

Assignment - 11

18K41A0587

g) Develop a simple linear regression model using NAG optimiser.

sample (i)	X_i^a	Y_i^a
1	0.2	3.4
2	0.4	3.8
3	0.6	4.2
4	0.8	4.6

Sol step 1 : $[X, Y]$, $m=1$, $c=-1$, $\eta=0.1$, epochs = 2, $\gamma=0.9$, $V_m=V_c=0$,
 $hs=2$.

step 2 : $itr=1$

step 3 : sample = 1

$$\begin{aligned}\text{step 4 : } g_m &= \frac{\partial E}{\partial m} = - (y_i - (m + \gamma_m)x_i - (c + \gamma_c))x_i \\ &= - (3.4 - (1 + (0.9)(0))0.2 - (-1 + (0.9)(0))0.2) \\ &= -0.84.\end{aligned}$$

$$\begin{aligned}g_c &= \frac{\partial E}{\partial c} = - (3.4 - (1 + 0.9 \times 0)0.2 - (-1 + (0.9)(0))) \\ &= -4.2.\end{aligned}$$

$$\begin{aligned}\text{step 5 : } V_m &= \gamma V_m - \eta g_m \\ &= (0.9)(0) - (-0.1) \times (-0.84) = -0.084\end{aligned}$$

$$\begin{aligned}V_c &= \gamma V_c - \eta g_c \\ &= (0.9)(0) - (-0.1)(-4.2) = -0.42.\end{aligned}$$

$$\text{step 6 : } m = m + V_m = 1 - 0.084 = 0.916$$

$$c = c + V_c = -1 - 0.42 = -1.42$$

$$\text{step 7 : } \text{sample} = \text{sample} + 1 = 1 + 1 = 2$$

step 8 : if (sample > ns)
goto step 9

else

goto step 4

$$\text{step 4 : } g_m = \frac{\partial \epsilon}{\partial m} = -(3.8 - (0.916 + (0.9 \times 0.084)) \cdot 0.4 - (-1.42 + (0.9 \times 0.084)) \cdot 0.4)$$

$$= -1.983$$

$$g_c = \frac{\partial \epsilon}{\partial c} = -4.954$$

$$\text{step 5 : } V_m = \eta V_m - \eta g_m$$

$$= (0.9 \times -0.084) - (0.1 \times -1.983) = -0.2739$$

$$V_c = (0.9 \times -0.42) - (0.1 \times -4.954) = -0.8739$$

$$\text{step 6 : } m = m + V_m = 0.916 - 0.2739 = 0.6421$$

$$c = c + V_c = -1.42 - 0.8739 = -2.2939$$

$$\text{step 7 : } \text{sample} = \text{sample} + 1 = 2 + 1 = 3$$

step 8 : if (sample > ns)
goto step 9

else

goto step 4

$$\text{step 9 : } \text{itr} = \text{itr} + 1 = 1 + 1 = 2$$

step 10 : if (itr > epochs)
goto step 11

else : goto step 3

step 3 : sample = 1

$$\text{step 4 : } \frac{\partial E}{\partial m} = -(3.4 - 0.642 + (0.9 \times 0.273)) \times 0.2 - (-2.293 + (0.9 \times -0.273)) \times 0.2$$
$$= -1.171$$

$$g_m = \frac{\partial E}{\partial m} = -5.859$$

$$\text{step 5 : } V_m = \eta V_m - \eta g_m = (0.9)(-0.273) - (-0.1 \times -1.171) = -0.3627$$

$$V_c = \eta V_c - \eta V_c = (0.9)(-0.273) - (-0.1)(-5.859) = -1.3707$$

$$\text{step 6 : } m = m + V_m = 0.6421 + (-0.3627) = 0.2794$$

$$c = c + V_c = -2.2939 - 1.3707 = -3.6646$$

$$\text{step 7 : } \text{sample} = \text{sample} + 1 = 1 + 1 = 2$$

step 8 : if (sample > ns) : goto step 9

else: goto step 4.

$$\text{step 4 : } g_m = \frac{\partial E}{\partial m} = -2.985$$

$$g_c = \frac{\partial E}{\partial c} = -7.4645$$

$$\text{step 5 : } V_m = (0.9 \times -0.3627) - (-0.1 \times -2.985) = -0.6249$$

$$V_c = (0.9 \times -1.3707) - (-0.1 \times -7.4645) = -1.9800$$

$$\text{step 6 : } m = m + V_m = 0.2794 + (-0.6249) = -0.3275$$

$$c = c + V_c = -3.6646 - 1.9800 = -4.6446$$

$$\text{step 7 : } \text{sample} = \text{sample} + 1 = 2 + 1 = 3$$

step 8 : if (sample > ns) : goto step 9

else: goto step 4.

$$\text{step 9 : } \text{itr} = \text{itr} + 1 = 2 + 1 = 3$$

step 10 : if (itr > epochs) : goto step 4

else : goto step 3.

step 11 : print m, c

$$m = 0.3275$$

$$c = -4.6446$$