

Cattle, Steaks and Restaurants: Development Accounting when Space Matters*

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Abstract

We introduce location choice in a multi-sector general equilibrium model to study how it affects development accounting. Producers in agriculture, manufacturing and services choose their location to trade off land rents with transport costs to the city center. We show how space affects the aggregate production function and decompose output per worker into productivity, land per worker, and a term adjusting for sector location. In our model, services are luxury goods. As a result, richer cities have larger service cores, higher service prices, and relatively less output per worker in services. These predictions are broadly consistent with the data. We calibrate our model to data on cities in OECD countries and show that land and location explain 10–30 percentage points of the variation in output per worker.

Output per worker is much lower in poor countries than in rich ones (Klenow and Rodriguez-Clare 1997; Hall and Jones 1999; Caselli 2005). To understand the fundamental causes of productivity differences, it is important to identify the sectors in which these differences are the greatest. Several recent papers have studied the sectoral composition of productivity differences by using data on sector-level inputs, outputs and prices (Baily and Solow 2001; Caselli 2005; Restuccia, Yang, and Zhu 2008; Duarte and Restuccia 2010; Duarte and Restuccia 2015). Their main result is

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that productivity differences are sizeable and they are larger in agriculture than in manufacturing and services.¹

Labor productivity depends on the quantity or quality of inputs used in the production process. Here we argue that land input has been conspicuously missing from development accounting exercises to date. Controlling for land when estimating macro productivity is important for two reasons. First, countries with high population density are relatively scarce in land and, to the extent that land matters in production, these countries will have low labor productivity. Second, land varies in a crucial quality component: its proximity to consumers. Urban land is more valuable because it is more productive in producing goods and services with high transport costs. Again, countries may differ in the availability of urban land. Accounting for land and location is especially important for sector-level development accounting. Agriculture uses land intensively and will be especially sensitive to controlling for the quantity of land. Services, in turn, locate in urban areas and will be especially sensitive to controlling for location.

To understand how land and location affect development accounting, we build a simple multi-sector general equilibrium model. Each sector uses labor (or a composite of other spatially mobile inputs) and land. The location of sectors is determined as in the canonical von Thünen city model. In the model, all trade happens in the city center, the central business district (CBD). Producers choose their location freely on a plane, and have to pay a shipping cost to transport their goods to the CBD. This spatial structure introduces variable land-quality to the model, as land closer to the CBD saves on transport cost. Equilibrium rents decrease with distance from the CBD, and the producers optimally choose locations to balance savings on transport costs with higher rents. Our model yields a simple spatial equilibrium in which agriculture (“cattle”) locates farthest away from the center, manufacturing (“steaks”) occupies a ring outside the center, and services (“restaurants”) are in a central circle.

We can decompose output per worker into three components: (i) Hicks neutral productivity (which will also capture the presence of spatially mobile factors such as capital), (ii) land per worker, and (iii) a term reflecting distance to consumers. Components (ii) and (iii) are novel to our model. First, as some sectors are more land intensive, their labor productivity will be more sensitive to the scarcity or abundance of land. Conditional on other productivity factors, agricultural output per worker will be higher in countries with an abundant supply of land. Second, urban sectors

¹These results are in line with the classic Balassa-Samuelson literature (Balassa 1964; Samuelson 1964; Baumol and Bowen 1965; Baumol 1967), which explains sectoral price-level differences by productivity advantage of manufacturing over services.

(such as services) will be relatively more productive in smaller cities where transport costs are lower.

To quantify the importance of these two mechanisms, we calibrate our model to city-level data on employment density, city size, and GDP per capita (from the OECD Metropolitan Areas Database) and country-level prices and expenditure shares (from the International Comparison Program). We set common technology parameters to match the sectoral land-shares and spatial distribution of economic activities in the U.S. We then use the calibrated model to decompose output per worker into the three components for each city.

Perhaps unsurprisingly, the largest variation across cities in output per worker is due to variation in Hicks neutral productivity. We estimate this productivity variation to be essentially the same in the three broad sectors. This is in contrast with the existing literature, which finds more variation agricultural productivity (Caselli 2005; Restuccia, Yang, and Zhu 2008),² and less variation in services productivity (Balassa 1964; Samuelson 1964; Herrendorf and Valentinyi 2012).³

Variation in land per worker explains up to 30 percentage points of productivity differences across the cities in our sample. This variation is biggest in agriculture, which uses land intensively. In our sample, land per worker does not vary systematically with development.

Sector location explains up to 10 percentage points of productivity differences. This varies systematically with development as poorer cities spend less on services and have smaller service cores. Transportation costs in these cities is lower and output per worker is higher.

More broadly, our model illustrates how to incorporate space in a simple development accounting model and that transport costs can have macro relevance. In related work, Ramondo, Rodríguez-Clare, and Saborío-Rodríguez (2016) incorporate space in a macro model with transport costs, arguing that large countries have larger transport costs and hence not as high GDP per capita. The main difference is that while Ramondo, Rodríguez-Clare, and Saborío-Rodríguez (2016) capture average trade costs across cities within a country, our main focus is the within-city trade cost and spatial structure. Also related are Desmet and Rossi-Hansberg (2013), who study an endogenous system of cities (in our work, cities are exogenous in size) and Desmet and Rossi-Hansberg (2014), who study cities and growth (our model is static). Neither of

²Admittedly, data on metropolitan areas is less informative about productivity in agriculture than in the two other sectors.

³Duarte and Restuccia (2015) find that productivity in tradable business services varies more than in manufacturing.

these papers focus on the spatial allocation of sectors as we do.

Lagakos and Waugh (2013) study a model of structural change where workers vary in agricultural productivity. In poor countries, more people will work in agriculture, and their average productivity will be low. Our model features a similar mechanism, but in our setting, it is the productivity of land that is heterogeneous, as it depends on distance to the center. In rich countries, more land will be devoted to services, resulting in relatively lower output per worker.

Our model is motivated by four robust empirical facts. First, urban land becomes more important with development relative to rural land (Clark 2007, Figure 10.3). Second, the relative price of services increase with development. This is known as Baumol’s cost disease (Baumol and Bowen 1965) or the Balassa-Samuelson effect (Balassa 1964; Samuelson 1964). Third, rich countries are more urbanized (United Nations 2014). Fourth, rich countries produce less agriculture and more services (Kuznets 1973; Ngai and Pissarides 2007; Kongsamut, Rebelo, and Xie 2001). As we show below, our model is capable of explaining these facts in a simple framework.

1 A model of industry location

We introduce location choice to a multi-sector general equilibrium model. We have three sectors: agriculture, manufacturing and services, each using land and labor for production. Our spatial structure follows the von Thünen monocentric city model: producers choose a location on the plane and need to transport their goods to the central business district.

1.1 Consumers

To be consistent with Fact 4, we assume non-homothetic consumer preferences. We follow Fielor (2011) in assuming an isoelastic utility function with different elasticities for the three sectors,⁴

$$u = \sum_{i=1}^3 \alpha_i^{1/\sigma_i} \frac{\sigma_i}{\sigma_i - 1} c_i^{1-1/\sigma_i}, \quad (1)$$

where $\alpha_i > 0$ is the weight of sector i and σ_i governs the sector’s price and income elasticity. Anticipating the spatial ordering of sectors, we let $i = 1$ index services, 2 will stand for manufacturing, and 3 for agriculture.

⁴We have estimated the preferences proposed by Kongsamut, Rebelo, and Xie (2001), Ngai and Pissarides (2007) and Herrendorf, Rogerson, and Valentinyi (2013) on cross-country data, but this provided a poor fit for rich countries, where the role of necessity spending is vanishingly small.

There is a mass N of consumers who supply one unit of labor inelastically, and rent land to producers in a competitive market. They are *absentee landlords*: the rents they collect are independent of the place of employment.

The budget constraint of a representative consumer is

$$\sum_i P_i c_i = W + \frac{1}{N} \int_z R(z) \tilde{L}(z) dz, \quad (2)$$

where $R(z)$ is the rent as a function of the distance to the center (see later), and W is the wage. Because labor is freely mobile, wages do not depend on location.

The sectoral consumption expenditures satisfy

$$P_i c_i = \alpha_i \lambda^{-\sigma_i} P_i^{1-\sigma_i}, \quad (3)$$

where λ is the Lagrange multiplier of the budget constraint, which is decreasing in income. For a given set of prices, the expenditure of good i relative to good j is increasing in income if $\sigma_i > \sigma_j$. The income elasticity of good i is

$$\frac{\partial \ln c_i}{\partial \ln y} = \frac{\sigma_i}{\sum_j x_j \sigma_j}, \quad (4)$$

where $x_j = P_j c_j / \sum_k P_k c_k$ is the expenditure share of good j .

1.2 Producers

Output in sector i at location z depends on labor N and land L used at that location,

$$Q_i(z) = A_i L_i(z)^{\beta_i} N_i(z)^{1-\beta_i}.$$

We take labor to be freely mobile within the country, land is in fixed $\bar{L}(z)$ supply in each location. The names “land” and “labor” are for the sake of convenience, these two factors correspond to spatially fixed and mobile factors, respectively, and we will calibrate them accordingly.

Sectors differ in their land shares β_i and Hicks neutral productivity shifter A_i . All products are sold and consumed at a single location, the central business district. This is location $z = 0$, so that z indexes distance to the center. To ship a product to the center, one has to incur shipping costs. If a unit of product i leaves location z , only

$$e^{-\tau_i z}$$

units arrive at the center. This is akin to the iceberg assumption of transport costs. Sectors also differ in the intensity of shipping costs τ_i .

Profits in sector i from production at z is

$$\Pi_i(z) = P_i e^{-\tau_i z} Q_i(z) - W N_i(z) - R(z) L_i(z). \quad (5)$$

A sector being active at location z requires that their maximized profit $\max \Pi_i(z) \geq 0$.

1.3 Spatial Equilibrium

We assume the city is circular with radius z_3 so that the available land at each distance z is $\bar{L}(z) \equiv 2z\pi$ for $z \in [0, z_3]$ and zero otherwise. We study symmetric equilibria where the distance to the CBD completely characterizes a location.

Definition 1. *The competitive spatial equilibrium in a circular city is a set of quantities $\{c_i, Q_i(z), L_i(z), N_i(z)\}_{i=1}^3$ and prices $\{P_i, R(z), W\}_{i=1}^3$ such that*

1. *The consumer chooses $\{c_i\}_{i=1}^3$ to maximize utility (1) subject to its budget constraint (2), taking prices as given.*
2. *The producers choose sector i and location z , and nonnegative quantities $\{Q_i(z), L_i(z), N_i(z)\}$ to maximize their profits (5), taking prices as given.*
3. *Sectoral goods market clear: $N c_i = \int_{z \in Z} e^{-\tau_i z} Q_i(z) dz$ for $i = 1, 2, 3$.*
4. *Labor market clears: $N = \sum_i \int_{z \in Z} N_i(z)$.*
5. *Land markets clear at every location: $\sum_i L_i(z) = \bar{L}(z)$ for all $z \in Z$.*

The equilibrium, as we show below, has a simple and intuitive spatial structure. Sectors with higher transport cost intensity (τ_i) and lower land share (β_i) locate closer to the center. Realistically, services locate in a circle around the center, manufacturing goods are produced on a ring around it, and agriculture occupies the outer ring.

To see why it is the case, construct the sectoral bid rent curves $R_i(z)$. These are the maximum rent an active producer in sector i would be willing to pay at location z . A profit maximizing producer is choosing its land $N_i(z)$ and labor demand $L_i(z)$ to equalize the value marginal product of land and labor to rents and wages, respectively. It is true for any rent function or wages it might face, so it is true for rents given by its own bid-rent curve $R_i(z)$, in particular.

$$R_i(z) = \beta_i P_i e^{-\tau_i z} A_i \left(\frac{N_i(z)}{L_i(z)} \right)^{1-\beta_i} \quad (6)$$

$$W = (1 - \beta_i) P_i e^{-\tau_i z} A_i \left(\frac{N_i(z)}{L_i(z)} \right)^{-\beta_i} \quad (7)$$

The sectoral labor-land ratio (employment density) can be expressed as

$$\frac{N_i(z)}{L_i(z)} = \frac{1 - \beta_i}{\beta_i} \frac{R_i(z)}{W}. \quad (8)$$

Substituting this into the first-order condition for land use, we can get an implicit expression for the sectoral bid rent curve:

$$R_i(z) = \beta_i P_i e^{-\tau_i z} A_i \left(\frac{1 - \beta_i}{\beta_i} \frac{R_i(z)}{W} \right)^{1-\beta_i},$$

from which

$$R_i(z) = \beta_i (1 - \beta_i)^{1/\beta_i - 1} (P_i A_i)^{1/\beta_i} W^{1-1/\beta_i} e^{-\frac{\tau_i}{\beta_i} z}. \quad (9)$$

Equation (9) pins down the gradient of the sectoral rent curve, which determines how fast the bid-rents decrease with the distance from the CBD. The gradient is an increasing function of the sectoral transport costs and a decreasing function of land shares $|\partial \log R_i(z) / \partial \log z| = \tau_i / \beta_i$. Intuitively, transport costs ($\tau_i z$) increase with distance, so producers offer lower rents for farther locations. If land were the only factor of production ($\beta_i = 1$), only this direct effect would be present and the gradient would only depend on the transport cost intensity. With labor present, however, the producers can substitute labor for land, introducing an indirect effect on the gradient. As the equilibrium land-labor ratio shows (see equation 8), the land share β_i determines the strength of this substitutability: higher land share implies bid-rent curves decreasing with a slower rate.

We can also get the employment gradient by substituting the bid rent curve into the labor-land ratio,

$$\frac{N_i(z)}{L_i(z)} = (1 - \beta_i)^{1/\beta_i} \left(\frac{P_i A_i}{W} \right)^{1/\beta_i} e^{-\frac{\tau_i}{\beta_i} z}. \quad (10)$$

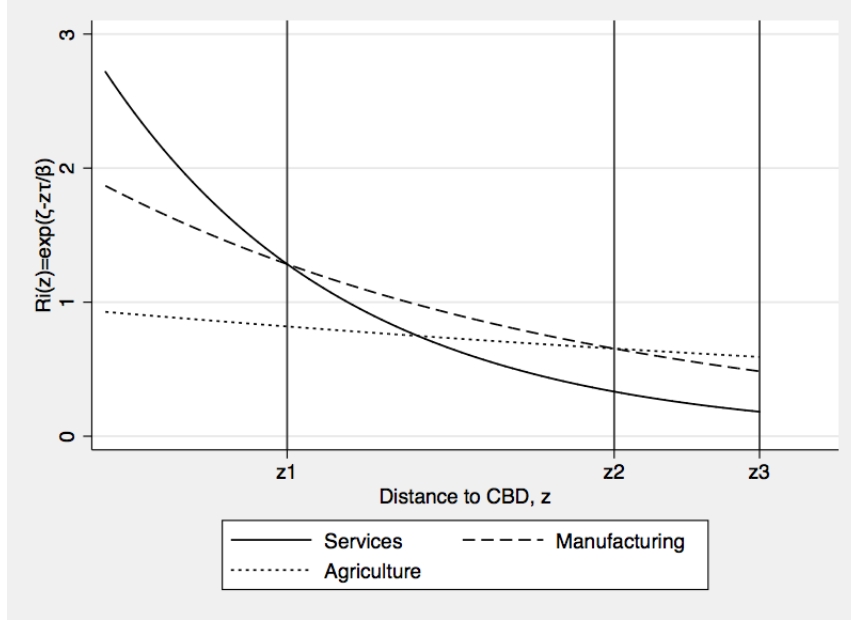
This is the relationship we use to calibrate the sectoral transport cost intensities.

Proposition 1. *Assume that $\tau_1/\beta_1 > \tau_2/\beta_2 > \tau_3/\beta_3 > 0$. There exists a competitive spatial equilibrium. The structure of this equilibrium is a partitioning, with locations $0 < z_1 < z_2 < z_3$ such that services with the highest τ_i/β_i rate locate closest to the CBD in $[0, z_1]$, manufacturing locates in $(z_1, z_2]$, and agriculture locates in $(z_2, z_3]$.*

The proof is provided in the Appendix. Intuitively, the different exponential slope of the bid-rent curves ensures that they cross exactly once. This results in a strict partitioning across sectors, as shown in Figure 1. Equilibrium further requires that these bid-rent curves are consistent with consumer expenditure shares.

The following propositions characterize how space use depends on development.

Figure 1: Spatial equilibrium



The figure plots the structure of a spatial competitive equilibrium. It shows equilibrium sectoral bid rent curves as a function of distance from the city center. A sector is active over an area where it is willing to overbid alternative sectors. Crossings of the bid-rent curves determine the borders of the sectors. Services are active in $[0, z_1]$, manufacturing in $(z_1, z_2]$, and agriculture in $(z_2, z_3]$.

Proposition 2. *Assume $\sigma_1 = \sigma_2 = \sigma_3$. Then a uniform increase in productivity across sectors leaves sectoral and spatial allocations (z_i, L_i) unchanged.*

Proposition 3. *Assume $\sigma_1 > \sigma_2 > \sigma_3$. Then a uniform increase in productivity across sectors expands the amount of land devoted to services, and shrinks the amount of land devoted to agriculture: z_1, z_2 and L_1 increase, L_3 decreases. The price of services increases relative to agriculture.*

Proposition 3 is consistent with the empirical facts about structural change, urbanization, and the relative price of services.

1.4 Aggregation across space

Sectoral production is a function of a suitably chosen representative location. Sectoral output measured at the center is

$$\tilde{Q}_i = \int_{z \in Z_i} e^{-\tau_i z} A_i L_i(z)_i^\beta N_i(z)^{1-\beta_i} dz,$$

where Z_i is the set of locations where sector i is active in equilibrium.

Let the representative location

$$\tilde{z}_i = -\frac{\beta_i}{\tau_i} \ln \int_{z \in Z_i} \frac{L_i(z)}{L_i} e^{-\frac{\tau_i}{\beta_i} z} dz \quad (11)$$

denote the average distance of sector i to the center, where $L_i = \int_{z \in Z_i} L_i(z) dz$ is the total amount of land devoted to sector i . This definition ensures that the trade cost going to location \tilde{z}_i equals the land-weighted average trade cost across all sectoral locations,

$$e^{-\frac{\tau_i}{\beta_i} \tilde{z}_i} = \int_{z \in Z_i} \frac{L_i(z)}{L_i} e^{-\frac{\tau_i}{\beta_i} z} dz.$$

As we will see below, \tilde{z}_i is a sufficient statistic about sector location for aggregation purposes.

Proposition 4. *Aggregate sectoral production function is of the form:*

$$\tilde{Q}_i = A_i L_i^{\beta_i} N_i^{1-\beta_i} e^{-\tau_i \tilde{z}_i}. \quad (12)$$

It depends on trade costs from the representative location (\tilde{z}_i) defined by equation (11) and is a Cobb-Douglas aggregate of sectoral land ($L_i = \int_{Z_i} L_i(z) dz$) and labor ($N_i = \int_{Z_i} N_i(z) dz$) use.

Using the aggregate production function, we can write output per worker in sector i as

$$\frac{\tilde{Q}_i}{N_i} = A_i \left(\frac{L_i}{N_i} \right)^{\beta_i} e^{-\tau_i \tilde{z}_i}. \quad (13)$$

This tends to be low when Hicks-neutral productivity is low, land is scarce (especially for land intensive sectors), trade costs are high, or cities are large.

We call the first term the contribution of *productivity*, the second term the contribution of *land*, and the third term the contribution of *location*. In the next section we calibrate the model and estimate each of the three components.

2 Mapping the model to data

We calibrate the model to city-level data from the OECD to show how land usage and sector location varies with development. We fix a number of parameters across cities, but the supply of land and labor, as well as sectoral productivity are allowed to vary.

We assume that cities are in autarky so that we can analyze them separately.⁵ First we calibrate land shares and shipping costs using US data. Then we turn to the calibration of parameters influencing cross-country, cross-city variations.

2.1 Common parameters

Land shares. We calibrate sectoral land shares (β_i) using US data. Our aim is to capture the share of immobile factors in production. These come from two sources: (i) the direct use of land in production and (ii) the land-rent paid by workers. We calibrate the direct use of land in sectoral production using US factor income share estimates of Valentinyi and Herrendorf (2008). The first two columns of Table 1 show their estimates for land and labor shares across sectors.

The indirect use of land is the land used by workers. We calibrate land-rent share in labor as a product of the US aggregate rent-share in consumption expenditure reported by the BLS (30%) and the average land-share of US house prices between 1984-1998 estimated by Davis and Palumbo (2008) (36%). We find it to be 10.8%. We multiply this by the labor shares to get the indirect land shares listed in column 3 of Table 1. Our calibrated overall land shares (β_i) are the sum of the direct and indirect land shares, and they are shown in column 4.

The calibrated values show that land is a non-negligible factor in production in each sectors. As expected, its role is the largest in agriculture (23%), but the land share in manufacturing and services are both double-digit (10%–13%), mainly because of the indirect land use of their workers.

Table 1: Calibrated factor shares

Factor shares	Direct land	Labor	Indirect land	Overall land share β_i
Agriculture	0.18	0.46	0.05	0.23
Manufacturing	0.03	0.67	0.07	0.10
Services	0.06	0.66	0.07	0.13

Land and Labor shares are estimates of Valentinyi and Herrendorf (2008). Land share in labor is the product of rent-share in US consumption expenditures, the average land-share of US house prices between 1984-1998 estimated by Davis and Palumbo (2008) and the labor shares. Our land share estimates are the sum of direct land share and the indirect land share in labor.

⁵Desmet and Rossi-Hansberg (2013) study a system of cities with endogenous mobility among them.

Shipping costs. We use the 2010 ZIP Business Patterns of the U.S. Census (U.S. Bureau of the Census 2010) to determine the location of sectors in the United States. We use this to calibrate transportation costs and distances of the sectors from the center.

The ZIP Business Patterns contains the number of establishments in employment size categories in each ZIP code for each 6-digit NAICS code. We merge NAICS codes into agriculture, manufacturing and services as follows. Agriculture is sector 11 of NAICS. We merge mining (21), utilities (22), and construction (23) together with manufacturing industries (31-33). As services, we categorize the rest, including public administration. We estimate employment by using the midpoints of the size categories.

To map the model into the data, we need to specify how far each ZIP code is from the city center. We take Urbanized Areas (UAs) as independent monocentric cities, and we assign the central point to the business or administrative center of the first-mentioned city in the UA, as given by Yahoo Maps. For example, the center of “New York–Newark, NY–NJ–CT Urbanized Area” is the corner of Broadway and Chamber St in downtown Manhattan, whereas the center of “Boston, MA–NH–RI Urbanized Area” is 1 Boston Pl. We calculate the distance of each ZIP code to business center of the nearest UA.

According to equation 8, the employment density of sector i in location z is proportional to the rent-wage ratio. When industry i demands positive land in the neighborhood of z , then the rent is proportional to $e^{-\tau_i/\beta_i z}$. We can use this observation to estimate τ_i :

$$\frac{d \ln n_i(z)/l_i(z)}{dz} = \frac{d \ln r_i(z)}{dz} = -\frac{\tau_i}{\beta_i}.$$

To get a sense where each sectors is active, we calculate location quotients by distance to the city center. For each sector, they measure the employment share at a certain distance relative to the average employment share of the same sector. A value higher than 1 implies that the sector is overrepresented in the particular distance from the center.

Figure 2 shows that sectors sort as in the model: services are overrepresented closer to the city center, while manufacturing and agriculture are both underrepresented there. Agriculture shows a particularly steep gradient, with high relative employment farther away from the city center. In the calculation of sectoral employment gradients below, we restrict attention to the areas where the sectors are overrepresented. We assume that services are active up to 30 kms from the center, manufacturing is active between 10 and 60 kms (there is some mixed use) and agriculture farther than 60 kms.

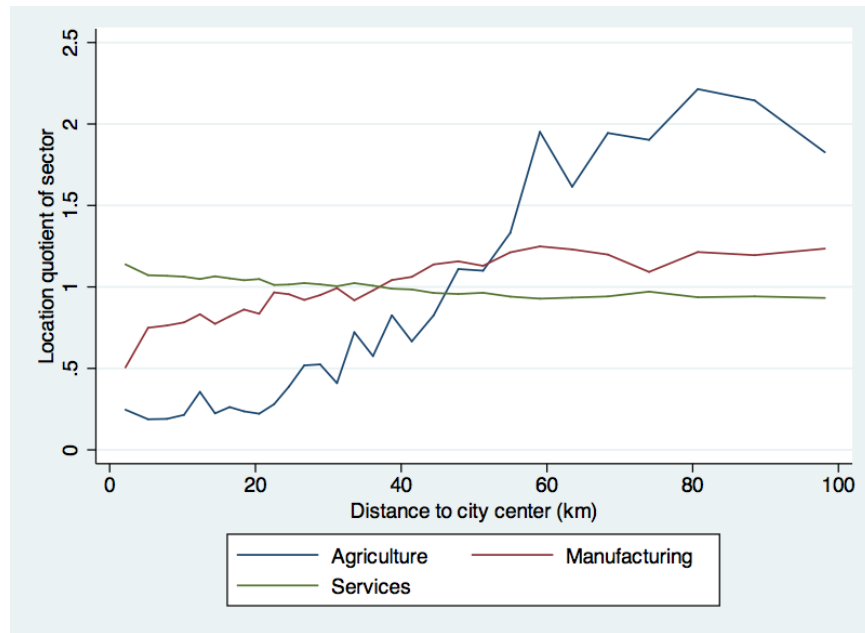


Figure 2: Sector location quotients

Source: ZIP Business Patterns. Plots the sectoral employment shares at a particular distance (in a 3km-wide ring) from the city center, relative to the average sectoral employment share. The figure shows that sectors sort as in the model: services are overrepresented closer the the city center, while manufacturing and agriculture are located mostly farther away, agriculture showing a particularly steep gradient.

Let n_{izc} be the employment of industry i in ZIP code z , belonging to city (MSA) c . Assuming that establishments in a given sector consume the same amount of land,⁶ we denote by l_{izc} the number of establishments of sector i in ZIP code z . We can then regress establishment size (workers per establishment) in each sector in each ZIP code on fixed effects, and the distance of the ZIP code to the city center,

$$\frac{n_{izc}}{l_{izc}} = e^{\mu_c + \nu_i - \gamma_i d(z,c)}. \quad (14)$$

The city fixed effect captures variation in rents and wages in the MSA, the sector fixed effect captures variation in land and labor intensity and establishment size across sectors. The key parameter of interest is γ_i , which captures how fast employment declines with distance to the center by sector.

From the ZBP, we have the approximate employment of the sector (reconstructed from establishment-size bins), and the total area of the ZIP code, but area is not broken down by sector. If a ZIP code is exclusively used by one of the three sector, this is not a problem. Otherwise, we impute the area used by sector i as follows.

The mode predicts the area per worker in sector i in ZIP-code z to be

$$\frac{L_i(z)}{N_i(z)} = \frac{1 - \beta_i}{\beta_i} \frac{W}{R(z)}.$$

Because all sectors face the same wages and rents in the same ZIP code, we can distribute land in proportion to

$$\frac{1 - \beta_i}{\beta_i} N_i(z).$$

In urban ZIP codes, there is also a substantial amount of residential land. We know that households spend 0.3×0.36 fraction of their income on residential land rent. Assuming that residents' only income are wages,

$$\frac{R(z)H(z)}{WP(z)} = 0.3 \times 0.36,$$

where $P(z)$ is the number of people living in ZIP code z . Hence total residential area is

$$H(z) = 0.3 \cdot 0.36 P(z) \frac{W}{R(z)}.$$

We then allocate residential land in proportion to $0.3 \cdot 0.36 P(z)$.

⁶We believe this approximation is likely to bias our estimates of the rent gradient downward. Rural establishments probably occupy more space than urban establishments even in the same narrow industry, so establishment sizes do not go down as fast with distance as employment density does.

We estimate (14) by a Poisson regression which ensures that the equation holds in expectation, and permits estimation even when $n_{izc} = 0$, which is often the case. The estimates of γ_i and the implied sectoral transport cost intensities τ_i in the three sectors are below.

Table 2: Estimated rent and price gradients			
	Gradient (per km)		
	Land share β_i	Rents γ_i	Prices τ_i
Services	13%	13.15%	1.71%
Manufacturing	10%	5.15%	0.52%
Agriculture	23%	3.54%	0.81%

Sectoral rent gradients γ_i are estimated using US employment-density observation across ZIP codes in MSAs. Price gradients reflect transport costs (τ_i) and are estimated by multiplying rent gradients with sectoral land shares (β_i).

The three columns report the calibrated land shares, and the estimates for rent and price gradients, respectively, for each sector. The estimated coefficients can be interpreted as follows. We find that the rents paid by services become 13.15% cheaper with every kilometer from the city center over the 0-30km range, where services are active. Though a 13% reduction is substantial, it does not seem unrealistic with a whole 1 kilometer distance. In line with our intuition, rent gradients of manufacturing and agriculture (measured further away from the city center) both imply slower rent declines. We infer price gradients reflecting the transportation cost intensities (τ_i) from the measured rent gradients $\gamma_i = \tau_i/\beta_i$ and the sectoral land shares. The last column of table 2.1 shows that we find transportation costs of services significantly higher (1.71%) than those of manufacturing and agriculture (0.52%, 0.81%). These rent gradients are in line with estimates of Schmenner (1981) and Eberts and Gronberg (1982) and are lower than historical rent gradients in New York City (Atack and Margo 1998). We hold these estimated technology parameters constant across countries and cities.

Utility parameters. We estimate the utility function (1) in cross-country data from 2007. Expenditure shares ($\{x_i\}$) are from the 2005 wave of the International Comparison Program (Bank 2005). We calculate sectoral price levels ($\{P_i\}$) from the International Comparison Program’s disaggregate data on 24 product headings. We measure per capita income by purchasing power parity adjusted GDP per capita (y).

We estimate the following equation for expenditure share of sector $i = 1, 2, 3$ in country c by non-linear least squares,

$$x_{ic} = \frac{\alpha_i \lambda(y_c)^{-\sigma_i} P_{ic}^{1-\sigma_i}}{\sum_j \alpha_j \lambda(y_c)^{-\sigma_j} P_{jc}^{1-\sigma_j}} + \varepsilon_{ic}, \quad (15)$$

where $\lambda(y_c) = by_c^{-1/\sum_j x_{j0}\sigma_j}$ is the first-order Taylor approximation of marginal utility around average expenditure shares $\{x_{j0}\}$, and ε_{ic} is an error term independent of income and prices.⁷

Our estimated elasticities are $\sigma_1 = 0.45$, $\sigma_2 = 0.46$ and $\sigma_3 = 0.16$. The model fits the expenditure share data quite well, with an R^2 between 0.86 for manufacturing and 0.95 for services. The model captures the fact that the expenditure share of agriculture is decreasing in income by estimating a low σ_3 . The income elasticities of manufacturing and services are not significantly different from one another.

Figure 3 plots the estimated expenditure shares against GDP per capita of the country. Note that because these shares also depend on prices, the univariate relationship is necessarily noisy. The well-known pattern of structural transformation is visible.⁸ The share of services is steadily growing with development, while the share of agriculture is shrinking and eventually vanishes. Manufacturing follows a hump shaped pattern with development.

2.2 Recovering city-level parameters

We use city-level data on land area, employment and GDP per capita from the the OECD Metropolitan Areas database (OECD 2012). Our sample includes 277 cities across OECD countries with non-missing area and employment data in 2007.⁹ Cities are defined as “functional urban areas,” and are typically extend beyond the administrative boundaries. For US cities, they roughly correspond to Metropolitan Statistical Areas. To obtain variation in expenditure shares across cities, we use the model-consistent expenditure shares predicted by our estimated utility function.

The following equations completely characterize the spatial equilibrium of city c .

⁷To be precise, since we are only approximating λ , higher-order terms in income will show up in the error term. As our results do not change when we include second-order terms in income, this effect is likely quantitatively small.

⁸See, for example, Buera and Kaboski (2012) for recent cross-country estimates of how expenditure shares depend on development.

⁹We impute employment from population for three cities in Switzerland.

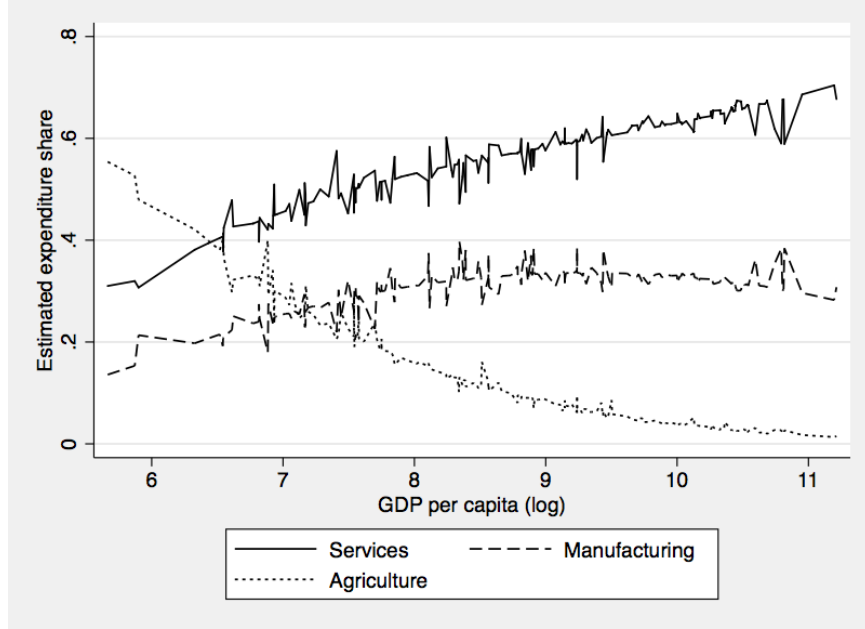


Figure 3: Estimated expenditure shares and GDP per capita
Fitted values of regression (15) plotted against log GDP per capita. Estimates also depend on sectoral relative prices, leading to variation independent of income.

Representative location.

$$\tilde{z}_{ic} = -\frac{\beta_i}{\tau_i} \ln \left[\int_{z=z_{i-1,c}}^{z_{ic}} \frac{z^2 \pi}{L_{ic}} \exp(-z\tau_i/\beta_i) dz \right] \quad (16)$$

Land market clearing.

$$L_{ic} = \int_{z=z_{i-1,c}}^{z_{ic}} z^2 \pi dz \quad (17)$$

with $L_{1c} + L_{2c} + L_{3c} = L_c$.

Labor intensity.

$$\frac{N_{ic}}{L_{ic}} = \frac{1 - \beta_i}{\beta_i} \exp(\zeta_{ic} - \tilde{z}_{ic}\tau_i/\beta_i), \quad (18)$$

where we introduced

$$\zeta_{ic} = \ln \beta_i + \frac{1 - \beta_i}{\beta_i} \ln(1 - \beta_i) + \frac{1}{\beta_i} (\ln P_{ic} + \ln A_{ic} - \ln W_c)$$

to simplify notation. The endogenous variable ζ_{ic} captures relative factor prices in sector i .

Rent arbitrage.

$$\zeta_{ic} - z_{ic}\tau_i/\beta_i = \zeta_{i+1,c} - z_{ic}\tau_{i+1}/\beta_{i+1} \quad (19)$$

Labor market clearing.

$$\sum_i N_{ic} = N_c \quad (20)$$

Goods market clearing.

$$W_c N_{ic} = (1 - \beta_i) x_{ic} y_c \quad (21)$$

For each city c , we solve these equations for (z_1, z_2, z_3) , $(\tilde{z}_1, \tilde{z}_2, \tilde{z}_3)$, (L_1, L_2, L_3) , (N_1, N_2, N_3) and $(\zeta_1, \zeta_2, \zeta_3)$.

Given city-level data on total area L , total employment N , sectoral prices P_i , and GDP per capita Y , we recover the sector-city level productivity parameters as follows.

1. Using the estimated expenditure shares x_{ic} and equations (21) and (20), calculate (N_{1c}, N_{2c}, N_{3c}) .
2. Assuming the city is circular, set $z_{3c} = \sqrt{L_c/\pi}$.
3. Pick a candidate z_{1c} and z_{2c} dividing the service and manufacturing areas.
4. Using equations (17) and (16), calculate (L_{1c}, L_{2c}, L_{3c}) and $(\tilde{z}_{1c}, \tilde{z}_{2c}, \tilde{z}_{3c})$.
5. Using equation (18), calculate $(\zeta_{1c}, \zeta_{2c}, \zeta_{3c})$.
6. If rent arbitrage equation (22) is not satisfied, go back to step 3.
7. Calculate equilibrium wages as

$$W_c = \frac{\sum_i (1 - \beta_i) Y_{ic}}{N_c}$$

and using data on prices, recover

$$A_{ic} = \frac{\beta_i}{(1 - \beta_i)^{1-\beta_i}} \frac{W_c}{P_{ic}} \exp(\zeta_{ic}).$$

Table 3: Distribution of productivity components across cities

	Contribution to output per worker of productivity land per worker location		
Services	0.186	1.083	0.987
	0.683	1.433	1.135
Manufacturing	0.149	0.968	0.985
	0.706	1.316	1.097
Agriculture	0.123	0.880	0.958
	0.589	1.911	1.200

Notes: Table presents the 10th and 90th percentiles of contributions to output per worker. All contributions are expressed relative to New York. See text for the precise definition of decomposition.

3 Decomposition of output per worker

To evaluate the quantitative importance of our mechanism, we report the decomposition of output per worker (13) into a Hicks-neutral productivity term, land per worker, and the representative location of the industry. We express each component relative to New York, one of the richest cities in the sample.

Table 3 presents the distribution of productivity components across cities. For each sector and each productivity component, we report the 10th and 90th percentile of the component relative to New York. For example, the 10th percentile of Hicks-neutral productivity in the service sector is only 18.6 percent of that in New York. The productivity gap is similar in the three sectors.

The contribution of land per worker ranges between 108 and 143 percent for services, 97 and 132 percent for manufacturing, and 88 and 191 percent for agriculture. This is not surprising, as agriculture is the most land intensive of the three sectors and many cities are smaller than New York and have less agricultural land available.

The contribution of sector location is generally between 96 and 120 percent.

To see how land usage and city structure varies with development, we plot these productivity contributions against GDP per capita of the cities. Figure 4 shows the nonparametric relationship between productivity and GDP per capita, separately for each of the three sectors. Not surprisingly, richer cities are estimated to have higher productivity. The three sectoral productivities run in parallel, showing that technological differences across cities are unbiased. This is in contrast with Herrendorf and Valentinyi (2012), who find large heterogeneity in sectoral productivities.

Figure 5 shows the contribution of land per worker to output per worker, relative

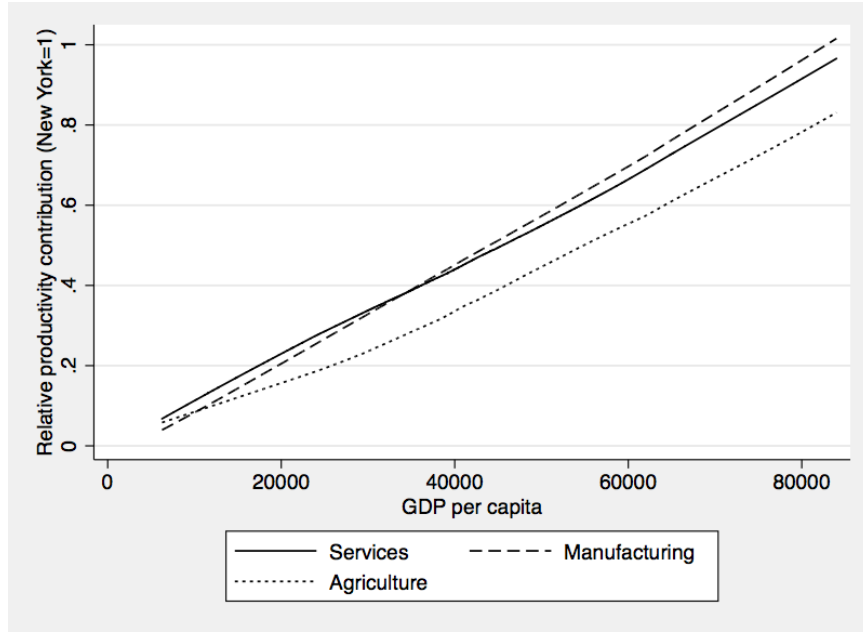


Figure 4: The contribution of productivity to output per worker

Notes: Figure presents the nonparametric relationship between city-level GDP per capita and sectoral productivity using locally weighted scatterplot smoothing. Productivity is expressed relative to that in New York.

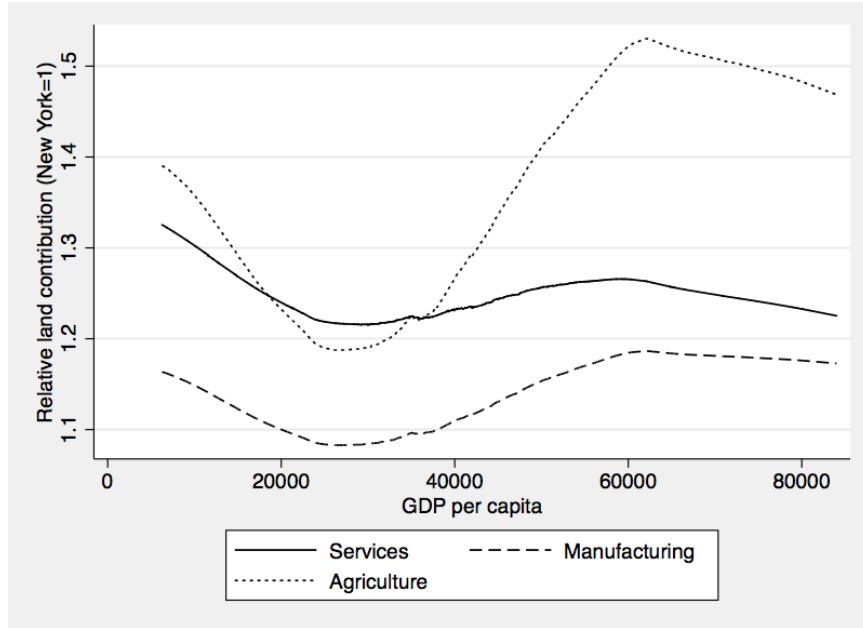


Figure 5: The contribution of land usage to output per worker

Notes: Figure presents the nonparametric relationship between city-level GDP per capita and the contribution of land usage to output per worker using locally weighted scatterplot smoothing. The contribution is expressed relative to that in New York.

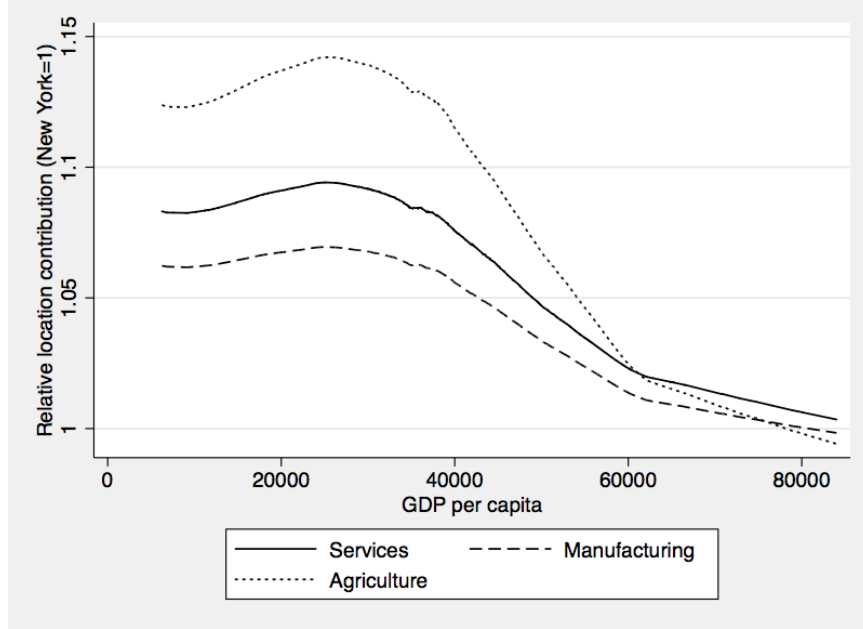


Figure 6: The contribution of sector location to output per worker

Notes: Figure presents the nonparametric relationship between city-level GDP per capita and the contribution of sector location to output per worker using locally weighted scatterplot smoothing. The contribution is expressed relative to that in New York.

to New York. Across the entire level of city GDP per capita, this contribution is less than one, because most cities are more densely populated than the New York metropolitan area. There is no clear tendency with development, but richer cities tend to have more land available for agriculture than for other sectors. This is because agricultural employment in these cities are smaller and they can use larger amounts of land on the city fringe.

Figure 6 plots the contribution of sector location to output per worker. For all cities this contribution is greater than in New York. This is because these cities tend to be smaller in area than New York, as is shown in Figure 7. For rich and large cities, the spatial sprawl reduces output per worker by about 10 percent in services and manufacturing, and even more in agriculture.

4 Conclusion

We introduced location choice in a multi-sector general equilibrium model. Producers in agriculture, manufacturing and services choose their location to trade off land rents with transport costs to the city center. We showed how space affects the aggregate production function and decompose output per worker into productivity, land per

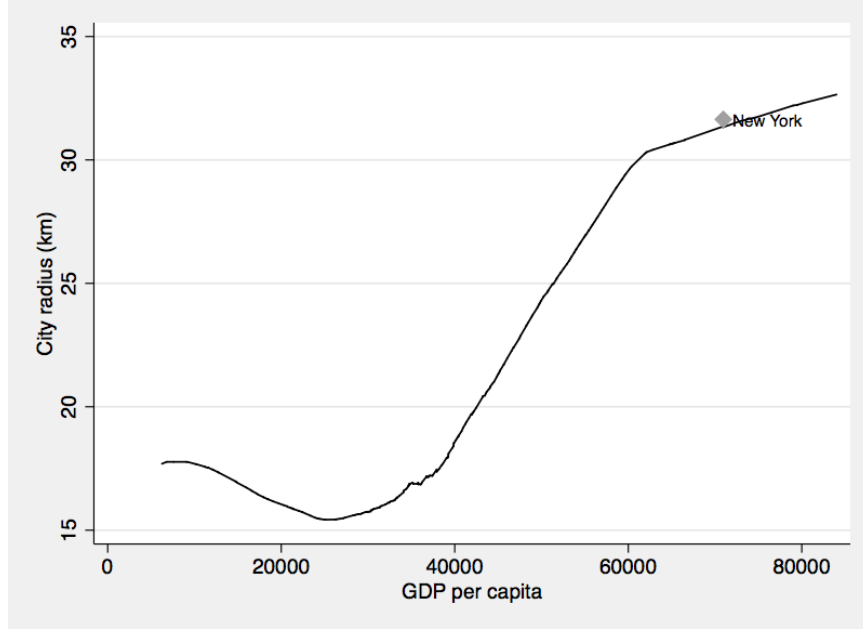


Figure 7: City radius and GDP per capita

Notes: Figure presents the nonparametric relationship between city-level GDP per capita and the radius of the city using locally weighted scatter plot smoothing. City radius is estimated using OECD data on city area and assuming circular cities.

worker, and a term adjusting for sector location. In our model, services are luxury goods. As a result, richer cities have larger service cores, higher service prices, and relatively less output per worker in services. These predictions are broadly consistent with the data. We calibrated our model to data on cities in OECD countries and showed that land and location explain 10–30 percentage points of the variation in output per worker.

In our calibration, sectoral productivities varied to the same extent across cities. This leaves less room for technology-based explanations as to why sectoral output per worker and sectoral prices vary with development.

We see two avenues for further research. First, the number and size of cities within countries can be endogenized to see how this contributes to aggregate outcomes (Desmet and Rossi-Hansberg 2013; Ramondo, Rodríguez-Clare, and Saborío-Rodríguez 2016). Second, urbanization patterns may be very different in less developed countries (Glaeser 2014; Harari 2016). The model can be calibrated to richer data on transport costs and land use across cities around the globe.

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Appendix

A Proofs

A.1 Proof of Proposition 1

We first show that the allocation of space across sectors follows a strict partitioning, and hence can be characterized by two cutoffs: z_1 denotes the boundary between services and manufacturing and z_2 denotes the boundary between manufacturing and agriculture. We then apply Brouwer's fixed point theorem to show there exist such equilibrium cutoffs.

First note that profit maximization requires $R_i(z) \geq R(z)$ for all industries and locations and a strict inequality implies that $Q_i(z) = 0$. Because the three bid-rent curves have different slopes, they can only intersect at a measure zero set of points. Hence all locations are used by a single industry, there is no mixed use.

The single-crossing property of bid-rent curves imply a strict partitioning. For any pair of sectors with $\tau_i/\beta_i > \tau_j/\beta_j$ we have $\sup\{z : Q_i(z) > 0\} \leq \inf\{z : Q_j(z) > 0\}$. That is, all sector i locations are closer to the CBD than any sector j location.

Equation (3) ensures positive demand for all three products so that all three sectors are active. The only such partitioning is where $\{z : Q_1(z) > 0\} = [0, z_1]$, $\{z : Q_2(z) > 0\} = (z_1, z_2]$ and $\{z : Q_3(z) > 0\} = (z_2, z_3]$. At these boundaries, a rent arbitrage condition holds:

$$R_i(z_i) = R_{i+1}(z_i). \quad (22)$$

To use Brouwer's fixed point theorem, construct the following mapping. Take a pair of $z_1 < z_2 \in [0, z_3]$. Denote the set of admissible z s by $Z = \{(z_1, z_2) : z_1 < z_2 \in [0, z_3]\}$, which is a compact and convex set. Let $W \equiv 1$ serve as the numeraire. Use the rent arbitrage condition at the boundaries (22) and the resource constraint for aggregate labor

$$N = \sum_{i=1}^3 \int_{z=z_{i-1}}^{z_i} (1 - \beta_i)^{1/\beta_i} (P_i A_i)^{1/\beta_i} e^{-z\tau_i/\beta_i} \bar{L}(z) dz,$$

to solve for prices P_1 , P_2 and P_3 . These prices are a continuous function of (z_1, z_2) . Given these prices, solve for utility-maximizing expenditure shares (x_1, x_2, x_3) . The total amount of rents payable to each sector can then be expressed, in relative terms, as

$$\frac{R_i}{R_j} = \frac{\beta_i x_i}{\beta_j x_j}.$$

Let (z'_1, z'_2) be the sector boundaries consistent with these relative rent amounts. Clearly, $(z'_1, z'_2) \in Z$ and the mapping is continuous. Applying Brouwer's fixed point

theorem, there exists a (z_1^*, z_2^*) such that $(z_1'^*, z_2'^*) = (z_1^*, z_2^*)$ and all equilibrium conditions hold with equality. Q.E.D.

A.2 Proof of Proposition 2

We will verify that when $d \ln A_i = \kappa$ for all i , $d \ln P_i = -\kappa$ is an equilibrium. Because resource allocations across sectors and space only depend on $P_i A_i$, these will not change. Output in each sector goes up by $d \ln Q_i = \kappa$. Because preferences are homothetic and relative prices have not changed, expenditure shares remain constant. They are hence still consistent with the equilibrium. Q.E.D.

A.3 Proof of Proposition 3

Let $d\mathbf{z}$ denote the 2×1 vector (dz_1, dz_2) , $d\mathbf{b}$ denote the 3×1 vector with elements $d \ln(P_i A_i / W) / \beta_i$, and $d\mathbf{q}$ denote the 3×1 vector with elements $d \ln(P_i Q_i / W)$.

Totally differentiating the production function (23) (below) yields

$$d\mathbf{q} - d\mathbf{b} = \mathbf{M}_1 d\mathbf{z},$$

where \mathbf{M}_1 is a 3×2 matrix,

$$\mathbf{M}_1 = \begin{bmatrix} e^{-z_1 \tau_1 / \beta_1} \bar{L}(z_1) / \tilde{L}_1 & 0 \\ -e^{-z_1 \tau_2 / \beta_2} \bar{L}(z_1) / \tilde{L}_2 & e^{-z_2 \tau_2 / \beta_2} \bar{L}(z_2) / \tilde{L}_2 \\ 0 & -e^{-z_2 \tau_3 / \beta_3} \bar{L}(z_2) / \tilde{L}_3 \end{bmatrix}.$$

Totally differentiating the rent arbitrage condition (22) yields

$$\mathbf{M}_2 d\mathbf{b} = d\mathbf{z},$$

where \mathbf{M}_2 is a 2×3 matrix,

$$\begin{bmatrix} \frac{1}{\tau_1 / \beta_1 - \tau_2 / \beta_2} & \frac{-1}{\tau_1 / \beta_1 - \tau_2 / \beta_2} & 0 \\ 0 & \frac{1}{\tau_2 / \beta_2 - \tau_3 / \beta_3} & \frac{-1}{\tau_2 / \beta_2 - \tau_3 / \beta_3} & 0 \end{bmatrix}.$$

Combining these two equilibrium conditions, we can express the changes in sector boundaries as a function of changes in sector shares,

$$d\mathbf{z} = \mathbf{M}_2 (\mathbf{I} + \mathbf{M}_1 \mathbf{M}_2)^{-1} d\mathbf{q} \equiv \mathbf{M}_3 d\mathbf{q}.$$

The 2×3 matrix \mathbf{M}_3 has the structure

$$\mathbf{M}_3 = \begin{bmatrix} \kappa_1 + \kappa_2 & -\kappa_1 & -\kappa_2 \\ \kappa_3 & \kappa_4 & -(\kappa_3 + \kappa_4) \end{bmatrix}$$

for some positive κ s.

Using equation (4) for the income elasticity of consumption in each of the three sectors, $dz_1/d \ln y > 0$ whenever

$$\sigma_1 > \frac{\kappa_1}{\kappa_1 + \kappa_2} \sigma_2 + \frac{\kappa_2}{\kappa_1 + \kappa_2} \sigma_3,$$

which holds for because $\sigma_1 > \sigma_2 > \sigma_3$.

Similarly, $dz_2/d \ln y > 0$ whenever

$$\sigma_3 < \frac{\kappa_3}{\kappa_3 + \kappa_4} \sigma_1 + \frac{\kappa_4}{\kappa_3 + \kappa_4} \sigma_2,$$

which holds for because $\sigma_1 > \sigma_2 > \sigma_3$. The amount of land usage and relative prices follow from the equilibrium conditions. Q.E.D.

A.4 Proof of Proposition 4

Let us express value added (measured at the center) at a location z per unit of land:

$$\frac{e^{-\tau_i z} Q_i(z)}{L_i(z)} = e^{-\tau_i z} A_i(z) \left(\frac{N_i(z)}{L_i(z)} \right)^{1-\beta_i} = (1 - \beta_i)^{1/\beta_i - 1} A_i^{1/\beta_i} \left(\frac{W}{P_i} \right)^{1-1/\beta_i} e^{-\frac{\tau_i}{\beta_i} z},$$

where we used equation 8 on employment density. From this, total supply of sector i becomes

$$\tilde{Q}_i = \int_{z \in Z_i} \frac{e^{-\tau_i z} Q_i(z)}{L_i(z)} L_i(z) dz = (1 - \beta_i)^{1/\beta_i - 1} (A_i)^{1/\beta_i} \left(\frac{W}{P_i} \right)^{1-1/\beta_i} L_i e^{-\frac{\tau_i}{\beta_i} \tilde{z}_i}. \quad (23)$$

by the definition of the representative location of the sector in equation 11.

Overall employment in the sector,

$$N_i = \int_{z \in Z_i} \frac{N_i(z)}{L_i(z)} L_i(z) dz = (1 - \beta_i)^{1/\beta_i} \left(\frac{P_i A_i}{W} \right)^{1/\beta_i} L_i e^{-\frac{\tau_i}{\beta_i} \tilde{z}_i},$$

so that we can express W/P_i as

$$\frac{W}{P_i} = (1 - \beta_i) N_i^{-\beta_i} A_i L_i^{\beta_i} e^{-\tau_i \tilde{z}_i}$$

Substituting this result to equation (23), we obtain the aggregate production function. Q.E.D.

Response to the Editor

Dear Diego,

Thank you for giving us the opportunity to revise our paper and for your and the referees' constructive comments. We believe the revised version has significantly improved and we hope you will find it acceptable for publication. Below we summarize the major changes, followed by a point-by-point reply to referees.

Cities vs countries . In our previous version, our analysis has jumped back and forth between cities and countries in a confusing manner. Both referees pointed out the restrictive assumptions needed to study cities in isolation.

To maintain the analytical tractability of our model, we have kept the baseline analysis at the city level. We have correspondingly reworded our Introduction (pages XX) to avoid overselling our results. We also added a new Section XX, which explicitly aggregates up the city-level results to the country level. Our language is still cautious here, as our baseline model has little to say about the system of cities within a country. [We added Appendix XX to illustrate how a richer model can be used to study multiple cities within the same country.]

Better connection to literature . We acknowledge the importance of earlier work in this literature and have rewritten the Introduction (pages XX) to carefully delineate our contribution. Indeed, the importance of land use, land restrictions and transport infrastructure for development has been highlighted by XX and XX. Our contribution is to study how the endogenous spatial sorting of sectors affects aggregate productivity.

Response to Referee 1

Response to Referee 2