Zadanie O6

Zadanie O6 (obowiązkowe)

Stosując metodę Laguerre'a wraz ze strategią obniżania stopnia wielomianu i wygładzania proszę znaleźć wszystkie rozwiązania następujących równań

$$243z^{7} - 486z^{6} + 783z^{5} - 990z^{4} + 558z^{3} - 28z^{2} - 72z + 16 = 0,$$

$$z^{10} + z^{9} + 3z^{8} + 2z^{7} - z^{6} - 3z^{5} - 11z^{4} - 8z^{3} - 12z^{2} - 4z - 4 = 0,$$

$$z^{4} + iz^{3} - z^{2} - iz + 1 = 0.$$

Zadanie polegało na znalezieniu miejsc zerowych powyższych wielomianów. Zgodnie z Podstawowym Twierdzeniem Algebry, wielomian posiada tyle pierwiastków jakiego jest stopnia.

ALGORYTM:

- 1. Musimy obrać sobie jakiś punkt początkowy
- 2. Wyliczamy z' metodą Laguerra

$$z_{i+1} = z_i - \frac{n P_n(z_i)}{P_n'(z_i) \pm \sqrt{(n-1) \left((n-1) \left[P_n'(z_i) \right]^2 - n P_n(z_i) P_n''(z_i) \right)}},$$
(11)

a.

- b. W pętli liczymy po przez algorytm Hornera wartości w danym wielomianie, jego pierwszej pochodnej, jego drugiej pochodnej.
- c. Znane wartości wstawiamy do równania
- d. Ważne też jest żeby wybrać odpowiedni znak mianownika (prosty if wystarcza)
- 3. Wygładzamy miejsce zerowe po przez użycie na nim ponownie metody Laguerra dla niezmienionego wielomianu.
- 4. Zmniejszamy stopień wielomianu przez deflację:

$$\begin{bmatrix} 1 & & & & & & \\ -z_0 & 1 & & & & & \\ & -z_0 & 1 & & & \\ & & -z_0 & 1 & & \\ & & -z_0 & 1 & \\ & & & -z_0 & 1 \end{bmatrix} \begin{bmatrix} b_{n-1} \\ b_{n-2} \\ b_{n-3} \\ \vdots \\ b_1 \\ b_0 \end{bmatrix} = \begin{bmatrix} a_n \\ a_{n-1} \\ a_{n-2} \\ \vdots \\ a_2 \\ a_1 \end{bmatrix}$$

Szybkość takiego działania jest bardzo duża, wykonujemy to w O(n);

- 5. Powtarzamy całą operację w pętli aż do 2 stopnia wielomianu.
- 6. Korzystamy z równania na deltę żeby obliczyć pierwiastki trójmianu kwadratowego.

Wyniki:

$$243z^7 - 486z^6 + 783z^5 - 990z^4 + 558z^3 - 28z^2 - 72z + 16 = 0,$$

(0.667027,0)

(0.666486,-0.000312597)

(0.666486, 0.000312597)

```
(0.3333333,0)
(0,-1.41421)
(-0.3333333,0)
(0,1.41421)
          In[5]:= y = 243 z^7 - 486 z^6 + 783 z^5 - 990 z^4 + 558 z^3 - 28 z^2 - 72 z + 16
      \mathsf{Out}[5] \texttt{=} \ 16 - 72 \ z - 28 \ z^2 + 558 \ z^3 - 990 \ z^4 + 783 \ z^5 - 486 \ z^6 + 243 \ z^7
          In[7]:= NSolve[y, z]
      \texttt{Out}(7) = \{ \{z \rightarrow -0.333333\}, \{z \rightarrow 0.-1.41421\,i\}, \{z \rightarrow 0.+1.41421\,i\}, \{z \rightarrow 0.333333\}, \{z \rightarrow 0.666667\}, \{z \rightarrow 0.666667\}, \{z \rightarrow 0.666667\}\}, \{z \rightarrow 0.666667\}, \{z \rightarrow 0.666667\}, \{z \rightarrow 0.666667\}, \{z \rightarrow 0.666667\}\}, \{z \rightarrow 0.666667\}, \{z 
                                        z^{10} + z^9 + 3z^8 + 2z^7 - z^6 - 3z^5 - 11z^4 - 8z^3 - 12z^2 - 4z - 4 = 0
(-0.5, 0.866025)
(-0.5, -0.866025)
(0,1.41421)
(-1.41421,0)
(0,-1.41421)
(0,1.00005)
(0,-1.00004)
(0,-0.999961)
(0.0.99995)
(1.41421,0)
          In[8]:= g = z^10 + z^9 + 3 z^8 + 2 z^7 - z^6 - 3 z^5 - 11 z^4 - 8 z^3 - 12 z^2 - 4 z - 4
      \mathsf{Out}[8] = \ -4 - 4 \ z - 12 \ z^2 - 8 \ z^3 - 11 \ z^4 - 3 \ z^5 - z^6 + 2 \ z^7 + 3 \ z^8 + z^9 + z^{16}
          In[9]:= NSolve[g, z]
       \text{OutSpin} \ \ \{ \ (z \rightarrow -1.41421) \ , \ (z \rightarrow -0.5 + 0.866025 \ i) \ , \ (z \rightarrow -0.5 - 0.866025 \ i) \ , \ (z \rightarrow 0.1 + 0.11 \ i) \ , \ (z \rightarrow 0.1 \ i
                                              z^4 + iz^3 - z^2 - iz + 1 = 0.
(-0.951057, 0.309017)
(-0.587785, -0.809017)
(0.587785, -0.809017)
(0.951057.0.309017)
          \begin{aligned} & \text{SQ(2)} + k = z \wedge 4 + z \wedge 3 \, \hat{a} - z \wedge 2 - \hat{a} z + 1 \\ & \text{SQ(2)} + 1 - z^2 + \hat{a} \, z^3 + z^4 - \hat{a} z \end{aligned}
          h(13) = NSolve[k, z]
           \bigcirc \text{Out(1)} \cdot \left[ \left[z + (0, -0.25 \, \mathrm{i}) + 0.5 \, \right] \cdot \left( 0.416667 + \frac{0.416667}{\left(43, -45, \, \mathrm{i}z + 5.19615\sqrt{-257, \, 758, \, \mathrm{i}z - 757, \, \mathrm{i}z^2 + 256, \, \mathrm{i}z^2} \right)^{1.5}} + 0.264567 \left[ 43, -45, \, \mathrm{i}z + 5.19615\sqrt{-257, \, 758, \, \mathrm{i}z - 757, \, \mathrm{i}z^2 + 256, \, \mathrm{i}z^2} \right]^{1.5} \right] 
                                                      \left. \left(0..+6.75\,i\right) \middle/ \left[ \sqrt{ \left[ 0.416667 + \frac{0.418974\,\left(13,-12.\,iz\right)}{\left(43,-45,\,iz+5.19613\,\sqrt{-257,\,\cdot756,\,iz-757,\,iz^2+256,\,iz^2}\right)^{1.3}} \right. + 0.264567\left[ 43,-45,\,iz+5.19615\,\sqrt{-257,\,\cdot756,\,iz-757,\,iz^2+256,\,iz^2} \right]^{1.3}} \right] \right] \right] \right]
                                      \left[x+(6,-8,25;1)+0.5\sqrt{\left[0.415667+\frac{0.41567}{\left[45,-45,\left(12+5,19615\sqrt{-257},-756,\left(12-757,\left(12^2+256,\left(12^2\right)^{1/3}\right)+0.5\sqrt{\left[0.423333+\frac{0.41567}{\left[45,-45,\left(12+5,19615\sqrt{-257},-756,\left(12-757,\left(12^2+256,\left(12^2\right)^{1/3}\right)+0.5\sqrt{\left[0.423333+\frac{0.41567}{\left[45,-45,\left(12+5,19615\sqrt{-257},-756,\left(12-757,\left(12^2+256,\left(12^2\right)^{1/3}\right)+0.5\sqrt{\left(0.423333+\frac{0.41567}{\left[45,-45,\left(12+5,19615\sqrt{-257},-756,\left(12-757,\left(12^2+256,\left(12^2\right)^{1/3}\right)+0.5\sqrt{\left(0.423333+\frac{0.41567}{\left[45,-45,\left(12+5,19615\sqrt{-257},-756,\left(12-757,\left(12^2+256,\left(12^2\right)^{1/3}\right)+0.5\sqrt{\left(0.423333+\frac{0.41567}{\left[45,-45,\left(12+5,19615\sqrt{-257},-756,\left(12-757,\left(12^2+256,\left(12^2\right)^{1/3}\right)+0.5\sqrt{\left(0.423333+\frac{0.41567}{\left[45,-45,\left(12+5,19615\sqrt{-257},-756,\left(12-757,\left(12-256,\left(12^2\right)^{1/3}\right)+0.5\sqrt{\left(0.423333+\frac{0.41567}{\left[45,-45,\left(12+5,19615\sqrt{-257},-756,\left(12-757,\left(12-256,\left(12^2\right)^{1/3}\right)+0.5\sqrt{\left(0.423333+\frac{0.41567}{\left[45,-45,\left(12+5,19615\sqrt{-257},-756,\left(12-757,\left(12-256,\left(12^2\right)^{1/3}\right)+0.5\sqrt{\left(0.423333+\frac{0.41567}{\left[45,-45,\left(12+5,19615\sqrt{-257},-756,\left(12-757,\left(12-256,\left(12^2\right)^{1/3}\right)+0.5\sqrt{\left(0.423333+\frac{0.41567}{\left[45,-45,\left(12+5,19615\sqrt{-257},-756,\left(12-757,\left(12-256,\left(12^2\right)^{1/3}\right)+0.5\sqrt{\left(0.423333+\frac{0.41567}{\left[45,-45,\left(12+5,19615\sqrt{-257},-756,\left(12-757,\left(12-256,\left(12^2\right)^{1/3}\right)+0.48667\right)+0.48667\right]}\right]}}\right]}}\right]}}\right]
                                                                          0.26657 \left[ 43, -45, iz + 5.19615 \sqrt{-257, +756, iz -757, iz^2 + 256, iz^2} \right]^{1.3} - (0, +0.75 i) / \left[ \sqrt{ \left[ 0.45667 + \frac{0.419974 \left[ 13, -12, iz \right]}{\left[ 43, -45, iz + 5.19615 \sqrt{-257, +756, iz -757, iz^2 + 256, iz^2} \right]^{1.3}} + 0.264567 \left[ 43, -45, iz + 5.19615 \sqrt{-257, +756, iz -757, iz^2 + 256, iz^2} \right]^{1.3}} \right] \right] \right] 
                                         \left[z + (0. - 0.25 \text{ i}) - 0.5 \sqrt{0.416667 + \frac{0.419974 \left(13. - 12. \left(z\right)}{\left(43. - 45. \left(z + 5.136615 \sqrt{-257. + 756. \left(z - 757. \left(z^2 + 256. \right)z^2\right)^{1.3}}\right) + 0.264567 \left(43. - 45. \left(z + 5.13615 \sqrt{-257. + 756. \left(z - 757. \left(z^2 + 256. \right)z^2\right)^{1.3}}\right) - 0.5 \sqrt{0.419974 \left(13. - 12. \left(z\right) - \frac{0.419974 \left(13. - 12. \left(z\right) + 2.5 \left(z - 757. \right)z^2 + 256. \left(z^2\right)^{1.3}}\right) + 0.264567 \left(43. - 45. \left(z + 5.13615 \sqrt{-257. + 756. \left(z - 757. \left(z^2 + 256. \left(z^2\right)\right)^{1.3}}\right) - 0.5 \sqrt{0.419974 \left(13. - 12. \left(z\right) + 2.5 \left(z - 756. (z - 756. \left(z - 
                                                                         0.264567 \left[ 43, -45, (z+5.19615 \sqrt{-257, -756, (z-797, (z^2+256, (z^2))^{1/3}} + (0, +0.751) / \left. \sqrt{ \left[ 0.415667 + \frac{0.419974 (13, -12, (z))}{[43, -45, (z+5.19615 \sqrt{-257, +756, (z-797, (z^2+256, (z^2))^{1/3}}] + 0.264567 \left[ 43, -45, (z+5.19615 \sqrt{-257, +756, (z-797, (z^2+256, (z^2))^{1/3}} + (0.415657 + (0.41567 + (0.41567 + (0.41567 + (0.41567 + (0.41567 + (0.41567 + (0.41567 + (0.41567 + (0.41567 + (0.41567 + (0.41567 + (0.41567 + (0.41567 + (0.41567 + (0.41567 + (0.41567 + (0.41567 + (0.41567 + (0.41567 + (0.41567 + (0.41567 + (0.41567 + (0.41567 + (0.41567 + (0.41567 + (0.41567 + (0.41567 + (0.41567 + (0.41567 + (0.41567 + (0.41567 + (0.41567 + (0.41567 + (0.41567 + (0.41567 + (0.41567 + (0.41567 + (0.41567 + (0.41567 + (0.41567 + (0.41567 + (0.41567 + (0.41567 + (0.41567 + (0.41567 + (0.41567 + (0.41567 + (0.41567 + (0.41567 + (0.41567 + (0.41567 + (0.41567 + (0.41567 + (0.41567 + (0.41567 + (0.41567 + (0.41567 + (0.41567 + (0.41567 + (0.41567 + (0.41567 + (0.41567 + (0.41567 + (0.41567 + (0.41567 + (0.41567 + (0.41567 + (0.41567 + (0.41567 + (0.41567 + (0.41567 + (0.41567 + (0.41567 + (0.41567 + (0.41567 + (0.41567 + (0.41567 + (0.41567 + (0.41567 + (0.41567 + (0.41567 + (0.41567 + (0.41567 + (0.41567 + (0.41567 + (0.41567 + (0.41567 + (0.41567 + (0.41567 + (0.41567 + (0.41567 + (0.41567 + (0.41567 + (0.41567 + (0.41567 + (0.41567 + (0.41567 + (0.41567 + (0.41567 + (0.41567 + (0.41567 + (0.41567 + (0.41567 + (0.41567 + (0.41567 + (0.41567 + (0.41567 + (0.41567 + (0.41567 + (0.41567 + (0.41567 + (0.41567 + (0.41567 + (0.41567 + (0.41567 + (0.41567 + (0.41567 + (0.41567 + (0.41567 + (0.41567 + (0.41567 + (0.41567 + (0.41567 + (0.41567 + (0.41567 + (0.41567 + (0.41567 + (0.41567 + (0.41567 + (0.41567 + (0.41567 + (0.41567 + (0.41567 + (0.41567 + (0.41567 + (0.41567 + (0.41567 + (0.41567 + (0.41567 + (0.41567 + (0.41567 + (0.41567 + (0.41567 + (0.41567 + (0.41567 + (0.41567 + (0.41567 + (0.41567 + (0.41567 + (0.41567 + (0.41567 + (0.41567 + (0.41567 + (0.41567 + (0.41567 + (0.41567 + (0.41567 + (0.41567 + (0
                                      \left[z + (0, -0.25 \pm) - 0.5 \sqrt{0.415657 + \frac{0.419974 \pm (13, -12, \pm z)}{(45, -45, \pm z + 5.19615 \sqrt{-257, -756, \pm z -757, \pm^2 + 356, \pm^2})^{1.5}} + 0.264567 \left[43, -45, \pm z + 5.19615 \sqrt{-257, -756, \pm z -757, \pm^2 + 256, \pm^2}\right]^{1.5}} + 0.5 \sqrt{0.4139333 - \frac{0.419974 \pm (13, -12, \pm z)}{(45, -45, \pm z + 5.19615 \sqrt{-257, -756, \pm z -757, \pm^2 + 356, \pm^2})^{1.5}} + 0.5 \sqrt{0.415657 + \frac{0.419974 \pm (13, -12, \pm z)}{(45, -45, \pm z + 5.19615 \sqrt{-257, -756, \pm z -757, \pm^2 + 356, \pm^2})^{1.5}}} + 0.549974 \pm \frac{0.419974 \pm (13, -12, \pm z)}{(45, -45, \pm z + 5.19615 \sqrt{-257, -756, \pm z -757, \pm^2 + 356, \pm^2})^{1.5}} + 0.5 \sqrt{0.415657 + \frac{0.419974 \pm (13, -12, \pm z)}{(45, -45, \pm z + 5.19615 \sqrt{-257, -756, \pm z -757, \pm^2 + 356, \pm^2})^{1.5}}} + 0.549974 \pm \frac{0.419974 \pm (13, -12, \pm z)}{(45, -45, \pm z + 5.19615 \sqrt{-257, -756, \pm z -757, \pm^2 + 356, \pm^2})^{1.5}} + 0.549974 \pm \frac{0.419974 \pm (13, -12, \pm z)}{(45, -45, \pm z + 5.19615 \sqrt{-257, -756, \pm z -757, \pm^2 + 356, \pm^2})^{1.5}}} + 0.549974 \pm \frac{0.419974 \pm (13, -12, \pm z)}{(45, -45, \pm z + 5.19615 \sqrt{-257, -756, \pm z -757, \pm^2 + 356, \pm^2})^{1.5}} + 0.549974 \pm \frac{0.419974 \pm (13, -12, \pm z)}{(45, -45, \pm z + 5.19615 \sqrt{-257, -756, \pm z -757, \pm^2 + 356, \pm^2})^{1.5}}} + 0.549974 \pm \frac{0.419974 \pm (13, -12, \pm z)}{(45, -45, \pm z + 5.19615 \sqrt{-257, -756, \pm z -757, \pm^2 + 356, \pm^2})^{1.5}} + 0.549974 \pm \frac{0.419974 \pm (13, -12, \pm z)}{(45, -45, \pm z + 5.19615 \sqrt{-257, -756, \pm z -757, \pm^2 + 356, \pm^2})^{1.5}}} + 0.549974 \pm \frac{0.419974 \pm (13, -12, \pm z)}{(45, -45, \pm z + 5.19615 \sqrt{-257, -756, \pm z -757, \pm^2 + 356, \pm^2})^{1.5}}} + 0.549974 \pm \frac{0.419974 \pm (13, -12, \pm z)}{(45, -45, \pm z + 5.19615 \sqrt{-257, -756, \pm z -757, \pm^2 + 356, \pm^2})^{1.5}}} + 0.549974 \pm \frac{0.419974 \pm (13, -12, \pm z)}{(45, -45, \pm z + 5.19615 \sqrt{-257, -756, \pm z -757, \pm^2 + 356, \pm^2})^{1.5}}} + 0.549974 \pm \frac{0.419974 \pm (13, -12, \pm z)}{(45, -45, \pm z + 5.19615 \sqrt{-257, -756, \pm z -757, \pm^2 + 356, \pm^2})^{1.5}}} + 0.549974 \pm \frac{0.419974 \pm 0.415 \pm 0.
                                                                      0.264507\left[43, -45, iz + 5.19615\sqrt{-257}, +756, iz - 757, iz^2 + 256, iz^2\right]^{1/3} + (0, +0.75 i) / \left[ \sqrt{\left[0.416667 + \frac{0.419976}{[43, -45, iz + 5.19615\sqrt{-257}, +756, iz - 757, iz^2 + 256, iz^2]^{1/3}} + 0.264567\left[43, -45, iz + 5.19615\sqrt{-257}, +756, iz - 757, iz^2 + 256, iz^2\right]^{1/3}} \right] \right] \right]
```

Niestety do tego ostatniego Mathematica podaje powyższy wynik. Nie potrafię go zinterpretować.

```
KOD:
#include <iostream>
#include <math.h>
#include <cstdlib>
#include <vector>
#include <complex>
#define epsilon 0.0000001
using namespace std;
complex<double> HornerMethod(vector<complex<double>> a, complex<double> x){
  complex<double> result = a[0];
  for(int i = 1; i < a.size(); i++){
    result = result*x + a[i];
  }
  return result;
}
vector<complex<double>> deflation(complex<double> root, vector<complex<double>> a){
  vector<complex<double>> newMultimian;
  root = -root;
  newMultimian.push_back(a[0]);
```

```
for (int i = 1; i < a.size() - 1; i++) {
    complex<double> bi = a[i] - (root)*newMultimian[i - 1];
    newMultimian.push_back(bi);
  }
return newMultimian;
}
vector<complex<double>> Delta(vector<complex<double>> equation){
  complex<double> x1,x2,b,c,a,delta;
  complex<double> four = 4.0;
  complex<double> two = 2.0;
  vector<complex<double>> roots;
  a = equation[0];
  b = equation[1];
  c = equation[2];
  delta = (b*b) - four*(a*c);
  complex<double> up1 = -b + sqrt(delta);
  complex<double> up2 = -b - sqrt(delta);
  x1 = up1 / (two*a);
  x2 = up2 / (two*a);
  roots.push_back(x1);
  roots.push_back(x2);
  return roots;
}
```

```
vector<complex<double>> Derivative(vector<complex<double>> multimian){
  vector<complex<double>> a;
  int k = multimian.size();
  complex<double> n((double)k);
  if(multimian.size() == 1){
    a.push_back(multimian[0]);
    return a;
  }
  for(int i = 0; i < k - 1; i++){
    a.push_back(multimian[i]*(n.real() - 1 - i));
  }
  return a;
}
complex<double> LaguerreMethod(vector<complex<double>> &a, complex<double> x){
  complex<double> z, x0;
  vector<complex<double>> firstDerivative;
  vector<complex<double>> secondDerivative;
  int f = a.size() - 1;
  complex<double> n(a.size() - 1);
  complex<double> upper, lowerPlus, lowerMinus;
  firstDerivative = Derivative(a);
  secondDerivative = Derivative(firstDerivative);
  for(int i = 0; i < 100000; i++){
    complex<double> value = HornerMethod(a, x);
    if(abs(value) < epsilon) break;</pre>
```

```
complex<double> firstDerivativeValue = HornerMethod(firstDerivative, x);
               complex<double> secondDerivativeValue = HornerMethod(secondDerivative, x);
               upper = (n*HornerMethod(a, x));
               lowerPlus = firstDerivativeValue + sqrt((n - 1.0)*((n - 1.0))*((n - 1.0))*((
1.0)*firstDerivativeValue*firstDerivativeValue - n*value*secondDerivativeValue));
               lowerMinus = (firstDerivativeValue - sqrt((n - 1.0)*((n -
1.0)*firstDerivativeValue*firstDerivativeValue - n*value*secondDerivativeValue)));
               if(abs(lowerPlus) > abs(lowerMinus)){
                     x0 = (upper / lowerPlus);
              }else{
                       x0 = (upper / lowerMinus);
                }
              x -= x0;
              if(abs(x0) < epsilon) break;
       }
       return x;
}
vector<complex<double>> FindRoots(vector<complex<double>> a, complex<double> x0){
       vector<complex<double>> roots;
       vector<complex<double>> activeVector;
       vector<complex<double>> tmpVector;
       activeVector = a;
       complex<double> z, value;
       z = x0;
       for(int i = 0; i < a.size() - 3; i++){}
```

```
z = LaguerreMethod(activeVector, x0);
    value = LaguerreMethod(a, z);
    roots.push_back(value);
    tmpVector = deflation(value, activeVector);
    activeVector = tmpVector;
  }
  tmpVector = Delta(activeVector);
  roots.push_back(tmpVector[0]);
  roots.push_back(tmpVector[1]);
  return roots;
}
void DisplayMZ(vector<complex<double>> roots){
  for (int i = 0; i < roots.size(); i++) {
    if(abs(roots[i].real()) < epsilon*1000)</pre>
      roots[i].real(0);
    if(abs(roots[i].imag()) < epsilon*1000)</pre>
      roots[i].imag(0);
    cout << roots[i] << " ";
  }cout << endl << endl;</pre>
}
int main(){
  //243z^7 - 486z^6 + 783z^5 - 990z^4 + 558z^3 - 28z^2 - 72z + 16 = 0
```

```
vector<complex<double>> a1 = {243.0, -486.0, 783.0, -990.0, 558.0, -28.0, -72.0, 16.0};
vector<complex<double>> a2 = {1.0, 1.0, 3.0, 2.0, -1.0, -3.0, -11.0, -8.0, -12.0, -4.0, -4.0};
vector<complex<double>> a3 = {1.0, {0.0, 1.0}, -1.0, {0.0, -1.0}, 1.0};
vector<complex<double>> a = {2.0, -3.0, 10.0};
// vector<complex<double>> a = {1.0, 12.0, 58.0, 134.0, 146.0, 60.0};
complex<double> z, value;
vector<complex<double>> roots;
complex<double> x1 = 1.0;
complex<double> x2 = -3.0;
complex<double> x3 = -1.0;
cout << "Równanie dla którego liczymy:\n";</pre>
for(int i = 0; i < a1.size(); i++)
  cout << a1[i] << " ";
cout << endl;
roots = FindRoots(a1, x1);
DisplayMZ(roots);
cout << "Równanie dla którego liczymy:\n";
for(int i = 0; i < a2.size(); i++)
  cout << a2[i] << " ";
cout << endl;
roots = FindRoots(a2, x2);
DisplayMZ(roots);
cout << "Równanie dla którego liczymy:\n";
for(int i = 0; i < a3.size(); i++)
```

```
cout << a3[i] << " ";
cout << endl;
roots = FindRoots(a3, x3);
DisplayMZ(roots);

return 0;
}</pre>
```