Untitled

Split the data

```
df <- read.csv("utilities.csv")</pre>
y <- df$gasbill/df$billingdays
x <- df$temp
n<-length(y)</pre>
train idx <- sample(1:n,0.8*n)
y_train <- y[train_idx]</pre>
x_train <- x[train_idx]</pre>
y_test <- y[-train_idx]</pre>
x_test <- x[-train_idx]</pre>
normal_kernel <- function(d,h){</pre>
  ##Input: d- distance (scalar), h-bandwith (scalar)
  ##Output: kernel value (scalar)
  return(1/h*dnorm(d/h,mean=0,sd=1))
get_W <- function(x,x_star,h,kern_func){</pre>
  W <- diag(kern_func(x-x_star,h))</pre>
  return(W/sum(W))
get_R <- function(x,x_star,D){</pre>
  R <- matrix(NA,ncol=D+1,nrow=length(x))</pre>
  for(i in 1:(D+1)){
    R[,i] <- (x-x_star)^(i-1)
  }
  return(R)
}
get_l <- function(R,W){</pre>
  return((solve(t(R)%*%W%*%R)%*%t(R)%*%W)[1,])
get_est <- function(1,y){</pre>
  return(1%*%y)
}
```

Find h that minimizes test error

```
get_err <-function(D,h){
    err <- rep(NA,n)
    for(i in 1:n){
        x_star <- x[i]
        x_train <- x[-i]
        y_train <- y[-i]
        y_test <- y[i]
        R <- get_R(x_train,x_star,D)
        W <- get_W(x_train,x_star,h,normal_kernel)
        1 <- get_1(R,W)</pre>
```

```
y_pred <- get_est(l,y_train)
    err[i] <- (y_test-y_pred)^2
}

return(err)
}

h_vec <- seq(1,10,1)
h_err <- rep(NA,length(h_vec))
for(i in 1:length(h_vec)){
    h_err[i] <-mean(get_err(1,h_vec[i]))
}
h_min <-h_vec[which.min(h_err)]
h_min</pre>
```

[1] 7

Confidence Band

```
get_pred<-function(x_train,x_star,y,D,h,kern_func){</pre>
                     R <- get_R(x_train,x_star,D)</pre>
                     W <- get_W(x_train,x_star,h,kern_func)</pre>
                     1 <- get_1(R,W)</pre>
                     y_pred <- get_est(1,y)</pre>
      return(list(y_pred,1))
y_fit <- rep(NA,length(x))</pre>
1 <- rep(NA,length(x))</pre>
err <- rep(NA,length(x))
D<-1
H <- matrix(NA, nrow= length(x), ncol=length(x))</pre>
for(i in 1:length(x)){
       ans <- get_pred(x,x[i],y,D,h_min,normal_kernel)</pre>
       y_fit[i] <- ans[[1]]</pre>
      H[i,] \leftarrow ans[[2]]
       err[i] <- y_fit[i] - y[i]
}
sigma_2 <- sum(err^2)/(length(x)-2*sum(diag(H))+sum(diag(t(H)%*%H)))
sd_vec <- rep(NA,length(x))</pre>
for(i in 1:dim(H)[1]){
      1 <- H[i,]
       sd_vec[i] <- sqrt(sigma_2*t(1)%*%1)</pre>
x_idx <- order(x)</pre>
plot(x,y,col="cyan4",pch=19)
lines(x[x_idx],y_fit[x_idx],lwd=2,col="red")
polygon(c(x[x_idx],rev(x[x_idx])), c(y_fit[x_idx]-sd_vec*qnorm(0.95,0,1), rev(y_fit[x_idx])+sd_vec*qnorm(0.95,0,1), rev(y_fit[x_idx])+sd_vec*qnorm(0.95,0,
```

