ETHIO NATIONAL SCHOOL

MATHEMATICS NATIONAL EXAM (EUEE) QUESTIONS FROM 2004 – 2011 E.C

COMPILED BY MR. SHISHAY

From grade 11

Unit 1 and 2

1. If x < 0, then the simplest form of $f(x) = \frac{x - |x|}{x}$ is equal to:

D. 0

2. If $f(x) = \frac{\sqrt{x+2}}{x+2}$ and $g(x) = \frac{1}{x} - 2$, then f(g(x)) is equal to?

A. $\sqrt{x}-2$

B. $\sqrt{x} + 2$

3. If $f(x) = \ln\left(\frac{x}{x-1} + 2\right)$, for x > 1, then which of the following is the inverse of f?

A. $g(x) = \frac{e^x - 2}{e^x - 3}$ B. $g(x) = \frac{e^x - 2}{e^x + 1}$ C. $g(x) = \frac{e^x}{e^x + 1} - 2$ D. $g(x) = e^{\frac{x}{x - 1} - 2}$

4. Which of the following is a simplified form of $\frac{4-(a-2)^2}{a^4+2a^2+1} \div \frac{1-\frac{1}{a^2+1}}{a}$?

A. $\frac{4-a}{a}$ B. $-\frac{a}{a^2+1}$ C. $-\frac{1}{a^2(a^2+1)}$ D. $\frac{4-a}{a^2+1}$

5. If $(x) = \frac{x-1}{(x-2)^2(x+1)}$, which of the following is true about f?

A. Its graph has an oblique asymptote. C. The graph of f does not meet its asymptote.

D. As $x \rightarrow 2^-$, $f(x) \rightarrow -\infty$

B. As $x \to -1^+$, $f(x) \to -\infty$.

6. What is the value of |x| + 2x if x < 0?

A. -3x

C. - x

D. x

7. Which of the following functions has **No** vertical asymptote?

 $A. f(x) = \ln(x+1)$

C. $f(x) = \frac{x^2 - 9}{x - 3}$

B. $f(x) = \frac{x^2+1}{x^3+8}$

D. $f(x) = \frac{x-1}{x^2-x}$

8. If $f(x) = \frac{1}{e^{x+1}}$, then which of the following is equal to $f^{-1}(x)$?

A. $\ln(1-x) - \ln(x)$

C. $\ln\left(\frac{1}{x+1}\right)$

B. $e^{-x} + 1$

D. $\frac{1}{e^{-x+1}}$

9. What is the solution set of $\frac{2}{x} - \frac{x-2}{x^2 - 2x} = 1 - \frac{2x-2}{3x-2}$?

D. {1}

10. Given $f(x) = \ln(x-1)$ and $g(x) = \sqrt{1-2x}$, which one of the following is the domain of $f \circ g$?

A. $\{x \in \Re: x > 1\}$

C. $\{x \in \Re: x < 0\}$

B. $\left\{x \in \Re: x \leq \frac{1}{2}\right\}$

D. $\{x \in \Re: x > \frac{1}{2}\}$

11. Which of the following is expression is a polynomial expression?

A. $x^2 - 3x + \sin x$

B. $\frac{4x^3+12x^2-x}{-x^2}$

D. $2 - 3x^{\frac{2}{3}} + 7x^{\frac{5}{2}} + 3x^{-1}$

12. If $f(x) = \frac{x+1}{x-1}$ and f(a) = 5, then f(2a) is equal to:

13. If $f(x) = \sqrt[3]{1 + e^{-x}}$, which of the following is equal to $f^{-1}(x)$?

A. $\ln\left(\frac{1}{x^3-1}\right)$

C. $\ln(1 - x^3)$

D. $(1 + e^{-x})^3$

14. Which one of the following is true?

A. A polynomial can have infinitely many vertical asymptotes.

B. The graph of a rational function can never cross its horizontal asymptote?

- C. The graph of $f(x) = \frac{3x-1}{x-1}$ has no horizontal asymptote.
- D. The graph of $f(x) = \frac{x^3 x}{x^2 x}$ has no vertical asymptote.
- 15. Which of the following is true about the graph of $f(x) = \frac{x^2-1}{x-x^2}$?
 - A. x = 0 and x = 1 are its vertical asymptotes
 - B. y=1 is its horizontal asymptote.
 - C. y = x 1 is its oblique asymptote.
 - D. It is almost the same as the horizontal line y = -1 as $x \to \pm \infty$.
- 16. Which one of the following functions is one-to-one correspondence?
 - A. $f: \Re' \to \Re$, $f(x) = \tan x$, where \Re' is the domain of f.
 - B. $g: \Re \to \Re, g(x) = 2^x$
 - C. $h:[0,\infty) \to [0,\infty), h(x) = x^2$
 - D. $r: [0, \infty) \to [0, \infty), r(x) = x + 5$
- 17. The inverse of the function defined by $g(x) = \frac{2x}{x+3}$ is equal to:

A.
$$g^{-1}(x) = -\frac{2x}{x-3}$$

C.
$$g^{-1}(x) = -\frac{x+3}{2x}$$

D. $g^{-1}(x) = \frac{x+2}{3x}$

B.
$$g^{-1}(x) = -\frac{3x}{x-2}$$

D.
$$g^{-1}(x) = \frac{x+2}{3x}$$

18. If $p(x) = 3x^2$ and $q(x) = x^2 + x$, then what is the solution set of $\frac{p(x)}{3q(x)} - \frac{1}{x} = \frac{1}{q(x)}$?

A.
$$\{-1, 2\}$$

C.
$$\{-3, 2\}$$

19. The value(s) of x where the graph of the function $y = \frac{x^2 - 1}{x^3}$ crosses its horizontal asymptote is(are):

A.
$$x = -2$$

C.
$$x = 0$$

B.
$$x = -1$$
 and $x = 1$

D.
$$x = -\sqrt{2} \text{ and } x = 1 + \sqrt{2}$$

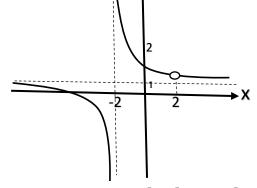
20. Which of the following functions could most likely be drawn as in the figure below?

A.
$$f(x) = \frac{x+3}{x+2}$$

B.
$$f(x) = \frac{x^2 - 2x}{x^2 - 4}$$

C.
$$f(x) = \frac{-x^2 - x + 6}{x^2 - 4}$$

D.
$$f(x) = \frac{x^2 + x - 6}{x^2 - 4}$$



21. Which of the following is one-to-one correspondence function from A = [0, 1] to B = [1, 2]?

A.
$$f(x) = x$$

C.
$$f(x) = 2x + 1$$

B.
$$f(x) = \frac{1}{3}x^3 + 1$$

D.
$$f(x) = x^2 + 1$$

22. What is the solution set of $\frac{1-\frac{1}{x}}{1-\frac{1}{x^2}} = 3x^2 - \frac{x}{1+\frac{1}{x}}$?

A.
$$\{-1,\frac{1}{2}\}$$

B.
$$\left\{\frac{1}{2}\right\}$$

A.
$$\left\{-1, \frac{1}{3}\right\}$$
 B. $\left\{\frac{1}{3}\right\}$ C. $\left\{3, \frac{-1}{3}\right\}$ D. $\left\{\frac{-1}{3}\right\}$

D.
$$\left\{ \frac{-1}{2} \right\}$$

- 23. Suppose $f(x) = \frac{Q(x)}{x(x^2-1)}$ where Q(x) is a quadratic function. Which of the following is necessarily true about the graph of f?
 - A. x = 0, x = 1 and x = -1 are the vertical asymptotes of the graph of f.
 - B. The graph of f does not intersect with its horizontal asymptote.
 - C. The vertical asymptote of the graph of f is only x = -1 if $Q(x) = x^2 x$.
 - D. The vertical asymptote of the graph of f is only x = 1 if $Q(x) = 2x^2$.
- 24. Which one of the following is true about the horizontal asymptote(s) of the graphs of $y = \frac{|x|+2}{x}$?
 - A. y = 2 is the only horizontal asymptote of the graph.

B. y = 1 and y = -1 are horizontal asymptotes of the graph.

C. y = 2 and y = -2 are horizontal asymptotes of the graph.

D. y = 1 is the only horizontal asymptote of the graph.

25. If $f: A \to B$ and $g: B \to C$ are functions, then which one of the following is true about the composition function?

A. Domain of $(g \circ f) \subseteq Domain \circ f$

C. Domain of $(gof) \nsubseteq Domain of f$

B. Range of $(g \circ f) \nsubseteq Range \circ f g$

D. Range of $(gof) \subseteq Range$ of f

26. If the point (3, -2) is on the graph of y = f(x), which point is on the graph of $y = f^{-1}(x)$?

A.
$$(\frac{1}{3}, -2)$$

B. (3,-1) C. (-2,3)

D. $(3, -\frac{1}{2})$

27. Which one of the following is true about the graph of $f(x) = \frac{x^3 - x}{x^3(x-1)}$?

A. The vertical asymptotes of the graph are x = 0 and x = 1.

B. The horizontal asymptote of the graph is y = 1.

C. The graph intersects its horizontal asymptote at the point (-1,0).

D. The graph intersects the vertical line x = 1 at the point (1, 2)

28. What is the solution set of $\frac{1}{1+\frac{1}{x}} - \frac{1}{1-\frac{1}{x}} = \frac{x+\frac{1}{x}}{x-\frac{1}{x}}$?

A. {}

B. $\{-1\}$

D. $\{-1,1\}$

29. Which of the following is the inverse of $f(x) = 8x^3 + 2$?

A.
$$f^{-1}(x) = \frac{1}{8x^3 + 2}$$

C.
$$f^{-1}(x) = 8x^{-3} - 2$$

B.
$$f^{-1}(x) = \frac{1}{2} \sqrt[3]{x-2}$$

D.
$$f^{-1}(x) = \frac{1}{8}\sqrt[3]{x-2}$$

30. If $f(x) = \sqrt{x^3}$ and $(f \circ g)(x) = \sqrt[4]{x}$, then what is the value of g(8)?

A. $\sqrt[3]{2}$

B. 2

C. $\sqrt{2}$

31. Which of the following functions is one-to-one correspondence?

A. $f:[0,\infty)\to\Re$ defined by f(x)=|x|. C. $f:\Re\to[0,\infty)$ defined by $f(x)=3^x$

B. $f: \mathbb{R} \to [0, \infty)$ defined by $f(x) = x^2$

D. $f:(0,\infty)\to\Re$ defined by $f(x)=\log_2 x$

32. Which of the following is true about signum, absolute value and greatest integer functions?

A. $sgn(x) = \pm |x|$, for all $x \in \mathbb{R}$.

C. |x| = x sgn(x), for all $x \in \mathbb{R}$.

B. $sgn(x) \le \lfloor x \rfloor$, for all $x \le 0$

D. $sgn(x) \le \lfloor x \rfloor$, for all $x \ge 0$

33. What is the partial fraction decomposition of $\frac{x^2+x+1}{(x+2)(x^2+1)}$?

A.
$$\frac{3}{5(x+2)} + \frac{2x+1}{5(x^2+1)}$$

C.
$$\frac{2}{5(x+2)} + \frac{3x+1}{5(x^2+1)}$$

B.
$$\frac{5}{3(x+2)} + \frac{2x+1}{3(x^2+1)}$$

D.
$$\frac{2}{3(x+2)} + \frac{2x+1}{3(x^2+1)}$$

34. Which of the following is true about the graph of $f(x) = \frac{2x^3 + 2x^2 + 3x}{x^2 + x}$?

A. The vertical asymptote of the graph is only x = -1 and its oblique asymptote is y = 2x.

B. The graph has y-intercept at (0, 3).

C. The graph has at least one x-intercept.

D. The vertical asymptotes of the graphs are at x = 0 and x = -1 but it has no vertical asymptote.

35. Let $f(x) = x - x^2$ and $g(x) = \frac{1}{x}$. Then $g(f(\frac{1}{x}))$ is equal to:

A.
$$x - x^2$$

C. $\frac{1}{x^2-1}$

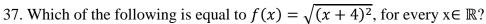
D. $\frac{x-1}{x^2}$

36. Let $f(x) = \frac{3x+1}{x-2}$. Then what is the range of f(x)?

A. $\mathbb{R}\setminus\{2\}$

B. ℝ

C. $\mathbb{R}\setminus\{3\}$ D. $\mathbb{R}\setminus\left\{\frac{-1}{3}\right\}$



A.
$$g(x) = x + 4$$

C.
$$g(x) = |x + 4|$$

B.
$$g(x) = x + 2$$

D.
$$g(x) = |x| + 4$$

38. What is the simplified form of
$$\frac{a^{-1}b^{-1}}{a^{-3}-b^{-3}}$$
?

A.
$$\frac{a^2b^2}{b^2-a^2}$$

C.
$$\frac{a^3-b^3}{ab}$$

B.
$$\frac{a^2b^2}{b^3-a^3}$$

$$D. \frac{a^3 - b^3}{a - b}$$

39. If f(x) = ax - b and $f^{-1}(x+1) = \frac{1}{2}x + 2$, for each $x \in \Re$, then what must be the value of a and b?

A.
$$a = \frac{1}{2}, b = -2$$

C.
$$a = 1, b = 1$$

B.
$$a = 2, b = 2$$

D.
$$a = 2, b = 3$$

40. Which of the following is true about the graph of $f(x) = \frac{x^2 + 5x + 6}{x^2 + 6} + 3$?

- A. The graph has a hole at x = 2.
- B. The vertical asymptotes of the graph are x = 2 and x = -2.
- C. The horizontal asymptote of the graph is y = 4.
- D. The graph has y-intercept at $\left(0, -\frac{3}{2}\right)$.

41. If f is greatest integer function and g is absolute value function, then what is the value of

$$((fog)\left(\frac{3}{2}\right) + (gof)\left(-\frac{4}{3}\right)?$$

C. -1

D. 2

42. A line ℓ passes through (0, 5) and (-5, 0). What is the acute angle between the y-axis and the line ℓ in radian measure?

A.
$$\frac{\pi}{4}$$

B.
$$\frac{\pi}{3}$$

$$C.\frac{\pi}{2}$$

A. $\frac{\pi}{4}$ B. $\frac{\pi}{3}$ C. $\frac{\pi}{2}$ D. $\frac{3\pi}{4}$ 43. Consider a circle whose center is on the x –axis. If a line given by y=x is tangent to the circle at the point (2, 2), what the equation of the circle?

A.
$$x^2 + y^2 = 8$$

C.
$$(x-4)^2 + y^2 = 8$$

B.
$$(x-2)^2 + y^2 = 4$$

D.
$$(x-1)^2 + y^2 = 5$$

44. What is the vertex and the equation of the directricx, respectively, of the parabola $x + y^2 + 2y + 1 = 0$?

A.
$$(0, -1)$$
, $x = \frac{-1}{4}$
B. $(-1, 0)$, $y = \frac{-1}{4}$

C.
$$(0, -1)$$
, $x = \frac{1}{4}$

B.
$$(-1, 0)$$
, $y = \frac{-1}{4}$

D.
$$(-1, 0)$$
, $y = \frac{1}{4}$

45. The orbit of Mercury around the sun forms an ellipse with eccentricity 0.206, length of major axis 1.16×10^8 km and the sun at one focus. Which of the following is the best approximation of the maximum distance from Mercury to the sun?

A.
$$7.596 \times 10^7 \text{km}$$

C.
$$8.695 \times 10^7 \text{km}$$

B.
$$5.695 \times 10^{-7}$$
 km

D.
$$6.995 \times 10^7 \text{km}$$

46. If $x^2 - 6x + y^2 + k = 0$ is equation of a circle with radius 2, then what is the value of k?

47. If a line with angle of inclination of $\frac{3\pi}{4}$ passes through (0. 1), which one of the following is the equation of the line?

A.
$$y = -x + 1$$

B.
$$y = x + 1$$

$$C.y = -x - 1$$

0.
$$v = x - 1$$

48. A parabola with focus at (3, -1) has directrix y = 3, which one of the following is the equation of the parabola?

A.
$$(X-3)^2 = -4(Y+1)$$

C.
$$(X-3)^2 = 4(Y+1)$$

B.
$$(X-3)^2 = -8(Y-1)$$

D.
$$(X-3)^2 = 8(Y-1)$$

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49. A satellite moves along a hyperbolic curve whose horizontal transverse axis is 24 km and an asymptote $y = \frac{5}{12}x + 2$. what is the eccentricity of the hyperbola?

50. For what value of b does the parabola $p(x) = ax^2 + x + b$ passes through the points (-1,5) and (2,-1)?

A. 9

B. 3

C. -3

51. What is the equation of the direcrix for the parabola whose equation is $y^2 + 8x + 6y + 25 = 0$?

B. x = 0

C.x = 2

52. If two lines y = x and y = x - 4 are tangent to a circle at (2, 2) and (4, 0), respectively, then what is the equation of the circle?

A. $(x-2)^2 + y^2 = 4$

C. $(x-3)^2 + (y-1)^2 = 2$

B. $(x-4)^2 + (y-2)^2 = 4$

D. $(x-1)^2 + (y+1)^2 = 10$

53. A semi elliptical arc over a tunnel for a road through a mountain has a major axis of length 80 m and height of 30 m at the center. What is the equation of the semi-elliptical arc over the tunnel, if the center is considered as the origin?

- A. $\frac{X^2}{6400} + \frac{Y^2}{900} = 1$ B. $\frac{X^2}{1600} + \frac{Y^2}{900} = 1$ C. $\frac{X^2}{900} + \frac{Y^2}{6400} = 1$ D. $\frac{X^2}{6400} + \frac{Y^2}{8100} = 1$ 54. Let the equation $x^2 + 2x + y^2 = 8$ represents a circle. Then which one of the following lines cut the circle at exactly two points?

A. 4x + 3y + 19 = 0

C. 2v = 5x + 43

B. 3x + 4y + 14 = 0

- D. 2x = y 50
- 55. If the equation $(x-2)^2 (y-2)^2 = 1$ represents a hyperbola, which one of the following represents the equation of an asymptote of the hyperbola?

A. y = 4 - x

B. x + y = 1

C. x = 2 - y

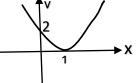
D. x + 2y = 3

56. Which of the equations below is represented by the following parabola?

A. $y = x^2 + 2$

B. $v = (2x - 1)^2$

C. $y = 2(x - 1)^2$ D. $y = (2x + 1)^2$



57. The equation of an ellipse with center at (1, 4) and vertices at (10, 4) and (1, 2) is:

A. $4(x-1)^2 + 8\overline{1}(y-4)^2 = 324$

C. $9(x-1)^2 + 4(y-4)^2 = 1$

B. $(x-1)^2 + 9(y-4)^2 = 4$

- D. $2(x-1)^2 + 9(y-4)^2 = 4$
- 58. What is the focus of the parabola $y^2 + 4y + 8x = 4$?

A. (1, -2)

B. (-1, -2)

C. (3, -2)

59. Two perpendicular lines l_1 and l_2 are intersecting at (-1, 2). If the angle of inclination of l_1 is 45^0 then what is the equation of l_2 ?

A. y = -x + 3

B. y = x + 3

C. y = -x + 1

- 60. Which of the following is true about a conic section represented by the equation $\frac{x^2}{\nu} + \frac{y^2}{\nu o} = 1$?
 - A. it is a circle whose center is at the origin for some $k \in \mathbb{R}$.
 - B. It is an ellipse whose major axis is vertical when k > 9.
 - C. it is a hyperbola whose foci are at (-3, 0) and (3, 0) when 0 < k < 9.
 - D. It is a hyperbola whose foci are (-3k, 0) and (3k, 0) when 0 < k < 9.

61. The planet Mercury's orbit around the sun is an ellipse with eccentricity 0.206, length of major axis 11.6×10⁸ km and the sun at one focus. What is the maximum distance from Mercury to the sun?

- A. 6.99×10^{8}
- . B. 6.99×10^7
- C. 9.66×10^7
- D. 9.66×10^8
- 62. The equation of the line that passes through (2, -1) and is perpendicular to 3x + 4y = 6 is:

A. -4x + 3y = 5

C. 4x + 3y = 11

B. 4x - 3y = 5

D. -4x + 3y = -11

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63. Which one of the following is the equation of a circle whose center is on the y-axis and radius 3?

$$A.x^2 + y^2 + 6y = 0$$

C.
$$x^2 + (y-2)^2 = 3$$

B.
$$(x-2)^2 + y^2 = 9$$

D.
$$x^2 - 2x + y^2 = 8$$

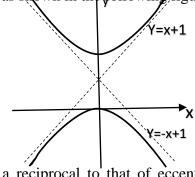
64. The graph of a hyperbola and the lines of its asymptotes are as shown in the following figure. Which one of the following is an equation of the hyperbola?

A.
$$y^2 - 2y - x^2 = 0$$

B.
$$y^2 - 3y - x^2 = 0$$

$$C.x^2 - (y-1)^2 = 1$$

D.
$$(x-1)^2 - y^2 = 1$$



65. Suppose the eccentricity of the hyperbola $\frac{x^2}{a^2} - \frac{y^2}{b^2} = 1$ is a reciprocal to that of eccentricity of the ellipse $x^2 + 4y^2 = 4$. If the hyperbola passes through a focus of the ellipse, then what is the equation of the hyperbola?

A.
$$x^2 - 2y^2 = 2$$

B.
$$x^2 - 3y^2 = 3$$

A.
$$x^2 - 2y^2 = 2$$
 B. $x^2 - 3y^2 = 3$ C. $\frac{x^2}{3} - \frac{y^2}{2} = 1$ D. $\frac{x^2}{2} - \frac{y^2}{3} = 1$

D.
$$\frac{x^2}{2} - \frac{y^2}{3} = 1$$

66. What is the radius of the largest possible circle that can be inscribed in the ellipse given by 5(x - $(1)^2 + 3y^2 = 15$?

A.
$$\sqrt{3}$$

B.
$$\sqrt{5}$$

67. What are the values of the center (C) and radius (r) of the circle $x^2 + y^2 - 4x + 6y = 5$?

A.
$$C = (-2,3), r = 3\sqrt{2}$$

C.
$$C = (2, -3), r = 2\sqrt{3}$$

B.
$$C = (2, -3), r = 3\sqrt{2}$$

D.
$$C = (-2, 3), r = 2\sqrt{3}$$

68. What is the equation of a line that passes through (a, a) in the xy-plane if it is parallel to a line that passes points through (a, b) and (b, a), where $a \neq b$? C. y = -x + 2a D. y = 2x - a

A.
$$y = x$$

B.
$$y = -x$$

C.
$$y = -x + 2a$$

$$D. y = 2x - a$$

69. What is the equation of the line that passes through (1, 1) and is parallel to 3y - x = 1?

A.
$$x - 3y + 2 = 0$$

B.
$$x + 3y = 4$$

C.
$$3y - x + 2 = 0$$
 D. $3x - y = 2$

$$D 3x - y = 2$$

70. Which one of the following is the equation of the circle whose end points of a diameter are (0, -2) and (2, 2)?

A.
$$x^2 + y^2 = 4$$

B. $x^2 + y^2 - 2y - 4 = 0$

C.
$$(x-1)^2 + y^2 = 4$$

$$D.x^2 + v^2 - 2x - 4 = 0$$

71. What is the area of the triangle in (sq. units) formed by the lines joining the vertex of the parabola $x^2 = -36y$ to the end points of the latus rectum?

- 72. A man running a race-course noted that the sum of the distances from the two flag posts from him is always 10 m and the distance between the flag posts is 8 m. what is the equation of the path traced by the man?
 - (Take the flag posts to be on the x-axis with the origin at their mid-point)

A.
$$\frac{X^2}{9} + \frac{Y^2}{25} = 1$$

C.
$$\frac{X^2}{100} + \frac{Y^2}{64} = 1$$

B.
$$\frac{X^2}{25} + \frac{Y^2}{9} = 1$$

$$D.\frac{X^2}{64} + \frac{Y^2}{100} = 1$$

- 73. Which one of the following is true about the pair of lines 3x + 9y 24 = 0 and 4x + 12y + 32 = 0?
 - A. Perpendicular lines

C. parallel and distinct lines

B. Intersecting lines

- D. representing the same lines
- 74. The center of a circle is on the line y = 2x and the line x = 1 is tangent to the circle at the point (1, 6). How long is the radius of the circle?
 - A. 5
- B. 4

C. 3

D. 2

75. If the circle passing through the point (-1,0) touches the y-axis at (0,2), then what is the equation of the circle?

A.
$$x^2 + y^2 + 5x + 4y + 4 = 0$$

C.
$$x^2 + y^2 - 5x - 4y + 4 = 0$$

B.
$$x^2 + y^2 - 5x + 4y + 4 = 0$$

D.
$$x^2 + y^2 + 5x - 4y + 4 = 0$$

76. The earth's orbit has a semi-major axis $a \approx 149.6$ *Gm*(gigameters) and an eccentricity of $e \approx 0.017$. What is the approximate value of the semi-minor axis?

<u>Unit 4</u> 2004

77. Suppose the proposition $p \Rightarrow \neg q$ is false (F), which of the following is true?

A.
$$\neg q \land (p \Rightarrow q)$$

C.
$$(\neg q \lor p) \Leftrightarrow q$$

B.
$$\neg p \lor (q \Rightarrow \neg p)$$

D.
$$(p \land q) \Leftrightarrow \neg q$$

78. Suppose $e(x) \equiv x$ is even; $p(x) \equiv x$ is prime; $d(x) \equiv x$ is divisible by 2. Which one of the following has the truth value F on the set of natural numbers?

A.
$$(\exists x)[e(x) \land p(x)]$$

C.
$$(\exists x)[e(x) \land \neg d(x)]$$

B.
$$(\forall x)[e(x) \Rightarrow d(x)]$$

D.
$$(\forall x)[e(x) \lor \neg d(x)]$$

79. If x and y are non-negative integers, which of the following is **NOT** true?

A.
$$(\forall x)(\exists y)(y > x^2 - 1)$$

C.
$$(\exists y)(\forall x)(y \le x^2 - 1)$$

B.
$$(\exists x)(\forall y)(y > x^2 - 1)$$

$$D. (\exists y)(\exists x)(y \le x^2 - 1)$$

80. . Consider the following argument form. Production is high if rain continues. Rain does not continue. Therefore, either production low or rain continues.

Let p: production is low

q: rain continues

The following table is also given about p and q.

row	P	Q	¬р	¬q	¬p⇒q	q⇒¬p	pVq
1	T	T	F	F	T	F	T
2	T	F	F	T	Т	T	T
3	F	T	T	F	T	T	T
4	F	F	T	T	F	T	F

Which of the following is necessarily true?

- A. The argument form is valid due to row 2.
- B. The argument form is valid due to row 2 and 3.
- C. The argument form is invalid due to row 4.
- D. The argument form is invalid due to row 1 and 3.

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81. For real numbers x and y, which one of the following statements is true?

A.
$$(\forall x)(\exists y)(x^2 + y + 1 = 0)$$

C.
$$(\exists y)(\forall x)(x^2 + y + 1 = 0)$$

B.
$$(\exists x)(\forall y)(x^2 + y + 1 = 0)$$

D.
$$(\forall y)(\exists x)(x^2 + y + 1 = 0)$$

82. Let p, q and r be propositions such that $p \Rightarrow (r \lor \neg q)$ is false. Then which one of the following proposition is true?

83. Consider the following argument:

"If he does not love her, she will not marry him. He loves her. Therefore, she will marry him."

If 'p≡ He loves her and 'q≡ she will marry him', which one of the following is correct representation of the argument form?

- A. $\neg p \Rightarrow \neg q, p \vdash q$; valid argument
- C. $p \Rightarrow q, p \vdash q$; valid argument
- B. $\neg p \Rightarrow \neg q, p \vdash q$; invalid argument
- D. $p \Rightarrow q, p \vdash q$; invalid argument
- 84. Suppose the following statements are the premises of an argument.

"He was lazy or he did not like the class room. If he was lazy, he could not pass the exam. He passed the exam."

Which one of the following could be a conclusion that makes the argument valid?

- A. He did like the class room
- C. If he was not lazy, he did like the class room
- B. He did not like the class room. D. He was not lazy and he did like the class room
- 85. If $(pVq) \Rightarrow (\neg r \land r)$ is true, then which one of the following is necessarily true?
 - A. $(pVq) \Rightarrow q$
- B. ¬q∧r
- C.¬p⇔r
- D.¬p∨r
- 86. Which one of the following is a valid logical argument?
 - A. $p \Rightarrow q, q \vdash p$

C. $\neg p \land q, q \Rightarrow r \vdash r$

B. $p \Leftrightarrow q, p \Rightarrow q \vdash q$

- D. $\neg p$, $p \lor q$, $r \Rightarrow q \vdash r$
- 87. Which one of the following is equivalent to $\neg [(\forall x)(p \Rightarrow q)]$?
 - A. $(\forall x)(\neg p(x) \Rightarrow \neg q(x))$

C. $(\exists x)(\neg p(x) \land q(x))$

B. $(\exists x)(\neg p(x) \Rightarrow \neg q(x))$

D. $(\exists x)(p(x) \land \neg q(x))$

- 88. Suppose that p represents the statement "He missed the tournament." q represents the statement "He got the gold medal." And r represents the statement "He took a trip abroad." Then which of the following symbolic expression represents the statement: "If he takes a trip abroad and he does not miss the tournament, then he will get the gold medal."
 - A. $(r \Rightarrow q) \land \neg p$

C. $(r \land \neg p) \Rightarrow q$

B. $r \land (P \Rightarrow q)$

- D. $\neg (r \lor p) \lor q$
- 89. For arbitrary propositions p and q, which one of the following is valid equivalence?
 - A. $\neg (p \Rightarrow q) \equiv (q \Rightarrow p)$
- C. $(p \lor \neg q) \equiv (p \Rightarrow q)$
- B. $[\neg (p \Rightarrow q) \land p)] \equiv (p \land \neg q)$ D. $[(p \lor q) \Rightarrow q] \equiv (p \Rightarrow \neg q)$
- 90. If each of the compound propositions $p \lor q, p \Rightarrow r$ and $\neg r$ is true, then which one of the following is True?
 - A. P

- C. $q \Rightarrow p$
- D. $p \land \neg r$

- 91. Which one of the following is not a tautology?
 - A. $[p \lor (q \Rightarrow r)] \Leftrightarrow [\neg p \Rightarrow (q \Rightarrow r)]$ C. $P \Rightarrow (P \Rightarrow q) \lor q$

B. pV $(q \Rightarrow \neg p)$

D. $[p \Leftrightarrow (q \land \neg r)] \Leftrightarrow [\neg p \Leftrightarrow (\neg q \lor r)]$

92. Which one of the following compound proposition is tautology?

A. $(qV \neg q) \Rightarrow p$

C. pV $(q \land \neg q)$

B. $p \Rightarrow (q \lor \neg q)$

- D. $p \Rightarrow (q \land \neg q)$
- 93. If the truth value of a proposition p is false, then which one of the following compound proposition has a truth value true?
 - A. $\neg p \land p$
- B. $\neg p \Rightarrow P$
- C. $\neg(\neg p \lor p)$
- D. $p \Rightarrow \neg p$
- 94. What is the contra positive of "If $x \in \mathbb{N}$, then x is integer and x > 0."?
 - A. If x is not integer or x<0, then $x\notin \mathbb{N}$. C. If x is not integer or $x\leq 0$, then $x\notin \mathbb{N}$.
 - B. If x is integer and x>0, then $x \in \mathbb{N}$. D If $x \notin \mathbb{N}$, then x is not integer and $x \le 0$
- 95. The valid conclusion from the premises: $p \lor q$, $q \Rightarrow r$, $p \Rightarrow m$, $\neg m$ is......

A.	$p \wedge (r \vee r)$	B. PA $(p \land r)$	C. $q \wedge (p \wedge r)$	D.	$r \land (p \lor q)$
		2000			

96. Let p and q stands for the statements "Nejat is intelligent" and "Almaz is hard working", respectively. Which of the following represent the statement "Almaz is hard working if Nejat is intelegent"?

A.
$$\neg p \land q$$

B.
$$\neg p \lor q$$

$$C. p \land q$$

D.
$$\neg a \lor p$$

97. Which of the following is a valid argument?

A.
$$\neg p \Rightarrow \neg q, q \vdash \neg p$$

$$C. \neg p \lor q, r \Rightarrow p, r \vdash \neg q$$

B.
$$p \Rightarrow \neg q, p, r \Rightarrow q \vdash \neg r$$

$$D. \neg p, p \lor q, r \Rightarrow q \vdash \neg r$$

98. Suppose "if $x \in A$, then $y \in B$ " is a true statement. Then which one of the following is necessarily true?

A.
$$y \in B$$
.

C. if
$$y \in B$$
, then $x \in A$.

B. If
$$x \notin A$$
, then $y \notin B$.

D. If
$$y \notin B$$
, then $x \notin A$.

99. Consider the following compound open proposition: $P(x) \equiv X$ is a prime number, $C(x) \equiv X$ is a composite number, and $\mathbf{E}(x) \equiv X$ is an even number. Which one of the following has a truth value of True in the set of positive integers?

A.
$$(\forall x) [P(x) \Rightarrow \neg E(x)]$$

$$C.(\exists x) [\neg P(x) \land \neg C(x)]$$

B.
$$\neg(\forall x) [C(x) \Rightarrow \neg P(x)]$$

$$D.\neg(\exists x) [E(x) \land \neg C(x)]$$

100. If the truth value of $(p \land \neg p) \Leftrightarrow [(q \lor \neg q) \Rightarrow r]$ is True, then which one of the following must be True?

101. Suppose the following are premises of an argument:

He is healthy and he is not angry.

He is angry or his plan fails.

His plan does not fail if he does not travel abroad.

Given that the premises are true, which one of the following can be a conclusion that makes the argument valid?

A. His plan fails and he is not angry.

C. He travels abroad.

B. His plan does not fail.

D. His plan fails and he does not travel abroad.

102. Let $U = \mathbb{N}$ (the set of natural numbers) be the universe. Which one of the following propulsion is True?

A.
$$(\exists x) (x + x = x)$$

C.
$$(\forall x)(\exists x)(x \div y = y \div x)$$

B.
$$(\forall x) (y < x)$$

D.
$$(\forall x)(\exists x)(x \div y = y \div x)$$

103. If $\neg p \Rightarrow r$ is false and $p \Leftrightarrow q$ is True, then which if the following is True?

A.
$$P \vee (\neg q \wedge r)$$

A.
$$P \lor (\neg q \land r)$$
 B. $\neg p \land (q \Rightarrow r)$ C. $\neg p \Rightarrow (q \lor r)$ D. $p \Leftrightarrow (\neg q \lor r)$

C.
$$\neg p \Rightarrow (q \lor r)$$

D.
$$p \Leftrightarrow (\neg q \lor r)$$

104. Which one of the following is a valid argument?

A. If I don't change my oil regularly, my engine will die. My engine died. Thus, I didn't change my oil regularly.

- B. If I am literate, then I can read and write. I can read but I can't write. Thus, I am not literate.
- C. If you do every problem in the book, then you will learn the subject. You learned the subject. Thus, you did every problem in the book.
- D. If it rains or snows, then my roof leaks. My roof is leaking. Thus, it is raining and snowing.

For real numbers x and y, which one of the following is NOT true?

A.
$$(\forall x)(\forall y)(y^2 + x^2 \ge -1)$$
 C. $(\exists x)(\forall y)(y \ge x^2 + 1)$

C.
$$(\exists x)(\forall y)(y \geq x^2 + 1)$$

B.
$$(\forall x)(\exists y) (y \ge x^2 + 1)$$

D.
$$(\exists x)(\exists y)(y \ge x^2 + 1)$$

Unit 5

A three-digit library identification card is to be printed from the numbers 0,1, 2,3,4,5 in a way that the first is non-zero and no number is to be repeated. How many such cards can be printed?

A. 100

B. 120

C. 150

D. 180

A. $\frac{3}{35}$

108.

B. $\frac{9}{35}$

	A. 0.2 B. 0.05		C.	0.1	D. 0.4		
109.	You are given a data on the	age of stud	lents, in a	primary sch	nool.		
	Age	8 10	11 12	13			
	Number of students	5 15	8 10	2			
V	Which of the following is not						
	A. The median is 10.5			C. The m	nean is 10.5		
	B. The mode is 10				range is 5		
110.	The following is a table of s	imple from	onov diet		•	rioblo v	
110.					i uata witii vai	Table X.	
	X 1	3 4		7			
	Frequency 2	5 6	5	2			
The	standard deviation of the date	. ia a aveal 4a					
The	standard deviation of the data						
	A. $\sqrt{3}$ B. $\sqrt{2.3}$			C. 3		$\sqrt{3.6}$	
	A school has three class roo	_		•			
th	ese classrooms is 28, 20 and	22, respect	vely. All	the students	s took an exan	nination and th	e average
SC	core of the students of 11A, 1	1B and 11C	is 60, 70	and 70, res	pectively. Wh	at is the averag	ge score in
th	is examination for all grade 1	1 students)				
	A. 66 B. 66.6	57	(C. 65	D. 65	5.67	
110	2005	1 <i>F</i>	م معسما میں	amad 6 20 a	4	d 7 10 aturdant	0 hanaaa
112.	Among students who took	_				1 /, 10 students	s scored 8
ar	nd 5 students scored 10. Wha	t is the aver					
	A. 7.8 B.7.5		C.		D. 7.0		
113.	How many four-digit even	numbers ca				f the numbers	start with 3?
	A. 40 B. 50		C. 100		D. 120		
114.	A committee consisting of 3	students is	to be sele	ected from 1	0 candidates	among which 4	4 are girls.
W	That is the probability that at I	least one gi	rl is select	ted.			
	A. $\frac{5}{6}$ B. $\frac{2}{3}$	C.	1	D. $\frac{1}{-}$,		
115	A group of six students take		J	· ·		cussion What	is the
					table for a dis	scussion, what	is the
pı	cobability that two specific st	udents do n			1		
	A. $\frac{3}{5}$ B. $\frac{2}{3}$		C	$\frac{2}{5}$	D. $\frac{1}{3}$		
116.	The mark of students score	d in an exar	nination i	s grouped in	n class interva	ls as shown be	low.
	Class interval(mark)	55-64	65-74	75-84	85-94	95-100	7
	` ´						4
	Number of students	8	12	20	6	4	
	What is the median of	the mark?					_
	A. 25.0 B. 75.5		C. 77.0	Т	D. 79.5		
117.	A box contains 5 white 6 red					are randomly to	iken out
	om the box one after the other					•	
	and the third are red?	i, what is th	ic probab.	inty that the	ilist ball is w	inte and both t	ne second
aı				4		5	
	A. $\frac{2}{15}$ B. $\frac{3}{15}$		C.	75	D.	91	
110	If the list of a massyroment	200 in 10 or 5	5				ha walua of
	If the list of a measurement $\overline{}$	18 10, α , 3,	$\alpha, 3, 10, 2$.0, 13, 20, 3	, with mean x	, men what is t	ne value of
α	in terms of \overline{x} ?	- 00	~	r - 00	ъ	4 🗖	
110	A. $10\bar{x} - 90$ B. 97				D. $5\overline{x}$	- 45	
119.	The following is the frequer	icy distribu	tion of a g	grouped data	ો.		
							10 Page

7. A student needs to select 3 books from 3 mathematics, 3 physics and 1 history book. What is the probability that one of them is mathematics and the other two are either physics or history books?

production, if 5% have defect D₁, 10% have defect D₂ and 2% have both defects, then what is the

probability for an item that have defect D_2 , given that it has defect D_1 ?

Items produced by a certain company are subjected to two kinds of defects D₁ and D₂. Out the total

Class intervals	3-7	8-12	13-17	18-22
Frequency(f)	2	2	10	6

What is the mean and the standard deviation of the distribution, respectively?

A. 15, $2\sqrt{5}$

B. 15, $\sqrt{7.5}$

C. 12.5, $5\sqrt{2}$

D. 12.5, $\sqrt{15}$

120. If distinct codes (words) of eight letters are formed by rearranging the letters in the word 'ABBEBAYE', how many of the codes begin with B or Y?

A. 840

B. 630

C. 1680

D. 4220

121. If Q_i , D_i , and P_i are respectively the ith-quartile, decile and percentile of a data arranged in increasing order, then which one of the following is necessarily true?

A. $Q2 = \frac{Q1+Q3}{2}$

C. $P_{25} > Q_1$

B. D₃>P₂₅

D. Q = mean of the data

122. A company produced 25,000 bulbs and randomly tested 2% of the product. Among the tested bulbs, if 40 have defect of D_1 , 60 have defect of D_2 and 25 have both types of defects, what is the probability that a bulb produced by the company has **none** of the defects?

A. 0.95

B. 0.80

C. 0.85

D. 0.20

123. If **S** is a set with **10** elements and $A \subseteq S$, what is the probability that **A** has **3** or more elements?

A. $\frac{7}{10}$

B. $\frac{8}{11}$

C. $\frac{121}{128}$

D. $\frac{7}{128}$

124. Different codes, each of which consisting of five characters, are to be generated in such a way that the first two characters are any of the English letters (A TO Z) and the remaining three are any of the digits (0, 1, . . . ,9). How many distinct codes can be generated so?

A. 468,000

B. 260

C. 676,000

D. $26! \times 10!$

125. The following is a set of data representing the average mark of 13 students: 91, 89, 93, 91, 87, 94, 92, 85, 91, 90, 96, 93, and 89. Then which of the following statements is true about the data?

A. The median is 90.5

C. The range of the mark is 11.

B. The upper quartile is 92

D. The mean is 91.5

126. A city has two daily newspapers, X and Y. the following information was obtained from a survey of 100 residents of the city: 35 people subscribe to X, 60 people subscribe to Y and 20 subscribe to both newspapers. Then how many of the people in the survey do not subscribe to either of the newspapers?

A. 5

B. 25

C. 40

D 5

127. Suppose that the first 3 letters (A, B and C) and number digits are to be used to form car plates in a small town. How many different plates can be formed in a total that contain 1, 2 or 3 letters and then followed by 3 digits?

A. 3,000

B. 27,000

C. 39,000

D. 100,000

128. A

Class interval	5-15	15-25	25-35	35-45	45-55
frequency	22	40	68	50	20

measurement is grouped into five

class intervals with the following frequency distribution.

What are the first quartile Q_1 and the 75^{th} percentile P_{75} of the measurement?

A. $Q_1=20$, $P_{75}=40$

C. $Q_1=20$, $P_{75}=39$

B. $Q_1=22$, $P_{75}=40$

D. $Q_1=22$, $P_{75}=39$

129. Three persons **P**₁, **P**₂ and **P**₃ are firing at a target independently and have a probability **0.7**, **0.5** and **0.4**, respectively, of hitting the target. What is the probability that at least one of them hits the target?

A. 0.95

B. 0.85

C. 0.91

D. 0.99

 X
 3
 5
 6
 7

 Frequency
 2
 5
 2
 1

130. The following is a simple frequency distribution of a data with variable X.

What are the mean (\bar{x}) and variance δ^2 of the data?

A.
$$\overline{X} = 5$$
, $\delta^2 = 0.7$

B.
$$\overline{X} = 6. \delta^2 = 1.4$$

A.
$$\overline{X} = 5, \delta^2 = 0.7$$
 B. $\overline{X} = 6, \delta^2 = 1.4$ C. $\overline{X} = 6, \delta^2 = 0.7$ D. $\overline{X} = 5, \delta^2 = 1.4$

D.
$$\overline{X} = 5.\delta^2 = 1.4$$

131. A box contains 10 items of which 3 are defective. If two items are randomly taken out of the box, what is the probability that both items are not defective?

A.
$$\frac{7}{10}$$

B.
$$\frac{4}{7}$$

C.
$$\frac{7}{15}$$

D.
$$\frac{49}{100}$$

A. $\frac{7}{10}$ B. $\frac{4}{7}$ C. $\frac{7}{15}$ D. $\frac{49}{100}$ 132. Items produced by a certain company are subjected to two kinds of defects $\mathbf{D_1}$ and $\mathbf{D_2}$. Out of the total product 5% have the defect D_1 , 10% have the defect D_2 , and 2% have both defects. What is the probability that a randomly selected item has neither defect D_1 or D_2 ?

133. There are three children in a room, ages three, four, and five, if a four- year-old child enters the room then which one of the following is true?

A. Mean age will stay the same but the standard deviation will increase.

B. Mean age will stay the same but the standard deviation will decrease.

C. Mean age and the standard deviation will increase.

D. Mean age and the standard deviation will stay the same.

In how many more ways can 4 people be arranged in a row than if they were arranged in a circle?

A. 1

B. 6

C. 18

D. 12

135. Two machines **A** and **B** work independently. The probability that both machines **A** and **B** work is **0.4.** if the conditional probability that machine **B** works given that machine **A** works is **0.5**, then the conditional probability that machine **A** works given that machine **B** works is.....

B.0

C. 0.5

D. 0.7

136. A team of 10 researchers consists of 4 biologists and 6 chemists. If 3 persons are chosen randomly from the team, what is the probability that at least one is a biologist?

A.
$$\frac{2}{3}$$

C.
$$\frac{5}{6}$$

D.
$$\frac{7}{10}$$

137. The probability that an electronic device produced by a company does not function properly is equal to 0.1. If two devices are bought, then what is the probability that at least one device function properly?

138. Two machines A and B produce respectively 60% and 40% of the total number of items of a factory. The percentages of defective of these machines are 2% and 5%, respectively. If an item is selected at random, then what is the probability that the item is defective?

139. In how many ways can a committee of 3 members be formed from 7 candidates?

A. 7

B. 21

C. 28

D. 35

	X	3-7	8-12	13-17	18-22
of a	Frequency	4	6	8	2

140. The following is a frequency distribution table grouped data with variable X.

What is the mean (\overline{x}) and the variance (δ^2) of the data respectively?

A.
$$\bar{x}_1 = 12, \delta^2 = 21$$

C.
$$\bar{x} = 13, \delta^2 = 9$$

B.
$$\bar{x} = 12, \delta^2 = 25$$

D.
$$\bar{x} = 13, \delta^2 = 16$$

141. The expenditure of 100 families is given below.

Expenditure	0-9	10-19	20-29	30-39	40-49
No. Of families	14	23	F_1	21	F_2

If the mode of the data is 23.5, what are the values of F_1 and $F_{2?}$

A.
$$F_1 = 27$$
, $F_2 = 15$

C.
$$F_1 = 25$$
, $F_2 = 17$

B.
$$F_1 = 15$$
, $F_2 = 27$

D.
$$F_1 = 17$$
, $F_2 = 25$

D. 32

D. $\frac{3}{4}$

A. 28

B. 29

probability that atleast one of the events occur?

What is t	he mean (\overline{x}) an	d the stan	dard deviation	on (<i>sd</i>) of	f the data	in minute?		
A. \overline{x}	$= 7$, $sd = \sqrt{1}$.	5		C	$\overline{x} = 8$, so	$d=\sqrt{2}$		
B. \overline{x}	$=7, sd = \sqrt{2}$			D.	$\overline{x} = 8$, s	$sd = \sqrt{1.5}$		
145. A priv	ate college has	1000 stu	dents. 60% of	f these st	udents ar	e males, 45%	% of these stude	ents pay their
	•	including	175 females.	What is	the proba	ibility that tl	he student is a 1	male or a
credit car						_		
A. 0.6			0.225	1.0 (0	C. 0.325		D. 0.775	
							numbers is dele	
•	multiple of 3?	mese sets.	, what is the p	товавш	y mat an	of the three	deleted number	ars are even
	-		C^{-1}		D 8			
_	B. $\frac{2}{21}$							
147. The ag	ge distribution						7	
Age		10-14	15-19	20-24		25-29		
N <u>o</u> .	Of students	2	10	6	7	7		
W	hat is the moda	ıl value of	the distributi	ion?				
A. 17		. 17.38	C. 18.		D. 18.73			
148. The va	ariance of 20 o	bservatior	s is 5. If each	observa	tion is m	ultiplied by	2, then what is	the variance
of the res	ulting observa	tions?						
A. 5		B. 10		. 20		D. 40		
149. If there family?	e are two child	ren in a fa	amily, what is	the prob	ability th	at there is a	t least one girl	in the
	B. $\frac{1}{4}$		C. $\frac{3}{4}$		Γ	$\frac{2}{3}$		
	_		_		-	le of certain	student's score	e is 90.
	the following							
	e students have			-		•		
	e student's sco e student's sco							
	e score of the			_				
	ark of 50 stude		_	as that of	7070 tile	stadents.		
	Marks	0-1		20-30	30-40	40-50		
	10. Of students	-	8	$\frac{20-30}{f_1}$	10	f_2		
<u> </u>	·							
	dian of the data	ı is 26, wh	at are the val					
-	$= 7, f_2 = 20$				•	$f_1, f_2 = 12$		
•	$= 12, f_2 = 15$	are produ	ead by a macl		$f_1 = 20$. , –	e randomly sele	acted and
		-	•			-	an item produc	
	has No defect?		e a derect, th	on white	is the pro	outility that	an item produc	ica oy u
A. 0.8		B. 0.85		C. 0.90		D. ().95	
								13 Page

142. The first group of 10 children has a mean weight of 15.6 kg, and the second group of another 10 children has a mean weight of 16 kg, and the third group of children has a mean weight 20kg. If the mean weight of all children is 17 kg, what is the total number of children in all of the three groups?

Let A and B be two events. Suppose that the probability that neither event occurs is $\frac{3}{8}$. What the

144. The time needed to type a sample of 8 business letters in an office is 7, 8, 6, 8, 9, 7, 5, 6 minutes.

C. 30

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153.	Fatuma can solve 90%	of the problems	given in a	book and	Mesfin car	n solve 70%.	What is the
pr	obability that at least or	ne of them will so	olve the \mathfrak{p}_{1}	oblem?			

- 154. There are three children in a room with, ages four, five, and six. If a five year old child enters the room, then which of the following statement is correct?
 - A. Mean age will stay the same the standard deviation will decrease.
 - B. Mean age will stay the same the standard deviation will increase.
 - C. Mean age will and standard deviation will increase.
 - D. Mean age and standard deviation will stay the same.

155. Let
$$A = \begin{pmatrix} -2 & 0 & x \\ 2y & x+y & -4 \end{pmatrix}$$
 and $B = \begin{pmatrix} 1 & -y \\ 0 & 3 \\ 1-x & 2 \end{pmatrix}$ such that $A+2B^T = 0$. Then which of the

following is the value of y?

B.
$$-\frac{13}{2}$$

A. 0 B.
$$-\frac{13}{2}$$
 C. -8 D. any real number

156. Let A and B be 3×3 matrices such that $A = \begin{pmatrix} 2 & 0 & 0 \\ 1 & 5 & 0 \\ 0 & -1 & \frac{1}{2} \end{pmatrix}$ and $|B| = \frac{1}{10}$. Which of the following is

equal to $|2AB^T|$

157. If
$$\begin{pmatrix} \alpha & 2 & \beta \\ 2 & 1 & 3 \\ -1 & 0 & 1 \end{pmatrix} \begin{pmatrix} x \\ y \\ z \end{pmatrix} = \begin{pmatrix} -5 \\ 5 \\ 0 \end{pmatrix}$$
 and the determinant of the coefficient matrix is -5, then the value of x is equal to:

B.
$$\alpha + \beta$$

$$C. -5a$$

A. 3 B.
$$\alpha + \beta$$
 C. -5α D. 5

158. What is the solution set of the following system of equation
$$\begin{cases} x + y + 2z = 1 \\ x + 2y + z = 2 \end{cases}$$
?
$$(-2x - 2y - 4z = -2)$$

A.
$$\{(0,1,0)$$

C.
$$\{(-3k, k+1, k) | k \in (-\infty, \infty)\}$$

B.
$$(-\infty, \infty)$$

D.
$$\{(3k, k-1, k) \mid k \in (-\infty, \infty)\}$$

A.
$$\{(0,1,0)\}$$
 C. $\{(-3k,k+1,k)\setminus k \in (-\infty,\infty)\}$
B. $(-\infty,\infty)$ D. $\{(3k,k-1,k)\setminus k \in (-\infty,\infty)\}$
159. Suppose $A = \begin{pmatrix} 1 & 2 \\ 2 & 3 \end{pmatrix}$. If X is 2×2 matrix such that $AX - A^T = 2A$, then what is the value of X?
A. $\begin{pmatrix} 3 & 1 \\ 1 & 3 \end{pmatrix}$ B. $\begin{pmatrix} 3 & 3 \\ 3 & 3 \end{pmatrix}$ C. $\begin{pmatrix} 3 & 6 \\ 6 & 9 \end{pmatrix}$ D. $\begin{pmatrix} 3 & 0 \\ 0 & 3 \end{pmatrix}$
160. Suppose that A and B are 3×3 matrices, I is identity matrix of order 3 such that $AB = 2I$. If $|B| = 6$, what is det $(A^T)^2$

A.
$$\begin{pmatrix} 3 & 1 \\ 1 & 3 \end{pmatrix}$$

B.
$$\begin{pmatrix} 3 & 3 \\ 3 & 3 \end{pmatrix}$$

C.
$$\begin{pmatrix} 3 & 6 \\ 6 & 9 \end{pmatrix}$$

D.
$$\begin{pmatrix} 3 & 0 \\ 0 & 3 \end{pmatrix}$$

what is $\det(A^T)$?

A.
$$\frac{1}{3}$$

B.
$$\frac{4}{3}$$

A. $\frac{1}{3}$ B. $\frac{4}{3}$ C. 12 D. 48 $\begin{cases} \alpha x + y + z = 1 \\ x + 2y + 4z = 0 \end{cases}$ 161. Consider the system $\begin{cases} x + y + z = 1 \\ x + 2y + 4z = 0 \end{cases}$. If the determinant of the coefficient matrix is 2, then what is 5x - y + z = 0

A.
$$\left(3\alpha, \frac{19\alpha}{2}, \frac{-11\alpha}{2}\right)$$

B.
$$\left(3, \frac{19}{2}, \frac{-11}{2}\right)$$

C.
$$\left(\frac{3}{\alpha}, \frac{-19}{2}, \frac{11}{2}\right)$$

D.
$$\left(\frac{3}{2}, \frac{19}{2}, \frac{-9}{2}\right)$$

the solution of the system of the equations?

A. $\left(3\alpha, \frac{19\alpha}{2}, \frac{-11\alpha}{2}\right)$ B. $\left(3, \frac{19}{2}, \frac{-11}{2}\right)$ C. $\left(\frac{3}{\alpha}, \frac{-19}{2}, \frac{11}{2}\right)$ D. $\left(\frac{3}{2}, \frac{19}{2}, \frac{-9}{2}\right)$ 162. Let $A = \begin{pmatrix} 2 & 0 & -1 \\ 1 & 2 & 0 \\ 0 & 0 & -1 \end{pmatrix}$ and $(2A + B)^T = A^T A$, then which of the following is equal to the value of **B**?

A.
$$\begin{pmatrix} 1 & 0 & -2 \\ 2 & 0 & 0 \\ 0 & 0 & 4 \end{pmatrix}$$

C.
$$\begin{pmatrix} 8 & 0 & -4 \\ 4 & 8 & 0 \\ 0 & 0 & -4 \end{pmatrix}$$

B.
$$\begin{pmatrix} 0 & 0 & 0 \\ 0 & 0 & 0 \\ 0 & 0 & 0 \end{pmatrix}$$
 D. $\begin{pmatrix} 1 & 2 & 0 \\ 0 & 0 & 0 \\ -2 & 0 & 4 \end{pmatrix}$

B. $\begin{pmatrix} 0 & 0 & 0 \\ 0 & 0 & 0 \\ 0 & 0 & 0 \end{pmatrix}$ $D. \begin{pmatrix} 0 & 0 & 0 \\ -2 & 0 & 4 \end{pmatrix}$ 163. If $M = \begin{pmatrix} 0 & 1 & 2 \\ 3 & -1 & 0 \\ 5 & 2 & 4 \\ 5 & 3 & 4 \end{pmatrix}$ and $A^{T}M = 2I$, where A is 3×3 matrix and I is identity matrix of order 3, then

B.
$$\frac{4}{17}$$

D.
$$\frac{1}{17}$$

 $x - y + z = 1$

A. 0.2 B. $\frac{1}{17}$ C. 0.8 D. $\frac{1}{17}$ 164. What should be the value of k so that the system of equation $\begin{cases} x - y + z = 1 \\ -x + 5y \pm 4z = 1 \\ 2x + 2y - z = k \end{cases}$

has a

solution?

165. Suppose AX = b, where A is a 3×3 matrix, $b = (b1, b2, b3)^T$ and $X = (x, y, z)^T$. Which of the following is necessarily true?

- A. The system has a solution only when $det(A) \neq 0$.
- B. The Cramer's is suitable to solve the system if two rows of A are identical.
- C. If $det(A) \neq 0$ and the second column of A is multiple of b, then x = 0.
- D. If b = 0, then $X = (0, 0, 0)^T$ is the only solution of the system.

166. Consider the following system of equations: $\begin{cases} ax + by = 2 \\ x + 3y + 2z = 0 \end{cases}$ if the determinant of the coefficient

matrix is 2, then what is the solution set of the system?

A.
$$\{(1,3,-5)\}$$

B.
$$\left\{ \left(\frac{1}{a}, \frac{1}{b}, 0 \right) \right\}$$

C.
$$\{(-2, -6, 10)\}$$

A. $\{(1,3,-5)\}$ B. $\{\left(\frac{1}{a},\frac{1}{b},0\right)\}$ C. $\{(-2,-6,10)\}$ D. \emptyset 167. If $A = \begin{pmatrix} 0 & x & 0 \\ 1 & -1 & 1 \\ 0 & y & -1 \end{pmatrix}$ and $A^{-1} = \begin{pmatrix} 1 & 1 & 1 \\ 3 & 0 & 0 \\ 2 & 0 & -1 \end{pmatrix}$, then what are the values of x and y?

A. x = 3, y = -2 C. x = -3, y = 2B. $x = \frac{2}{3}, y = \frac{1}{3}$ D. $x = \frac{1}{3}, y = \frac{2}{3}$

A.
$$x = 3, y = -2$$

C.
$$x = -3, y = 2$$

B.
$$x = \frac{2}{3}, y = \frac{1}{3}$$

D.
$$x = \frac{1}{3}, y = \frac{2}{3}$$

A. 12

169. What is the solution set of the system $\begin{cases} x + y - z = 1 \\ x + 2y - 3z = 1 \\ 2x + 3y - 4z = 2 \end{cases}$

A.
$$\{(0,2,1)\}$$

C.
$$\{(2k+1, -k, k) | k \in \Re\}$$

B.
$$\{(1-k, 2k, k) | k \in \mathcal{R}\}$$

170. If $A = \begin{pmatrix} 2 & 7 \\ 1 & 3 \end{pmatrix}$ and $B^{-1} = \begin{pmatrix} 1 & 1 \\ 0 & 2 \end{pmatrix}$, then $(AB)^{-1}$ is equal to:

A. $\begin{pmatrix} 4 & -3 \\ 4 & -5 \end{pmatrix}$ B. $\begin{pmatrix} -2 & 5 \\ 2 & -4 \end{pmatrix}$ C. $\begin{pmatrix} -3 & 11 \\ 1 & -3 \end{pmatrix}$ D. $\begin{pmatrix} 4 & 0 \\ 0 & 4 \end{pmatrix}$

A.
$$\begin{pmatrix} 4 & -3 \\ 4 & 5 \end{pmatrix}$$

B.
$$\begin{pmatrix} -2 & 5 \\ 2 & 4 \end{pmatrix}$$

C.
$$\begin{pmatrix} -3 & 11 \\ 1 & 2 \end{pmatrix}$$

D.
$$\begin{pmatrix} 4 & 0 \\ 0 & 4 \end{pmatrix}$$

171. Let $A = \begin{pmatrix} 0 & \alpha & \beta \\ 2 & 2 & 1 \\ 3 & 1 & 2 \end{pmatrix}$, $b = \begin{pmatrix} 6 \\ 0 \\ 0 \end{pmatrix}$, and $X = \begin{pmatrix} x \\ y \\ z \end{pmatrix}$. If det(A) = 3, then what is the solution set of the system AX = b?

A. $\{(6, -2, -8)^T\}$ B. $\{(0, \frac{1}{\alpha}, \frac{1}{\beta})^T\}$ C. $\{(-3, 1, 4)^T\}$ D. \emptyset

A.
$$\{(6, -2, -8)^T\}$$

B.
$$\left\{ \left(0, \frac{1}{\alpha}, \frac{1}{\beta}\right)^T \right\}$$

C.
$$\{(-3,1,4)^T\}$$

172. For any n×n square matrix A, which one of the following is true?

- A. $det(A) = -det(A^T)$, where A^T is the transpose of A.
- B. If k is scalar, then $det(kA) = k^n det(A)$.
- C. If B is a matrix obtained from A by interchanging of two rows of A, det(B)=det(A).

- D. If A is invertible, then $det(A) = det(A^{-1})$.
- x 3y 2z = 6173. The solution of the system of linear equation of $\begin{cases} 2x - 4y - 3z = 8 \\ -3x + 6y + 8z = -5 \end{cases}$
 - A. $\{(-1, -3, -2)\}$

C. $\{(1, -3, 2)\}$

B. $\{(-1, -3, 2)\}$

- D. $\{(1, 3, -2)\}$

- 174. If $A = (a_{ij})_{3\times 3}$ is a square matrix with $A^{-1} = \begin{pmatrix} 1 & 3 & 2 \\ 1 & 1 & 3 \\ 0 & 4 & 5 \end{pmatrix}$, then what is the cofactor of a_{23} ?

 A. $-\frac{3}{14}$ B. $-\frac{2}{7}$ C. $\frac{2}{7}$ D. $-\frac{3}{7}$ 175. When $\begin{vmatrix} a & b & c \\ a & -a & a \\ a & a & -a \end{vmatrix} = a^3$, and $a \neq 0$, what is the solution of $\begin{pmatrix} a & b & c \\ a & -a & a \\ a & a & -a \end{pmatrix} \begin{pmatrix} x \\ y \\ z \end{pmatrix} = \begin{pmatrix} 1 \\ 0 \\ 0 \end{pmatrix}$
 - A. $\{(0, 2a, 2a)\}$

- A. $\{(0, 2a, 2a)\}$ B. $\left\{\left(\frac{1}{a}, -2a, 2a\right)\right\}$ D. $\left\{\left(0, \frac{2}{a}, \frac{2}{a}\right)\right\}$ $\left\{x + y + z = 6\right\}$ 176. What are the values of γ and μ so that the system $\begin{cases} x + 2y + 3z = 10, \text{ has infinitely many solutions?} \\ x + 2y + \gamma z = \mu \end{cases}$
 - A. $\gamma \neq 3$ and $\mu \in \Re$

C. $\gamma = 3$ and $\mu = 10$

B. $\gamma = 3$ and $\mu \neq 10$

D. $\gamma \in \Re$ and $\mu = 10$

177. A salesman sold items x_1 x and x_3 , with different rates of commissions as shown in the table below.

Month	Sales of units			Total commission(in Birr)
	\mathbf{x}_1	\mathbf{x}_2	X3	
February	90	100	20	800
March	130	50	40	900
April	60	100	30	850

What the rates of commission on items x_1 , x_2 and x_3 respectively.

A. 4, 2 and 11

C. 4, 11 and 2

B. 2, 4 and 11

- D. 11, 2 and 11
- 178. If A is a square matrix of order 3 and det(A) = 5, then what is the value of det(A.adi(A))?
 - A. 3
- B. 5
- C. 125
- 179. Let A be a 3×3 invertible of matrix and B be any 3×3 matrix. If |A| = a and, |B| = b, then which of the following is not true?
 - A. $|A^{T}A| = a^{2}$

- C. $|A^{-1}B| = ab$
- B. $|kA| = k^3 |A|$, for any $k \in \mathbb{R}$

- D. if b = 0, then B is not invertible
- 180. Let A be a 3×3 matrix and |A| = -2. Then what is the value of |adj(A)|?

- D. 4
- 181. If $\begin{vmatrix} -1 & 1 & 2 \\ 3 & 2 & x \\ 2 & 4 & 1 \end{vmatrix} = \begin{vmatrix} -x & 3 & 2 \\ 2 & 2 & 3 \\ 1 & -1 & -2 \end{vmatrix}$, then what is the value of x?

- 182. Consider the following system of equation: $\begin{cases} x 2y + z = 1 \\ -x + y + z = 3 \end{cases}$ How much should be the value of k so that the system has a solution?

so that the system has a solution?

C. 0

- D. -1
- 183. If A is a 3×3 matrix and det(A) = 5, then $det(2A^TA)$ is equal to:

ETHIO NATIONAL SCHOOL MATHEMATICS EUEE QUESTION FROM 2004-2011 E.C. D. 20 184. If $2\begin{pmatrix} 2x & x \\ -5 & -3 \end{pmatrix}^{-1} = \begin{pmatrix} 3 & 2 \\ -5 & -4 \end{pmatrix}$, then what is the value of x? 185. Which of the following is the simplest form of $\frac{4-3i}{3+4i} + \overline{1-2i}$? B. 1 + 3i186. Let z be a complex number. Which of the following is the solution set of $z^3 - iz = 0$? C. $\{\pm\sqrt{2}(1+i)\}$ A. $\left\{ \pm \frac{1}{\sqrt{2}} (1+i) \right\}$ B. $\left\{0, \pm \frac{1}{\sqrt{2}}(1-i)\right\}$ D. $\left\{0, \pm \frac{1}{\sqrt{2}}(1+i)\right\}$ 187. In the set of complex numbers, the solution set of $x^2 - 2x + 5 = 0$? C. $\{1 + 2i, 1 - 2i\}$ B. $\{2+i, 2-i\}$ D. $\{2+4i, 2-4i\}$ Which one of the following is the simplest form of $|3 + 4i| - \frac{25i}{3+4i}$? 188. B. 5+5iD. 1 - 3i189. If $z = \cos\left(\frac{\pi}{10}\right) + i\sin\left(\frac{\pi}{10}\right)$, then what is the value of z^5 ? A. $\frac{\pi}{2} + \frac{\pi}{2}i$ B. $\frac{1}{2} + \frac{1}{2}i$ 190. In the set of complex numbers, which one of the following is the solution set of $z^3 - iz^2 + 2z = 0?$ C. $\{0, -i, 2i\}$ B. $\{0, -i\}$ D. $\{0, i, -2i\}$ 191. If z = x + yi, is a complex number, then $|z|^2 + \frac{1}{2}(z - \bar{z})^2 = 1$ is equivalent to which one of the following equation? C. $x^2 - y^2 = 2$ D. $2x^2 - y^2 = 2$ A. $x^2 - y^2 = 1$ B. $x^2 - 3iy^2 = 1$ 192. If $w = \frac{16i}{1+i} + (1-3i)^2$ and $z = |w| + \overline{w}$, which one of the following is the simplest form of z? C. 4 - 2iD. 2 - 2i193. If $z = \frac{3+i}{i-2}$ is a given complex number, then what is the conjugate, \bar{z} , of z? C. $\bar{z} = -6 - 2i$ D. $\bar{z} = -1 - i$ 194. What is the principal argument of $(5 + 5i)^{11}$?

A. $\frac{\pi}{2}$ B $\frac{2\pi}{3}$ C. $\frac{\pi}{4}$ 195. What are the values of u and v that satisfy the equation: $\frac{u+3i}{4-2i} = \frac{2+vi}{20}$? A. u = 2, v = 3B. u = -6, v = 10C. u = 2, v = 16D. u = -4, v = 6196. In the set of complex numbers, what is the solution set of $x^2 + 4x + 5 = 0$? C. $\{2-i, 2+i\}$ B. $\{1-2i, 1+2i\}$ D. $\{-2-i, -2+i\}$ 197. If $z = (1+i)^{10}$, then which of the following is equal to z? B. 32*i* D. 1 + 10i198. If $z = \frac{2-4i}{1+i}$, then the modulus of the conjugate of z, $|\bar{z}|$ is: D. $2\sqrt{2}$ 199. If $z = \sqrt{2}\cos\left(\frac{\pi}{12}\right) + i\sqrt{2}\sin\left(\frac{\pi}{12}\right)$, then what is the value of z^3 ? C. $2\sqrt{2} + 2i\sqrt{2}$ A. 2 + 2i

B.
$$\sqrt{2} + i\sqrt{2}$$

D.
$$3\sqrt{2} + 3i\sqrt{2}$$

200. Which one of the following is the conjugate of $|3 + 4i| - \frac{25i}{3+4i}$?

A.
$$5 + 3i$$

B.
$$1 + 3i$$

C.
$$3 - 5i$$

D.
$$1 - 3i$$

201. If $z_1 = \frac{2-i}{1+i}$, $z_2 = \frac{1+i}{1-i}$ then what is the value of $z_1 + 2z_2$?

A.
$$1 + i$$

B.
$$\frac{1+i}{2}$$

C.
$$\frac{1-}{2}$$

D.
$$1 - i$$

202. If z = -3 + 4i and w = 1 + 2i, then what is the value of $\frac{2z}{w} + \overline{w}$?

A. 2 + 3iB. 3 + 5iC. 3 + 2i

A.
$$2 + 3i$$

$$C \cdot 3 + 2$$

D.
$$3 - 2i$$

203. Let $z = \left(\frac{1-i}{1+i}\right)^{18}$, then what is the value of z?

A.
$$-1$$

D.
$$1 - i$$

204. If $z = (1 + i\sqrt{3})(1 + i)$, then which one of the following is the polar representation of z?

A.
$$z = 4(\cos(105^\circ) + i\sin(105^\circ))$$

C.
$$z = 2\sqrt{2}(\cos(15^\circ) + i\sin(15^\circ))$$

B.
$$z = 2\sqrt{2}(\cos(105^\circ) + i\sin(105^\circ))$$

D.
$$z = 4(\cos(75^\circ) + i\sin(75^\circ))$$

205. Which of the following is the multiplicative inverse of $z = \frac{3+4i}{4-5i}$?

A.
$$\frac{8}{25} - \frac{31}{25}i$$

A.
$$\frac{8}{25} - \frac{31}{25}i$$
 B. $-\frac{8}{25} + \frac{31}{25}i$

C.
$$-\frac{8}{25} - \frac{31}{25}i$$
 D. $\frac{8}{25} + \frac{31}{25}i$

D.
$$\frac{8}{25} + \frac{31}{25}i$$

206. Let z be a complex number and w = 3 + 4i. If $\frac{z^2 + 1}{z + i} = |w|z - \frac{1}{i}\overline{w}$, then what is the value of z?

A.
$$-4 - 2i$$

B.
$$4 - 2i$$

C.
$$-1 + i$$

D.
$$-1 - i$$

207. What is the polar form of $\frac{7-i}{3-4i}$?

A.
$$\sqrt{2}\left(\cos\frac{\pi}{2} + i\sin\frac{\pi}{2}\right)$$

C.
$$2\left(\cos\frac{\pi}{2} + i\sin\frac{\pi}{2}\right)$$

B.
$$\sqrt{2}\left(\cos\frac{\pi}{4} + i\sin\frac{\pi}{4}\right)$$

D.
$$2\left(\cos\frac{\pi}{4} + i\sin\frac{\pi}{4}\right)$$

208. Which of the following is a vector that lies on the line through (0, 0) and (2, 4)?

A.
$$\vec{u} = (2, 1)$$

C.
$$\vec{u} = (\frac{1}{2}, 2)$$

B.
$$\vec{u} = (-1, -2)$$

D.
$$\vec{u} = (-2, -6)$$

209. Let i and j be the standard unit vectors in the direction of positive X-axis and positive Y-axis, respectively, and \overrightarrow{AB} be a vector from the point B(2,2). If $\overrightarrow{v} = 3\overrightarrow{AB} + 2i$, the unit vector in the direction of \vec{v} is equal to:

A.
$$(\frac{3}{5}, \frac{4}{5})$$

B.
$$\left(\frac{-3}{5}, \frac{-4}{5}\right)$$

C.
$$\left(\frac{-3}{5}, \frac{4}{5}\right)$$

D.
$$\left(\frac{3}{5}, \frac{-4}{5}\right)$$

210. Which of the following is a vector equation of the line tangent to the circle $x^2 + y^2 + 2x - 7 = 0$ at (1, 2)

A.
$$(x, y) = (0,3) + \lambda(-1,2)$$

C.
$$(x, y) = (0, 3) + \lambda(1, -1)$$

B.
$$(x, y) = (1, 2) + \lambda(2, -1)$$

D.
$$(x, y) = (1, 2) + \lambda(-1, 2)$$

211. Let ℓ be the line whose equation is 2x - y = 10. Which one of the following is the equation of the image of ℓ after a reflection in the line y = 2x - 5 followed by a rotation through the angle of 90° about the origin?

A.
$$x + 2y = 0$$

B.
$$2x + y = 0$$

B.
$$2x + y = 0$$
 C. $x + 2y = 5$

D.
$$x - 2y = 5$$

212. If $\vec{u} = (-3, x)$ and $\vec{v} = (x, y - 2)$ are vectors, what is the value of y so that

$$\vec{u} + \vec{v} = 3\vec{u} - \frac{1}{2}\vec{v}?$$

A.
$$\frac{2}{3}$$

B.
$$-\frac{10}{3}$$

D.
$$-\frac{22}{3}$$

	A line given by a vector equation $r(x) = (0$		
ra	dius of the circle is $\sqrt{2}$, which one of the following	owing is the of the circle?	,
	A. (1,4) B. (1,-4)	C. (-1,2) D.	(1,2)
214.	What is the image of the ellipse whose equat	$x = (x + 2)^2 + (y - 2)^2$	$1)^2 = 2$ under a translation that
ta	kes (2, 1) to (4, 0) followed by a rotation of 9	0°?	
	A. $x^2 + 2y^2 = 2$	C. $2(x-4)^2 + y^2 = 2$	
	B. $2x^2 + y^2 = 2$	C. $2(x-4)^2 + y^2 = 2$ D. $(x-4)^2 + 2y^2 = 2$	
215.	If \vec{A} is perpendicular to \vec{B} , what is the cosine	e of the angle between \vec{A} :	and $\vec{A} - \vec{B}$?
	A. $\frac{ \vec{A} - \vec{B} }{ \vec{A} }$ B. $\frac{ \vec{A} }{ \vec{A} - \vec{B} }$		1 ->1
	A. $ \vec{A} $ B. $ \vec{A}-\vec{B} $	$C. { \vec{B} }$	D. $\frac{ B }{ \vec{A}-\vec{B} }$
216.	Which of the following is necessarily true?		
	A. If $ \vec{A} = \vec{B} $, then $\vec{A} = \vec{B}$. C. If \vec{u}	is a unit vector in the dire	ection of \vec{A} , then $\vec{A} \cdot \vec{u} = \vec{A} $
	B. $ k\vec{A} = k \vec{A} $, for any real number. D. If	\vec{A} is parallel to \vec{B} , then \vec{A} .	$ \vec{B} = 0 $
017	2006		
217.	If a point (2, 5) is reflected under a line to th		ne line of reflection?
	A. 2x + 3y = 7	C. $8y + 10x = 19$	
210	B. $x + 3y = 7$	D. $2x + 3y + 5 = 0$	1:1 64 611 : :
	If $A = (-2, 3)$, $B = (3, 1)$ and C is any other	point on the plane, then v	which one of the following is
th	e coordinate form of $\overrightarrow{AC} - \overrightarrow{BC}$?		
	A. $(-5,2)$ B. $(5,-2)$		
219.	What is the equation of a line that passes thr		and parallel to the vector $(1,-1)$?
	A. $2x - y = 1$	C. $x - 2y = 3$	
	B. $x + y - 1 = 0$	D. $y - 2x + 1 = 0$	
	What is the image of the line given by (x, y)		\Re , under the translation that
ta	kes $(1, 0)$ to $(0, 1)$ followed by the reflection a		
	A. $y = 2x + 3$	C. $y = 2x + 6$	
	B. $y = 2x - 3$	D. $y = 2x - 3$	
	If a translation T takes the circle $x^2 + y^2 - \frac{1}{2}$		e circle whose equation is
()	$(x + 2)^2 + (y - 4)^2 = 7$, then what is the image		
		C. (13)	
	If ℓ is the line that passes through $(0, 2)$ and		ich of the following is true
ab	Shout ℓ and the circle $(x-2)^2 + (y-1)^2 = 5$	5?	
	A. ℓ is tangent to circle at $(0, 2)$.		
	B. ℓ is tangent to the circle at some point p	, where $p \neq (0, 2)$.	
	C. ℓ Intersects the circle at exactly two points	its.	
	D. The distance between ℓ and the center of		
223.	Suppose $\vec{A} = 3i - 4j$ and \vec{B} is a vector in the	e xy-plane such that the a	angle between \vec{A} and \vec{B} is $\frac{\pi}{3}$. \vec{u}
is	a unit vector in the direction of \vec{B} , then \vec{A} . (\vec{A}		3
	A. 20 B. 5	C. 15	D. 30
	2007		
224.	If $A = (1, -2)$, $B = (-3, 2)$ and \vec{V} is a posi	tion vector such that $2V$ -	$+AB = 0$, then \vec{V} is equal to:
		C. $(-2,2)$	
225.	If $\vec{A} = 4i - 3j$ and \vec{u} is a unit vector such t	that $ \vec{A} + u ^2 = 27$, then	the cosine of the angle between
	and \vec{u} is equal to		-
	A. 0.1 B. 0.2	C. 0.3	D. 0.4
226.	What is the image of the ellipse $(x-1)^2 +$	$4y^2 = 1$ under the transl	ation that takes $(1, 1)$ and $(0, 2)$

C. $x^2 + 4(y+1)^2 = 1$ D. $4x^2 + (y+1)^2 = 1$

followed by the reflection through the x-axis? A. $x^2 + 4(y - 1)^2 = 1$ B. $4x^2 + (y - 1)^2 = 1$

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			en a force of 50N is used to p	oull a crate 20m along a level pa	ath
if	the force is at an ang			5	
	A. 360	B. 500	C. 760	D. $1500\sqrt{2}$	
228.	The image of a figu	are with vertices A(1, 2), $B(3, 6) C(-1, 2)$ and I	O(-2, -2) after reflection across	SS
th	e x-axis is:				
	A. $A'(1,-2)$, $B'($	•			
	B. $A'(1,-2)$, $B'($				
	C. A' $(-1,2)$, B' $($				
220	D. A'(1, -2), B'(1
			distinct points in the coordin	nate plane, then which one of the	ne
10	ollowing is equal to \overrightarrow{A} . \overrightarrow{AB}	B. $-6\overrightarrow{AB}$	C. $12\overrightarrow{AB}$	$D = 12\overline{4R}$	
220					
230.			\vec{A} and $ \vec{A} = 4$, $\vec{A} \cdot \vec{u}$ is equa		
	A. $\frac{1}{4}$	B. 4	2	D. 2	
231.	If \vec{A} and \vec{B} are para			$2\vec{A} $, then $\vec{B} - \vec{A}$ is equal to:	
	A. \vec{A}	B. $-\vec{A}$	$C3\vec{A}$	D. $3\vec{A}$	
232.	What is the translat	tion vector u=(h. k`	so that the equation $x^2 + 2$	$v^2 + 6x - 8v + 15 = 0$ is	
			$x^{2} + 2y^{2} + d = 0$ where d is	-	
	A. $u = (-3, 2)$		C. $u = (-2, 3)$		
	B. $u = (3, 2)$		D. $u = (2, -3)$		
				R, is tangent to a circle at point	t (1,
4)	_	1 —	enter is on the y-axis?	7. / 10	
	A. $\sqrt{5}$	2	C. 2√5	D. $\sqrt{10}$	
234.			$\left \vec{a} + \vec{b} \right = \vec{a} $, then which of		
	A. $2\vec{a} \cdot \vec{b} = \vec{b} \cdot \vec{b}$			$2\vec{a} + \vec{b}$ are parallel	
	_	$d \; ec{b}$ are perpendicul		_	
				$t Q = (4, 0)$. If $\vec{V} = xi + 2j$ is	
pa	rallel to PQ , then when				
	A. $-\frac{6}{5}$	B3	C. $-\frac{2}{5}$	D. 3	
236.	Let ℓ be the line gi	ven by the vector e	quation $(x, y) = (-2, 1) + \lambda$	$l(1,1), \lambda \in \mathbb{R}$. Which one of the	he
				(2, -1) followed by a rotation	
th	rough 45° about the	_		_	
227	-		C. x = 0		
	What is the image one $y = -x$?	of the circle $x^2 + y$	$x^2 - 4x - 6y + 12 = 0$ whe	en it is reflected with respect the	e
1111	A. $(x+3)^2 +$	$(y+2)^2=1$	$(x+2)^2$	$+(y+3)^2=1$	
	B. $(x-2)^2 +$		D. $(x-3)^2$		
238.			under a translation is $2x - 3$	y = 0, which one of the	
fo	llowing is a translat			->	
	A. $u = (2, -1)$		C. $u = (-1)^{n}$		
230	B. $u = (-2, 1)$		D. $u = (1, -60^{\circ})$	-2) ne length of AC and the cosine	of
	A, respectively?	5, DC — 4 and m($\langle D \rangle = 00$, then what are the	ic length of Ac and the cosme	OI
Ì	A. $\sqrt{13}$ and $\frac{1}{\sqrt{1}}$	<u>.</u>	C. $\sqrt{13}$ an	d <u>6</u>	
	•	_	D. $\sqrt{13}$ and	5√13 2d	
	B. $\sqrt{13}$ and $\frac{1}{\sqrt{100}}$	1 3	D. V13 at	$\frac{10}{5\sqrt{13}}$	

ETHIO NATIONAL SCHOOL	MATHEMATICS EUEE QUESTION FROM 2004-2011	E.C.
240. What is the standard equation of the	line passing through the point (2, 3) and parallel to the line	;
given by $\begin{cases} x = 1 + 2\lambda \\ y = -2 - \lambda \end{cases}$, $\lambda \in \mathbb{R}$?		
A. $\frac{x-2}{-1} = \frac{y-3}{2}$	C. $\frac{x-2}{2} = \frac{y-3}{-1}$	
B. $\frac{x-1}{2} = \frac{y-3}{2}$	D. $\frac{x-1}{1} = \frac{y-3}{-2}$	
2 –2	2011	Cand
	se vertices $A=(0, 3)$ and $B=(4, 0)$ and the other vertices, e plane. If its height BC is half of the length of its base, the	
which of the following indicates the co		•
A. $(4, \frac{5}{2})$ B. $(6, \frac{3}{2})$	$C.\left(\frac{5}{2},-2\right) D.\left(\frac{11}{2},2\right)$	
	$+y^2 - 4x - 6x + 11 = 0$ when the origin is shifted to the	point
(1, 1) after translation of axes? A. $x^2 + y^2 - 6x - 8y + 23 =$	0 C. $x^2 + y^2 + 6x + 8y - 23 = 0$	
B. $x^2 + y^2 - 4x - 6y + 3 = 0$		
-	the point $(1,-2)$, then what would be the image of the point	ıt
(2,4)?		
A. $\left(1 - \frac{5\sqrt{2}}{2}, -2 + \frac{7\sqrt{2}}{2}\right)$	$C.\left(\frac{5\sqrt{2}}{2},\frac{7\sqrt{2}}{2}\right)$	
B. $\left(1 - \frac{\sqrt{2}}{2}, -2 + \frac{\sqrt{2}}{2}\right)$	D. $\left(\frac{\sqrt{2}}{2}, \frac{\sqrt{2}}{2}\right)$	
244. Let ℓ be a line given by the equation	$a(x,y) = (1,1) + t(\sqrt{3},1), t \in \mathbb{R}$, what is the equation of	the
	at $(1, 1)$ and then translated by the vector $\mathbf{u} = (-1, 1)$?	
A. $-x + y = 2$	C. $\sqrt{3}x - y = 2$	
B. $x - y = 2$	D. $-x + \sqrt{3}y = 1$	
\underline{U}_{i}	<u>nit 9</u> ₂₀₀₄	
	plified form of $\csc\left(\frac{\pi}{2} - x\right)\cos x - \sin^2 x$?	
A. $2\cos x$ B.cos	S^2 C. $2\sin x$ D. $\sin 2x$	
246. $\cos(\tan^{-1}(0.5))$ is equal to:		
A. $\frac{1}{\sqrt{5}}$ B. $\frac{1}{\sqrt{3}}$	vo vo	
	s station 10km to the south and then changed its course and	
sailed $5 + \sqrt{6}$ km in the direction of N6 station by the shortest route?	60°E. What is the boat should travel in order to return to its	
A. $4\sqrt{6}$ km B. 9 km	m C. $3\sqrt{6}$ km D. 7 km	
200:	5	
248. If $f(x) = 2 - \frac{1}{2}\sin\left(\frac{n}{2}x\right)$, then whic	th of the following is the amplitude and period of f , respect	ively?
A. $\frac{1}{2}$ and 4 B. $\frac{-1}{2}$ a		
249. Which of the following is equal to so	$\operatorname{ec}\left(\frac{\pi}{2}-x\right)\sin^3x+\cos 2x$?	
A. $2\cos x$ B. $2\sin$	(2)	
050 What is 1 1 1 1 2 2 2	1 -4-2 1 : 4 : 1 [0.2.]0	

250. What is the source

A. $\left\{0, \frac{\pi}{4}, \pi, \frac{5\pi}{4}\right\}$ B. $\left\{0, \frac{\pi}{4}, \frac{3\pi}{4}, \pi\right\}$ 251. What is $\cot(\arcsin(x))$ if 0 < x < 1?

A. $\frac{x}{2}$ B. $\frac{\sqrt{1-x^2}}{x}$ 250. What is the solution set of $\cos^2 x + \frac{1}{2}\sin 2x = 1$ in the interval $[0, 2\pi]$?

C. $\{0, \pi\}$

 $D.\left\{0,\frac{\pi}{4},\pi\right\}$

C. $\sqrt{1-x^2}$

D. $\frac{1}{\sqrt{1-x^2}}$

252. Suppose an airplane is descending at a speed of 50 miles per hour at an angle of 30° below the horizontal line. What is the x- and y- components, respectively, of the velocity of the plane?

A. $50\sqrt{3}$, 25

B. $-25,50\sqrt{3}$

C. 25, $-25\sqrt{3}$

D. $-25\sqrt{3}$, -25

 253. An observer on level ground is at a distance 10√3 m from a building. The angle of elevation to bottom of the windows on the second and third floors are 30° and 60°, respectively. What is the distance h between the bottoms of the windows? A. 15m B. 20m C. 15√3m D. 32m 254. If θ = 2arctan (1/2), then which of the following is equal to sec(θ)? 	
A. 15m B. 20m C. $15\sqrt{3}$ m D. 32m	that
254 If $\theta = 2 \arctan\left(\frac{1}{2}\right)$ then which of the following is equal to $\sec(\theta)$?	that
234. If $0 = 2$ arctair $\binom{1}{2}$, then which of the following is equal to sec(0):	that
A. $\frac{25}{3}$ B. $\frac{4}{5}$ C. $\frac{5}{3}$ D. $\frac{5}{4}$	that
255. If angle θ is an acute angle of a right triangle, what is the length of the side adjacent to θ , given the hypotenuse has 6 unit length and $\sec \theta = \frac{10}{3}$?	ınal
A. 1.8 units B. 2 units C. 18 units D. 20 units	iits
256. What is the possible value of x that solves the equation: $\sin^{-1} x + \cos^{-1} \left(\frac{5}{3}\right) = \pi$?	
A. $\frac{\pi}{3}$ B. $\frac{3}{5}$ C. $\frac{5\pi}{2}$ D. $\frac{4}{5}$	
257. Two ships, one with angle of depression 60° due to east and the other with 30° due to west are observed from a plane 1000m above a sea. If the two ships are on the same line, what is the distance between the two ships?	e
A. $\frac{1}{\sqrt{3}}$ 600m B. 2000m C. $500\sqrt{3}$ m D. $\frac{1}{\sqrt{3}}$ 4000r	n
258. What is the amplitude and period, respectively, of the graph of $f(x) = -6 \sin x \cdot \cos x$?	
A. $3, \pi$ B. $6, \pi$ C. $3, \frac{\pi}{2}$ D. $6, 2\pi$	
259. If $\cot(\theta) = 2$, then which of the following is equal to $\csc(\theta)$?	
$\sqrt{5}$ B. $\frac{2}{\sqrt{5}}$ C. $\frac{1}{\sqrt{5}}$ D. $\frac{1}{2}$	
260. What is the amplitude and period, respectively, of the graph of $f(x) = 4 \sin\left(\frac{x}{3}\right) \cos\left(\frac{x}{3}\right)$?	
A. $4, \frac{\pi}{3}$ B. $2, 3\pi$ C. $2, \frac{2\pi}{3}$ D. $4, 3\pi$	
261. A boat on a sea sailed from its station toward North with constant speed of 80 km/hr. Another be	oat
from the same station sailed 60° NE(North East) with constant speed of 100 km/hr. if the two boats state sailing at the same time, what is the straight distance between them after they have sailed for just 30 minutes?	
A. $10\sqrt{42} \text{ km}$ B. 90 km C. $10\sqrt{41} \text{ km}$ D. $10\sqrt{2}$	1 km
262. What is the value of $\arcsin\left(-\frac{\sqrt{2}}{2}\right)$?	
A. $\frac{\pi}{4}$ B. $\frac{\pi}{2}$ C. $-\frac{\pi}{4}$ D. $-\frac{\pi}{2}$	
263. Which one of the following is true?	
A. The amplitude of $f(x) = \sin 3x$ is 3. C. The period of $f(x) = \cos \left(\frac{1}{2}x - \frac{\pi}{3}\right)$ is 4π	
B. The period of $f(x) = 2\sin 4x$ is π D. The amplitude of $f(x) = -5\cos(3x + 2) - 2$ is 7 264. If $\theta = \arctan(2)$, then what is the value of $\sin(2\theta)$?	
A. $\frac{2}{5}$ B. $\frac{4}{5}$ C. $\frac{4}{\sqrt{5}}$ D. $\frac{2}{\sqrt{5}}$	
265. If $\cot \theta = \sqrt{8}$, and θ is in the first quadrant angle, then what is the value of $\csc \theta$?	

 $D.\frac{1}{\sqrt{8}}$ B. 3

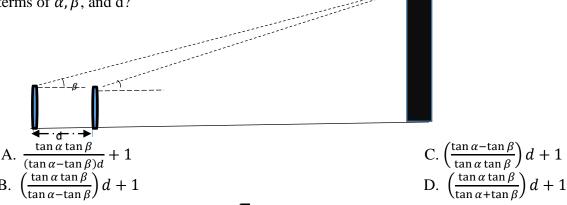
266. A patrol on a sea sailed from its station 7 km to the North; and changed its course and sailed $4\sqrt{2}$ km in the direction of 45° South-East. What is the shortest (straight) distance the boat should travel in order to return to its station?

C. $5\sqrt{2}$ km D. $5 + \sqrt{2} \text{ km}$ A. 5 km B. 7 KM

267. What is the period (p) and the range(R) of $f(x) = 5 \sin(\frac{1}{3}x + 2) + 3$?

C. $p = 6\pi$, R = [-5, 5]D. $p = \frac{2\pi}{3}$, R = [-2, 8]A. $p = 6\pi$, R = [-2, 8]B. $p = \frac{2\pi}{3}$, R = [-5, 5]

268. In order to measure the height of a tower, suppose a surveyor takes two sightings from a transit 1m high which are positioned d meters apart on the same ground level as in the figure below. If the first measured angle is α and the second is β (see, in the figure), then what is the height of the tower (in meter) in terms of α , β , and d?



269. If θ is a fourth quadrant angle and $\sec \theta = \sqrt{2}$ then $\csc \theta$ is equal to? A. $\frac{-1}{\sqrt{2}}$ B. $-\sqrt{2}$ C. $\frac{1}{\sqrt{2}}$

A.
$$\frac{-1}{\sqrt{2}}$$

B.
$$-\sqrt{2}$$

C.
$$\frac{1}{\sqrt{2}}$$

D.
$$\sqrt{2}$$

270. Ship A and B depart from the same point at the same time on the course N60°E and N40°E, respectively. If the speed of ship A is 20 km/hr and the speed of ship b is 30 km/hr, what is the distance between the two ships just after 30 minutes of their departure? (you may take $\cos(40^\circ)$ =

 $0.77, \cos(20^\circ) = 0.94, \sin(20^\circ) = 0.34$

A.
$$\sqrt{40}$$
 km

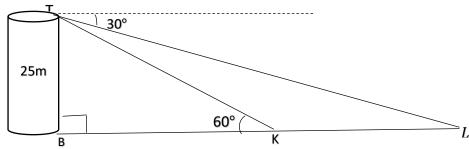
$$B.\sqrt{43}$$

C.
$$\sqrt{50}$$
 km

D.
$$\sqrt{53} \, k$$

271. What is the value of $\cot 270^{\circ} + 2 \cos 90^{\circ} + 4 \sec^2 180^{\circ}$?

272. The diagram below is a representation of 25m vertical observation of tower TB and two cars K and L on a road. The angle of depression from T to car L is 30°. The angle of elevation from car K to the top of the tower is 60°. B, K and L lie in a straight line and lie on the same horizontal plane as the base of the tower.



What is the distance between the two cars?

A.
$$\frac{50\sqrt{3}}{3}$$
 M

B.
$$50\sqrt{3}$$

$$C. \ \frac{50\sqrt{3}}{2} \, m$$

D.
$$50 + \sqrt{3} \text{ m}$$

273. What is the solution set of $\sin^2 x - \sin x \cos x = 0$?

A.
$$\left\{0, \pi, \frac{5\pi}{4}, 2\pi\right\}$$

C.
$$\left\{0, \frac{\pi}{4}, \pi, \frac{5\pi}{4}, 2\pi\right\}$$

D. $\left\{0, \frac{\pi}{4}, \pi, \frac{5\pi}{4}\right\}$

B.
$$\left\{0, \frac{\pi}{4}, \pi, 2\pi\right\}$$

From grade 12

$\frac{Unit \ 1}{2004}$ 274. Let $a_{n=}n + \cos n\pi$, n = 1, 2, 3, ... be the n^{th} terms of a sequence. Then which of the following is

tr	ue?		•		
	A. The fifth to	erm is 6	C. $a_7 + a_8 = 15$		
	B. The 10^{th} t		D. $a_7 - a_6 = 1$		
275.		f the series $\sum_{n=0}^{\infty} (2^2 3^{2-})$			
_,,,	A. 6	B. 18	C. 27	D. ∞	
276.			t term $A_1 = 5$ and the fifth term		1
	$\lim_{n=1}^{30} A_n$ is equal			21, men me partie	••
50	A. 760	B. 780	C. 860	D. 870	
277			Birr 3,000 at the end of each		
			the starting amount of the bu		
,	A. 47,000	B. 50,000	C. 53,000	D. 56,000	
	,	,	2005	•	
278.			$1 a_{n+1} = a_n + 4 \text{ for all } n \ge 1,$		
	A. 2460	B. 2458	C.2450	D. 2442	
279.		term of the sequence 3, 1			
	A. 310	B. 346	C. 510	D. 531	
280.	What is the sum o	f the series $\sum_{n=1}^{\infty} \left(\frac{2^{2n+1}}{5^{n-1}} \right)$)?		
200.	What is the sain o				
	A. 40	B. 20	C. 10	D. 8	
281.	The population of	certain country is 80 mil	llion with growth rate of 2%	per year.	
	Cit	$ven (0.02)^9 = 5.12 \times 10^{-1}$	16	$(1.02)^9 = 1.19$	
	GIV	•			
		$(0.02)^{10} = 1.024 \times 10$)-17,	$(1.02)^{10} = 1.22$	
W	hich of the followi	ng is the best approxima	tion of the population (in mi	llion) after 10 years?	
	A. 81.9	B. 86.8	C. 95.2	D. 97.6	
202	XXII : 1 . C.1	C 11	2006		
282.		following represents a ge	-		
	A. $3, 1, \frac{1}{3}, \frac{1}{9}, \frac{1}{2}$	- 7,	C. 1, 3, 6, 10, 15,	•••	
	A. $3, 1, \frac{1}{3}, \frac{1}{9}, \frac{1}{2}$ B. $\frac{1}{2}, -\frac{1}{3}, \frac{1}{4}, -\frac{1}{3}$	$-\frac{1}{5}, \frac{1}{6}, \dots$	D3, 6, -9, 12,	-15,	
202	2 3 4	of the sum $\sum_{n=1}^{\infty} \left(\frac{2^{n}}{1}\right)^{n}$	+5 ⁿ \		
283.	What is the value	of the sum $\sum_{n=1}^{\infty} \left(\frac{1}{n} \right)^{n}$	$\overline{0^n}$)		
	A. 0.325	B. 1	C. $\frac{5}{4}$	D. $\frac{37}{9}$	
	11. 0.323	D. 1	C. ₄	D. 9	
204	Wile of the same of	f the series ∇^{∞} (1) n	(2)-2n 9		
284.		f the series $\sum_{n=1}^{\infty} (-1)^n$		1	
	A. $-\frac{1}{8}$	B. -0.13	C0.1	D. $\frac{1}{8}$	
		2007		· ·	
285.		following is an arithmeti	•		
	A. 3, 5, 7, 11,		C3, 6, -9,		
• • •	B. 3, 6, 12, 24		D. 1, 3, 6, 10,		
286.	_		s. There are 20 seats in the fin		
rc			w many seats are there on the		l?
205	A. 46	B. 58	C. 760	D. 5240	
287.		f all multiples of three be		D # 166	
200	A. 7,227	B. 6,570	C. 6,150	D. 5, 166	
288.			to a height of 16m. Each tim		
		=	s every height of h twice, wh	at is the total vertical dista	nce
tr	•	before it comes to rest?	C 160	D 220	
	A. 40m	B. 80m	C. 160m	D. 320m	

: 4		metic sequence such that its	s 1^{3i} term $A_1 = -5$ and its 5	tn term $A_5 = 15$, then
10	s 11^{th} term A_{11} is equa A. 40	B. 50	C. 45	D. 55
290.		multiples of 4 that are bet		D < 000
201	A. $12,882$	B. 11,288 equence:1, -4, 9, -16, is:	C. 6,288	D. 6, 882
291.	A. $a_n = (-2)^n$	equence.1, -4, 9, -10, is.	$C_{n} = (-1)^{2n} n^2$	
	B. $a_n = (-1)^n n$.2	C. $a_n = (-1)^{2n} n^2$ D. $a_n = (-1)^{n-1} n^2$	
292.	The sum of $\sum_{n=0}^{\infty} 5$ ($\left(\frac{2}{3}\right)^n$ is		
	A. 0	B. 15	C. $\frac{10}{3}$	D. 5
293.	Suppose a radioactive	material loses one-third of	f its mass per year. If its curre	ent mass is 81 gram,
		nass (in gram) just after 7 y		400
	A. 27	B. $\frac{1}{27}$ ag is the sum of the series 5	C. $\frac{128}{27}$	D. $\frac{128}{81}$
294.	Which of the followin	g is the sum of the series 5	$5 - \frac{10}{2} + \frac{20}{2} - \frac{40}{27} + \cdots$?	01
	11. 5	D . 3	C. 3	D. 5
295.	What is the sum of $\sum_{n=0}^{\infty} A_n = \frac{29}{30}$	$\sum_{n=1}^{30} (-1)^n \left(\frac{1}{n} + \frac{1}{n+1}\right)$		
	$A_{1} - \frac{29}{1}$	$-n=1$ B $\frac{29}{}$	C. $\frac{30}{31}$	D. $-\frac{30}{31}$
296.	50		juence: $-10, -3, 4, 11, \dots$?	31
270.	A. $a_n = a_{n-1} - 8$		C. $a_n = a_{n-1} - 7$	
	B. $a_n = a_{n-1} + 7$	7	D. $a_n = a_{n-1} + 8$	
297.	What is the value of A . $\frac{17}{20}$	$\sum_{n=2}^{20} \left(\frac{1}{n-1} - \frac{1}{n}\right) ?$	24	40
	A. $\frac{17}{20}$	B. $\frac{23}{20}$	C. $\frac{21}{20}$	D. $\frac{19}{20}$
298.		-	rate of 3% per year. If the p	opulation was 100,000
		will be the population in 20		2.50
((Fiven: $(1.03)^{7} = 1.30$, A. $134,000$	$(1.30)^{10} = 134, (1.30)^{10}$ B. 130,000	$(3)^9 = 10.60, (1.3)^{10} = 10.60, (1.3)^{10$	3.78) D. 1,378.000
299	*	D. 130,000		
		ree consecutive terms of a		
1S			n arithmetic sequence is $\{A_n\}$	with $A_n > 0$ for all n,
	9 and the sum of their A. $n^2 + 1$	squares is 35, then what is B. $n^2 - 1$		with $A_n > 0$ for all n,
	9 and the sum of their A. $n^2 + 1$	squares is 35, then what is B. $n^2 - 1$	n arithmetic sequence is $\{A_n\}$ the sum s_n of the first n term	with $A_n > 0$ for all n, as?
	9 and the sum of their	squares is 35, then what is B. $n^2 - 1$ e series $\sum_{n=1}^{\infty} (3^n 4^{-n})$	n arithmetic sequence is $\{A_n\}$ the sum s_n of the first n term	with $A_n > 0$ for all n, as?
300.	9 and the sum of their A. $n^2 + 1$ What is the sum of the A. ∞	squares is 35, then what is B. $n^2 - 1$ e series $\sum_{n=1}^{\infty} (3^n 4^{-n})$ B. $\frac{3}{16}$	n arithmetic sequence is $\{A_n\}$ the sum s_n of the first n term C. n^2	e, with $A_n > 0$ for all n, as? D. $2n^2 + 1$
300.	9 and the sum of their A. $n^2 + 1$ What is the sum of the A. ∞ If $a_1 = 2$, $a_2 = 6$, a_3	squares is 35, then what is B. $n^2 - 1$ e series $\sum_{n=1}^{\infty} (3^n 4^{-n})$ B. $\frac{3}{16}$ $= 10, a_4 = 14,, then \sum_{n=1}^{\infty} (3^n 4^{-n})$	n arithmetic sequence is $\{A_n\}$ the sum s_n of the first n term C. n^2	e, with $A_n > 0$ for all n, as? D. $2n^2 + 1$ D. 4
300. 301.	9 and the sum of their A. $n^2 + 1$ What is the sum of the A. ∞ If $a_1 = 2$, $a_2 = 6$, a_3 A. 20,020	squares is 35, then what is B. $n^2 - 1$ e series $\sum_{n=1}^{\infty} (3^n 4^{-n})$ B. $\frac{3}{16}$ = 10, $a_4 = 14,$, then $\sum_{n=1}^{\infty} (3^n 4^{-n})$ B. 20,200	n arithmetic sequence is $\{A_n\}$ the sum s_n of the first n term C. n^2 C. 3 $C_n = 0$ C_n	p, with $A_n > 0$ for all n, as? D. $2n^2 + 1$ D. 4
300. 301. 302.	9 and the sum of their A. $n^2 + 1$ What is the sum of the A. ∞ If $a_1 = 2$, $a_2 = 6$, a_3 A. 20,020 Every day a person sale we the total amount of	squares is 35, then what is B. $n^2 - 1$ e series $\sum_{n=1}^{\infty} (3^n 4^{-n})$ B. $\frac{3}{16}$ = 10, $a_4 = 14,$, then $a_4 = 14$ B. 20,200 ves 5 cents more than the a 3225 cents by the end of 36	n arithmetic sequence is $\{A_n\}$ the sum s_n of the first n term C. n^2	t, with $A_n > 0$ for all n, as? D. $2n^2 + 1$ D. 4 D. 22,000 ous day. His target is to
300. 301. 302. sa	9 and the sum of their A. $n^2 + 1$ What is the sum of the A. ∞ If $a_1 = 2$, $a_2 = 6$, a_3 A. 20,020 Every day a person sale the total amount of a ving to meet the target A. 35	squares is 35, then what is B. $n^2 - 1$ e series $\sum_{n=1}^{\infty} (3^n 4^{-n})$ B. $\frac{3}{16}$ = 10, $a_4 = 14,$, then $\sum_{n=1}^{\infty} (3^n 4^{-n})$ B. 20,200 ves 5 cents more than the a 3225 cents by the end of 36? B. 25	the sum s_n of the first n term C . n^2 C. 3 C C C C C C C	t, with $A_n > 0$ for all n, as? D. $2n^2 + 1$ D. 4 D. 22,000 tous day. His target is to st to be the starting D. 60
300. 301. 302. sa	9 and the sum of their A. $n^2 + 1$ What is the sum of the A. ∞ If $a_1 = 2$, $a_2 = 6$, a_3 A. 20,020 Every day a person sale the total amount of a ving to meet the target A. 35	squares is 35, then what is B. $n^2 - 1$ e series $\sum_{n=1}^{\infty} (3^n 4^{-n})$ B. $\frac{3}{16}$ = 10, $a_4 = 14,$, then $\sum_{n=1}^{\infty} (3^n 4^{-n})$ B. 20,200 ves 5 cents more than the a 3225 cents by the end of 36? B. 25	the sum s_n of the first n term C . n^2 C. 3 C C C C C C C	t, with $A_n > 0$ for all n, as? D. $2n^2 + 1$ D. 4 D. 22,000 tous day. His target is to st to be the starting D. 60
300. 301. 302. sa sa 303.	9 and the sum of their A. $n^2 + 1$ What is the sum of the A. ∞ If $a_1 = 2$, $a_2 = 6$, a_3 A. 20,020 Every day a person sale the total amount of a ving to meet the target A. 35	squares is 35, then what is B. $n^2 - 1$ e series $\sum_{n=1}^{\infty} (3^n 4^{-n})$ B. $\frac{3}{16}$ $= 10, a_4 = 14,$, then $\sum_{n=1}^{\infty} (3^n 4^{-n})$ B. 20,200 ves 5 cents more than the a 3225 cents by the end of 36? B. 25 terms of a geometric program	the sum s_n of the first n term C . n^2 C . a C C C C C C C	t, with $A_n > 0$ for all n, as? D. $2n^2 + 1$ D. 4 D. 22,000 tous day. His target is to st to be the starting D. 60
300. 301. 302. sa sa 303.	9 and the sum of their A. $n^2 + 1$ What is the sum of the A. ∞ If $a_1 = 2$, $a_2 = 6$, a_3 A. 20,020 Every day a person sale the total amount of a ving to meet the target A. 35 If the second and fifth the first eight terms of $\frac{85}{1000}$	squares is 35, then what is B. $n^2 - 1$ e series $\sum_{n=1}^{\infty} (3^n 4^{-n})$ B. $\frac{3}{16}$ $= 10$, $a_4 = 14$,, then $\sum_{n=1}^{\infty} (3^n 4^{-n})$ B. 20,200 ves 5 cents more than the asset of 3225 cents by the end of 36? B. 25 terms of a geometric program of the sequence?	the sum s_n of the first n term C . n^2 C. 3 C. 3 $a_{n=1}^{100}$ $a_{n} = \dots$ $a_{n=1}^{100}$ $a_{n} = \dots$	b, with $A_n > 0$ for all n, as? D. $2n^2 + 1$ D. 4 D. 22,000 Out day. His target is to st to be the starting D. 60 ctively, what is the sum
300. 301. 302. sa sa 303.	9 and the sum of their A. $n^2 + 1$ What is the sum of the A. ∞ If $a_1 = 2$, $a_2 = 6$, a_3 A. 20,020 Every day a person sale the total amount of a ving to meet the target A. 35 If the second and fifth the first eight terms of $\frac{85}{1000}$	squares is 35, then what is B. $n^2 - 1$ e series $\sum_{n=1}^{\infty} (3^n 4^{-n})$ B. $\frac{3}{16}$ $= 10$, $a_4 = 14$,, then $\sum_{n=1}^{\infty} (3^n 4^{-n})$ B. 20,200 ves 5 cents more than the asset of 3225 cents by the end of 36? B. 25 terms of a geometric program of the sequence?	the sum s_n of the first n term C . n^2 C. 3 C. 3 $a_{n=1}^{100}$ $a_{n} = \dots$ $a_{n=1}^{100}$ $a_{n} = \dots$	t, with $A_n > 0$ for all n, as? D. $2n^2 + 1$ D. 4 D. 22,000 tous day. His target is to st to be the starting D. 60
300. 301. 302. sa sa 303.	9 and the sum of their A. $n^2 + 1$ What is the sum of the A. ∞ If $a_1 = 2$, $a_2 = 6$, a_3 A. 20,020 Every day a person sale the total amount of a ving to meet the target A. 35 If the second and fifth the first eight terms of $\frac{85}{1000}$	squares is 35, then what is B. $n^2 - 1$ e series $\sum_{n=1}^{\infty} (3^n 4^{-n})$ B. $\frac{3}{16}$ $= 10$, $a_4 = 14$,, then $\sum_{n=1}^{\infty} (3^n 4^{-n})$ B. 20,200 ves 5 cents more than the asset of 3225 cents by the end of 36? B. 25 terms of a geometric program of the sequence?	the sum s_n of the first n term C . n^2 C. 3 C. 3 $a_{n=1}^{100}$ $a_{n} = \dots$ $a_{n=1}^{100}$ $a_{n} = \dots$	t, with $A_n > 0$ for all n, as? D. $2n^2 + 1$ D. 4 D. 22,000 Out day. His target is to st to be the starting D. 60 Ctively, what is the sum D. $\frac{256}{255}$
300. 301. 302. sa sa 303.	9 and the sum of their A. $n^2 + 1$ What is the sum of the A. ∞ If $a_1 = 2$, $a_2 = 6$, a_3 A. 20,020 Every day a person sale the total amount of a ving to meet the target A. 35 If the second and fifth the first eight terms of $\frac{85}{1000}$	squares is 35, then what is B. $n^2 - 1$ e series $\sum_{n=1}^{\infty} (3^n 4^{-n})$ B. $\frac{3}{16}$ $= 10, a_4 = 14,$, then $\sum_{n=1}^{\infty} (3^n 4^{-n})$ B. 20,200 ves 5 cents more than the a 3225 cents by the end of 36? B. 25 terms of a geometric progential for the sequence?	the sum s_n of the first n term C . n^2 C. 3 C. 3 $a_{n=1}^{100}$ $a_{n} = \dots$ $a_{n=1}^{100}$ $a_{n} = \dots$	b, with $A_n > 0$ for all n, as? D. $2n^2 + 1$ D. 4 D. 22,000 Out day. His target is to st to be the starting D. 60 ctively, what is the sum

305.	Which of the following is equal to $\lim_{n\to\infty}$	$\frac{3\sqrt{n}-6n+5}{4n+1}?$	
	A. $-\frac{3}{2}$ B. 0	C. $\frac{3}{4}$	D. $\frac{5}{4}$
306.	$\lim_{x\to 0} \frac{x \csc 3x}{x+1}$ is equal to:		
	A. $\frac{1}{3}$ B. 0	C. 1	D. 3
307.	$\lim_{x\to\infty} \left(1+\frac{1}{x}\right)^{2x+4}$ is equal to:		
	A. e B. e^2 $\lim_{x\to 1^-} \frac{x^4-1}{ x-1 }$ is equal to:	C. <i>e</i> ⁴	D. ∞
308.	$\lim_{x\to 1^-} \frac{x^{x-1}}{ x-1 }$ is equal to:		
	A. 4 B. 0	C1	D4
309.	Let $f(x) = \begin{cases} \frac{a}{x^2 + 1}, & \text{if } x \le 1\\ \frac{x - 1}{\sqrt{x} - 1}, & \text{if } x > 1 \end{cases}$ what is the	value of a if f is continuous at	x= 1?
	A. 0 B. 0	C. 4	D. 8
310	What is the value of $\lim_{x\to\infty} \left(1+\frac{1}{x}\right)^{-\frac{x^2}{2}}$?	5	
310.	1	C. e ⁻²	D. ∞
211	A. $\frac{1}{\sqrt{e}}$ B. \sqrt{e}	C. 6	Д. ॐ
311.	$\lim_{n\to\infty} \frac{1-n-3n^2}{6n^2+1}$ is equal to:	~ 1	_
	A. $\frac{1}{6}$ B. $-\frac{1}{2}$	C. $-\frac{1}{6}$	D. −∞
312.	A. $\frac{1}{6}$ B. $-\frac{1}{2}$ Let $(x) = \begin{cases} 3^{x} + k, & x \le 0 \\ 3\frac{\sin(2x)}{x}, & x > 0 \end{cases}$, if f is cont	inuous at $x = 0$, then what is t	he value of k?
	A. 6 B. 5	C. 2	D. 0
313.	Which of the following is equal to $\lim_{x\to x} x ^2$	$\rightarrow 1 \frac{\sqrt{x-1}}{x^2-1}$?	
	A. ∞ B. $\frac{1}{2}$	C. $\frac{1}{4}$	D. 0
314.	Which of the following is equal to $\lim_{x\to a} \frac{1}{x}$	$\frac{1-x}{1-\frac{1}{2}}$?	
	A. 1 B.0	C. $-\frac{1}{2}$	D. Doesn't exist
315.	The sequence $\left\{\frac{(n-1)(2n+1)}{1-n^2}\right\}_{n=1}^{\infty}$ converges	s to:	
	A. $-\infty$ B. -2	C. 0	D. 1
316.	Given that $\lim_{x\to 3} f(x) = 5$ and $\lim_{x\to 3} f(x) = 5$	g(x) = 11, what is the value of	of $\lim_{x\to 3}$
$\left(\frac{\cdot}{2}\right)$	$\frac{f(x) - g(x))(g(x) - 2f(x))}{g(x)^2 - f(x)^2}$?		
`	A. $-\frac{66}{96}$ B. $-\frac{1}{16}$	C. 0	D. Doesn't exist
317.	Let $f(x) = \begin{cases} a \frac{\sin x}{x - x }, & x < 0 \\ e^{-x} + \cos x, & x \ge 0 \end{cases}$ if f is	continuous at $x = 0$ then who	at is the value of a^{9}
	$(e^{-x} + \cos x, \ x \ge 0)$	1	
	A. 4 B.2	C. $-\frac{1}{2}$	D4
318.	If $a_n = \left(\frac{n+3}{n+1}\right)^n$, then the limit of the sequ	uence $\{a_n\}_{n=1}^{\infty}$ is equal to:	
	A. 1 B. $\frac{1}{2}e$	C. <i>e</i> ²	D. +∞
319.	Which of the following is equal to $\lim_{x\to a}$		
	A. e^6 B. e^{-3}	C. $e^{\frac{-3}{2}}$	D. e^{-6}
320.	Which of the following sequences is a co	onvergent sequence?	_
	A. $1, \frac{1}{2}, 1, \frac{1}{3}, 1, \frac{1}{4}, \dots$	C. $\left\{ 100^{109} - \frac{1}{100} n \right\}_{n}^{\circ}$	o 1=1

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B.
$$\{(-1)^n\}_{n=1}^{\infty}$$

D.
$$\left\{\sin\left(\frac{1}{n}\right)\right\}_{n=1}^{\infty}$$

321. Let $f(x) = \begin{cases} a \frac{\sin 2x}{x}, & \text{if } x < 0 \\ e^{2x} - 2, & \text{if } x \ge 0 \end{cases}$ if f is continuous at x = 0, then what is the value of a?

A.
$$\frac{1}{2}$$

C.
$$-\frac{1}{2}$$

A. $\frac{1}{2}$ B. 2 C. $-\frac{1}{2}$ 322. Which one of the following is equal to $\lim_{x\to 9} \frac{x-9}{3-\sqrt{x}}$?

$$D \propto$$

A. 6 B. -3 C. -6 D. ∞ 323. Let $f(x) = \begin{cases} 3 - e^{2x}, & \text{if } x < 0.5 \\ \frac{2^{x} - 5}{x + 1}, & \text{if } x \ge 0.5 \end{cases}$ if c is a zero of f, that is f(c) = 0, then which one of the

following intervals must contain c?

A.
$$(-\infty,0]$$

324. Which one of the following is equal to $\lim_{x\to\infty} \left(\frac{3x}{3x+2}\right)^{-3x}$ A. e^2 B. e^{-3} C. e^{-2}

A.
$$e^2$$

B.
$$e^{-3}$$

C.
$$e^{-2}$$

D.
$$e^3$$

325. The left hand side limit, $\lim_{x\to 0^-} \frac{xe^x - |x|}{x}$ is equal to:
A. 0
B. 2

D. Doesn't exist

A. 0 B. 2 C. 1 326. Which one of the following is equal to $\lim_{x\to 0} \frac{C. 1}{x \sec x}$?

327. In which interval the sequence $\left\{\frac{(-1)^n}{3n}\right\}_{n=1}^{\infty}$ is bounded?

A.
$$\left[\frac{-1}{9}, \frac{1}{12}\right]$$

B.
$$\left[\frac{-1}{3}, \frac{1}{6}\right]$$

C.
$$\left[\frac{-1}{6}, \frac{1}{3}\right]$$
 D. $\left[\frac{-1}{12}, \frac{1}{9}\right]$

D.
$$\left[\frac{-1}{12}, \frac{1}{9}\right]$$

328. Which one of the following is true about the function $(x) = \begin{cases} \frac{x^2}{x}, & x \neq 0 \\ 0, & x \neq 0 \end{cases}$?

A. f is continuous except at x = 0

C. *f* is continuous everywhere

B. f has an infinite discontinuity at x = 0

D. f has a vertical asymptote at x = 0

329. $\lim_{x\to\infty} x \sin\frac{1}{x}$ is equal to:

D. -1

330. Which one of the following is a convergent sequence?

A.
$$\{(\frac{5}{2})^n\}$$

$$B \cdot \left\{ \frac{n^2}{n+1} \right\}$$

C.
$$\left\{\frac{2n}{n+1}\right\}$$

D.
$$\left\{ \frac{(-1)^n}{2} \right\}$$

331. What is the value of k so that $f(x) = \begin{cases} \frac{\tan(2x)}{x}, & \text{if } x > 0 \\ k - e^{2x}, & \text{if } x \le 0 \end{cases}$ is continuous at x = 0?

A. 2

B. 3

332. If f is continuous at x = 0 and $g(x) = \sqrt{x} \left(2f(x) + \frac{3}{\sqrt{x}} \right)$ for all x > 0, then what is the value of $\lim_{x\to 0^+} g(x)$?

D. 5

333. What is the value of $\lim_{x\to 0} \frac{\sin x \cos 2x}{x^2+3x}$?

D. 2

334. If $a \neq 0$, then what is the value of $\lim_{x \to a} \frac{x^2 - a^2}{x^4 - a^4}$?

D. 0

335. Which one of the following is a convergent sequence?

A.
$$\left\{ \frac{1+2^n}{2^n} \right\}$$

B.
$$\left\{ \frac{1}{n} + \sin(n) \right\}$$
 C. $\left\{ \frac{1-3^n}{2^n} \right\}$

C.
$$\left\{ \frac{1-3^n}{2^n} \right\}$$

D.
$$\left\{ \frac{(-1)^n}{2} \right\}$$

336. What are the greatest lower bound and the least upper bound of the sequence $\left\{(-1)^n\left(1+\frac{1}{n}\right)\right\}$, respectively?

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A.
$$-2$$
 and 2
B. $-\frac{3}{2}$ and 2
C. -2 and $\frac{3}{2}$
D. -2 and $-\frac{3}{2}$
337. What is the value of $\lim_{x\to 0} \frac{1}{x^2} \sin^2\left(\frac{x}{2}\right)$?
A. $\frac{1}{2}$
B. $\frac{1}{4}$
C. 2
D. 4
338. What are the values of a and b so that the function $\begin{cases} x+1, & x<1\\ ax+b, & 1\leq x<2 \end{cases}$ is continuous everywhere?

A. $a=4,b=-2$
B. $a=-4,b=-2$
C. $a=4,b=2$
B. $a=-4,b=2$
D. $a=-4,b=2$
339. If $f(x)=\frac{|x|}{x}$ and $g(x)=\frac{x+2}{x^2-4x}$, then what is the value of $\lim_{x\to-2} f(x)+g(x)$?
A. $-\frac{9}{8}$
B. ∞
C. $\frac{2}{9}$
D. $-\frac{7}{8}$
340. Let $\{a_n\}$ be a sequence with $a_1=a,a_2=f(a_1)=f(a_1)=f(a),a_3=f(a_2)=f(f(a)),...,a_{n+1}=f(a_n),x_n$ where f is continuous function. If $\lim_{n\to\infty} \sum_{k=1}^n \left[\frac{2}{n}\left(\frac{2k}{n}\right)^3+5\left(\frac{2k}{n}\right)\right]$
A. 4
B. 14
B. 14
C. 10
D. 18
341. What is the value of $\lim_{n\to\infty} \sum_{k=1}^n \left[\frac{2}{n}\left(\frac{2k}{n}\right)^3+5\left(\frac{2k}{n}\right)\right]$
A. 4
B. 10
C. 10
D. 18
342. What is the greatest lower bound of the sequence $\left\{(-1)^n \frac{1}{n+1}\right\}_{n=1}^\infty$?
A. 1
B. 0
C. 10
D. 10
D. 10
C. 10
D. 10
D.

349. If $f(x) = \pi^2$, then f'(x) is equal to:

C. 1 D. 0

350. Let $(x) = \frac{6x}{x+a}$. For value of *a* is f'(a) = 1?

 $B.\frac{2}{3}$ D. 3

351. If $g(x) = \frac{f(x)}{x+1} + (f(x))^2$, f(1) = 8 and f'(1) = 2, then g'(1) is equal to: D. 16

352. If $f(x) = xe^{3x} - \cos(2x)$, then f''(0) is equal to:

	A. 0	B. 2	C. 6	D. 10	
353.	If $f(x) = x^2 +$	$2 \ln x$, then what is	$\lim_{h \to 0} \frac{f(2+h) - f(2)}{h} ?$		
	A. 5		$C. 2^h$	D. 0	
354.		$+x-3\cos(x)$, then	of $f''(x)$ is equal to:		
	A. $e^{2x} + 1 - 3$	$3\sin(x)$	C. $4e^{2x} - 3c$ D. $4e^{2x} + 3$	$\cos(x)$	
255	B. $e^{2x} + 1 + 3$				a avval to a /(m)?
333.	g(x) = xf(x) A. 11			which of the following is D. 0	equal to $g(x)$?
356				line to the graph of $f(x)$	$a = \frac{1}{1} + \cos x$ at
	f(0)?	ie rono wing is the ex	quation of the tangent	Time to the graph of f (x)	x+1
(0	A. $x + y = 1$		C. $x + y = 2$		
	B. $x - y = -2$		D. $x + 4y = 2$		
		-	about the derivative of		
A.	f is not differe			$2x$, for every $x \in (-\infty, \infty)$ $ x + x$, for every $x \in (-\infty)$	
			2006		
358.	If $f(x) = \frac{x^2}{1 + xg(x)}$	$\frac{1}{(x)}$, $g(2) = 1$ and $g'(2) = 1$	(2) = 10, then which	h of the following is equa	ol to $f'(2)$?
	A8	$B\frac{8}{9}$	C. $\frac{4}{3}$	D. $\frac{8}{9}$	
		,	we of $f(x) = \frac{1+\sin x}{\cos x}$ i	•	
	A. $\sec x + \tan x$	$x B.\frac{1+\sin x}{2}$	C. $\frac{1}{1+\tan x}$	D. $\frac{\cos x}{\cos x}$	
		τος χ	$1 + tan \lambda$	$\sin^2 x$ ne to the graph of f at $x = 1$	= 2?
500.	A. -4	B. 2	C. 18	D. 17	2.
361.		in x , then $f''(x)$ is			
	A. $3e^{2x} \sin x - \frac{1}{2}e^{-2x} \sin x$	$-4e^{2x}\cos x$	C. $e^{2x}(3\sin x +$	$4\cos x$	
			D. $e^{2x}(4\sin x - e^{2x})$	$3\sin x$	
362.), then the simplified	ux		
	A. $-6\sin(3x^2)$)	C. $6\cos(3x^2)$ – D. $x^2\cos(3x^2)$	$-36x^2 sin(3x^2)$	
262				$+ 6\sin(3x^2)$ = 4, g(1) = -5, and g'	(1) = 1 than what
	the value of $F'(t)$		$\min_{j} (2) = -3, j (2)$	y = 4, y(1) = -3, and y	(1) = 1, then what
15	A40		C. 0	D. 19	
364	If $f(x) = \ln(\sqrt{x})$		2007 ne following is equal t	f'(x)?	
	`	•	C. $\frac{2x}{\sqrt{x^2+1}}$		
	.,,,		1,70 . =	0 = 4, g(1) = -5, and g'	(1) = 1 than what
	the value of $F'(t)$		$\min_{j} (2) = -3, j (2)$	y = 4, y(1) = -3, and y	(1) = 1, then what
15	•	B20	C. 0	D. 19	
				f(x)f(y) for all values of	
f(esents the formula for the	derivative $f'(x)$?
	A. $f'(x) = 2f$	• •	C. $f'(x) =$ D. $f'(x) = 2$		
	$B. \ f'(x) = f(x)$				
367.	For what value	of a and b is the fun	$action f(x) = \begin{cases} 1 - 3x \\ ax + 3x \end{cases}$	x^2 , $for x \le 1$ b, $for x > 1$ differential	able at $x = 1$?
	A. $a = 6, b =$		C. $a = 0, b$	= -2	
	B. $a = -3, b =$	= 1	D. $a = -6$,	b = 4	

368.	If $f(x) = 2x^5 - 3x$, then $\lim_{x \to 1} \frac{f(x) - 3x}{x - 3x}$	$\frac{f(1)}{1}$ is equal to:	
	A. 1 B1		D. ∞
369.	If $f(x) = e^{3x} \cos x - \frac{x+\pi}{x^2+2}$, then $f'(0)$		
	A. $3 - \frac{\pi}{2}$ B. $\frac{3}{2}$		
370.	If $f(x) = \ln(\sqrt{x^2 - 5})$, which one of t	=	——————————————————————————————————————
	A. $\frac{x}{x^2-5}$ B. $\frac{-x}{\sqrt{x^2-5}}$	C. $\frac{2x}{\sqrt{x^2-5}}$	
371	$\frac{d}{dx}(\ln e^{2x}) \text{ is equal to:}$	$\sqrt{x^2-5}$	x ² -5
371.	A. $\frac{1}{e^{2x}}$ B. $\frac{2}{e^{2x}}$	C. 2x	D 2
372	C		D. 2 a derivative $f'(x)$ at $x = 32$
312.	If $f(x) = 2 + x - 3 $ for all x, then w A1 B. 1	C. 2	D. does not exist
373.	Let f be a differentiable function with	f(1) = -1 and f'(1)	$f(x) = 1$. If $g(x) = [f(2x + 1) + 2]^2$, then
	hat is the value of $g'(x)$?	f(1) = 1 and f(1)	f = 1. If $g(x) = f(2x + 1) + 2f$, then
	A. 4 B. 2		D4
374.	If $(x) = \ln(x^2 + 2)$, then what is the	_	2
	A. $\frac{3}{2}$ B. $\frac{5}{9}$	C. $\frac{2}{3}$	D. $\frac{2}{9}$
375.	If $x^2 + xy = 10$, then what is the value	e of $\frac{dy}{dx}$ when $x = 2$?
	A. $-\frac{7}{2}$ B. $\frac{2}{7}$	C. $\frac{3}{2}$	D. $\frac{7}{2}$
376.	What is the equation of the tangent line	e to the graph of $f(x)$	$=3x^{2}+4x-5$ at $(1,2)$?
	A. $10x - y - 8 = 0$	C. $-10x - y -$	
277		D. $10x + y - 8$	= 0
311.	If $f(x) = \pi^2 + 1$, then what is the value A. $2\pi + 1$ B. 2π	$\begin{array}{c} \text{ce of } f(x) : \\ \text{C. 2} \end{array}$	D. 0
270		2010	
3/8.	If a function f is differentiable at a , the A. $f(a)$ B. $f'(a)$		
379.	What is the slope of the tangent line to		
	A. 2 B. 3	C. 5	D. 4
380.	If $f(x) = k \ln x + e^{\sin x}$ and $f''(x) =$		
201	A. $2\pi^2$ B. π^2	C. π	D. 2π
361.	Let $f(x) = \ln(x\sqrt{x})$. Then $f'(x)$ is eq	_	5 3
	A. $\frac{2x}{3}$ B. $\frac{\sqrt{x}}{2}$	C. $\frac{2}{x\sqrt{x}}$	D. $\frac{3}{2x}$
382.	Which one of the following is equal to		
	A. $\frac{1}{2x \ln(2)}$ B. $\frac{3}{2x \ln(2)}$	C. $\frac{3x}{2 \ln(2)}$	D. $\frac{1}{6x \ln(2)}$
383.	Let $f(x) = 2e^x - k \sin x + 1$. If the expression $f(x) = 2e^x - k \sin x + 1$.		at line to the graph of f at $(0, 3)$ is
	= $5x + 3$, then what is the value of k?		
20.4	A. 3 B3	C5	D. 2
384.	If $f(x) = \ln(2^{\tan x})$, then what is the v		5.4
	A. ln 2 B2 ln 2	C. $\frac{\ln 2}{2}$	D. 1
385.	If $h(x) = \sqrt{1 + \sqrt{x}}$, then which of the		
	A. $\frac{1}{2\sqrt{1+\sqrt{x}}}$ B. $\frac{1}{4\sqrt{x+x\sqrt{x}}}$	C. $\frac{\lambda}{2\sqrt{1+\sqrt{x}}}$	D. $\frac{x}{4\sqrt{x+x\sqrt{x}}}$
386.	If $(x) = \frac{1}{x}$, then what is the value of f	$^{(n)}(x)$?	
	A. $f^{(n)}(x) = \frac{(-1)^n n!}{x^n}$	C. $f^{(n)}(x) = \frac{(-1)^n}{n!}$	$(1)^n n!$
	χ"ι	x^{1}	r= T

B.
$$f^{(n)}(x) = \frac{(-1)^{n+1}(n+1)!}{x^{n+1}}$$

D.
$$f^{(n)}(x) = \frac{(-1)^n n!}{x^{n+1}}$$

387. Which of the following is necessarily true about a function f(x)?

A. If f is continuous at x = a, then it is differentiable at x = a.

B. If f is not differentiable at x = a, then $\lim_{x \to a^-} f(x) \neq \lim_{x \to a^+} f(x)$.

C. If f is differentiable at x = a, then $\lim_{x \to a^{-}} f(x) = f(a) = \lim_{x \to a^{+}} f(x)$.

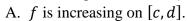
D. If f'(a) = 0, then f attains its maximum value at x = a.

388. At what value(s) of x does $f(x) = \frac{1}{3}x^3 - \frac{1}{2}x^2 - 2x + 1$ have a local maximum?

A. x = 2

D. x = 2, x = -1

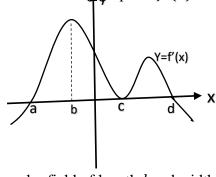
389. Look at the following graph of f'(x). Which of the following is true about f?



B. f is decreasing on [b, c].

C. f has local minimum at d.

D. f has local extreme value at c.



390. A rectangular field of length l and width w meters for w < l. Has perimeter 400 meters. If a circular region of area w^2 is to be reserved for office purpose, what should be the length of the field (in meters) so that the area of the remaining region is maximum?

A. 50

B. 100

D. 150

391. On which of the following intervals is the graph of $f(x) = \ln(x^2 + 1)$ concave upward?

A. $(-\infty, -1] \cup [1, \infty)$ B. $[0, \infty)$

C. $(-\infty,0]$

D. [-1,1]

392. Water is poured into a cylindrical tanker of radius 5m at a rate of $10m^3/min$ what is the rate of change of the height of the level of water (in m/min) when it rises to 3m?

393. The volume of the solid which is generated when the region bounded by $y = \sqrt{x+1}$ and the x-axis from x = 0 to x = 2 is rotated bout the x-axis is equal to:

Α. 4π

 $C.\frac{4}{3}\pi$

D. $\frac{3}{4}\pi$

394. On which of the following intervals does $f(x) = x^4 + 4x$ increase?

A. $(-\infty, -1]$

B. $(-\infty,0]$

C. [−1,∞)

395. At which value(s) of x does $f(x) = \frac{1}{4}x^4 - 2x^2$ have a local maximum?

B. x = 0

C. x = -2, x = 2 D. x = 0, x = 2

396. The volume V of a melting ice cube after t seconds is $V = 2000 - 4t + 0.2t^2$ (in cm^3). How fast is the volume changing (in cm^3/sec) when t = 40 seconds?

B. 15

C. -15

D. -24

397. A box seen below is to have a square base, an open top and volume of 32 cubic unit. If x is length of each side of its base and y is its height, how many units should x and y be in order to make the box with the smallest amount of material?

A. x = 4, y = 2

C. $x = \sqrt{8}$, y = 4

B. x = 2, y = 8

D. $x = \sqrt{2}$, y = 16

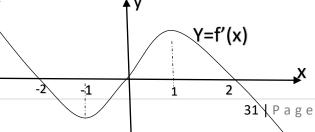
398. Suppose f is differentiable on $(-\infty, \infty)$ and the graph of its usualive is as shown below? Which of the following is true about f?

A. f is decreasing on $(-\infty,-1] \cup [1,\infty)$

B. f has a local minimum at x = -2

C. f is concave downward on $[0,\infty)$

D. f is concave up on (-1,1)



D. 5,800

A. 8.5

A. $\left\{\frac{1}{4}, 2\right\}$

volume of the box in cm^3 ?

2006

 $0 \le x \le 100$. What is the marginal (rate of change of) cost at a production level of 80 iron sheets?

C. $\{-2, 2\}$

401. If a box with a square base and open top is made from 1,200 cm^2 material, what is the largest

C. 1,800

399. The total cost (in Birr) of producing x iron sheets per day is $C(x) = 1,000 + 10x - 0.5x^2$,

400. Which one of the following is the set of all critical numbers of $f(x) = \frac{1}{3}x^3 - |4x - 1|$?

B. $\left\{-2, \frac{1}{4}, 2\right\}$

	A. 4,000	B. 8,000	C. 15,000	D. 3,000
402.	Suppose equal squar	es are cut from each of t	he four corners of a sq	uare cardboard whose sides are 72
			-	a top. How long should be each of
		s to be cut off to maximi		
	A. 6 cm	B. 12 cm	C. 15 cm	D. 24 cm
403.	What is the absolute	maximum value of $f(x)$	$= 2x^2 - x^4 - 4$ on [0, 2]?
	A3	B. 3	C4	D. 12
fe	ormula: $(t) = 80 + 12$		t = 0 correspond	opolitan area is given by the ds to 9 A.M. What is the rate of
11	A. 6ppb	,	C. 107ppb	D. 113ppb
		along the parabola $y = \frac{1}{2}$		At what point on its path does the
	A. $(3, \sqrt{6})$	B.(1, 1)	C. $(1, \sqrt{2})$	D. (2,2)
406.		lowing is necessarily tru		
	A. If $f'(x) = 0$	for all x in the interval I	, then $f(x) = 0$ for all	x in I.
		$\sin x + 5$, then there is		f'(c)=0.
	• • •	$+ x^2$, then f is increasi	-	
		then f attains its extrem		
				ladder slides away from the wall
a	t the rate (speed) of $\frac{1}{2}$ r	n/sec, how fast is the ar	igle between the top of	the ladder and the wall changing
	when the angle is $\frac{\pi}{4}$ rad	?		
	A. $\frac{\sqrt{2}}{12}$ rad/sec	B. $\frac{\sqrt{2}}{2}$ rad/sec	C. $\frac{\sqrt{2}}{6}$ rad/se	D. $\frac{\sqrt{2}}{3}$ rad/sec
	perates:		roduce per day is a fun	nction of the number of hours t it
	s(t)	$= 40t \text{ for } 0 \le t \le 12.$		
	-	Birr, to manufacture s sh = $0.1s^2 + 90s + 800$	oes is given by the fun	ction
	` '		he cost it incurs in pro-	ducing as much shoes it can
	within this time?	,	1 · · · · · · · · · · · · · · · · · · ·	8
	A. Birr 400	B. Birr 1,600	C. Birr 52,800	D. Birr 124,600
409.		,		•
				the expression $\frac{1}{4}x^2 + 35x + 25$
a	nd the price per set at	which they may be sold	is given by $50 - \frac{1}{2}x$. V	What should be the daily output
р	er day to a maximum t	total profit?	_	
-	A. 50	B. 23	C. 10	D. 7
_	A company manufac y:	tures x computer sets pe	r month. The monthly	marginal profit (in Birr) is given
U		$= 165 - 0.1x$, for $0 \le x$	$x \le 400.$	

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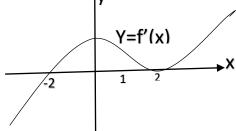
The company is currently manufacturing 10 sets of computers per month, but it is planning to increase production. What is the total change in the monthly profit if the monthly production is increased to 60 sets?

- A. Birr 500
- B. Birr 1, 865
- C. Birr 8,075
- D. Birr 18,635

- 411. Let f be twice differentiable function on \Re . Which one of the following is necessarily true?
 - A. If f'(c) = 0, at some $c \in \Re$, then f has relative extreme value at x = c.
 - B. If f'(x) is increasing, then the graph of y = f(x) is concave upward.
 - C. If f'(x) = 0, for all $x \in \Re$, then f(x) = 0 for all $x \in \Re$.
 - D. If f(x) is increasing, then $f''(x) \ge 0$ for all $\in \Re$.
- 412. Suppose f(x) is differentiable on $(-\infty, \infty)$ and the graph of its derivative, y = f'(x) is as shown in the figure below.

Which one of the following is true about f(x)?

- A. f(x) is increasing on $(-\infty, 0) \cup (2, \infty)$.
- B. f(x) has local extreme value at x = 2.
- C. f(x) has a local minimum value at x = -2
- D. f(x) has a local maximum value at x = 0



413. A closed cylindrical can is to be made to hold $1000cm^3$ of oil. What are the dimensions (r radius and h height) that will minimize the total surface area of the can?

A.
$$r = \frac{\sqrt[3]{50}}{\pi}$$
, $h = 2\frac{\sqrt[3]{50}}{\pi}$

C.
$$r = \sqrt[3]{\frac{50}{\pi}}, h = 2\left(\sqrt[3]{\frac{50}{\pi}}\right)$$

B.
$$r = \frac{\sqrt[3]{500}}{\pi}$$
, $h = 2\frac{\sqrt[3]{500}}{\pi}$

D.
$$r = \sqrt[3]{\frac{500}{\pi}}$$
, $h = 2\left(\sqrt[3]{\frac{500}{\pi}}\right)$

- 414. The graph of $y = 5x^4 x^5$ has a point of inflection at:
 - A. (3, 162) only
- B. (4, 256) only
- C. (0,0) *only*
- D. (0,0) and (3,162)
- 415. Which of the following is true about the function f defined by $f(x) = x^2 + e^{2x}$?
 - A. f is decreasing for $x \ge 0$

- C. f has a relative minimum at x = 0
- B. f is increasing for $x \le 0$

D. f has a relative maximum at x = 0

- 416. Which of the following is the set of critical numbers of $f(x) = \frac{4}{3}x^3 + |x|$?
- B. $\{0,\frac{1}{2}\}$
- C. $\left\{0, -\frac{1}{2}\right\}$
- D. $\left\{-\frac{1}{2}, 0, \frac{1}{2}\right\}$
- 417. Suppose f is continuous on [2, 6] and the only solutions of the equation f(x) = 7 are x = 2 and x = 5. If f(3) = 9, then one of the following **CANNOT** be the value of f(4):

- 418. Suppose $f:(-\infty,\infty)\to\Re$ is differentiable and the graph of its derivative, y=f'(x), is as shown in the figure below.

Which one of the following is true about f?

- A. f is increasing on $(1, \infty)$.
- C. f has no relative maximum value.
- A. f is increasing on $(1, \infty)$. C. f has no relative maximum value. B. f is concave upward on $(0, \infty)$. D. f has a relative minimum value at x = 2.
- 419. A tin can of volume $54\pi cm^3$ is to be made in the form of a circular cylinder that has both flat top and bottom. What is the base radius of the tin if it is to be made of the least amount of metal?
 - A. 2 cm
- B. 3 cm
- C. 4 cm
- 420. Air is being pumped into a spherical balloon so that its volume increases at a rate of $50 \text{ cm}^3/\text{se}$. How fast is the radius of the balloon increasing when the diameter is 5 cm?

- A. $\frac{1}{50\pi}cm/sec$ B. $\frac{1}{25\pi}cm/sec$ C. $\frac{5}{\pi}cm/sec$ D. $\frac{2}{\pi}cm/sec$ 421. What is the maximum value of the function $f(x) = x^4 - 2x^2$ on [-2, 1]?

- 422. Which one of the following is NOT true about the function $f(x) = 3x^4 4x^3$?
 - A. (0,0) is point of inflection of f.

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- B. 0 and 1 are critical numbers of f.
- C. f is concave upward on $\left(0,\frac{2}{3}\right)$ and concave downward on $\left(-\infty,0\right)$ and $\left(\frac{2}{3},\infty\right)$
- D. f is decreasing on $(-\infty, 1)$ and increasing on $(1, \infty)$.
- 423. if $f(x) = \frac{1}{3}x^3 + cx^2 + ax + 5$ has a local minimum value at x = 1, then which one of the following is true about the possible values of a and c?

A.
$$a = 3$$
, $c = -2$

C.
$$a = -2c - 1$$
, $c < -1$

B.
$$a = -2c - 1$$
, c is any real number.

D.
$$a = -2c - 1$$
, $c > -1$

424. What is the maximum possible area of a rectangle in square units with diagonal of length 16 units?

425. Which one of the following is the set of critical numbers of $(x) = \frac{3}{8}x^{\frac{8}{3}} - 6x^{\frac{2}{3}}$?

B.
$$\{-1, 1\}$$

D.
$$\{-2,0,2\}$$

426. If $f(x) = ax^3 + \frac{b}{x} + 5$ has a local minimum value at (2, -3), what are the values of a and b?

A.
$$a = -\frac{1}{4}$$
, $b = 12$

C.
$$a = \frac{1}{4}$$
, $b = 12$

B.
$$a = \frac{-1}{4}$$
, $b = -12$

D.
$$a = \frac{1}{4}$$
, $b = -12$

427. At value of x does the function $f(x) = \frac{4x^3}{3} - x^4$ attains its maximum value?

A.
$$-1$$

D.
$$\frac{4}{3}$$

428. A man wants to fence two identical rectangular enclosures in a field alongside a straight river as shown in the following figure.



What is the maximum area of each enclosure that he can make with 192 m fencing material if the side along the river do not need a fence?

A.
$$1530m^2$$

B.
$$1564m^2$$

C.
$$1664m^2$$

D.
$$1536m^2$$

- 429. A water tank is a rectangular parallelepiped with base length 3m, width 2m and height 2.5m. if water is flowing into the tank at the rate of $0.12m^3/\text{sec}$, then how fast does the level of water rises up in the tank?
 - A. 0.02 m/sec
- B. 0.03 m/sec
- C. 0.04 m/sec
- D. 0.06 m/sec

Unit 5
2004

430. Which of the following is equal to $\int \frac{x}{x^2 + 2x + 1} dx$?

A.
$$\ln(x^2 + 2x + 1) + c$$

C.
$$\ln(x^2 + 2x + 1) - \frac{1}{x+1} - c$$

B.
$$\ln|x+1| - \frac{1}{x+1} + c$$

C.
$$\ln(x^2 + 2x + 1) - \frac{1}{x+1} - c$$

D. $\ln(x^2 + 2x + 1) + \frac{1}{x+1} + c$

431. $\int \frac{e^{2x}-4x}{xe^{2x}} dx$ is equal to:

A.
$$\ln|x| + 2e^{-2x} + c$$

C.
$$\ln|x| + 4e^{-2x} + c$$

B.
$$\ln|x| - 4e^{2x} + c$$

C.
$$\ln|x| + 4e^{-2x} + c$$

D. $-\frac{1}{x^2} + 2e^{-2x} + c$

432. Which of the following is equal to $\int_0^1 \frac{(x-1)^2}{x+1} dx$?

A.
$$-\frac{3}{2} + \ln 16$$

C.
$$-\frac{5}{2} + 4 \ln 2$$

B.
$$-\frac{5}{2} + \ln 15$$

D.
$$\frac{5}{2} + \ln 16$$

- 432. Which of the following is equal to $J_0 = x+1$ A. $-\frac{3}{2} + \ln 16$ B. $-\frac{5}{2} + \ln 15$ C. $-\frac{5}{2} + 4\ln 2$ D. $\frac{5}{2} + \ln 16$ 433. If $f(x) = \begin{cases} \sin x, & x \le 0 \\ 3x\sqrt{x^2 + 1}, & x > 0 \end{cases}$, which of the following is equal to $\int_{-\frac{\pi}{2}}^{\sqrt{8}} f(x) dx$?

- 434. Which of the following is an anti-derivative of $f(x) = \tan x$?

A.	$\frac{1}{2}tar$	i^2x
----	------------------	--------

B.
$$sec^2x$$

C.
$$ln(cos x)$$

D.
$$ln(sec x)$$

435. The volume of the solid which is generated when the region bounded by $y = \sqrt{x+1}$ about the xaxis from x = 0 to x = 2 is rotated about the x-axis is equal to?

C.
$$\frac{4}{3}\pi$$

D.
$$\frac{3}{4}\pi$$

436. What is the ant-derivative of $f(x) = \frac{2}{4x^2 + 4x + 1}$?

A. $\frac{1}{2x+1}$ B. $\frac{-2}{2x+1}$ C. $-\frac{1}{2x+1}$ 437. Which one of the following is equal to $\int (1+x)3^x dx$?

A.
$$\frac{1}{2x+1}$$

B.
$$\frac{-2}{2n+1}$$

C.
$$-\frac{1}{2x+1}$$

D.
$$\ln(4x^2 + 4x + 1)$$

A.
$$(1+x)3^x - 3^x + c$$

C.
$$(1+x)(3^x \log_3 e) - 3^x (\log_3 e)^2 + c$$

B.
$$(1+x)3^x + 3^x(\log_3 e) + c$$

D.
$$(1+x)(3^x \log_3 e) - 3^x(\log_3 e) + c$$

438. Which one of the following is equal to $\int \frac{1}{x^2+x} dx$?

A.
$$\ln|x^2 + x| + c$$

C.
$$\ln|x| - \ln|x + 1| + c$$

B.
$$2 \ln|x + 1| + \ln|x| + c$$

$$2 \ln|x + 1| + \ln|x| + c$$
 D. $\ln|x| + \ln|x + 1| + c$

439. What is the value of $\int_0^{\frac{\pi}{2}} 2x \cos x \, dx$?

A. $\pi - 2$ B. $\frac{\pi}{2} + 1$ C. $\pi + 2$

A.
$$\pi - 2$$

B.
$$\frac{\pi}{2} + 1$$

C.
$$\pi + 2$$

D.
$$\frac{\pi}{2} - 1$$

440. Which one of the following is equal to $\int \frac{\ln(xe^x)}{r} dx$?

A.
$$\ln|x| + \frac{1}{2}e^x + c$$

C.
$$\ln|x| + e^{2x} + c$$

B.
$$\frac{1}{2}(\ln x)^2 + x + a$$

D.
$$-\frac{1}{x^2} + (\ln x)^2 + c$$

B. $\frac{1}{2}(\ln x)^2 + x + c$ D. $-\frac{1}{x^2} + (\ln x)^2 + c$ 441. What is the area of the region between the graphs of $y = x^2$ and y = -x + 2, where $0 \le x \le 2$? A. 3 B. 2 C. $\frac{3}{2}$ D. $\frac{2}{3}$

C.
$$\frac{3}{2}$$

D.
$$\frac{2}{3}$$

442. A water tank is a circular cylinder with base radius 2m and height 3m. if the tank is empty and water is pumped into it at rate of $2 m^3/min$, how long does it take for the tank to be full?

B.
$$\frac{3}{2}\pi$$
 min

C.
$$6\pi$$
 min

- 443. If F(x) is anti-derivative of $f(x) = 1 \frac{2}{x^2}$ and F(1) = 0, then F(2) is equal to:

B.
$$\frac{1}{2}$$

C.
$$-\frac{1}{2}$$

444. What is the area of the region between the graphs of $y = -x^2 + 2$ and y = |x|, where $-1 \le x \le 2$?

A.
$$\frac{11}{6}$$

B.
$$\frac{25}{6}$$

C.
$$\frac{7}{2}$$

D.
$$\frac{11}{3}$$

445. What is the derivative of $(x) = \int_0^{(x^2 + \pi)} \frac{dt}{\sin t + 1}$?

A. $\frac{\cos x}{\sin(x^2 + \pi) + 1}$ C. $\frac{2x \cos x}{\sin(x^2 + \pi) + 1}$

A.
$$\frac{\cos x}{\sin(x^2+\pi)+1}$$

C.
$$\frac{2x\cos x}{\sin(x^2+\pi)+}$$

B.
$$\frac{2x}{\sin(x^2+\pi)+1}$$

D.
$$\int_0^{2x} \frac{dt}{\sin t + 1}$$

Which one of the following is equal to $\int_0^{\frac{\pi}{2}} (\frac{x-\sin x}{\sec x}) dx$?

A.
$$\frac{\pi - 3}{2}$$

$$B.\frac{\pi-1}{2}$$

C.
$$\frac{3-\pi}{2}$$

D.
$$\frac{\pi+3}{2}$$

A. $\frac{\pi-3}{2}$ B. $\frac{\pi-1}{2}$ C. $\frac{3-\pi}{2}$ D. $\frac{\pi+3}{2}$ 447. What is the area of the region between the graph of $f(x) = -x^2 + 4x - 3$ and the x-axis from x = 0 to x = 3?

A.
$$-\frac{2}{3}$$

B.
$$\frac{2}{3}$$

C.
$$\frac{4}{5}$$

D.
$$\frac{8}{3}$$

448. Which one of the following is equal to $\int \frac{x + \ln(x+1)}{(x+1)^2} dx$?
A. $\ln(x+1) + \frac{x}{1-x} = 0$

A.
$$\ln(x+1) + \frac{x}{x+1} + c$$

C.
$$(x+1)^2 - \frac{x}{x+1} + c$$

D. $\frac{x \ln(x+1)}{x+1} + c$

B.
$$(x+1)^2 + \frac{x}{x+1} + c$$

D.
$$\frac{x \ln(x+1)}{x+1} + e^{-x}$$

- 449. If $f(x) = 2x(x^2 + 1)^4$ which one of the following is an anti-derivative of f(x)? C. $\frac{x}{5}(x^2+1)^5+c$ A. $\frac{2x}{5}(x^2+1)^5+c$
 - B. $\frac{2}{5}(x^2+1)^5+c$ D. $\frac{1}{5}(x^2+1)^5+c$
- 450. What is the area of the region between the graphs of $y = \sin x$ and the x-axis where $0 \le x \le 2\pi$? A. 4 B. 4π
- 451. If f and g are continuous on \Re and $a, b \in \Re$, which one of the following is necessarily true? A. If $\int_a^b f(x)dx = \int_a^b g(x)dx$, then f(x) = g(x) for all $x \in [a, b]$.
 - B. If f'(x) = g'(x) for all $x \in [a, b]$, then $\int_a^b f(x) dx = \int_a^b g(x) dx$.
 - C. If $f(x) \ge 3$ for all x[-2, 2], then $\int_{-2}^{2} f(x) \ge 12$.
- D. $\int_{a}^{b} f(x)dx = \int_{b}^{a} f(x)dx$. 452. Which one of the following is equal to $\int \frac{\ln x + x^{2}e^{x}}{x}$ A. $\frac{1}{2}\ln^{2}x + e^{x}(x^{2} 1) + c$ C. $\frac{1}{x^{2}}\ln x + e^{x}(x 1) + c$ D $-\frac{1}{x^{2}}\ln x + e^{x}(x^{2} 1) + c$
- 453. The derivative of the function $F(x) = \int_{-x}^{x} \frac{1}{1+t} dt$ is equal to:
- A. $\frac{2}{1-x^2}$ B. $\ln|1+x|$ C. $\frac{1}{1+x}$ D. $\ln\left|\frac{1+x}{1-x}\right|$ 454. Which of the following is equal to $\int \frac{(\ln x)^2 + x^2 \cos x}{x} dx$?

 A. $\frac{1}{x^2} \ln x + x \sin x \cos x + c$ C. $\frac{1}{3} (\ln x)^3 + x \sin x + \cos x + c$ B. $\frac{1}{3} (\ln x)^3 + x \sin x \cos x + c$ D. $\frac{1}{x^2} \ln x + x \sin x + \cos x + c$ 455. The volume of the solid generated when the region bounded between the graph of $(x^2, 0 < x < 2)$
- - $y = \begin{cases} x^2, & 0 \le x \le 2\\ 4, & 2 \le x \le 3 \end{cases} \text{ and the x-axis is:}$ A. $\frac{32\pi}{5}$ B. $\frac{112\pi}{5}$ C. $\frac{112\pi}{3}$
- 456. If $(x) = 3x^2\sqrt{x^3 1}$, then which one of the following is an anti-derivative of f(x)?
 - A. $\frac{3x}{2}(x^3-1)^{\frac{3}{2}}+c$

C. $\frac{3}{2}(x^3-1)^{\frac{3}{2}}+c$

B. $\frac{2}{3}(x^3-1)^{\frac{3}{2}}$

- D. $\frac{3}{2}(x^3-1)^{\frac{2}{3}}+c$
- 457. $\int_0^3 (x+1)^{\frac{1}{2}} dx$ is equal to:

- 457. $\int_{0}^{3} (x+1)^{\frac{1}{2}} dx \text{ is equal to:}$ A. $\frac{21}{2} \qquad \text{B. } \frac{14}{3} \qquad \text{C. 7} \qquad \text{D. } \frac{16}{3}$ 458. Given $f_{0} = \begin{cases} -x+1, & x < 0 \\ \cos \pi x, & x \ge 0 \end{cases}$, then $\int_{-1}^{1} f(x) dx = \frac{1}{2} \qquad \text{C. } \frac{1}{2} \qquad \text{D. } -\frac{1}{2}$ 458. Given $(x) = (\cos nx)$, $x = -\frac{1}{2}$ A. $\frac{1}{2} + \frac{1}{\pi}$ B. $\frac{1}{2} - \frac{1}{\pi}$ C. $\frac{1}{2}$ 459. The value of $\int_0^1 (x+1) e^{(x^2+2x)} dx$ is:

 B. $\frac{e^4 - e}{2}$ C. $\frac{e^3 - 1}{2}$ D. $e^3 - 1$

- 460. If f(0) = -1, f(1) = 2 and f'(x) is continuous on [0, 1], then which of the following is equal to $\int_0^1 f'(x) \sqrt{2 + f(x)} \, dx ?$

D. $\frac{4}{3}$

- 461. What is the value of $\int_0^{\ln\sqrt{3}} \frac{e^x}{e^{-x} + e^x} dx$?
 - A. $\frac{1}{2} \ln 2$
- C. ln 2
- D. 1

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462.	What is the value of the	he area of the r	region enclosed	by the graph	$of f(x) = e^x$	and	g(x) = x	x
h	etween the lines γ	1 and $r = 19$						

A.
$$\frac{e^2-1}{a}$$

B.
$$e^{2} - \frac{1}{e}$$

C.
$$e^2 - \frac{1}{a} + 2$$

A.
$$\frac{e^2-1}{e}$$
 C. $e^2 - \frac{1}{e} + 2$ D. $e - \frac{1}{e} + 2$

463. Which of the following is equal to the volume of the solid generated when the region bounded by the $y = 2\sqrt{x+1}$ and the x-axis, when $0 \le x \le 2$, rotates about the x-axis? graph of

$$B.8\pi^2$$

C.
$$16\pi$$

464. A particle moves along the x-axis with velocity given by $v(x) = 3t^2 + 6t$ for time $t \ge 0$. If the particle is at position

x = 2 at time t = 0, what is the position of the particle at t = 1?

$$\mathbf{B}$$

465. Which of the following is equal to $\int x(e^x + \sin(x^2))dx$?

A.
$$e^{x}(x+1) + \frac{1}{2}\sin(x^2) + e^{x}$$

C.
$$e^{x}(x-1) - \frac{1}{2}\cos(x^2) + c$$

B.
$$e^x(x-1) - \frac{1}{2}\sin(x^2) + c$$

A.
$$e^{x}(x+1) + \frac{1}{2}\sin(x^{2}) + c$$
 C. $e^{x}(x-1) - \frac{1}{2}\cos(x^{2}) + c$
B. $e^{x}(x-1) - \frac{1}{2}\sin(x^{2}) + c$ D. $e^{x}(x-1) + \frac{1}{2}\cos(x^{2}) + c$

466. If $2 \le f'(x) \le 4$ for all values of x, then the value of f(8) - f(2) is between which of the following numbers?

467. What is the area of the region enclosed by the graph of $y^2 = x + 1$ and $y^2 = -x + 1$?

C.
$$\frac{8}{3}$$
 sq. units D. $\frac{3}{4}$ sq. units

A. $\frac{3}{8}$ sq. units

B. $\frac{4}{3}$ sq. units

468. What is the value of $\int_{1}^{2} \frac{x+4}{x(x+2)} dx$?

D.
$$\ln 4 - \ln 2$$

469. If $f'(x) = e^{x-1} + 3x^2 - \frac{1}{x}$ and f(1) = 5, what is f(x)?

A.
$$f(x) = e^{x-1} + 3x^2 + \frac{1}{x^2} + 2$$

C.
$$f(x) = e^{x-1} + 3x^2 - \frac{1}{x} + 5$$

B.
$$f(x) = e^{x-1} - x^3 + \ln x + 5$$

D.
$$f(x) = e^{x-1} + x^3 - \ln x + 3$$

470. What is the value of $\int_1^9 \frac{e^{\sqrt{x}}}{\sqrt{x}} dx$?

A.
$$e^3 - e$$

B.
$$\frac{e^3}{3} - e$$

C.
$$e\left(e^2 - \frac{1}{3}\right)$$
 D. $2(e^3 - e)$

D.
$$2(e^3 - e)$$

471. What is the value of $\int x\sqrt{1-x^2} dx$?

A.
$$-\frac{1}{3}(1-x^2)^{\frac{3}{2}}+c$$

C.
$$(1-x^2)^{\frac{3}{2}}+c$$

B.
$$-2x\sqrt{1-x^2} + c$$

D.
$$\frac{1}{2}\sqrt{1-x^2} + c$$

472. What is the value of $\int \frac{1}{x} (\ln x + x^2 e^{-x}) dx$?

A.
$$\frac{1}{2}x^2 \ln x - (x+1)e^{-x} + c$$

C.
$$\frac{1}{2}x^2 \ln x + (2-x)e^{-x} + c$$

B.
$$\frac{1}{2}ln^2x - (x+1)e^{-x} + c$$

D.
$$\frac{1}{2}ln^2x + (2-x)e^{-x} + c$$

473. A cylindrical tank whose inner diameter is 2 m and contains $4\pi m^3$ oil. If the oil is discharged from the tank at the rate of $\frac{2\pi}{3}m^3/min$, then how long (in min) does it take for the tank to be empty?

A.
$$\frac{4}{3}$$

474. If $F(X) = \int_0^x e^{-t} dt$, then what is the value of F'(x)?

A.
$$e^{-x}$$

B.
$$-e^{-x} - 1$$

C.
$$\frac{e^{-x+1}}{-x+1}$$

D.
$$-e^{-x}$$

475. What is the value of $\int_{1}^{2} \frac{\ln x}{x^{2}} dx?$ A. $-\frac{\ln 2}{2} - \frac{1}{2}$ B. $\frac{\ln 2}{2}$

A.
$$-\frac{\ln 2}{2} - \frac{1}{2}$$

B.
$$\frac{\ln 2}{2} - \frac{1}{2}$$

C.
$$-\frac{\ln 2}{2} + \frac{1}{2}$$
 D. $\frac{\ln 2}{2} + \frac{1}{2}$

D.
$$\frac{\ln 2}{2} + \frac{1}{2}$$

476. What is the value of $\int \frac{x^{e^{-1}} + e^{x-1}}{x^e + e^x} dx$?

A.
$$\frac{1}{2}\ln(x^e + e^{x+1}) + c$$

C.
$$\frac{1}{2}\ln((x+1)^e + e^{x+1}) + c$$

$$B. \quad \frac{1}{2}\ln(x^e + e^x) + c$$

D.
$$\frac{1}{2}\ln(x^{e+1}+e^{x+1})+c$$

477. What is the area of the region bounded by the lines x = 0, x = 2, y = 1 and the curve $y = e^{2x}$?

A.
$$\frac{e^4}{2} - \frac{5}{2}$$

B.
$$\frac{e^2}{2} - \frac{1}{2}$$

C.
$$\frac{e^3}{3} - \frac{1}{3}$$

478. If the region enclosed by the graphs of $f(x) = x^2$ and $f(x) = x^3$ from x = 0 to x = 1 rotates about the x-axis, what is the volume of the solid revolution (in cubic units)?

A.
$$\frac{2\pi}{27}$$

B.
$$\frac{2\pi}{25}$$

C.
$$\frac{2\pi}{5}$$

D. $\frac{2\pi}{35}$

479. What is the value of $\int 4x \left(\ln x + \frac{1}{x^2} \right) dx$?

A.
$$4x^2(\ln x + 1) - 2x^2 + c$$

C.
$$x^2(2 \ln x + 1) + 4 \ln x + c$$

B.
$$x^2(4 \ln x - 1) + 2 \ln x + c$$

D.
$$x^2(2 \ln x - 1) + 4 \ln x + c$$

480. If a sphere with center C(0, 1, 1) intersects the z-axis at p(0, 0, 3), then the radius of the sphere is equal to:

B. 3

 $C.\sqrt{3}$

481. Let ℓ_1 and ℓ_1 be two lines in space intersecting at the origin, (0, 0, 0). If ℓ_1 and ℓ_1 passes through A(1, 1, 0) and B(0, 1, 1), respectively, then the angle between ℓ_1 and ℓ_1 is equal to:

B. 45°

482. Let $\vec{V} = 3i - 4k$, and \vec{AB} is a vector from point A(0, 1, 2) to a point B in space. If \vec{AB} is parallel to \vec{V} and $|\overrightarrow{AB}| = 10$, then point B is at:

A.
$$(-6, -1, 10)$$

C.
$$(6, 1, -6)$$

B.
$$(6, -1, -10)$$

D.
$$(-6, -1, 6)$$

483. Let $\vec{a} = -i + 3k$ and $\vec{b} = -i + j$ be vectors in space. Which one of the following is the cosine of the angle between \vec{a} and $\vec{a} - \vec{b}$?

A. $\frac{9}{10}$ B. $\frac{3}{5}$ C. $\frac{3}{\sqrt{10}}$ D. $-\frac{9}{10}$ 484. Suppose A and B are the end points of a diameter of the sphere whose equation is $x^2 + y^2 + (z + 2)^2 = 1$. If A=(1, 0, -2), then B is equal to:

A. (0, 1, -2)

C. (-1, 0, -2)

B. (0, 0, -1)

D. (0, -1, -2)

485. Suppose P(1, 2, 1) and Q(1, 0, 2) are points in space and $\vec{A} = \overrightarrow{PQ}$ if \vec{B} is parallel to \vec{PQ} and $\vec{A} \cdot \vec{B} = -10$, then which one of the following is true?

A. \vec{A} and \vec{B} have the same direction.

C.
$$|\vec{B}| = \frac{1}{10} |\vec{A}|$$

B.
$$|\vec{B}| = 10|\vec{A}|$$

D.
$$|\vec{B}| = 2|\vec{A}|$$

486. Which one of the following points is closer to the sphere $x^2 + y^2 + z^2 - 2x + 6z + 9 = 0$?

A. (1, 0, 0)

B.(0,0,0)

C. (0, -1, 0)

D. (0, 0, -1)

487. Suppose $\vec{A} = 2j - k$ and $\vec{B} = 5i + 15k$ where i, j and k are the standard unit vectors in the direction of positive x, y and z-axis, respectively. Which one of the following is the unit vector in the direction of $\vec{A} + \frac{1}{5}\vec{B}$?

A.
$$\frac{3}{5}i + \frac{4}{5}k$$

B. $\frac{1}{3}i + \frac{2}{3}j + \frac{2}{3}k$

A. $\frac{3}{5}i + \frac{4}{5}k$ B. $\frac{1}{3}i + \frac{2}{3}j + \frac{2}{3}k$ D. $\frac{2}{3}i - \frac{1}{3}j + \frac{2}{3}k$ 488. Let $\vec{a} = 2i + (x - 1)j + k$ and $\vec{c} = i - j + yk$ be vectors. If $\vec{a} \cdot \vec{c} = 0$ and $|\vec{a}| = 3$, which one of the following is possible value of y?

A. -4

C. 3

D. 4

489. Suppose $\vec{A} = 2i - j + 2k$ and \vec{B} is a vector in space such that $|\vec{B}| = \vec{A} \cdot \vec{B}$. if \vec{u} is a unit vector in the direction of $|\vec{B}|$, then $|\vec{A} + \vec{u}|^2$ is equal to:

A. 16

C. 10

D. 14

respectively, what is \vec{A} ?

		•	<u>-</u>	is on the negative z-axis and the
an		Ind Q is 6.11 P = (2, -	(1,0), then what is the coord	
	A. $(-2, 1, 4)$		C. $(2,-1,-6)$	
	B. $(2, -1, 6)$	21	D. $(-2, 1, -4)$	1
	_		+ 1, 3, 3 α) are points in spa	ace, what should be the value(s) of
и	A. $\alpha = -2$	<u>=</u>	C. $\alpha = -1$	or $\alpha = 3$
	B. $\alpha = 0$ or		D. $\alpha = -3$ or	
402				re, then which one of the following
	true about the sphe		ints of a diameter of a spiler	e, then which one of the following
13	-	a point on the sphere		
			$z^2 + (y-1)^2 + z^2 = 6.$	
			$x^2 + (y-1)^2 + z^2 = 0.$	
	-	s of the sphere is 6.	+ (y-2) + 2 = 0.	
402			$\frac{2}{3} + \frac{2}{3} + \frac{2}$	mussants a subara Whore is the
493.				presents a sphere. Where is the
ро		ted relative to the sph		f the enhance
	A. Inside the	•	C. At the center o	±
404	B. On the sph		D. outside the sph	
494.		_		$(z-2)^2 = 9$ and intersects the
sp	2		ne angle between ℓ and posi	
	A. $\frac{2}{3}$	B. $\frac{1}{3}$	C. $\frac{3}{5}$	D. $\frac{4}{5}$
		<u>-</u>	2008	
				and Q are points in space. If
\vec{V} .	$\overrightarrow{PQ} = 2$, the what	is the distance between		
	A. $\frac{3}{4}$	B. $\frac{4}{5}$	C. $\frac{4}{3}$	D. $\frac{5}{4}$
	4	3	S	4
496.	What is the value	of k, for which the tw	vo vectors $\vec{u} = \begin{pmatrix} 1 \\ k \\ -3 \end{pmatrix}$ and \vec{b}	$\vec{V} = \begin{pmatrix} 2k \\ -5 \\ 4 \end{pmatrix}$ are perpendicular?
	A. 4	B4	C. 3	D3
497.	If one of the end p	point of the line segme	ent is $(3, 2, -4)$ and the mi	d-point is $(4, 1, -2)$, then the
	ordinate of the oth		` ' '	1
			C. (5. 1. 2)	D (3.1.0)
	11. (5, 6, 6)	2009	C. (5, 1, 2)	2. (3, 1, 5)
498.	Let \vec{A} and \vec{B} be ve	ectors in space such the	hat \vec{A} and \vec{B} be vectors in sp	pace such that \vec{A} . $\vec{B} = -2$ and
			ween \vec{A} and \vec{B} , then what is	
	A. $\frac{1}{5}\cos\theta$	B. $\frac{1}{5\cos\theta}$	C. $-\frac{1}{5}\cos\theta$	D. $-\frac{1}{5\cos\theta}$
499.	If P(2, $\sqrt{5}$, 1) and	O(3, 0, 9) are points	on a sphere whose center is	s on z-axis, then which one of the
	, ,	outside of the sphere?		
10	A. $(-4, 3, 5)$		C. (3, 1, 1)	D. (0,0,0)
				-
		$(0,2)$ and $C(2,\sqrt{3},2)$	are vertices of equilateral t	triangle in space, then what is the
va	lue of x?			
	A. 5	B. 3	C. 2	D. 1
		a > 0, be a point or	1 the sphere $x^2 + y^2 + z^2$	-6z = 0 and C be center of the
_	here. If $P(k, 2, 4)$	——	—	
$\frac{\mathrm{Is}}{P0}$	A CONTRACTOR OF THE CONTRACTOR	ch that <i>PA</i> is perpend	dicular to CA , what is the co	osine of the angle between \overrightarrow{PA} and
	A. $\frac{5}{\sqrt{35}}$	B. $\frac{7}{\sqrt{35}}$	C. $\frac{7}{\sqrt{70}}$	D. $\frac{5}{\sqrt{70}}$
	√3 <u>5</u>	$-\sqrt{35}$	$\sqrt{70}$	$\sqrt{70}$

502. If the dot product of a vector \vec{A} with the vectors i - j + k, 2i + j - 3k and i + j + k are 4, 0 and 2,

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A.
$$\vec{A} = (2, 1, 1)$$

C.
$$\vec{A} = (-2, -1, 1)$$

B.
$$\vec{A} = (-2, 1, -1)$$

D.
$$\vec{A} = (2, -1, 1)$$

503. Let $P = (1, \alpha, \alpha)$ and $Q = (\alpha - 1, 1, 1)$ be two points in space and the distance between P and Q is 3. Then what is the value(s) of α ?

A.
$$\alpha = -1$$
, $\alpha = 9$

C.
$$\alpha = 3$$
, $\alpha = \frac{-1}{3}$

B.
$$\alpha = 1$$
, $\alpha = -9$

D.
$$\alpha = -3$$
, $\alpha = \frac{1}{3}$

504. If the angle between the vectors $\vec{A} = (2, -1, 1)$ and $\vec{B} = (1, 1, \alpha)$ is $\frac{\pi}{3}$, then what is the value of α ?

- B. -1

C. 2

D. -2

505. If the point $(\alpha, 0, 3)$ is on the sphere whose center is (1, 2, 3) and radius 2, what is the value of α ?

C. 2

D.
$$-3$$

506. If $\vec{u} = 2j - k$ and $\vec{v} = i - 8j + 3k$, then what is the unit vector in the direction of 5u + v?

A.
$$i + 2j - 2k$$

C.
$$\frac{1}{3}i + \frac{2}{3}j - \frac{2}{3}k$$

B.
$$\frac{2}{3}i + \frac{1}{3}j - \frac{2}{3}k$$

D.
$$\frac{1}{3}i + \frac{2}{3}j + \frac{2}{3}k$$

507. Let $a_n = n^2 - n$, when $n \in \mathbb{N}$ (the set of natural number). Which one of the following is true, when k is arbitrary chosen natural number and m is an integer?

A. a_n is not a multiple of 2 for some $n \in \mathbb{N}$ because $a_1 = 0$.

B. a_n is a multiple of 2 for all $n \in \mathbb{N}$ because $a_1 = 0$ and if $a_k = 2m$, then $a_{k+1} = 2(m+1)$.

C. a_n is a multiple of 2 for all $n \in \mathbb{N}$ because $a_1 = 0$ and if $a_k = 2m$, then $a_{k+1} = 2(m+k)$.

D. a_n is a multiple of 3 for all $n \in \mathbb{N}$ because $a_1 = 0$ and if $a_k = 3m$, then $a_{k+1} = 3(m+k-1)$.

Consider the following statement:

$$\frac{x^2+2}{x} \neq 0$$
 for every real number x.

To show this, a person constructed the following proof.

"**Proof**: Take
$$x = 1$$
. Then $\frac{x^2+2}{x} = \frac{1^2+2}{1} \neq 0$.
In the same way, if we take $x = n$ for any real number n we get

$$\frac{x^2 + 2}{x} = \frac{n^2 + 2}{n} \neq 0.$$

It follows that $\frac{x^2+2}{x} \neq 0$, for real number x."

Which one of the following is true about the proof?

A. The proof is correct by the principle of induction.

B. The proof is correct by the method of exhaustion.

C. The proof is correct and it uses the method of direct proof.

D. It is not a valid proof since its argument cannot lead to the conclusion.

509. Which one of the following describes the principle of Mathematical induction on the set of natural numbers?

A. If an assertion is true for a natural number n, then it is true for n + 1.

B. If the assertion is true for 1 and it is true for n + 1, then it is true for some n.

C. If the assertion holds for n = 20 and for any $n \ge 20$, then it is true for n implies true for n + 1.

D. If an assertion is true for n = 1, and is true for n = k, whenever is true for n = k + 1

The following is an assertion of a person and his proof. 510.

"for any natural number n, $n! < 10^n$.

Proof:

Step1. Let n = 1. Since 1! = 1 and $10^1 = 10$, it is true that 1! < 10.

Step2. Let n = 2. Since 2! = 2 and $10^2 = 100$, it is true that $2! < 10^2$.

Step3. Let n = 3. Since 3! = 6 and $10^3 = 1000$, it is true that $3! < 10^3$.

Step4. Continuing in this manner, we can see that whenever

 $k! < 10^k$ is true, then $(k+1)! < 10^{k+1}$ is also true.

Therefore, by induction, $n! < 10^n$ for all natural numbers."

- A. The proof is correct by the principle of mathematical induction, though step2 and step3 can be omitted.
- B. The proof is correct by the principle of mathematical induction; and step2 and step3 are necessary since they provide additional information.
- C. The proof is invalid because step4 did not justify the desired induction step.
- D. The proof follows the technique of a proof by exhaustion.
- 511. Consider the formula for a natural number $n \in \mathbb{N}$:

$$2 + 4 + 8 + \dots + 2^n = 2^{n+1} + 1$$

To proof this formula a person has used the following argument.

"Assume the formula is true for n = k, for some $k \in \mathbb{N}$. Then the person has shown that the formula is also true for n = k + 1. And then, the person has conclude that, by the principle of Mathematical induction, the formula is true for all natural number $n \in \mathbb{N}$." Which one of the following is true about the above arguments?

- A. The formula holds true through it does not work for n = 1.
- B. Since the left-hand side is an even number and the right hand-hand side an odd number, the principle of Mathematical induction is false.
- C. This is one example where the principle of mathematical induction fails to work.
- D. The above formula does not work for all natural numbers for $n \in \mathbb{N}$.
- 512. Which one of the following is a valid assertion that can be proved by the principle of mathematical induction?
 - A. $2^n > 10n$ for every integer n such that $n \ge 6$.
 - B. $r^2 > 0$ for every real number r such that $r \ge 1$.
 - C. $n^2 + 10n > 2n^2$ for every natural number $n \ge 1$.
 - D. $2^n > 8n$ for every integer n such that $n \ge 3$.
- 513. Consider the following assertion of a person and his proof.

"If x and y are equal positive integers, then x + y = y."

Proof: The following steps and reasons are used to proof the assertion.

Step

1. x = y

2.
$$x^2 = xy$$

3. $x^2 - y^2 = xy - y^2$

4.
$$(x - y)(x + y) = (x - y)y$$

5. x + y = y

Reason

Given hypothesis

Multiply both sides of (1) by x

Subtract y^2 from both sides of (2)

Factor both sides of (3)

Divide both sides of (4) by x - y

Step 5 completes the proof.

Which one of the following is true about this proof?

- A. It is a correct direct proof of the assertion.
- B. It follows the technique of a proof by contradiction because the steps lead to a contradiction.
- C. The proof is invalid because step 4 does not lead to step 5.
- D. The proof is invalid because step 4 does not followed from step 3.

514. Which one of the following is a valid assertion that can be proved by the principle of mathematical induction?

- A. The sum of any two rational numbers is positive.
- B. $r^2 \ge 1$, for every real number $r \ge 1$.
- C. $n^2 \ge 4n$, for every integer $n \ge 4$.
- D. $2^n \le 4^n$, for every integer $n \le 100$.
- 515. Consider the assertion: "The sum of positive irrational numbers is positive irrational number". Which one of the following is correct about the assertion?
 - A. Taking the irrational numbers such as $\sqrt{2}$, $\sqrt{3}$, $\sqrt{5}$, $\sqrt{6}$, $\sqrt{7}$ and so on, if we add any two of them, the sum is irrational. Therefore the assertion is true.
 - B. The sum of $1 + \sqrt{2}$ and $1 \sqrt{2}$ is 2, which is rational. This is a counter example that disproves the assertion.

- C. The sum of $\sqrt{7}$ and $\sqrt{2}$ is a counter example that shows the assertion is false.
- D. The assertion can be disproved by taking the sum of $1 + \sqrt{2}$ and $2 \sqrt{2}$.

- 516. Let P(n) be an open proposition on the set of natural number (\mathbb{N}). Which one of the following is correct application of the principle of mathematical induction?
 - A. If P(1) is true for n = 1; and if both P(n) and P(n+1) are true for a certain $n \in \mathbb{N}$, then P(n) is true for all $n \in \mathbb{N}$.
 - B. If P(10) is true; and if P(n) is true implies that P(n+1) is true, then P(n) is true for all $n \in \mathbb{N}$.
 - C. If P(1) is true; and P(n) \Rightarrow P(n+1) is true for any $n \in \mathbb{N}$, then P(n) is true for all $n \in \mathbb{N}$.
 - D. If P(10) is true; and assuming P(n) is true for any n > 10 if it follows that P(n+1) is true, then P(n) is true for all n > 10.
- Consider the following assertion: 517.

 $p + 2^n$ is an odd number for any prime p and any $n \in \mathbb{N}$.

Which one of the following is correct about a prove or disprove of the assertion?

- A. The assertion can be proved by direct method; because p is odd and $2^n = 2(2^{n-1})$ is even imply $p + 2^n$ is odd since the sum of even and odd is odd.
- B. There is a counter example that disproves the assertion.
- C. The assertion can be proved by the direct method; because if $n \notin \mathbb{N}$, then $2^n \notin \mathbb{N}$ and hence $p + 2^n$ is not odd.
- D. The assertion can be proved by the method of assertion.

- 518. Which one of the following is a valid assertion that can be proved by the principle of mathematical induction?
 - A. $3n + 25 < 3^n$, for every integer $n \ge 3$. C. $n^2 \le 2^n$, for every integer $n \ge 1$.
 - B. $2^n > n + 20$, for every integer $n \ge 4$. D. $n^3 n$ is divisible by 6, for every integer $n \ge 1$.
- 519. Which of the following is a correct assertion that can be proved by the principle of mathematical induction?
 - A. $\frac{1}{n+1} \le 1$, for each real number $n \ge 1$. C. $2^p 1$ is prime for each prime integer p.
 - B. $m! \le 4^m$, for each positive integer m. D. $k! \ge 2^k$, for each integer $k \ge 4$.
- 520. $\forall_n \in \mathbb{N}, 3^n 2$ is prime number that can be proved or disproved by which of the following mathematical proof?
 - A. Direct proof

C. Disprove by counter example

B. Proof by exhaustion

D. proof by contradiction.