## scipy / scipy

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                                                                                                                            Find file Copy path
pv ENH: optimize: call callback with a copy for scipy.optimize
                                                                                                                              7f43e34 4 days ago
469 lines (397 sloc) 16.5 KB
       Functions
       .. autosummary::
          :toctree: generated/
           fmin 1 bfgs b
   8
       ## License for the Python wrapper
  14
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  16
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       ## Modifications by Travis Oliphant and Enthought, Inc. for inclusion in SciPy
       from future import division, print function, absolute import
  38
       import numpy as np
       from numpy import array, asarray, float64, int32, zeros
  40
       from . import lbfgsb
  41
       from .optimize import (approx_fprime, MemoizeJac, OptimizeResult,
  42
                             _check_unknown_options, wrap_function,
  43
                             _approx_fprime_helper)
       from scipy.sparse.linalg import LinearOperator
  44
  45
  46
       __all__ = ['fmin_l_bfgs_b', 'LbfgsInvHessProduct']
  47
  48
  49
       def fmin_1_bfgs_b(func, x0, fprime=None, args=(),
  50
                        approx_grad=0,
                        bounds=None, m=10, factr=1e7, pgtol=1e-5,
                         epsilon=1e-8.
                        iprint=-1, maxfun=15000, maxiter=15000, disp=None,
  54
                        callback=None, maxls=20):
           Minimize a function func using the L-BFGS-B algorithm.
  58
           Parameters
           func : callable f(x,*args)
               Function to minimise.
```

```
Initial guess.
          fprime : callable fprime(x,*args), optional
              The gradient of `func`. If None, then `func` returns the function
              value and the gradient (``f, g = func(x, *args)``), unless
 67
              `approx grad` is True in which case `func` returns only ``f``.
          args : sequence, optional
              Arguments to pass to `func` and `fprime`.
          approx grad : bool, optional
              Whether to approximate the gradient numerically (in which case
              `func` returns only the function value).
          bounds : list, optional
              ``(min, max)`` pairs for each element in ``x``, defining
              the bounds on that parameter. Use None or +-inf for one of ``min`` or
              ``max`` when there is no bound in that direction.
          m : int, optional
 78
              The maximum number of variable metric corrections
              used to define the limited memory matrix. (The limited memory BFGS
 80
              method does not store the full hessian but uses this many terms in an
 81
              approximation to it.)
          factr : float, optional
 82
83
             The iteration stops when
 84
              (f^k - f^{k+1})/\max\{|f^k|,|f^{k+1}|,1\} \le factr * eps^,
 85
              where ``eps`` is the machine precision, which is automatically
 86
              generated by the code. Typical values for `factr` are: 1e12 for
 87
              low accuracy; 1e7 for moderate accuracy; 10.0 for extremely
 88
              high accuracy. See Notes for relationship to `ftol`, which is exposed
              (instead of `factr`) by the `scipy.optimize.minimize` interface to
 89
              L-BFGS-B.
          pgtol : float, optional
              The iteration will stop when
              ``max{|proj g_i | i = 1, ..., n} <= pgtol``
              where ``pg_i`` is the i-th component of the projected gradient.
          epsilon : float, optional
              Step size used when `approx_grad` is True, for numerically
 97
              calculating the gradient
          iprint : int, optional
             Controls the frequency of output. ``iprint < 0`` means no output;
100
              ``iprint = 0`` print only one line at the last iteration;
              ``0 < iprint < 99`` print also f and ``|proj g|`` every iprint iterations;
              ``iprint = 99`` print details of every iteration except n-vectors;
              ``iprint = 100`` print also the changes of active set and final x;
              ``iprint > 100`` print details of every iteration including \boldsymbol{x} and \boldsymbol{g}.
105
          disp : int, optional
106
              If zero, then no output. If a positive number, then this over-rides
              `iprint` (i.e., `iprint` gets the value of `disp`).
          maxfun : int, optional
109
              Maximum number of function evaluations.
          maxiter : int, optional
110
             Maximum number of iterations.
          callback : callable, optional
             Called after each iteration, as ``callback(xk)``, where ``xk`` is the
              current parameter vector.
          maxls : int, optional
             Maximum number of line search steps (per iteration). Default is 20.
119
          x : array_like
              Estimated position of the minimum.
              Value of `func` at the minimum.
          d : dict
             Information dictionary.
              * d['warnflag'] is
                - 0 if converged,
                - 1 if too many function evaluations or too many iterations,
                - 2 if stopped for another reason, given in d['task']
              * d['grad'] is the gradient at the minimum (should be 0 ish)
              * d['funcalls'] is the number of function calls made.
              * d['nit'] is the number of iterations.
```

```
See also
138
          minimize: Interface to minimization algorithms for multivariate
             functions. See the 'L-BFGS-B' `method` in particular. Note that the
              `ftol` option is made available via that interface, while `factr` is
             provided via this interface, where `factr` is the factor multiplying
              the default machine floating-point precision to arrive at `ftol`:
              ``ftol = factr * numpy.finfo(float).eps``.
146
147
          License of L-BFGS-B (FORTRAN code):
150
          The version included here (in fortran code) is 3.0
          (released April 25, 2011). It was written by Ciyou Zhu, Richard Byrd,
          and Jorge Nocedal <nocedal@ece.nwu.edu>. It carries the following
          condition for use:
          This software is freely available, but we expect that all publications
          describing work using this software, or all commercial products using it,
          quote at least one of the references given below. This software is released
158
          under the BSD License.
159
          References
          * R. H. Byrd, P. Lu and J. Nocedal. A Limited Memory Algorithm for Bound
            Constrained Optimization, (1995), SIAM Journal on Scientific and
           Statistical Computing, 16, 5, pp. 1190-1208.
          * C. Zhu, R. H. Byrd and J. Nocedal. L-BFGS-B: Algorithm 778: L-BFGS-B,
           FORTRAN routines for large scale bound constrained optimization (1997),
           ACM Transactions on Mathematical Software, 23, 4, pp. 550 - 560.
          * J.L. Morales and J. Nocedal. L-BFGS-B: Remark on Algorithm 778: L-BFGS-B,
           FORTRAN routines for large scale bound constrained optimization (2011),
170
           ACM Transactions on Mathematical Software, 38, 1.
          # handle fprime/approx_grad
174
          if approx grad:
             fun = func
             jac = None
          elif fprime is None:
178
             fun = MemoizeJac(func)
              jac = fun.derivative
180
          else:
             fun = func
181
              jac = fprime
183
184
          # build options
          if disp is None:
             disp = iprint
          opts = {'disp': disp,
188
                  'iprint': iprint,
                  'maxcor': m,
                  'ftol': factr * np.finfo(float).eps,
                  'gtol': pgtol,
                  'eps': epsilon,
                  'maxfun': maxfun,
                  'maxiter': maxiter
                  'callback': callback,
196
                  'maxls': maxls}
          res = _minimize_lbfgsb(fun, x0, args=args, jac=jac, bounds=bounds,
                                 **opts)
          d = {'grad': res['jac'],
               'task': res['message'],
               'funcalls': res['nfev'],
202
203
               'nit': res['nit'],
204
               'warnflag': res['status']}
205
          f = res['fun']
          x = res['x']
207
208
          return x, f, d
209
210
```

```
def _minimize_lbfgsb(fun, x0, args=(), jac=None, bounds=None,
                           disp=None, maxcor=10, ftol=2.2204460492503131e-09,
                           gtol=1e-5, eps=1e-8, maxfun=15000, maxiter=15000,
                           iprint=-1, callback=None, maxls=20, **unknown_options):
          Minimize a scalar function of one or more variables using the L-BFGS-B
          algorithm.
          Options
          disp : bool
            Set to True to print convergence messages.
          maxcor : int
224
             The maximum number of variable metric corrections used to
             define the limited memory matrix. (The limited memory BFGS
             method does not store the full hessian but uses this many terms
              in an approximation to it.)
          ftol : float
             The iteration stops when ``(f^k -
              f^{k+1})/\max\{|f^k|,|f^{k+1}|,1\} \leftarrow ftol^*.
          gtol : float
             The iteration will stop when ``max{|proj g_i | i = 1, ..., n}
              <= gtol`` where ``pg_i`` is the i-th component of the
              projected gradient.
          eps : float
236
             Step size used for numerical approximation of the jacobian.
          disp : int
              Set to True to print convergence messages.
          maxfun : int
240
             Maximum number of function evaluations.
241
          maxiter : int
242
             Maximum number of iterations.
          maxls : int, optional
             Maximum number of line search steps (per iteration). Default is 20.
          Notes
247
248
          The option `ftol` is exposed via the `scipy.optimize.minimize` interface,
          but calling `scipy.optimize.fmin_l_bfgs_b` directly exposes `factr`. The
          relationship between the two is ``ftol = factr * numpy.finfo(float).eps``.
          I.e., `factr` multiplies the default machine floating-point precision to
          arrive at `ftol`.
254
          _check_unknown_options(unknown_options)
          m = maxcor
          epsilon = eps
258
          pgtol = gtol
          factr = ftol / np.finfo(float).eps
          x0 = asarray(x0).ravel()
          n, = x0.shape
          if bounds is None:
              bounds = [(None, None)] * n
          if len(bounds) != n:
              raise ValueError('length of x0 != length of bounds')
          # unbounded variables must use None, not +-inf, for optimizer to work properly
269
          bounds = [(None if 1 == -np.inf else 1, None if u == np.inf else u) for 1, u in bounds]
270
          if disp is not None:
             if disn == 0:
                 iprint = -1
274
                  iprint = disp
          n function evals, fun = wrap function(fun, ())
278
          if jac is None:
              def func_and_grad(x):
                  f = fun(x, *args)
281
                  g = _approx_fprime_helper(x, fun, epsilon, args=args, f0=f)
282
                  return f, g
          else:
283
              def func_and_grad(x):
```

```
285
                  f = fun(x, *args)
286
                  g = jac(x, *args)
287
                   return f, g
289
          nbd = zeros(n, int32)
290
          low_bnd = zeros(n, float64)
          upper_bnd = zeros(n, float64)
          bounds_map = {(None, None): 0,
                        (1, None): 1,
                        (1, 1): 2,
                        (None, 1): 3}
          for i in range(0, n):
             1, u = bounds[i]
298
              if 1 is not None:
299
                  low_bnd[i] = 1
                  1 = 1
              if u is not None:
301
302
                  upper\_bnd[i] = u
303
              nbd[i] = bounds_map[1, u]
306
          if not maxls > 0:
307
              raise ValueError('maxls must be positive.')
          x = array(x0, float64)
310
          f = array(0.0, float64)
          g = zeros((n,), float64)
          wa = zeros(2*m*n + 5*n + 11*m*m + 8*m, float64)
          iwa = zeros(3*n, int32)
314
          task = zeros(1, 'S60')
          csave = zeros(1, 'S60')
          lsave = zeros(4, int32)
          isave = zeros(44, int32)
318
          dsave = zeros(29, float64)
          task[:] = 'START'
          n iterations = 0
          while 1:
              # x, f, g, wa, iwa, task, csave, lsave, isave, dsave = \
              _lbfgsb.setulb(m, x, low_bnd, upper_bnd, nbd, f, g, factr,
                              pgtol, wa, iwa, task, iprint, csave, lsave,
328
                              isave, dsave, maxls)
              task_str = task.tostring()
330
              if task_str.startswith(b'FG'):
                  \mbox{\tt\#} The minimization routine wants f and g at the current x.
                  \ensuremath{\text{\#}} 
 Note that interruptions due to maxfun are postponed
                  # until the completion of the current minimization iteration.
                  # Overwrite f and g:
                  f, g = func\_and\_grad(x)
336
              elif task_str.startswith(b'NEW_X'):
                  # new iteration
                  n iterations += 1
339
                  if callback is not None:
340
                      callback(np.copy(x))
342
                  if n iterations >= maxiter:
343
                       task[:] = 'STOP: TOTAL NO. of ITERATIONS REACHED LIMIT'
344
                   elif n_function_evals[0] > maxfun:
                      task[:] = ('STOP: TOTAL NO. of f AND g EVALUATIONS '
                                  'EXCEEDS LIMIT')
347
              else:
348
                  break
          task_str = task.tostring().strip(b'\x00').strip()
          if task str.startswith(b'CONV'):
          elif n_function_evals[0] > maxfun or n_iterations >= maxiter:
              warnflag = 1
          else:
356
              warnflag = 2
          # These two portions of the workspace are described in the mainlb
358
```

```
# subroutine in lbfgsb.f. See line 363.
          s = wa[0: m*n].reshape(m, n)
          y = wa[m*n: 2*m*n].reshape(m, n)
          # See lbfgsb.f line 160 for this portion of the workspace.
          # isave(31) = the total number of BFGS updates prior the current iteration;
          n_bfgs_updates = isave[30]
          n corrs = min(n bfgs updates, maxcor)
          hess_inv = LbfgsInvHessProduct(s[:n_corrs], y[:n_corrs])
          return OptimizeResult(fun=f, jac=g, nfev=n_function_evals[0],
                                nit=n_iterations, status=warnflag, message=task_str,
                                x=x, success=(warnflag == 0), hess_inv=hess_inv)
      class LbfgsInvHessProduct(LinearOperator):
           """Linear operator for the L-BFGS approximate inverse Hessian.
          This operator computes the product of a vector with the approximate inverse
          of the Hessian of the objective function, using the L-BFGS limited
380
          memory approximation to the inverse Hessian, accumulated during the
381
          optimization.
          Objects of this class implement the ``scipy.sparse.linalg.LinearOperator``
384
          interface.
          Parameters
387
388
          sk : array_like, shape=(n_corr, n)
389
              Array of `n_corr` most recent updates to the solution vector.
             (See [1]).
          yk : array_like, shape=(n_corr, n)
             Array of `n_corr` most recent updates to the gradient. (See [1]).
          References
396
          .. [1] Nocedal, Jorge. "Updating quasi-Newton matrices with limited
             storage." Mathematics of computation 35.151 (1980): 773-782.
          def __init__(self, sk, yk):
400
               """Construct the operator."""
401
402
              if sk.shape != yk.shape or sk.ndim != 2:
403
                 raise ValueError('sk and yk must have matching shape, (n_corrs, n)')
404
              n corrs, n = sk.shape
405
406
              super(LbfgsInvHessProduct, self).__init__(
407
                  dtype=np.float64, shape=(n, n))
408
409
              self.sk = sk
410
              self.yk = yk
411
              self.n_corrs = n_corrs
              self.rho = 1 / np.einsum('ij,ij->i', sk, yk)
412
413
414
          def _matvec(self, x):
415
              """Efficient matrix-vector multiply with the BFGS matrices.
416
417
              This calculation is described in Section (4) of [1].
418
419
              Parameters
420
421
              x : ndarrav
422
                  An array with shape (n,) or (n,1).
423
424
              Returns
425
426
              y : ndarray
                  The matrix-vector product
428
429
430
              s, y, n_corrs, rho = self.sk, self.yk, self.n_corrs, self.rho
431
              q = np.array(x, dtype=self.dtype, copy=True)
              if q.ndim == 2 and q.shape[1] == 1:
```

```
433
                 q = q.reshape(-1)
434
435
              alpha = np.zeros(n_corrs)
436
437
              for i in range(n_corrs-1, -1, -1):
438
                 alpha[i] = rho[i] * np.dot(s[i], q)
439
                 q = q - alpha[i]*y[i]
440
              r = q
441
442
              for i in range(n_corrs):
                 beta = rho[i] * np.dot(y[i], r)
443
                 r = r + s[i] * (alpha[i] - beta)
444
445
446
447
          def todense(self):
448
449
              """Return a dense array representation of this operator.
450
451
452
453
              arr : ndarray, shape=(n, n)
454
                 An array with the same shape and containing
455
                 the same data represented by this `LinearOperator`.
456
457
              s, y, n_corrs, rho = self.sk, self.yk, self.n_corrs, self.rho
458
459
              I = np.eye(*self.shape, dtype=self.dtype)
              Hk = I
461
462
              for i in range(n_corrs):
463
                 A1 = I - s[i][:, np.newaxis] * y[i][np.newaxis, :] * rho[i]
                 A2 = I - y[i][:, np.newaxis] * s[i][np.newaxis, :] * rho[i]
464
465
466
                 Hk = np.dot(A1, np.dot(Hk, A2)) + (rho[i] * s[i][:, np.newaxis] *
467
                                                             s[i][np.newaxis, :])
468
              return Hk
```