fit, as.matrix(subset(test_set_fill, select = ___
       →-c(DIEBLS))))
       RSS_las = (as.vector(preds_lasso) - test_set_fill$DIEBLS)%*%(as.
       →vector(preds lasso)-test set fill$DIEBLS)
       TSS_las = (test_set_fill$DIEBLS -_
       →mean(test_set_fill$DIEBLS))%*%(test_set_fill$DIEBLS-__
       →mean(test_set_fill$DIEBLS))
       R2 las= 1 - RSS las/TSS las
       RSE_las = sqrt(RSS_las/(length(preds_lasso)-length(coefficients(lasso_fit)-1)))
       MSE_las = RSS_las/length(preds_lasso)
[194]: lasso_stats = c(RSS_las, TSS_las, R2_las, RSE_las, MSE_las)
[195]: lasso_stats ##R2 still around 51%
      1.\ \ 2851.53438818623\ \ 2.\ 5824.5\ \ 3.\ \ 0.510424175777109\ \ 4.\ \ 9.74941774019733\ \ 5.\ \ 83.8686584760656
      0.3.4 Test Results
      Create a results data frame for all test scores
[196]: results = data.frame(full_stats, ridge_stats, lasso_stats)
[197]: rownames(results) <- c("RSS", "TSS", "R2", "RSE", "MSE")
[198]: results ##super similar (TSS is obviously the same for all), although the R2,
        →MSE, RSS, RSE are just marginally better
```

		full_stats	$ridge_stats$	lasso_stats
		<dbl></dbl>	<dbl></dbl>	<dbl $>$
	RSS	2860.4747198	2853.0415328	2851.5343882
A data.frame: 5×3	TSS	5824.5000000	5824.5000000	5824.5000000
	R2	0.5088892	0.5101654	0.5104242
	RSE	9.7646893	9.7519939	9.7494177
	MSE	84.1316094	83.9129863	83.8686585

Create data frame with all coefficients

 $colnames(results) = c("full", "ridge", "lasso") \ rownames(results) = c("Int", "RSCORE", 'LSCORE', 'FARMBIN')$

[200]: results

	as.vector.full_fit_coef.	$as.vector.rid_fit_coef.$	as.vector.lass_fit_coef.
A data.frame: 4×3	<dbl></dbl>	<dbl></dbl>	<dbl></dbl>
	-18.91319055	-16.8139770	-17.022647
	1.15634800	1.0958708	1.098742
	1.23235286	1.1711869	1.172488
	0.01713377	-0.2618117	0.000000

0.3.5 Testing on Marginal Effect/Model Accuracy for FARM

We already know LASSO reduced FARM to 0. Our test on marginal effect can be found in summary tables. We can then compared accuracy between models within full/ridge. If we were to compute marginal manually for both models, our hypotheses are as follows:

```
H_0: \beta_{FARM} = 0 versus H_1: \beta_{FARM} \neq 0.
```

For full model, we have $\hat{\sigma} = RSE_{full} = 9.4546198$ and for ridge model, we have $\hat{\sigma} = RSE_{ridge} = 9.4423275$. In both cases, we need to compute $\sqrt{\nu_j}$ which is the third diagonal entry in $(X^TX)^{-1}$, our train features matrix with added intercept. Our test statistic for both models will be $t = \frac{\hat{\beta}_{FARM}}{\sqrt{\nu_{FARM}RSE}} \sim t_{n-p-1} = t_{136-3-1} = t_{132}$. But instead of doing this for the full, we can use summary.

[201]: summary(full_fit)

Call:

lm(formula = DIEBLS ~ ., data = train_set_fill, x = TRUE, y = TRUE)

Residuals:

Coefficients:

Estimate Std. Error t value Pr(>|t|)

```
(Intercept) -18.91319
                        4.01468 -4.711 6.16e-06 ***
R.SCORE
             1.15635
                        0.23264
                                  4.971 2.03e-06 ***
                                  5.223 6.69e-07 ***
L.SCORE
             1.23235
                        0.23597
             0.01713
                        1.70673
                                  0.010
                                          0.992
FARM_BIN
Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
```

Residual standard error: 9.342 on 132 degrees of freedom Multiple R-squared: 0.496, Adjusted R-squared: 0.4846

F-statistic: 43.31 on 3 and 132 DF, p-value: < 2.2e-16

Since .992 > .05 we fail the reject the hypothesis that FARMBIN is 0. Let's now compute the test stat for ridge.

```
[202]: features = subset(train_set_fill, select = -c(DIEBLS))
[203]: features_inter = cbind(intercept = rep(1,136), features)
[204]: solve(as.matrix(t(features_inter))%*%as.matrix(features_inter))
```

		intercept	R.SCORE	L.SCORE	FARM_BIN
	intercept	0.184664153	-0.0045825060	-0.0051293269	-0.0397955442
A matrix: 4×4 of type dbl	R.SCORE	-0.004582506	0.0006200687	-0.0003491395	0.0010932296
	L.SCORE	-0.005129327	-0.0003491395	0.0006379494	0.0002767817
	FARM_BIN	-0.039795544	0.0010932296	0.0002767817	0.0333741279

We retrieve the 3rd diagonal (0-3 indexing). And so we have $\nu_{FARM} = 0.0333741279$.

For the ridge model:

```
[207]: t = (-0.2618117)/(sqrt(0.0333741279)*RSE_rid)

[208]: pt(-.153224, 132)
```

0.439227809270612

We fail to reject the hypothesis that FARM is 0.

0.3.6 Next we compare accuracy of models on training using F-test.

Really, we should only do this for the full model, since both ridge and lasso penalize coefficients to reduce error. We already have the full model (full_fit). Let's train another model without using FARM.

11521.0642338322

[180]: fit_full = lm(DIEBLS~., train_set_fill, x = TRUE, y = TRUE)

[181]: rss_full = sum((residuals(fit_full))^2)

[182]: rss_full

11521.0554376173

[183]: # follows $f_{-}(p-po,n-p-1) = f_{-}(1,132)$ distribution F = (rss_no_farm - rss_full)/(rss_full/(132))

[185]: qf(.025,1,132, lower = TRUE)

0.000985799773244089

We keep FARM BIN and REJECT the null, since .0001 < .000985.

[186]: anova(fit_no_farm, fit_full)

Res.Df RSS Df Sum of Sq \mathbf{F} Pr(>F)<dbl> <dbl><dbl><dbl><dbl><dbl>A anova: 2×6 133 11521.06 NA NANANA132 11521.06 0.0087962150.00010078070.99200541