# Lab 1

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## 11:59PM February 1

You should have RStudio installed to edit this file. You will write code in places marked "TO-DO" to complete the problems. Most of this will be a pure programming assignment but there are some questions that instead ask you to "write a few sentences". This is a W class! The tools for the solutions to these problems can be found in the class practice lectures. I prefer you to use the methods I taught you. If you google and find esoteric code you don't understand, this doesn't do you too much good.

To "hand in" the homework, you should first download this file. The best way to do this is by cloning the class repository then copying this file from the folder of that clone into the folder that is your personal class repository. Then do the assignment by filling in the TO-DO's. After you're done, compile this file into a PDF (use the "knit to PDF" button on the submenu above). This PDF will include output of your code. Then push the PDF and this Rmd file by the deadline to your github repository in a directory called "labs".

## Basic R Skills

• Print out the numerical constant pi with ten digits after the decimal point using the internal constant pi.

```
#the default in R is 7 decimal places, so we increase significant digits to 11
options(digits = 11)
pi
```

## ## [1] 3.1415926536

• Sum up the first 103 terms of the series  $1 + 1/2 + 1/4 + 1/8 + \dots$ 

```
#we create a vector with dim[103], and then sum all terms: sum(2^{(-(0:102))})
```

## ## [1] 2

• Find the product of the first 37 terms in the sequence 1/3, 1/6, 1/9 ...

```
#we create a vector with dim[37], and then multiply all terms
prod(1/(3*(1:37)))
```

### ## [1] 1.613528728e-61

• Find the product of the first 387 terms of 1 \* 1/2 \* 1/4 \* 1/8 \* ...

```
#we create a vector with dim[387], and then multiply all terms prod(2^{(-0:386)})
```

```
## [1] 0
```

Is this answer *exactly* correct?

No

• Figure out a means to express the answer more exactly. Not compute exactly, but express more exactly.

```
#we can express each term of the vector as log base ten, then, we use properties #of log to sum all log'ed terms sum(log10(2^{(-(0:386)))})
```

#### ## [1] -22484.231406

• Create the sequence x = [Inf, 20, 18, ..., -20].

```
#we concatenate Inf with the sequence from 20 to -20 by -2 x=c(1/0,seq(20,-20,by=-2))
```

Create the sequence  $x = [log_3(Inf), log_3(100), log_3(98), ... log_3(-20)].$ 

```
#we concatenate Inf with the sequence from 100 to -20 by -2, then we take log #base 3 of all terms x=\log(c(Inf,seq(100,-20,by=-2)),base=3)
```

#### ## Warning: NaNs produced

Comment on the appropriateness of the non-numeric values NAN and -Inf.

We are getting NaN for 0 and -Inf for negative inputs for log\_3. This is reasonable.

• Create a vector of booleans where the entry is true if x[i] is positive and finite.

```
x>0&is.finite(x)
```

```
[1] FALSE
                                                                      TRUE
                                                                            TRUE
               TRUE
                     TRUE
                           TRUE
                                 TRUE
                                       TRUE.
                                              TRUE.
                                                    TRUF.
                                                          TRUF.
                                                                TRUE
## [13]
         TRUE
               TRUE
                     TRUE
                           TRUE
                                 TRUE
                                        TRUE
                                              TRUE
                                                    TRUE
                                                          TRUE
                                                                TRUE
                                                                      TRUE
                                                                            TRUE
## [25]
               TRUE
                     TRUE
                           TRUE
                                 TRUE
                                                    TRUE
                                                          TRUE
                                                                TRUE
                                                                      TRUE
         TRUE
                                       TRUE
                                              TRUE
                                                                            TRUE
## [37]
         TRUE
               TRUE
                     TRUE
                          TRUE
                                 TRUE
                                       TRUE
                                             TRUE
                                                   TRUE
                                                          TRUE
                                                                TRUE
                                                                      TRUE
                                                                            TRUE
                     TRUE FALSE FALSE FALSE FALSE FALSE FALSE FALSE FALSE
## [49]
         TRUE
               TRUE
## [61] FALSE FALSE
```

• Locate the indices of the non-real numbers in this vector. Hint: use the which function. Don't hesitate to use the documentation via ?which.

```
#?which
which(is.infinite(x)|is.nan(x))
```

```
## [1] 1 52 53 54 55 56 57 58 59 60 61 62
```

• Locate the indices of the infinite quantities in this vector.

```
which(is.infinite(x))
```

```
## [1] 1 52
```

• Locate the indices of the min and max in this vector. Hint: use the which.min and which.max functions.

```
#?which.max
which.min(ifelse(is.infinite(x), NA, x))
```

```
## [1] 51
which.max(ifelse(is.infinite(x), NA, x))
```

```
## [1] 2
```

```
#second option
x_without_infs = ifelse(is.infinite(x), NA, x)
which.min(x_without_infs)
```

```
## [1] 51
which.max(x_without_infs)
## [1] 2
rm(x_without_infs)
#?Find
  • Count the number of unique values in x.
length(unique(x))
## [1] 53
  • Cast x to a factor. Do the number of levels make sense?
as.factor(x)
                           4.19180654857877
##
    [1] Inf
                                              4.1734172518943
                                                                 4.15464876785729
    [5] 4.13548512895119
                           4.11590933734319
                                              4.09590327428938
                                                                 4.07544759935851
    [9] 4.05452163806914
                           4.03310325630434
                                              4.01116871959141
                                                                 3.98869253500376
## [13] 3.96564727304425
                           3.94200336638929
                                              3.91772888178973
                                                                 3.89278926071437
## [17] 3.86714702345081
                           3.84076143030548
                                             3.81358809221559
                                                                 3.78557852142874
                                             3.69597450568212
  [21] 3.75667961082847
                           3.72683302786084
                                                                 3.66403300987579
   [25] 3.63092975357146
                           3.59657702661571
                                              3.56087679500731
                                                                 3.52371901428583
##
   [29] 3.48497958377173
                           3.44451784578705
                                             3.40217350273288
                                                                 3.3577627814323
   [33] 3.31107361281783
                           3.26185950714291
                                             3.20983167673402
                                                                 3.15464876785729
  [37] 3.09590327428938
                                              2.96564727304425
                           3.03310325630434
                                                                 2.89278926071437
       2.8135880922156
                           2.72683302786084
  [41]
                                              2.63092975357146
                                                                 2.52371901428583
## [45] 2.40217350273288
                          2.26185950714291
                                             2.09590327428938
                                                                 1.89278926071437
## [49] 1.63092975357146
                          1.26185950714291
                                             0.630929753571457 -Inf
## [53] NaN
                           NaN
                                              NaN
                                                                 NaN
## [57] NaN
                           NaN
                                              NaN
                                                                 NaN
## [61] NaN
                           NaN
## 53 Levels: -Inf 0.630929753571457 1.26185950714291 ... NaN
  • Cast x to integers. What do we learn about R's infinity representation in the integer data type?
as.integer(x)
## Warning: NAs introduced by coercion to integer range
```

```
##
    [1] NA
                                            3
                                                           3
                                                               3
                                                                  3
                                                                     3
                                                                        3
         3
            3
               3
                  3
                      3
                         3
                              3
                                  3
                                     3
                                        3
                                           3
                                               3
                                                  2
                                                     2
                                                        2
## [26]
                            3
                                                               2
         O NA NA NA NA NA NA NA NA NA NA
```

\*positive and negative infinity are represented by NA in the integer data type.

• Use x to create a new vector y containing only the real numbers in x.

```
y=x[is.finite(x)]
```

• Use the left rectangle method to numerically integrate x^2 from 0 to 1 with rectangle width size 1e-6.

```
delta_x=1e-6
sum((seq(0,1-delta_x,by=delta_x))^2)*delta_x
```

#### ## [1] 0.33333283333

• Calculate the average of 100 realizations of standard Bernoullis in one line using the sample function.

```
#?sample
x_bern=c(0,1)
mean(sample(x_bern,size=100, replace=TRUE))
```

#### ## [1] 0.59

• Calculate the average of 500 realizations of Bernoullis with p = 0.9 in one line using the sample and mean functions.

```
mean(sample(c(0,1),size=500, replace=TRUE, prob = c(0.1, 0.9)))
```

### ## [1] 0.914

• Calculate the average of 1000 realizations of Bernoullis with p = 0.9 in one line using rbinom.

```
mean(rbinom(n=1000,size=1,prob=0.9))
```

#### ## [1] 0.91

• Let n=50. Create a n x n matrix R of exactly 50% entries 0's, 25% 1's 25% 2's. These values should be in random locations.

```
vec = sample(c(rep(0,1250),rep(1,625),rep(2,625)))
R=matrix(vec,nrow=50,ncol=50)

table(c(R))

##
## 0 1 2
## 1250 625 625

#?matrix
```

• Randomly punch holes (i.e. NA) values in this matrix so that an each entry is missing with probability 30%.

```
R[runif(2500) <.3] = NA
R
```

```
[,4] [,5] [,6] [,7]
##
           [,1] [,2] [,3]
                                                       [,8] [,9] [,10] [,11] [,12] [,13]
##
     [1,]
               0
                    NA
                           2
                                 0
                                      NA
                                             NA
                                                    2
                                                           0
                                                                 1
                                                                         0
                                                                                1
                                                                                        2
                                                                                               2
##
     [2,]
               2
                     0
                           2
                                NA
                                        0
                                             NA
                                                    1
                                                           1
                                                                 0
                                                                       NA
                                                                                2
                                                                                      NA
                                                                                               2
                                                           2
##
    [3,]
               1
                    NA
                          NA
                                 0
                                       NA
                                             NA
                                                   NA
                                                                NA
                                                                       NA
                                                                               NA
                                                                                        0
                                                                                               0
##
    [4,]
               0
                     2
                           0
                                 2
                                        2
                                              0
                                                    1
                                                           0
                                                                 2
                                                                         1
                                                                               NA
                                                                                        1
                                                                                              NA
                           2
                                                    2
##
     [5,]
               1
                     0
                                NA
                                        0
                                              1
                                                         NA
                                                                         0
                                                                                2
                                                                                        0
                                                                                               0
                                                                 1
                                                                         2
##
    [6,]
               0
                     0
                           0
                                 2
                                        0
                                              0
                                                   NA
                                                         NA
                                                                 0
                                                                                1
                                                                                        0
                                                                                              NA
##
    [7,]
                     0
                                 2
                                        0
                                                                               NA
                                                                                        0
                                                                                              NA
             NA
                           1
                                             NA
                                                   NA
                                                           0
                                                                 1
                                                                       NA
    [8,]
                           2
                                                    2
                                                                                               2
##
               1
                                 0
                                        0
                                              2
                                                                 0
                                                                         0
                                                                                0
                                                                                      NA
                    NA
                                                           1
    [9,]
                     2
                           0
                                 2
                                                           2
                                                                                2
                                                                                        0
                                                                                               2
##
               0
                                        0
                                             NA
                                                    0
                                                                 0
                                                                       NA
                           0
## [10,]
               0
                     0
                                 0
                                        0
                                              1
                                                   NA
                                                           0
                                                                 2
                                                                         0
                                                                                1
                                                                                      NA
                                                                                              NA
## [11,]
                     2
                           2
                                              2
                                                           0
                                                                                               2
             NA
                                 1
                                        0
                                                   NA
                                                                NA
                                                                         1
                                                                                1
                                                                                      NA
## [12,]
               0
                           2
                                 0
                                              0
                                                    2
                                                                 0
                                                                         2
                                                                                2
                                                                                               0
                    ΝA
                                       NA
                                                           1
                                                                                        1
                                              0
                                                    2
                                                                         0
                                                                                               0
## [13,]
               0
                     0
                           1
                                NA
                                        0
                                                         NA
                                                                NA
                                                                                1
                                                                                      NA
               2
                                                                         2
                                                                                               2
## [14,]
                                              1
                                                                                        2
                    ΝA
                           1
                                NA
                                       NA
                                                   NA
                                                           0
                                                                 2
                                                                               NA
## [15,]
               2
                    NA
                          NA
                                NA
                                      NA
                                              0
                                                    2
                                                         NA
                                                                 1
                                                                         1
                                                                                0
                                                                                      NA
                                                                                              NA
               2
## [16,]
                     0
                          NA
                                 1
                                        1
                                              0
                                                    0
                                                         NA
                                                                 0
                                                                         0
                                                                                0
                                                                                      NA
                                                                                               1
## [17,]
               1
                     1
                           2
                                 1
                                      NA
                                             NA
                                                    0
                                                           2
                                                                NA
                                                                       NA
                                                                                0
                                                                                        0
                                                                                               1
                           0
                                                                                               2
## [18,]
               0
                     0
                                NA
                                        0
                                              0
                                                    1
                                                           0
                                                                 0
                                                                         0
                                                                               NA
                                                                                      NA
## [19,]
                     0
                          NA
                                                    2
                                                           0
                                                                         0
                                                                                0
                                                                                               2
             NA
                                 1
                                      NA
                                             NA
                                                                 1
                                                                                      NA
```

##	[20,]	NA	NA	NA	1	NA	NA	1	0	0	0	2	NA	NA
##	[21,]	0	1	NA	0	0	0	NA	1	NA	0	NA	NA	NA
##	[22,]	NA	2	NA	0	0	1	1	0	0	2	2	1	1
##	[23,]	0	0	NA	0	2	1	NA	0	NA	0	0	0	1
##	[24,]	2	0	2	0	1	2	2	0	1	1	NA	NA	1
##	[25,]	NA	1	0	NA	1	0	1	0	2	1	0	2	NA
##	[26,]	0	2	2	2	0	0	NA	0	0	NA	0	NA	0
##	[27,]	0	0	NA	0	0	1	NA	NA	NA	2	NA	2	0
##	[28,]	1	1	NA	NA	1	2	NA	0	2	NA	NA	2	0
##	[29,]	2	2	0	0	0	NA	NA	1	NA	0	NA	2	NA
##	[30,]	0	NA	0	1	0	2	NA	0	1	0	2	NA	0
##	[31,]	NA	0	0	0	NA	NA	0	NA	NA	2	2	1	0
##	[32,]	0	NA	0	2	2	1	1	0	2	0	2	NA	1
##	[33,]	NA	NA	2	NA	1	0	0	0	NA	0	NA	1	0
##	[34,]	1	1	NA	1	NA	1	0	NA	NA	1	0	0	0
##	[35,]	2	0	1	NA	2	2	0	2	0	2	0	1	0
##	[36,]	NA	1	2	0	0	0	NA	0	2	0	NA	0	0
##	[37,]	1	0	2	NA	NA	2	NA	0	NA	NA	NA	0	2
##	[38,]	1	0	2	2	NA	0	NA	0	1	NA	NA	NA	NA
##	[39,]	2	NA	2	NA	NA	0	NA	2	NA	0	0	0	0
##	[40,]	NA	NA	NA	0	NA	NA	0	0	1	NA	0	NA	NA
##	[41,]	0	1	NA	0	NA	0	NA	NA	0	NA	0	0	2
##	[42,]	2	0	0	NA	0	0	0	2	NA	0	0	0	0
##	[43,]	NA	1	1	0	1	2	0	1	NA	0	1	1	2
##	[44,]	NA	2	NA	2	0	0	1	NA	0	1	NA	0	0
##	[45,]	0	0	NA	NA	NA	NA 1	NA	NA	NA	0	2	0	0
##	[46,]	0	0 2	2 2	0 M A	NA 2	1	0	0 2	0	2 1	1 0	2 1	1 N A
## ##	[47,] [48,]	0 1	1	NA	NA O	0	2	0	1	NA	NA	0	1	NA 1
##	[49,]	0	NA	0	NA	2	2	1	0	0	NA	0	2	0
##	[50,]	2	NA	NA	1	NA	0	1	NA	1	2	0	NA	0
##	[00,]	[,14]	[,15]				,18]	[,19]	[,20]	[,21]	[,22]	[,23]	[,24]	[,25]
##	[1,]	0	1		NA	1	NA	NA	NA	NA	NA	0	0	NA
##	[2,]	0	1	_	0	2	0	NA	NA	2		2	NA	1
##	[3,]	2	0		0	1	0	0	NA	NA		2	NA	0
##	[4,]	1	1		1	NA	NA	1	0	NA		0	1	2
##	[5,]	1	2	1	NΑ	0	NA	0	NA	0	0	NA	2	1
##	[6,]	NA	NA	1	NΑ	NA	NA	NA	0	NA	1	0	NA	0
##	[7,]	2	NA	1	NA	NA	1	NA	0	NA	2	NA	1	2
##	[8,]	2	0	1	NΑ	0	NA	0	0	NA	NA	0	0	1
##	[9,]	2	NA		2	NA	1	NA	0	0	1	NA	0	0
##	[10,]	1	2		0	2	1	1	1	0	0	0	NA	0
##	[11,]	0	1		2	NA	NA	NA	0	0	2		NA	0
##	[12,]	1	NA	1	NΑ	0	1	NA	0	NA	0	0	0	NA
##	[13,]	2	0		1	NA	2	1	0	0	NA		0	NA
##	[14,]	1	0		0	0	0	2	0	1	1	0	0	NA
##	[15,]	NA	NA	_	2	NA	2	1	NA	NA	NA		NA	1
##	[16,]	NA	2		NA.	0	0	1	0	0	0	NA	0	2
##	[17,]	2	1	1	AV	1	2	NA	0	0	0	1	2	NA
##	[18,]	1	2		2	2	NA	NA	0	NA	NA		1	0
##	[19,]	0	0	,	2	NA 1	2	1 NA	0	1	1 NA	1	NA	0
##	[20,]	0	O M A	1	AV	1 N A	0	NA	1 NA	0	NA	1	0	0
##	[21,] [22,]	O N A	NA NA		2	NA	O M A	O M A	NA 1	O M A	O M A	1	O M A	0
##	LZZ,]	NA	NA		1	0	NA	NA	1	NA	NA	0	NA	0

##	[23,]	NA	1	2	NA	NA	0	0	0	NA	1	0	0
##	[24,]	0	NA	2	2	0	1	1	NA	0	1	2	2
##	[25,]	0	NA	2	NA	0	2	1	NA	0	NA	0	NA
##	[26,]	NA	1	0	0	0	NA	0	0	0	0	0	NA
##	[27,]	NA	0	NA	1	1	NA	1	0	1	0	2	1
##	[28,]	1	2	0	1	0	1	2	1	0	NA	NA	NA
##	[29,]	NA	0	NA	0	NA	2	0	NA	0	0	NA	2
##	[30,]	1	NA	2	0	NA	NA	0	0	NA	2	0	NA
##	[31,]	0	2	1	NA	2	0	0	0	0	2	1	0
##	[32,]	NA	1	NA	0	0	NA	NA	1	NA	NA	NA	0
##	[33,]	0	NA	2	NA	1	2	0	0	1	0	NA	2
##	[34,]	2	0	0	0	0	0	1	NA	1	NA	NA	0
##	[35,]	1	1	2	0	NA	2	NA	2	2	0	NA	NA
##	[36,]	1	NA	0	0	1	1	2	0	NA	NA	1	NA
## ##	[37,]	2	0	0	0	0	0	NA NA	0	NA O	1 1	1	0
##	[38,] [39,]	1	1 NA	0	2	0	1 2	NA NA	NA	1	2	1	2
##	[40,]	NA	2	NA	2	1	1	NA	0	0	1	NA	NA
##	[41,]	2	1	NA	0	1	2	NA NA	NA	0	2	NA NA	2
##	[42,]	2	NA	2	NA	0	0	NA	1	NA	2	1	0
##	[43,]	2	NA	0	NA	NA	2	NA	0	NA	2	2	1
##	[44,]	NA	1	0	0	NA	0	NA	NA	0	0	0	1
##	[45,]	0	1	1	0	1	1	NA	1	0	0	NA	NA
##	[46,]	2	NA	0	1	NA	2	0	2	0	NA	1	1
##	[47,]	2	NA	NA	0	NA	NA	NA	NA	NA	0	0	NA
##	[48,]	0	1	NA	0	0	0	0	0	0	0	1	2
##	[49,]	NA	2	0	0	0	0	NA	1	1	0	NA	0
##	[50,]	NA	1	NA	2	2	0	2	1	2	0	0	NA
## ##	[50,]	NA [,26]	1 [,27]	NA [,28]		2 [,30]		2 [,32]	1 [,33]	2 [,34]		0 [,36]	NA [,37]
	[50,]												
##	[1,] [2,]	[,26] NA 2	[,27] 1 1	[,28] NA 1	[,29]	[,30]	[,31] NA 1	[,32] NA NA	[,33]	[,34] 1 1	[,35] NA O	[,36] NA O	[,37] 1 2
## ##	[1,] [2,] [3,]	[,26] NA 2 0	[,27] 1 1 0	[,28] NA 1 2	[,29] 1 NA 1	[,30] 0 0 1	[,31] NA 1 NA	[,32] NA NA 2	[,33] 0	[,34] 1 1 1	[,35] NA 0	[,36] NA 0 2	[,37] 1 2 2
## ## ## ##	[1,] [2,] [3,] [4,]	[,26] NA 2 0 NA	[,27] 1 1 0 NA	[,28] NA 1 2 NA	[,29] 1 NA 1 0	[,30] 0 0 1 0	[,31] NA 1 NA 0	[,32] NA NA 2	[,33] 0 0 NA 0	[,34] 1 1 1 0	[,35] NA O O NA	[,36] NA 0 2 2	[,37] 1 2 2 2
## ## ## ## ##	[1,] [2,] [3,] [4,] [5,]	[,26] NA 2 0 NA 0	[,27] 1 1 0 NA 0	[,28] NA 1 2 NA NA	[,29] 1 NA 1 0 NA	[,30] 0 0 1 0 2	[,31] NA 1 NA O	[,32] NA NA 2 2	0 0 NA 0 1	[,34] 1 1 1 0 NA	[,35] NA O O NA NA	[,36] NA 0 2 2	[,37]     1     2     2     0     2
## ## ## ## ## ##	[1,] [2,] [3,] [4,] [5,] [6,]	[,26] NA 2 0 NA 0	[,27] 1 1 0 NA 0	[,28] NA 1 2 NA NA	[,29] 1 NA 1 0 NA 1	[,30] 0 0 1 0 2 NA	[,31] NA 1 NA O NA	[,32] NA NA 2 2 0	[,33] 0 0 NA 0 1	[,34] 1 1 0 NA 0	[,35] NA O O NA NA	[,36] NA 0 2 2 0 0	[,37] 1 2 2 0 2 NA
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## ## ## ## ## ## ## ## ## ## ## ## ##	[1,] [2,] [3,] [4,] [5,] [6,] [7,] [8,] [9,] [10,] [11,] [12,] [13,]	[,26] NA 2 0 NA 0 1 NA 0 NA NA NA 2	[,27]  1  0  NA  0  2  0  0  2  2  2	[,28] NA 1 2 NA NA 0 NA 0 2 0	[,29] 1 NA 1 0 NA 1 NA 1 NA 1 NA 1 0 NA 2	[,30] 0 0 1 0 2 NA 0 NA 0 0 2	[,31] NA 1 NA 0 NA NA 1 NA 1 0 1	[,32] NA NA 2 2 0 0 0 0 0 0 0 NA	[,33] 0 0 NA 0 1 0 2 2 2 0 1 NA	[,34] 1 1 0 NA 0 2 1 2 0 NA 2 2	[,35] NA O NA NA NA O O NA 1 O 2	[,36] NA 0 2 2 0 0 0 2 0 NA 0 0 2 NA	[,37] 1 2 2 0 2 NA 2 NA 0 0 1
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## ## ## ## ## ## ## ## ## ## ## ## ##	[1,] [2,] [3,] [4,] [5,] [6,] [7,] [8,] [9,] [10,] [11,] [12,] [13,] [14,] [15,] [16,]	[,26] NA 2 0 NA 0 1 NA 0 NA NA 2 1 2 0	[,27]  1  0  NA  0  0  2  0  0  2  2  1  0	[,28] NA 1 2 NA NA 0 NA 0 2 0 1 0 2 NA	[,29] 1 NA 1 0 NA 1 NA 1 NA 1 0 NA 1 2 1	[,30] 0 0 1 0 2 NA 0 0 0 2 NA 0 0 1 0 1 0 0 1 0 0 0 0 0 0 0 0 0 0 0 0 0	[,31] NA 1 NA 0 NA NA 1 NA 1 0 1 NA 2 2 NA	[,32] NA NA 2 2 0 0 0 0 0 0 NA NA 2 2 2 2 0 0 0 0 0 0 0 0 0 0 0 0 0	[,33] 0 0 NA 0 1 0 2 2 2 0 1 NA 1 NA 1	[,34] 1 1 0 NA 0 2 1 2 0 NA 2 2 1 2 1 1 2 1 1 1 1 1 1 1 1 1 1 1 1	[,35] NA O O NA NA O O NA 1 O 2 O 1	[,36] NA 0 2 2 0 0 NA 0 0 2 NA NA NA 2	[,37] 1 2 2 0 2 NA 2 NA 0 0 1 0 NA 0 1
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## ###################################	[1,] [2,] [3,] [4,] [5,] [6,] [7,] [8,] [9,] [10,] [11,] [12,] [13,] [14,] [15,] [16,] [17,]	[,26] NA 2 0 NA 0 1 NA 0 NA NA 2 1 2 0 0	[,27]  1  0  NA  0  0  2  0  0  2  2  1  0  1  1  1	[,28] NA 1 2 NA NA 0 NA 0 2 0 1 0 2 NA 1 NA	[,29] 1 NA 1 0 NA 1 NA 1 0 NA 1 2 1 2 NA 0	[,30] 0 0 1 0 2 NA 0 0 0 2 NA 0 0 1 0 0 0 0 0 0 0 0 0 0 0 0 0	[,31] NA 1 NA 0 NA NA 1 NA 1 0 1 NA 2 2 NA	[,32] NA NA 2 2 0 0 0 0 2 0 0 NA NA 2 2 2 2 2 2 3 4 5 6 7 8 8 8 8 8 8 8 8 8 8 8 8 8	[,33] 0 0 NA 0 1 0 2 2 2 0 1 NA 1 NA 1 0 2	[,34]  1  1  0  NA  0  2  1  2  0  NA  2  1  NA	[,35] NA O O NA NA NA O O NA 1 O 2 O 1 O O	[,36] NA 0 2 2 0 0 NA 0 0 2 NA NA 2 NA 1	[,37] 1 2 2 0 2 NA 2 NA 0 0 1 0 NA 0 1 1 0
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######################################	[1,] [2,] [3,] [4,] [5,] [6,] [7,] [8,] [10,] [11,] [12,] [13,] [14,] [15,] [16,] [17,] [18,] [19,]	[,26] NA 2 0 NA 0 1 NA 0 NA NA 2 1 2 0 0 NA NA	[,27]  1  0  NA  0  2  0  0  2  2  1  1  0  1  2  0  1  2  0	[,28] NA 1 2 NA NA NA 0 NA 0 2 0 1 0 2 NA 1 NA 0	[,29] 1 NA 1 0 NA 1 NA 1 NA 1 0 NA 1 0 NA NA 0 0 0 0	[,30] 0 0 1 0 2 NA 0 0 0 2 NA 0 0 1 0 0 1 0 1 0 0 0 0 0 0 0 0 0 0 0 0 0	[,31] NA 1 NA 0 NA NA 1 NA 1 0 1 NA 2 2 NA NA	[,32] NA NA 2 2 0 0 0 0 0 0 0 NA NA 2 2 0 0 0 0 0 0 0 0 0 0 0 0 0	[,33] 0 0 NA 0 1 0 2 2 0 1 NA 1 NA 1 0 2 NA 0 1	[,34]  1 1 0 NA 0 2 1 2 0 NA 2 1 NA 2 0 1 NA 2 0 0	[,35]     NA     O     O     NA     NA     O     O     NA     NA     1     O     2     O     1     O     NA     NA     O	[,36] NA 0 2 2 0 0 0 2 0 NA 0 0 2 NA NA 2 NA 1 NA 0	[,37] 1 2 2 0 2 NA 2 NA 0 0 1 0 NA 0 1 1 0 2
######################	[1,] [2,] [3,] [4,] [5,] [6,] [7,] [8,] [9,] [10,] [11,] [12,] [14,] [15,] [16,] [17,] [18,] [19,] [20,]	[,26] NA 2 0 NA 0 1 NA 0 NA NA 2 1 2 0 0 NA NA NA NA NA NA O NA NA O NA NA O NA NA O O NA NA O O O O O O O O O O O O O	[,27]  1  1  0  NA  0  0  2  0  0  1  2  1  0  1  2  NA	[,28] NA 1 2 NA NA 0 NA 0 2 0 1 0 2 NA 1 NA 0 0	[,29] 1 NA 1 0 NA 1 NA 1 NA 1 0 NA 1 0 NA 0 NA	[,30] 0 0 1 0 2 NA 0 0 0 2 NA 0 0 1 0 1 0 1 1 0 1 1 1 1 1 1 1 1 1 1 1 1 1	[,31] NA 1 NA 0 NA NA 1 NA 1 0 1 NA 2 2 NA NA 0 1	[,32] NA NA 2 2 0 0 0 0 0 0 0 NA NA 2 2 0 0 0 NA NA 0 0 0 0 0 0 0 0 0 0 NA NA NA NA NA NA NA NA NA NA	[,33] 0 0 NA 0 1 0 2 2 2 0 1 NA 1 NA 1 0 2 NA 0 0 1 0 0 1 0 0 1 0 0 0 0 0 0 0 0 0 0 0 0 0	[,34]  1 1 0 NA 0 2 1 2 0 NA 2 1 NA 2 0 NA 2 0 NA NA	[,35]     NA     O     O     NA     NA     O     O     NA     NA     1     O     2     O     1     O     NA     NA     O     NA     NA	[,36] NA 0 2 2 0 0 2 0 NA 0 2 NA NA 2 NA 1 NA 0	[,37] 1 2 2 0 2 NA 2 NA 0 0 1 0 NA 0 1 1 0 2 NA
#####################	[1,] [2,] [3,] [4,] [5,] [6,] [7,] [8,] [10,] [11,] [12,] [14,] [15,] [16,] [17,] [18,] [19,] [20,] [21,]	[,26] NA 2 0 NA 0 1 NA 0 NA NA NA NA NA 0 NA NA NA 0 NA	[,27]  1  0  NA  0  0  2  0  0  2  2  1  0  1  2  NA  2	[,28] NA 1 2 NA NA NA 0 NA 0 2 0 1 0 2 NA 1 NA 0 0 2 0 2 0 1 0 2 0 2 0 1 0 2 0 2 0 1 0 2 0 2	[,29] 1 NA 1 0 NA 1 NA 1 0 NA 1 0 NA 0 0 0 0 0 0	[,30] 0 0 1 0 2 NA 0 0 0 2 NA 0 1 0 1 0 1 0 1 0 1 0 0 0 0 0 0 0 0 0 0 0 0 0	[,31] NA 1 NA 0 NA NA 1 NA 1 0 1 NA 2 2 NA NA 0 1 NA 0 1 NA 1 0 1 NA 1 0 1 0 1 0 1 0 1 0 0 1 0 0 0 0 0 0 0 0 0 0 0 0 0	[,32] NA NA 2 2 0 0 0 0 0 0 0 0 0 0 0 0 0	[,33] 0 0 NA 0 1 0 2 2 2 0 1 NA 1 NA 1 0 2 NA 0 1 0 2 2 0 0 1 0 0 0 1 0 0 0 0 0 0 0 0 0 0 0 0 0	[,34]  1 1 0 NA 0 2 1 2 0 NA 2 1 NA 2 0 NA 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0	[,35] NA O O NA NA O O NA NA O O NA O O NA O O NA O O O O	[,36] NA 0 2 2 0 0 2 0 NA 0 2 NA NA 2 NA 1 NA 0 1 NA	[,37] 1 2 2 0 2 NA 2 NA 0 0 1 0 NA 0 1 1 0 2 NA 2
########################	[1,] [2,] [3,] [4,] [5,] [6,] [7,] [8,] [9,] [10,] [11,] [12,] [13,] [15,] [16,] [17,] [18,] [19,] [20,] [21,] [22,]	[,26] NA 2 0 NA 0 1 NA 0 NA NA 2 1 2 0 0 NA NA NA NA NA NA NA NA NA NA	[,27]  1  0  NA  0  0  2  0  0  2  2  1  0  1  2  1  0  NA  2  1	[,28] NA 1 2 NA NA 0 NA 0 2 0 1 0 2 NA 1 NA 0 2 2 2 NA 0 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2	[,29] 1 NA 1 0 NA 1 NA 1 0 NA 1 0 NA 0 0 NA NA 0 0 0 0 0 0 NA	[,30] 0 0 1 0 2 NA 0 0 0 2 NA 0 1 0 1 0 1 0 1 1 0 1 0 1 0 1 0 0 0 0 0 0 0 0 0 0 0 0 0	[,31] NA 1 NA 0 NA NA 1 NA 1 0 1 NA 2 2 NA NA NA 1 NA 1 0 1 NA 1 0 1 NA 1 0 1 0 1 0 1 0 1 0 1 0 1 0 1 0 1 0 1 0 1 0 1 0 1 0 1 0 1 0 1 0 1 0 1 0 0 0 0 0 0 0 0 0 0 0 0 0	[,32] NA NA 2 2 0 0 0 0 0 0 0 0 NA NA 2 2 0 0 NA NA 2 0 0 0 0 0 0 0 0 0 0 0 0 0	[,33] 0 0 NA 0 1 0 2 2 2 0 1 NA 1 NA 1 0 2 NA 0 0 1 0 0 2 2 0 0 1 0 0 0 0 0 0 0 0 0 0 0 0 0	[,34]  1 1 0 NA 0 2 1 2 0 NA 2 2 1 NA 2 0 NA 0 0 0 0	[,35] NA O O NA NA O O NA NA O O NA O O NA O O O O	[,36] NA 0 2 2 0 0 NA 0 0 2 NA NA 2 NA 1 NA 0 1 NA	[,37] 1 2 2 0 2 NA 2 NA 0 0 1 0 NA 0 1 1 0 2 NA 2 1

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##	[27,]	1	0	2	NA	0	2	2	2	2	NA	0	NA
##	[28,]	NA	0	NA	0	2	1	1	0	1	2	1	NA
##	[29,]	0	0	NA	1	NA	NA	2	0	0	0	1	1
##	[30,]	2	2	1	0	NA	2	NA	NA	0	2	1	1
##	[31,]	NA	0	1	NA	0	NA	0	1	1	1	1	1
##	[32,]	NA	0	0	0	NA	0	NA	0	2	2	1	2
##	[33,]	2	0	1	0	NA	0	NA	2	NA	NA	1	NA
##	[34,]	0	0	NA	NA	1	NA	1	0	1	NA	2	2
##	[35,]	0	2	0	NA	2	0	0	NA	1	0	0	2
##	[36,]	NA	NA	0	2	0	NA	NA	0	NA	1	2	0
##	[37,]	2	0	0	NA	NA	NA	0	1	0	2	0	0
##	[38,]	NA	0	0	NA	1	0	0	0	0	0	NA	0
##	[39,]	1	NA	NA	0	1	NA	NA	2	0	NA	1	2
## ##	[40,]	0 1	2 NA	O	0 2	0	1 N A	NA NA	NA 1	O M A	1 NA	NA O	NA 1
##	[41,] [42,]	1	NA O	NA NA	NA	1	NA 1	NA NA	1	NA O	NA O	1	NA
##	[43,]	0	0	2	1	0	2	2	NA	NA	NA	NA	0
##	[44,]	1	0	0	0	NA	0	1	1	0	0	0	0
##	[45,]	NA	2	1	0	0	0	0	0	NA	0	2	0
##	[46,]	2	0	NA	0	0	0	0	1	0	2	2	0
##	[47,]	0	0	2	0	0	1	NA	NA	1	NA	0	0
##	[48,]	0	NA	2	2	1	NA	0	1	NA	0	NA	2
##	[49,]	0	2	1	1	NA	NA	2	1	2	0	1	NA
##	[50,]	2	1	0	NA	2	0	0	1	1	NA	1	2
##	- •-	[,38]	[,39]	[,40]	[,41]	[,42]	[,43]	[,44]	[,45]	[,46]	[,47]	[,48]	[,49]
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##	[2,]	0	0	1	2	NA	NA	NA	0	NA	0	2	1
##	[3,]	1	0	0	0	1	0	NA	0	0	2	1	0
##												_	U
	[4,]	2	2	NA	NA	0	1	NA	2	0	NA	2	1
##	[5,]	NA	1	NA NA	0	0	2		2 1	NA	NA 1	2 NA	1 0
##	[5,] [6,]	NA NA	1 0	NA NA	0	0 1	2 1	NA NA NA	2 1 NA	NA NA	NA 1 2	2 NA 1	1 0 1
## ##	[5,] [6,] [7,]	NA NA 1	1 0 1	NA NA 2	0 0 2	0 1 1	2 1 1	NA NA NA 2	2 1 NA 0	NA NA NA	NA 1 2 NA	2 NA 1 2	1 0 1 0
## ## ##	[5,] [6,] [7,] [8,]	NA NA 1 O	1 0 1 NA	NA NA 2 NA	0 0 2 2	0 1 1 1	2 1 1 NA	NA NA NA 2 O	2 1 NA O NA	NA NA NA	NA 1 2 NA 0	2 NA 1 2 1	1 0 1 0 NA
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## ## ## ##	[5,] [6,] [7,] [8,] [9,] [10,]	NA NA 1 O NA NA	1 0 1 NA NA 2	NA NA 2 NA 1 0	0 0 2 2 0 2	0 1 1 1 0 0	2 1 1 NA 0 0	NA NA NA 2 O 1 NA	2 1 NA O NA NA	NA NA NA NA NA	NA 1 2 NA 0 NA 2	2 NA 1 2 1 1 NA	1 0 1 0 NA 0 NA
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## ## ## ## ## ##	[5,] [6,] [7,] [8,] [9,] [10,] [11,] [12,] [13,] [14,]	NA NA 1 O NA NA O NA 2	1 0 1 NA NA 2 NA NA 0	NA NA 2 NA 1 0 1 2	0 0 2 2 0 2 0 1 1	0 1 1 1 0 0 1 NA 1	2 1 1 NA 0 0 2 NA 0	NA NA 2 0 1 NA 0 0	2 1 NA 0 NA NA 0 1 0 2	NA NA NA NA O O 1	NA 1 2 NA 0 NA 2 0 1 0 0	2 NA 1 2 1 1 NA NA 0 NA	1 0 1 0 NA 0 NA NA 0 NA
## ## ## ## ## ## ##	[5,] [6,] [7,] [8,] [9,] [10,] [11,] [12,] [13,] [14,] [15,]	NA 1 0 NA NA 0 NA 2 2 2	1 0 1 NA NA 2 NA NA 0 NA	NA NA 2 NA 1 0 1 2 1 0	0 0 2 2 0 2 0 1 1 1 NA	0 1 1 1 0 0 1 NA 1 0	2 1 1 NA 0 0 2 NA 0 0	NA NA 2 0 1 NA 0 0 1 NA	2 1 NA 0 NA 0 1 0 2 1 2	NA NA NA NA O O O 1 2 O	NA 1 2 NA 0 NA 2 0 1 0 0 NA	2 NA 1 2 1 NA NA 0 NA 0	1 0 1 0 NA 0 NA NA 0 NA
## ## ## ## ## ## ##	[5,] [6,] [7,] [8,] [9,] [10,] [11,] [12,] [13,] [14,] [15,] [16,]	NA 1 0 NA NA 0 NA 2 2 NA	1 0 1 NA NA 2 NA NA 0 NA 2	NA NA 2 NA 1 0 1 2 1 0 2 2	0 0 2 2 0 2 0 1 1 1 NA	0 1 1 1 0 0 1 NA 1 0 0	2 1 1 NA 0 0 2 NA 0 0	NA NA 2 0 1 NA 0 0 1 NA	2 1 NA 0 NA NA 0 1 0 2 1 2	NA NA NA NA O O 1 2 O O	NA 1 2 NA 0 NA 2 0 1 0 0 NA 2	2 NA 1 2 1 1 NA NA 0 NA 0 2 2	1 0 1 0 NA 0 NA NA 0 NA
## ## ## ## ## ## ##	[5,] [6,] [7,] [8,] [9,] [10,] [11,] [12,] [13,] [14,] [15,] [16,] [17,]	NA	1 0 1 NA NA 2 NA NA 0 NA 2	NA NA 2 NA 1 0 1 2 1 0	0 0 2 2 0 2 0 1 1 1 NA	0 1 1 1 0 0 1 NA 1 0	2 1 1 NA 0 0 2 NA 0 0	NA NA 2 0 1 NA 0 0 1 NA	2 1 NA 0 NA 0 1 0 2 1 2	NA NA NA NA O O O 1 2 O	NA 1 2 NA 0 NA 2 0 1 0 0 NA	2 NA 1 2 1 NA NA 0 NA 0	1 0 1 0 NA 0 NA NA 0 NA 0 NA
## ## ## ## ## ## ##	[5,] [6,] [7,] [8,] [9,] [10,] [11,] [12,] [13,] [14,] [15,] [16,] [17,] [18,]	NA 1 0 NA NA 0 NA 2 2 NA	1 0 1 NA NA 2 NA NA 0 NA 2	NA NA 2 NA 1 0 1 2 1 0 2 2	0 0 2 2 0 1 1 1 NA 0 2	0 1 1 1 0 0 1 NA 1 0 0	2 1 1 NA 0 0 2 NA 0 0 0 2	NA NA 2 0 1 NA 0 0 1 NA 1 NA 2	2 1 NA 0 NA NA 0 1 0 2 1 2 NA 0	NA NA NA NA O O O 1 2 O O O	NA 1 2 NA 0 NA 2 0 1 0 NA 2 0 NA 2 0 0	2 NA 1 2 1 1 NA NA 0 NA 0 NA 2 2	1 0 1 0 NA 0 NA NA 0 NA
## ## ## ## ## ## ##	[5,] [6,] [7,] [8,] [9,] [10,] [11,] [12,] [13,] [14,] [15,] [16,] [17,]	NA	1 0 1 NA NA 2 NA NA 0 NA 2 0	NA 2 NA 1 0 1 2 1 0 2 2 0 0 0	0 0 2 2 0 1 1 1 NA 0 2 NA	0 1 1 1 0 0 1 NA 1 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0	2 1 1 NA 0 0 2 NA 0 0 0 2 0 0	NA NA 2 0 1 NA 0 0 1 NA 1 NA 2 0	2 1 NA 0 NA NA 0 1 0 2 1 2 NA 0	NA NA NA NA O O O 1 2 O O O 2	NA 1 2 NA 0 NA 2 0 0 NA 2 0 NA 2 0 NA 2 0 NA 2 0 NA	2 NA 1 2 1 NA NA 0 NA 0 2 2 NA 0	1 0 1 0 NA 0 NA NA 0 NA 0 0 0 0 2 2
## ## ## ## ## ## ## ## ## ## ## ## ##	[5,] [6,] [7,] [8,] [9,] [10,] [11,] [12,] [13,] [14,] [15,] [16,] [17,] [18,] [19,]	NA NA 1 0 NA NA 0 NA 0 NA 0 NA 0 NA NA NA NA	1 0 1 NA NA 2 NA 0 NA 2 0 1 2 NA	NA NA 2 NA 1 0 1 2 1 0 2 1 0 NA NA NA	0 0 2 2 0 1 1 1 NA 0 2 NA 0	0 1 1 1 0 0 1 NA 1 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0	2 1 1 NA 0 0 2 NA 0 0 0 2 0 0 0 2	NA NA 2 0 1 NA 0 0 1 NA 1 NA 2 0 0	2 1 NA 0 NA NA 0 1 0 2 1 2 NA 0 0	NA NA NA NA O O 1 2 O O O O O	NA 1 2 NA 0 NA 2 0 0 NA 2 0 0 NA 2 NA NA NA	2 NA 1 2 1 NA NA 0 NA 0 2 2 NA 0	1 0 1 0 NA 0 NA NA 0 0 0 2 2
## ## ## ## ## ## ## ## ## ## ## ## ##	[5,] [6,] [7,] [8,] [9,] [10,] [11,] [12,] [13,] [14,] [15,] [16,] [17,] [18,] [19,] [20,]	NA	1 0 1 NA NA 2 NA 0 NA 2 0 1 2 NA	NA NA 2 NA 1 0 1 2 1 0 2 2 0 0 NA NA	0 0 2 2 0 2 0 1 1 1 NA 0 2 NA 0 NA	0 1 1 1 0 0 1 NA 1 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0	2 1 1 NA 0 0 2 NA 0 0 0 2 0 0 0 1	NA NA 2 0 1 NA 0 0 1 NA 1 NA 2 0 0 NA	2 1 NA 0 NA NA 0 1 0 2 1 2 NA 0 0 0	NA NA NA NA O O 1 2 O O O O O	NA 1 2 NA 0 NA 2 0 NA 2 0 NA 2 0 NA 2 1	2 NA 1 2 1 NA NA 0 NA 0 2 2 2 NA 0	1 0 1 0 NA 0 NA 0 NA 0 0 2 2 NA
######################################	[5,] [6,] [7,] [8,] [9,] [10,] [11,] [12,] [13,] [14,] [15,] [16,] [17,] [18,] [20,] [21,] [22,] [23,]	NA	1 0 1 NA NA 2 NA 0 NA 2 0 1 2 NA NA 2 0 1 2 NA	NA NA 2 NA 1 0 1 2 1 0 2 2 0 NA NA NA 1	0 0 2 2 0 1 1 1 NA 0 2 NA 0 NA NA	0 1 1 1 0 0 0 1 NA 1 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0	2 1 1 NA 0 0 2 NA 0 0 0 2 0 0 1 0 0 1 0 0 1 1 1 1 1 1 1 1	NA NA 2 0 1 NA 0 0 1 NA 1 NA 2 0 NA 2 0 2 0 2	2 1 NA 0 NA 0 1 0 2 1 2 NA 0 0 0 1 0 0 0 1 1 0 0 0 0 0 0 0 0 0 0	NA NA NA NA O O 1 2 O O O O O O	NA 1 2 NA 0 NA 2 0 1 0 NA 2 0 NA 1 2 1 2 0 NA 2 2 0 1	2 NA 1 2 1 1 NA NA 0 NA 0 2 2 2 NA 0 0 0	1 0 1 0 NA 0 NA NA 0 0 0 2 2 NA 2
######################################	[5,] [6,] [7,] [8,] [9,] [10,] [11,] [12,] [13,] [14,] [15,] [16,] [17,] [18,] [20,] [21,] [22,] [23,] [24,]	NA NA 1 0 NA NA 0 NA 0 NA 0 NA 0 0 NA 0 NA	1 0 1 NA NA 2 NA 0 NA 2 0 1 2 NA NA 2 0 1 2 NA NA 0 NA 0 1 2 0 0 1 0 0 0 0 0 0 0 0 0 0 0 0 0	NA NA 2 NA 1 0 1 2 1 0 2 2 0 NA NA NA 1	0 0 2 2 0 1 1 1 NA 0 2 NA 0 NA NA	0 1 1 1 0 0 0 1 NA 1 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0	2 1 1 NA 0 0 2 NA 0 0 0 2 0 0 1 0 0 1 0 0 1 0 0 0 0 1 0 0 0 0	NA NA 2 0 1 NA 0 0 1 NA 1 NA 2 0 NA 0 2 0 2 2	2 1 NA 0 NA 0 1 0 2 1 2 NA 0 0 0 1 0 0 1 2 1 2 0 0 0 0 0 0 0 0 0 0	NA NA NA NA O O O 1 2 O O O O 2 O O O 2	NA 1 2 NA 0 NA 2 0 1 0 NA 2 0 NA 2 0 NA 1 2 0 NA NA 1 2 NA NA	2 NA 1 2 1 NA NA 0 NA 0 2 2 NA 0 0 0 1 1	1 0 1 0 NA 0 NA NA 0 0 2 2 NA 2 0 2 1 NA
## ## ## ## ## ## ## ## ## ##	[5,] [6,] [7,] [8,] [9,] [10,] [11,] [12,] [13,] [14,] [15,] [16,] [17,] [18,] [20,] [21,] [22,] [23,] [24,] [25,]	NA NA 1 0 NA NA 0 NA 0 NA 0 NA 0 0 NA 0 NA	1 0 1 NA NA 2 NA 0 NA 2 0 1 2 NA NA 2 0 1 2 NA NA 0 1 2 NA 0 1 2 0 0 1 0 0 0 0 0 0 0 0 0 0 0 0 0	NA NA 2 NA 1 0 1 2 1 0 2 2 0 0 NA NA 1 NA NA	0 0 2 2 0 1 1 1 NA 0 2 NA 0 NA NA 0 0 NA	0 1 1 1 0 0 1 NA 1 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0	2 1 1 NA 0 0 2 NA 0 0 0 2 0 0 1 0 NA 1 2 0 NA 1 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0	NA NA NA 2 0 1 NA 0 0 1 NA 1 NA 2 0 NA 0 2 2 2 1	2 1 NA 0 NA NA 0 1 0 2 1 2 NA 0 0 0 0 1 0 0 0 0 0 0 0 0 0 0 0 0 0 0	NA NA NA NA NA O O 1 2 O O O O 2 NA O NA	NA 1 2 NA 0 NA 2 0 1 0 NA 2 0 NA 1 2 0 NA NA NA 1 2 0 NA NA NA NA NA O	2 NA 1 2 1 1 NA NA 0 NA 0 2 2 2 NA 0 0 0 1 1 1 0 0 0 0 0 0 0 0 0 0 0 0 0	1 0 1 0 NA 0 NA 0 NA 0 0 2 2 NA 2 0 2 1 NA
#########################	[5,] [6,] [7,] [8,] [9,] [10,] [11,] [12,] [13,] [14,] [15,] [16,] [17,] [18,] [20,] [21,] [22,] [23,] [24,] [25,] [26,]	NA NA 1 0 NA NA 0 NA 0 2 2 NA 0 NA 0 0 NA 0 1 0 1	1 0 1 NA NA 2 NA 0 NA 2 0 1 2 NA NA 2 0 1 2 NA NA 0 1 2 0 1 2 0 0 1 0 0 0 0 0 0 0 0 0 0 0 0 0	NA NA 2 NA 1 0 1 2 1 0 2 2 0 NA NA NA NA NA	0 0 2 2 0 2 0 1 1 1 NA 0 NA 0 NA 0 NA 0 NA	0 1 1 1 0 0 0 1 NA 1 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0	2 1 1 NA 0 0 2 NA 0 0 2 0 0 1 0 NA 1 2 0 NA 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0	NA NA NA 2 0 1 NA 0 0 1 NA 1 NA 2 0 NA 0 2 2 1 0	2 1 NA 0 NA NA 0 1 0 2 1 2 NA 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0	NA NA NA NA NA O O 1 2 O O O O 2 NA O NA O	NA 1 2 NA 0 NA 2 0 1 0 NA 2 0 NA 1 2 0 NA NA NA 1 2 0 NA NA NA NA NA NA NA NA NA	2 NA 1 2 1 NA NA 0 NA 0 2 2 2 NA 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0	1 0 1 0 NA 0 NA 0 NA 0 0 2 2 NA 2 0 2 1 NA
#########################	[5,] [6,] [7,] [8,] [9,] [10,] [11,] [12,] [13,] [14,] [15,] [16,] [17,] [18,] [20,] [21,] [22,] [23,] [24,] [25,]	NA NA 1 0 NA NA 0 NA 0 NA 0 NA 0 0 NA 0 NA	1 0 1 NA NA 2 NA 0 NA 2 0 1 2 NA NA 2 0 1 2 NA NA 0 1 2 NA 0 1 2 0 0 1 0 0 0 0 0 0 0 0 0 0 0 0 0	NA NA 2 NA 1 0 1 2 1 0 2 2 0 0 NA NA 1 NA NA	0 0 2 2 0 1 1 1 NA 0 2 NA 0 NA NA 0 0 NA	0 1 1 1 0 0 1 NA 1 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0	2 1 1 NA 0 0 2 NA 0 0 0 2 0 0 1 0 NA 1 2 0 NA 1 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0	NA NA NA 2 0 1 NA 0 0 1 NA 1 NA 2 0 NA 0 2 2 2 1	2 1 NA 0 NA NA 0 1 0 2 1 2 NA 0 0 0 0 1 0 0 0 0 0 0 0 0 0 0 0 0 0 0	NA NA NA NA NA O O 1 2 O O O O 2 NA O NA	NA 1 2 NA 0 NA 2 0 1 0 NA 2 0 NA 1 2 0 NA NA NA 1 2 0 NA NA NA NA NA O	2 NA 1 2 1 1 NA NA 0 NA 0 2 2 2 NA 0 0 0 1 1 1 0 0 0 0 0 0 0 0 0 0 0 0 0	1 0 1 0 NA 0 NA 0 NA 0 0 2 2 NA 2 0 2 1 NA

##	[29,]	0	2	0	NA	0	1	NA	2	0	NA	NA	1
##	[30,]	NA	NA	2	0	NA	NA	NA	NA	NA	NA	NA	NA
##	[31,]	1	2	2	1	0	NA	NA	0	0	2	0	1
##	[32,]	NA	1	NA	NA	NA	1	1	2	NA	2	2	2
##	[33,]	1	1	NA	1	2	1	0	NA	0	0	1	0
##	[34,]	0	0	NA	NA	NA	1	0	0	2	0	2	NA
##	[35,]	NA	NA	0	0	NA	1	1	2	0	NA	0	0
##	[36,]	NA	0	NA	0	NA	2	NA	0	0	0	0	NA
##	[37,]	NA 2	O M A	O M A	0	O	NA O	NA 2	2	NA O	0	NA	2
## ##	[38,] [39,]	0	NA O	NA 2	0 2	NA O	NA	NA	O M A	NA	1 1	0	1 2
##	[40,]	NA	NA	0	1	NA	0	1	NA O	NA NA	NA	2	1
##	[41,]	1	0	NA	NA	0	NA	1	0	2	0	NA	2
##	[42,]	2	NA	1	2	NA	NA	0	0	NA	0	NA	NA
##	[43,]	NA	0	2	0	NA	2	2	0	2	0	NA	NA
##	[44,]	NA	1	NA	1	1	0	1	0	NA	2	0	0
##	[45,]	0	ΝA	NA	0	0	NA	2	NA	0	NA	0	0
##	[46,]	2	2	0	NA	2	NA	0	2	0	1	0	0
##	[47,]	0	2	NA	2	1	NA	NA	0	NA	NA	0	NA
##	[48,]	2	2	0	2	0	2	NA	2	2	1	2	1
##	[49,]	NA	0	1	0	NA	1	1	1	1	0	0	NA
##	[50,]	NA	NA	NA	NA	2	2	0	2	2	NA	2	NA
##		[,50]											
##	[1,]	NA											
##	[2,]	2											
##	[3,]	0											
##	[4,]	2											
##	[5,]	2											
##	[6,]	2											
##	[7,]	0											
##	[8,]	0											
##	[9,]	1											
##	[10,]	NA 1											
## ##	[11,] [12,]	1 2											
##	[13,]	NA											
	[14,]	NA											
	[15,]	NA											
	[16,]	0											
	[17,]	0											
	[18,]	0											
	[19,]	0											
	[20,]	1											
##	[21,]	2											
##	[22,]	1											
##	[23,]	1											
##	[24,]	NA											
##	[25,]	1											
##	[26,]	1											
##	[27,]	1											
##	[28,]	0											
##	[29,]	0											
##	[30,]	NA											
##	[31,]	2											

```
## [32,]
              2
## [33,]
              0
## [34,]
              1
## [35,]
              0
## [36,]
              1
## [37,]
              0
## [38,]
              2
## [39,]
             NA
## [40,]
              2
## [41,]
              2
## [42,]
              0
## [43,]
              0
## [44,]
              1
## [45,]
              2
## [46,]
              2
## [47,]
              2
## [48,]
             NA
## [49,]
              2
## [50,]
             NA
table(c(R))
##
```

• Sort the rows in matrix R by the largest row sum to lowest. Be careful about the NA's!

R[order(rowSums(R,na.rm=TRUE),decreasing=TRUE),]

##

## 861 437 439

```
##
           [,1] [,2] [,3] [,4] [,5] [,6] [,7] [,8] [,9] [,10] [,11] [,12] [,13]
                                                    2
##
     [1,]
              2
                   NA
                          NA
                                NA
                                      NA
                                              0
                                                         NA
                                                                1
                                                                        1
                                                                                0
                                                                                      NA
                                                                                             NA
##
     [2,]
               2
                     0
                           2
                                 0
                                              2
                                                    2
                                                          0
                                                                              NA
                                                                                      NA
                                                                                               1
                                       1
                                                                 1
                                                                        1
               2
##
     [3,]
                   NA
                          NA
                                 1
                                      NA
                                              0
                                                    1
                                                         NA
                                                                1
                                                                        2
                                                                                0
                                                                                      NA
                                                                                               0
##
    [4,]
               0
                     0
                           2
                                 0
                                      NA
                                              1
                                                    0
                                                          0
                                                                0
                                                                        2
                                                                                1
                                                                                       2
                                                                                               1
##
    [5,]
               0
                     2
                           0
                                 2
                                        2
                                              0
                                                    1
                                                          0
                                                                2
                                                                        1
                                                                              NA
                                                                                       1
                                                                                             NA
                                              2
    [6,]
                                       0
                                                    0
                                                                                0
                                                                                               1
##
               1
                     1
                          NA
                                 0
                                                          1
                                                               NA
                                                                       NA
                                                                                       1
##
     [7,]
               2
                     0
                           2
                                       0
                                                    1
                                                                0
                                                                                2
                                                                                      NA
                                                                                               2
                                NA
                                            NA
                                                          1
                                                                       NA
                                                                                       0
##
    [8,]
                     0
                           1
                                 2
                                        0
                                            NA
                                                          0
                                                                                             NA
             NA
                                                   NA
                                                                1
                                                                       ΝA
                                                                              NA
##
    [9,]
             NA
                     1
                           1
                                 0
                                        1
                                              2
                                                    0
                                                          1
                                                               ΝA
                                                                        0
                                                                                1
                                                                                       1
                                                                                               2
## [10,]
               0
                    NA
                           0
                                 2
                                        2
                                              1
                                                    1
                                                          0
                                                                2
                                                                        0
                                                                                2
                                                                                      NA
                                                                                               1
## [11,]
               2
                                        2
                                              2
                                                    0
                                                          2
                                                                0
                                                                        2
                                                                                0
                                                                                               0
                     0
                           1
                                NA
                                                                                       1
                                                                                               2
                                                          0
                                                                2
                                                                        2
                                                                                       2
## [12,]
               2
                   NA
                           1
                                NA
                                              1
                                      NA
                                                   NA
                                                                              NA
## [13,]
                                                                        2
                                                                                       2
                                                                                               0
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                     0
                          NA
                                 0
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                                              1
                                                   NA
                                                         NA
                                                               NA
                                                                              NA
## [14,]
               0
                   NA
                           2
                                 0
                                      NA
                                              0
                                                    2
                                                          1
                                                                0
                                                                        2
                                                                                2
                                                                                       1
                                                                                               0
## [15,]
               1
                     1
                           2
                                 1
                                      NA
                                            NA
                                                    0
                                                          2
                                                               NA
                                                                       NA
                                                                                0
                                                                                       0
                                                                                               1
               2
                           2
                                                          2
## [16,]
                    NA
                                NA
                                      NA
                                                   NA
                                                               NA
                                                                        0
                                                                                0
                                                                                       0
                                                                                               0
## [17,]
                     0
                           0
                                 0
                                      NA
                                            NA
                                                         NA
                                                               NA
                                                                        2
                                                                                2
                                                                                               0
             NA
                                                    0
                                                                                       1
## [18,]
                                              2
                                                                                       2
               1
                     1
                          NA
                                NA
                                        1
                                                   NA
                                                          0
                                                                2
                                                                       NA
                                                                              NA
                                                                                               0
## [19,]
                     0
                           1
                                NA
                                       0
                                              0
                                                    2
                                                         NA
                                                                        0
                                                                                1
                                                                                      NA
                                                                                               0
              0
                                                               NA
## [20,]
             NA
                     2
                          NA
                                 0
                                        0
                                              1
                                                    1
                                                          0
                                                                0
                                                                        2
                                                                                2
                                                                                       1
                                                                                               1
## [21,]
                                                                                0
                                                                                       2
                                                                                               0
               0
                   NA
                           0
                                NA
                                        2
                                              2
                                                    1
                                                          0
                                                                0
                                                                       NA
## [22,]
               1
                     0
                           2
                                NA
                                       0
                                              1
                                                    2
                                                         NA
                                                                        0
                                                                                2
                                                                                       0
                                                                                               0
                                                                1
                                                                                       2
## [23,]
                     1
                           0
                                              0
                                                    1
                                                          0
                                                                2
                                                                        1
                                                                                0
             NA
                                NA
                                        1
                                                                                             NA
## [24,]
                           2
                                 0
                                            NA
                                                    2
                                                          0
                                                                        0
                                                                                       2
                                                                                               2
               0
                    NA
                                      NA
                                                                1
                                                                                1
## [25,]
                                                                                               2
               0
                     1
                          NA
                                 0
                                      NA
                                              0
                                                   NA
                                                         NA
                                                                0
                                                                       NA
                                                                                0
                                                                                       0
```

##	[26,]	0	1	NA	0	0	0	NA	1	NA	0		NA	NA	NA
##	[27,]	NA	NA	2	NA	1	0	0	0	NA	0		NA	1	0
##	[28,]	1	NA	NA	0	NA	NA	NA	2	NA	NA		NA	0	0
##	[29,]	0	2	0	2	0	NA	0	2	0	NA		2	0	2
##	[30,]	NA	2	2	1	0	2	NA	0	NA	1		1	NA	2
##	[31,]	0	NA	0	1	0	2	NA	0	1	0		2	NA	0
##	[32,]	0	0	0	0	0	1	NA	0	2	0		1	NA	NA
##	[33,]	2	0	NA	1	1	0	0	NA	0	0		0	NA	1
##	[34,]	0	2	2	NA	2	0	0	2	0	1		0	1	NA
##	[35,]	1	NA	2	0	0	2	2	1	0	0		0	NA	2
##	[36,]	0	0		NA	0	0	1	0	0	0		NA	NA	2
##	[37,]	0	0	NA	0	2	1	NA	0	NA	0		0	0	1
##	[38,]	2	2	0	0	0	NA	NA	1	NA	0		NA	2	NA
##	[39,]	1	1	NA	1	NA	1	0	NA	NA	1		0	0	0
##	[40,]	2	0		NA	0	0	0	2	NA	0		0	0	0
##	[41,]	1	0	2	NA	NA	2	NA	0	NA	NA		NA	0	2
##	[42,]	NA	0	NA	1	NA	NA	2	0	1	0		0	NA	2
##	[43,]	NA	1	2	0	0	0	NA	0	2	0		NA	0	0
##	[44,]	NA	NA	NA	0	NA	NA	0	0	1	NA		0	NA	NA
##	[45,]	1	0	2	2	NA	0	NA	0	1	NA		NA	NA	NA
##	[46,]	NA	2	NA	2	0	0	1	NA	0	1		NA	0	0
##	[47,]	0	2	2	2	0	0	NA	0	0	NA		0	NA	0
##	[48,]	0	0	0	2	0	0	NA	NA	0	2		1	0	NA
##	[49,]	0	0		NA	NA	NA	NA	NA	NA	0		2	0	0
##	[50,]	NA L 447	NA L 4 E J	NA	1	NA 477 F	NA	1	0	0	0	101	2	NA	NA
## ##	[1,]	[,14] NA	[,15] NA	[,16]		17] [ NA	,18] 2	[,19] 1	[,20] NA	[,21] N <i>A</i>		NA	[,23]	[,24] N <i>A</i>	
##	[2,]	0	NA NA	2		2	0	1	1			0	1	10 F	
##	[3,]	NA	1	NA		2	2	0	2			2	0	(	
##	[4,]	2	NA	C		1	NA	2	0			0	NA	1	
##	[5,]	1	1	1		ΝA	NA	1	0			1	0	1	
##	[6,]	0	1	N A		0	0	0	0			0	0	1	
##	[7,]	0	1	C		2	0	NA	NA			0	2	N A	
##	[8,]	2	NA	N A		NA	1	NA	0			2	NA	1	
##	[9,]	2	NA	C		NA	NA	2	NA			NA	2	2	
##	[10,]	NA	1	NA		0	0	NA	NA			NA	NA	N A	
##	[11,]	1	1	2		0	NA	2	NA			2	0	NA	
	[12,]	1	0	C		0	0	2	0			1	0	(	
	[13,]	NA	0	NA		1	1	NA	1			1	0	2	
	[14,]	1	NA	NA		0	1	NA	0			0	0	C	
	[15,]	2	1	NA		1	2	NA	0			0	1	2	
	[16,]	1	NA	C	)	2	0	2	NA			1	2	1	
	[17,]	0	2	1		NA	2	0	0	(	)	0	2	1	
##	[18,]	1	2	C	)	1	0	1	2	1		0	NA	NA	NA NA
##	[19,]	2	0	1		NA	2	1	0	C	)	NA	1	(	) NA
##	[20,]	NA	NA	1		0	NA	NA	1	NA		NA	0	NA	0
##	[21,]	NA	2	C	)	0	0	0	NA	1		1	0	NA	0
##	[22,]	1	2	NA		0	NA	0	NA	C	)	0	NA	2	2 1
##	[23,]	0	NA	2		NA	0	2	1	NA	L	0	NA	(	) NA
##	[24,]	0	1	NA		1	NA	NA	NA	NA	L	NA	0	(	) NA
##	[25,]	2	1	NA		0	1	2	NA	NA	L	0	2	NA	
##	[26,]	0	NA	2		NA	0	0	NA		)	0	1	(	
##	[27,]	0	NA	2	!	NA	1	2	0	(	)	1	0	NA	2
##	[28,]	2	0	C	)	1	0	0	NA	NA		NA	2	NA	0

##	[29,]	2	NA	2	NA	1	NA	0	0	1	NA	0	0
##	[30,]	0	1	2	NA	NA	NA	0	0	2	NA	NA	0
##	[31,]	1	NA	2	0	NA	NA	0	0	NA	2	0	NA
##	[32,]	1	2	0	2	1	1	1	0	0	0	NA	0
##	[33,]	NA	2	NA	0	0	1	0	0	0	NA	0	2
##	[34,]	2	NA	NA	0	NA	NA	NA	NA	NA	0	0	NA
##	[35,]	2	0	NA	0	NA	0	0	NA	NA	0	0	1
##	[36,]	1	2	2	2	NA	NA	0	NA	NA	NA	1	0
##	[37,]	NA	1	2	NA	NA	0	0	0	NA	1	0	0
##	[38,]	NA	0	NA	0	NA	2	0	NA	0	0	NA	2
##	[39,]	2	0	0	0	0	0	1	NA	1	NA	NA	0
##	[40,]	2	NA	2	NA	0	0	NA	1	NA	2	1	0
##	[41,]	2	0	0	0	0	0	NA	0	NA	1	1	0
##	[42,]	0	0	2	NA	2	1	0	1	1	1	NA	0
##	[43,]	1	NA	0	0	1	1	2	0	NA	NA	1	NA
##	[44,]	NA	2	NA	2	1	1	NA	0	0	1	NA	NA
##	[45,]	0	1	0	0	0	1	NA	0	0	1	0	0
##	[46,]	NA	1	0	0	NA	0	NA	NA	0	0	0	1
##	[47,]	NA	1	0	0	0	NA	0	0	0	0	0	NA
##	[48,]	NA	NA	NA	NA	NA	NA	0	NA	1	0	NA	0
##	[49,]	0	1	1	0	1	1	NA	1	0	0	NA	NA
##	[50,]	0	0	NA	1	0	NA	1	0	NA	1	0	0
##		[,26]	[,27]	[,28]	[,29]	[,30]	[,31]	[,32]	[,33]	[,34]	[,35]	[,36]	[,37]
##	[1,]	0	1	NA	2	1	2	2	1	2	1	2	0
##	[2,]	NA	0	2	2	NA	NA	2	0	NA	0	NA	2
##	[3,]	2	1	0	NA	2	0	0	1	1	NA	1	2
##	[4,]	2	0	NA	0	0	0	0	1	0	2	2	0
##	[5,]	NA	NA	NA	0	0	0	2	0	0	NA	2	0
##	[6,]	0 2	NA 1	2 1	2 NA	1	NA 1	O N A	1	NA 1	0	NA O	2 2
##	[7,] [8,]	NA	2	0	NA NA	0	NA	NA O	2	2	0	2	2
##	[9,]	0	0	2	1	0	2	2	NA	NA	NA	NA	0
##	[10,]	NA	0	0	0	NA	0	NA	0	2	2	1	2
##	[11,]	0	2	0	NA	2	0	0	NA	1	0	0	2
##	[12,]	2	2	2	1	0	2	NA	NA	0	0	NA	NA
##	[13,]	1	0	2	NA	0	2	2	2	2	NA	0	NA
##	[14,]	2	2	1	NA	2	1	0	NA	2	0	2	1
##	[15,]	NA	1	NA	0	0	NA	2	2	NA	0	1	1
	[16,]	1	NA	NA	0	1	NA	NA	2	0	NA	1	2
##	[17,]	NA	0	1	NA	0	NA	0	1	1	1	1	1
##	[18,]	NA	0	NA	0	2	1	1	0	1	2	1	NA
##	[19,]	1	2	0	2	NA	NA	NA	1	2	2	NA	0
##	[20,]	1	1	2	NA	1	1	0	0	0	0	1	1
##	[21,]	0	2	1	1	NA	NA	2	1	2	0	1	NA
##	[22,]	0	0	NA	NA	2	NA	0	1	NA	NA	0	2
##	[23,]	2	NA	0	2	1	0	1	NA	0	NA	0	1
##	[24,]	NA	1	NA	1	0	NA	NA	0	1	NA	NA	1
##	[25,]	1	NA	NA	2	0	NA	NA	1	NA	NA	0	1
##	[26,]	NA	2	2	0	0	NA	2	2	0	0	NA	2
##	[27,]	2	0	1	0	NA	0	NA	2	NA	NA	1	NA
##	[28,]	0	0	2	1	1	NA	2	NA	1	0	2	2
##	[29,]	NA	0	0	0	0	NA	0	2	2	NA	NA	NA
##	[30,]	NA	0	0	NA	0	0	0	1	NA	1	0	0
##	[31,]	2	2	1	0	NA	2	NA	NA	0	2	1	1

##	[32,]	NA	0	2	NA	0	1	2	0	0	NA	0	0
##	[33,]	0	0	1	NA	0	NA	2	0	1	0	NA	1
##	[34,]	0	0	2	0	0	1	NA	NA	1	NA	0	0
##	[35,]	0	0	NA	1	NA	1	0	2	1	0	0	NA
##	[36,]	NA	2	NA	0	1	NA	0	NA	2	NA	NA	0
##	[37,]	2	NA	1	0	1	NA	NA	NA	0	0	1	0
##	[38,]	0	0	NA	1	NA	NA	2	0	0	0	1	1
##	[39,]	0	0	NA	NA	1	NA	1	0	1	NA	2	2
##	[40,]	1	0	NA	NA	1	1	NA	1	0	0	1	NA
##	[41,]	2	0	0	NA	NA	NA	0	1	0	2	0	0
	[42,]	NA	0	0	0	2	0	NA	0	0	0	0	2
	[43,]	NA	NA	0	2	0	NA	NA NA	O	NA	1	2	0
	[44,] [45,]	O	2	0	0	0	1	NA	NA	0	1	NA	NA
## ##	[46,]	NA 1	0	0	NA O	1 N A	0	0 1	0	0	0	NA O	0
##	[47,]	0	2	0	0	NA 1	NA	NA	2	2	1	NA	0
##	[48,]	1	0	NA	1	NA	NA	0	0	0	NA	0	NA
##	[49,]	NA	2	1	0	0	0	0	0	NA	0	2	0
##	[50,]	0	NA	0	0	1	NA	NA	0	NA	NA	1	NA
##	[00,]	[,38]	[,39]	[,40]	[,41]	[,42]	[,43]	[,44]	[,45]	[,46]	[,47]	[,48]	[,49]
##	[1,]	2	2	2	NA	0	0	1	2	0	NA	2	0
##	[2,]	NA	0	NA	0	NA	0	2	2	0	NA	2	NA
##	[3,]	NA	NA	NA	NA	2	2	0	2	2	NA	2	NA
##	[4,]	2	2	0	NA	2	NA	0	2	0	1	0	0
##	[5,]	2	2	NA	NA	0	1	NA	2	0	NA	2	1
##	[6,]	2	2	0	2	0	2	NA	2	2	1	2	1
##	[7,]	0	0	1	2	NA	NA	NA	0	NA	0	2	1
##	[8,]	1	1	2	2	1	1	2	0	NA	NA	2	0
##	[9,]	NA	0	2	0	NA	2	2	0	2	0	NA	NA
##	[10,]	NA	1	NA	NA	NA	1	1	2	NA	2	2	2
##	[11,]	NA	NA	0	0	NA	1	1	2	0	NA	0	0
##	[12,]	2	NA	0	1	0	0	NA	1	2	0	0	NA
##	[13,]	NA	NA	NA	NA	1	NA	2	1	2	0	NA	2
## ##	[14,] [15,]	NA	NA 1	2	1 2	NA	NA	0 2	0	0	1	O N A	0 2
##	[16,]	0	0	2	2	0	O NA	NA	NA	NA	1	NA O	2
##	[17,]	1	2	2	1	0	NA	NA	0	0	2	0	1
	[18,]	2	NA	NA	1	0	NA	0	1	0	NA	0	0
	[19,]	0	0	1	1	1	0	1	2	1	0	NA	NA
##	[20,]	0	0	NA	0	1	1	0	NA	2	0	1	2
##	[21,]	NA	0	1	0	NA	1	1	1	1	0	0	NA
##	[22,]	NA	1	NA	0	0	2	NA	1	NA	1	NA	0
##	[23,]	0	2	NA	2	NA	NA	1	0	NA	0	0	1
##	[24,]	0	1	NA	1	0	2	1	2	0	1	0	2
##	[25,]	1	0	NA	NA	0	NA	1	0	2	0	NA	2
##	[26,]	0	2	1	NA	NA	NA	2	0	0	2	1	0
##	[27,]	1	1	NA	1	2	1	0	NA	0	0	1	0
##	[28,]	1	0	0	0	1	0	NA	0	0	2	1	0
##	[29,]	NA	NA	1	0	0	0	1	NA	NA	NA	1	0
##	[30,]	0	NA	1	0	1	2	0	1	0	0	NA	NA
##	[31,]	NA	NA	2	0	NA	NA	NA	NA	NA	NA	NA	NA
##	[32,]	NA	2	0	2	0	0	NA	0	NA	2	NA	NA
##	- ,-	NA	0	2	0	0	2	NA	NA	0	2	2	0
##	[34,]	0	2	NA	2	1	NA	NA	0	NA	NA	0	NA

					_								
	[35,]	0	NA	NA	2	1	NA	0	NA	NA	0	1	NA
	[36,]	NA	2	0	NA	0	0	0	0	2	NA	0	2
	[37,]	0	NA	NA	NA	2	2	2	1	NA	NA	0	1
	[38,]	0	2	0	NA	0	1	NA	2	0	NA	NA	1
	[39,]	0	0	NA	NA	NA	1	0	0	2	0	2	NA
	[40,]	2	NA	1	2	NA	NA	0	0	NA	0	NA	NA
	[41,]	NA	0	0	0	0	NA	NA	2	NA	0	NA	2
	[42,]	NA	NA	NA	0	0	1	NA	0	0	NA	0	NA
	[43,]	NA	0	NA	0	NA	2	NA	0	0	0	0	NA
	[44,]	NA	NA	0	1	NA	0	1	0	NA	NA	2	1
	[45,]	2	NA	NA	0	NA	0	2	0	0	1	0	1
##	[46,]	NA	1	NA	1	1	0	1	0	NA	2	0	0
##	[47,]	1	0	NA	NA	0	0	0	NA	0	NA	NA	0
##	[48,]	NA	0	NA	0	1	1	NA	NA	NA	2	1	1
##	[49,]	0	NA	NA	0	0	NA	2	NA	0	NA	0	0
##	[50,]	0	NA	NA	NA	0	0	0	1	0	1	0	2
##		[,50]											
##	[1,]	NA											
##	[2,]	NA											
##	[3,]	NA											
##	[4,]	2											
##	[5,]	2											
##	[6,]	NA											
##	[7,]	2											
##	[8,]	0											
##	[9,]	0											
##	[10,]	2											
##	[11,]	0											
##	[12,]	NA											
##	[13,]	1											
##	[14,]	2											
##	[15,]	0											
##	[16,]	NA											
##	[17,]	2											
##	[18,]	0											
##	[19,]	NA											
##	[20,]	1											
	[21,]	2											
	[22,]	2											
	[23,]	1											
	[24,]	NA											
	[25,]	2											
	[26,]	2											
	[27,]	0											
	[28,]	0											
	[29,]	1											
	[30,]	1 NA											
	[31,]	NA NA											
	[32,]	NA											
	[33,]	0											
	[34,]	2											
	[35,]	0											
##	[36,]	0											
##	[37,]	1											

```
## [38,]
   [39.]
##
               1
   [40,]
   [41,]
               0
##
##
   [42,]
               0
## [43,]
               1
## [44.]
               2
## [45,]
               2
## [46.]
               1
## [47,]
               1
## [48,]
               2
## [49,]
               2
## [50,]
               1
```

• We will now learn the apply function. This is a handy function that saves writing for loops which should be eschewed in R. Use the apply function to compute a vector whose entries are the standard deviation of each row. Use the apply function to compute a vector whose entries are the standard deviation of each column. Be careful about the NA's! This should be one line.

```
#?apply
apply(R, MARGIN=1, sd, na.rm=TRUE)
    [1] 0.78030184399 0.86211556258 0.83212797981 0.84806793314 0.84492824744
    [6] 0.73611950197 0.88334762710 0.80752760964 0.87141166435 0.82836355919
  [11] 0.79599839534 0.86645874152 0.79681907289 0.88730016753 0.82060166754
  [16] 0.82329180024 0.83359407964 0.88975652100 0.78000215471 0.62389687596
  [21] 0.89348717267 0.72351284664 0.77390598995 0.90563130866 0.80752760964
   [26] 0.77408420033 0.84723257155 0.78537043660 0.85391256383 0.89087080637
  [31] 0.80985828720 0.86602540378 0.78857386432 0.73106345929 0.90433056190
   [36] 0.79176634141 0.85697307545 0.73111868704 0.89746506806 0.77237351493
  [41] 0.86010752016 0.81211855162 0.89066116505 0.64668978758 0.75503361354
  [46] 0.89788727042 0.89322419491 0.85297368222 0.79471941424 0.85723303999
apply(R,MARGIN=2,sd,na.rm=TRUE)
    [1] 0.85215816722 0.82182530102 0.92728015446 0.83591400764 0.80070533423
    [6] 0.85215816722 0.82043785845 0.79516676548 0.80127738926 0.84540801671
  [11] 0.87735277919 0.83219007599 0.87480946920 0.84983658560 0.74747048183
  [16] 0.93338744432 0.81167944991 0.77390598995 0.80771679264 0.67202150503
  [21] 0.66901468232 0.70647628014 0.80229046222 0.75134288380 0.85208592300
  [26] 0.87038827978 0.89130527156 0.85700278968 0.81211855162 0.74293796182
  [31] 0.77757017987 0.93945503223 0.80064076903 0.83286086471 0.79415478226
  [36] 0.78747706006 0.87010632698 0.86834497091 0.89294371875 0.86380197161
  [41] 0.85588532090 0.70173853734 0.82139397188 0.81996858772 0.88288571145
  [46] 0.89928422716 0.83937205966 0.88616323851 0.84515425473 0.86194473022
```

• Use the apply function to compute a vector whose entries are the count of entries that are 1 or 2 in each column. This should be one line.

```
apply(R, MARGIN = 2, function(x){length(x[(x == 1 | x == 2) & !is.na(x)])})
## [1] 19 17 21 16 12 19 18 14 17 17 17 17 19 24 23 18 14 16 21 10 11 14 19 15 17
## [26] 18 18 19 15 19 14 16 22 21 12 23 23 14 18 15 19 14 20 20 20 11 16 18 20 26
```

• Use the split function to create a list whose keys are the column number and values are the vector of the columns. Look at the last example in the documentation ?split.

```
#?split
#?list
R split=split(R,col(R))
R_split[4]
## $`4`
## [1]
         O NA O
                  2 NA 2 2 0 2 0 1 0 NA NA NA
                                                       1 1 NA 1 1 0 0 0
## [26]
        2 O NA O 1 O 2 NA 1 NA O NA 2 NA O O NA O 2 NA O NA O NA 1
  • In one statement, use the lapply function to create a list whose keys are the column number and
     values are themselves a list with keys: "min" whose value is the minimum of the column, "max" whose
     value is the maximum of the column, "pct_missing" is the proportion of missingness in the column and
    "first NA" whose value is the row number of the first time the NA appears.
#?lapply
length(R_split)
## [1] 50
#lapply(R_split,)
#max in each column
max(R split[[1]],na.rm=TRUE)
## [1] 2
#min in each column
min(R_split[[2]],na.rm=TRUE)
## [1] 0
#proportion of NA's in each column
apply(R, MARGIN = 2, function(x){length(x[is.na(x)])})/50
## [1] 0.24 0.28 0.34 0.32 0.36 0.24 0.38 0.24 0.34 0.26 0.30 0.36 0.24 0.26 0.34
## [16] 0.34 0.30 0.32 0.32 0.38 0.36 0.32 0.24 0.36 0.30 0.34 0.16 0.30 0.32 0.22
## [31] 0.48 0.34 0.22 0.22 0.34 0.26 0.22 0.40 0.34 0.48 0.28 0.30 0.32 0.34 0.20
## [46] 0.34 0.34 0.26 0.30 0.20
\#first_NA \ row \ number \ of \ the \ first \ time \ the \ NA \ appears
\#Position(function(x)\{R\_split[x] == NA\}, x)
#?Position
R_split[4]
## $`4`
## [1]
        0 NA 0 2 NA 2 2 0 2 0
                                       1 O NA NA NA 1 1 NA 1 1 O
                                                                        0
## [26] 2 0 NA 0 1 0 2 NA 1 NA 0 NA 2 NA 0 0 NA 0
                                                                2 NA O NA O NA
\#lapply(R\_split, (function(x)\{\}()))
max(R,na.rm=TRUE)
## [1] 2
```

• Set a seed and then create a vector **v** consisting of a sample of 1,000 iid normal realizations with mean -10 and variance 100.

#?max

```
set.seed(123)
n=1000
v=rnorm(n,-10,100)
   • Repeat this exercise by resetting the seed to ensure you obtain the same results.
set.seed(123)
v2=rnorm(n,-10,100)
   • Find the average of v and the standard error of v.
mean(v)
## [1] -8.3872134065
#?SE
#?mean
sd(v)/sqrt(length(v))
## [1] 3.1360148696
summary(v)
                                                                  3rd Qu.
##
            Min.
                       1st Qu.
                                      Median
                                                       Mean
                                                                                    Max.
## -290.9774679
                 -72.8324243
                                  -9.0790361
                                                -8.3872134
                                                              56.4601867 314.1039935
   • Find the 5%ile of v and use the qnorm function to compute what it theoretically should be. Is the
     estimate about what is expected by theory?
v3=sort(v)
v3[50]
## [1] -173.63792681
#?qnorm
qnorm(0.05,-10,100)
```

## [1] -174.4853627

diff=(v3[50])-(qnorm(0.05,-10,100)) diff

## [1] 0.84743588924

 $\textit{\#Yes, the estimate is close to what is expected by theory, as the difference is <\!1. \\$ 

 $\bullet$  What is the percentile of v that corresponds to the value 0? What should it be theoretically? Is the estimate about what is expected by theory?

#between 535 and 536 is when the values change from negative to positive, so we can say 53.55% pnorm(0,-10,100)

## [1] 0.53982783728 .5355-pnorm(0,-10,100)

## [1] -0.004327837277

#we can say that the estimate is close to what is expected by theory, as the difference is <0.005

• Create a function my\_reverse which takes as required input a vector v and returns the vector in reverse where the first entry is the last entry, etc. No function calls are allowed inside your function otherwise

that would defeat the purpose of the exercise! (Yes, there is a base R function that does this called rev). Use head on v and tail on my\_reverse(v) to verify it works.

```
rvrsx=c(rep(NA, 1000))
l=length(v)
my_reverse=function(x){
  }
l=length(v)
rvrsv=c(rep(NA,1))
for (i in 1:1){
  rvrsv[i]=v[l+1-i]
}
rvrsv
##
      [1]
           -34.919067775540
                              -62.261669719592 -145.110038570333
                                                                     97.051603677834
##
      [5]
           -18.997519701566
                               21.322877199433
                                                 -31.330714323307
                                                                     35.457780905774
##
      [9]
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                                                 -92.947761162452
                                                                      78.425082002821
##
    [609] -225.764633501528
                              -74.704563131827
                                                   24.610361955361
                                                                     -53.564546969191
##
    [613] -123.558847037434
                               35.623640317981
                                                 127.857013695924
                                                                      37.613327830263
##
    [617] -115.501704260268
                                 7.472639698184
                                                    9.023031569246
                                                                      -6.544893286615
##
    [621] -189.028123726406
                              -11.430741316691
                                                    4.447570471070 -109.678074220752
##
    [625]
           -68.948103851500
                               41.013254687866
                                                   72.537986275924
                                                                     -56.398724296601
##
    [629] -175.104889568819
                              231.677335378821
                                                  -56.103833888435
                                                                      75.692301089932
##
    [633]
          -104.540883112389
                               27.816777220851
                                                  -30.979317122851
                                                                      71.765944637409
##
    [637]
            92.467323481835
                               17.376649103655
                                                   55.119328158767
                                                                     -30.529925746820
    [641]
           247.145814586664
##
                             -256.589819376003
                                                 -13.303615927599
                                                                      31.142992061573
##
    [645]
                              -99.320757005495
                                                                     -52.727928720543
            23.390294249923
                                                    1.663728358271
##
    [649]
          -209.274848868858
                               91.494317274366
                                                 -27.990623104754
                                                                   -107.400958280409
##
    [653]
           -67.185005789556
                               -0.067240591217 -185.323735914227
                                                                     -15.198190618090
##
    [657]
            -4.398326672504
                              157.105482886294
                                                   85.900537778783
                                                                      52.418747202065
##
    [661]
           -20.188325571522
                               76.577940433449
                                                 -30.078101558912 -146.403745208238
    [665]
##
          -215.222282043373
                               27.738797302393
                                                 141.921771138818
                                                                     -82.160444043602
##
    [669]
          -128.843403514798
                               91.755863695209
                                                   -9.270990968310
                                                                     123.551761505939
##
    [673]
            53.296071303145
                              -16.082195466007
                                                   58.374552185071
                                                                     -62.291237631342
    [677]
##
            56.082029778980
                             -143.877428723497
                                                 111.810861032581
                                                                      13.743027249103
    [681]
##
            81.139129179596
                              158.443570809411
                                                -135.864862806017
                                                                     -20.567133400377
                              -45.204645658262
##
    [685]
            60.352390275689
                                                 -70.150670800678
                                                                   -182.673039911433
##
    [689]
            65.677476379596
                              120.117599220059
                                                 193.757401824044
                                                                     113.667504641657
##
    [693]
                             -211.421049792072
            11.198043337229
                                                   23.117917295898
                                                                     -53.715953318040
##
    [697]
          -115.251327933874
                             -103.853870360689
                                                 -85.268896821774
                                                                     -81.524218722280
##
                                                                     176.685184470686
    [701]
           114.991457096922
                               -7.901641364576
                                                -145.090268603071
##
    [705]
            -3.329912906982
                              190.248273029283
                                                 -67.746800105956
                                                                     104.526311038036
##
    [709]
            95.418102337692
                              106.838387306909
                                                    6.806538388466
                                                                     -31.905037893348
##
    [713]
           154.084616597749
                               12.101946856100
                                                    3.403864536846
                                                                       1.814451104668
##
    [717]
           -36.565162527822
                               28.602656834968
                                                   63.649596477344
                                                                   -176.747509758566
    [721]
##
            -7.532501717386
                                                   -2.544882282627
                                                                       7.480270016126
                               32.816676497051
##
    [725]
           -54.655721642722
                               74.964304563336
                                                 -149.527434979947
                                                                      58.430942941646
##
    [729]
            86.252796848427
                               74.501300406744
                                                   -1.079277692671
                                                                     -48.877986407174
##
    [733]
          -185.652739555764
                              -23.315096432894
                                                 144.758105898377
                                                                     219.307897383109
##
    [737]
           120.019867766682
                               -5.284556723847
                                                  -58.987045313847
                                                                     -62.111731755252
    [741]
          -163.290200289060
                                                                      98.079949615152
##
                              -21.363989550614
                                                   53.075411565057
##
    [745]
           -18.856511213888
                              149.850877114583
                                                   -0.950335286078
                                                                     -44.391723412846
##
    [749]
           -66.187636354978
                              -47.560287166977
                                                   38.545997890488
                                                                     -76.476943527406
                                                                     -27.905159438020
##
    [753]
          -145.984070382139
                              -20.097488532881
                                                 180.236182167893
##
    [757]
          -123.730362066575
                              139.606066984635
                                                  -60.219871834286
                                                                     -88.862197085400
##
                                                                     -28.292538837273
    [761]
           -88.153648705475
                               22.430434416138
                                                   31.898240492446
##
    [765] -141.701613230524
                              -67.438868976327
                                                  -83.852770473957
                                                                      11.453882662922
    [769]
##
           -19.031959396585
                              185.529396549246
                                                -111.559257860354
                                                                      78.465049897692
##
    [773]
           -81.721816157401
                              -80.459646368007
                                                   -4.025006261540
                                                                     -46.365729709525
##
    [777]
            60.758835383559
                              100.984813892972
                                                   51.798581716653
                                                                     -67.397347929799
                             -133.627311888329
                                                  -82.306596993987
##
    [781]
          -138.471572231780
                                                                     -54.116321690529
##
    [785]
           157.569693240319
                             -109.250715039204
                                                  -61.606383094478
                                                                     113.247587848534
##
    [789]
            14.368742959909
                                 1.924523642758
                                                 -15.402812508544
                                                                     155.090746733669
##
    [793]
           -69.461726745951
                              -88.860283785024
                                                 -57.624689461558
                                                                     -51.433994791886
##
    [797]
            44.319405923209
                              -36.514505669635
                                                 121.241297643351
                                                                     209.881034888372
##
    [801] -128.548008459731
                              -71.116591668042 -135.127136162494
                                                                      50.070882367242
```

```
##
    [805]
           189.721338474797 -141.080153332797
                                                -99.536335797754
                                                                     -0.541647182643
##
    [809]
           -42.468591149083
                               11.444530958160
                                                 -59.929201717226
                                                                     65.405378518452
##
    [813]
            -1.526270780280
                              100.992028971364
                                                 -29.717589434855
                                                                    -33.627956894110
    [817]
                              -44.965038795355
                                                116.318517608949 -116.332613397119
##
           -96.551286265337
##
    [821]
           -55.836533271111
                               33.652347891018
                                                  21.048074944314
                                                                     -6.221160082892
                                                 202.845189901618
                                                                   -13.406725373846
##
    [825]
          -119.599626707466
                              -84.133609627283
    [829]
            -3.470696647468
                              -31.538050764169
                                                  26.896452738509
                                                                     41.686204431361
                                                  19.822759154072
##
    [833]
           -58.378062570874
                               53.656967403385
                                                                    -51.685758816043
##
    [837]
           314.103993494240 -136.015524475811 -114.917700666607
                                                                     95.271146557933
##
    [841]
           -47.458085776701
                               87.697338668562
                                                 -47.243875610383
                                                                     46.298953322048
    [845]
           -38.039533517025
                              -21.945260663066 -110.837660827701
                                                                     23.220257895012
                               68.773884747518 -138.703047603518
                                                                    200.010894052567
##
    [849]
            66.904224100091
##
    [853]
            58.791677297583 -156.175558499590
                                                 -63.090652217030 -170.153617357459
##
    [857] -161.466765378175 -167.214415914549
                                                 -36.219748940247
                                                                     60.178433537471
##
                              180.910356921748
                                                  63.994751087733 -156.064007092482
    [861] -154.389316097180
##
    [865]
           103.133721341418 -215.324722154052
                                                 -52.249683233962
                                                                     -5.876707800706
##
    [869]
            35.150405307921
                              134.455085842335
                                                 -17.130808612360 -106.185663413013
##
    [873]
            -2.203915043629
                               13.538657228486
                                                 -75.194990169546
                                                                    174.386200523221
##
    [877]
           -35.609219219825
                              -59.055744370067 -104.747461418480
                                                                      1.764659710013
    [881] -112.412879060491
                              -94.970434603358
                                                -74.070600830538
                                                                      0.567619414894
##
    [885]
            20.115336216671
                               41.940720394346
                                                 -15.556196552454 -171.788270828916
    [889]
                              -67.534696260839
                                                                    -48.022652028776
##
            50.796432222503
                                                  81.899660906077
##
    [893] -176.794193658814
                              -88.490446945708
                                                -14.502772480892 -105.161856726502
                                                                    -81.040656369930
##
    [897]
           -44.754259939773
                              -34.669187846237
                                                  15.688370915653
##
    [901] -112.642090030678
                              -33.570035910048
                                                 143.261062618519
                                                                    208.733299301658
    [905]
           -70.025958714713
                              126.065244853001
                                                 -72.790607603937
                                                                    13.873173511144
##
    [909]
                                                 104.880761845109
                                                                    -42.593158553123
            44.839695950807
                               89.350385596212
##
    [913]
            33.518149083380
                               99.683901314935
                                                  23.178196391570
                                                                    -32.048656181875
##
    [917]
                              -47.066003179241
                                                  28.528040112633
                                                                    -9.423581410011
            54.437654851883
##
    [921]
           -23.889136243904
                                8.130347974915 -132.071771225454
                                                                    -38.477300705101
##
    [925]
            92.557136969670
                              -78.800861646736
                                                -80.920076258239
                                                                     90.573852446226
##
    [929] -240.916887564081
                              -59.103116605654
                                                 195.008468562714
                                                                     82.226746787974
##
    [933]
            -4.699577326950
                               34.820977862943
                                                  20.352864140426 -117.179122647558
##
    [937] -111.857538310709
                              -43.320738366942
                                                 -60.232345310930
                                                                     27.963948275988
##
    [941]
            11.594156874397
                                2.385424384461
                                                  48.461374963607 -164.875280423022
                                                                   -14.287045729132
##
    [945]
           141.647060442954
                              -32.577098565927
                                                 126.860228401446
##
    [949]
           -12.854675534870
                               15.331851399475
                                                 -18.336906647183
                                                                     67.996511833632
##
    [953]
           -56.665535362322
                              -50.288483529908 -122.310858320335
                                                                    110.796199830499
    [957]
           206.895596533851 -136.539635156826
                                                 -30.791727801960
                                                                    -79.470697892051
##
##
                                                 -16.191171057672
    [961]
           -48.047100101238
                              -40.596266373992
                                                                     45.391765353759
    [965]
            58.864025410009
                               72.158108163749
                                                  77.813348753304
                                                                     79.512566104502
    [969]
           -39.507148299227
                                                 115.381492106993 -123.813693701195
##
                               32.646422147681
##
    [973]
             5.337311783652
                               73.778704449452 -178.669331074241
                                                                   -72.503926784926
##
    [977]
           -82.889122929114 -112.600444830724
                                                -31.797491465830 -116.782370598685
##
    [981]
           -57.279140772793
                               60.135590156369 -206.661715662964
                                                                     39.785047822924
    [985]
##
           168.691313680308
                              -65.584113475407
                                                   1.068271594512
                                                                     30.077145059405
##
    [989]
            25.981382705736
                              112.408179743946
                                                 -54.566197009996
                                                                    -78.685285189353
##
    [993] -136.506123460653
                               36.091620598920
                                                 161.506498688328
                                                                      2.928773516095
    [997]
            -2.949160857542
                              145.870831414912
                                                 -33.017748948328
                                                                    -66.047564655221
what=my_reverse(v)
what
```

## NULL

what

#### ## NULL

Create a function flip\_matrix which takes as required input a matrix, an argument dim\_to\_rev that
returns the matrix with the rows in reverse order or the columns in reverse order depending on the
dim\_to\_rev argument. Let the default be the dimension of the matrix that is greater. If the number of
rows

#### #T0-D0

• Create a list named my\_list with keys "A", "B", ... where the entries are arrays of size 1, 2 x 2, 3 x 3 x 3, etc. Fill the array with the numbers 1, 2, 3, etc. Make 8 entries according to this sequence.

```
my_list=list()
my_list$A=1
my_list$B=array(1:4,dim=c(2,2))
my_list$C=array(1:27,dim=c(3,3,3))
my_list$D=array(1:4^4,dim=c(4,4,4,4))
my_list$E=array(1:5^5,dim=c(rep(5,5)))
my_list$F=array(1:6^6,dim=c(rep(6,6)))
my_list$G=array(1:7^7,dim=c(rep(7,7)))
my_list$H=array(1:8^8,dim=c(rep(8,8)))
```

Run the following code:

```
lapply(my_list, object.size)
```

```
## $A
## 56 bytes
##
## $B
## 232 bytes
##
## $C
## 352 bytes
##
## $D
## 1248 bytes
##
## $E
## 12744 bytes
##
## $F
## 186864 bytes
##
## $G
## 3294416 bytes
##
## $H
## 67109104 bytes
#?object.size
```

Use **?object.size** to read about what these functions do. Then explain the output you see above. For the later arrays, does it make sense given the dimensions of the arrays?

From C onwards, it does make sense as the rate of increase is really high. Each upward step in alphabet results in an increase of at least 10 times.

```
#TO-DO
```

## **Packages**

Install the package pacman using regular base R.

```
#install.packages("pacman")
#package is installed
```

First, install the package testthat (a widely accepted testing suite for R) from https://github.com/r-lib/testthat using pacman. If you are using Windows, this will be a long install, but you have to go through it for some of the stuff we are doing in class. LINUX (or MAC) is preferred for coding. If you can't get it to work, install this package from CRAN (still using pacman), but this is not recommended long term.

```
pacman::p_load(testthat)
#package is installed
```

• Create vector v consisting of all numbers from -100 to 100 and test using the second line of code su

```
v = seq(-100, 100)
#expect_equal(v, -100 : 101)
```

If there are any errors, the expect\_equal function will tell you about them. If there are no errors, then it will be silent.

Yes, there was an error as the two sequences are not equal.

Test the my\_reverse function using the following code:

## A little about strings

• Use the strsplit function and sample to put the sentences in the string lorem below in random order. You will also need to manipulate the output of strsplit which is a list. You may need to learn basic concepts of regular expressions.

```
## [[1]]
                                       "dolor"
                                                                      "amet,"
   [1] "Lorem"
                        "ipsum"
                                                      "sit"
                       "adipiscing"
                                       "elit."
                                                      "Morbi"
                                                                      "posuere"
    [6] "consectetur"
        "varius"
                        "volutpat."
                                       "Morbi"
                                                      "faucibus"
                                                                     "ligula"
## [11]
## [16]
       "id"
                        "massa"
                                                                     "Donec"
                                       "ultricies"
                                                      "viverra."
## [21] "vehicula"
                        "sagittis"
                                       "nisi"
                                                      "non"
                                                                      "semper."
## [26]
        "Donec"
                        "at"
                                       "tempor"
                                                      "erat."
                                                                     "Integer"
## [31]
       "dapibus"
                        "mi"
                                       "lectus,"
                                                      "eu"
                                                                     "posuere"
## [36] "arcu"
                                       "in."
                        "ultricies"
                                                      "Cras"
                                                                     "suscipit"
                        "nibh"
                                       "lacinia"
                                                                     "Curabitur"
## [41] "id"
                                                      "elementum."
## [46] "est"
                        "augue,"
                                       "congue"
                                                      "eget"
                                                                     "quam"
## [51] "in,"
                                      "semper"
                                                                     "Aenean"
                        "scelerisque"
                                                      "magna."
## [56] "nulla"
                        "ante."
                                       "iaculis"
                                                      "sed"
                                                                     "vehicula"
## [61] "ac,"
                                                                     "Mauris"
                        "finibus"
                                       "vel"
                                                      "arcu."
```

```
## [66] "at" "sodales" "augue."
#?sample
```

You have a set of names divided by gender (M / F) and generation (Boomer / GenX / Millenial):

- M / Boomer "Theodore, Bernard, Gene, Herbert, Ray, Tom, Lee, Alfred, Leroy, Eddie"
- M / GenX "Marc, Jamie, Greg, Darryl, Tim, Dean, Jon, Chris, Troy, Jeff"
- M / Millennial "Zachary, Dylan, Christian, Wesley, Seth, Austin, Gabriel, Evan, Casey, Luis"
- F / Boomer "Gloria, Joan, Dorothy, Shirley, Betty, Dianne, Kay, Marjorie, Lorraine, Mildred"
- F / GenX "Tracy, Dawn, Tina, Tammy, Melinda, Tamara, Tracey, Colleen, Sherri, Heidi"
- F / Millennial "Samantha, Alexis, Brittany, Lauren, Taylor, Bethany, Latoya, Candice, Brittney, Cheyenne"

Create a list-within-a-list that will intelligently store this data.

## \$F\$Millennial

```
#HINT:
#strsplit("Theodore, Bernard, Gene, Herbert, Ray, Tom, Lee, Alfred, Leroy, Eddie", split = ", ")[[1]]
list_within_list = list(
 M = list(
    Boomer = strsplit("Theodore, Bernard, Gene, Herbert, Ray, Tom, Lee, Alfred, Leroy, Eddie", split =
    GenX = strsplit("Marc, Jamie, Greg, Darryl, Tim, Dean, Jon, Chris, Troy, Jeff", split = ", ")[[1]],
    Millennial = strsplit("Zachary, Dylan, Christian, Wesley, Seth, Austin, Gabriel, Evan, Casey, Luis"
    ),
  F = list(
    Boomer = strsplit("Gloria, Joan, Dorothy, Shirley, Betty, Dianne, Kay, Marjorie, Lorraine, Mildred"
    GenX = strsplit("Tracy, Dawn, Tina, Tammy, Melinda, Tamara, Tracey, Colleen, Sherri, Heidi", split
    Millennial = strsplit("Samantha, Alexis, Brittany, Lauren, Taylor, Bethany, Latoya, Candice, Brittn
  )
list_within_list
## $M
## $M$Boomer
    [1] "Theodore" "Bernard"
                               "Gene"
                                           "Herbert"
                                                      "Rav"
                                                                  "Tom"
    [7] "Lee"
##
                   "Alfred"
                               "Leroy"
                                           "Eddie"
##
## $M$GenX
##
    [1] "Marc"
                  "Jamie"
                           "Greg"
                                    "Darryl" "Tim"
                                                       "Dean"
                                                                 "Jon"
                                                                          "Chris"
##
    [9] "Troy"
                  "Jeff"
##
## $M$Millennial
    [1] "Zachary"
                     "Dylan"
                                 "Christian" "Wesley"
                                                          "Seth"
                                                                       "Austin"
##
##
    [7] "Gabriel"
                     "Evan"
                                 "Casey"
                                              "Luis"
##
##
## $F
  $F$Boomer
    [1] "Gloria"
##
                    "Joan"
                               "Dorothy"
                                           "Shirley"
                                                      "Betty"
                                                                  "Dianne"
##
    [7] "Kay"
                    "Marjorie" "Lorraine" "Mildred"
##
## $F$GenX
##
    [1] "Tracy"
                   "Dawn"
                             "Tina"
                                        "Tammy"
                                                  "Melinda" "Tamara"
##
    [8] "Colleen" "Sherri"
                             "Heidi"
##
```

```
## [1] "Samantha" "Alexis" "Brittany" "Lauren" "Taylor" "Bethany"
## [7] "Latoya" "Candice" "Brittney" "Cheyenne"
```

Now cleanup the namespace by deleting all stored objects and functions:

```
rm(list = ls())
```