

Part a

GIF

$$\frac{\{P \wedge E_1\}S_1\{Q\}, \{P \wedge E_2\}S_2\{Q\}, \dots, \{P \wedge E_n\}S_n\{Q\}}{\{P\} \text{ gif } E_1 \rightarrow S_1 \ E_2 \rightarrow S_2 \ \dots \ E_n \rightarrow S_n \text{ end}\{Q\}}$$

Part b

$$\frac{\frac{\overline{\{z < 0 \wedge x \leq 0\}y := -x\{z < 0 \wedge y \geq 0\}}^{ASSIGN}}{\overline{\{z < 0 \wedge x > -5 \wedge x \leq 0\}y := -x\{z < 0 \wedge y \geq 0\}}^{CONS}, \frac{\overline{\{z < 0 \wedge x \geq 0\}y := x\{z < 0 \wedge y \geq 0\}}^{ASSIGN}}{\overline{\{z < 0 \wedge x > -5 \wedge x \geq 0\}y := x\{z < 0 \wedge y \geq 0\}}^{CONS}}{\overline{\{z < 0 \wedge x > -5\} \text{ gif } x \leq 0 \rightarrow y := -x \parallel x \geq 0 \rightarrow y := x \text{ end}\{z < 0 \wedge y \geq 0\}}^{GIF} \frac{\overline{\{z - y < 0\} z := z - y\{z < 0\}}^{ASSIGN}}{\overline{\{z < 0 \wedge y \geq 0\} z := z - y\{z < 0\}}^{CONS}}^{COMP}$$
$$\frac{\overline{\{z < 0 \wedge x > -5\} \text{ gif } x \leq 0 \rightarrow y := -x \parallel x \geq 0 \rightarrow y := x \text{ end } z := z - y\{z < 0\}}}{\overline{\{z < 0\} \text{ while } x > -5 \text{ do gif } x \leq 0 \rightarrow y := -x \parallel x \geq 0 \rightarrow y := x \text{ end } z := z - y \text{ end } \{z < 0 \wedge \neg(x > -5)\}}^{WHILE}}^{CONSEQ}$$
$$\overline{\{z < 0\} \text{ while } x > -5 \text{ do gif } x \leq 0 \rightarrow y := -x \parallel x \geq 0 \rightarrow y := x \text{ end } z := z - y \text{ end } \{z < 0\}}$$