

Practice problem

1.
 - a) Write the balanced equation for the reaction of acetic acid with aluminum hydroxide to form water and aluminum acetate.
 - b) Using the equation from problem part a, determine the mass of aluminum acetate that can be made if I do this reaction with 125 grams of acetic acid and 275 grams of aluminum hydroxide.
 - c) What is the limiting reagent in part b?
 - d) How much of the excess reagent will be left over after the reaction is complete?

2. The power output of a laser is measured in units of watts (W), where one watt is equal to one joule per second. ($1J = 1W \times 1s^{-1}$) What is the number of photons emitted per second by a 1.00 mW nitrogen laser? The wavelength emitted by a nitrogen laser is 337 nm.

3. An experiment is conducted to investigate the photoelectric effect. When light of frequency 1.0×10^{15} hertz is incident on a photocathode, electrons are emitted with maximum kinetic energy 1.0 eV. Light of frequency 1.5×10^{15} hertz produces photoelectrons with maximum kinetic energy 1.5 eV.
 - a) Calculate an experimental value of Planck's constant based on these data.
 - b) Calculate the work function of the photocathode.
 - c) Will electrons be emitted from the photocathode when green light of wavelength 5.0×10^{-7} meter is incident on the photocathode?

4. Use the simple Z_{eff} model from lecture, i.e.,

$$Z_{eff} = Z - \#e^{-} \text{ in lower shells} - \frac{1}{2} \# \text{ other } e^{-} \text{ in the same shell}$$

estimate the ionization energies of H, He, and Li.

5. Consider an electron in the 1s state of the hydrogen atom. Its normalized wavefunction is given by:

$$\psi_{1s}(r) = 2\left(\frac{1}{4\pi a_0^3}\right)^{1/2} e^{-\frac{r}{a_0}} \quad (r = \sqrt{x^2 + y^2 + z^2})$$

- (a) What is the probability of finding the electron in the region:

$$\frac{1}{\sqrt{2}}a_0 < x < \left(\frac{1}{\sqrt{2}} + 0.0001\right)a_0,$$

$$\frac{1}{\sqrt{2}}a_0 < y < \left(\frac{1}{\sqrt{2}} + 0.0001\right)a_0,$$

$$0 < z < 0.0001a_0?$$
- (b) Same, for the region:

$$\frac{5}{\sqrt{2}}a_0 < x < \left(\frac{5}{\sqrt{2}} + 0.0001\right)a_0,$$

$$\frac{5}{\sqrt{2}}a_0 < y < \left(\frac{5}{\sqrt{2}} + 0.0001\right)a_0,$$

$$0 < z < 0.0001a_0?$$
- (c) And, finally, same, but for the region:

$$\frac{0.01}{\sqrt{2}}a_0 < x < \left(\frac{0.01}{\sqrt{2}} + 0.0001\right)a_0,$$

$$\frac{0.01}{\sqrt{2}}a_0 < y < \left(\frac{0.01}{\sqrt{2}} + 0.0001\right)a_0,$$

$0 < z < 0.0001a_0$?

(d) What is the probability of finding the electron having a distance between a_0 and $a_0 + 10^{-12}m$ from the nucleus?

(e) Same, but for the distance between $5a_0$ and $5a_0 + 10^{-12}m$ from the nucleus.

(f) Finally, same, but for the distance between $0.01a_0$ and $0.01a_0 + 10^{-12}m$ from the nucleus.

6. Now consider an electron in the 2px state of the hydrogen atom:

$$\psi_{2p}(r, \theta, \phi) = \frac{1}{4} \left(\frac{1}{2\pi a_0^3} \right)^{1/2} \frac{r}{a_0} e^{-\frac{r}{2a_0}} \sin\theta \cos\phi$$

Suppose we go looking for the this electron in a small volume $(10^{-12}m)^3$ centered at various positions.

(a) At what position will the probability of finding the electron be a maximum?

(b) At what position will it be a minimum?