

# Programming Languages Workshop CS 67420 Lecture 7

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*Prevs summary*

## Kb's

- A **fact** declares that something is true.
- A **rule** states **conditions** for something to be true.
- *Programs* are kb's of facts and rules.
- Queries are submitted to the system to **initiate** a computation.

## Summary: Answering Queries

- When answering a query, Prolog tries to prove that the corresponding goal is satisfiable (can be made true).
- This is done using the rules and facts given in a program.
- A goal is executed by matching it with the *first possible* fact or head of a rule. In the latter case, the rule's body becomes the new goal.
- The variable instantiations made during matching are *carried along throughout the computation and reported at the end*.
- Only the anonymous variable `_` can be instantiated differently whenever it occurs.

# Terms

- Prolog terms are either
  - numbers,
  - atoms,
  - variables, or
  - compound terms.
- Atoms: start with a lower case letter, or are enclosed in single quotes:  
`moshe, abC, x_3, ' Can you whistle ?'`
- Vars: start with a capital letter, or with an underscore:  
`X1, Epsilon, _var7, LastVar, _`

# Matching

- Two terms match if:
  - are *identical*, or
  - can be made *identical* by substituting *their vars* with suitable *ground terms*.

- Use `=/2` predicate to ask Prolog if 2 terms **match**:

?- loves(iosi, ety) = loves(iosi, X).

X = *ety*

Prolog displays the values that enabled the match.

## Matching compound terms

?- f(c, k(X, Y)) = f(X, Z), Z = k(W, p(X)).

X = c

Y = p(c)

Z = k(c, p(c))

W = c

true

?- k(X, 2, 2) = k(1, Y, X).

false

Using = (unification) yields more flexible code than using == (testing for equality).

?- X=1+1.

X = 1+1.

?- X==1+1.

false.

**$=/2$**

**$=/2$**  succeeds when the two terms are unified.

$A = 2$  or  $2 = A$  ,are the same thing, a goal to unify  $A$  with  $2$ .

**?-  $2=2$ .**

**true.**

**?-  $A=2$ .**

**$A = 2$ .**



**==/2**

The ==/2 "operator" succeeds only if the two terms are already identical without further unification.

A == 2 is true only if the variable A had **previously** been assigned the value 2.

?- 2==2.  
true.

?- A==2.  
false.

?- B=2, B==2.  
B = 2.

$\backslash =$

$\backslash =$  means the two terms cannot be unified : unification fails.

"not unified" does not result in any unification between terms.

?- 2 $\backslash$ =2.

false.

?- 2 $\backslash$ =3.

true.

?- A $\backslash$ =2.

false.

**$\backslash ==$**

$\backslash ==$  means the two terms are not identical. Here also no unification takes place even if this succeeds.

**?- 2 $\backslash ==$ 2.**

**false.**

**?- 2 $\backslash ==$ 3.**

**True.**

**?- A $\backslash ==$ 3.**

**true.**

**?- A $\backslash ==$ 3, A = 5.**

**A = 5.**

## Matching with the Anonymous Variable

- The variable    (underscore) is called the *anonymous* variable.
- Every occurrence of    may represent a diff var.

?-p(  , 2, 2) = p(1, Y,   ).

Y=2

true

   first it unifies with 1,  
then with 2,  
so all these changing values, are not printed

## Matching Queries

- If a goal matches with a *fact*, then it is satisfied.
- If a goal matches the *head of a rule*, then it is satisfied if the goal represented by the rule's body is satisfied.
- If a goal consists of several sub-goals separated by commas, then it is satisfied if all its sub-goals are satisfied.
- When trying to satisfy goals with built-in predicates such as `write/1`, Prolog also performs the action associated with it (e.g., writing something on the screen).

`?-X=Y,Y=2,write(X).`

2

`X = Y, Y = 2.`

# Built-in Predicates

- Read and compile a program file:

```
?- consult('aProg.pl').  
true
```

- Displaying terms on the screen :

```
?- write('The blue is also sky'), nl.  
The blue is also sky  
true
```

*nl is a new line*

## *what helps readability*

- meaningful names
- spaces, indentation
- one clause per line
- Comments – long, short:

*/\* a long comment,...*

*... \*/*

```
uncle(X,Y) :- brother(X, Z), % some males..(a short comment.)  
parent(Z,Y).
```

# *Some predicates*

## *examples*



# *socrates*

All men are mortal.

Socrates is a man.

Hence, Socrates is mortal.

In Prolog:

```
mortal(X):-man(X).
```

```
man(socrates).
```

```
?-mortal(socrates).
```

```
true
```

## *Family business*

father(X,Y) :- parent(X,Y), male(X).

grandparent(X,Y) :- parent(X,Z), parent(Z,Y).

paternalgrandfather(X,Y) :- father(X,Z), father(Z,Y).

sibling(X,Y) :- parent(Z,X), parent(Z,Y).

descend(X,Y):- child(X,Y).

descend(X,Y):- child(X,Z), descend(Z,Y).

# *lists*

sequences of things  
a special kind of data structure

# Lists in Prolog

- Example :

[ship, plane, car, bike]

-square brackets, commas between elements

-The empty list is written as: [].

-elements : *any* Prolog terms (vars, and other lists too).

[T, \_X, [], g(X,Z,y), \_ ,8, [D,d,c], reads(iosi,Book)]

# The built-in bar | operator

- Prolog has a special built-in operator `|` (bar), which can be used to *decompose a list into its head and tail*
- The `|` operator is a main tool for writing list manipulation predicates :

```
?- [Head | Tail] = [a,b,c,d].
```

```
Head = a,
```

```
Tail = [b, c, d].
```

```
?- [H|T]==[a,b,c,d]. % equality check doesn't work in decomposition business
```

```
false.
```

```
?- [Head|Tail] = [].
```

```
false.
```

```
?- [X,Y|Tail] = [a,b,c,d,e,f].
```

```
X = a,
```

```
Y = b,
```

```
Tail = [c, d, e, f].
```

## more list partitions

- If a bar **|** is put just before the *last term in a list*, this means that this last term denotes a sub-list.

$$?- [1,2,3,4]=[1 \mid X].$$

$$X = [2, 3, 4].$$

$$?- [1,2,3,4]=[1,2 \mid X].$$

$$X = [3, 4].$$

$$?- [1,2,3,4]=[1,2,3 \mid X].$$

$$X = [4].$$

## More examples

Remember `cons` from racket? – a parallel view

```
(cons Head Tail) ... [Head|Tail]
```

```
(cons a Tail) ... [a|Tail]           % Tail is a sublist
```

```
(cons a (cons b Tail)) ... [a,b|Tail]
```

```
(cons a (cons b (cons c []))) ... [a,b,c]
```

```
?- [ship, plane, bus, car] = [Head | Tail].
```

```
Head = ship
```

```
Tail = [plane, bus, car]
```

```
?- [1,2,3,4]=[1,Y,3|X].% extract from specific locations
```

```
Y = 2,
```

```
X = [4].% right to the bar lives a sublist
```



## *more Head and Tail*

- Another example:

?- [bike] = [X | Y].

X = bike

Y = []

?- [[iosi],[ety]] = [X|Y].

X = [iosi],

Y = [[ety]].



# Head and tail of empty list

- The empty list has *neither* a head nor a tail
- In Prolog, `[]` is a special simple list *without any internal structure*
- The empty list is important for writing recursive predicates, and for list processing in Prolog

*Using anonymous vars*

## Using anonymous variables

- A simple way of obtaining only the information we want:

The 3<sup>rd</sup> and the 5<sup>th</sup> elements:

?- [,,X,,Y|]=[a,b,c,d,e,f,g,h].

X = c, % the 3<sup>rd</sup> element

Y = e. % the 5<sup>th</sup> element

# Examples

- Extract the second element from a given list:

?- [a, b, c, d, e] = [\_, X | \_].

X=b

- Make sure the first element is a 1 and get the rest elements after the second element “packed in a list”:

?- MyList = [1, 2, 3, 4, 5], MyList = [1, \_ | Rest].

MyList = [1, 2, 3, 4, 5]

Rest = [3, 4, 5]

*List predicates examples*

## *the recursive machinery of my\_append*

- base case: when one of the lists is empty.
- Recursion:
- In every step we *take off the head*, and recall the predicate, with the (shorter) tail. Done until the base case is reached.

```
my_append([], List, List).
```

```
my_append([Elem|List1], List2, [Elem|List3]) :-  
    my_append(List1, List2, List3).
```

# Appending Lists

```
?- my_append ([1,2], [3,4], L).
```

```
L = [1,2,3,4]
```

*Interesting uses:*

```
?- my_append([1,2],L,[1,2,3,4]).
```

```
L = [3,4]
```

```
?- my_append(L,[1,2],[1,2,3,4]).
```

```
false.
```

```
?- my_append(L,[3],[1,2,3,4]).
```

```
False.
```

```
?- my_append(L,[3,4],[1,2,3,4]).
```

```
L = [1, 2] .
```

## More interesting uses: decomposing lists – "חלקי חילוף"

```
?- my_append(L1, L2, [a, b, c]).
```

```
L1 = []
```

```
L2 = [a, b, c] ;
```

```
L1 = [a]
```

```
L2 = [b, c] ;
```

```
L1 = [a, b]
```

```
L2 = [c] ;
```

```
L1 = [a, b, c]
```

```
L2 = [] ;
```

```
false
```



## חברי סועדון – member

```
member(X, [X|_]). % true if X is the Head  
member(X, [_|Tail]) :- member(X, Tail). % true if X is in the Tail
```

- One liner with **or**:

```
member(X, [Y|T]) :- X = Y; member(X, T).
```

# *member & bar “adventures”*

?- member(a,L).% list L unknown yet

L = [a|\_G1805]

L = [\_G1804, a|\_G1808]

L = [\_G1804, \_G1807, a|\_G1811]

L = [\_G1804, \_G1807, \_G1810, a|\_G1814]

L = [\_G1804, \_G1807, \_G1810, \_G1813, a|\_G1817]

L = [\_G1804, \_G1807, \_G1810, \_G1813, \_G1816, a|\_G1820]

L = [\_G1804, \_G1807, \_G1810, \_G1813, \_G1816, \_G1819, a|\_G1823]

L = [\_G1804, \_G1807, \_G1810, \_G1813, \_G1816, \_G1819, \_G1822, a|\_G1826]

L = [\_G1804, \_G1807, \_G1810, \_G1813, \_G1816, \_G1819, \_G1822, \_G1825, a|...].

## *reverse/3 a list*

```
reverse([],X,X).
```

```
reverse([H | T], X, Acc) :- reverse(T, X,[H | Acc]).
```

```
?- reverse([1,2],X,Y).
```

```
X = [2, 1|Y].
```

```
?- Y=[],reverse([1,2],X,Y).
```

```
Y = [],
```

```
X = [2, 1].
```

```
?- Y=[7],reverse([1,2],X,Y).
```

```
Y = [7],
```

```
X = [2, 1, 7].
```

```
?- Y=[7],reverse([1,2],X,[8]).
```

```
Y = [7],
```

```
X = [2, 1, 8].
```

## 2 more reverse runs

?- reverse([1,2],X,[]).

X = [2, 1].

?- reverse([1,2,3],X,[]).

X = [3, 2, 1].

# *Arithmetic in Prolog*

## *Expressions*

# *successor: a way to describe the natural numbers:*

natNumber(0).                      % 0 is a natNumber.

natNumber(succ(X)):-

natNumber(X). % If X is a natNumber, then so is succ(X).

?- natNumber(succ(succ(succ(succ(0))))).

true

?- natNumber(X).

**X = 0 ;**

**X = succ(0);**

**X = succ(succ(0));**

X = succ(succ(succ(0)))

X = succ(succ(succ(succ(0))))

X = succ(succ(succ(succ(succ(0)))))

X = succ(succ(succ(succ(succ(succ(0))))))

X = succ(succ(succ(succ(succ(succ(succ(0)))))))

X = succ(succ(succ(succ(succ(succ(succ(succ(0))))))))

X = succ(succ(succ(succ(succ(succ(succ(succ(succ(0)))))))))

X = succ(succ(succ(succ(succ(succ(succ(succ(succ(succ( . . . ))))))))))

## *addition with successors*

`add(0,X,X).` % base clause

`add(succ(X),Y,succ(Z)):-add(X,Y,Z).` % recursive clause

Try : -, \*, \*\*

# Arithmetic operators

- Arithmetic expressions in Prolog are *just terms*, which are **not** evaluated *automatically*. (*"Everything is a term in Prolog"*)
- (Remember quoted lists in Racket).
- So,  $2 + 3$  is just the same as  $+(2, 3)$ , which does *nothing* on its own.
- It is the responsibility of individual predicates to *evaluate* those terms.
- Several built-in predicates do *implicit evaluation*, like :
  - arithmetic comparison operators like **`==`**, (there are more..)
  - and **`is`**.



## ***== operator***

*== evaluates both args on (both sides) and compares their values,*

?- 2==1+1.

true.

?- 3-1==7-5.

true.

?- X = 6, X == 2+3.

false.

?- X=1+4, X==2+3. % evaluates 1+4 only at == not in X=1+4  
X = 1+4.

?- 1+4==2+3.

true.

# The *is/2* operator

**is** accepts and evaluates only its *right* arg as an arith expression.

**is** *left* arg has to be an *atom*, either a *numeric* constant (which is then compared to the result of the evaluation of the right operand), or a *variable*.

- If it is a *bound* variable, its value has to be numeric and is compared to the right operand as in the former case.

```
?- X=6, X is 7-1.
```

```
X = 6.
```

- If it is an *unbound* variable, the result of the evaluation of the right operand *will be bounded* to that variable.

```
?- X is 5/6-2.                                % start with an unbounded X.
```

```
X = -1.16666666666666665.
```

**is** is often used in this latter case, to bind variables, the prolog assignment

## More is/2-op examples

?- X is 2+3.

X = 5 ;

?- X is 12\*-4.

X = -48 ;

?- X is 2\*4.

X = 8 ;

?- X is 2/3.

X = 0.6666666666666666.

## Errors of “habit”

?- 2+3 is 5. % no calculations on the left side.

false

?- 5 is 2+3. % is calculates on the right side and unifies with 5.

true.

?- 5 is 2+X. % unification is not wizardry

ERROR: Arguments are not sufficiently instantiated

But:

?- **X = 3**, 5 is 2+X. % this will work

X = 3.

?- X = 3, 5 is 1+X. % works but is false

false.

## *is/2 or ==/2*

- To test if a number N is even, we could use both operators:

0 *is* N mod 2 % true if N is even

0 *==* N mod 2 % true as above

But if you want at the same time, to *capture the result* of the operation, you can only use the first variant. If X is unbound, then:

X *is* N mod 2 % X will be 0 if N is even

X *==* N mod 2 % will errorize!! with argument/instantiation error! (of X)

For just *comparison of values of arith expressions*, use *==*.

To *capture the result* of an evaluation, use *is*.

*is/2 or ==/2 or ==/2*

?- N=8, X **==** N mod 2 .

ERROR: **==/2**: Arguments are not sufficiently instantiated (X..)

?- N=8, X **is** N mod 2. % X is bounded to mod result

N = 8,

X = 0.

**==** is a comparison operator.

A1 **==** A2 succeeds if *values* of expressions A1 and A2 are equal.

A1 **==** A2 succeeds if *terms* A1 and A2 are *identical*;

# Checking if a num is odd

Using `is/2` :

`odd(Num) :- 1 is Num mod 2.`

Using `==/2` :

`odd(Num) :- Num mod 2 == 1.`

More cautious? check first if Num is integer:

`odd(Num) :- integer(Num), 1 is Num mod 2.`

## *=/2 does not evaluate*

No arith evaluations are done here just term matching :

```
?- 2+3 = +(2,3). % 2+3 is a valid Prolog term
```

```
true           % as a match of operators not of arith values
```

```
?- 2+3 = +(3,2). % args not in the right places ? False!
```

```
false
```

```
?- 2+3 = 5. % no wonder..
```

```
False
```

```
?- X is 2 + 3. % is does it
```

```
X = 5
```



# *int vs float battles of honour*

With **is** we can open an arithmetic center:

?- X **is** 2 \* 4 + 3 \* -7, Y **is** X / 5, Z **is** Y/X.

X = -13,

Y = -2.6,

Z = 0.2.

?- X **is** 1.2 + 2.8, X = **4**.

false.

?- X **is** 1.2 + 2.8, X = **4.0**.

X = 4.0.

- Some systems will try to instantiate X with the `int` 4,
- others with the `float` 4.0.

# Some built-in arith functions

- Examples:

```
?- X is max(12, 11).
```

```
X = 12.
```

```
?- X is sqrt(11.23) * 1.2.
```

```
X = 4.021343059227849.
```

```
?- X is (123 mod 11) ** -1.2.
```

```
X = 0.43527528164806206.
```

More functions in the Manual

*Built-in predicates for comparing vals of arith exprs,  
all evaluate their L,R args, as does ==*

?- 7 > 2.

true

?- 7+2 > 8-2.

true

?- 7 =< 2.

false

?- 7 == 2.

false

?- 7 =\ 2. % not equal

true

?- 7 >= 2.

true

## Find the max number in a list

- It takes 3 args: a list, *Max* (a var for the max) in the list, and *Res* (var for the ans):
- Max gets updated with the highest number met so far.

```
findMax([H|T],Max,Res):-
```

```
    H > Max,
```

```
    findMax(T,H,Res).
```

```
findMax([H|T],Max,Res):-
```

```
    H =< Max,
```

```
    findMax(T,Max,Res).
```

```
findMax([],Max,Max).
```

## *getMax/2 wrapper for findMax/3*

```
?- findMax([5,2,6,1], 0, Res).
```

```
Res = 6.
```

```
?- Max=-1, findMax([5,2,6,1], Max, Res).
```

```
Max = -1
```

```
Res = 6.
```

**Wrapper** getMax/2:

```
getMax([H|T],Res):- findMax(T,H,Res).
```

Use:

```
?- getMax([1,5,2,7,2,99],X).
```

```
X = 99.
```

# Examples

- Recall the difference between matching and arithmetic evaluation:

?- 3 + 5 = 5 + 3.

false

?- 3 + 5 == 5 + 3.

true

Different precedencies :

?- 2 + 3 \* 4 == (2 + 3) \* 4.

false

?- 2 + 3 \* 4 == 2 + (3 \* 4).

true

# Summary: Arith in Prolog

- For logical pattern matching use `=`,
- for arithmetic evaluation use the `is op`.
- A range of built-in arithmetic functions is available (some are written as *infix* operators, e.g., `+`).
- Arithmetic expressions can be *compared* using arithmetic relations such as `<` or `:=` (i.e., not using the `is`-operator)

## Length of a list

Using the arithmetic operator **is**:

```
len([],0).
```

```
len([H|T],N) :- len(T,M), N is M+1.
```

The second clause can also be

% who cares what H is, after counting it here..

```
len(_|T],N) :- len(T,M), N is M+1.
```



```
?- len([11,12,-33,-4],N).
```

```
N=4
```