# **GPy Documentation**

Release

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For a quick start, you can have a look at one of the tutorials:

- Basic Gaussian process regression
- Interacting with models
- A kernel overview
- Writing new kernels
- Writing new models

You may also be interested by some examples in the GPy/examples folder.

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# The detailed Developers Documentation is listed below

Contents:

# 1.1 GPy package

# 1.1.1 Subpackages

# **GPy.core** package

**Submodules** 

# GPy.core.domains module

Created on 4 Jun 2013

@author: maxz

(Hyper-)Parameter domains defined for priors and kern. These domains specify the legitimate realm of the parameters to live in.

**REAL:** real domain, all values in the real numbers are allowed

**POSITIVE:** positive domain, only positive real values are allowed

**NEGATIVE:** same as POSITIVE, but only negative values are allowed

**BOUNDED:** only values within the bounded range are allowed, the bounds are specified withing the object with the bounded range

# GPy.core.fitc module

```
class GPy.core.fitc.FITC(X, likelihood, kernel, Z, normalize_X=False)
    Bases: GPy.core.sparse_gp.SparseGP
```

Sparse FITC approximation

# **Parameters**

- **X** (*np.ndarray* (*num\_data x Q*)) inputs
- **likelihood** (*GPy.likelihood.*(*Gaussian* | *EP*)) a likelihood instance, containing the observed data

- **kernel** (a GPy.kern.kern instance) the kernel (covariance function). See link kernels
- **Z** (np.ndarray (M x Q) | None) inducing inputs (optional, see note)
- **normalize\_(XIY)** (*bool*) whether to normalize the data before computing (predictions will be in original scales)

```
dL_dZ()
dL_dtheta()
log_likelihood()
```

Compute the (lower bound on the) log marginal likelihood

```
update_likelihood_approximation(**kwargs)
```

Approximates a non-Gaussian likelihood using Expectation Propagation

For a Gaussian likelihood, no iteration is required: this function does nothing

#### GPy.core.gp module

```
 \begin{array}{c} \textbf{class} \; \texttt{GPy.core.gp.GP} \; (\textit{X, likelihood, kernel, normalize\_X=False}) \\ \textbf{Bases:} \; \texttt{GPy.core.gp\_base.GPBase} \end{array}
```

Gaussian Process model for regression and EP

#### **Parameters**

- **X** input observations
- kernel a GPy kernel, defaults to rbf+white
- likelihood a GPy likelihood
- **normalize\_X** (*False|True*) whether to normalize the input data before computing (predictions will be in original scales)

**Return type** model object

**Note:** Multiple independent outputs are allowed using columns of Y

```
getstate()
```

```
log_likelihood()
```

The log marginal likelihood of the GP.

For an EP model, can be written as the log likelihood of a regression model for a new variable  $Y^* = v_{tilde/tau_tilde}$ , with a covariance matrix  $K^* = K + diag(1./tau_{tilde})$  plus a normalization term.

```
predict (Xnew, which_parts='all', full_cov=False, **likelihood_args)
```

Predict the function(s) at the new point(s) Xnew.

# **Parameters**

- **Xnew** (np.ndarray, Nnew x self.input\_dim) The points at which to make a prediction
- which\_parts (('all', list of bools)) specifies which outputs kernel(s) to use in prediction
- full\_cov (bool) whether to return the full covariance matrix, or just the diagonal

**Returns** mean: posterior mean, a Numpy array, Nnew x self.input\_dim

**Returns** var: posterior variance, a Numpy array, Nnew x 1 if full\_cov=False, Nnew x Nnew otherwise

#### Returns

lower and upper boundaries of the 95% confidence intervals, Numpy arrays, Nnew x self.input\_dim

If full\_cov and self.input\_dim > 1, the return shape of var is Nnew x Nnew x self.input\_dim. If self.input\_dim == 1, the return shape is Nnew x Nnew. This is to allow for different normalizations of the output dimensions.

```
predict_single_output (Xnew, output=0, which_parts='all', full_cov=False, likeli-
hood_args={})
```

For a specific output, calls predict() at the new point(s) Xnew. This functions calls \_add\_output\_index(), so Xnew should not have an index column specifying the output.

#### **Parameters**

- **Xnew** (*np.ndarray*, *Nnew x self.input\_dim*) The points at which to make a prediction
- which\_parts (('all', list of bools)) specifies which outputs kernel(s) to use in prediction
- full\_cov (bool) whether to return the full covariance matrix, or just the diagonal

**Returns** mean: posterior mean, a Numpy array, Nnew x self.input\_dim

**Returns** var: posterior variance, a Numpy array, Nnew x 1 if full\_cov=False, Nnew x Nnew otherwise

**Returns** lower and upper boundaries of the 95% confidence intervals, Numpy arrays, Nnew x self.input dim

**Note:** For multiple non-independent outputs models only.

```
setstate(state)
```

```
update_likelihood_approximation(**kwargs)
```

Approximates a non-gaussian likelihood using Expectation Propagation

For a Gaussian likelihood, no iteration is required: this function does nothing

# GPy.core.gp base module

```
class GPy.core.gp_base.GPBase(X, likelihood, kernel, normalize_X=False)
    Bases: GPy.core.model.Model
```

Gaussian process base model for holding shared behaviour between sparse\_GP and GP models, and potentially other models in the future.

Here we define some functions that are use

```
getstate()
```

Get the curent state of the class. This is only used to efficiently pickle the model. See also self.setstate

```
log_predictive_density(x_test, y_test)
```

Calculation of the log predictive density

#### **Parameters**

- x test ((Nx1) array) test observations (x {\*})
- **y\_test** ((Nx1) array) test observations (y\_{\*})

plot (plot\_limits=None, which\_data\_rows='all', which\_data\_ycols='all', which\_parts='all',
 fixed\_inputs=[], levels=20, samples=0, fignum=None, ax=None, resolution=None,
 plot\_raw=False, linecol='#204a87', fillcol='#729fcf')

# Plot the posterior of the GP.

- In one dimension, the function is plotted with a shaded region identifying two standard deviations.
- In two dimsensions, a contour-plot shows the mean predicted function
- In higher dimensions, use fixed\_inputs to plot the GP with some of the inputs fixed.

Can plot only part of the data and part of the posterior functions using which\_data\_rowsm which\_data\_ycols and which\_parts

# **Parameters**

- **plot\_limits** (*np.array*) The limits of the plot. If 1D [xmin,xmax], if 2D [[xmin,ymin],[xmax,ymax]]. Defaluts to data limits
- which\_data\_rows ('all' or a list of integers) which of the training data to plot (default all)
- which\_data\_ycols when the data has several columns (independant outputs), only plot these
- which\_parts ('all', or list of bools) which of the kernel functions to plot (additively)
- fixed\_inputs (a list of tuples) a list of tuple [(i,v), (i,v)...], specifying that input index i should be set to value v.
- **resolution** (*int*) the number of intervals to sample the GP on. Defaults to 200 in 1D and 50 (a 50x50 grid) in 2D
- **levels** (*int*) number of levels to plot in a contour plot.
- samples (int) the number of a posteriori samples to plot
- **fignum** (*figure number*) figure to plot on.
- ax (axes handle) axes to plot on.
- linecol color of line to plot.
- fillcol color of fill
- **levels** for 2D plotting, the number of contour levels to use is ax is None, create a new figure

```
plot_f (*args, **kwargs)
```

Plot the GP's view of the world, where the data is normalized and before applying a likelihood.

This is a convenience function: we simply call self.plot with the argument use\_raw\_predict set True. All args and kwargs are passed on to plot.

```
see also: gp_base.plot
```

**posterior\_samples** (X, size=10,  $which\_parts='all'$ ,  $noise\_model=None$ ) Samples the posterior GP at the points X.

#### **Parameters**

- **X** (np.ndarray, Nnew x self.input\_dim.) the points at which to take the samples.
- size (int.) the number of a posteriori samples to plot.
- which\_parts ('all', or list of bools.) which of the kernel functions to plot (additively).

- full\_cov (bool.) whether to return the full covariance matrix, or just the diagonal.
- **noise model** (*integer*.) for mixed noise likelihood, the noise model to use in the samples.

Returns Ysim: set of simulations, a Numpy array (N x samples).

```
posterior_samples_f (X, size=10, which_parts='all')
```

Samples the posterior GP at the points X.

#### **Parameters**

- **X** (*np.ndarray, Nnew x self.input\_dim.*) The points at which to take the samples.
- size (int.) the number of a posteriori samples to plot.
- which\_parts ('all', or list of bools.) which of the kernel functions to plot (additively).
- full\_cov (bool.) whether to return the full covariance matrix, or just the diagonal.

Returns Ysim: set of simulations, a Numpy array (N x samples).

```
setstate(state)
```

Set the state of the model. Used for efficient pickling

# GPy.core.mapping module

```
class GPy.core.mapping.Mapping(input_dim, output_dim)
     Bases: GPy.core.parameterized.Parameterized
```

Base model for shared behavior between models that can act like a mapping.

```
df_dx (dL_df, X)
```

Evaluate derivatives of mapping outputs with respect to inputs.

#### **Parameters**

- **dL\_df** (*ndarray* (*num\_data* x *output\_dim*)) gradient of the objective with respect to the function.
- **X** (*ndarray* (*num\_data* x *input\_dim*)) the input locations where derivatives are to be evaluated.

**Returns** matrix containing gradients of the function with respect to the inputs.

```
df dtheta(dL df, X)
```

The gradient of the outputs of the multi-layer perceptron with respect to each of the parameters. :param dL\_df: gradient of the objective with respect to the function. :type dL\_df: ndarray (num\_data x output\_dim) :param X: input locations where the function is evaluated. :type X: ndarray (num\_data x input\_dim) :returns: Matrix containing gradients with respect to parameters of each output for each input data. :rtype: ndarray (num\_params length)

```
f(X)
```

```
plot (plot_limits=None, which_data='all', which_parts='all', resolution=None, levels=20, samples=0,
     fignum=None, ax=None, fixed_inputs=[], linecol='#204a87')
Plot the mapping.
```

# Plots the mapping associated with the model.

- In one dimension, the function is plotted.
- In two dimsensions, a contour-plot shows the function
- In higher dimensions, we've not implemented this yet !TODO!

Can plot only part of the data and part of the posterior functions using which\_data and which\_functions

#### **Parameters**

- **plot\_limits** (*np.array*) The limits of the plot. If 1D [xmin,xmax], if 2D [[xmin,ymin],[xmax,ymax]]. Defaluts to data limits
- which\_data ('all' or a slice object to slice self.X, self.Y) which if the training data to plot (default all)
- which\_parts ('all', or list of bools) which of the kernel functions to plot (additively)
- **resolution** (*int*) the number of intervals to sample the GP on. Defaults to 200 in 1D and 50 (a 50x50 grid) in 2D
- **levels** (*int*) number of levels to plot in a contour plot.
- samples (int) the number of a posteriori samples to plot
- **fignum** (*figure number*) figure to plot on.
- ax (axes handle) axes to plot on.
- fixed\_inputs (a list of tuples) a list of tuple [(i,v), (i,v)...], specifying that input index i should be set to value v.
- **linecol** color of line to plot.
- **levels** for 2D plotting, the number of contour levels to use is ax is None, create a new figure

```
class GPy.core.mapping.Mapping_check_df_dX (mapping=None, dL_df=None, X=None)
    Bases: GPy.core.mapping.Mapping_check_model
```

This class allows gradient checks for the gradient of a mapping with respect to X.

```
class GPy.core.mapping.Mapping_check_df_dtheta(mapping=None, dL_df=None, X=None)
    Bases: GPy.core.mapping.Mapping_check_model
```

This class allows gradient checks for the gradient of a mapping with respect to parameters.

```
class GPy.core.mapping.Mapping_check_model (mapping=None, dL_df=None, X=None)
    Bases: GPy.core.model.Model
```

This is a dummy model class used as a base class for checking that the gradients of a given mapping are implemented correctly. It enables checkgradient() to be called independently on each mapping.

```
log_likelihood()
```

#### GPy.core.model module

```
class GPy.core.model.Model
    Bases: GPy.core.parameterized.Parameterized
    Laplace_covariance()
```

return the covariance matrix of a Laplace approximation at the current (stationary) point.

#### Laplace\_evidence()

Returns an estiamte of the model evidence based on the Laplace approximation. Uses a numerical estimate of the Hessian if none is available analytically.

```
checkgrad (target_param=None, verbose=False, step=1e-06, tolerance=0.001)
```

Check the gradient of the ,odel by comparing to a numerical estimate. If the verbose flag is passed, invividual components are tested (and printed)

#### **Parameters**

- verbose (bool) If True, print a "full" checking of each parameter
- step (float (default 1e-6)) The size of the step around which to linearise the objective
- **tolerance** (*float* (*default 1e-3*)) the tolerance allowed (see note)

**Note:-** The gradient is considered correct if the ratio of the analytical and numerical gradients is within <tolerance> of unity.

#### ensure\_default\_constraints()

Ensure that any variables which should clearly be positive have been constrained somehow. The method performs a regular expression search on parameter names looking for the terms 'variance', 'lengthscale', 'precision' and 'kappa'. If any of these terms are present in the name the parameter is constrained positive.

# get\_gradient (name, return\_names=False)

Get model gradient(s) by name. The name is applied as a regular expression and all parameters that match that regular expression are returned.

#### **Parameters**

- name (regular expression) the name of parameters required (as a regular expression).
- return\_names (bool) whether or not to return the names matched (default False)

#### getstate()

Get the current state of the class. Inherited from Parameterized, so add those parameters to the state

**Returns** list of states from the model.

#### input\_sensitivity()

return an array describing the sesitivity of the model to each input

NB. Right now, we're basing this on the lengthscales (or variances) of the kernel. TODO: proper sensitivity analysis where we integrate across the model inputs and evaluate the effect on the variance of the model output.

#### log\_likelihood()

#### log\_prior()

evaluate the prior

# objective\_and\_gradients(x)

Compute the objective function of the model and the gradient of the model at the point given by x.

**Parameters**  $\mathbf{x}$  – the point at which gradients are to be computed.

#### objective function(x)

The objective function passed to the optimizer. It combines the likelihood and the priors.

Failures are handled robustly. The algorithm will try several times to return the objective, and will raise the original exception if it the objective cannot be computed.

#### **Parameters**

- $\mathbf{x}$  the parameters of the model.
- type np.array

# objective\_function\_gradients(x)

Gets the gradients from the likelihood and the priors.

Failures are handled robustly. The algorithm will try several times to return the gradients, and will raise the original exception if it the objective cannot be computed.

#### **Parameters**

- $\mathbf{x}$  the parameters of the model.
- type np.array

```
optimize (optimizer=None, start=None, **kwargs)
```

Optimize the model using self.log\_likelihood and self.log\_likelihood\_gradient, as well as self.priors. kwargs are passed to the optimizer. They can be:

#### **Parameters**

- max\_f\_eval (int) maximum number of function evaluations
- **optimzer** (*string TODO: valid strings?*) which optimizer to use (defaults to self.preferred optimizer)

Messages whether to display during optimisation

```
optimize_SGD (momentum=0.1, learning_rate=0.01, iterations=20, **kwargs)
```

Perform random restarts of the model, and set the model to the best seen solution.

If the robust flag is set, exceptions raised during optimizations will be handled silently. If \_all\_ runs fail, the model is reset to the existing parameter values.

#### **Notes**

#### **Parameters**

- **num restarts** (*int*) number of restarts to use (default 10)
- **robust** (*bool*) whether to handle exceptions silently or not (default False)
- **parallel** (*bool*) whether to run each restart as a separate process. It relies on the multiprocessing module.
- num\_processes number of workers in the multiprocessing pool

#### **Parameters**

- max\_f\_eval (int) maximum number of function evaluations
- max\_iters (int) maximum number of iterations
- messages (bool) whether to display during optimisation

**Note:** If num\_processes is None, the number of workes in the multiprocessing pool is automatically set to the number of processors on the current machine.

```
pseudo_EM (stop_crit=0.1, **kwargs)
```

EM - like algorithm for Expectation Propagation and Laplace approximation

**Parameters stop\_crit** (*float*) – convergence criterion

#### randomize()

Randomize the model. Make this draw from the prior if one exists, else draw from N(0,1)

# set\_prior (regexp, what)

Sets priors on the model parameters.

#### **Notes**

<sup>\*\*</sup>kwargs are passed to the optimizer. They can be:

Asserts that the prior is suitable for the constraint. If the wrong constraint is in place, an error is raised. If no constraint is in place, one is added (warning printed).

For tied parameters, the prior will only be "counted" once, thus a prior object is only inserted on the first tied index

#### **Parameters**

- regexp regular expression of parameters on which priors need to be set.
- what (GPy.core.Prior type) prior to set on parameter.

#### setstate (state)

set state from previous call to getstate call Parameterized with the rest of the state

**Parameters** state (*list as returned from getstate.*) – the state of the model.

# GPy.core.parameterized module

```
class GPy.core.parameterized.Parameterized
    Bases: object
    all_constrained_indices()
    constrain(regexp, transform, warning=True)
    constrain_bounded(regexp, lower, upper, warning=True)
        Set bounded constraints.
    constrain_fixed(regexp, value=None, warning=True)
```

#### **Parameters**

- regexp (ndarray(dtype=int) or regular expression object or string) which parameters need to be fixed.
- value (float) the value to fix the parameters to. If the value is not specified, the parameter is fixed to the current value

#### Notes

Fixing a parameter which is tied to another, or constrained in some way will result in an error.

To fix multiple parameters to the same value, simply pass a regular expression which matches both parameter names, or pass both of the indexes.

```
constrain_negative (regexp, warning=True)
    Set negative constraints.
constrain_positive (regexp, warning=True)
    Set positive constraints.
copy()
    Returns a (deep) copy of the current model
getstate()
```

Get the current state of the class, here just all the indices, rest can get recomputed For inheriting from Parameterized:

Allways append the state of the inherited object and call down to the inherited object in setstate!!

```
grep_model (regexp)
grep_param_names (regexp, transformed=False, search=False)
```

**Parameters regexp**  $(re \mid str \mid int)$  – regular expression to select parameter names **Return type** the indices of self.\_get\_param\_names which match the regular expression.

Note:- Other objects are passed through - i.e. integers which weren't meant for grepping

```
num_params_transformed()
pickle(filename, protocol=-1)
setstate(state)
tie_params(regexp)
        Tie (all!) parameters matching the regular expression regexp.
unconstrain(regexp)
        Unconstrain matching parameters. Does not untie parameters
untie_everything()
        Unties all parameters by setting tied_indices to an empty list.
```

# GPy.core.priors module

```
class GPy.core.priors.Gamma (a, b)
    Bases: GPy.core.priors.Prior
```

Implementation of the Gamma probability function, coupled with random variables.

#### **Parameters**

- **a** shape parameter
- **b** rate parameter (warning: it's the *inverse* of the scale)

**Note:** Bishop 2006 notation is used throughout the code

```
domain = 'positive'
static from_EV (E, V)
```

Creates an instance of a Gamma Prior by specifying the Expected value(s) and Variance(s) of the distribution.

#### **Parameters**

- E expected value
- V variance

```
lnpdf(x)
lnpdf_grad(x)
rvs(n)
summary()
class GPy.core.priors.Gaussian(mu, sigma)
Bases: GPy.core.priors.Prior
```

Implementation of the univariate Gaussian probability function, coupled with random variables.

#### **Parameters**

• mu – mean

• sigma – standard deviation

```
Note: Bishop 2006 notation is used throughout the code
```

```
domain = 'real'
lnpdf(x)
lnpdf_grad(x)
rvs(n)
class GPy.core.priors.LogGaussian(mu, sigma)
Bases: GPy.core.priors.Prior
```

Implementation of the univariate log-Gaussian probability function, coupled with random variables.

# **Parameters**

- mu mean
- sigma standard deviation

Note: Bishop 2006 notation is used throughout the code

Implementation of the multivariate Gaussian probability function, coupled with random variables.

# **Parameters**

- **mu** mean (N-dimensional array)
- var covariance matrix (NxN)

Note: Bishop 2006 notation is used throughout the code

```
domain = 'real'
lnpdf(x)
lnpdf_grad(x)
pdf(x)
plot()
rvs(n)
summary()
class GPy.core.priors.Prior
domain = None
pdf(x)
plot()
```

```
GPy.core.priors.gamma_from_EV (E, V) class GPy.core.priors.inverse_gamma (a, b) Bases: GPy.core.priors.Prior
```

Implementation of the inverse-Gamma probability function, coupled with random variables.

#### **Parameters**

- **a** shape parameter
- **b** rate parameter (warning: it's the *inverse* of the scale)

Note: Bishop 2006 notation is used throughout the code

```
domain = 'positive'
lnpdf(x)
lnpdf_grad(x)
rvs(n)
```

#### GPy.core.sparse\_gp module

```
 \begin{array}{lll} \textbf{class} \ \texttt{GPy.core.sparse\_gp.SparseGP} \ (X, & likelihood, & kernel, & Z, & X\_variance=None, & normal-ize\_X=False) \\ \textbf{Bases:} \ \texttt{GPy.core.gp\_base.GPBase} \end{array}
```

Variational sparse GP model

#### **Parameters**

- **X** (*np.ndarray* (*num\_data x input\_dim*)) inputs
- **likelihood** (*GPy.likelihood.*(*Gaussian* | *EP* | *Laplace*)) a likelihood instance, containing the observed data
- **kernel** (a GPy.kern.kern instance) the kernel (covariance function). See link kernels
- **X\_variance** (*np.ndarray* (*num\_data x input\_dim*) | *None*) The uncertainty in the measurements of X (Gaussian variance)
- **Z** (*np.ndarray* (*num\_inducing x input\_dim*) | *None*) inducing inputs (optional, see note)
- **num\_inducing** (*int*) Number of inducing points (optional, default 10. Ignored if Z is not None)
- **normalize\_(XIY)** (*bool*) whether to normalize the data before computing (predictions will be in original scales)

# $dL_dz$ ()

The derivative of the bound wrt the inducing inputs Z

# ${\tt dL\_dtheta}\,(\,)$

Compute and return the derivative of the log marginal likelihood wrt the parameters of the kernel

#### getstate()

Get the current state of the class, here just all the indices, rest can get recomputed

# log\_likelihood()

Compute the (lower bound on the) log marginal likelihood

# Plot the posterior of the sparse GP.

- In one dimension, the function is plotted with a shaded region identifying two standard deviations.
- In two dimsensions, a contour-plot shows the mean predicted function
- In higher dimensions, use fixed\_inputs to plot the GP with some of the inputs fixed.

Can plot only part of the data and part of the posterior functions using which\_data\_rowsm which\_data\_ycols and which\_parts

#### **Parameters**

- **plot\_limits** (*np.array*) The limits of the plot. If 1D [xmin,xmax], if 2D [[xmin,ymin],[xmax,ymax]]. Defaluts to data limits
- which\_data\_rows ('all' or a list of integers) which of the training data to plot (default all)
- which\_data\_ycols when the data has several columns (independant outputs), only plot these
- which parts ('all', or list of bools) which of the kernel functions to plot (additively)
- fixed\_inputs (a list of tuples) a list of tuple [(i,v), (i,v)...], specifying that input index i should be set to value v.
- **resolution** (*int*) the number of intervals to sample the GP on. Defaults to 200 in 1D and 50 (a 50x50 grid) in 2D
- **levels** (*int*) number of levels to plot in a contour plot.
- samples (int) the number of a posteriori samples to plot
- **fignum** (*figure number*) figure to plot on.
- ax (axes handle) axes to plot on.
- linecol color of line to plot.
- fillcol color of fill
- **levels** for 2D plotting, the number of contour levels to use is ax is None, create a new figure

#### Plot the GP's view of the world, where the data is normalized and the

- In one dimension, the function is plotted with a shaded region identifying two standard deviations.
- In two dimsensions, a contour-plot shows the mean predicted function
- · Not implemented in higher dimensions

#### **Parameters**

- samples the number of a posteriori samples to plot
- **plot\_limits** The limits of the plot. If 1D [xmin,xmax], if 2D [[xmin,ymin],[xmax,ymax]]. Defaluts to data limits

- which\_data\_rows ('all' or a slice object to slice self.X, self.Y) which if the training data to plot (default all)
- which\_parts ('all', or list of bools) which of the kernel functions to plot (additively)
- **resolution** (*int*) the number of intervals to sample the GP on. Defaults to 200 in 1D and 50 (a 50x50 grid) in 2D
- **full\_cov** (bool :param fignum: figure to plot on.) –
- ax (axes handle) axes to plot on.
- **output** (*integer* (*first output is 0*)) which output to plot (for multiple output models only)

predict (Xnew, X\_variance\_new=None, which\_parts='all', full\_cov=False, \*\*likelihood\_args)
Predict the function(s) at the new point(s) Xnew.

# **Arguments**

#### **Parameters**

- **Xnew** (*np.ndarray*, *Nnew x self.input\_dim*) The points at which to make a prediction
- **X\_variance\_new** (*np.ndarray, Nnew x self.input\_dim*) The uncertainty in the prediction points
- which\_parts (('all', list of bools)) specifies which outputs kernel(s) to use in prediction
- full\_cov (bool) whether to return the full covariance matrix, or just the diagonal

Return type posterior mean, a Numpy array, Nnew x self.input\_dim

**Return type** posterior variance, a Numpy array, Nnew x 1 if full\_cov=False, Nnew x Nnew otherwise

# Return type

lower and upper boundaries of the 95% confidence intervals, Numpy arrays, Nnew x self.input\_dim

If full\_cov and self.input\_dim > 1, the return shape of var is Nnew x Nnew x self.input\_dim. If self.input\_dim == 1, the return shape is Nnew x Nnew. This is to allow for different normalizations of the output dimensions.

setstate (state)

# update\_likelihood\_approximation(\*\*kwargs)

Approximates a non-gaussian likelihood using Expectation Propagation

For a Gaussian likelihood, no iteration is required: this function does nothing

# GPy.core.svigp module

```
class GPy.core.svigp.SVIGP (X, likelihood, kernel, Z, q_u=None, batchsize=10, X_variance=None)
    Bases: GPy.core.gp_base.GPBase
```

Stochastic Variational inference in a Gaussian Process

#### **Parameters**

- **X** (np.ndarray (num data x num inputs)) inputs
- Y (np.ndarray of observations (num\_data x output\_dim)) observed data
- batchsize the size of a minibatch

```
• q_u (np.ndarray) – canonical parameters of the distribution squasehd into a 1D array
           • kernel (a GPy kernel) – the kernel/covariance function. See link kernels
           • Z (np.ndarray (num_inducing x num_inputs)) – inducing inputs
dL_dtheta()
get_vb_param()
     Return the canonical parameters of the distribution q(u)
getstate()
load_batch()
     load a batch of data (set self.X_batch and self.likelihood.Y from self.X, self.Y)
log_likelihood()
     As for uncollapsed sparse GP, but account for the proportion of data we're looking at right now.
     NB. self.batchsize is the size of the batch, not the size of X_all
optimize (iterations, print_interval=10, callback=<function <lambda> at 0x7f37af1867d0>, call-
            back interval=5)
plot (ax=None, fignum=None, Z_height=None, **kwargs)
plot_traces()
predict (Xnew, X_variance_new=None, which_parts='all', full_cov=False, sampling=False,
          num\_samples=15000)
set vb param(vb param)
     set the distribution q(u) from the canonical parameters
setstate(state)
vb grad natgrad()
     Compute the gradients of the lower bound wrt the canonical and Expectation parameters of u.
```

Note that the natural gradient in either is given by the gradient in the other (See Hensman et al 2012 Fast Variational inference in the conjugate exponential Family)

# GPy.core.transformations module

```
class GPy.core.transformations.exponent
    Bases: GPy.core.transformations.transformation
    domain = 'positive'
    \mathbf{f}(x)
    finv(x)
    gradfactor(f)
    initialize(f)
class GPy.core.transformations.logexp
    Bases: GPy.core.transformations.transformation
    domain = 'positive'
    \mathbf{f}(x)
    finv(f)
```

```
gradfactor(f)
    initialize(f)
class GPy.core.transformations.logexp_clipped(lower=1e-06)
    Bases: GPy.core.transformations.logexp
    domain = 'positive'
    \mathbf{f}(x)
    finv(f)
    gradfactor(f)
    initialize(f)
    log_max_bound = 230.25850929940458
    log_min_bound = -23.025850929940457
    max\_bound = 1e+100
    min bound = 1e-10
class GPy.core.transformations.logistic(lower, upper)
    Bases: GPy.core.transformations.transformation
    domain = 'bounded'
    \mathbf{f}(x)
    finv(f)
    gradfactor(f)
    initialize(f)
class GPy.core.transformations.negative_exponent
    Bases: GPy.core.transformations.exponent
    domain = 'negative'
    \mathbf{f}(x)
    finv(f)
    gradfactor(f)
    initialize(f)
class GPy.core.transformations.negative_logexp
    Bases: GPy.core.transformations.transformation
    domain = 'negative'
    \mathbf{f}(x)
    finv(f)
    gradfactor(f)
    initialize(f)
class GPy.core.transformations.square
    Bases: GPy.core.transformations.transformation
    domain = 'positive'
    f(x)
```

```
finv(x)
     gradfactor(f)
     initialize(f)
class GPy.core.transformations.transformation
     Bases: object
     domain = None
     f(x)
     finv(x)
     gradfactor(f)
          df_dx evaluated at self.f(x)=f
     initialize(f)
          produce a sensible initial value for f(x)
Module contents
GPy.examples package
Submodules
GPy.examples.classification module
Gaussian Processes classification
GPy.examples.classification.crescent_data(model_type='Full',
                                                                                 num inducing=10,
                                                       seed=10000, kernel=None, optimize=True,
                                                       plot=True)
     Run a Gaussian process classification on the crescent data. The demonstration calls the basic GP classification
     model and uses EP to approximate the likelihood.
          Parameters
                • model_type – type of model to fit ['Full', 'FITC', 'DTC'].
                • inducing (int) – number of inducing variables (only used for 'FITC' or 'DTC').
                • seed (int) – seed value for data generation.
                • kernel (a GPy kernel) – kernel to use in the model
GPy.examples.classification.oil(num_inducing=50, max_iters=100, kernel=None,
                                          mize=True, plot=True)
     Run a Gaussian process classification on the three phase oil data. The demonstration calls the basic GP classifi-
     cation model and uses EP to approximate the likelihood.
GPy.examples.classification.sparse_toy_linear_1d_classification(num_inducing=10,
                                                                                    seed=10000,
                                                                                    opti-
                                                                                    mize=True,
                                                                                    plot=True)
     Sparse 1D classification example
```

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**Parameters seed** (*int*) – seed value for data generation (default is 4).

```
GPy.examples.classification.toy heaviside (seed=10000, optimize=True, plot=True)
     Simple 1D classification example using a heavy side gp transformation
         Parameters seed (int) – seed value for data generation (default is 4).
GPy.examples.classification.toy_linear_1d_classification(seed=10000,
                                                                                       opti-
                                                                      mize=True, plot=True)
     Simple 1D classification example using EP approximation
         Parameters seed (int) – seed value for data generation (default is 4).
GPy.examples.classification.toy_linear_1d_classification_laplace(seed=10000,
                                                                                opti-
                                                                                mize=True,
                                                                                plot=True)
     Simple 1D classification example using Laplace approximation
         Parameters seed (int) – seed value for data generation (default is 4).
GPy.examples.dimensionality_reduction module
GPy.examples.dimensionality_reduction.bcgplvm_linear_stick(kernel=None,
                                                                         optimize=True,
                                                                         verbose=True,
                                                                         plot=True)
GPy.examples.dimensionality_reduction.bcgplvm_stick(kernel=None,
                                                                               optimize=True,
                                                                verbose=True, plot=True)
GPy.examples.dimensionality_reduction.bgplvm_oil(optimize=True,
                                                                                  verbose=1.
                                                                           N=200,
                                                            plot=True,
                                                                                       O = 7,
                                                            num_inducing=40, max_iters=1000,
                                                            **k)
GPy.examples.dimensionality reduction.bqplvm simulation(optimize=True,
                                                                                        ver-
                                                                     bose=1.
                                                                                  plot=True,
                                                                     plot_sim=False,
                                                                     max iters=20000.0)
GPy.examples.dimensionality_reduction.bgplvm_test_model(seed=None,
                                                                                       opti-
                                                                     mize=False,
                                                                                  verbose=1,
                                                                     plot=False)
     model for testing purposes. Samples from a GP with rbf kernel and learns the samples with a new kernel.
     Normally not for optimization, just model cheking
GPy.examples.dimensionality reduction.brendan faces (optimize=True,
                                                                               verbose=True,
                                                                plot=True)
GPy.examples.dimensionality reduction.cmu mocap (subject='35',
                                                                               motion=['01'],
                                                           in place=True,
                                                                               optimize=True,
                                                           verbose=True, plot=True)
GPy.examples.dimensionality_reduction.gplvm_oil_100(optimize=True,
                                                                                  verbose=1,
                                                                plot=True)
GPy.examples.dimensionality_reduction.mrd_simulation(optimize=True, verbose=True,
                                                                 plot=True,
                                                                              plot_sim=True,
                                                                 **kw)
GPy.examples.dimensionality_reduction.olivetti_faces(optimize=True, verbose=True,
                                                                 plot=True)
```

```
GPy.examples.dimensionality_reduction.robot_wireless(optimize=True, verbose=True,
                                                              plot=True)
GPy.examples.dimensionality reduction.sparse qplvm oil(optimize=True,
                                                                                   ver-
                                                                bose=0, plot=True, N=100,
                                                                0 = 6.
                                                                       num inducing=15,
                                                                max iters=50)
GPy.examples.dimensionality_reduction.stick(kernel=None, optimize=True, verbose=True,
                                                   plot=True)
GPy.examples.dimensionality_reduction.stick_bgplvm(model=None, optimize=True, ver-
                                                           bose=True, plot=True)
GPy.examples.dimensionality_reduction.stick_play(range=None,
                                                                          frame rate=15,
                                                         optimize=False,
                                                                           verbose=True,
                                                         plot=True)
GPy.examples.dimensionality_reduction.swiss_roll(optimize=True,
                                                                             verbose=1,
                                                                               N=1000,
                                                         plot=True,
                                                         num_inducing=15,
                                                                                  Q=4
                                                         sigma=0.2)
```

#### GPy.examples.non\_gaussian module

- GPy.examples.non\_gaussian.boston\_example(optimize=True, plot=True)
- GPy.examples.non\_gaussian.student\_t\_approx(optimize=True, plot=True)
  Example of regressing with a student t likelihood using Laplace

# GPy.examples.regression module

# Gaussian Processes regression examples

- GPy.examples.regression.coregionalization\_sparse(optimize=True, plot=True)
  A simple demonstration of coregionalization on two sinusoidal functions using sparse approximations.
- GPy.examples.regression.coregionalization\_toy2(optimize=True, plot=True)
  A simple demonstration of coregionalization on two sinusoidal functions.
- GPy.examples.regression.epomeo\_gpx (max\_iters=200, optimize=True, plot=True)

  Perform Gaussian process regression on the latitude and longitude data from the Mount Epomeo runs. Requires gpxpy to be installed on your system to load in the data.
- GPy.examples.regression.multiple\_optima (gene\_number=937, resolution=80, model\_restarts=10, seed=10000, max\_iters=300, optimize=True, plot=True)

  Show an example of a multimodal error surface for Gaussian process regression. Gene 939 has bimodal behaviour where the noisy mode is higher.
- GPy.examples.regression.olympic\_100m\_men(optimize=True, plot=True)
- GPy.examples.regression.olympic\_marathon\_men(optimize=True, plot=True)
  Run a standard Gaussian process regression on the Olympic marathon data.

Run a standard Gaussian process regression on the Rogers and Girolami olympics data.

GPy.examples.regression.robot\_wireless ( $max\_iters=100$ , kernel=None, optimize=True, plot=True)

Predict the location of a robot given wirelss signal strength readings.

GPy.examples.regression.silhouette(max iters=100, optimize=True, plot=True) Predict the pose of a figure given a silhouette. This is a task from Agarwal and Triggs 2004 ICML paper. GPy.examples.regression.sparse\_GP\_regression\_1D (num\_samples=400, num\_inducing=5, max iters=100, optimize=True, plot=True) Run a 1D example of a sparse GP regression. GPy.examples.regression.sparse\_GP\_regression\_2D (num\_samples=400,  $num\ inducing=50$ , max iters=100, optimize=True, plot=True) Run a 2D example of a sparse GP regression. GPy.examples.regression.toy\_ARD (max\_iters=1000, kernel\_type='linear', num\_samples=300, D=4, optimize=True, plot=True) GPy.examples.regression.toy\_ARD\_sparse(max\_iters=1000, kernel type='linear', optimize=True,  $num\_samples=300$ , D=4plot=True) GPy.examples.regression.toy\_poisson\_rbf\_1d\_laplace(optimize=True, plot=True) Run a simple demonstration of a standard Gaussian process fitting it to data sampled from an RBF covariance. GPy.examples.regression.toy\_rbf\_1d(optimize=True, plot=True) Run a simple demonstration of a standard Gaussian process fitting it to data sampled from an RBF covariance. GPy.examples.regression.toy\_rbf\_1d\_50 (optimize=True, plot=True) Run a simple demonstration of a standard Gaussian process fitting it to data sampled from an RBF covariance. GPy.examples.regression.uncertain\_inputs\_sparse\_regression(max\_iters=200,

# GPy.examples.stochastic module

GPy.examples.stochastic.toy\_1d(optimize=True, plot=True)

Run a 1D example of a sparse GP regression with uncertain inputs.

#### GPy.examples.tutorials module

#### Code of Tutorials

- GPy.examples.tutorials.model\_interaction(optimize=True, plot=True)
- GPy.examples.tutorials.tuto\_GP\_regression (optimize=True, plot=True)

  The detailed explanations of the commands used in this file can be found in the tutorial section
- GPy.examples.tutorials.tuto\_kernel\_overview(optimize=True, plot=True)

  The detailed explanations of the commands used in this file can be found in the tutorial section

optimize=True,
plot=True)

#### **Module contents**

# GPy.inference package

#### **Submodules**

#### GPy.inference.conjugate gradient descent module

```
Created on 24 Apr 2013
@author: maxz
class GPy.inference.conjugate gradient descent. Async Optimize
     Bases: object
     SENTINEL = 'SENTINEL'
     async\_callback\_collect(q)
     callback (*x)
     opt (f, df, x0, callback=None, update rule=<class GPv.inference.gradient descent update rules.FletcherReeves
           at 0xff37ad8317a0>, messages=0, maxiter=5000.0, max_f_eval=15000.0, gtol=1e-06, re-
           port_every=10, *args, **kwargs)
     opt_async (f, df, x0, callback, update_rule=<class GPy.inference.gradient_descent_update_rules.PolakRibiere
                   at 0x7f37ad831738>, messages=0, maxiter=5000.0, max_f_eval=15000.0, gtol=1e-06,
                   report_every=10, *args, **kwargs)
     runsignal = <multiprocessing.synchronize.Event object at 0x7f37ae075450>
class GPy.inference.conjugate_gradient_descent.CGD
     Bases: GPy.inference.conjugate_gradient_descent.Async_Optimize
     Conjugate gradient descent algorithm to minimize function f with gradients df, starting at x0 with update rule
     update_rule
     if df returns tuple (grad, natgrad) it will optimize according to natural gradient rules
     opt (*a, **kw)
          opt(self, f, df, x0, callback=None, update rule=FletcherReeves, messages=0,
                                                                                               maxiter=5e3,
               max_f_eval=15e3, gtol=1e-6, report_every=10, *args, **kwargs)
          Minimize f, calling callback every report_every iterations with following syntax:
               callback(xi, fi, gi, iteration, function_calls, gradient_calls, status_message)
          if df returns tuple (grad, natgrad) it will optimize according to natural gradient rules
          f, and df will be called with
               f(xi, *args, **kwargs) df(xi, *args, **kwargs)
          returns
               x_opt, f_opt, g_opt, iteration, function_calls, gradient_calls, status_message
          at end of optimization
     opt_async(*a, **kw)
          opt_async(self, f, df, x0, callback, update_rule=FletcherReeves, messages=0,
                                                                                               maxiter=5e3.
               max f eval=15e3, gtol=1e-6, report every=10, *args, **kwargs)
```

```
callback gets called every report_every iterations
              callback(xi, fi, gi, iteration, function_calls, gradient_calls, status_message)
          if df returns tuple (grad, natgrad) it will optimize according to natural gradient rules
          f, and df will be called with
              f(xi, *args, **kwargs) df(xi, *args, **kwargs)
          Returns:
              Started Process object, optimizing asynchronously
          Calls:
              callback(x_opt, f_opt, g_opt, iteration, function_calls, gradient_calls, status_message)
          at end of optimization!
     opt_name = 'Conjugate Gradient Descent'
GPy.inference.gradient descent update rules module
Created on 24 Apr 2013
@author: maxz
class GPy.inference.gradient_descent_update_rules.FletcherReeves (initgrad,
                                                                                    gradnat=None)
     Bases: GPy.inference.gradient_descent_update_rules.GDUpdateRule
     Fletcher Reeves update rule for gamma
class GPy.inference.gradient_descent_update_rules.GDUpdateRule(initgrad, initgrad-
                                                                                 nat=None)
class GPy.inference.gradient_descent_update_rules.PolakRibiere(initgrad, initgrad-
     Bases: GPy.inference.gradient_descent_update_rules.GDUpdateRule
     Fletcher Reeves update rule for gamma
GPy.inference.optimization module
class GPy.inference.optimization.Optimizer(x_init,
                                                                                       model=None,
                                                                  messages=False,
                                                      max \ f \ eval=10000.0,
                                                                                  max iters=1000.0,
                                                      ftol=None,
                                                                                         xtol=None,
                                                                       gtol=None,
                                                      bfgs_factor=None)
     Superclass for all the optimizers.
          Parameters
                • x_init – initial set of parameters
                • f fp – function that returns the function AND the gradients at the same time
                • f – function to optimize
                • fp – gradients
                • messages ((True | False)) – print messages from the optimizer?
                • max f eval – maximum number of function evaluations
```

```
Return type optimizer object.
     opt (f_fp=None, f=None, fp=None)
     plot()
     run (**kwargs)
GPy.inference.optimization.get optimizer(f min)
class GPy.inference.optimization.opt SCG(*args, **kwargs)
     Bases: GPy.inference.optimization.Optimizer
     opt (f_fp=None, f=None, fp=None)
class GPy.inference.optimization.opt_lbfgsb(*args, **kwargs)
     Bases: GPy.inference.optimization.Optimizer
     opt (f_fp=None, f=None, fp=None)
          Run the optimizer
class GPy.inference.optimization.opt_rasm(*args, **kwargs)
     Bases: GPy.inference.optimization.Optimizer
     opt (f_fp=None, f=None, fp=None)
          Run Rasmussen's Conjugate Gradient optimizer
class GPy.inference.optimization.opt_simplex(*args, **kwargs)
     Bases: GPy.inference.optimization.Optimizer
     opt (f_fp=None, f=None, fp=None)
          The simplex optimizer does not require gradients.
class GPy.inference.optimization.opt_tnc(*args, **kwargs)
     Bases: GPy.inference.optimization.Optimizer
     opt (f_fp=None, f=None, fp=None)
          Run the TNC optimizer
GPy.inference.samplers module
class GPy.inference.samplers.Metropolis Hastings (model, cov=None)
     new_chain (start=None)
     predict (function, args)
          Make a prediction for the function, to which we will pass the additional arguments
     sample (Ntotal, Nburn, Nthin, tune=True, tune_throughout=False, tune_interval=400)
GPy.inference.scg module
GPy.inference.scg. SCG(f, gradf, x, optargs=(), maxiters=500, max\_f\_eval=inf, display=True,
                            xtol=None, ftol=None, gtol=None)
     Optimisation through Scaled Conjugate Gradients (SCG)
     f: the objective function gradf: the gradient function (should return a 1D np.ndarray) x: the initial condition
     Returns x the optimal value for x flog: a list of all the objective values function_eval number of fn evaluations
     status: string describing convergence status
```

```
GPy.inference.scg.exponents(fnow, current_grad)
GPy.inference.scg.print_out(len_maxiters, fnow, current_grad, beta, iteration)
GPy.inference.sgd module
                                             iterations=10,
class GPy.inference.sqd.opt_SGD (start,
                                                              learning_rate=0.0001,
                                     tum = 0.9,
                                                model=None,
                                                              messages=False,
                                                                                batch\_size=1,
                                     self_paced=False, center=True, iteration_file=None, learn-
                                     ing_rate_adaptation=None, actual_iter=None, schedule=None,
     Bases: GPy.inference.optimization.Optimizer
     Optimize using stochastic gradient descent.
         Parameters
               • Model – reference to the Model object
               • iterations – number of iterations
               • learning_rate – learning rate
               • momentum – momentum
     adapt_learning_rate(t, D)
     check_for_missing(data)
     get_param_shapes (N=None, input_dim=None)
     non_null_samples(data)
     opt (f_fp=None, f=None, fp=None)
     plot_traces()
     restore\_constraints(c)
     shift_constraints(j)
     step_with_missing_data(f_fp, X, step, shapes)
     subset_parameter_vector (x, samples, param_shapes)
Module contents
GPy.kern package
```

# **Subpackages**

GPy.kern.parts package

# **Submodules**

# GPy.kern.parts.Brownian module

class GPy.kern.parts.Brownian.Brownian(input\_dim, variance=1.0)

Bases: GPy.kern.parts.kernpart.Kernpart

Brownian Motion kernel.

# **Parameters**

- **input\_dim** (*int*) the number of input dimensions
- variance (float) –

**K** (*X*, *X*2, target)

**Kdiag** (*X*, target)

 $dK_dX$  ( $dL_dK$ , X, X2, target)

dK\_dtheta (dL\_dK, X, X2, target)

dKdiag\_dX (dL\_dKdiag, X, target)

 $\texttt{dKdiag\_dtheta} (\textit{dL\_dKdiag}, \textit{X}, \textit{target})$ 

GPy.kern.parts.Brownian.theta(x)

Heavisdie step function

# GPy.kern.parts.Matern32 module

class GPy.kern.parts.Matern32.Matern32(input\_dim, variance=1.0, lengthscale=None,

ARD=False)

Bases: GPy.kern.parts.kernpart.Kernpart

Matern 3/2 kernel:

$$k(r) = \sigma^2 (1 + \sqrt{3}r) \exp(-\sqrt{3}r)$$
 where  $r = \sqrt{\sum_{i=1}^i nput_d im \frac{(x_i - y_i)^2}{\ell_i^2}}$ 

# **Parameters**

- **input\_dim** (*int*) the number of input dimensions
- variance (float) the variance  $\sigma^2$
- lengthscale (array or list of the appropriate size (or float if there is only one lengthscale parameter)) the vector of lengthscale  $\ell_i$
- ARD (Boolean) Auto Relevance Determination. If equal to "False", the kernel is isotropic
  (ie. one single lengthscale parameter ell), otherwise there is one lengthscale parameter per
  dimension.

Return type kernel object

**Gram matrix** (*F*, *F1*, *F2*, *lower*, *upper*)

Return the Gram matrix of the vector of functions F with respect to the RKHS norm. The use of this function is limited to input\_dim=1.

# **Parameters**

- **F** (*np.array*) vector of functions
- **F1** (*np.array*) vector of derivatives of F
- **F2** (*np.array*) vector of second derivatives of F
- **lower,upper** (*floats*) boundaries of the input domain

 $\mathbf{K}(X, X2, target)$ 

Compute the covariance matrix between X and X2.

Kdiag(X, target)

Compute the diagonal of the covariance matrix associated to X.

 $dK_dX$  ( $dL_dK$ , X, X2, target)

derivative of the covariance matrix with respect to X.

dK dtheta (dL dK, X, X2, target)

derivative of the covariance matrix with respect to the parameters.

dKdiag\_dX (dL\_dKdiag, X, target)

dKdiag\_dtheta(dL\_dKdiag, X, target)

derivative of the diagonal of the covariance matrix with respect to the parameters.

# GPy.kern.parts.Matern52 module

Bases: GPy.kern.parts.kernpart.Kernpart

Matern 5/2 kernel:

$$k(r) = \sigma^2 (1 + \sqrt{5}r + \frac{5}{3}r^2) \exp(-\sqrt{5}r)$$
 where  $r = \sqrt{\sum_{i=1}^{i} nput_d im \frac{(x_i - y_i)^2}{\ell_i^2}}$ 

#### **Parameters**

- input\_dim (int) the number of input dimensions
- variance (float) the variance  $\sigma^2$
- lengthscale (array or list of the appropriate size (or float if there is only one lengthscale parameter)) the vector of lengthscale  $\ell_i$
- **ARD** (*Boolean*) Auto Relevance Determination. If equal to "False", the kernel is isotropic (ie. one single lengthscale parameter ell), otherwise there is one lengthscale parameter per dimension.

Return type kernel object

**Gram matrix** (*F*, *F1*, *F2*, *F3*, *lower*, *upper*)

Return the Gram matrix of the vector of functions F with respect to the RKHS norm. The use of this function is limited to input\_dim=1.

#### **Parameters**

- **F** (*np.array*) vector of functions
- **F1** (*np.array*) vector of derivatives of F
- **F2** (*np.array*) vector of second derivatives of F
- **F3** (*np.array*) vector of third derivatives of F
- lower,upper (floats) boundaries of the input domain

 $\mathbf{K}(X, X2, target)$ 

Compute the covariance matrix between X and X2.

Kdiag(X, target)

Compute the diagonal of the covariance matrix associated to X.

```
dK dX (dL dK, X, X2, target)
```

derivative of the covariance matrix with respect to X.

# $dK_dtheta(dL_dK, X, X2, target)$

derivative of the covariance matrix with respect to the parameters.

```
dKdiag_dX (dL_dKdiag, X, target)
```

```
dKdiag_dtheta(dL_dKdiag, X, target)
```

derivative of the diagonal of the covariance matrix with respect to the parameters.

#### GPv.kern.parts.ODE 1 module

```
 \begin{array}{ll} \textbf{class} \; \texttt{GPy.kern.parts.ODE\_1.ODE\_1} \; (input\_dim=1, & variance U=1.0, & variance Y=1.0, & length-scale U=None, lengthscale Y=None) \end{array}
```

Bases: GPy.kern.parts.kernpart.Kernpart

kernel resultiong from a first order ODE with OU driving GP

#### **Parameters**

- **input\_dim** (*int*) the number of input dimension, has to be equal to one
- variance U (float) variance of the driving GP
- **lengthscale**U (*float*) lengthscale of the driving GP (sqrt(3)/lengthscaleU)
- varianceY (float) 'variance' of the transfer function
- **lengthscaleY** (*float*) 'lengthscale' of the transfer function (1/lengthscaleY)

# Return type kernel object

```
\mathbf{K}(X, X2, target)
```

Compute the covariance matrix between X and X2.

# Kdiag(X, target)

Compute the diagonal of the covariance matrix associated to X.

```
dK_dtheta(dL_dK, X, X2, target)
```

derivative of the covariance matrix with respect to the parameters.

#### **GPy.kern.parts.ODE** UY module

```
 \textbf{class} \ \texttt{GPy.kern.parts.ODE\_UY.ODE\_UY} \ (input\_dim=2, \quad variance U=1.0, \quad variance Y=1.0, \quad length-scale U=None, \ length scale Y=None)
```

Bases: GPy.kern.parts.kernpart.Kernpart

kernel resultiong from a first order ODE with OU driving GP

#### **Parameters**

- input\_dim (int) the number of input dimension, has to be equal to one
- input\_lengthU the number of input U length
- varianceU (float) variance of the driving GP
- **lengthscale**U (*float*) lengthscale of the driving GP (sqrt(3)/lengthscaleU)
- varianceY (float) 'variance' of the transfer function
- **lengthscaleY** (*float*) 'lengthscale' of the transfer function (1/lengthscaleY)

Return type kernel object

```
\mathbf{K}(X, X2, target)
          Compute the covariance matrix between X and X2.
     Kdiag(X, target)
          Compute the diagonal of the covariance matrix associated to X.
     dK dtheta(dL dK, X, X2, target)
          derivative of the covariance matrix with respect to the parameters.
GPy.kern.parts.ODE_UY.index_to_slices(index)
     take a numpy array of integers (index) and return a nested list of slices such that the slices describe the start,
     stop points for each integer in the index.
     e.g. >>  index = np.asarray([0,0,0,1,1,1,2,2,2]) returns >>  [[slice(0,3,None)],[slice(3,6,None)],[slice(6,9,None)]]
         a more complicated example >> index = np.asarray([0,0,1,1,0,2,2,2,1,1]) returns >>>
     [[slice(0,2,None),slice(4,5,None)],[slice(2,4,None),slice(8,10,None)],[slice(5,8,None)]]
GPy.kern.parts.bias module
class GPy.kern.parts.bias.Bias (input_dim, variance=1.0)
     Bases: GPy.kern.parts.kernpart.Kernpart
     K (X, X2, target)
     Kdiag(X, target)
     dK_dX (dL_dK, X, X2, target)
     dK_dtheta (dL_dKdiag, X, X2, target)
     dKdiag_dX (dL_dKdiag, X, target)
     dKdiag_dtheta(dL_dKdiag, X, target)
     dpsi0_dz (dL_dpsi0, Z, mu, S, target)
     dpsi0_dmuS (dL_dpsi0, Z, mu, S, target_mu, target_S)
     dpsi0_dtheta (dL_dpsi0, Z, mu, S, target)
     dpsi1 dZ (dL dpsi1, Z, mu, S, target)
     dpsil_dmuS(dL_dpsil, Z, mu, S, target_mu, target_S)
     dpsi1_dtheta (dL_dpsi1, Z, mu, S, target)
     dpsi2_dz (dL_dpsi2, Z, mu, S, target)
     dpsi2\_dmuS (dL\_dpsi2, Z, mu, S, target\_mu, target\_S)
     dpsi2_dtheta (dL_dpsi2, Z, mu, S, target)
     psi0(Z, mu, S, target)
     psil(Z, mu, S, target)
     psi2(Z, mu, S, target)
GPy.kern.parts.coregionalize module
class GPy.kern.parts.coregionalize.Coregionalize(output_dim,
                                                                                            W=None,
                                                                               rank=1,
                                                               kappa=None)
     Bases: GPy.kern.parts.kernpart.Kernpart
     Covariance function for intrinsic/linear coregionalization models
     This covariance has the form: .. math:
```

```
\mathbb{W} = \mathbb{W} \setminus \mathbb{W}^{0} + \mathbb{W} \in \mathbb{W}
```

An intrinsic/linear coregionalization covariance function of the form: .. math:

```
k_2(x, y) = \mathbb{B} k(x, y)
```

it is obtained as the tensor product between a covariance function k(x,y) and B.

#### **Parameters**

- output\_dim (int) number of outputs to coregionalize
- rank (int) number of columns of the W matrix (this parameter is ignored if parameter W is not None)
- W (numpy array of dimensionality (num\_outpus, W\_columns)) a low rank matrix that determines the correlations between the different outputs, together with kappa it forms the coregionalization matrix B
- **kappa** (*numpy array of dimensionality* (*output\_dim*,)) a vector which allows the outputs to behave independently

```
K (index, index2, target)
Kdiag (index, target)
dK_dX (dL_dK, X, X2, target)
dK_dtheta (dL_dK, index, index2, target)
dK_dtheta_old (dL_dK, index, index2, target)
dKdiag_dtheta (dL_dKdiag, index, target)
```

# GPy.kern.parts.eq\_ode1 module

Covariance function for first order differential equation driven by an exponentiated quadratic covariance.

This outputs of this kernel have the form .. math:

```
rac{ext{d}y_j}{ext{d}t} = sum_{i=1}^R w_{j,i} f_i(t-delta_j) + sqrt{kappa_j}g_j(t) - d_jy_j(t)
```

where R is the rank of the system,  $w_{j,i}$  is the sensitivity of the j'thoutputtothe : math : 'i'thlatentfunction,: math : ' $d_j$  is the decay rate of the j'thoutputand : math : ' $f_i(t)$  and  $g_i(t)$  are independent latent Gaussian processes governed by an exponentiated quadratic covariance.

**param output\_dim** number of outputs driven by latent function.

```
type output_dim int
```

param W sensitivities of each output to the latent driving function.

**type W** ndarray (output\_dim x rank).

**param rank** If rank is greater than 1 then there are assumed to be a total of rank latent forces independently driving the system, each with identical covariance.

type rank int

param decay decay rates for the first order system.

type decay array of length output\_dim.

param delay delay between latent force and output response.

type delay array of length output\_dim.

**param kappa** diagonal term that allows each latent output to have an independent component to the response.

type kappa array of length output\_dim.

**K** (*X*, *X*2, *target*)

Kdiag (index, target)

 $dK_dX$  ( $dL_dK$ , X, X2, target)

 $dK_dtheta(dL_dK, X, X2, target)$ 

dKdiag\_dtheta (dL\_dKdiag, index, target)

# GPy.kern.parts.exponential module

class GPy.kern.parts.exponential.Exponential( $input\_dim$ , variance=1.0, lengthscale=None, ARD=False)

Bases: GPy.kern.parts.kernpart.Kernpart

Exponential kernel (aka Ornstein-Uhlenbeck or Matern 1/2)

$$k(r) = \sigma^2 \exp(-r)$$
 where  $r = \sqrt{\sum_{i=1}^{i} nput_d im \frac{(x_i - y_i)^2}{\ell_i^2}}$ 

#### **Parameters**

- **input\_dim** (*int*) the number of input dimensions
- variance (float) the variance  $\sigma^2$
- lengthscale (array or list of the appropriate size (or float if there is only one lengthscale parameter)) the vector of lengthscale  $\ell_i$
- **ARD** (*Boolean*) Auto Relevance Determination. If equal to "False", the kernel is isotropic (ie. one single lengthscale parameter ell), otherwise there is one lengthscale parameter per dimension.

Return type kernel object

 $Gram_matrix(F, F1, lower, upper)$ 

Return the Gram matrix of the vector of functions F with respect to the RKHS norm. The use of this function is limited to input\_dim=1.

#### **Parameters**

- **F** (*np.array*) vector of functions
- **F1** (*np.array*) vector of derivatives of F
- lower,upper (floats) boundaries of the input domain

 $\mathbf{K}(X, X2, target)$ 

Compute the covariance matrix between X and X2.

Kdiag(X, target)

Compute the diagonal of the covariance matrix associated to X.

```
dK_dX (dL_dK, X, X2, target)
```

derivative of the covariance matrix with respect to X.

## $dK_dtheta(dL_dK, X, X2, target)$

derivative of the covariance matrix with respect to the parameters.

dKdiag\_dX (dL\_dKdiag, X, target)

dKdiag\_dtheta(dL\_dKdiag, X, target)

derivative of the diagonal of the covariance matrix with respect to the parameters.

### GPy.kern.parts.finite dimensional module

```
class GPy.kern.parts.finite_dimensional.FiniteDimensional(input\_dim, F, G, variance=1.0, weights=None)
```

Bases: GPy.kern.parts.kernpart.Kernpart

**K** (*X*, *X*2, target)

Kdiag (X, target)

dK dtheta(X, X2, target)

Return shape is NxMx(Ntheta)

dKdiag\_dtheta(X, target)

# **GPy.kern.parts.fixed module**

class GPy.kern.parts.fixed.Fixed(input\_dim, K, variance=1.0)

Bases: GPy.kern.parts.kernpart.Kernpart

**K** (*X*, *X*2, target)

**dK\_dX** (partial, X, X2, target)

dK\_dtheta (partial, X, X2, target)

dKdiag\_dX (partial, X, target)

### GPy.kern.parts.gibbs module

class GPy.kern.parts.gibbs.Gibbs (input\_dim, variance=1.0, mapping=None, ARD=False)

Bases: GPy.kern.parts.kernpart.Kernpart

Gibbs non-stationary covariance function.

$$r = sqrt((x_i - x_j)' * (x_i - x_j))$$

$$k(x_i, x_j) = \sigma^2 * Z * exp(-r^2/(l(x) * l(x) + l(x') * l(x')))$$

$$Z = (2 * l(x) * l(x')/(l(x) * l(x) + l(x') * l(x')^{q/2})$$

 $where: math: `l(x)` is a function giving the length scale as a function of space and: math: `q` is the dimensionality of the input the parameters are: math: `\sigma^2`, the process variance, and the parameters of l(x) which is a function that can be specified by <math display="block">: paraminput_dim: the number of input dimensions: type input_dim: int: paramvariance: the variance: math: `\sigma^2`: type input_dim: for length scale as a function of space and: math: `q` is the dimensionality of the input_dimensionality of the inpu$ 

See Mark Gibbs's thesis for more details: Gibbs, M. N. (1997). Bayesian Gaussian Processes for Regression and Classification. PhD thesis, Department of Physics, University of Cambridge. Or also see Page 93 of Gaussian Processes for Machine Learning by Rasmussen and Williams. Although note that we do not constrain the lengthscale to be positive by default. This allows anticorrelation to occur. The positive constraint can be included by the user manually.

**K** (*X*, *X*2, target)

Return covariance between X and X2.

Kdiag(X, target)

Compute the diagonal of the covariance matrix for X.

 $dK_dX (dL_dK, X, X2, target)$ 

Derivative of the covariance matrix with respect to X.

dK dtheta (dL dK, X, X2, target)

Derivative of the covariance with respect to the parameters.

dKdiag\_dX (dL\_dKdiag, X, target)

Gradient of diagonal of covariance with respect to X.

dKdiag\_dtheta(dL\_dKdiag, X, target)

Gradient of diagonal of covariance with respect to parameters.

## GPy.kern.parts.hetero module

class GPy.kern.parts.hetero.Hetero(input\_dim, mapping=None, transform=None)

Bases: GPy.kern.parts.kernpart.Kernpart

TODO: Need to constrain the function outputs positive (still thinking of best way of doing this!!! Yes, intend to use transformations, but what's the *best* way). Currently just squaring output.

Heteroschedastic noise which depends on input location. See, for example, this paper by Goldberg et al.

$$k(x_i, x_j) = \delta_{i,j} \sigma^2(x_i)$$

 $where: math: `\sigma^2(x)` is a function giving the variance as a function of input space and: math: `\delta_{i,j}` is the Kronecker delta function of the partial properties of the p$ 

The parameters are the parameters of sigma $^2(x)$  which is a function that can be specified by the user, by default an multi-layer peceptron is used.

#### **Parameters**

- **input\_dim** (*int*) the number of input dimensions
- **mapping** (*GPy.core.Mapping*) the mapping that gives the lengthscale across the input space (by default GPy.mappings.MLP is used with 20 hidden nodes).

Return type Kernpart object

See this paper:

Goldberg, P. W. Williams, C. K. I. and Bishop, C. M. (1998) Regression with Input-dependent Noise: a Gaussian Process Treatment In Advances in Neural Information Processing Systems, Volume 10, pp. 493-499. MIT Press

for a Gaussian process treatment of this problem.

**K** (*X*, *X*2, target)

Return covariance between X and X2.

Kdiag(X, target)

Compute the diagonal of the covariance matrix for X.

 $dK_dX$  ( $dL_dK$ , X, X2, target)

Derivative of the covariance matrix with respect to X.

 $dK_dtheta(dL_dK, X, X2, target)$ 

Derivative of the covariance with respect to the parameters.

 $dKdiag_dX (dL_dKdiag, X, target)$ 

Gradient of diagonal of covariance with respect to X.

dKdiag\_dtheta(dL\_dKdiag, X, target)

Gradient of diagonal of covariance with respect to parameters.

## GPy.kern.parts.hierarchical module

```
class GPy.kern.parts.hierarchical.Hierarchical(parts)
Bases: GPy.kern.parts.kernpart.Kernpart
A kernel part which can reopresent a hierarchy of independence: a generalisation of independent_outputs
K(X, X2, target)
Kdiag(X, target)
dK_dX(dL_dK, X, X2, target)
dK_dtheta(dL_dK, X, X2, target)
dKdiag_dX(dL_dKdiag, X, target)
dKdiag_dtheta(dL_dKdiag, X, target)
```

### **GPy.kern.parts.independent\_outputs module**

A kernel part shich can reopresent several independent functions. this kernel 'switches off' parts of the matrix where the output indexes are different.

The index of the functions is given by the last column in the input X the rest of the columns of X are passed to the kernel for computation (in blocks).

```
K(X, X2, target)
Kdiag(X, target)
dK_dX(dL_dK, X, X2, target)
dK_dtheta(dL_dK, X, X2, target)
dKdiag_dX(dL_dKdiag, X, target)
dKdiag_dtheta(dL_dKdiag, X, target)
GPy.kern.parts.independent outputs.index to slices(index)
```

[[slice(0,2,None),slice(4,5,None)],[slice(2,4,None),slice(8,10,None)],[slice(5,8,None)]]

take a numpy array of integers (index) and return a nested list of slices such that the slices describe the start,

```
stop points for each integer in the index.

e.g. >>> index = np.asarray([0,0,0,1,1,1,2,2,2]) returns >>> [[slice(0,3,None)],[slice(3,6,None)],[slice(6,9,None)]]

or, a more complicated example >>> index = np.asarray([0,0,1,1,0,2,2,2,1,1]) returns >>>
```

### GPy.kern.parts.kernpart module

```
class GPy.kern.parts.kernpart.Kernpart (input_dim)
    Bases: object
    K(X, X2, target)
    Kdiag(X, target)
    dK_dX(dL_dK, X, X2, target)
    dK_dtheta(dL_dK, X, X2, target)
    dKdiag_dX(dL_dK, X, target)
    dKdiag_dtheta(dL_dKdiag, X, target)
    dpsi0_dmuS(dL_dpsi0, Z, mu, S, target_mu, target_S)
```

```
dpsi0_dtheta(dL_dpsi0, Z, mu, S, target)
     dpsi1_dz (dL_dpsi1, Z, mu, S, target)
     dpsi1_dmuS (dL_dpsi1, Z, mu, S, target_mu, target_S)
     dpsi1_dtheta(Z, mu, S, target)
     dpsi2 dZ (dL dpsi2, Z, mu, S, target)
     dpsi2 dmuS (dL dpsi2, Z, mu, S, target mu, target S)
     dpsi2_dtheta (dL_dpsi2, Z, mu, S, target)
     psi0(Z, mu, S, target)
     psil(Z, mu, S, target)
     psi2(Z, mu, S, target)
class GPy.kern.parts.kernpart.Kernpart_inner(input_dim)
     Bases: GPy.kern.parts.kernpart.Kernpart
class GPy.kern.parts.kernpart.Kernpart_stationary(input_dim,
                                                                             lengthscale=None,
                                                            ARD=False)
     Bases: GPy.kern.parts.kernpart.Kernpart
     dKdiag_dX (dL_dK, X, target)
     dKdiag_dtheta(dL_dKdiag, X, target)
```

## GPy.kern.parts.linear module

class GPy.kern.parts.linear.Linear(input\_dim, variances=None, ARD=False)
 Bases: GPy.kern.parts.kernpart.Kernpart

Linear kernel

$$k(x,y) = \sum_{i=1}^{i} nput_d im \sigma_i^2 x_i y_i$$

### **Parameters**

- **input\_dim** (*int*) the number of input dimensions
- variances (array or list of the appropriate size (or float if there is only one variance parameter)) the vector of variances  $\sigma_i^2$
- **ARD** (*Boolean*) Auto Relevance Determination. If equal to "False", the kernel has only one variance parameter sigma^2, otherwise there is one variance parameter per dimension.

#### **Return type** kernel object

```
K(X, X2, target)

Kdiag(X, target)

dK_dX(dL_dK, X, X2, target)

dK_dtheta(dL_dK, X, X2, target)

dKdiag_dX(dL_dKdiag, X, target)

dKdiag_dtheta(dL_dKdiag, X, target)

dpsi0_dmuS(dL_dpsi0, Z, mu, S, target_mu, target_S)

dpsi0_dtheta(dL_dpsi0, Z, mu, S, target)
```

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 $dpsi1_dz$  ( $dL_dpsi1, Z, mu, S, target$ )  $dpsi1\_dmuS$  ( $dL\_dpsi1$ , Z, mu, S,  $target\_mu$ ,  $target\_S$ ) Do nothing for S, it does not affect psi1 dpsi1\_dtheta (dL\_dpsi1, Z, mu, S, target) the variance, it does nothing dpsi2 dZ (dL dpsi2, Z, mu, S, target) dpsi2\_dmuS (dL\_dpsi2, Z, mu, S, target\_mu, target\_S) Think N,num\_inducing,num\_inducing,input\_dim  $dpsi2\_dmuS\_new(dL\_dpsi2, Z, mu, S, target\_mu, target\_S)$ dpsi2\_dtheta (dL\_dpsi2, Z, mu, S, target) dpsi2\_dtheta\_new (dL\_dpsi2, Z, mu, S, target) psi0(Z, mu, S, target)psil(Z, mu, S, target)the variance, it does nothing psi2(Z, mu, S, target) $psi2\_new(Z, mu, S, target)$ 

# GPy.kern.parts.mlp module

Multi layer perceptron kernel (also known as arc sine kernel or neural network kernel)

$$k(x,y) = \sigma^2 \frac{2}{\pi} a \sin \left( \frac{\sigma_w^2 x^{\mathsf{T}} y + \sigma_b^2}{\sqrt{\sigma_w^2 x^{\mathsf{T}} x + \sigma_b^2 + 1} \sqrt{\sigma_w^2 y^{\mathsf{T}} y \sigma_b^2 + 1}} \right)$$

### **Parameters**

- **input\_dim** (*int*) the number of input dimensions
- variance (float) the variance  $\sigma^2$
- weight\_variance (array or list of the appropriate size (or float if there is only one weight variance parameter)) the vector of the variances of the prior over input weights in the neural network  $\sigma_w^2$
- bias\_variance the variance of the prior over bias parameters  $\sigma_b^2$
- **ARD** (*Boolean*) Auto Relevance Determination. If equal to "False", the kernel is isotropic (ie. one weight variance parameter sigma^2\_w), otherwise there is one weight variance parameter per dimension.

### Return type Kernpart object

**K** (*X*, *X*2, target)

Return covariance between X and X2.

**Kdiag** (X, target)

Compute the diagonal of the covariance matrix for X.

 $dK_dX (dL_dK, X, X2, target)$ 

Derivative of the covariance matrix with respect to X

```
dK dtheta (dL dK, X, X2, target)
```

Derivative of the covariance with respect to the parameters.

```
dKdiag_dX (dL_dKdiag, X, target)
```

Gradient of diagonal of covariance with respect to X

### GPy.kern.parts.periodic\_Matern32 module

Bases: GPy.kern.parts.kernpart.Kernpart

Kernel of the periodic subspace (up to a given frequency) of a Matern 3/2 RKHS. Only defined for input\_dim=1.

#### **Parameters**

- **input\_dim** (*int*) the number of input dimensions
- variance (float) the variance of the Matern kernel
- **lengthscale** (*np.ndarray of size* (*input\_dim*,)) the lengthscale of the Matern kernel
- **period** (*float*) the period
- **n\_freq** (*int*) the number of frequencies considered for the periodic subspace

### Return type kernel object

```
Gram_matrix()
```

**K** (*X*, *X*2, *target*)

Compute the covariance matrix between X and X2.

# Kdiag(X, target)

Compute the diagonal of the covariance matrix associated to X.

```
dK dtheta(*args, **kwds)
```

derivative of the covariance matrix with respect to the parameters (shape is num\_data x num\_inducing x num\_params)

```
dKdiag_dtheta(*args, **kwds)
```

derivative of the diagonal covariance matrix with respect to the parameters

## GPy.kern.parts.periodic Matern52 module

Bases: GPy.kern.parts.kernpart.Kernpart

Kernel of the periodic subspace (up to a given frequency) of a Matern 5/2 RKHS. Only defined for input\_dim=1.

- **input\_dim** (*int*) the number of input dimensions
- variance (*float*) the variance of the Matern kernel
- **lengthscale** (*np.ndarray of size* (*input\_dim*,)) the lengthscale of the Matern kernel

- **period** (*float*) the period
- **n\_freq** (*int*) the number of frequencies considered for the periodic subspace

# Return type kernel object

```
Gram_matrix()
```

 $\mathbf{K}(X, X2, target)$ 

Compute the covariance matrix between X and X2.

### Kdiag(X, target)

Compute the diagonal of the covariance matrix associated to X.

```
dK_dtheta(*args, **kwds)
```

derivative of the covariance matrix with respect to the parameters (shape is num\_data x num\_inducing x num\_params)

```
dKdiag_dtheta(*args, **kwds)
```

derivative of the diagonal of the covariance matrix with respect to the parameters

# GPy.kern.parts.periodic\_exponential module

```
class GPy.kern.parts.periodic_exponential.PeriodicExponential (input_dim=1, variance=1.0, length-scale=None, period=6.283185307179586, n_freq=10, lower=0.0, up-per=12.566370614359172)
```

Bases: GPy.kern.parts.kernpart.Kernpart

Kernel of the periodic subspace (up to a given frequency) of a exponential (Matern 1/2) RKHS. Only defined for input\_dim=1.

#### **Parameters**

- **input\_dim** (*int*) the number of input dimensions
- variance (float) the variance of the Matern kernel
- **lengthscale** (*np.ndarray of size* (*input\_dim*,)) the lengthscale of the Matern kernel
- **period** (*float*) the period
- **n\_freq** (*int*) the number of frequencies considered for the periodic subspace

### Return type kernel object

```
Gram_matrix()
```

```
K (X, X2, target)
```

Compute the covariance matrix between X and X2.

# Kdiag(X, target)

Compute the diagonal of the covariance matrix associated to X.

```
dK_dtheta(*args, **kwds)
```

derivative of the covariance matrix with respect to the parameters (shape is  $N \times num_i$  num\_params)

```
dKdiag_dtheta(*args, **kwds)
```

derivative of the diagonal of the covariance matrix with respect to the parameters

#### GPy.kern.parts.poly module

Polynomial kernel parameter initialisation. Included for completeness, but generally not recommended, is the polynomial kernel:

$$k(x,y) = \sigma^2(\sigma_w^2 x' y + \sigma_b^b)^d$$

The kernel parameters are  $\sigma^2$  (variance),  $\sigma^2_w$  (weight\_variance),  $\sigma^2_b$  (bias\_variance) and d (degree). Only gradients of the first three are provided for kernel optimisation, it is assumed that polynomial degree would be set by hand.

The kernel is not recommended as it is badly behaved when the  $\sigma_w^2 x'y + \sigma_b^2$  has a magnitude greater than one. For completeness there is an automatic relevance determination version of this kernel provided (NOTE YET IMPLEMENTED!). :param input\_dim: the number of input dimensions :type input\_dim: int :param variance: the variance  $\sigma^2$  :type variance: float :param weight\_variance: the vector of the variances of the prior over input weights in the neural network  $\sigma_w^2$  :type weight\_variance: array or list of the appropriate size (or float if there is only one weight variance parameter) :param bias\_variance: the variance of the prior over bias parameters  $\sigma_b^2$  :param degree: the degree of the polynomial. :type degree: int :param ARD: Auto Relevance Determination. If equal to "False", the kernel is isotropic (ie. one weight variance parameter  $\sigma_w^2$ ), otherwise there is one weight variance parameter per dimension. :type ARD: Boolean :rtype: Kernpart object

**K** (*X*, *X*2, target)

Return covariance between X and X2.

Kdiag(X, target)

Compute the diagonal of the covariance matrix for X.

 $dK_dX$  ( $dL_dK$ , X, X2, target)

Derivative of the covariance matrix with respect to X

 $dK_dtheta(dL_dK, X, X2, target)$ 

Derivative of the covariance with respect to the parameters.

 $dKdiag_dX (dL_dKdiag, X, target)$ 

Gradient of diagonal of covariance with respect to X

# GPy.kern.parts.prod module

class GPy.kern.parts.prod.Prod(k1, k2, tensor=False)
Bases: GPy.kern.parts.kernpart.Kernpart

Computes the product of 2 kernels

## **Parameters**

- $\mathbf{k2}$  (k1,) the kernels to multiply
- **tensor** (*Boolean*) The kernels are either multiply as functions defined on the same input space (default) or on the product of the input spaces

Return type kernel object

**K** (*X*, *X*2, target)

**K1** (X, X2)

Compute the part of the kernel associated with k1.

K2(X, X2)

Compute the part of the kernel associated with k2.

**Kdiag** (*X*, target)

Compute the diagonal of the covariance matrix associated to X.

 $dK_dX (dL_dK, X, X2, target)$ 

derivative of the covariance matrix with respect to X.

 $dK_dtheta(dL_dK, X, X2, target)$ 

Derivative of the covariance matrix with respect to the parameters.

 $dKdiag_dX (dL_dKdiag, X, target)$ 

dKdiag\_dtheta(dL\_dKdiag, X, target)

## GPy.kern.parts.prod\_orthogonal module

class GPy.kern.parts.prod\_orthogonal.prod\_orthogonal(k1, k2)

Bases: GPy.kern.parts.kernpart.Kernpart

Computes the product of 2 kernels

**Parameters k2** (kl) – the kernels to multiply

Return type kernel object

**K** (*X*, *X*2, *target*)

Kdiag(X, target)

Compute the diagonal of the covariance matrix associated to X.

 $dK_dX (dL_dK, X, X2, target)$ 

derivative of the covariance matrix with respect to X.

 $dK_dtheta(dL_dK, X, X2, target)$ 

derivative of the covariance matrix with respect to the parameters.

dKdiag\_dX (dL\_dKdiag, X, target)

dKdiag\_dtheta(dL\_dKdiag, X, target)

### GPy.kern.parts.rational\_quadratic module

 $\begin{array}{ll} \textbf{class} \ \texttt{GPy.kern.parts.rational\_quadratic.RationalQuadratic} \ (\textit{input\_dim}, & \textit{variance=1.0}, \textit{lengthscale=1.0}, \\ & \textit{power=1.0}) \end{array}$ 

Bases: GPy.kern.parts.kernpart.Kernpart

rational quadratic kernel

$$k(r) = \sigma^2 \left(1 + \frac{r^2}{2\ell^2}\right)^{-\alpha}$$
 where  $r^2 = (x - y)^2$ 

#### **Parameters**

- **input\_dim** (*int* (*input\_dim=1 is the only value currently supported*)) the number of input dimensions
- variance (*float*) the variance  $\sigma^2$
- lengthscale (float) the lengthscale  $\ell$
- **power** (*float*) the power  $\alpha$

Return type Kernpart object

**K** (*X*, *X*2, target)

### GPy.kern.parts.rbf module

class GPy.kern.parts.rbf.RBF (input\_dim, variance=1.0, lengthscale=None, ARD=False)
 Bases: GPy.kern.parts.kernpart.Kernpart

Radial Basis Function kernel, aka squared-exponential, exponentiated quadratic or Gaussian kernel:

$$k(r) = \sigma^2 \exp\left(-\frac{1}{2}r^2\right)$$
 where  $r^2 = \sum_{i=1}^d \frac{(x_i - x_i')^2}{\ell_i^2}$ 

where ell\_i is the lengthscale, sigma^2 the variance and d the dimensionality of the input.

#### **Parameters**

- **input\_dim** (*int*) the number of input dimensions
- variance (float) the variance of the kernel
- **lengthscale** (array or list of the appropriate size (or float if there is only one lengthscale parameter)) the vector of lengthscale of the kernel
- **ARD** (*Boolean*) Auto Relevance Determination. If equal to "False", the kernel is isotropic (ie. one single lengthscale parameter ell), otherwise there is one lengthscale parameter per dimension.

### Return type kernel object

```
K (X, X2, target)
Kdiag(X, target)
dK dX (dL dK, X, X2, target)
dK_dtheta(dL_dK, X, X2, target)
dKdiag_dX (dL_dKdiag, X, target)
dKdiag_dtheta(dL_dKdiag, X, target)
dpsi0\_dmuS (dL\_dpsi0, Z, mu, S, target\_mu, target\_S)
dpsi0_dtheta(dL_dpsi0, Z, mu, S, target)
dpsi1_dz (dL_dpsi1, Z, mu, S, target)
dpsi1\_dmuS (dL\_dpsi1, Z, mu, S, target\_mu, target\_S)
dpsi1_dtheta (dL_dpsi1, Z, mu, S, target)
dpsi2_dz (dL_dpsi2, Z, mu, S, target)
dpsi2_dmuS (dL_dpsi2, Z, mu, S, target_mu, target_S)
    Think N,num_inducing,num_inducing,input_dim
dpsi2_dtheta (dL_dpsi2, Z, mu, S, target)
     Shape N,num_inducing,num_inducing,Ntheta
```

```
psi0 (Z, mu, S, target)
psi1 (Z, mu, S, target)
psi2 (Z, mu, S, target)
weave_psi2 (mu, Zhat)
```

# GPy.kern.parts.rbf\_inv module

Radial Basis Function kernel, aka squared-exponential, exponentiated quadratic or Gaussian kernel. It only differs from RBF in that here the parametrization is wrt the inverse lengthscale:

$$k(r) = \sigma^2 \exp\left(-\frac{1}{2}r^2\right)$$
 where  $r^2 = \sum_{i=1}^d \frac{(x_i - x_i')^2}{\ell_i^2}$ 

where ell\_i is the lengthscale, sigma^2 the variance and d the dimensionality of the input.

### **Parameters**

- input\_dim (int) the number of input dimensions
- variance (*float*) the variance of the kernel
- **lengthscale** (array or list of the appropriate size (or float if there is only one lengthscale parameter)) the vector of lengthscale of the kernel
- ARD (Boolean) Auto Relevance Determination. If equal to "False", the kernel is isotropic
  (ie. one single lengthscale parameter ell), otherwise there is one lengthscale parameter per
  dimension.

```
Return type kernel object
```

```
dK_dX (dL_dK, X, X2, target)

dK_dtheta (dL_dK, X, X2, target)

dKdiag_dX (dL_dKdiag, X, target)

dpsi1_dZ (dL_dpsi1, Z, mu, S, target)

dpsi1_dmuS (dL_dpsi1, Z, mu, S, target_mu, target_S)

dpsi1_dtheta (dL_dpsi1, Z, mu, S, target)

dpsi2_dZ (dL_dpsi2, Z, mu, S, target)

dpsi2_dmuS (dL_dpsi2, Z, mu, S, target_mu, target_S)

Think N,num_inducing,num_inducing,input_dim

dpsi2_dtheta (dL_dpsi2, Z, mu, S, target)

Shape N,num_inducing,num_inducing,Ntheta

weave_psi2 (mu, Zhat)
```

### GPy.kern.parts.rbfcos module

```
Kdiag(X, target)
     dK_dX (dL_dK, X, X2, target)
     dK_dtheta(dL_dK, X, X2, target)
     dKdiag_dX (dL_dKdiag, X, target)
     dKdiag_dtheta(dL_dKdiag, X, target)
GPy.kern.parts.spline module
class GPy.kern.parts.spline.Spline (input_dim, variance=1.0, lengthscale=1.0)
     Bases: GPy.kern.parts.kernpart.Kernpart
     Spline kernel
          Parameters
                • input_dim (int) – the number of input dimensions (fixed to 1 right now TODO)
                • variance (float) – the variance of the kernel
     K (X, X2, target)
     Kdiag(X, target)
     dK_dtheta (X, X2, target)
     dKdiag_dX(X, target)
     dKdiag_dtheta(X, target)
GPy.kern.parts.spline.theta(x)
     Heaviside step function
GPy.kern.parts.symmetric module
class GPy.kern.parts.symmetric.Symmetric(k, transform=None)
     Bases: GPy.kern.parts.kernpart.Kernpart
     Symmetrical kernels
          Parameters
                • k (Kernpart) – the kernel to symmetrify
                • transform (A numpy array (input_dim x input_dim) specifying the transform) – the trans-
                  form to use in symmetrification (allows symmetry on specified axes)
          Return type Kernpart
     K (X, X2, target)
          Compute the covariance matrix between X and X2.
     Kdiag(X, target)
          Compute the diagonal of the covariance matrix associated to X.
     dK_dX (dL_dK, X, X2, target)
          derivative of the covariance matrix with respect to X.
     dK_dtheta(dL_dK, X, X2, target)
          derivative of the covariance matrix with respect to the parameters.
     dKdiag_dX (dL_dKdiag, X, target)
     dKdiag_dtheta(dL_dKdiag, X, target)
          Compute the diagonal of the covariance matrix associated to X.
```

## GPy.kern.parts.sympy\_helpers module

```
GPy.kern.parts.sympy_helpers.erfcx(x)
GPy.kern.parts.sympy_helpers.h(t, tprime, d_i, d_j, t)
GPy.kern.parts.sympy_helpers.ln_diff_erf(x, y)
```

# GPy.kern.parts.sympykern module

```
 \begin{array}{ll} \textbf{class} \; \texttt{GPy.kern.parts.sympykern.spkern} \; (\textit{input\_dim}, & \textit{k=None}, & \textit{output\_dim=1}, & \textit{name=None}, \\ & \textit{param=None}) \\ & \textbf{Bases:} \; \texttt{GPy.kern.parts.kernpart.Kernpart} \end{array}
```

A kernel object, where all the hard work in done by sympy.

**Parameters k** (a positive definite sympy function of x\_0, z\_0, x\_1, z\_1, x\_2, z\_2...) – the covariance function

# To construct a new sympy kernel, you'll need to define:

- a kernel function using a sympy object. Ensure that the kernel is of the form k(x,z).
- that's it! we'll extract the variables from the function k.

#### Note:

- to handle multiple inputs, call them x\_1, z\_1, etc
- to handle multiple correlated outputs, you'll need to add parameters with an index, such as length-scale\_i and lengthscale\_j.

```
K (X, Z, target)
Kdiag (X, target)
compute_psi_stats()
dK_dX (partial, X, Z, target)
dK_dtheta (partial, X, Z, target)
dKdiag_dX (partial, X, target)
dKdiag_dtheta (partial, X, target)
```

### GPy.kern.parts.white module

```
class GPy.kern.parts.white.White(input_dim, variance=1.0)
    Bases: GPy.kern.parts.kernpart.Kernpart
```

White noise kernel.

#### **Parameters**

- **input\_dim** (*int*) the number of input dimensions
- variance (float) -

```
K (X, X2, target)
Kdiag (X, target)
dK_dX (dL_dK, X, X2, target)
dK_dtheta (dL_dK, X, X2, target)
dKdiag_dX (dL_dKdiag, X, target)
```

```
dRdiag_dtheta (dL_dKdiag, X, target)
dpsi0_dmuS (dL_dpsi0, Z, mu, S, target_mu, target_S)
dpsi0_dtheta (dL_dpsi0, Z, mu, S, target)
dpsi1_dZ (dL_dpsi1, Z, mu, S, target)
dpsi1_dmuS (dL_dpsi1, Z, mu, S, target_mu, target_S)
dpsi1_dtheta (dL_dpsi1, Z, mu, S, target)
dpsi2_dZ (dL_dpsi2, Z, mu, S, target)
dpsi2_dmuS (dL_dpsi2, Z, mu, S, target_mu, target_S)
dpsi2_dtheta (dL_dpsi2, Z, mu, S, target_mu, target_S)
dpsi2_dtheta (dL_dpsi2, Z, mu, S, target)
psi0 (Z, mu, S, target)
psi1 (Z, mu, S, target)
psi2 (Z, mu, S, target)
```

#### Module contents

### **Submodules**

# GPy.kern.constructors module

GPy.kern.constructors.**Brownian** (input\_dim, variance=1.0)
Construct a Brownian motion kernel.

# **Parameters**

- **input\_dim** (*int*) Dimensionality of the kernel
- variance (float) the variance of the kernel

GPy.kern.constructors.Matern32 (input\_dim, variance=1.0, lengthscale=None, ARD=False)

Construct a Matern 3/2 kernel.

### Parameters

- input\_dim (int) dimensionality of the kernel, obligatory
- variance (float) the variance of the kernel
- lengthscale (float) the lengthscale of the kernel
- ARD (Boolean) Auto Relevance Determination (one lengthscale per dimension)

GPy.kern.constructors.Matern52 (input\_dim, variance=1.0, lengthscale=None, ARD=False)

Construct a Matern 5/2 kernel.

- **input\_dim** (*int*) dimensionality of the kernel, obligatory
- variance (float) the variance of the kernel
- lengthscale (float) the lengthscale of the kernel

• ARD (Boolean) – Auto Relevance Determination (one lengthscale per dimension)

GPy.kern.constructors.**ODE\_1** (input\_dim=1, varianceU=1.0, varianceY=1.0, lengthscaleU=None, lengthscaleY=None)

kernel resultiong from a first order ODE with OU driving GP

#### **Parameters**

- input\_dim (int) the number of input dimension, has to be equal to one
- variance U (float) variance of the driving GP
- lengthscaleU (float) lengthscale of the driving GP
- varianceY (float) 'variance' of the transfer function
- lengthscaleY (float) 'lengthscale' of the transfer function

Return type kernel object

GPy.kern.constructors.**ODE\_UY** (input\_dim=2, varianceU=1.0, varianceY=1.0, lengthscaleU=None, lengthscaleY=None)

kernel resultiong from a first order ODE with OU driving GP:param input\_dim: the number of input dimension, has to be equal to one :type input\_dim: int :param input\_lengthU: the number of input U length :param varianceU: variance of the driving GP:type varianceU: float :param varianceY: 'variance' of the transfer function :type varianceY: float :param lengthscaleY: 'lengthscale' of the transfer function :type lengthscaleY: float :rtype: kernel object

GPy.kern.constructors.bias(input\_dim, variance=1.0)

Construct a bias kernel.

#### **Parameters**

- **input dim** (*int*) dimensionality of the kernel, obligatory
- variance (float) the variance of the kernel

GPy.kern.constructors.build\_lcm(input\_dim, output\_dim, kernel\_list=[], rank=1, W=None, kappa=None)

Builds a kernel of a linear coregionalization model

**Input\_dim** Input dimensionality

Output\_dim Number of outputs

**Kernel\_list** List of coregionalized kernels, each element in the list will be multiplied by a different corregionalization matrix

**Parameters rank** (*integer*) – number tuples of the corregionalization parameters 'coregion\_W' ...note the kernels dimensionality is overwritten to fit input dim

GPy.kern.constructors.coregionalize (output\_dim, rank=1, W=None, kappa=None)
Coregionlization matrix B, of the form:

$$\mathbf{B} = \mathbf{W}\mathbf{W}^{o}p + kappa\mathbf{I}$$

An intrinsic/linear coregionalization kernel of the form:

$$k_2(x,y) = \mathbf{B}k(x,y)$$

it is obtained as the tensor product between a kernel k(x,y) and B.

#### **Parameters**

- output\_dim (int) the number of outputs to corregionalize
- rank (int) number of columns of the W matrix (this parameter is ignored if parameter W is not None)
- W (numpy array of dimensionality (num\_outpus, rank)) a low rank matrix that determines the correlations between the different outputs, together with kappa it forms the coregionalization matrix B
- **kappa** (*numpy array of dimensionality (output\_dim*,)) a vector which allows the outputs to behave independently

# Return type kernel object

GPy.kern.constructors.eq\_sympy(input\_dim, output\_dim, ARD=False)

Latent force model covariance, exponentiated quadratic with multiple outputs. Derived from a diffusion equation with the initial spatial condition layed down by a Gaussian process with lengthscale given by shared\_lengthscale.

See IEEE Trans Pattern Anal Mach Intell. 2013 Nov;35(11):2693-705. doi: 10.1109/TPAMI.2013.86. Linear latent force models using Gaussian processes. Alvarez MA, Luengo D, Lawrence ND.

#### **Parameters**

- **input\_dim** (*int*) Dimensionality of the kernel
- **output\_dim** (*int*) number of outputs in the covariance function.
- ARD (bool) whether or not to user ARD (default False).

GPy.kern.constructors.**exponential** (input\_dim, variance=1.0, lengthscale=None, ARD=False) Construct an exponential kernel

#### **Parameters**

- input\_dim (int) dimensionality of the kernel, obligatory
- variance (float) the variance of the kernel
- lengthscale (float) the lengthscale of the kernel
- ARD (Boolean) Auto Relevance Determination (one lengthscale per dimension)
- GPy.kern.constructors.finite\_dimensional(input\_dim, F, G, variances=1.0, weights=None)
  Construct a finite dimensional kernel.

#### **Parameters**

- **input\_dim** (*int*) the number of input dimensions
- $\mathbf{F}(np.array)$  np.array of functions with shape (n,) the n basis functions
- G(np.array) np.array with shape (n,n) the Gram matrix associated to F
- variances np.ndarray with shape (n,)

# Type np.ndarray

GPy.kern.constructors.fixed(input\_dim, K, variance=1.0)

Construct a Fixed effect kernel.

- **input\_dim** (*int* (*input\_dim=1 is the only value currently supported*)) the number of input dimensions
- **K** (np.array) the variance  $\sigma^2$

• variance (float) – kernel variance

## Return type kern object

GPy.kern.constructors.gibbs(input\_dim, variance=1.0, mapping=None) Gibbs and MacKay non-stationary covariance function.

$$r = \sqrt{((x_i - x_j)' * (x_i - x_j))}$$

$$k(x_i, x_j) = \sigma^2 * Z * exp(-r^2/(l(x) * l(x) + l(x') * l(x')))$$

$$Z = \sqrt{2 * l(x) * l(x')/(l(x) * l(x) + l(x') * l(x')}$$

Where l(x) is a function giving the length scale as a function of space.

This is the non stationary kernel proposed by Mark Gibbs in his 1997 thesis. It is similar to an RBF but has a length scale that varies with input location. This leads to an additional term in front of the kernel.

The parameters are  $\sigma^2$ , the process variance, and the parameters of l(x) which is a function that can be specified by the user, by default an multi-layer peceptron is used is used.

#### **Parameters**

- **input\_dim** (*int*) the number of input dimensions
- variance (float) the variance  $\sigma^2$
- **mapping** (*GPy.core.Mapping*) the mapping that gives the lengthscale across the input space.
- ARD (Boolean) Auto Relevance Determination. If equal to "False", the kernel is isotropic (ie. one weight variance parameter  $\sigma_w^2$ ), otherwise there is one weight variance parameter per dimension.

## Return type Kernpart object

GPy.kern.constructors.hetero(input\_dim, mapping=None, transform=None)

GPy.kern.constructors.hierarchical(k)

TODO This can't be right! Construct a kernel with independent outputs from an existing kernel

GPy.kern.constructors.independent\_outputs(k)

Construct a kernel with independent outputs from an existing kernel

GPy.kern.constructors.linear(input\_dim, variances=None, ARD=False)

Construct a linear kernel.

#### **Parameters**

- **input\_dim** (*int*) dimensionality of the kernel, obligatory
- variances (np.ndarray) –
- ARD (Boolean) Auto Relevance Determination (one lengthscale per dimension)

GPy.kern.constructors.mlp(input\_dim, variance=1.0, weight\_variance=None, bias\_variance=100.0, ARD=False)

Construct an MLP kernel

### **Parameters**

- **input\_dim** (*int*) dimensionality of the kernel, obligatory
- variance (float) the variance of the kernel

- weight\_scale (vector of weight variances for input weights in neural network (length 1 if kernel is isotropic)) the lengthscale of the kernel
- bias\_variance (*float*) the variance of the biases in the neural network.
- ARD (Boolean) Auto Relevance Determination (allows for ARD version of covariance)
- GPy.kern.constructors.ode1\_eq(output\_dim=1)

Latent force model covariance, first order differential equation driven by exponentiated quadratic.

See N. D. Lawrence, G. Sanguinetti and M. Rattray. (2007) 'Modelling transcriptional regulation using Gaussian processes' in B. Schoelkopf, J. C. Platt and T. Hofmann (eds) Advances in Neural Information Processing Systems, MIT Press, Cambridge, MA, pp 785–792.

**Parameters output\_dim** (*int*) – number of outputs in the covariance function.

GPy.kern.constructors.**periodic\_Matern32** (input\_dim, variance=1.0, lengthscale=None, period=6.283185307179586, n\_freq=10, lower=0.0, upper=12.566370614359172)

Construct a periodic Matern 3/2 kernel.

#### **Parameters**

- **input\_dim** (*int*) dimensionality, only defined for input\_dim=1
- variance (float) the variance of the kernel
- lengthscale (float) the lengthscale of the kernel
- **period** (*float*) the period
- **n\_freq** (*int*) the number of frequencies considered for the periodic subspace

GPy.kern.constructors.**periodic\_Matern52** (input\_dim, variance=1.0, lengthscale=None, period=6.283185307179586, n\_freq=10, lower=0.0, upper=12.566370614359172)

Construct a periodic Matern 5/2 kernel.

## **Parameters**

- input\_dim (int) dimensionality, only defined for input\_dim=1
- variance (float) the variance of the kernel
- lengthscale (float) the lengthscale of the kernel
- **period** (*float*) the period
- **n\_freq** (*int*) the number of frequencies considered for the periodic subspace

```
GPy.kern.constructors.periodic_exponential(input_dim=1, variance=1.0, length-scale=None, period=6.283185307179586, n\_freq=10, lower=0.0, up-per=12.566370614359172)
```

Construct an periodic exponential kernel

- input dim (int) dimensionality, only defined for input dim=1
- variance (*float*) the variance of the kernel
- lengthscale (float) the lengthscale of the kernel
- **period** (*float*) the period
- n\_freq (int) the number of frequencies considered for the periodic subspace

GPy.kern.constructors.poly(input\_dim, variance=1.0, weight\_variance=None, bias\_variance=1.0, degree=2, ARD=False)

Construct a polynomial kernel

#### **Parameters**

- **input\_dim** (*int*) dimensionality of the kernel, obligatory
- variance (float) the variance of the kernel
- weight\_scale (vector of weight variances for input weights.) the lengthscale of the kernel
- bias\_variance (*float*) the variance of the biases.
- degree (int) the degree of the polynomial
- ARD (Boolean) Auto Relevance Determination (allows for ARD version of covariance)

GPy.kern.constructors.**prod**(*k1*, *k2*, *tensor=False*)

Construct a product kernel over input\_dim from two kernels over input\_dim

#### **Parameters**

- $\mathbf{k2}$  (k1,) the kernels to multiply
- **tensor** (*Boolean*) The kernels are either multiply as functions defined on the same input space (default) or on the product of the input spaces

### Return type kernel object

GPy.kern.constructors.rational\_quadratic(input\_dim, variance=1.0, lengthscale=1.0, power=1.0)

Construct rational quadratic kernel.

### **Parameters**

- **input\_dim** (*int* (*input\_dim=1 is the only value currently supported*)) the number of input dimensions
- variance (float) the variance  $\sigma^2$
- **lengthscale** (*float*) the lengthscale  $\ell$

# Return type kern object

GPy.kern.constructors.**rbf** (input\_dim, variance=1.0, lengthscale=None, ARD=False)
Construct an RBF kernel

#### **Parameters**

- input\_dim (int) dimensionality of the kernel, obligatory
- variance (*float*) the variance of the kernel
- **lengthscale** (*float*) the lengthscale of the kernel
- **ARD** (*Boolean*) Auto Relevance Determination (one lengthscale per dimension)

GPy.kern.constructors.rbf\_inv(input\_dim, variance=1.0, inv\_lengthscale=None, ARD=False)
Construct an RBF kernel

### **Parameters**

• **input\_dim** (*int*) – dimensionality of the kernel, obligatory

- variance (float) the variance of the kernel
- lengthscale (float) the lengthscale of the kernel
- ARD (Boolean) Auto Relevance Determination (one lengthscale per dimension)
- GPy.kern.constructors.rbf\_sympy (input\_dim, ARD=False, variance=1.0, lengthscale=1.0) Radial Basis Function covariance.
- GPy.kern.constructors.rbfcos(input\_dim, variance=1.0, frequencies=None, bandwidths=None, ARD=False)

construct a rbfcos kernel

GPy.kern.constructors.**spline**(input\_dim, variance=1.0)
Construct a spline kernel.

#### **Parameters**

- input\_dim (int) Dimensionality of the kernel
- variance (float) the variance of the kernel
- GPy.kern.constructors.symmetric(k)

Construct a symmetric kernel from an existing kernel

The symmetric kernel works by adding two GP functions together, and computing the overall covariance.

Let 
$$f \sim GP(x \mid 0, k(x, x'))$$
. Now let  $g = f(x) + f(-x)$ .

It's easy to see that g is a symmetric function: g(x) = g(-x).

by construction, g, is a gaussian Process with mean 0 and covariance

$$k(x, x') + k(-x, x') + k(x, -x') + k(-x, -x')$$

This constructor builds a covariance function of this form from the initial kernel

GPy.kern.constructors.sympykern(input\_dim, k=None, output\_dim=1, name=None, param=None)

A base kernel object, where all the hard work in done by sympy.

**Parameters k** (a positive definite sympy function of x1, z1, x2, z2...) – the covariance function

### To construct a new sympy kernel, you'll need to define:

- a kernel function using a sympy object. Ensure that the kernel is of the form k(x,z).
- that's it! we'll extract the variables from the function k.

#### Note:

- to handle multiple inputs, call them x1, z1, etc
- to handle multiple correlated outputs, you'll need to define each covariance function and 'cross' variance function. TODO

GPy.kern.constructors.white(input\_dim, variance=1.0)

Construct a white kernel.

- input\_dim (int) dimensionality of the kernel, obligatory
- variance (float) the variance of the kernel

#### GPy.kern.kern module

This class allows gradient checks for the gradient of a kernel with respect to X.

```
class GPy.kern.kern_check_dK_dtheta (kernel=None, dL_dK=None, X=None, X2=None)
Bases: GPy.kern.kern.kern check model
```

This class allows gradient checks for the gradient of a kernel with respect to parameters.

```
class GPy.kern.kern_check_dKdiag_dX (kernel=None, dL_dK=None, X=None, X2=None)
Bases: GPy.kern.kern_check_model
```

This class allows gradient checks for the gradient of a kernel diagonal with respect to X.

```
log_likelihood()
```

```
class GPy.kern.kern_check_dKdiag_dtheta(kernel=None, dL_dK=None, X=None)
    Bases: GPy.kern.kern_kern_check_model
```

This class allows gradient checks of the gradient of the diagonal of a kernel with respect to the parameters.

```
log_likelihood()
```

```
class GPy.kern.kern.Kern_check_model (kernel=None, dL_dK=None, X=None, X2=None)
    Bases: GPy.core.model.Model
```

This is a dummy model class used as a base class for checking that the gradients of a given kernel are implemented correctly. It enables checkgradient() to be called independently on a kernel.

```
is_positive_definite()
log_likelihood()

class GPy.kern.kern.kern(input_dim, parts=[], input_slices=None)
Bases: GPy.core.parameterized.Parameterized

K(X, X2=None, which_parts='all')
```

Compute the kernel function.

### **Parameters**

- $\mathbf{X}$  the first set of inputs to the kernel
- X2 (optional) the second set of arguments to the kernel. If X2 is None, this is passed through to the 'part' object, which handles this as X2 == X.
- which\_parts a list of booleans detailing whether to include each of the part functions. By default, 'all' indicates [True]\*self.num\_parts

```
Kdiag (X, which parts='all')
```

Compute the diagonal of the covariance function for inputs X.

```
add (other, tensor=False)
```

Add another kernel to this one.

If Tensor is False, both kernels are defined on the same \_space\_. then the created kernel will have the same number of inputs as self and other (which must be the same).

If Tensor is True, then the dimensions are stacked 'horizontally', so that the resulting kernel has self.input\_dim + other.input\_dim

**Parameters other** (*GPy.kern*) – the other kernel to be added

```
compute param slices()
```

Create a set of slices that can index the parameters of each part.

```
dK_dX (dL_dK, X, X2=None)
```

Compute the gradient of the objective function with respect to X.

#### **Parameters**

- **dL\_dK** (*np.ndarray* (*num\_samples x num\_inducing*)) An array of gradients of the objective function with respect to the covariance function.
- **X** (np.ndarray (num\_samples x input\_dim)) Observed data inputs
- **X2** (*np.ndarray* (*num\_inducing x input\_dim*)) Observed data inputs (optional, defaults to X)

```
dK_dtheta(dL_dK, X, X2=None)
```

Compute the gradient of the covariance function with respect to the parameters.

#### **Parameters**

- **dL\_dK** (*Np.ndarray* (*num\_samples x num\_inducing*)) An array of gradients of the objective function with respect to the covariance function.
- **X** (np.ndarray (num\_samples x input\_dim)) Observed data inputs
- **X2** (*np.ndarray* (*num\_inducing* x *input\_dim*)) Observed data inputs (optional, defaults to X)

```
returns: \ dL\_dtheta
```

```
dKdiag_dX (dL_dKdiag, X)
```

```
dKdiag_dtheta(dL_dKdiag, X)
```

Compute the gradient of the diagonal of the covariance function with respect to the parameters.

```
dpsi0_dZ (dL_dpsi0, Z, mu, S)
dpsi0_dmuS (dL_dpsi0, Z, mu, S)
dpsi0_dtheta (dL_dpsi0, Z, mu, S)
dpsi1_dZ (dL_dpsi1, Z, mu, S)
dpsi1_dmuS (dL_dpsi1, Z, mu, S)
    return shapes are num_samples,num_inducing,input_dim
dpsi1_dtheta (dL_dpsi1, Z, mu, S)
dpsi2_dZ (dL_dpsi2, Z, mu, S)
```

 $dpsi2\_dmuS(dL\_dpsi2, Z, mu, S)$ 

dpsi2\_dtheta(dL\_dpsi2, Z, mu, S)

getstate()

Get the current state of the class, here just all the indices, rest can get recomputed

```
plot (x=None, plot_limits=None, which_parts='all', resolution=None, *args, **kwargs)
```

```
plot_ARD (fignum=None, ax=None, title='', legend=False)
```

If an ARD kernel is present, plot a bar representation using matplotlib

- fignum figure number of the plot
- **ax** matplotlib axis to plot on

• title – title of the plot, pass "to not print a title pass None for a generic title

```
prod (other, tensor=False)
```

Multiply two kernels (either on the same space, or on the tensor product of the input space).

#### **Parameters**

- **other** (*GPy.kern*) the other kernel to be added
- **tensor** (*bool*) whether or not to use the tensor space (default is false).

```
psi0(Z, mu, S)
```

psil(Z, mu, S)

psi2(Z, mu, S)

#### **Parameters**

- $\mathbf{Z}$  np.ndarray of inducing inputs (M x Q)
- $S(mu_1)$  np.ndarrays of means and variances (each N x Q)

Returns psi2 np.ndarray (N,M,M)

setstate (state)

```
GPy.kern.kern_test(kern, X=None, X2=None, output\_ind=None, verbose=False, X positive=False)
```

This function runs on kernels to check the correctness of their implementation. It checks that the covariance function is positive definite for a randomly generated data set.

#### **Parameters**

- **kern** (*GPy.kern.Kernpart*) the kernel to be tested.
- **X** (*ndarray*) X input values to test the covariance function.
- X2 (ndarray) X2 input values to test the covariance function.

## **Module contents**

## GPy.likelihoods package

## **Subpackages**

## GPy.likelihoods.noise\_models package

### **Submodules**

### GPy.likelihoods.noise models.bernoulli noise module

Bernoulli likelihood

$$p(y_i|\lambda(f_i)) = \lambda(f_i)^{y_i} (1 - f_i)^{1 - y_i}$$

**Note:** Y is expected to take values in {-1,1} Probit likelihood usually used

## d2logpdf\_dlink2 (link\_f, y, extra\_data=None)

Hessian at y, given link\_f, w.r.t link\_f the hessian will be 0 unless i == j i.e. second derivative logpdf at y given link(f\_i) link(f\_j) w.r.t link(f\_i) and link(f\_j)

$$\frac{d^2 \ln p(y_i|\lambda(f_i))}{d\lambda(f)^2} = \frac{-y_i}{\lambda(f)^2} - \frac{(1-y_i)}{(1-\lambda(f))^2}$$

#### **Parameters**

- link\_f (Nx1 array) latent variables link(f)
- **y** (*Nx1 array*) data
- extra\_data extra\_data not used in bernoulli

**Returns** Diagonal of log hessian matrix (second derivative of log likelihood evaluated at points link(f))

Return type Nx1 array

**Note:** Will return diagonal of hessian, since every where else it is 0, as the likelihood factorizes over cases (the distribution for y\_i depends only on link(f\_i) not on link(f\_(i!=i))

# d3logpdf\_dlink3 (link\_f, y, extra\_data=None)

Third order derivative log-likelihood function at y given link(f) w.r.t link(f)

$$\frac{d^{3} \ln p(y_{i}|\lambda(f_{i}))}{d^{3}\lambda(f)} = \frac{2y_{i}}{\lambda(f)^{3}} - \frac{2(1-y_{i})}{(1-\lambda(f))^{3}}$$

#### **Parameters**

- link\_f (Nx1 array) latent variables link(f)
- **y** (*Nx1 array*) data
- extra\_data extra\_data not used in bernoulli

**Returns** third derivative of log likelihood evaluated at points link(f)

**Return type** Nx1 array

### dlogpdf\_dlink (link\_f, y, extra\_data=None)

Gradient of the pdf at y, given link(f) w.r.t link(f)

$$\frac{d\ln p(y_i|\lambda(f_i))}{d\lambda(f)} = \frac{y_i}{\lambda(f_i)} - \frac{(1-y_i)}{(1-\lambda(f_i))}$$

### **Parameters**

- link\_f (Nx1 array) latent variables link(f)
- y (Nx1 array) data
- extra\_data extra\_data not used in bernoulli

**Returns** gradient of log likelihood evaluated at points link(f)

**Return type** Nx1 array

logpdf\_link (link\_f, y, extra\_data=None)

Log Likelihood function given link(f)

$$\ln p(y_i|\lambda(f_i)) = y_i \log \lambda(f_i) + (1 - y_i) \log(1 - f_i)$$

#### **Parameters**

- link\_f (Nx1 array) latent variables link(f)
- **y** (*Nx1 array*) data
- extra\_data extra\_data not used in bernoulli

**Returns** log likelihood evaluated at points link(f)

Return type float

pdf\_link (link\_f, y, extra\_data=None)

Likelihood function given link(f)

$$p(y_i|\lambda(f_i)) = \lambda(f_i)^{y_i} (1 - f_i)^{1 - y_i}$$

#### **Parameters**

- link\_f (Nx1 array) latent variables link(f)
- **y** (*Nx1 array*) data
- extra\_data extra\_data not used in bernoulli

Returns likelihood evaluated for this point

Return type float

samples(gp)

Returns a set of samples of observations based on a given value of the latent variable.

Parameters gp – latent variable

## GPy.likelihoods.noise\_models.exponential\_noise module

cal\_mean=False,

analyti-

cal\_variance=False)

Bases: GPy.likelihoods.noise\_models.noise\_distributions.NoiseDistribution

Expoential likelihood Y is expected to take values in  $\{0,1,2,...\}$  — \$\$  $L(x) = \exp(lambda) * lambda**Y_i / Y_i! $$$ 

d2logpdf\_dlink2 (link\_f, y, extra\_data=None)

Hessian at y, given link(f), w.r.t link(f) i.e. second derivative logpdf at y given link(f\_i) and link(f\_j) w.r.t link(f\_i) and link(f\_j). The hessian will be 0 unless i == j

$$\frac{d^2 \ln p(y_i|\lambda(f_i))}{d^2 \lambda(f)} = -\frac{1}{\lambda(f_i)^2}$$

### **Parameters**

- link\_f (Nx1 array) latent variables link(f)
- **y** (*Nx1 array*) data
- extra\_data extra\_data which is not used in exponential distribution

**Returns** Diagonal of hessian matrix (second derivative of likelihood evaluated at points f)

Return type Nx1 array

**Note:** Will return diagonal of hessian, since every where else it is 0, as the likelihood factorizes over cases (the distribution for  $y_i$  depends only on  $link(f_i)$  not on  $link(f_i)$ )

d3logpdf\_dlink3 (link\_f, y, extra\_data=None)

Third order derivative log-likelihood function at y given link(f) w.r.t link(f)

$$\frac{d^3 \ln p(y_i|\lambda(f_i))}{d^3 \lambda(f)} = \frac{2}{\lambda(f_i)^3}$$

#### **Parameters**

- link\_f (Nx1 array) latent variables link(f)
- **y** (*Nx1 array*) data
- extra\_data extra\_data which is not used in exponential distribution

Returns third derivative of likelihood evaluated at points f

Return type Nx1 array

dlogpdf\_dlink (link\_f, y, extra\_data=None)

Gradient of the log likelihood function at y, given link(f) w.r.t link(f)

$$\frac{d\ln p(y_i|\lambda(f_i))}{d\lambda(f)} = \frac{1}{\lambda(f)} - y_i$$

#### **Parameters**

- link\_f (Nx1 array) latent variables (f)
- **y** (*Nx1 array*) data
- extra\_data extra\_data which is not used in exponential distribution

Returns gradient of likelihood evaluated at points

Return type Nx1 array

logpdf\_link (link\_f, y, extra\_data=None)

Log Likelihood Function given link(f)

$$\ln p(y_i|\lambda(f_i)) = \ln \lambda(f_i) - y_i\lambda(f_i)$$

### **Parameters**

- link\_f (Nx1 array) latent variables (link(f))
- y (Nx1 array) data
- extra\_data extra\_data which is not used in exponential distribution

**Returns** likelihood evaluated for this point

Return type float

pdf\_link (link\_f, y, extra\_data=None)

Likelihood function given link(f)

$$p(y_i|\lambda(f_i)) = \lambda(f_i) \exp(-y\lambda(f_i))$$

#### **Parameters**

- link\_f (Nx1 array) latent variables link(f)
- **y** (*Nx1 array*) data
- extra\_data extra\_data which is not used in exponential distribution

**Returns** likelihood evaluated for this point

### Return type float

samples(gp)

Returns a set of samples of observations based on a given value of the latent variable.

**Parameters gp** – latent variable

### GPy.likelihoods.noise\_models.gamma\_noise module

class GPy.likelihoods.noise\_models.gamma\_noise.Gamma(gp\_link=None, analyti-

cal\_mean=False, analyti-

 ${\it cal\_variance=False, beta=1.0})\\ Bases: {\tt GPy.likelihoods.noise\_models.noise\_distributions.NoiseDistribution}$ 

Gamma likelihood

$$p(y_i|\lambda(f_i)) = \frac{\beta^{\alpha_i}}{\Gamma(\alpha_i)} y_i^{\alpha_i - 1} e^{-\beta y_i}$$
$$\alpha_i = \beta y_i$$

## d2logpdf\_dlink2 (link\_f, y, extra\_data=None)

Hessian at y, given link(f), w.r.t link(f) i.e. second derivative logpdf at y given link(f\_i) and link(f\_j) w.r.t link(f\_i) and link(f\_j). The hessian will be 0 unless i == j

$$\frac{d^2 \ln p(y_i|\lambda(f_i))}{d^2 \lambda(f)} = -\beta^2 \frac{d\Psi(\alpha_i)}{d\alpha_i}$$
$$\alpha_i = \beta y_i$$

#### **Parameters**

- link\_f (Nx1 array) latent variables link(f)
- **y** (*Nx1 array*) data
- extra\_data extra\_data which is not used in gamma distribution

Returns Diagonal of hessian matrix (second derivative of likelihood evaluated at points f)

Return type Nx1 array

**Note:** Will return diagonal of hessian, since every where else it is 0, as the likelihood factorizes over cases (the distribution for y\_i depends only on link(f\_i) not on link(f\_(j!=i))

### d3logpdf\_dlink3 (link\_f, y, extra\_data=None)

Third order derivative log-likelihood function at y given link(f) w.r.t link(f)

$$\frac{d^3 \ln p(y_i|\lambda(f_i))}{d^3 \lambda(f)} = -\beta^3 \frac{d^2 \Psi(\alpha_i)}{d\alpha_i}$$
$$\alpha_i = \beta y_i$$

### **Parameters**

- link\_f (Nx1 array) latent variables link(f)
- **y** (*Nx1 array*) data
- extra\_data extra\_data which is not used in gamma distribution

Returns third derivative of likelihood evaluated at points f

Return type Nx1 array

dlogpdf\_dlink (link\_f, y, extra\_data=None)

Gradient of the log likelihood function at y, given link(f) w.r.t link(f)

$$\frac{d \ln p(y_i | \lambda(f_i))}{d \lambda(f)} = \beta(\log \beta y_i) - \Psi(\alpha_i)\beta$$

$$\alpha_i = \beta y_i$$

#### **Parameters**

- link\_f (Nx1 array) latent variables (f)
- y (Nx1 array) data
- extra\_data extra\_data which is not used in gamma distribution

**Returns** gradient of likelihood evaluated at points

Return type Nx1 array

logpdf\_link (link\_f, y, extra\_data=None)

Log Likelihood Function given link(f)

$$\ln p(y_i|\lambda(f_i)) = \alpha_i \log \beta - \log \Gamma(\alpha_i) + (\alpha_i - 1) \log y_i - \beta y_i$$
$$\alpha_i = \beta y_i$$

### **Parameters**

- link\_f (Nx1 array) latent variables (link(f))
- **y** (*Nx1 array*) data
- extra\_data extra\_data which is not used in poisson distribution

**Returns** likelihood evaluated for this point

Return type float

pdf\_link (link\_f, y, extra\_data=None)

Likelihood function given link(f)

$$p(y_i|\lambda(f_i)) = \frac{\beta^{\alpha_i}}{\Gamma(\alpha_i)} y_i^{\alpha_i - 1} e^{-\beta y_i}$$
$$\alpha_i = \beta y_i$$

## **Parameters**

- link\_f (Nx1 array) latent variables link(f)
- **y** (*Nx1 array*) data
- extra\_data extra\_data which is not used in poisson distribution

**Returns** likelihood evaluated for this point

Return type float

### GPy.likelihoods.noise\_models.gaussian\_noise module

class GPy.likelihoods.noise\_models.gaussian\_noise.Gaussian ( $gp\_link=None$ , analytical\_mean=False, analytical\_variance=False, variance=1.0, D=None, N=None)

Bases: GPy.likelihoods.noise\_models.noise\_distributions.NoiseDistribution

Gaussian likelihood

$$\ln p(y_i|\lambda(f_i)) = -\frac{N \ln 2\pi}{2} - \frac{\ln |K|}{2} - \frac{(y_i - \lambda(f_i))^T \sigma^{-2}(y_i - \lambda(f_i))}{2}$$

### **Parameters**

- variance variance value of the Gaussian distribution
- N (int) Number of data points

# d2logpdf\_dlink2 (link\_f, y, extra\_data=None)

Hessian at y, given link\_f, w.r.t link\_f. i.e. second derivative logpdf at y given link(f\_i) link(f\_j) w.r.t link(f\_i) and link(f\_j)

The hessian will be 0 unless i == j

$$\frac{d^2 \ln p(y_i|\lambda(f_i))}{d^2 f} = -\frac{1}{\sigma^2}$$

#### **Parameters**

- link\_f (Nx1 array) latent variables link(f)
- y (Nx1 array) data
- extra\_data extra\_data not used in gaussian

**Returns** Diagonal of log hessian matrix (second derivative of log likelihood evaluated at points link(f))

Return type Nx1 array

**Note:** Will return diagonal of hessian, since every where else it is 0, as the likelihood factorizes over cases (the distribution for  $y_i$  depends only on  $link(f_i)$  not on  $link(f_i)$ )

d2logpdf\_dlink2\_dtheta(f, y, extra\_data=None)

d2logpdf\_dlink2\_dvar (link\_f, y, extra\_data=None)

Gradient of the hessian (d2logpdf\_dlink2) w.r.t variance parameter (noise\_variance)

$$\frac{d}{d\sigma^2} \left( \frac{d^2 \ln p(y_i | \lambda(f_i))}{d^2 \lambda(f)} \right) = \frac{1}{\sigma^4}$$

### **Parameters**

- link\_f (Nx1 array) latent variables link(f)
- **y** (*Nx1 array*) data
- extra\_data extra\_data not used in gaussian

**Returns** derivative of log hessian evaluated at points  $link(f_i)$  and  $link(f_j)$  w.r.t variance parameter

**Return type** Nx1 array

d3logpdf\_dlink3 (link\_f, y, extra\_data=None)

Third order derivative log-likelihood function at y given link(f) w.r.t link(f)

$$\frac{d^3 \ln p(y_i|\lambda(f_i))}{d^3 \lambda(f)} = 0$$

#### **Parameters**

- link\_f (Nx1 array) latent variables link(f)
- y (Nx1 array) data
- extra\_data extra\_data not used in gaussian

**Returns** third derivative of log likelihood evaluated at points link(f)

Return type Nx1 array

dlogpdf\_dlink (link\_f, y, extra\_data=None)

Gradient of the pdf at y, given link(f) w.r.t link(f)

$$\frac{d\ln p(y_i|\lambda(f_i))}{d\lambda(f)} = \frac{1}{\sigma^2}(y_i - \lambda(f_i))$$

#### **Parameters**

- link\_f (Nx1 array) latent variables link(f)
- **y** (*Nx1 array*) data
- extra\_data extra\_data not used in gaussian

**Returns** gradient of log likelihood evaluated at points link(f)

**Return type** Nx1 array

dlogpdf\_dlink\_dtheta(f, y, extra\_data=None)

dlogpdf\_dlink\_dvar (link\_f, y, extra\_data=None)

Derivative of the dlogpdf\_dlink w.r.t variance parameter (noise\_variance)

$$\frac{d}{d\sigma^2} \left( \frac{d \ln p(y_i | \lambda(f_i))}{d\lambda(f)} \right) = \frac{1}{\sigma^4} \left( -y_i + \lambda(f_i) \right)$$

### **Parameters**

- link\_f (Nx1 array) latent variables link(f)
- **y** (*Nx1 array*) data
- extra\_data extra\_data not used in gaussian

**Returns** derivative of log likelihood evaluated at points link(f) w.r.t variance parameter

Return type Nx1 array

dlogpdf\_link\_dtheta(f, y, extra\_data=None)

dlogpdf\_link\_dvar (link\_f, y, extra\_data=None)

Gradient of the log-likelihood function at y given link(f), w.r.t variance parameter (noise\_variance)

$$\frac{d \ln p(y_i|\lambda(f_i))}{d\sigma^2} = -\frac{N}{2\sigma^2} + \frac{(y_i - \lambda(f_i))^2}{2\sigma^4}$$

### **Parameters**

• link\_f (Nx1 array) – latent variables link(f)

- **y** (*Nx1 array*) data
- extra\_data extra\_data not used in gaussian

Returns derivative of log likelihood evaluated at points link(f) w.r.t variance parameter

Return type float

logpdf\_link (link\_f, y, extra\_data=None)

Log likelihood function given link(f)

$$\ln p(y_i|\lambda(f_i)) = -\frac{N \ln 2\pi}{2} - \frac{\ln |K|}{2} - \frac{(y_i - \lambda(f_i))^T \sigma^{-2}(y_i - \lambda(f_i))}{2}$$

#### **Parameters**

- link\_f (Nx1 array) latent variables link(f)
- **y** (*Nx1 array*) data
- extra\_data extra\_data not used in gaussian

**Returns** log likelihood evaluated for this point

Return type float

pdf\_link (link\_f, y, extra\_data=None)

Likelihood function given link(f)

$$\ln p(y_i|\lambda(f_i)) = -\frac{N \ln 2\pi}{2} - \frac{\ln |K|}{2} - \frac{(y_i - \lambda(f_i))^T \sigma^{-2}(y_i - \lambda(f_i))}{2}$$

### **Parameters**

- link\_f (Nx1 array) latent variables link(f)
- **y** (*Nx1 array*) data
- extra\_data extra\_data not used in gaussian

**Returns** likelihood evaluated for this point

Return type float

 ${\tt samples}\,(gp)$ 

Returns a set of samples of observations based on a given value of the latent variable.

**Parameters gp** – latent variable

### GPy.likelihoods.noise\_models.gp\_transformations module

class GPy.likelihoods.noise\_models.gp\_transformations.GPTransformation
 Bases: object

Link function class for doing non-Gaussian likelihoods approximation

**Parameters Y** – observed output (Nx1 numpy.darray)

Note: Y values allowed depend on the likelihood\_function used

 $d2transf_df2(f)$ 

second derivative of transf(f) w.r.t. f

 $d3transf_df3(f)$ 

third derivative of transf(f) w.r.t. f

```
dtransf df(f)
         derivative of transf(f) w.r.t. f
    transf(f)
         Gaussian process tranformation function, latent space -> output space
class GPy.likelihoods.noise_models.gp_transformations.Heaviside
    Bases: GPy.likelihoods.noise_models.gp_transformations.GPTransformation
                                          q(f) = I_{x \in A}
    d2transf_df2(f)
    dtransf_df(f)
    transf(f)
class GPy.likelihoods.noise_models.gp_transformations.Identity
    Bases: GPy.likelihoods.noise_models.gp_transformations.GPTransformation
                                           q(f) = f
    d2transf_df2(f)
    d3transf_df3(f)
    dtransf df(f)
    {\tt transf}\,(f)
class GPy.likelihoods.noise_models.gp_transformations.Log
    Bases: GPy.likelihoods.noise_models.gp_transformations.GPTransformation
                                         g(f) = \log(\mu)
    d2transf_df2(f)
    d3transf_df3(f)
    dtransf_df(f)
    transf(f)
class GPy.likelihoods.noise models.qp transformations.Log ex 1
    Bases: GPy.likelihoods.noise_models.gp_transformations.GPTransformation
                                     q(f) = \log(\exp(\mu) - 1)
    d2transf_df2(f)
    d3transf_df3(f)
    dtransf_df(f)
    transf(f)
```

```
 \begin{tabular}{l} \textbf{class} \ GPy.likelihoods.noise\_models.gp\_transformations.Probit \\ Bases: \ GPy.likelihoods.noise\_models.gp\_transformations.GPTransformation \\ g(f) = \Phi^{-1}(mu) \\ \\ \begin{tabular}{l} d2transf\_df2 \ (f) \\ d3transf\_df3 \ (f) \\ dtransf\_df \ (f) \\ transf \ (f) \\ \\ \begin{tabular}{l} class \ GPy.likelihoods.noise\_models.gp\_transformations.Reciprocal \\ Bases: \ GPy.likelihoods.noise\_models.gp\_transformations.GPTransformation \\ d2transf\_df2 \ (f) \\ d3transf\_df3 \ (f) \\ d4transf\_df3 \ (f) \\ d4transf\_df3 \ (f) \\ dtransf\_df3 \ (f) \\ dtransf\_df3 \ (f) \\ dtransf\_df3 \ (f) \\ \end{tabular}
```

## GPy.likelihoods.noise\_models.noise\_distributions module

 ${\bf class}~{\tt GPy.likelihoods.noise\_models.noise\_distributions.} {\bf NoiseDistribution}~({\it gp\_link},$ 

analytical\_mean=False, analyti-

lyti-

 $cal\_variance {=} False)$ 

Bases: object

transf(f)

Likelihood class for doing approximations

$$\verb"d2logpdf_df2" (f, y, extra\_data = None")$$

Evaluates the link function link(f) then computes the second derivative of log likelihood using it Uses the Faa di Bruno's formula for the chain rule

$$\frac{d^2 \log p(y|\lambda(f))}{df^2} = \frac{d^2 \log p(y|\lambda(f))}{d^2 \lambda(f)} \left(\frac{d\lambda(f)}{df}\right)^2 + \frac{d \log p(y|\lambda(f))}{d\lambda(f)} \frac{d^2 \lambda(f)}{df^2}$$

#### **Parameters**

- **f** (Nx1 array) latent variables f
- **y** (*Nx1 array*) data
- extra\_data extra\_data which is not used in student t distribution not used

**Returns** second derivative of log likelihood evaluated for this point (diagonal only)

**Return type** 1xN array

d3logpdf\_df3 (f, y, extra\_data=None)

Evaluates the link function link(f) then computes the third derivative of log likelihood using it Uses the Faa di Bruno's formula for the chain rule

$$\frac{d^3 \log p(y|\lambda(f))}{df^3} = \frac{d^3 \log p(y|\lambda(f))}{d\lambda(f)^3} \left(\frac{d\lambda(f)}{df}\right)^3 + 3\frac{d^2 \log p(y|\lambda(f))}{d\lambda(f)^2} \frac{d\lambda(f)}{df} \frac{d^2\lambda(f)}{df^2} + \frac{d \log p(y|\lambda(f))}{d\lambda(f)} \frac{d^3\lambda(f)}{df^3} \frac{d^3\lambda(f)}{df^3} + \frac{d^3 \log p(y|\lambda(f))}{df^3} + \frac{d^3 \log p(y|\lambda(f))}{d$$

#### **Parameters**

- **f** (Nx1 array) latent variables f
- **y** (*Nx1 array*) data
- extra\_data extra\_data which is not used in student t distribution not used

**Returns** third derivative of log likelihood evaluated for this point

Return type float

d3logpdf\_dlink3 (link\_f, y, extra\_data=None)

**dlogpdf df** (*f*, *y*, *extra data=None*)

Evaluates the link function link(f) then computes the derivative of log likelihood using it Uses the Faa di Bruno's formula for the chain rule

$$\frac{d\log p(y|\lambda(f))}{df} = \frac{d\log p(y|\lambda(f))}{d\lambda(f)} \frac{d\lambda(f)}{df}$$

#### **Parameters**

- **f** (Nx1 array) latent variables f
- y (Nx1 array) data
- extra\_data extra\_data which is not used in student t distribution not used

**Returns** derivative of log likelihood evaluated for this point

**Return type** 1xN array

dlogpdf\_df\_dtheta (f, y, extra\_data=None)

TODO: Doc strings

dlogpdf\_dlink (link\_f, y, extra\_data=None)

dlogpdf\_dlink\_dtheta (link\_f, y, extra\_data=None)

dlogpdf\_dtheta (f, y, extra\_data=None)

TODO: Doc strings

dlogpdf\_link\_dtheta(link\_f, y, extra\_data=None)

log\_predictive\_density (y\_test, mu\_star, var\_star)

Calculation of the log predictive density

### **Parameters**

- **y\_test** ((Nx1) array) test observations (y\_{\*})
- **mu\_star** ((Nx1) array) predictive mean of gaussian p(f\_{\*}|mu\_{\*}, var\_{\*})
- $var\_star((Nx1) array)$  predictive variance of gaussian  $p(f_{*}) mu_{*}$ ,  $var_{*}$

logpdf (f, y, extra\_data=None)

Evaluates the link function link(f) then computes the log likelihood (log pdf) using it

- **f** (Nx1 array) latent variables f
- **y** (*Nx1 array*) data
- extra\_data extra\_data which is not used in student t distribution not used

**Returns** log likelihood evaluated for this point

Return type float

logpdf\_link (link\_f, y, extra\_data=None)

**pdf** (*f*, *y*, *extra\_data=None*)

Evaluates the link function link(f) then computes the likelihood (pdf) using it

#### **Parameters**

- **f** (Nx1 array) latent variables f
- **y** (*Nx1 array*) data
- extra\_data extra\_data which is not used in student t distribution not used

**Returns** likelihood evaluated for this point

**Return type** float

pdf\_link (link\_f, y, extra\_data=None)

**predictive\_values** (*mu*, *var*, *full\_cov=False*, *sampling=False*, *num\_samples=10000*)

Compute mean, variance and conficence interval (percentiles 5 and 95) of the prediction.

#### **Parameters**

- mu mean of the latent variable, f, of posterior
- var variance of the latent variable, f, of posterior
- full\_cov (Boolean) whether to use the full covariance or just the diagonal
- num\_samples (integer) number of samples to use in computing quantiles and possibly mean variance
- sampling (Boolean) Whether to use samples for mean and variances anyway

samples(gp)

Returns a set of samples of observations based on a given value of the latent variable.

Parameters gp – latent variable

# GPy.likelihoods.noise\_models.poisson\_noise module

 $\begin{array}{ll} \textbf{class} \ \texttt{GPy.likelihoods.noise\_models.poisson\_noise.Poisson} \ (\textit{gp\_link=None}, & \textit{analytical\_mean=False}, \\ & \textit{cal\_mean=False}, & \textit{cal variance=False}) \end{array}$ 

Bases: GPy.likelihoods.noise models.noise distributions.NoiseDistribution

Poisson likelihood

$$p(y_i|\lambda(f_i)) = \frac{\lambda(f_i)^{y_i}}{y_i!}e^{-\lambda(f_i)}$$

**Note:** Y is expected to take values in  $\{0,1,2,...\}$ 

### d2logpdf\_dlink2 (link\_f, y, extra\_data=None)

Hessian at y, given link(f), w.r.t link(f) i.e. second derivative logpdf at y given  $link(f_i)$  and  $link(f_j)$  w.r.t link(f) i and link(f) i.e. second derivative logpdf at y given  $link(f_i)$  and  $link(f_j)$  w.r.t link(f) i and link(f) i.e. second derivative logpdf at y given  $link(f_i)$  and  $link(f_j)$  w.r.t

$$\frac{d^2 \ln p(y_i|\lambda(f_i))}{d^2 \lambda(f)} = \frac{-y_i}{\lambda(f_i)^2}$$

#### **Parameters**

- link\_f (Nx1 array) latent variables link(f)
- **y** (*Nx1 array*) data
- extra\_data extra\_data which is not used in poisson distribution

**Returns** Diagonal of hessian matrix (second derivative of likelihood evaluated at points f)

Return type Nx1 array

**Note:** Will return diagonal of hessian, since every where else it is 0, as the likelihood factorizes over cases (the distribution for y\_i depends only on link(f\_i) not on link(f\_(j!=i))

# d3logpdf\_dlink3 (link\_f, y, extra\_data=None)

Third order derivative log-likelihood function at y given link(f) w.r.t link(f)

$$\frac{d^3 \ln p(y_i|\lambda(f_i))}{d^3 \lambda(f)} = \frac{2y_i}{\lambda(f_i)^3}$$

#### **Parameters**

- link\_f (Nx1 array) latent variables link(f)
- **y** (*Nx1 array*) data
- extra data extra data which is not used in poisson distribution

**Returns** third derivative of likelihood evaluated at points f

Return type Nx1 array

# dlogpdf\_dlink (link\_f, y, extra\_data=None)

Gradient of the log likelihood function at y, given link(f) w.r.t link(f)

$$\frac{d\ln p(y_i|\lambda(f_i))}{d\lambda(f)} = \frac{y_i}{\lambda(f_i)} - 1$$

### **Parameters**

- link\_f (Nx1 array) latent variables (f)
- **y** (*Nx1 array*) data
- extra\_data extra\_data which is not used in poisson distribution

Returns gradient of likelihood evaluated at points

**Return type** Nx1 array

logpdf\_link (link\_f, y, extra\_data=None)

Log Likelihood Function given link(f)

$$\ln p(y_i|\lambda(f_i)) = -\lambda(f_i) + y_i \log \lambda(f_i) - \log y_i!$$

- link\_f (Nx1 array) latent variables (link(f))
- y (Nx1 array) data
- extra\_data extra\_data which is not used in poisson distribution

**Returns** likelihood evaluated for this point

Return type float

pdf\_link (link\_f, y, extra\_data=None)

Likelihood function given link(f)

$$p(y_i|\lambda(f_i)) = \frac{\lambda(f_i)^{y_i}}{y_i!}e^{-\lambda(f_i)}$$

#### **Parameters**

- link f (Nx1 array) latent variables link(f)
- **y** (*Nx1 array*) data
- extra\_data extra\_data which is not used in poisson distribution

Returns likelihood evaluated for this point

Return type float

samples(gp)

Returns a set of samples of observations based on a given value of the latent variable.

Parameters gp – latent variable

# GPy.likelihoods.noise\_models.student\_t\_noise module

Bases: GPy.likelihoods.noise\_models.noise\_distributions.NoiseDistribution

Student T likelihood

For nomanclature see Bayesian Data Analysis 2003 p576

$$p(y_i|\lambda(f_i)) = \frac{\Gamma\left(\frac{v+1}{2}\right)}{\Gamma\left(\frac{v}{2}\right)\sqrt{v\pi\sigma^2}} \left(1 + \frac{1}{v}\left(\frac{(y_i - f_i)^2}{\sigma^2}\right)\right)^{\frac{-v+1}{2}}$$

d2logpdf\_dlink2 (link\_f, y, extra\_data=None)

Hessian at y, given link(f), w.r.t link(f) i.e. second derivative logpdf at y given link(f\_i) and link(f\_j) w.r.t link(f\_i) and link(f\_j). The hessian will be 0 unless i == j

$$\frac{d^2 \ln p(y_i|\lambda(f_i))}{d^2 \lambda(f)} = \frac{(v+1)((y_i - \lambda(f_i))^2 - \sigma^2 v)}{((y_i - \lambda(f_i))^2 + \sigma^2 v)^2}$$

## **Parameters**

- link\_f (Nx1 array) latent variables link(f)
- **y** (*Nx1 array*) data
- extra\_data extra\_data which is not used in student t distribution

**Returns** Diagonal of hessian matrix (second derivative of likelihood evaluated at points f)

# **Return type** Nx1 array

**Note:** Will return diagonal of hessian, since every where else it is 0, as the likelihood factorizes over cases (the distribution for  $y_i$  depends only on link( $f_i$ ) not on link( $f_i$ ).

d2logpdf\_dlink2\_dtheta(f, y, extra\_data=None)

d2logpdf\_dlink2\_dvar (link\_f, y, extra\_data=None)

Gradient of the hessian (d2logpdf\_dlink2) w.r.t variance parameter (t\_noise)

$$\frac{d}{d\sigma^2} \left( \frac{d^2 \ln p(y_i | \lambda(f_i))}{d^2 f} \right) = \frac{v(v+1)(\sigma^2 v - 3(y_i - \lambda(f_i))^2)}{(\sigma^2 v + (y_i - \lambda(f_i))^2)^3}$$

#### **Parameters**

- link\_f (Nx1 array) latent variables link(f)
- **y** (*Nx1 array*) data
- extra\_data extra\_data which is not used in student t distribution

**Returns** derivative of hessian evaluated at points f and f\_j w.r.t variance parameter

**Return type** Nx1 array

d3logpdf\_dlink3 (link\_f, y, extra\_data=None)

Third order derivative log-likelihood function at y given link(f) w.r.t link(f)

$$\frac{d^3 \ln p(y_i|\lambda(f_i))}{d^3 \lambda(f)} = \frac{-2(v+1)((y_i - \lambda(f_i))^3 - 3(y_i - \lambda(f_i))\sigma^2 v))}{((y_i - \lambda(f_i)) + \sigma^2 v)^3}$$

## **Parameters**

- link\_f (Nx1 array) latent variables link(f)
- **y** (*Nx1 array*) data
- extra\_data extra\_data which is not used in student t distribution

**Returns** third derivative of likelihood evaluated at points f

Return type Nx1 array

dlogpdf\_dlink (link\_f, y, extra\_data=None)

Gradient of the log likelihood function at y, given link(f) w.r.t link(f)

$$\frac{d \ln p(y_i|\lambda(f_i))}{d\lambda(f)} = \frac{(v+1)(y_i - \lambda(f_i))}{(y_i - \lambda(f_i))^2 + \sigma^2 v}$$

# **Parameters**

- link\_f (Nx1 array) latent variables (f)
- **y** (*Nx1 array*) data
- extra data extra data which is not used in student t distribution

**Returns** gradient of likelihood evaluated at points

**Return type** Nx1 array

dlogpdf\_dlink\_dtheta(f, y, extra\_data=None)

dlogpdf\_dlink\_dvar (link\_f, y, extra\_data=None)

Derivative of the dlogpdf\_dlink w.r.t variance parameter (t\_noise)

$$\frac{d}{d\sigma^2} \left( \frac{d \ln p(y_i | \lambda(f_i))}{df} \right) = \frac{-2\sigma v(v+1)(y_i - \lambda(f_i))}{(y_i - \lambda(f_i))^2 + \sigma^2 v)^2}$$

## **Parameters**

- link\_f (Nx1 array) latent variables link\_f
- **y** (*Nx1 array*) data
- extra\_data extra\_data which is not used in student t distribution

Returns derivative of likelihood evaluated at points f w.r.t variance parameter

Return type Nx1 array

dlogpdf\_link\_dtheta(f, y, extra\_data=None)

dlogpdf\_link\_dvar (link\_f, y, extra\_data=None)

Gradient of the log-likelihood function at y given f, w.r.t variance parameter (t\_noise)

$$\frac{d \ln p(y_i|\lambda(f_i))}{d\sigma^2} = \frac{v((y_i - \lambda(f_i))^2 - \sigma^2)}{2\sigma^2(\sigma^2v + (y_i - \lambda(f_i))^2)}$$

#### **Parameters**

- link\_f (Nx1 array) latent variables link(f)
- **y** (*Nx1 array*) data
- extra data extra data which is not used in student t distribution

Returns derivative of likelihood evaluated at points f w.r.t variance parameter

Return type float

logpdf\_link (link\_f, y, extra\_data=None)

Log Likelihood Function given link(f)

$$\ln p(y_i|\lambda(f_i)) = \ln \Gamma\left(\frac{v+1}{2}\right) - \ln \Gamma\left(\frac{v}{2}\right) - \ln \sqrt{v\pi\sigma^2} - \frac{v+1}{2}\ln\left(1 + \frac{1}{v}\left(\frac{(y_i - \lambda(f_i))^2}{\sigma^2}\right)\right)$$

## **Parameters**

- link\_f (Nx1 array) latent variables (link(f))
- y (Nx1 array) data
- extra\_data extra\_data which is not used in student t distribution

Returns likelihood evaluated for this point

Return type float

pdf\_link (link\_f, y, extra\_data=None)

Likelihood function given link(f)

$$p(y_i|\lambda(f_i)) = \frac{\Gamma\left(\frac{v+1}{2}\right)}{\Gamma\left(\frac{v}{2}\right)\sqrt{v\pi\sigma^2}} \left(1 + \frac{1}{v}\left(\frac{(y_i - \lambda(f_i))^2}{\sigma^2}\right)\right)^{\frac{v+1}{2}}$$

## **Parameters**

• link\_f (Nx1 array) – latent variables link(f)

- **y** (*Nx1 array*) data
- extra data extra data which is not used in student t distribution

Returns likelihood evaluated for this point

Return type float

samples(gp)

Returns a set of samples of observations based on a given value of the latent variable.

Parameters gp – latent variable

variance

## Module contents

#### **Submodules**

# GPy.likelihoods.ep module

```
class GPy.likelihoods.ep.EP (data, noise_model)
    Bases: GPy.likelihoods.likelihood.likelihood
```

**fit\_DTC** (*Kmm*, *Kmn*, *epsilon=0.001*, *power\_ep=[1.0, 1.0]*)

The expectation-propagation algorithm with sparse pseudo-input. For nomenclature see ... 2013.

#### **Parameters**

- **epsilon** (*float*) Convergence criterion, maximum squared difference allowed between mean updates to stop iterations (float)
- power\_ep (list of floats) Power EP parameters

```
fit_FITC (Kmm, Kmn, Knn_diag, epsilon=0.001, power_ep=[1.0, 1.0])
```

The expectation-propagation algorithm with sparse pseudo-input. For nomenclature see Naish-Guzman and Holden, 2008.

## **Parameters**

- **epsilon** (*float*) Convergence criterion, maximum squared difference allowed between mean updates to stop iterations (float)
- **power\_ep** (*list of floats*) Power EP parameters

```
fit_full (K, epsilon=0.001, power_ep=[1.0, 1.0])
```

The expectation-propagation algorithm. For nomenclature see Rasmussen & Williams 2006.

## **Parameters**

- **epsilon** (*float*) Convergence criterion, maximum squared difference allowed between mean updates to stop iterations (float)
- power\_ep (list of floats) Power EP parameters

```
log_predictive_density (y_test, mu_star, var_star)
```

Calculation of the log predictive density

## **Parameters**

- **y\_test** ((Nx1) array) test observations (y\_{\*})
- mu\_star ((Nx1) array) predictive mean of gaussian p(f\_{\*}|mu\_{\*}, var\_{\*})

```
• var_star((Nx1) array) – predictive variance of gaussian p(f_{*}) mu_{*}, var_{*}
     predictive_values (mu, var, full_cov, **noise_args)
     restart()
GPy.likelihoods.ep_mixed_noise module
class GPy.likelihoods.ep_mixed_noise.EP_Mixed_Noise (data_list,
                                                                              noise_model_list,
                                                                   silon=0.001, power\_ep=[1.0, 1.0])
     Bases: GPy.likelihoods.likelihood.likelihood
     fit DTC(Kmm, Kmn)
          The expectation-propagation algorithm with sparse pseudo-input. For nomenclature see ... 2013.
     fit_FITC (Kmm, Kmn, Knn_diag)
          The expectation-propagation algorithm with sparse pseudo-input. For nomenclature see Naish-Guzman
          and Holden, 2008.
     fit full(K)
          The expectation-propagation algorithm. For nomenclature see Rasmussen & Williams 2006.
     predictive_values (mu, var, full_cov, noise_model)
          Predicts the output given the GP
              Parameters
                   • mu – GP's mean
                   • var – GP's variance
                   • full cov (False|True) – whether to return the full covariance matrix, or just the diagonal
                   • noise_model (integer) – noise model to use
     restart()
GPy.likelihoods.gaussian module
class GPy.likelihoods.gaussian.Gaussian (data, variance=1.0, normalize=False)
     Bases: GPy.likelihoods.likelihood.likelihood
     Likelihood class for doing Expectation propagation
          Parameters
                • data (Nx1 numpy.darray) – observed output
                • variance – noise parameter
                • normalize (False|True) – whether to normalize the data before computing (predictions will
                  be in original scales)
     log_predictive_density(y_test, mu_star, var_star)
          Calculation of the log predictive density
              Parameters
                   • y_test ((Nx1) array) – test observations (y_{*})
                   • mu_star((Nx1) array) – predictive mean of gaussian p(f_{*}) | mu_{*}, var_{*}
                   • var\_star((Nx1) array) – predictive variance of gaussian p(f_{*}) mu_{*}, var_{*}
```

```
predictive_values (mu, var, full_cov, **likelihood_args)
```

Un-normalize the prediction and add the likelihood variance, then return the 5%, 95% interval

```
set_data(data)
```

## GPy.likelihoods.gaussian mixed noise module

Bases: GPy.likelihoods.likelihood.likelihood

Gaussian Likelihood for multiple outputs

This is a wrapper around likelihood. Gaussian class

## **Parameters**

- data\_list (list of numpy arrays (num\_data\_output\_i x 1), one array per output) data observations
- noise\_params (list of floats, one per output) noise parameters of each output
- **normalize** (*False*|*True*) whether to normalize the data before computing (predictions will be in original scales)

```
predictive_values (mu, var, full_cov, noise_model)
```

Predicts the output given the GP

## **Parameters**

- mu GP's mean
- var GP's variance
- full\_cov (False|True) whether to return the full covariance matrix, or just the diagonal
- noise\_model (integer) noise model to use

set\_data(data\_list)

# GPy.likelihoods.laplace module

```
class GPy.likelihoods.laplace.Laplace(data, noise_model, extra_data=None)
    Bases: GPy.likelihoods.likelihood.likelihood
```

Laplace approximation to a posterior

```
fit full (K)
```

The laplace approximation algorithm, find K and expand hessian For nomenclature see Rasmussen & Williams 2006 - modified for numerical stability

Parameters K (NxN matrix) – Prior covariance matrix evaluated at locations X

```
log_predictive_density (y_test, mu_star, var_star)
```

Calculation of the log predictive density

## **Parameters**

- **y\_test** ((Nx1) array) test observations (y\_{\*})
- **mu\_star** ((Nx1) array) predictive mean of gaussian p(f\_{\*}|mu\_{\*}, var\_{\*})

```
• var_star ((Nx1) array) – predictive variance of gaussian p(f_{*}|mu_{*}, var_{*})
     predictive_values (mu, var, full_cov, **noise_args)
     rasm_mode(K, MAX\_ITER=40)
           Rasmussen's numerically stable mode finding For nomenclature see Rasmussen & Williams 2006 Influ-
           enced by GPML (BSD) code, all errors are our own
               Parameters
                   • K (NxD matrix) – Covariance matrix evaluated at locations X
                   • MAX_ITER (scalar) – Maximum number of iterations of newton-raphson before forcing
                      finish of optimisation
               Returns f_hat, mode on which to make laplace approxmiation
               Return type NxD matrix
     restart()
           Reset likelihood variables to their defaults
GPy.likelihoods.likelihood module
class GPy.likelihoods.likelihood.likelihood
     Bases: GPy.core.parameterized.Parameterized
     The atom for a likelihood class
     This object interfaces the GP and the data. The most basic likelihood (Gaussian) inherits directly from this, as
     does the EP algorithm
     Some things must be defined for this to work properly:
          •self.Y: the effective Gaussian target of the GP
          •self.N, self.D: Y.shape
          •self.covariance_matrix : the effective (noise) covariance of the GP targets
          •self.Z: a factor which gets added to the likelihood (0 for a Gaussian, Z_EP for EP)
          •self.is heteroscedastic: enables significant computational savings in GP
          •self.precision: a scalar or vector representation of the effective target precision
          •self.YYT : (optional) = np.dot(self.Y, self.Y.T) enables computational savings for D>N
          •self.V: self.precision * self.Y
     fit full(K)
           No approximations needed by default
     log_predictive_density (y_test, mu_star, var_star)
           Calculation of the predictive density
               Parameters
                   • y test ((Nx1) array) – test observations (y \{*\})
                   • mu_star((Nx1) array) – predictive mean of gaussian p(f_{*}) mu_{*}, var_{*}
```

predictive values(mu, var)

• var\_star ((Nx1) array) – predictive variance of gaussian p(f\_{\*}|mu\_{\*}, var\_{\*})

## restart()

No need to restart if not an approximation

# GPy.likelihoods.noise\_model\_constructors module

GPy.likelihoods.noise\_model\_constructors.bernoulli(gp\_link=None)
 Construct a bernoulli likelihood

# **Parameters gp\_link** – a GPy gp\_link function

GPy.likelihoods.noise\_model\_constructors.exponential(gp\_link=None)
Construct a exponential likelihood

# **Parameters gp\_link** – a GPy **gp\_link** function

GPy.likelihoods.noise\_model\_constructors.gamma(gp\_link=None, beta=1.0)
Construct a Gamma likelihood

## **Parameters**

- **gp\_link** a GPy gp\_link function
- **beta** scalar

GPy.likelihoods.noise\_model\_constructors.gaussian( $gp\_link=None$ , variance=2, D=None, N=None)

Construct a Gaussian likelihood

#### **Parameters**

- **gp\_link** a GPy gp\_link function
- variance (scalar) variance

## **Returns** Gaussian noise model:

GPy.likelihoods.noise\_model\_constructors.gaussian\_ep(gp\_link=None, variance=1.0)
Construct a gaussian likelihood

## **Parameters**

- gp\_link a GPy gp\_link function
- variance scalar

GPy.likelihoods.noise\_model\_constructors.poisson(gp\_link=None)
Construct a Poisson likelihood

# **Parameters gp\_link** – a GPy **gp\_link** function

GPy.likelihoods.noise\_model\_constructors.student\_t (gp\_link=None, sigma2=2)
deg\_free=5,

Construct a Student t likelihood

## **Parameters**

- **gp\_link** a GPy gp\_link function
- **deg\_free** (*scalar*) degrees of freedom of student-t
- sigma2 (scalar) variance

Returns Student-T noise model

## **Module contents**

# GPy.mappings package

# **Submodules**

# GPy.mappings.kernel module

```
class GPy.mappings.kernel.Kernel (X, output_dim=1, kernel=None)
    Bases: GPy.core.mapping.Mapping
```

Mapping based on a kernel/covariance function.

$$f(\mathbf{x}^*) = \mathbf{Ak}(\mathbf{X}, \mathbf{x}^*) + \mathbf{b}$$

# **Parameters**

- **X** (*ndarray*) input observations containing **X**
- **output\_dim** (*int*) dimension of output.
- **kernel** (*GPy.kern.kern*) a GPy kernel, defaults to GPy.kern.rbf

```
\begin{split} & \texttt{df\_dX} \; (dL\_df, X) \\ & \texttt{df\_dtheta} \; (dL\_df, X) \\ & \texttt{f} \; (X) \\ & \texttt{randomize} \; () \end{split}
```

# GPy.mappings.linear module

```
class GPy.mappings.linear.Linear(input_dim=1, output_dim=1)
    Bases: GPy.core.mapping.Mapping
```

Mapping based on a linear model.

$$f(\mathbf{x}*) = \mathbf{W}\mathbf{x}^* + \mathbf{b}$$

## **Parameters**

- **X** (*ndarray*) input observations
- **output\_dim** (*int*) dimension of output.

```
\begin{split} \mathbf{df\_dX} & (dL\_df, X) \\ \mathbf{df\_dtheta} & (dL\_df, X) \\ \mathbf{f} & (X) \\ \\ \mathbf{randomize} & () \end{split}
```

# GPy.mappings.mlp module

```
class GPy.mappings.mlp.MLP (input_dim=1, output_dim=1, hidden_dim=3)
    Bases: GPy.core.mapping.Mapping
```

Mapping based on a multi-layer perceptron neural network model.

$$f(\mathbf{x}*) = \mathbf{W}^0 \phi (\mathbf{W}^1 \mathbf{x} + \mathbf{b}^1)^* + \mathbf{b}^0$$

where

$$\phi(\cdot) = \tanh(\cdot)$$

## **Parameters**

- **X** (*ndarray*) input observations
- **output\_dim** (*int*) dimension of output.
- hidden\_dim (int or list of ints.) dimension of hidden layer. If it is an int, there is one hidden layer of the given dimension. If it is a list of ints there are as manny hidden layers as the length of the list, each with the given number of hidden nodes in it.

```
\begin{split} & \texttt{df\_dX} \; (dL\_df, X) \\ & \texttt{df\_dtheta} \; (dL\_df, X) \\ & \texttt{f} \; (X) \\ & \texttt{randomize} \; () \end{split}
```

## **Module contents**

# GPy.models\_modules package

# **Submodules**

# GPy.models\_modules.bayesian\_gplvm module

```
class GPy.models_modules.bayesian_gplvm.BayesianGPLVM(likelihood\_or\_Y, input\_dim, X=None, X\_variance=None, init='PCA', num\_inducing=10, Z=None, kernel=None, **kwargs)
```

Bases: GPy.core.sparse\_gp.SparseGP, GPy.models\_modules.gplvm.GPLVM

Bayesian Gaussian Process Latent Variable Model

# **Parameters**

- Y (np.ndarray| GPy.likelihood instance) observed data (np.ndarray) or GPy.likelihood
- **input\_dim** (*int*) latent dimensionality
- init ('PCA'|'random') initialisation method for the latent space

```
KL_divergence()
dKL_dmuS()
dL_dmuS()
dmu_dX(Xnew)
Calculate the gradient of the prediction at Xnew w.r.t Xnew.
dmu_dXnew(Xnew)
Individual gradient of prediction at Xnew w.r.t. each sample in Xnew
```

```
do test latents (Y)
           Compute the latent representation for a set of new points Y
           Notes: This will only work with a univariate Gaussian likelihood (for now)
     getstate()
           Get the current state of the class, here just all the indices, rest can get recomputed
     log_likelihood()
     plot_X_1d (fignum=None, ax=None, colors=None)
           Plot latent space X in 1D:
              •if fig is given, create input_dim subplots in fig and plot in these
              •if ax is given plot input_dim 1D latent space plots of X into each axis
              •if neither fig nor ax is given create a figure with fignum and plot in there
           colors: colors of different latent space dimensions input_dim
     plot latent(plot inducing=True, *args, **kwargs)
     plot_steepest_gradient_map (fignum=None, ax=None, which_indices=None, labels=None,
                                           data_labels=None, data_marker='o', data_s=40, resolu-
                                           tion=20, aspect='auto', updates=False, **kwargs)
     setstate (state)
class GPy.models_modules.bayesian_gplvm.BayesianGPLVMWithMissingData(likelihood_or_Y,
                                                                                             input_dim,
                                                                                             X=None,
                                                                                             X_variance=None,
                                                                                             init='PCA',
                                                                                             num_inducing=10,
                                                                                             Z=None,
                                                                                             ker-
                                                                                             nel=None,
                                                                                             **kwargs)
     Bases: GPy.core.model.Model
     Bayesian Gaussian Process Latent Variable Model with missing data support. NOTE: Missing data is assumed
     to be missing at random!
     This extension comes with a large memory and computing time deficiency. Use only if fraction of missing data
     at random is higher than 60%. Otherwise, try filtering data before using this extension.
     Y can hold missing data as given by missing, standard is nan.
     If likelihood is given for Y, this likelihood will be discarded, but the parameters of the likelihood will be taken.
     Also every effort of creating the same likelihood will be done.
           Parameters
                 • likelihood_or_Y (ndarray | likelihood instance) - observed data (np.ndarray) or
                   GPy.likelihood
                 • input_dim (int) – latent dimensionality
                 • init ('PCA' | 'random') – initialisation method for the latent space
     getstate()
     log_likelihood()
```

#### setstate (state)

```
GPy.models_modules.bayesian_gplvm.latent_cost (mu_s, kern, Z, dL_dpsi0, dL_dpsi1, dL_dpsi2) objective function for fitting the latent variables (negative log-likelihood: should be minimised!) This is the same as latent_cost_and_grad but only for the objective
```

```
GPy.models_modules.bayesian_gplvm.latent_cost_and_grad (mu_S, kern, Z, dL_dpsi0, dL_dpsi1, dL_dpsi2) objective function for fitting the latent variables for test points (negative log-likelihood: should be minimised!)
```

GPy.models\_modules.bayesian\_gplvm.latent\_grad( $mu\_S$ , kern, Z,  $dL\_dpsi0$ ,  $dL\_dpsi1$ ,  $dL\_dpsi2$ )

This is the same as latent\_cost\_and\_grad but only for the grad

## GPy.models modules.bcgplvm module

 $Bases: \verb|GPy.models_modules.gplvm.GPLVM| \\$ 

Back constrained Gaussian Process Latent Variable Model

## **Parameters**

- Y (np.ndarray) observed data
- input\_dim (int) latent dimensionality
- init ('PCA'|'random') initialisation method for the latent space
- mapping (GPy.core.Mapping object) mapping for back constraint

# GPy.models\_modules.fitc\_classification module

Bases: GPy.core.fitc.FITC

FITC approximation for classification

This is a thin wrapper around the FITC class, with a set of sensible defaults

## **Parameters**

- **X** input observations
- Y observed values
- likelihood a GPy likelihood, defaults to Bernoulli with probit link function
- **kernel** a GPy kernel, defaults to rbf+white
- **normalize\_X** (*False*|*True*) whether to normalize the input data before computing (predictions will be in original scales)

rank=1)

• **normalize\_Y** (*False|True*) – whether to normalize the input data before computing (predictions will be in original scales)

Return type model object

# GPy.models\_modules.gp\_classification module

```
class GPy.models_modules.gp_classification.GPClassification (X, Y=None, like-lihood=None, ker-nel=None, normal-ize_X=False, normal-ize_Y=False)
```

Bases: GPy.core.gp.GP

Gaussian Process classification

This is a thin wrapper around the models.GP class, with a set of sensible defaults

## **Parameters**

- **X** input observations
- Y observed values, can be None if likelihood is not None
- likelihood a GPy likelihood, defaults to Bernoulli with Probit link\_function
- **kernel** a GPy kernel, defaults to rbf
- **normalize\_X** (*False*|*True*) whether to normalize the input data before computing (predictions will be in original scales)
- **normalize\_Y** (*False*|*True*) whether to normalize the input data before computing (predictions will be in original scales)

Note: Multiple independent outputs are allowed using columns of Y

# ${\bf GPy. models\_modules.gp\_multioutput\_regression\ module}$

```
 \textbf{class} \ \texttt{GPy.models\_modules.gp\_multioutput\_regression.} \textbf{GPMultioutputRegression} \ (X\_list, \\ Y\_list, \\ ker- \\ nel\_list=None, \\ noise\_variance\_list=None \\ nor- \\ mal- \\ ize\_X=False, \\ nor- \\ mal- \\ ize\_Y=False, \\ \end{aligned}
```

Bases: GPy.core.gp.GP

Multiple output Gaussian process with Gaussian noise

This is a wrapper around the models.GP class, with a set of sensible defaults

## **Parameters**

- X\_list (list of numpy arrays (num\_data\_output\_i x input\_dim), one array per output) input observations
- Y\_list (list of numpy arrays (num\_data\_output\_i x 1), one array per output) observed values
- **kernel\_list** (*list of GPy kernels*) GPy kernels, defaults to rbf
- **noise\_variance\_list** (*list of floats*) noise parameters per output, defaults to 1.0 for every output
- **normalize\_X** (*False*|*True*) whether to normalize the input data before computing (predictions will be in original scales)
- **normalize\_Y** (*False|True*) whether to normalize the input data before computing (predictions will be in original scales)
- rank (integer) number tuples of the corregionalization parameters 'coregion\_W' (see coregionalize kernel documentation)

# GPy.models\_modules.gp\_regression module

Bases: GPy.core.gp.GP

Gaussian Process model for regression

This is a thin wrapper around the models.GP class, with a set of sensible defaults

## **Parameters**

- **X** input observations
- Y observed values
- kernel a GPy kernel, defaults to rbf
- **normalize\_X** (*False|True*) whether to normalize the input data before computing (predictions will be in original scales)
- **normalize\_Y** (*False*|*True*) whether to normalize the input data before computing (predictions will be in original scales)

**Note:** Multiple independent outputs are allowed using columns of Y

```
getstate()
setstate(state)
```

# GPy.models\_modules.gplvm module

```
 \begin{aligned} \textbf{class} \; \texttt{GPy.models\_modules.gplvm.GPLVM} (\textit{Y}, \textit{input\_dim}, \textit{init='PCA'}, \textit{X=None}, \textit{kernel=None}, \textit{normal-ize\_Y=False}) \\ & \textit{Bases: GPy.core.gp.GP} \end{aligned}
```

Gaussian Process Latent Variable Model

# **Parameters**

• Y (np.ndarray) – observed data

```
• input_dim (int) – latent dimensionality
               • init ('pca'|'random') – initialisation method for the latent space
     getstate()
     jacobian(X)
     magnification(X)
     plot()
     plot_latent(*args, **kwargs)
     plot_magnification(*args, **kwargs)
     setstate (state)
GPy.models_modules.gplvm.initialise_latent(init, input_dim, Y)
GPy.models modules.gradient checker module
Created on 17 Jul 2013
@author: maxz
class GPy.models_modules.gradient_checker.GradientChecker(f, df, x0, names=None,
                                                                       *args, **kwargs)
     Bases: GPy.core.model.Model
     log_likelihood()
GPy.models_modules.gradient_checker.at_least_one_element(x)
GPy.models_modules.gradient_checker.flatten_if_needed(x)
GPy.models_modules.gradient_checker.get_shape(x)
GPy.models modules.mrd module
Created on 10 Apr 2013
@author: Max Zwiessele
class GPy.models_modules.mrd.MRD (likelihood_or_Y_list,
                                                               input dim,
                                                                              num inducing=10,
                                       names=None, kernels=None, initx='PCA', initz='permute',
                                       debug=False, **kw)
     Bases: GPy.core.model.Model
     Do MRD on given Datasets in Ylist. All Ys in likelihood_list are in [N x Dn], where Dn can be different per
     Yn, N must be shared across datasets though.
          Parameters
               • likelihood_list ([likelihood|ndarray]) - list of observed datasets (Gaussian if not
                 supplied directly)
               • names ([str]) – names for different gplvm models
               • input_dim (int) – latent dimensionality
               • initx (['concat'|'single'|'random']) – initialisation method for the latent space :
                 - 'concat' - pca on concatenation of all datasets
```

- 'single' Concatenation of pca on datasets, respectively
- 'random' Random draw from a normal
- initz ('permute' | 'random') initialisation method for inducing inputs
- X Initial latent space
- X variance Initial latent space variance
- **Z** initial inducing inputs
- num\_inducing number of inducing inputs to use
- **kernels** ([GPy.kern.kern] | GPy.kern.kern | None (default)) list of kernels or kernel shared for all BGPLVMS

```
Х
X_variance
auto scale factor
    set auto_scale_factor for all gplvms :param b: auto_scale_factor :type b:
getstate()
likelihood_list
log likelihood()
plot_X (fignum=None, ax=None)
plot_X_1d(*a, **kw)
plot_latent (fignum=None, ax=None, *args, **kwargs)
plot_predict (fignum=None, ax=None, sharex=False, sharey=False, **kwargs)
plot_scales (fignum=None, ax=None, titles=None, sharex=False, sharey=True, *args, **kwargs)
    TODO: Explain other parameters
        Parameters titles – titles for axes of datasets
propagate_param(**kwargs)
randomize (initx='concat', initz='permute', *args, **kw)
setstate(state)
update_likelihood_approximation()
```

# GPy.models modules.sparse gp classification module

```
 \textbf{class} \ \texttt{GPy.models\_modules.sparse\_gp\_classification.SparseGPClassification} \ (X, \\ Y=None, \\ like-\\ li-\\ hood=None, \\ ker-\\ nel=None, \\ nor-\\ mal-\\ ize\_X=False, \\ nor-\\ mal-\\ ize\_Y=False, \\ Z=None, \\ num\_inducing=10)
```

Bases: GPy.core.sparse\_gp.SparseGP

sparse Gaussian Process model for classification

This is a thin wrapper around the sparse\_GP class, with a set of sensible defaults

## **Parameters**

- **X** input observations
- Y observed values
- likelihood a GPy likelihood, defaults to Bernoulli with probit link\_function
- **kernel** a GPy kernel, defaults to rbf+white
- **normalize\_X** (*False*|*True*) whether to normalize the input data before computing (predictions will be in original scales)
- **normalize\_Y** (*False|True*) whether to normalize the input data before computing (predictions will be in original scales)

Return type model object

```
getstate()
setstate(state)
```

## GPy.models modules.sparse gp multioutput regression module

 ${\bf class} \; {\tt GPy.models\_modules.sparse\_gp\_multioutput\_regression. {\tt SparseGPMultioutputRegression} \; (X\_list, Y\_list) \\ {\tt V} \; list \\ {\tt V} \; list \\ {\tt SparseGPMultioutputRegression} \; (X\_list, Y\_list) \\ {\tt V} \; list \\ {\tt SparseGPMultioutputRegression} \; (X\_list, Y\_list) \\ {\tt V} \; list \\ {\tt SparseGPMultioutputRegression} \; (X\_list, Y\_list) \\ {\tt V} \; list \\ {\tt SparseGPMultioutputRegression} \; (X\_list, Y\_list) \\ {\tt SparseGPMultioutputRegression} \; (X\_list) \\ {\tt SparseGP$ 

kernel\_lis
noise\_
normalize\_X=
normalize\_Y=
Z list=

num\_ii rank=.

Bases: GPy.core.sparse\_gp.SparseGP

Sparse multiple output Gaussian process with Gaussian noise

This is a wrapper around the models. SparseGP class, with a set of sensible defaults

## **Parameters**

- **X\_list** (*list of numpy arrays* (*num\_data\_output\_i x input\_dim*), *one array per output*) input observations
- **Y\_list** (list of numpy arrays (num\_data\_output\_i x 1), one array per output) observed values
- **kernel\_list** (*list of GPy kernels*) GPy kernels, defaults to rbf
- noise\_variance\_list (list of floats) noise parameters per output, defaults to 1.0 for every output
- **normalize\_X** (*False*|*True*) whether to normalize the input data before computing (predictions will be in original scales)
- **normalize\_Y** (*False*|*True*) whether to normalize the input data before computing (predictions will be in original scales)
- **Z\_list** (list of numpy arrays (num\_inducing\_output\_i x input\_dim), one array per output | empty list) inducing inputs (optional)
- **num\_inducing** (*integer*) number of inducing inputs per output, defaults to 10 (ignored if Z\_list is not empty)
- rank (integer) number tuples of the corregionalization parameters 'coregion\_W' (see coregionalize kernel documentation)

## GPy.models modules.sparse gp regression module

Bases: GPy.core.sparse\_gp.SparseGP

Gaussian Process model for regression

This is a thin wrapper around the SparseGP class, with a set of sensible defalts

## **Parameters**

- **X** input observations
- Y observed values
- **kernel** a GPy kernel, defaults to rbf+white
- **normalize\_X** (*False|True*) whether to normalize the input data before computing (predictions will be in original scales)
- **normalize\_Y** (*False|True*) whether to normalize the input data before computing (predictions will be in original scales)
- **Z** (*np.ndarray* (*num\_inducing x input\_dim*) | *None*) inducing inputs (optional, see note)
- **X\_variance** (*np.ndarray* (*num\_data x input\_dim*) | *None*) The uncertainty in the measurements of X (Gaussian variance)

Return type model object

```
Note: Multiple independent outputs are allowed using columns of Y
```

```
getstate()
setstate(state)
```

# GPy.models\_modules.sparse\_gplvm module

Sparse Gaussian Process Latent Variable Model

# **Parameters**

- Y (np.ndarray) observed data
- **input dim** (*int*) latent dimensionality
- init ('PCA'|'random') initialisation method for the latent space

dL\_dX()

```
getstate()
     log_likelihood()
     plot()
     plot_latent(*args, **kwargs)
     setstate (state)
GPy.models_modules.svigp_regression module
class GPy.models_modules.svigp_regression.SVIGPRegression(X,
                                                                                              ker-
                                                                                          Z=None,
                                                                          nel=None,
                                                                         num_inducing=10,
                                                                          q u=None, batchsize=10,
                                                                         normalize_Y=False)
     Bases: GPy.core.svigp.SVIGP
     Gaussian Process model for regression
     This is a thin wrapper around the SVIGP class, with a set of sensible defalts
          Parameters
                • X – input observations
                • Y – observed values
                • kernel – a GPy kernel, defaults to rbf+white
                • normalize_X (False|True) – whether to normalize the input data before computing (predic-
                  tions will be in original scales)
                • normalize_Y (False|True) – whether to normalize the input data before computing (predic-
                  tions will be in original scales)
          Return type model object
     Note: Multiple independent outputs are allowed using columns of Y
     getstate()
     setstate (state)
GPy.models modules.warped gp module
class GPy.models_modules.warped_gp.WarpedGP(X, Y, kernel=None, warping_function=None,
                                                       warping_terms=3, normalize_X=False, normal-
```

```
transform_data()
    warping_function_gradients(Kiy)
Module contents
GPy.testing package
Submodules
GPy.testing.bcgplvm_tests module
class GPy.testing.bcgplvm_tests.BCGPLVMTests (methodName='runTest')
    Bases: unittest.case.TestCase
    test_kernel_backconstraint()
    test_linear_backconstraint()
    test_mlp_backconstraint()
GPy.testing.bgplvm_tests module
class GPy.testing.bgplvm_tests.BGPLVMTests (methodName='runTest')
    Bases: unittest.case.TestCase
    test_bias_kern()
    test_linear_bias_kern()
    test_linear_kern()
    test_rbf_bias_kern()
    test_rbf_kern()
    test_rbf_line_kern()
GPy.testing.cgd_tests module
Created on 26 Apr 2013
@author: maxz
class GPy.testing.cgd_tests.Test (methodName='runTest')
    Bases: unittest.case.TestCase
    testMinimizeSquare()
    testRosen()
GPy.testing.examples_tests module
class GPy.testing.examples_tests.ExamplesTests (methodName='runTest')
    Bases: unittest.case.TestCase
GPy.testing.examples_tests.flatten_nested(lst)
```

```
GPy.testing.examples_tests.model_checkgrads(model)
GPy.testing.examples_tests.model_instance(model)
GPy.testing.examples_tests.test_models()
GPy.testing.gp_transformation_tests module
class GPy.testing.gp_transformation_tests.TestTransformations
    Bases: object
    Generic transformations checker
    setUp()
    t_d2transf_df2 (transformation, f)
    t_d3transf_df3(transformation, f)
    t_dtransf_df(transformation, f)
    tearDown()
    test_transformations()
GPy.testing.gplvm_tests module
class GPy.testing.gplvm_tests.GPLVMTests (methodName='runTest')
    Bases: unittest.case.TestCase
    test_bias_kern()
    test_linear_kern()
    test_rbf_kern()
GPy.testing.kernel_tests module
class GPy.testing.kernel_tests.KernelTests (methodName='runTest')
    Bases: unittest.case.TestCase
    test_Matern32kernel()
    test_Matern52kernel()
    test_eq_sympykernel()
    test_fixedkernel()
        Fixed effect kernel test
    test_gibbskernel()
    test_heterokernel()
    test_kerneltie()
    test_linearkernel()
    test_mlpkernel()
    test_ode1_eqkernel()
    test_periodic_Matern32kernel()
```

```
test_periodic_Matern52kernel()
     test_periodic_exponentialkernel()
     test_polykernel()
     test_rational_quadratickernel()
     test_rbf_invkernel()
     test_rbf_sympykernel()
     test_rbfkernel()
GPy.testing.likelihood tests module
class GPy.testing.likelihood_tests.LaplaceTests (methodName='runTest')
     Bases: unittest.case.TestCase
     Specific likelihood tests, not general enough for the above tests
     setUp()
     tearDown()
     test_gaussian_d2logpdf_df2_2()
     test_laplace_log_likelihood()
class GPy.testing.likelihood_tests.TestNoiseModels
     Bases: object
     Generic model checker
     setUp()
     t d2logpdf2 df2 dparams (model, Y, f, params, param constraints)
     t_d2logpdf2_dlink2_dparams (model, Y, f, params, param_constraints)
     t_d2logpdf_df2 (model, Y, f)
     t_d2logpdf_dlink2 (model, Y, f, link_f_constraints)
     t_d3logpdf_df3 (model, Y, f)
     t_d3logpdf_dlink3 (model, Y, f, link_f_constraints)
     t_dlogpdf_df(model, Y, f)
     t_dlogpdf_df_dparams (model, Y, f, params, param_constraints)
     t_dlogpdf_dlink (model, Y, f, link_f_constraints)
     t_dlogpdf_dlink_dparams (model, Y, f, params, param_constraints)
     t_dlogpdf_dparams (model, Y, f, params, param_constraints)
     t_dlogpdf_link_dparams (model, Y, f, params, param_constraints)
     t_ep_fit_rbf_white (model, X, Y, f, step, param_vals, param_names, constraints)
     t_laplace_fit_rbf_white (model, X, Y, f, step, param_vals, param_names, constraints)
     t_logpdf(model, Y, f)
     tearDown()
```

```
test noise models()
GPy.testing.likelihood_tests.dparam_checkgrad(func,
                                                                   dfunc,
                                                                           params,
                                                                                      args,
                                                                                             con-
                                                            straints=None.
                                                                                 randomize=False,
                                                            verbose=False)
     checkgrad expects a f: R^N -> R^1 and df: R^N -> R^N However if we are holding other parameters fixed and
     moving something else We need to check the gradient of each of the fixed parameters (f and y for example)
     seperately, whilst moving another parameter. Otherwise f: gives back R^N and
          df: gives back R^NxM where M is
     The number of parameters and N is the number of data Need to take a slice out from f and a slice out of df
GPy.testing.likelihood_tests.dparam_partial(inst_func, *args)
     If we have a instance method that needs to be called but that doesn't take the parameter we wish to change to
     checkgrad, then this function will change the variable using set params.
     inst_func: should be a instance function of an object that we would like to change
     param: the param that will be given to set params args: anything else that needs to be given to the function (for
     example
          the f or Y that are being used in the function whilst we tweak the param
GPy.testing.mapping tests module
class GPy.testing.mapping_tests.MappingTests(methodName='runTest')
     Bases: unittest.case.TestCase
     test_kernelmapping()
     test_linearmapping()
     test_mlpmapping()
GPy.testing.mrd tests module
Created on 10 Apr 2013
@author: maxz
class GPy.testing.mrd_tests.MRDTests (methodName='runTest')
     Bases: unittest.case.TestCase
     test gradients()
GPy.testing.prior tests module
class GPy.testing.prior_tests.PriorTests (methodName='runTest')
     Bases: unittest.case.TestCase
```

test\_Gamma()

test\_lognormal()

test\_incompatibility()

# GPy.testing.psi\_stat\_expectation\_tests module

```
Created on 26 Apr 2013
@author: maxz
class GPy.testing.psi_stat_expectation_tests.Test (methodName='runTest')
                     Bases: unittest.case.TestCase
                     N = 300
                     Nsamples = 1000000.0
                     input_dim = 9
                     num_inducing = 13
                     setUp()
                     test_psi0()
                     test_psi1()
                     test_psi2()
GPy.testing.psi_stat_expectation_tests.ard(p)
GPy.testing.psi_stat_gradient_tests module
Created on 22 Apr 2013
@author: maxz
class GPy.testing.psi_stat_gradient_tests.DPsiStatTest (methodName='runTest')
                     Bases: unittest.case.TestCase
                    N = 50
                     x_{var} = array([0.85395518, 0.5, 0.9, 0.53474051, 0.80066698, 0.9, 0.5, 0.5, 0.67069375, 0.5, 0.5, 0.5, 0.5, 0.5627431, 0.5, 0.5, 0.5627431, 0.5, 0.5627431, 0.5, 0.5627431, 0.5, 0.5627431, 0.5627431, 0.5627431, 0.5627431, 0.5627431, 0.5627431, 0.5627431, 0.5627431, 0.5627431, 0.5627431, 0.5627431, 0.5627431, 0.5627431, 0.5627431, 0.5627431, 0.5627431, 0.5627431, 0.5627431, 0.5627431, 0.5627431, 0.5627431, 0.5627431, 0.5627431, 0.5627431, 0.5627431, 0.5627431, 0.5627431, 0.5627431, 0.5627431, 0.5627431, 0.5627431, 0.5627431, 0.5627431, 0.5627431, 0.5627431, 0.5627431, 0.5627431, 0.5627431, 0.5627431, 0.5627431, 0.5627431, 0.5627431, 0.5627431, 0.5627431, 0.5627431, 0.5627431, 0.5627431, 0.5627431, 0.5627431, 0.5627431, 0.5627431, 0.5627431, 0.5627431, 0.5627431, 0.5627431, 0.5627431, 0.5627431, 0.5627431, 0.5627431, 0.5627431, 0.5627431, 0.5627431, 0.5627431, 0.5627431, 0.5627431, 0.5627431, 0.5627431, 0.5627431, 0.5627431, 0.5627431, 0.5627431, 0.5627431, 0.5627431, 0.5627431, 0.5627431, 0.5627431, 0.5627431, 0.5627431, 0.5627431, 0.5627431, 0.5627431, 0.5627431, 0.5627431, 0.5627431, 0.5627431, 0.5627431, 0.5627431, 0.5627431, 0.5627431, 0.5627431, 0.5627431, 0.5627431, 0.5627431, 0.5627431, 0.5627431, 0.5627431, 0.5627431, 0.5627431, 0.5627431, 0.5627431, 0.5627431, 0.5627431, 0.5627431, 0.5627431, 0.5627431, 0.5627431, 0.5627431, 0.5627431, 0.5627431, 0.5627431, 0.5627431, 0.5627431, 0.5627431, 0.5627431, 0.5627431, 0.5627431, 0.5627431, 0.5627431, 0.5627431, 0.5627431, 0.5627431, 0.5627431, 0.5627431, 0.5627431, 0.5627431, 0.5627431, 0.5627431, 0.5627431, 0.5627431, 0.5627431, 0.5627431, 0.5627431, 0.5627431, 0.5627431, 0.56274410, 0.5627441, 0.5627441, 0.5627441, 0.5627441, 0.5627441, 0.5627441, 0.5627441, 0.5627441, 0.5627441, 0.5627441, 0.5627441, 0.5627441, 0.5627441, 0.5627441, 0.5627441, 0.5627441, 0.5627441, 0.5627441, 0.5627441, 0.5627441, 0.5627441, 0.5627441, 0.5627441, 0.5627441, 0.5627441, 0.5627441, 0.5627441, 0.5627441, 0.5627441, 0.5627441, 0.5627441, 0.5627441, 0.5627441, 0.5627441, 0.562
                     Y = array([[-2.20747097e+00, -5.73524833e-01, 7.73270442e-01, -3.29475962e+00, 3.30574015e+00, -6.65849736e-01, 2.6648e-01, -6.65849736e-01, -6.6584976e-01, -6.6584976e-01, -6.6584976e-01, -6.6584976e-01, -6.6584976e-01, -6.6584976e-01, -6.6584976e-01, -6.658496e-01, -6.658496e-01, -6.658496e-01, -6.658496e-01, -6.6584966e-01, -6.658496e-01, -6.6584966e-01, -6.658496e-01, -6.658496e-01, -6.658496e-01, -6.658496e-01, -6.658496e-01, -6.658496e-01, -6.658496e-01, -6.65866e-01, -6.65866e-01, -6.65866e-01, -6.65866e-01, -6.65866e-01, -6.65866e
                     z = array([[0.05342464, -0.85023395, 1.16623315, -0.43332385, -0.72547002, -1.56199585, 0.007915, -1.04764369, -0.51913])
                     input_dim = 20
                     kernels = [<GPy.kern.kern.kern object at 0x7f37ab632a50>, <GPy.kern.kern.kern object at 0x7f37ab632bd0>, <GPy.ke
                     num_inducing = 10
                     testPsi0()
                     testPsi1()
                     testPsi2_bia()
                     testPsi2_lin()
                     testPsi2_lin_bia()
                     testPsi2_rbf()
                     testPsi2_rbf_bia()
```

```
class GPy.testing.psi_stat_gradient_tests.PsiStatModel(which, X, X_variance,
                                                                                       Z
                                                               num inducing, kernel)
     Bases: GPy.core.model.Model
     log_likelihood()
GPy.testing.sparse_gplvm_tests module
class GPy.testing.sparse_gplvm_tests.sparse_GPLVMTests (methodName='runTest')
     Bases: unittest.case.TestCase
     test_bias_kern()
     test_linear_kern()
     test_rbf_kern()
GPy.testing.unit_tests module
class GPy.testing.unit_tests.GradientTests (methodName='runTest')
     Bases: unittest.case.TestCase
     check_model (kern, model_type='GPRegression', dimension=1, uncertain_inputs=False)
     multioutput_regression_1D()
     multioutput_sparse_regression_1D()
     setUp()
     test_GPLVM_rbf_bias_white_kern_2D()
         Testing GPLVM with rbf + bias kernel
     test_GPLVM_rbf_linear_white_kern_2D()
         Testing GPLVM with rbf + bias kernel
     test_GPRegression_bias_kern_1D()
         Testing the GP regression with bias kernel on 1d data
     test_GPRegression_bias_kern_2D()
         Testing the GP regression with bias kernel on 2d data
     test_GPRegression_exponential_1D()
         Testing the GP regression with exponential kernel on 1d data
     test_GPRegression_exponential_2D()
         Testing the GP regression with exponential kernel on 2d data
     test_GPRegression_exponential_ARD_2D()
         Testing the GP regression with exponential kernel on 2d data
     test_GPRegression_linear_kern_1D()
         Testing the GP regression with linear kernel on 1d data
     test_GPRegression_linear_kern_1D_ARD()
         Testing the GP regression with linear kernel on 1d data
     test_GPRegression_linear_kern_2D()
         Testing the GP regression with linear kernel on 2d data
     test_GPRegression_linear_kern_2D_ARD()
         Testing the GP regression with linear kernel on 2d data
```

```
test GPRegression matern32 1D()
          Testing the GP regression with matern32 kernel on 1d data
     test_GPRegression_matern32_2D()
          Testing the GP regression with matern32 kernel on 2d data
     test GPRegression matern32 ARD 2D()
          Testing the GP regression with matern32 kernel on 2d data
     test GPRegression matern52 1D()
          Testing the GP regression with matern52 kernel on 1d data
     test_GPRegression_matern52_2D()
          Testing the GP regression with matern52 kernel on 2d data
     test_GPRegression_matern52_ARD_2D()
          Testing the GP regression with matern52 kernel on 2d data
     test_GPRegression_mlp_1d()
          Testing the GP regression with mlp kernel with white kernel on 1d data
     test GPRegression poly 1d()
          Testing the GP regression with polynomial kernel with white kernel on 1d data
     test_GPRegression_rbf_1d()
          Testing the GP regression with rbf kernel with white kernel on 1d data
     test GPRegression rbf 2D()
          Testing the GP regression with rbf kernel on 2d data
     test_GPRegression_rbf_ARD_2D()
          Testing the GP regression with rbf kernel on 2d data
     test_GP_EP_probit()
     test_SparseGPRegression_rbf_linear_white_kern_1D()
          Testing the sparse GP regression with rbf kernel on 2d data
     test_SparseGPRegression_rbf_linear_white_kern_1D_uncertain_inputs()
          Testing the sparse GP regression with rbf, linear kernel on 1d data with uncertain inputs
     test_SparseGPRegression_rbf_linear_white_kern_2D()
          Testing the sparse GP regression with rbf kernel on 2d data
     test_SparseGPRegression_rbf_linear_white_kern_2D_uncertain_inputs()
          Testing the sparse GP regression with rbf, linear kernel on 2d data with uncertain inputs
     test_SparseGPRegression_rbf_white_kern_1d()
          Testing the sparse GP regression with rbf kernel with white kernel on 1d data
     test_SparseGPRegression_rbf_white_kern_2D()
          Testing the sparse GP regression with rbf kernel on 2d data
     test_generalized_FITC()
     test_sparse_EP_DTC_probit()
Module contents
```

# MaxZ

GPy.testing.deepTest (reason)

```
GPy.util package
Subpackages
GPy.util.latent_space_visualizations package
Subpackages
GPy.util.latent_space_visualizations.controllers package
Submodules
GPy.util.latent_space_visualizations.controllers.axis_event_controller module Created on 24 Jul 2013
@author: maxz
class GPy.util.latent_space_visualizations.controllers.axis_event_controller.AxisChangedContr
                Bases: GPy.util.latent_space_visualizations.controllers.axis_event_controller.AxisEventController.AxisEventControllers.axis_event_controller.AxisEventControllers.axis_event_controllers.axis_event_controllers.axis_event_controllers.axis_event_controllers.axis_event_controllers.axis_event_controllers.axis_event_controllers.axis_event_controllers.axis_event_controllers.axis_event_controllers.axis_event_controllers.axis_event_controllers.axis_event_controllers.axis_event_controllers.axis_event_controllers.axis_event_controllers.axis_event_controllers.axis_event_controllers.axis_event_controllers.axis_event_controllers.axis_event_controllers.axis_event_controllers.axis_event_controllers.axis_event_controllers.axis_event_controllers.axis_event_controllers.axis_event_controllers.axis_event_controllers.axis_event_controllers.axis_event_controllers.axis_event_controllers.axis_event_controllers.axis_event_controllers.axis_event_controllers.axis_event_controllers.axis_event_controllers.axis_event_controllers.axis_event_controllers.axis_event_controllers.axis_event_controllers.axis_event_controllers.axis_event_controllers.axis_event_controllers.axis_event_controllers.axis_event_controllers.axis_event_controllers.axis_event_controllers.axis_event_controllers.axis_event_controllers.axis_event_controllers.axis_event_controllers.axis_event_controllers.axis_event_controllers.axis_event_controllers.axis_event_controllers.axis_event_controllers.axis_event_controllers.axis_event_controllers.axis_event_controllers.axis_event_controllers.axis_event_controllers.axis_event_controllers.axis_event_controllers.axis_event_controllers.axis_event_controllers.axis_event_controllers.axis_event_controllers.axis_event_controllers.axis_event_controllers.axis_event_controllers.axis_event_controllers.axis_event_controllers.axis_event_controllers.axis_event_controllers.axis_event_controllers.axis_event_controllers.axis_event_controllers.axis_event_controllers.axis_event_controllers.axis_event_controllers.axis_event_controllers.axis_event_controller
                Buffered control of axis limit changes
                extent (lim)
                lim_changed(axlim, savedlim)
                update (ax)
                xlim_changed(ax)
                ylim_changed(ax)
class GPy.util.latent_space_visualizations.controllers.axis_event_controller.AxisEventControl
                Bases: object
                activate()
                deactivate()
                xlim_changed(ax)
                ylim_changed(ax)
class GPy.util.latent_space_visualizations.controllers.axis_event_controller.BufferedAxisChar
```

```
\textbf{Bases:} \ \texttt{GPy.util.latent\_space\_visualizations.controllers.axis\_event\_controller.AxisChanged and the action of the action
```

get\_grid()

```
recompute_X()
    update (ax)
    update_view (view, X, xmin, xmax, ymin, ymax)
GPy.util.latent_space_visualizations.controllers.imshow_controller module Created on 24 Jul 2013
@author: maxz
class GPy.util.latent_space_visualizations.controllers.imshow_controller.ImAnnotateController
    Bases: GPy.util.latent_space_visualizations.controllers.imshow_controller.ImshowController
    update_view (view, X, xmin, xmax, ymin, ymax)
class GPy.util.latent_space_visualizations.controllers.imshow_controller.ImshowController(ax,
                                                                                                     plot
                                                                                                     plot
                                                                                                     res-
                                                                                                     lu-
                                                                                                     tion
                                                                                                     ир-
                                                                                                     date
    Bases: GPy.util.latent_space_visualizations.controllers.axis_event_controller.BufferedAx.
    update_view (view, X, xmin, xmax, ymin, ymax)
Module contents
Module contents
Submodules
GPy.util.Tango module
GPy.util.Tango.currentDark()
GPy.util.Tango.currentLight()
GPy.util.Tango.currentMedium()
GPy.util.Tango.fewerXticks(ax=None, divideby=2)
```

GPy.util.Tango.hex2rgb(hexcolor)

```
GPy.util.Tango.nextDark()
GPy.util.Tango.nextLight()
GPy.util.Tango.nextMedium()
GPy.util.Tango.removeRightTicks(ax=None)
GPy.util.Tango.removeUpperTicks(ax=None)
GPy.util.Tango.reset()
GPy.util.Tango.setDarkFigures()
GPy.util.Tango.setLightFigures()
GPy.util.block_matrices module
GPy.util.block_matrices.get_blocks(A, blocksizes)
```

## GPy.util.classification module

GPy.util.classification.conf\_matrix (p, labels, names=['1', '0'], threshold=0.5, show=True)
Returns error rate and true/false positives in a binary classification problem - Actual classes are displayed by column. - Predicted classes are displayed by row.

## **Parameters**

- **p** array of class '1' probabilities.
- labels array of actual classes.
- names list of class names, defaults to ['1','0'].
- **threshold** probability value used to decide the class.
- **show** (*False*|*True*) whether the matrix should be shown or not

# GPy.util.config module

# GPy.util.datasets module

```
GPy.util.datasets.authorize_download(dataset_name=None)
     Check with the user that the are happy with terms and conditions for the data set.
GPy.util.datasets.boston_housing(data_set='boston_housing')
GPy.util.datasets.brendan_faces (data_set='brendan_faces')
                                                             test_motions=[],
                                                                                sample\_every=4,
GPy.util.datasets.cmu_mocap(subject,
                                             train_motions,
                                    data_set='cmu_mocap')
     Load a given subject's training and test motions from the CMU motion capture data.
GPy.util.datasets.cmu_mocap_35_walk_jog(data_set='cmu_mocap')
     Load CMU subject 35's walking and jogging motions, the same data that was used by Taylor, Roweis and Hinton
     at NIPS 2007. but without their preprocessing. Also used by Lawrence at AISTATS 2007.
GPy.util.datasets.cmu_mocap_49_balance(data_set='cmu_mocap')
     Load CMU subject 49's one legged balancing motion that was used by Alvarez, Luengo and Lawrence at
     AISTATS 2009.
```

```
GPy.util.datasets.cmu_urls_files(subj_motions, messages=True)
     Find which resources are missing on the local disk for the requested CMU motion capture motions.
GPy.util.datasets.creep_data(data_set='creep_rupture')
     Brun and Yoshida's metal creep rupture data.
GPy.util.datasets.crescent data(num data=200, seed=10000)
     Data set formed from a mixture of four Gaussians. In each class two of the Gaussians are elongated at right
     angles to each other and offset to form an approximation to the crescent data that is popular in semi-supervised
     learning as a toy problem.
             param num_data_part number of data to be sampled (default is 200).
             type num_data int
             param seed random seed to be used for data generation.
             type seed int
GPy.util.datasets.data_available(dataset_name=None)
     Check if the data set is available on the local machine already.
GPy.util.datasets.data_details_return(data, data_set)
     Update the data component of the data dictionary with details drawn from the data resources.
GPy.util.datasets.della_gatta_TRP63_gene_expression(data_set='della_gatta',
                                                                 gene_number=None)
GPy.util.datasets.download_data(dataset_name=None)
     Check with the user that the are happy with terms and conditions for the data set, then download it.
GPy.util.datasets.download_rogers_girolami_data(data_set='rogers_girolami_data')
GPy.util.datasets.download_url(url, store_directory, save_name=None, messages=True, suf-
     Download a file from a url and save it to disk.
GPy.util.datasets.hapmap3(data_set='hapmap3')
GPy.util.datasets.isomap_faces(num_samples=698, data_set='isomap_face_data')
GPy.util.datasets.oil (data_set='three_phase_oil_flow')
     The three phase oil data from Bishop and James (1993).
GPy.util.datasets.oil_100 (seed=10000, data_set='three_phase_oil_flow')
GPy.util.datasets.olivetti_faces (data_set='olivetti_faces')
GPy.util.datasets.olympic_100m_men(data_set='rogers_girolami_data')
GPy.util.datasets.olympic_100m_women(data_set='rogers_girolami_data')
GPy.util.datasets.olympic_200m_men(data_set='rogers_girolami_data')
GPy.util.datasets.olympic_200m_women(data_set='rogers_girolami_data')
GPy.util.datasets.olympic 400m men(data set='rogers girolami data')
GPy.util.datasets.olympic_400m_women(data_set='rogers_girolami_data')
GPy.util.datasets.olympic_marathon_men(data_set='olympic_marathon_men')
GPy.util.datasets.olympic_sprints(data_set='rogers_girolami_data')
     All olympics sprint winning times for multiple output prediction.
GPy.util.datasets.osu_run1(data_set='osu_run1', sample_every=4)
```

```
GPy.util.datasets.prompt_user(prompt)
    Ask user for agreeing to data set licenses.
GPy.util.datasets.pumadyn(seed=10000, data_set='pumadyn-32nm')
GPy.util.datasets.reporthook (a, b, c)
GPy.util.datasets.ripley_synth(data_set='ripley_prnn_data')
GPy.util.datasets.robot_wireless(data_set='robot_wireless')
GPy.util.datasets.sample_class(f)
GPy.util.datasets.silhouette(data_set='ankur_pose_data')
GPy.util.datasets.simulation_BGPLVM()
GPy.util.datasets.swiss_roll(num_samples=3000, data_set='swiss_roll')
GPy.util.datasets.swiss_roll_1000()
GPy.util.datasets.swiss_roll_generated(num_samples=1000, sigma=0.0)
GPy.util.datasets.toy linear 1d classification (seed=10000)
GPy.util.datasets.toy_rbf_1d(seed=10000, num_samples=500)
    Samples values of a function from an RBF covariance with very small noise for inputs uniformly distributed
    between -1 and 1.
```

## **Parameters**

- **seed** (*int*) seed to use for random sampling.
- **num\_samples** (*int*) number of samples to sample in the function (default 500).

```
GPy.util.datasets.toy_rbf_1d_50 (seed=10000)
GPy.util.datasets.xw_pen (data_set='xw_pen')
```

# GPy.util.decorators module

```
GPy.util.decorators.silence_errors(f)
```

This wraps a function and it silences numpy errors that happen during the execution. After the function has exited, it restores the previous state of the warnings.

## GPy.util.diag module

```
GPy.util.diag.add (A, b, offset=0)
```

Add b to the view of A in place (!). Returns modified A. Broadcasting is allowed, thus b can be scalar.

if offset is not zero, make sure b is of right shape!

# **Parameters**

- A (*ndarray*) 2 dimensional array
- **b** (*ndarray-like*) either one dimensional or scalar
- **offset** (*int*) same as in view.

**Return type** view of A, which is adjusted inplace

## GPy.util.diag.**divide** (A, b, offset=0)

Divide the view of A by b in place (!). Returns modified A Broadcasting is allowed, thus b can be scalar.

if offset is not zero, make sure b is of right shape!

#### **Parameters**

- A (*ndarray*) 2 dimensional array
- **b** (*ndarray-like*) either one dimensional or scalar
- **offset** (*int*) same as in view.

**Return type** view of A, which is adjusted inplace

## GPy.util.diag.**multiply** (A, b, offset=0)

Times the view of A with b in place (!). Returns modified A Broadcasting is allowed, thus b can be scalar.

if offset is not zero, make sure b is of right shape!

## **Parameters**

- A (ndarray) 2 dimensional array
- **b** (*ndarray-like*) either one dimensional or scalar
- **offset** (*int*) same as in view.

**Return type** view of A, which is adjusted inplace

# GPy.util.diag.**subtract**(*A*, *b*, offset=0)

Subtract b from the view of A in place (!). Returns modified A. Broadcasting is allowed, thus b can be scalar.

if offset is not zero, make sure b is of right shape!

# **Parameters**

- A (*ndarray*) 2 dimensional array
- **b** (*ndarray-like*) either one dimensional or scalar
- **offset** (*int*) same as in view.

**Return type** view of A, which is adjusted inplace

# GPy.util.diag.times (A, b, offset=0)

Times the view of A with b in place (!). Returns modified A Broadcasting is allowed, thus b can be scalar.

if offset is not zero, make sure b is of right shape!

## **Parameters**

- A (*ndarray*) 2 dimensional array
- **b** (*ndarray-like*) either one dimensional or scalar
- **offset** (*int*) same as in view.

Return type view of A, which is adjusted inplace

## GPy.util.diag.view (A, offset=0)

Get a view on the diagonal elements of a 2D array.

This is actually a view (!) on the diagonal of the array, so you can in-place adjust the view.

:param ndarray A: 2 dimensional numpy array :param int offset: view offset to give back (negative entries allowed) :rtype: ndarray view of diag(A)

```
>>> import numpy as np
     >>> X = np.arange(9).reshape(3,3)
     >>> view(X)
     array([0, 4, 8])
     >>> d = view(X)
     >>> d += 2
     >>> view(X)
     array([ 2, 6, 10])
     >>> view(X, offset=-1)
     array([3, 7])
     >>> subtract(X, 3, offset=-1)
     array([[ 2, 1, 2],
             [ 0, 6, 5],
             [ 6, 4, 10]])
GPy.util.erfcx module
GPy.util.erfcx.erfcx(arg)
GPy.util.linalg module
GPy.util.linalg.DSYR(*args, **kwargs)
GPy.util.linalg.DSYR_blas (A, x, alpha=1.0)
     Performs a symmetric rank-1 update operation: A \leftarrow A + alpha * np.dot(x,x.T)
          Parameters
                • A – Symmetric NxN np.array
               • x - Nx1 np.array
               • alpha – scalar
GPy.util.linalg.DSYR_numpy (A, x, alpha=1.0)
     Performs a symmetric rank-1 update operation: A \leftarrow A + alpha * np.dot(x,x.T)
          Parameters
                • A – Symmetric NxN np.array
                • x − Nx1 np.array
               • alpha - scalar
GPy.util.linalg.backsub both sides (L, X, transpose='left')
     Return L^-T * X * L^-1, assumuing X is symmetrical and L is lower cholesky
GPy.util.linalg.chol_inv(L)
     Inverts a Cholesky lower triangular matrix
          Parameters L – lower triangular matrix
          Return type inverse of L
```

GPy.util.linalg.cholupdate (L, x) update the LOWER cholesky factor of a pd matrix IN PLACE

if L is the lower chol. of K, then this function computes  $L_{-}$  where  $L_{-}$  is the lower chol of  $K + x*x^{T}$ 

```
GPy.util.linalg.dpotri(A, lower=0)
```

Wrapper for lapack dpotri function

## **Parameters**

- A Matrix A
- lower is matrix lower (true) or upper (false)

## Returns A inverse

GPy.util.linalg.dpotrs(A, B, lower=0)

Wrapper for lapack dpotrs function

## **Parameters**

- A Matrix A
- B Matrix B
- lower is matrix lower (true) or upper (false)

## Returns

GPy.util.linalg.dtrtrs(A, B, lower=0, trans=0, unitdiag=0)

Wrapper for lapack dtrtrs function

## **Parameters**

- A Matrix A
- **B** Matrix B
- lower is matrix lower (true) or upper (false)

# Returns

```
GPy.util.linalg.jitchol(A, maxtries=5)
```

GPy.util.linalg.jitchol\_old(A, maxtries=5)

**Parameters** A – An almost pd square matrix

Rval L the Cholesky decomposition of A

GPy.util.linalg.mdot(\*args)

Multiply all the arguments using matrix product rules. The output is equivalent to multiplying the arguments one by one from left to right using dot(). Precedence can be controlled by creating tuples of arguments, for instance mdot(a,((b,c),d)) multiplies a  $(a^*((b^*c)^*d))$ . Note that this means the output of dot(a,b) and mdot(a,b) will differ if a or b is a pure tuple of numbers.

GPy.util.linalg.multiple\_pdinv(A)

**Parameters** A – A DxDxN numpy array (each A[:,:,i] is pd)

**Rval invs** the inverses of A

Rtype invs np.ndarray

**Rval hld** 0.5\* the log of the determinants of A

**Rtype hld** np.array

GPy.util.linalg.pca(Y, input\_dim)

Principal component analysis: maximum likelihood solution by SVD

## **Parameters**

• **Y** – NxD np.array of data

• input\_dim – int, dimension of projection

#### Rval X

• Nxinput\_dim np.array of dimensionality reduced data

## Rval W

• input dimxD mapping from X to Y

GPy.util.linalg.pddet(A)

Determinant of a positive definite matrix, only symmetric matricies though

GPy.util.linalg.pdinv(A, \*args)

**Parameters** A - A DxD pd numpy array

**Rval Ai** the inverse of A

Rtype Ai np.ndarray

Rval L the Cholesky decomposition of A

Rtype L np.ndarray

Rval Li the Cholesky decomposition of Ai

Rtype Li np.ndarray

**Rval logdet** the log of the determinant of A

Rtype logdet float64

GPy.util.linalg.ppca(Y, Q, iterations=100)

EM implementation for probabilistic pca.

# **Parameters**

- Y (array-like) Observed Data
- **Q** (*int*) Dimensionality for reduced array
- iterations (int) number of iterations for EM

## GPy.util.linalq.ppca\_missinq\_data\_at\_random(Y, Q, iters=100)

EM implementation of Probabilistic pca for when there is missing data.

Taken from <SheffieldML, https://github.com/SheffieldML>

**Returns** X, W, sigma^2

GPy.util.linalg.symmetrify(A, upper=False)

Take the square matrix A and make it symmetrical by copting elements from the lower half to the upper works IN PLACE.

```
GPy.util.linalg.symmetrify_murray(A)
```

GPy.util.linalg.tdot(\*args, \*\*kwargs)

GPy.util.linalg.tdot\_blas(mat, out=None)

returns np.dot(mat, mat.T), but faster for large 2D arrays of doubles.

GPy.util.linalg.tdot\_numpy (mat, out=None)

GPy.util.linalg.trace\_dot(a, b)

Efficiently compute the trace of the matrix product of a and b

#### GPy.util.In diff erfs module

GPy.util.ln\_diff\_erfs.ln\_diff\_erfs (x1, x2, return\_sign=False)

Function for stably computing the log of difference of two erfs in a numerically stable manner. :param x1: argument of the positive erf :type x1: ndarray :param x2: argument of the negative erf :type x2: ndarray :return: tuple containing (log(abs(erf(x1) - erf(x2))), sign(erf(x1) - erf(x2)))

Based on MATLAB code that was written by Antti Honkela and modified by David Luengo and originally derived from code by Neil Lawrence.

#### GPy.util.misc module

GPy.util.misc.chain\_1 ( $df_dg$ ,  $dg_dx$ )

Generic chaining function for first derivative

$$\frac{d(f.g)}{dx} = \frac{df}{dg}\frac{dg}{dx}$$

GPy.util.misc.chain\_2 ( $d2f_dg2$ ,  $dg_dx$ ,  $df_dg$ ,  $d2g_dx2$ )

Generic chaining function for second derivative

$$\frac{d^2(f.g)}{dx^2} = \frac{d^2f}{dg^2} \left(\frac{dg}{dx}\right)^2 + \frac{df}{dg} \frac{d^2g}{dx^2}$$

GPy.util.misc.chain\_3 (d3f\_dg3, dg\_dx, d2f\_dg2, d2g\_dx2, df\_dg, d3g\_dx3)

Generic chaining function for third derivative

$$\frac{d^{3}(f.g)}{dx^{3}} = \frac{d^{3}f}{dg^{3}} \left(\frac{dg}{dx}\right)^{3} + 3\frac{d^{2}f}{dg^{2}}\frac{dg}{dx}\frac{d^{2}g}{dx^{2}} + \frac{df}{dg}\frac{d^{3}g}{dx^{3}}$$

GPy.util.misc.fast\_array\_equal(A, B)

GPy.util.misc.fast\_array\_equal2(A, B)

GPy.util.misc.kmm\_init(X, m=10)

This is the same initialization algorithm that is used in Kmeans++. It's quite simple and very useful to initialize the locations of the inducing points in sparse GPs.

#### **Parameters**

- **X** data
- m number of inducing points

GPy.util.misc.linear\_grid(D, n=100,  $min_max=(-100, 100)$ )

Creates a D-dimensional grid of n linearly spaced points

#### **Parameters**

- **D** dimension of the grid
- **n** number of points
- min\_max (min, max) list

GPy.util.misc.opt\_wrapper(m, \*\*kwargs)

This function just wraps the optimization procedure of a GPy object so that optimize() pickleable (necessary for multiprocessing).

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#### GPy.util.mocap module

# class GPy.util.mocap.acclaim\_skeleton(file\_name=None) Bases: GPy.util.mocap.skeleton get\_child\_xyz (ind, channels) load\_channels (file\_name) load\_skel (file\_name) Loads an ASF file into a skeleton structure. **Parameters file name** – The file name to load in. $read\_bonedata(fid)$ Read bone data from an acclaim skeleton file stream. read channels (fid) Read channels from an acclaim file. read\_documentation(fid) Read documentation from an acclaim skeleton file stream. read\_hierarchy(fid) Read hierarchy information from acclaim skeleton file stream. read\_line(fid) Read a line from a file string and check it isn't either empty or commented before returning. read root (fid) Read the root node from an acclaim skeleton file stream. read skel(fid) Loads an acclaim skeleton format from a file stream. read units (fid) Read units from an acclaim skeleton file stream. resolve indices (index, start val) Get indices for the skeleton from the channels when loading in channel data. set\_rotation\_matrices() Set the meta information at each vertex to contain the correct matrices C and Cinv as prescribed by the rotations and rotation orders. to\_xyz (channels) GPy.util.mocap.load\_text\_data (dataset, directory, centre=True) Load in a data set of marker points from the Ohio State University C3D motion capture files (http://accad.osu.edu/research/mocap/mocap\_data.htm). GPy.util.mocap.parse text(file name) Parse data from Ohio State University text mocap files (http://accad.osu.edu/research/mocap/mocap\_data.htm). GPy.util.mocap.read\_connections (file\_name, point\_names) Read a file detailing which markers should be connected to which for motion capture data.

### **Parameters**

• **xangle** – rotation for x-axis.

matrix for a given set of angles in a given order.

GPy.util.mocap.rotation\_matrix(xangle, yangle, zangle, order='zxy', degrees=False)

Compute the rotation matrix for an angle in each direction. This is a helper function for computing the rotation

- yangle rotation for y-axis.
- **zangle** rotation for z-axis.
- **order** the order for the rotations.

#### class GPy.util.mocap.skeleton

```
Bases: GPy.util.mocap.tree
```

#### connection\_matrix()

#### finalize()

After loading in a skeleton ensure parents are correct, vertex orders are correct and rotation matrices are correct.

#### smooth\_angle\_channels (channels)

Remove discontinuities in angle channels so that they don't cause artifacts in algorithms that rely on the smoothness of the functions.

#### to\_xyz (channels)

```
class GPy.util.mocap.tree
```

```
branch_str (index, indent='')
```

#### find children()

Take a tree and set the children according to the parents.

Takes a tree structure which lists the parents of each vertex and computes the children for each vertex and places them in.

## find\_parents()

Take a tree and set the parents according to the children

Takes a tree structure which lists the children of each vertex and computes the parents for each vertex and places them in.

#### find\_root()

Finds the index of the root node of the tree.

#### get\_index\_by\_id(id)

Give the index associated with a given vertex id.

#### get index by name(name)

Give the index associated with a given vertex name.

#### order\_vertices()

Order vertices in the graph such that parents always have a lower index than children.

#### $swap\_vertices(i, j)$

Swap two vertices in the tree structure array. swap\_vertex swaps the location of two vertices in a tree structure array.

#### **Parameters**

- tree the tree for which two vertices are to be swapped.
- $\mathbf{i}$  the index of the first vertex to be swapped.
- $\mathbf{j}$  the index of the second vertex to be swapped.

Rval tree the tree structure with the two vertex locations swapped.

```
class GPy.util.mocap.vertex(name, id, parents=[], children=[], meta={})
```

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#### GPy.util.multioutput module

```
GPy.util.multioutput.build_lcm(input_dim, num_outputs, CK=[], NC=[], W\_columns=1, W=None, kappa=None)
```

Builds a kernel for a linear coregionalization model

Input\_dim Input dimensionality

Num\_outputs Number of outputs

#### **Parameters**

- **CK** List of coregionalized kernels (i.e., this will be multiplied by a coregionalize kernel).
- K List of kernels that will be added up together with CK, but won't be multiplied by a
  coregionalize kernel
- W\_columns (integer) number tuples of the corregionalization parameters 'coregion\_W'

## GPy.util.netpbmfile module

Read and write image data from respectively to Netpbm files.

This implementation follows the Netpbm format specifications at http://netpbm.sourceforge.net/doc/. No gamma correction is performed.

The following image formats are supported: PBM (bi-level), PGM (grayscale), PPM (color), PAM (arbitrary), XV thumbnail (RGB332, read-only).

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**Version** 2013.01.18

#### Requirements

- CPython 2.7, 3.2 or 3.3
- Numpy 1.7
- Matplotlib 1.2 (optional for plotting)

#### **Examples**

```
>>> im1 = numpy.array([[0, 1], [65534, 65535]], dtype=numpy.uint16)
>>> imsave('_tmp.pgm', im1)
>>> im2 = imread('_tmp.pgm')
>>> assert numpy.all(im1 == im2)

GPy.util.netpbmfile.imread(filename, *args, **kwargs)
    Return image data from Netpbm file as numpy array.
    args and kwargs are arguments to NetpbmFile.asarray().
>>> image = imread('_tmp.pgm')

GPy.util.netpbmfile.imsave(filename, data, maxval=None, pam=False)
    Write image data to Netpbm file.
```

```
>>> image = numpy.array([[0, 1],[65534, 65535]], dtype=numpy.uint16)
     >>> imsave('_tmp.pgm', image)
class GPy.util.netpbmfile.NetpbmFile (arg=None, **kwargs)
     Bases: object
     Read and write Netpbm PAM, PBM, PGM, PPM, files.
     asarray (copy=True, cache=False, **kwargs)
          Return image data from file as numpy array.
     close()
          Close open file. Future asarray calls might fail.
     write(arg, **kwargs)
          Write instance to file.
GPy.util.plot module
GPy.util.plot.align_subplot_array (axes, xlim=None, ylim=None)
     make all of the axes in the array hae the same limits, turn off unnecessary ticks
     use pb.subplots() to get an array of axes
GPy.util.plot.align_subplots(N, M, xlim=None, ylim=None)
     make all of the subplots have the same limits, turn off unnecessary ticks
GPy.util.plot.fewerXticks (ax=None, divideby=2)
GPy.util.plot.gpplot(x, mu, lower, upper, edgecol='#204a87', fillcol='#729fcf', axes=None,
                           **kwargs)
GPy.util.plot.removeRightTicks(ax=None)
GPy.util.plot.removeUpperTicks(ax=None)
GPy.util.plot.x_frame1D(X, plot_limits=None, resolution=None)
     Internal helper function for making plots, returns a set of input values to plot as well as lower and upper limits
GPy.util.plot.x_frame2D(X, plot_limits=None, resolution=None)
     Internal helper function for making plots, returns a set of input values to plot as well as lower and upper limits
GPy.util.plot latent module
GPy.util.plot_latent.most_significant_input_dimensions (model, which_indices)
GPy.util.plot_latent.plot_latent (model,
                                                   labels=None,
                                                                   which_indices=None,
                                                                                         resolu-
                                          tion=50, ax=None, marker='o', s=40, fignum=None,
```

```
plot inducing=False, legend=True, aspect='auto', up-
dates = False)
```

#### **Parameters**

- labels a np.array of size model.num\_data containing labels for the points (can be number, strings, etc)
- resolution the resolution of the grid on which to evaluate the predictive variance

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```
GPy.util.plot_latent.plot_magnification (model, labels=None, which_indices=None, resolution=60, ax=None, marker='o', s=40, fignum=None, plot_inducing=False, legend=True, aspect='auto', updates=False)
```

#### **Parameters**

- **labels** a np.array of size model.num\_data containing labels for the points (can be number, strings, etc)
- resolution the resolution of the grid on which to evaluate the predictive variance

#### GPy.util.squashers module

```
GPy.util.squashers.sigmoid(x)
GPy.util.squashers.single_softmax(x)
GPy.util.squashers.softmax(x)
```

# GPy.util.subarray\_and\_sorting module

```
GPy.util.subarray_and_sorting.common_subarrays(X, axis=0)
```

Find common subarrays of 2 dimensional X, where axis is the axis to apply the search over. Common subarrays are returned as a dictionary of <subarray, [index]> pairs, where the subarray is a tuple representing the subarray and the index is the index for the subarray in X, where index is the index to the remaining axis.

: param np.ndarray X: 2d array to check for common subarrays in <math>: param int axis: axis to apply subarray detection over.

When the index is 0, compare rows, columns, otherwise.

In a 2d array: >>> import numpy as np >>> X = np.zeros((3,6), dtype=bool) <math>>>> X[[1,1,1],[0,4,5]] = 1; X[1:,[2,3]] = 1 >>> X array([[False, False, False, False, False, False],

[ True, False, True, True, True, True], [False, False, True, True, False, False]], dtype=bool)

#### GPy.util.symbolic module

```
class GPy.util.symbolic.dh_dd_i
    Bases: Function
    classmethod eval (t, tprime, d_i, d_j, l)
    nargs = 5
```

```
class GPy.util.symbolic.dh_dd_j
     Bases: Function
     classmethod eval (t, tprime, d_i, d_j, l)
     nargs = 5
class GPy.util.symbolic.dh_dl
     Bases: Function
     \textbf{classmethod eval} \; (\textit{t, tprime}, \textit{d\_i}, \textit{d\_j}, \textit{l})
     nargs = 5
class GPy.util.symbolic.dh_dt
     Bases: Function
     classmethod eval (t, tprime, d_i, d_j, l)
     nargs = 5
class GPy.util.symbolic.dh_dtprime
     Bases: Function
     classmethod eval (t, tprime, d_i, d_j, l)
     nargs = 5
class GPy.util.symbolic.erfc
     Bases: Function
     classmethod eval (arg)
     nargs = 1
class GPy.util.symbolic.erfcx
     Bases: Function
     classmethod eval (arg)
     nargs = 1
class GPy.util.symbolic.h
     Bases: Function
     classmethod eval (t, tprime, d_i, d_j, l)
     fdiff(argindex=5)
     nargs = 5
class GPy.util.symbolic.ln_diff_erf
     Bases: Function
     classmethod eval (x0, x1)
     fdiff(argindex=2)
     nargs = 2
GPy.util.univariate_Gaussian module
GPy.util.univariate_Gaussian.inv_std_norm_cdf(x)
     Inverse cumulative standard Gaussian distribution Based on Winitzki, S. (2008)
```

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#### GPy.util.visualize module

```
GPy.util.visualize.data_play(Y, visualizer, frame_rate=30)
Play a data set using the data_show object given.
```

Y the data set to be visualized.

**Parameters visualizer** (data\_show) – the data show objectwhether to display during optimisation

#### Example usage:

This example loads in the CMU mocap database (http://mocap.cs.cmu.edu) subject number 35 motion number 01. It then plays it using the mocap\_show visualize object.

```
data = GPy.util.datasets.cmu_mocap(subject='35', train_motions=['01'])
Y = data['Y']
Y[:, 0:3] = 0.  # Make figure walk in place
visualize = GPy.util.visualize.skeleton_show(Y[0, :], data['skel'])
GPy.util.visualize.data_play(Y, visualize)
```

```
class GPy.util.visualize.data_show(vals)
```

The data\_show class is a base class which describes how to visualize a particular data set. For example, motion capture data can be plotted as a stick figure, or images are shown using imshow. This class enables latent to data visualizations for the GP-LVM.

```
close()
modify(vals)
```

Show a data vector as an image. This visualizer rehapes the output vector and displays it as an image.

#### **Parameters**

- vals (axes handle) the values of the output to display.
- axes the axes to show the output on.
- **dimensions** (tuple) the dimensions that the image needs to be transposed to for display.
- **transpose** whether to transpose the image before display.
- **order** (*string*) whether array is in Fortan ordering ('F') or Python ordering ('C'). Default is python ('C').
- **invert** (*bool*) whether to invert the pixels or not (default False).
- palette a palette to use for the image.
- **preset\_mean** (*double*) the preset mean of a scaled image.
- **preset\_std** (*double*) the preset standard deviation of a scaled image.

modify (vals)

```
set_image (vals)
class GPy.util.visualize.lvm(vals, model, data_visualize, latent_axes=None, sense_axes=None, la-
                                   tent index=[0, 1]
     Bases: GPy.util.visualize.matplotlib_show
     modify (vals)
          When latent values are modified update the latent representation and ulso update the output visualization.
     on_click(event)
     on_enter(event)
     on_leave (event)
     on_move (event)
     show_sensitivities()
class GPy.util.visualize.lvm_dimselect (vals,
                                                       model,
                                                                data_visualize,
                                                                                latent_axes=None,
                                                sense_axes=None, latent_index=[0, 1], labels=None)
     Bases: GPy.util.visualize.lvm
     A visualizer for latent variable models which allows selection of the latent dimensions to use by clicking on a
     bar chart of their length scales.
     For an example of the visualizer's use try:
     GPy.examples.dimensionality_reduction.BGPVLM_oil()
     on_click (event)
     on_leave(event)
class GPy.util.visualize.lvm_subplots(vals,
                                                      Model,
                                                                data visualize,
                                                                                latent axes=None,
                                              sense_axes=None)
     Bases: GPy.util.visualize.lvm
     latent_axes is a np array of dimension np.ceil(input_dim/2), one for each pair of the latent dimensions.
class GPy.util.visualize.matplotlib_show(vals, axes=None)
     Bases: GPy.util.visualize.data_show
     the matplotlib_show class is a base class for all visualization methods that use matplotlib. It is initialized with
     an axis. If the axis is set to None it creates a figure window.
     close()
class GPy.util.visualize.mocap data show (vals, axes=None, connect=None)
     Bases: GPy.util.visualize.matplotlib_show
     Base class for visualizing motion capture data.
     draw_edges()
     draw_vertices()
     finalize_axes()
     finalize_axes_modify()
     initialize_axes()
          Set up the axes with the right limits and scaling.
     initialize_axes_modify()
     modify (vals)
     process_values()
```

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```
class GPy.util.visualize.mocap_data_show_vpython(vals, scene=None, connect=None, ra-
                                                            dius=0.1)
     Bases: GPy.util.visualize.vpython_show
     Base class for visualizing motion capture data using visual module.
     draw_edges()
     draw_vertices()
     modify (vals)
     modify_edges()
     modify_vertices()
     pos_axis(i, j)
     process_values()
class GPy.util.visualize.skeleton show (vals, skel, scene=None, padding=0)
     Bases: GPy.util.visualize.mocap_data_show_vpython
     data_show class for visualizing motion capture data encoded as a skeleton with angles.
     process_values()
          Takes a set of angles and converts them to the x,y,z coordinates in the internal prepresentation of the class,
          ready for plotting.
              Parameters vals – the values that are being modelled.
     wrap_around (lim, connect)
class GPy.util.visualize.stick_show(vals, connect=None, scene=None)
     Bases: GPy.util.visualize.mocap data show vpython
     Show a three dimensional point cloud as a figure. Connect elements of the figure together using the matrix
     connect.
     process_values()
class GPy.util.visualize.vector show (vals, axes=None)
     Bases: GPy.util.visualize.matplotlib_show
     A base visualization class that just shows a data vector as a plot of vector elements alongside their indices.
     modify (vals)
class GPy.util.visualize.vpython_show(vals, scene=None)
     Bases: GPy.util.visualize.data_show
     the vpython_show class is a base class for all visualization methods that use vpython to display. It is initialized
     with a scene. If the scene is set to None it creates a scene window.
     close()
GPy.util.warping functions module
class GPy.util.warping_functions.TanhWarpingFunction(n_terms=3)
     Bases: GPy.util.warping_functions.WarpingFunction
     f(v, psi)
          transform y with f using parameter vector psi psi = [[a,b,c]] ::math::f = sum\_\{terms\} a * tanh(b*(y+c))
```

```
f_{inv}(y, psi, iterations=10)
           calculate the numerical inverse of f
               Parameters iterations – number of N.R. iterations
     fgrad_y (y, psi, return_precalc=False)
           gradient of f w.r.t to y ([N x 1]) returns: Nx1 vector of derivatives, unless return_precalc is true, then it
           also returns the precomputed stuff
     fgrad_y_psi (y, psi, return_covar_chain=False)
           gradient of f w.r.t to y and psi
           returns: NxIx3 tensor of partial derivatives
class GPy.util.warping_functions.TanhWarpingFunction_d(n_terms=3)
     Bases: GPy.util.warping_functions.WarpingFunction
     f(y, psi)
           Transform y with f using parameter vector psi psi = [[a,b,c]]
           f = \sum_{terms} a * tanh(b * (y + c))
     f_inv (z, psi, max_iterations=1000, y=None)
           calculate the numerical inverse of f
               Parameters max iterations – maximum number of N.R. iterations
     fgrad_y (y, psi, return_precalc=False)
           gradient of f w.r.t to y ([N x 1])
               Returns Nx1 vector of derivatives, unless return_precalc is true, then it also returns the precom-
                   puted stuff
     fgrad_y_psi (y, psi, return_covar_chain=False)
           gradient of f w.r.t to y and psi
               Returns NxIx4 tensor of partial derivatives
class GPy.util.warping_functions.WarpingFunction
     Bases: object
     abstract function for warping z = f(y)
     f(y, psi)
           function transformation y is a list of values (GP training data) of shpape [N,1]
     f_inv(z, psi)
           inverse function transformation
     fgrad_y(y, psi)
           gradient of f w.r.t to y
     fgrad_y_psi(y, psi)
           gradient of f w.r.t to y
     plot (psi, xmin, xmax)
```

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#### **Module contents**

## 1.1.2 Submodules

# 1.1.3 GPy.models module

Implementations for common models used in GP regression and classification. The different models can be viewed in GPy.models\_modules, which holds detailed explanations for the different models.

**Note:** This module is a convienince module for endusers to use. For developers see <code>GPy.models\_modules</code>, which holds the implementions for each model.:

# 1.1.4 Module contents

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GPy.read(fname)
GPy.tests()
```

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