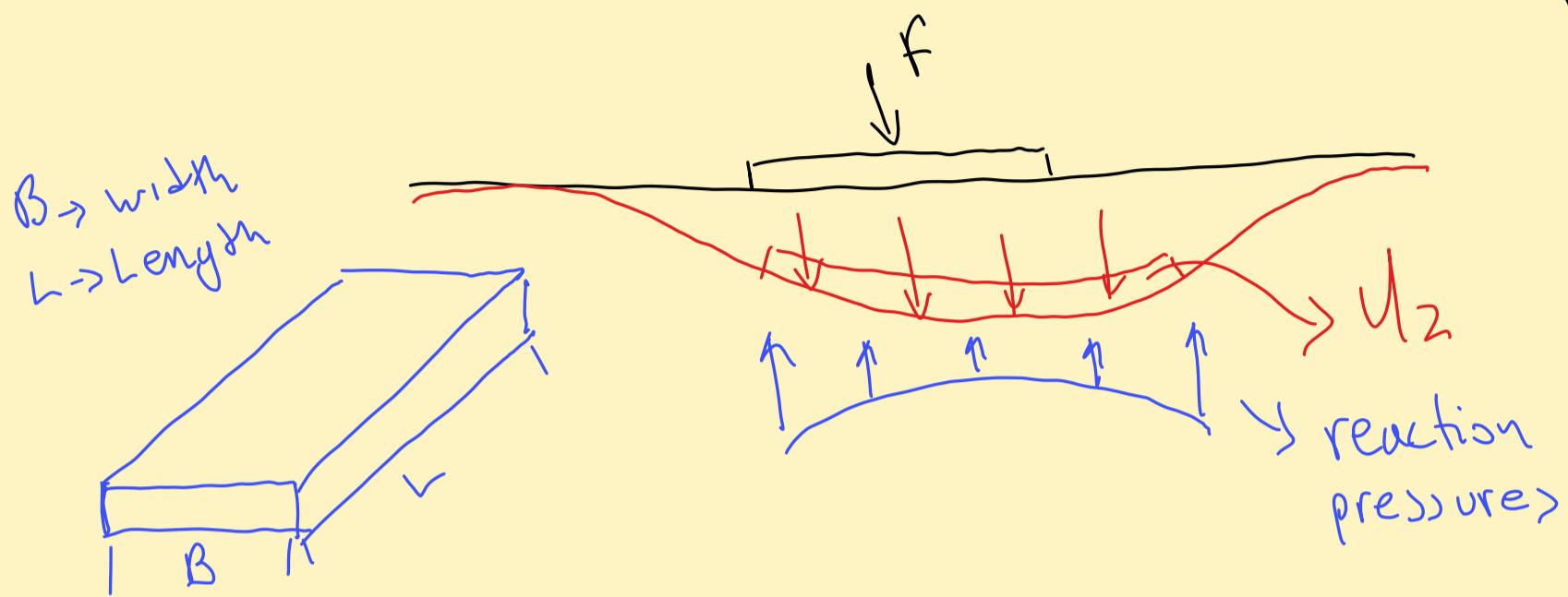
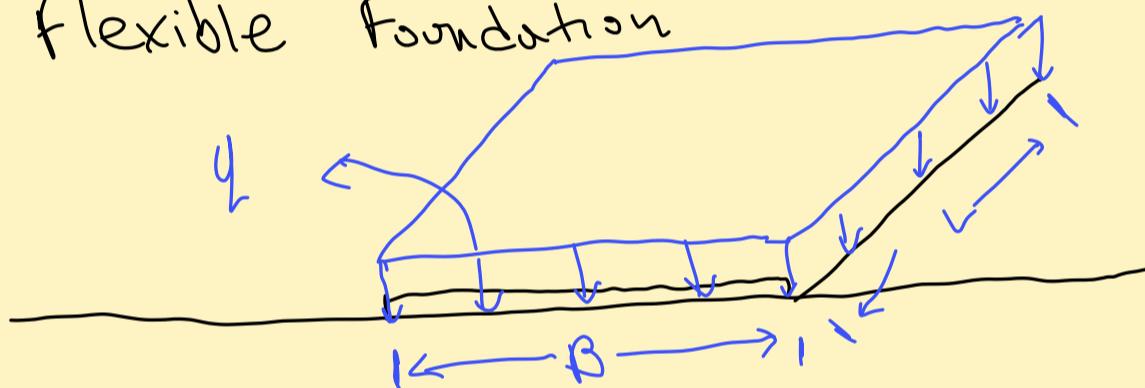


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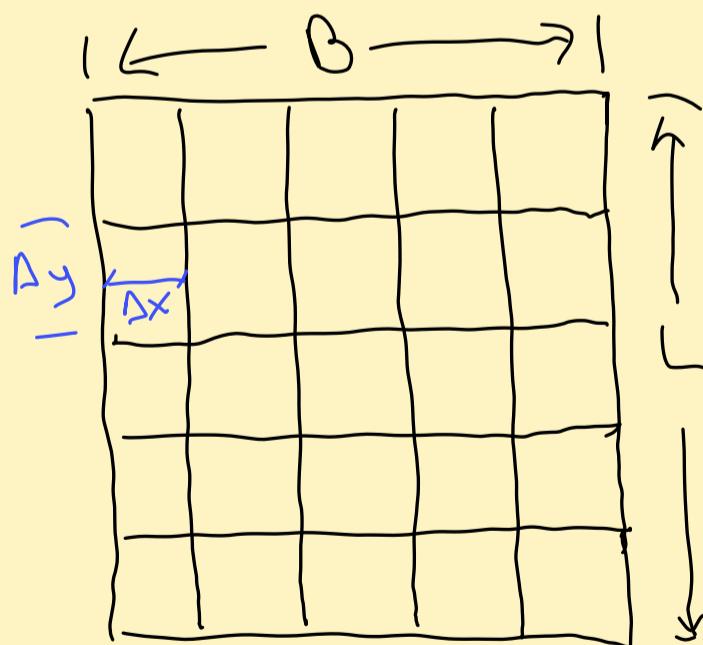
7/9/23



Extremely flexible Foundation

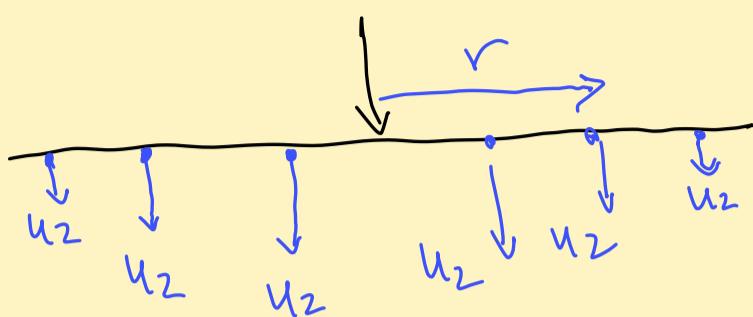


Plan View



Boussinesq Theory

Concentrated force = P



Settlement (u_2)

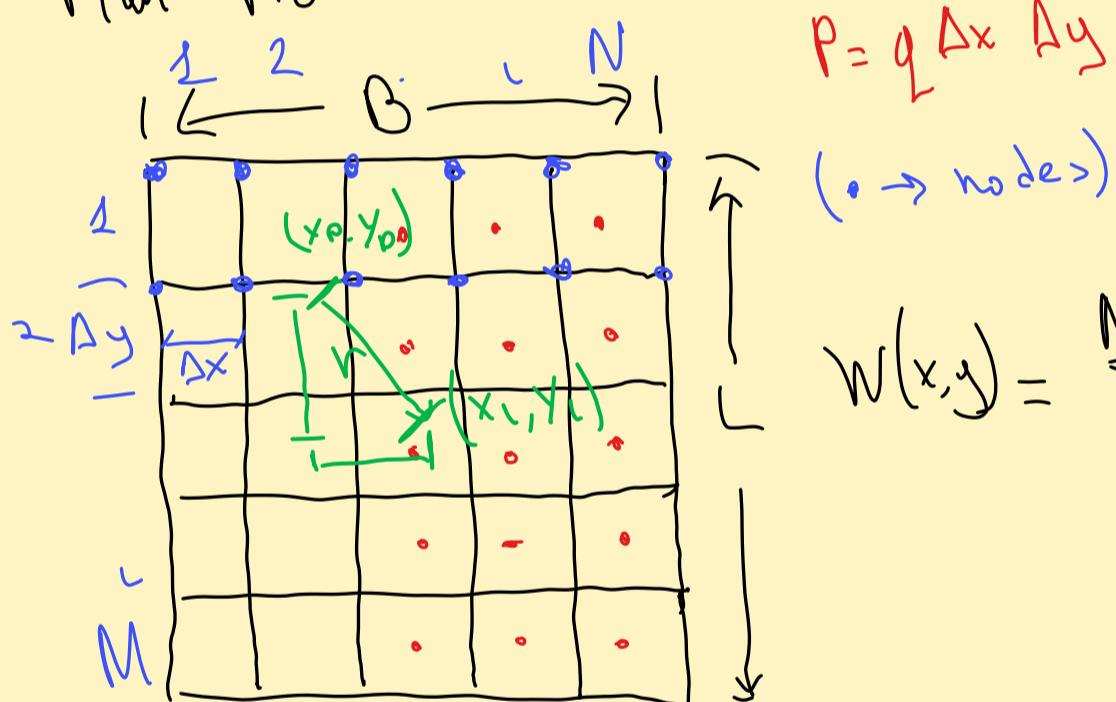
$$u_2(r) = \frac{P(1-v)}{2\pi G r}$$

G = shear modulus
(Hooke's Law)

$$\zeta = \frac{E}{2(1+v)}$$

v = Poisson's ratio

Plan View (\rightarrow Concentrated Force)



$$P = q \Delta x \Delta y$$

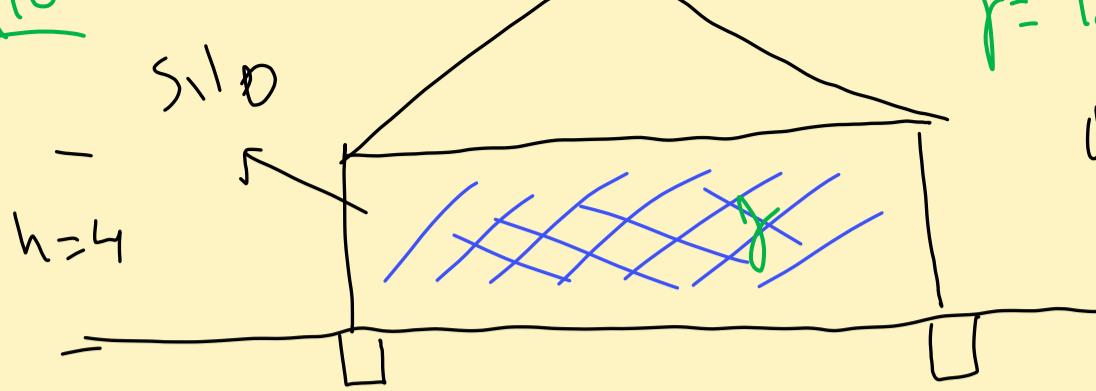
(\rightarrow nodes)

$$w(x,y) = \sum_{i=1}^N \sum_{j=1}^M \frac{P(1-v)}{2\pi G r}$$

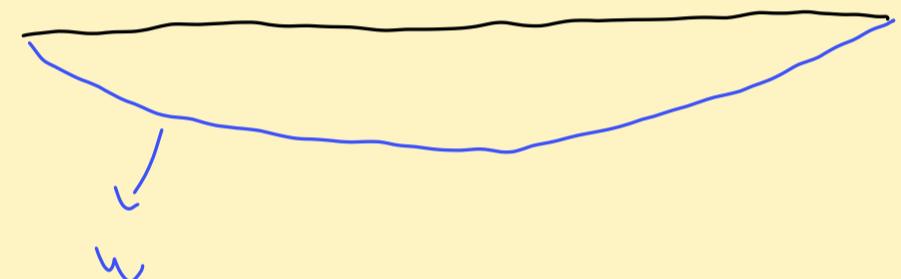
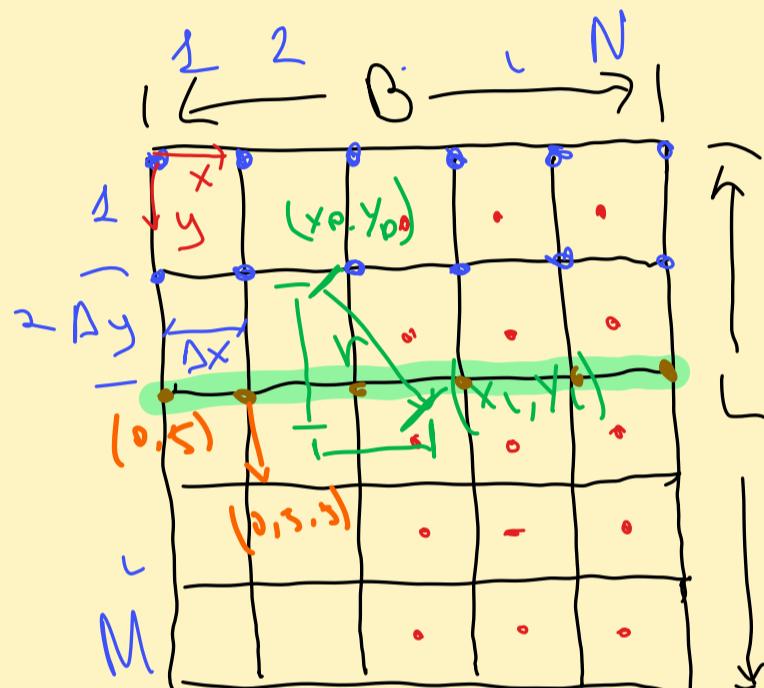
$$\Rightarrow w(x,y) = \sum_{i=1}^N \sum_{j=1}^M \frac{q(1-v)}{2\pi G r} \Delta x \Delta y$$

$$r = \sqrt{(x_i - x_p)^2 + (y_i - y_p)^2}$$

Example 1



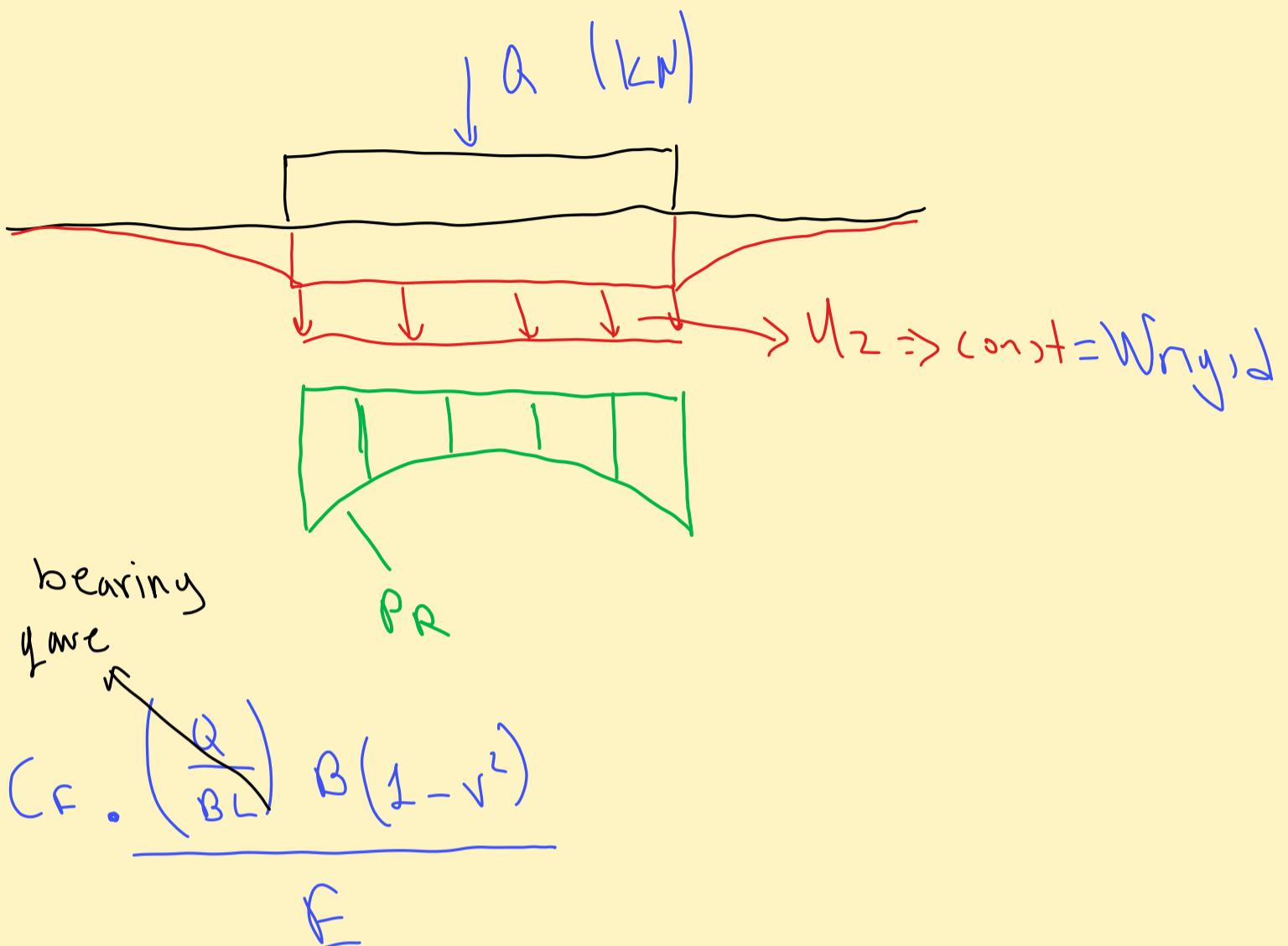
$$B = L = 10 \text{ m}$$



x	0	0.5	1.0	1.5	2	2.5	3	3.5	4	4.5	5.0
w	3.29	3.72	4.015	4.231	4.348	4.527	4.627	4.700	4.751	4.791	

x	5.5	6	6.5	7	7.5	8	8.5	9	9.5	10
w	4.781	4.751	4.700	4.672	4.572	4.398	4.231	4.015	3.726	3.29

Example 2 Perfectly Rigid Foundation



$$W_{\text{avg}, \text{id}} = C_F \cdot \frac{\left(\frac{Q}{BL}\right) B(1 - v^2)}{E}$$

$$C_F = 0,85 \left(\frac{L}{B}\right)^{0,45} \left[1 + 0,1 \left(2 + \frac{L}{B}\right) \frac{B}{H} \right]^{1 + \exp(-5\beta)}$$

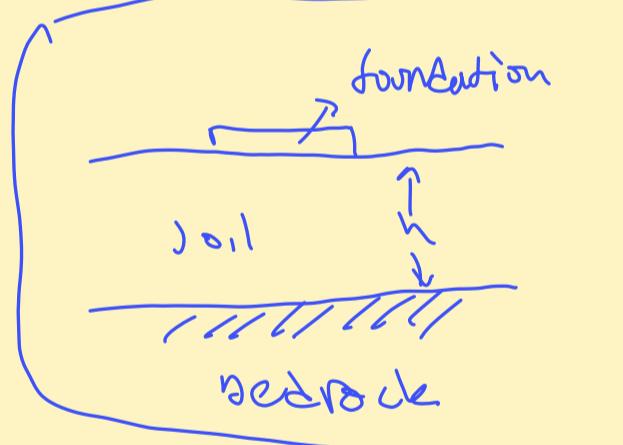
for $B = L$

$H \rightarrow$ very large

$$C_F = 0,85 \left(\frac{L}{B}\right)^{0,45} \left[1 + 0,1 \left(2 + \frac{L}{B}\right) \frac{B}{H} \right]^{1 + \exp(-5\beta)} \Rightarrow C_F = 0,85$$

$\downarrow 1,0$

$H \rightarrow$ thickness of soil



$$W_{rigid} = \frac{C_f \gamma_{WC} B (1 - v^2)}{E D_F} \rightarrow \text{stiffer soil} \rightarrow \text{less } W_{rigid}$$

$\Rightarrow B \uparrow \rightarrow \text{large } W_{rigid}$

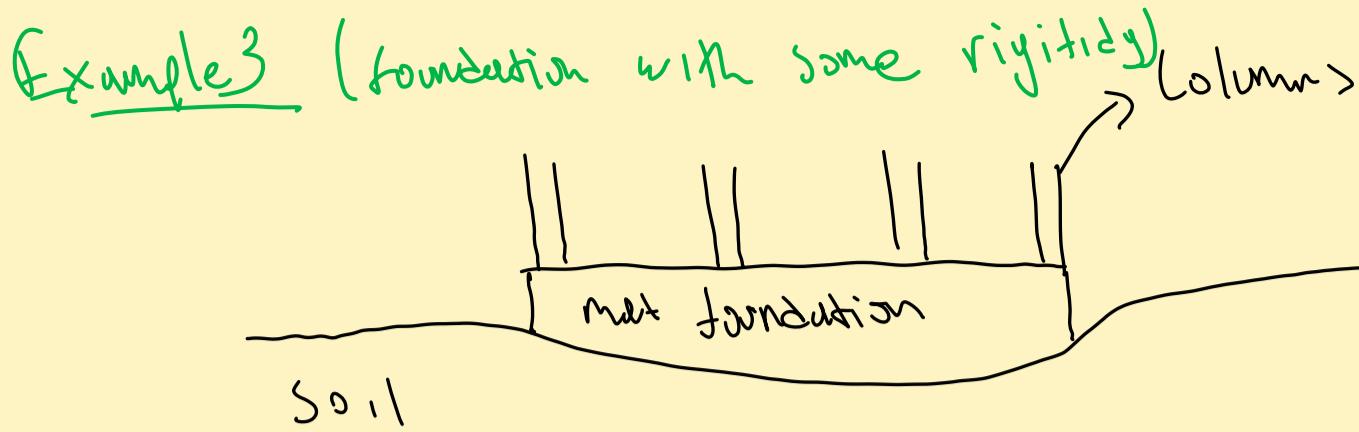
$D \rightarrow \text{embedment}$



$$D_F = 1 + (0.27 - 0.12 \ln v) \left(1 - \exp \left(-0.93 \left(\frac{D}{D_0} \right)^{0.83} \right) \right)$$

if $D = D_0$

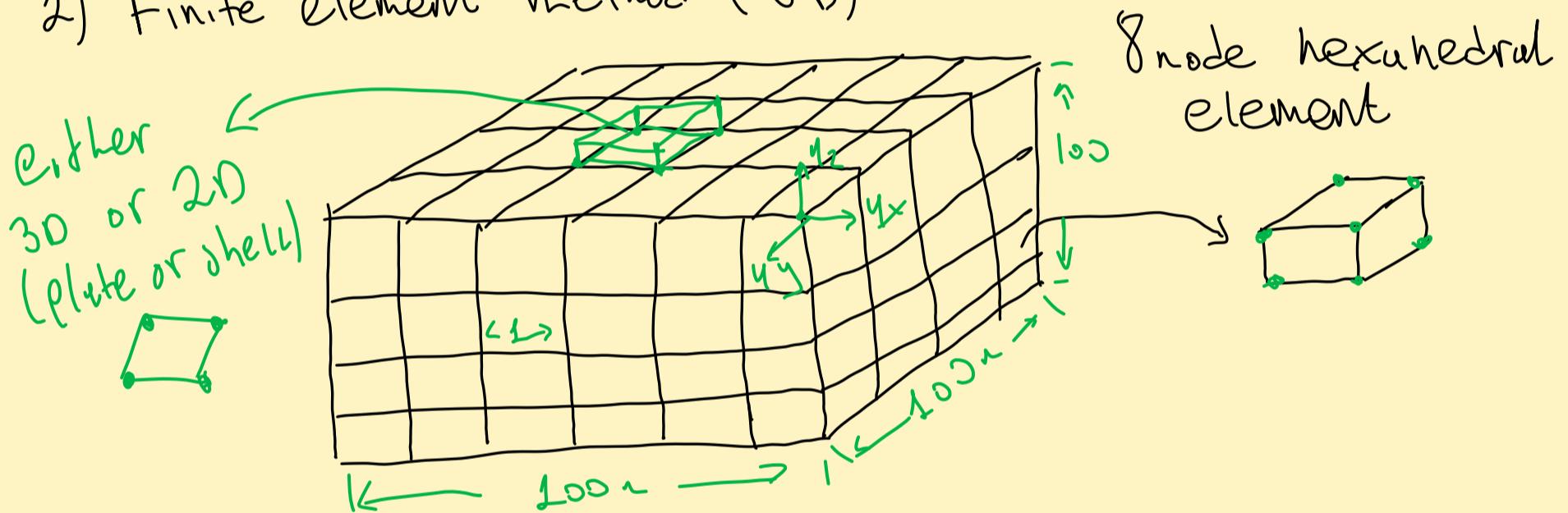
$\hookrightarrow D_F = 1$



1) "Exact" semi-analytical methods

- very complicated
- not all input has physical meaning

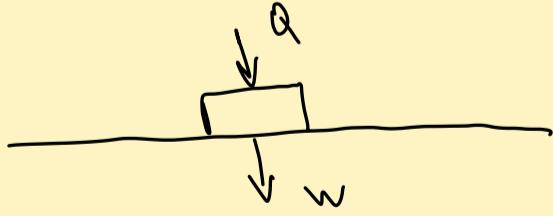
2) Finite element method (3D)



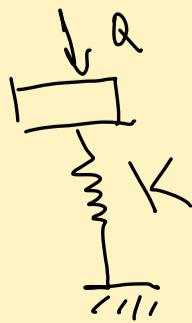
(Shell for modeling foundations in SAP 2000)

The FEM is very computationally costly

3) Winkler Spring Approach

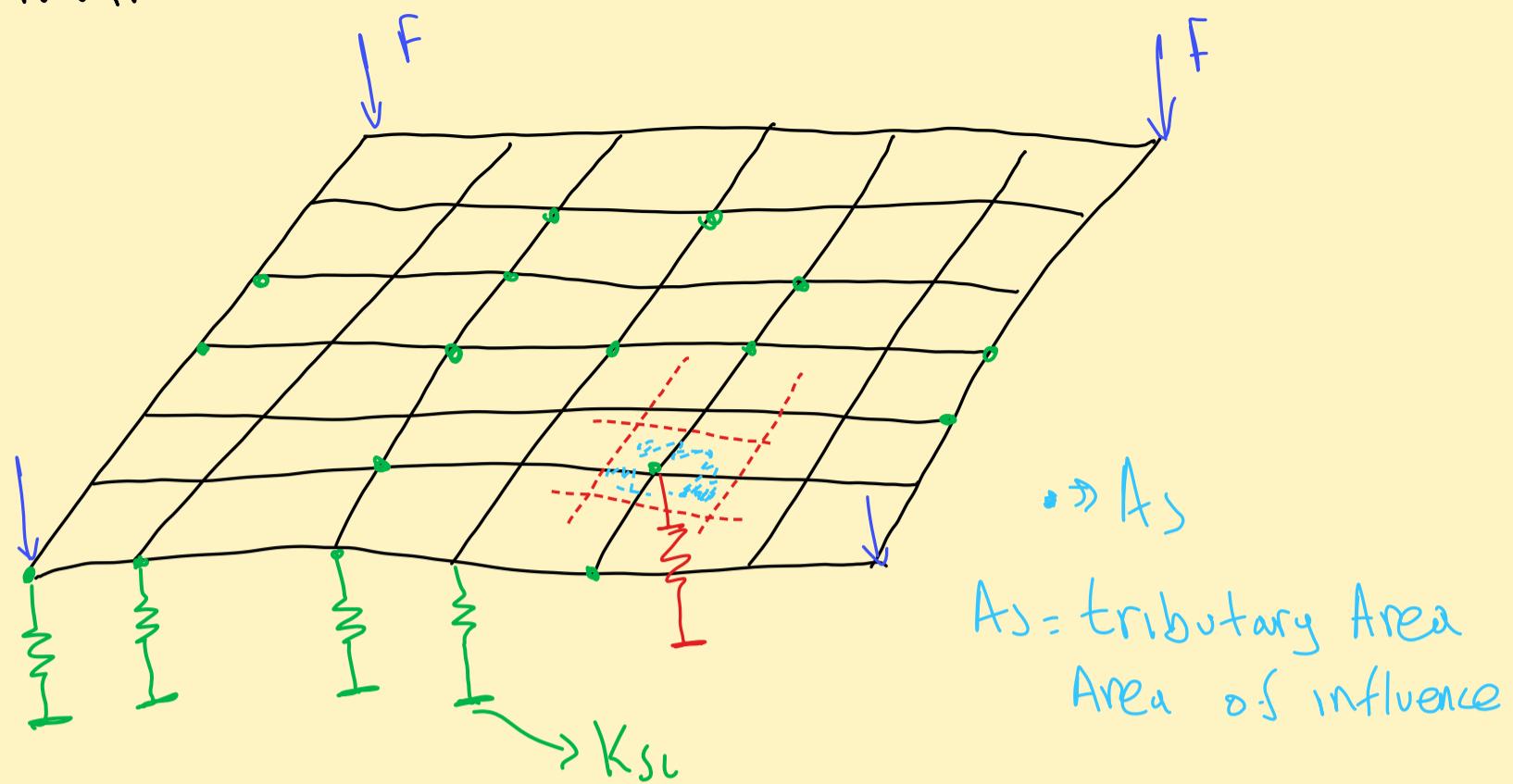


↓ equivalent static analog



$$W = \frac{Q}{K}$$

Mat Foundation



$\rightarrow A_s$
 $A_s = \text{tributary Area}$
 $\text{Area o.f influence}$

$$K_{SL} = k_s \cdot A_s$$

$k_s \rightarrow$ modulus of subgrade reaction (Stiffness & Stiffness)

$$\uparrow E \Rightarrow \uparrow k_s \quad \uparrow v \Rightarrow \uparrow k_s$$

$$W_{rigid} = \frac{q_{are} B(1-v^2)}{E}$$

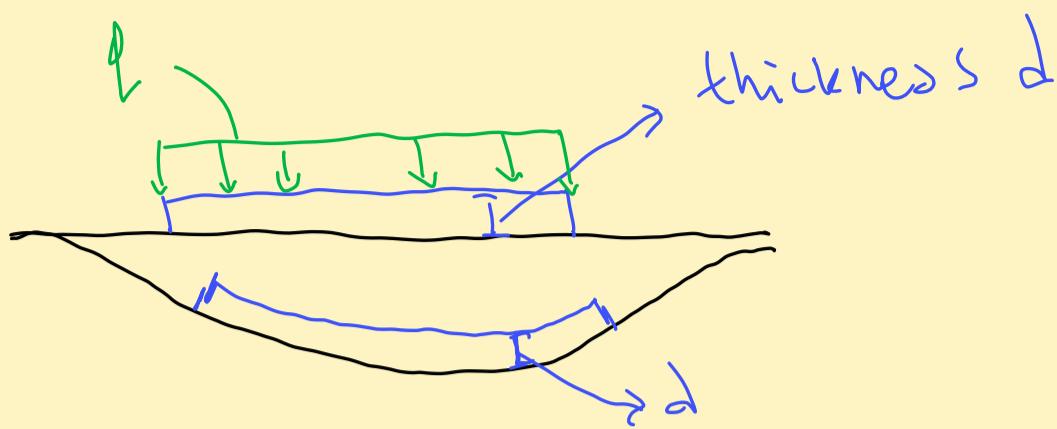
$$k_s = \frac{E}{B(1-v^2)}$$

$$k_s = \frac{q_{are}}{W_{rigid}}$$

$$q_{are} = \frac{Q}{BL}$$

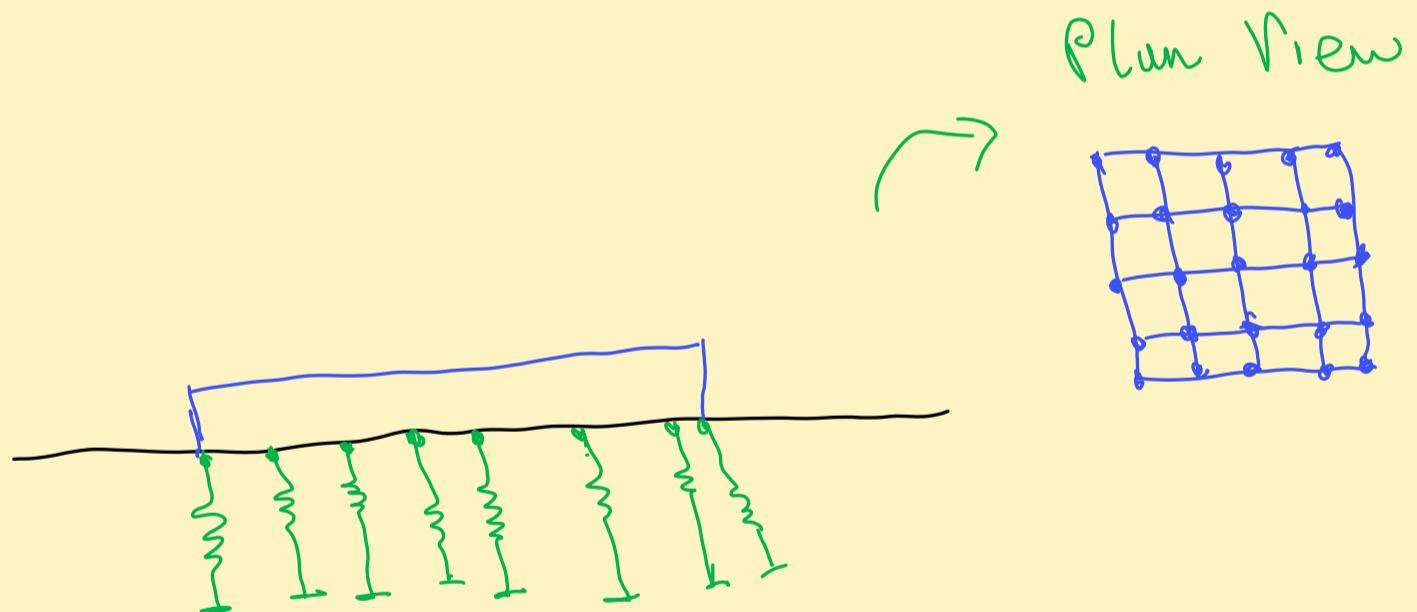
$W_{rigid} \rightarrow$ calculated using geotech approaches

14/9/23



Solution methodologies

- 1) Semi-analytical methods
- 2) 3-dimensional methods
 - very expensive (too much time)
- 3) Winkler springs approach
 - what we use in practice

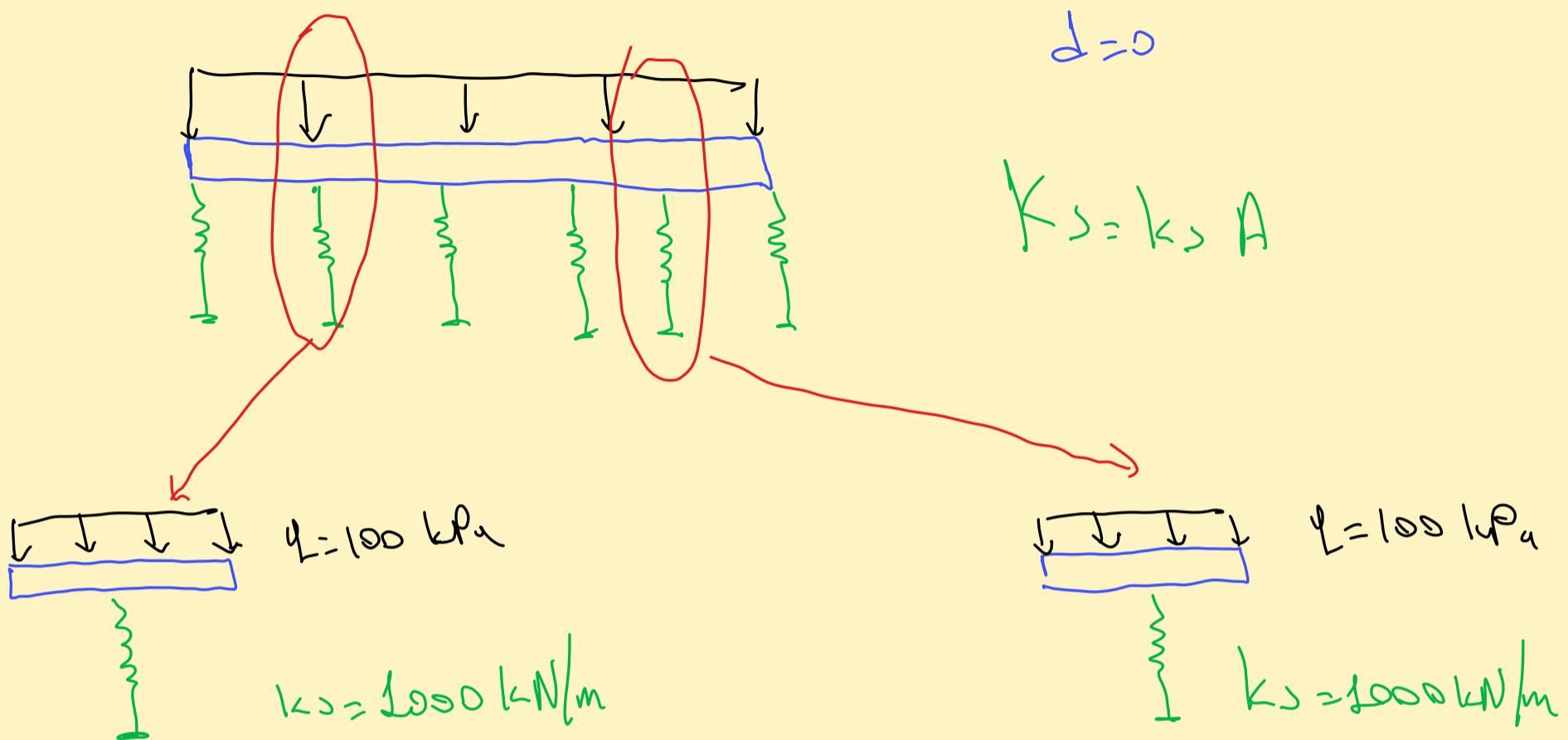


At each node we connect a spring, which has a k_s (spring coefficient)

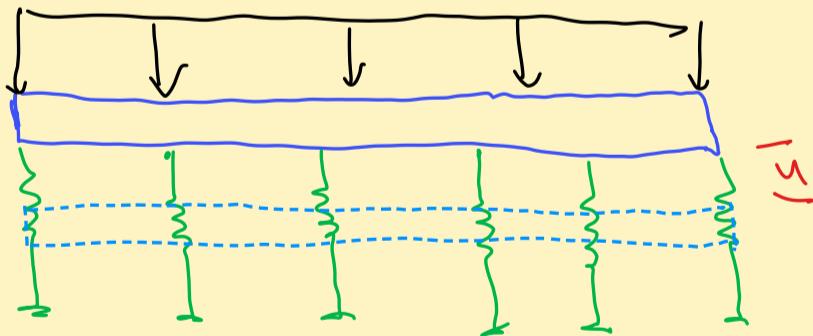
$$K_s = k_s A \quad A \rightarrow \text{area of influence}$$

$k_s \rightarrow$ Coefficient of subgrade reaction

Why we can't use the same k_s for every spring, example



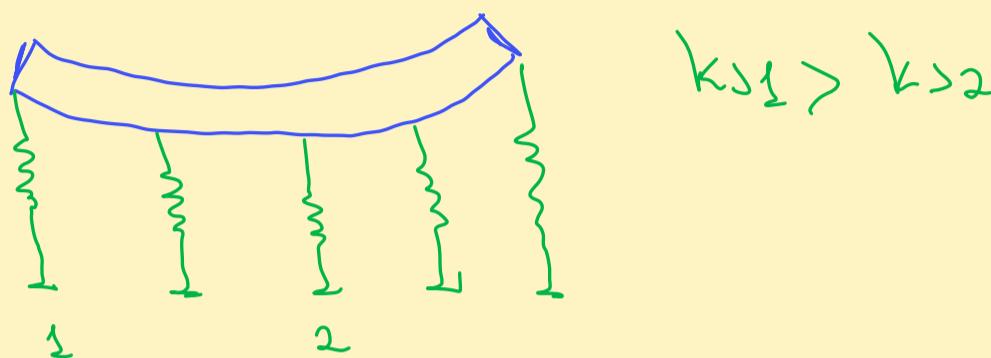
- ⇒ All spring will have the same displacements
- ⇒ The mat foundation will not bend (No moments will appear)



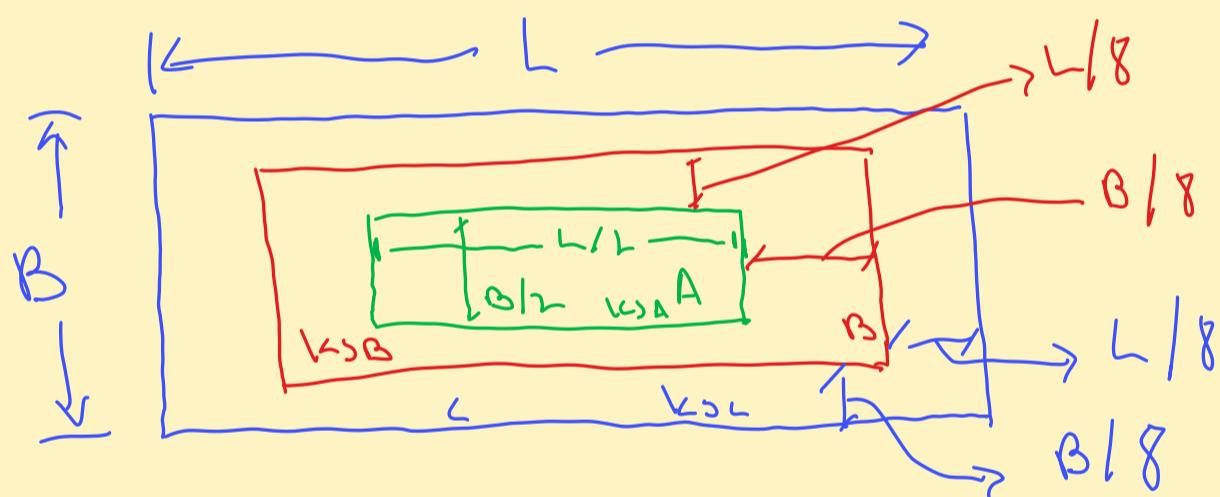
Solution to this problem \rightarrow Pseudo-coupled approach

Large $k_s \rightarrow$ on the edges of the mat

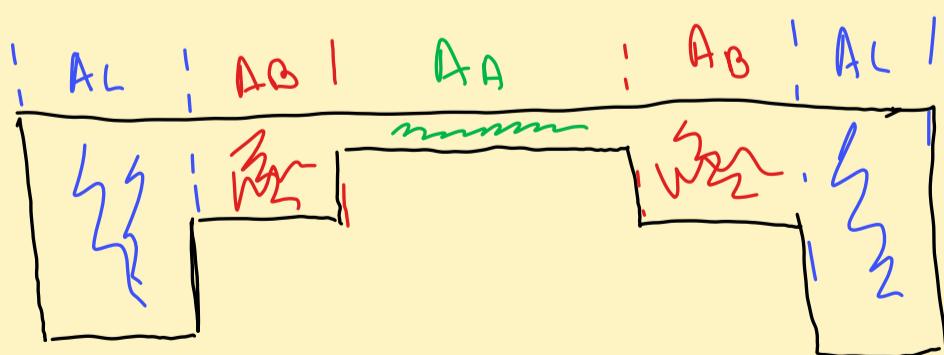
Small $k_s \rightarrow$ in the middle of the mat



Conduits Approach



Cross Section



$$\sum k_s = k_s A_C + k_s B A_B + k_s A_A + A_A$$

$$K = k_s A_s$$



$$k_{s, \text{rigid}} = \frac{q_{\text{ave}}}{w_{\text{rigid}}} \quad q_{\text{ave}} = \frac{\sum Q}{A_{\text{tot}}} \rightarrow \text{Area of mat}$$

$$k_{s, \text{average}}$$

$$\sum k_s = k_{s, \text{rigid}} \cdot A_{\text{total}}$$

$$k_s A_C + k_s B A_B + k_s A_A = k_{s, \text{rigid}} A_{\text{tot}}$$

$$A_{\text{total}} = B \cdot L$$

$$A_A = \frac{B}{2} \cdot \frac{L}{2} \Rightarrow A_A = \frac{BL}{4}$$

$$A_B = \left(\frac{4B}{8} + \frac{B}{8} + \frac{B}{8} \right) \left(\frac{4L}{8} + \frac{L}{8} + \frac{L}{8} \right) - \frac{BL}{4}$$

$\downarrow \quad \quad \quad \downarrow \quad \quad \quad \downarrow$
 $\frac{6B}{8} = \frac{3}{4} B \quad \quad \quad \frac{3L}{4} \quad \quad \quad \frac{4BL}{16}$

$$A_B = \frac{5}{16} BL$$

$$A_L = BL - \frac{9}{16} BL \Rightarrow A_L = \frac{7}{16} BL$$

$$\Rightarrow k_{SL} \frac{7}{16} BL + k_{SB} \frac{5}{16} BL + k_{SA} \cdot \frac{4}{16} BL = k_s, \text{rigid} \cdot \frac{16}{16} BL$$

$$\Rightarrow 7k_{SL} + 5k_{SB} + 4k_{SA} = 16 k_s, \text{rigid}$$

$$\Rightarrow 0.4375 k_{SL} + 0.3125 k_{SB} + 0.25 k_{SA} = k_s, \text{rigid}$$

Conduo Proposed.

$$k_{SL} = 2k_{SA}$$

$$k_{SB} = 1.5k_{SA}$$

$$\Rightarrow 0.4375 \cdot 2k_{SA} + 0.3125 \cdot 1.5k_{SA} + 0.25k_{SA} = k_s, \text{rigid}$$

$$\Rightarrow k_{SA} = \frac{k_s, \text{rigid}}{0.4375 \cdot 2 + 0.3125 \cdot 1.5 + 0.25}$$

$$\Rightarrow k_{SA} = 0.627 k_s, \text{rigid}$$

$$k_{SB} = 0.941 k_s, \text{rigid}$$

$$k_{SL} = 1.255 k_s, \text{rigid}$$

Conduo Approach (2001)

$$W_{rigid} = \frac{C_F \cdot q_{ave} B (1 - v^L)}{E D_F}$$

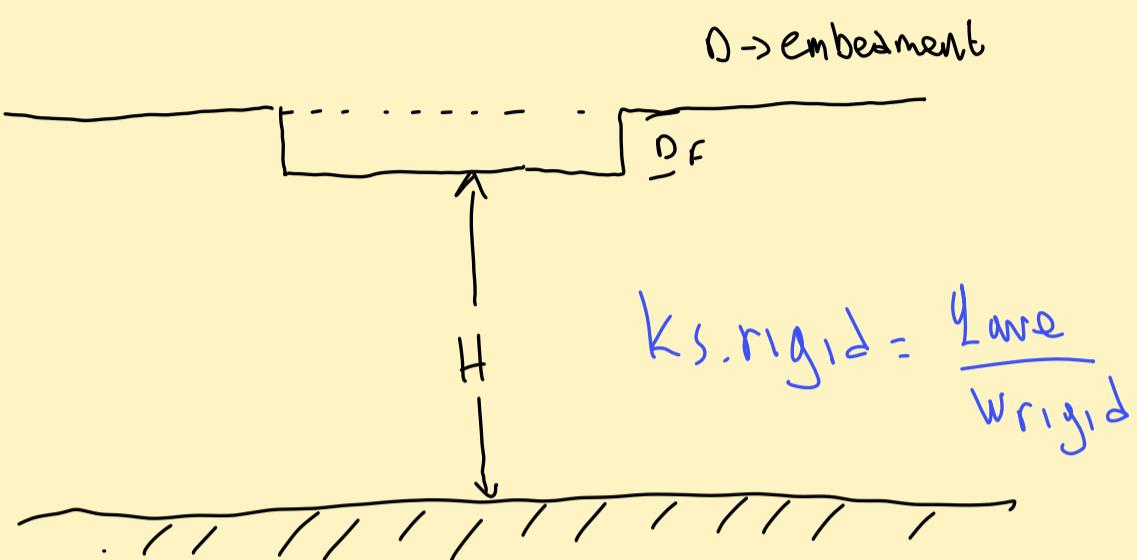
C_F → "Shape Factor"

D_F → Depth Factor

B → Width

E → Young's modulus

v → Poisson's Ratio



$$C_F = 0,85 \left(\frac{L}{B} \right)^{0,45} \frac{1}{\left[1 + 0,1 \left(2 + \frac{L}{B} \right) \frac{B}{H} \right]^{1 + \exp(5v)}}$$

$$D_F = 1 + (0,27 - 0,12 \ln v) (1 - \exp(-0,93 \left(\frac{D}{B} \right)^{0,83}))$$

if $D = 0$

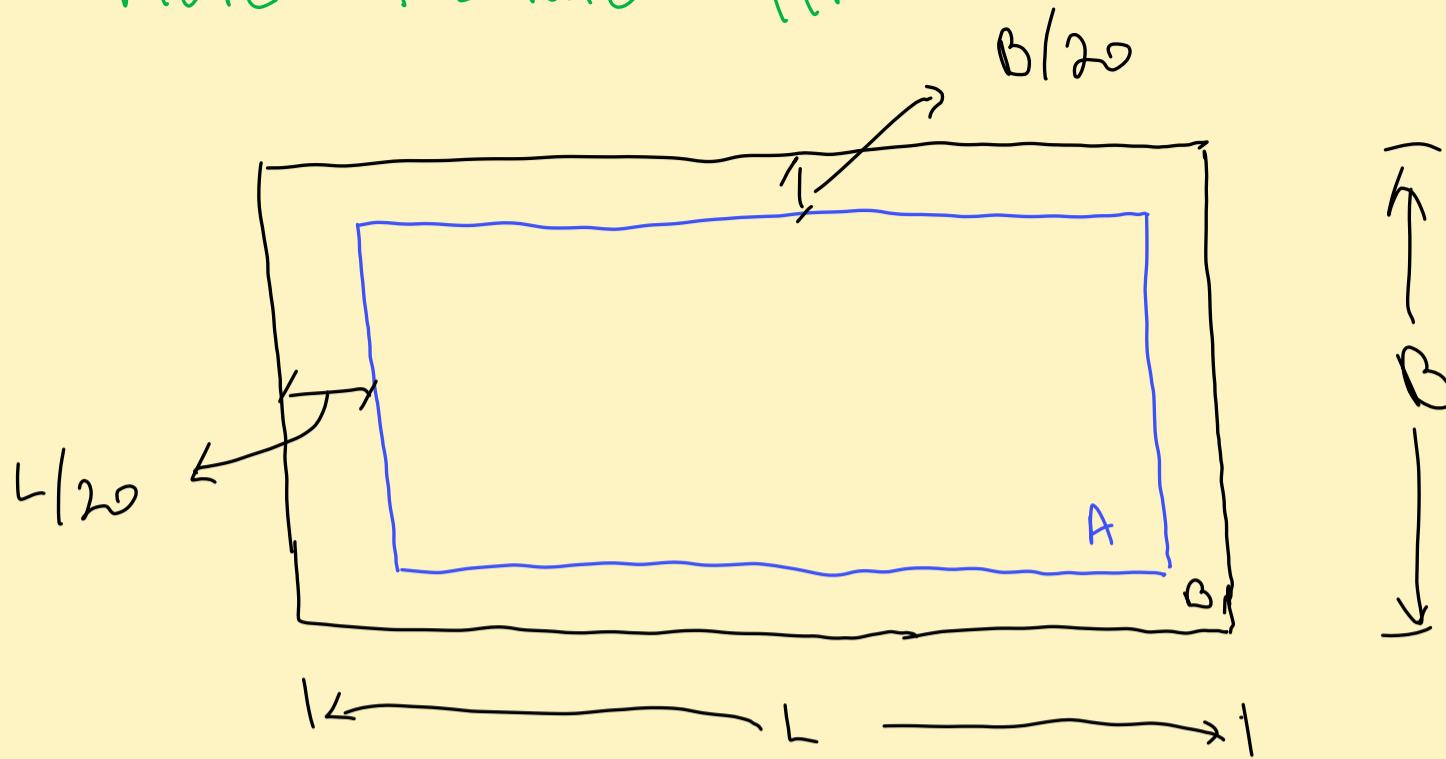
$\hookrightarrow D_F = 1$

Concrete Approach

↳ Good for 2-5 storey buildings

↳ Underestimates positive moments

More Accurate Approach



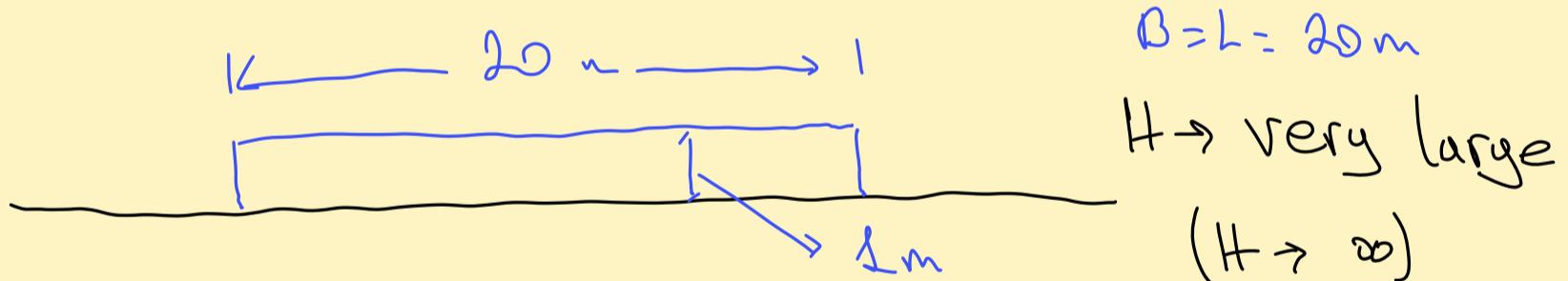
$$k_s B = 4 k_s A$$

EXAMPLE

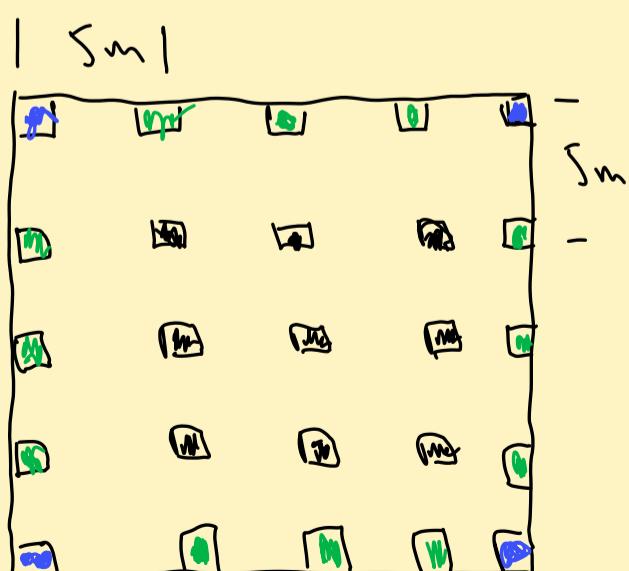
$$\sigma = 0 \Rightarrow \sigma_F = 1$$

$$E_s = 20000 \text{ kPa}$$

$$r_s = 0.3$$



Plan View



Columns carry $\approx 250 \text{ kN}/\text{floor}$

For 4 floors $\rightarrow 1000 \text{ kN}$
 \hookrightarrow interior columns

for columns on the side
 $\hookrightarrow 500 \text{ kN}$ (less Area)

for corner columns

$\hookrightarrow 250 \text{ kN}$ (less Area)

$$q_{ave} = \frac{\sum Q}{A_{total}} = \frac{9200 + 12.500 + 4250}{20 \cdot 20}$$

$$q_{ave} = \frac{16000 \text{ kN}}{400 \text{ m}} \Rightarrow q_{ave} = 40 \text{ kPa}$$

$$C_f = 0,85 \left(\frac{L}{B} \right)^{0,45} \quad \Rightarrow \quad C_f = 0,85 \\ \left[1 + 0,1 \left(2 + \frac{L}{B} \right) \frac{B}{H} \right]^{1 + \exp(-5\beta)}$$

$$D_F = 1 + (0,27 - 0,12 \ln v) (1 - \exp(-0,93 \left(\frac{v}{v_0} \right)^{0,83}))$$

if $v = 0$
 $\hookrightarrow D_F = 1$

$$W_{rigid} = \frac{C_f \cdot q_{ave} \cdot B (1 - v^2)}{E \cdot D_F} \Rightarrow W_{rigid} = 0,062 \text{ m}$$

$W_{rigid} = 62 \text{ cm}$

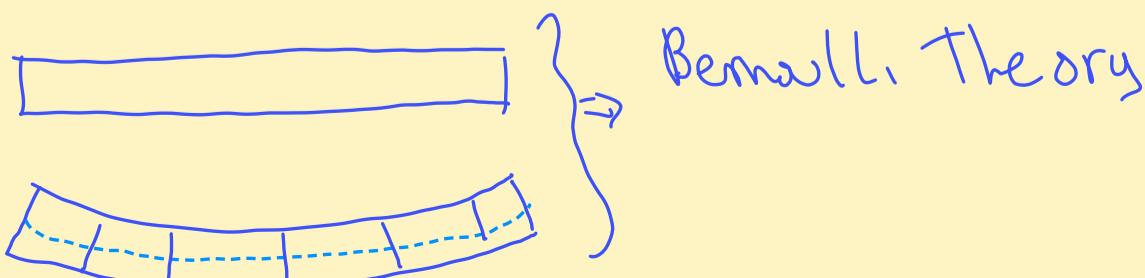
$$k_{s, rigid} = \frac{q_{ave}}{W_{rigid}} = \frac{40 \text{ kPa}}{0,062} \Rightarrow k_{s, rigid} = 645 \frac{\text{kPa}}{\text{m}}$$

$$k_{SA} = 0,627 k_{s, rigid} \Rightarrow k_{SA} = 404 \text{ kPa/m}$$

$$k_{SB} = 0,441 k_{s, rigid} \Rightarrow k_{SB} = 276 \text{ kPa/m}$$

$$k_{SL} = 1,255 k_{s, rigid} \Rightarrow k_{SL} = 808 \text{ kPa/m}$$

SAP 2000



	Beams	Plates / Shell
Thin formulation	Euler	Bernoulli
Thick formulation	Timoshenko	Mindlin

Thin \rightarrow good for very flexible elements
 \rightarrow does not take into account shear deformation

Thick \rightarrow takes account shear deformations

* On Mat foundations we select thick shell because we have many springs which are close to each other therefore the mat foundation is not flexible

28/9/23

* \rightarrow The plates (foundation and slabs) we must always mesh our area SAP 2000

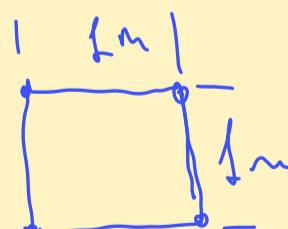
User FEM

using Assign Automatic Area Mesh

Proper Size of elements



or



for bigger structures

Case 1 $\Rightarrow k_{s,\text{rigid}}$ is uniform

$$k_{s,\text{rigid}} = 645 \text{ kPa/m}$$

For the centre column (green color \rightarrow positive M)

$$m = 184 \text{ kNm/m}$$

$$r = 272 \text{ kN/m}$$

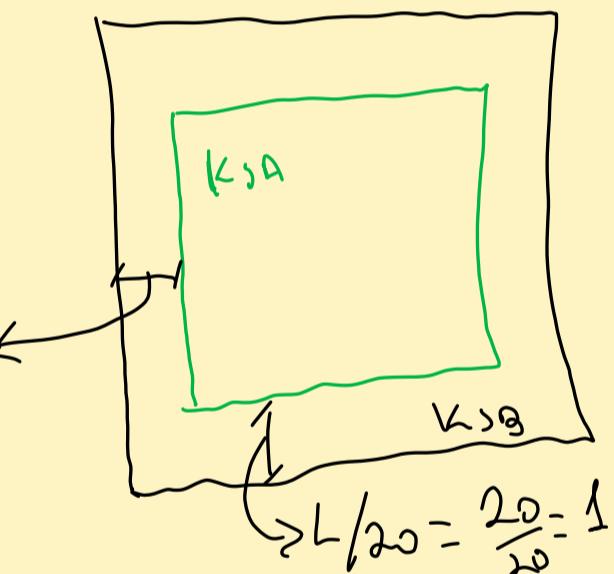
for the middle of the span

$$M_{\min} = 130 \text{ kNm/m}$$

Case 2 \rightarrow

$$B = L = 20$$

$$I = \frac{B_1}{20}$$



$$k_{sA} = 0,66 k_{s,\text{rigid}}$$

$$k_{sA} = 426 \text{ kPa/m}$$

$$k_{sB} = 1,75 k_{s,\text{rigid}}$$

$$k_{sB} = 1129 \text{ kPa/m}$$

For the centre column

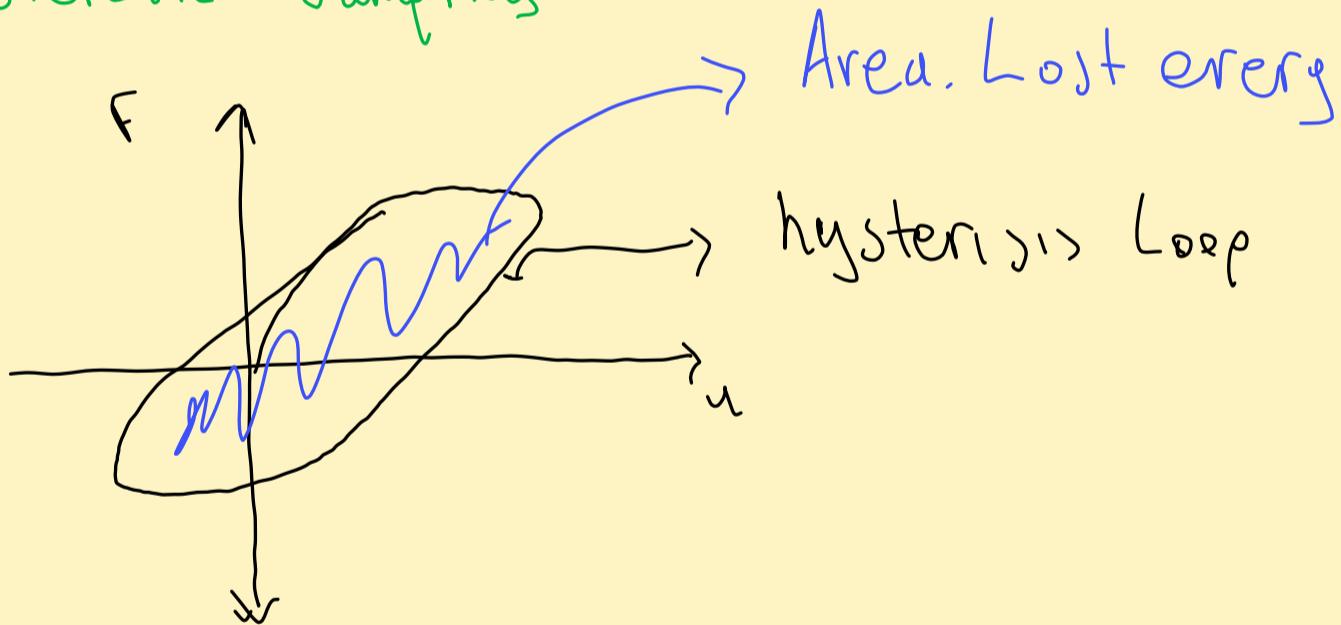
$$m = 521 \text{ kNm/m}$$

$$m_{\min} = -69 \text{ kNm/m} \quad (\text{at different position})$$

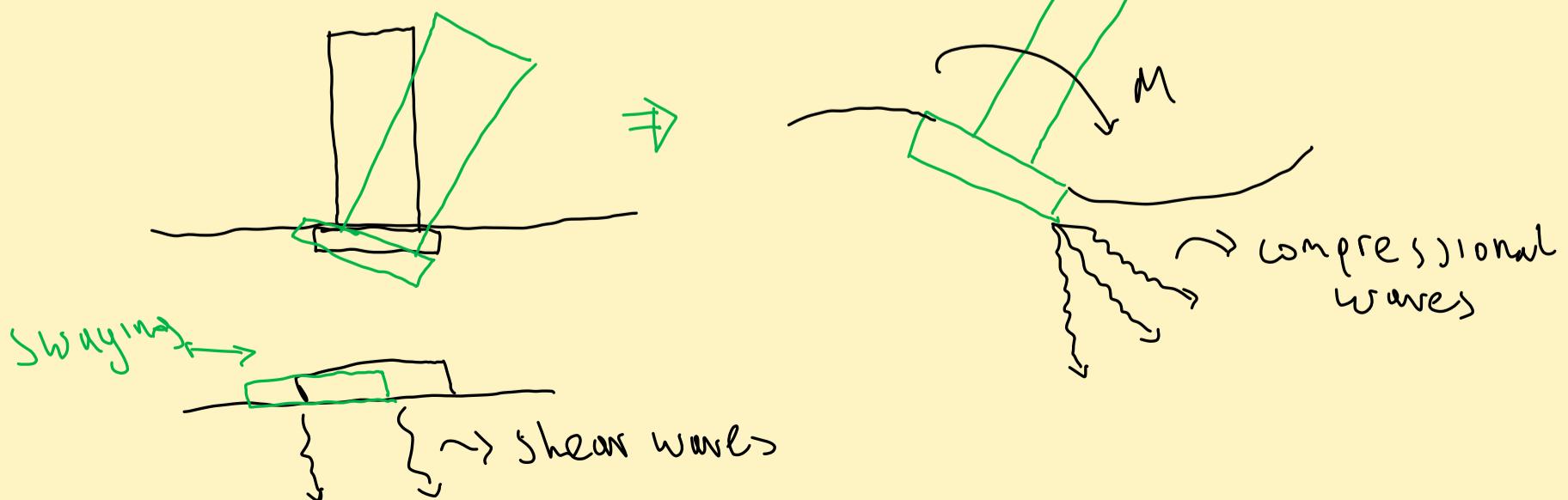
$$r = 239 \text{ kN/m}$$

Eurocode 8

- Shall → requirement
(must)
 - Should → recommendation
 - may → an option
-
- The natural T of a building is higher if it have SSI (soil structure interaction)
 - SSI gives us higher damper
- Two kinds of damping
- Hysteretic Damping

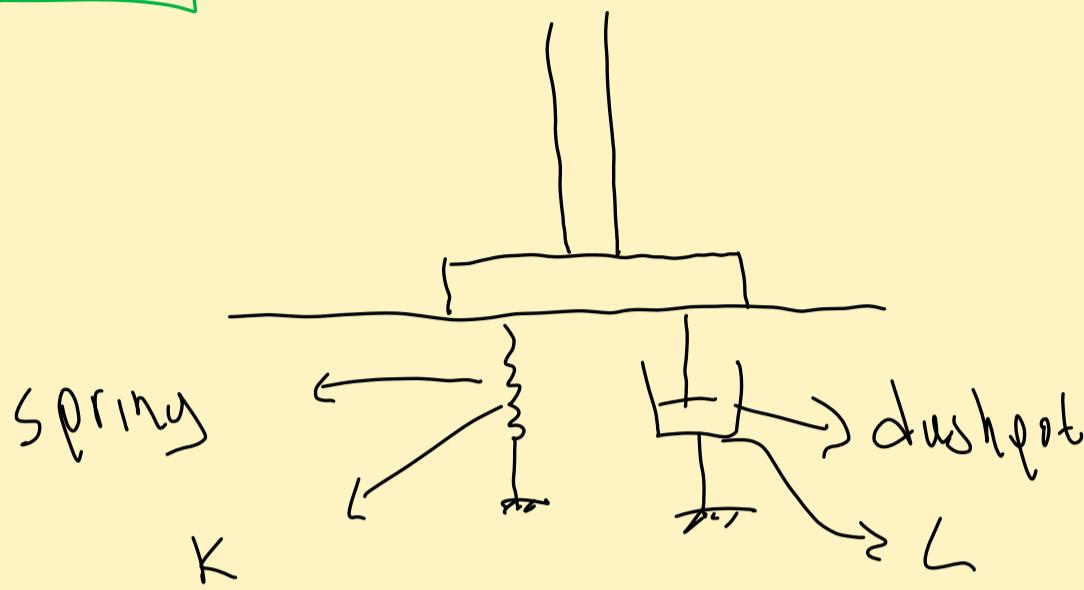


- Radiation Damping



Energy \rightarrow lost due to the travelling of the waves

28/9/23

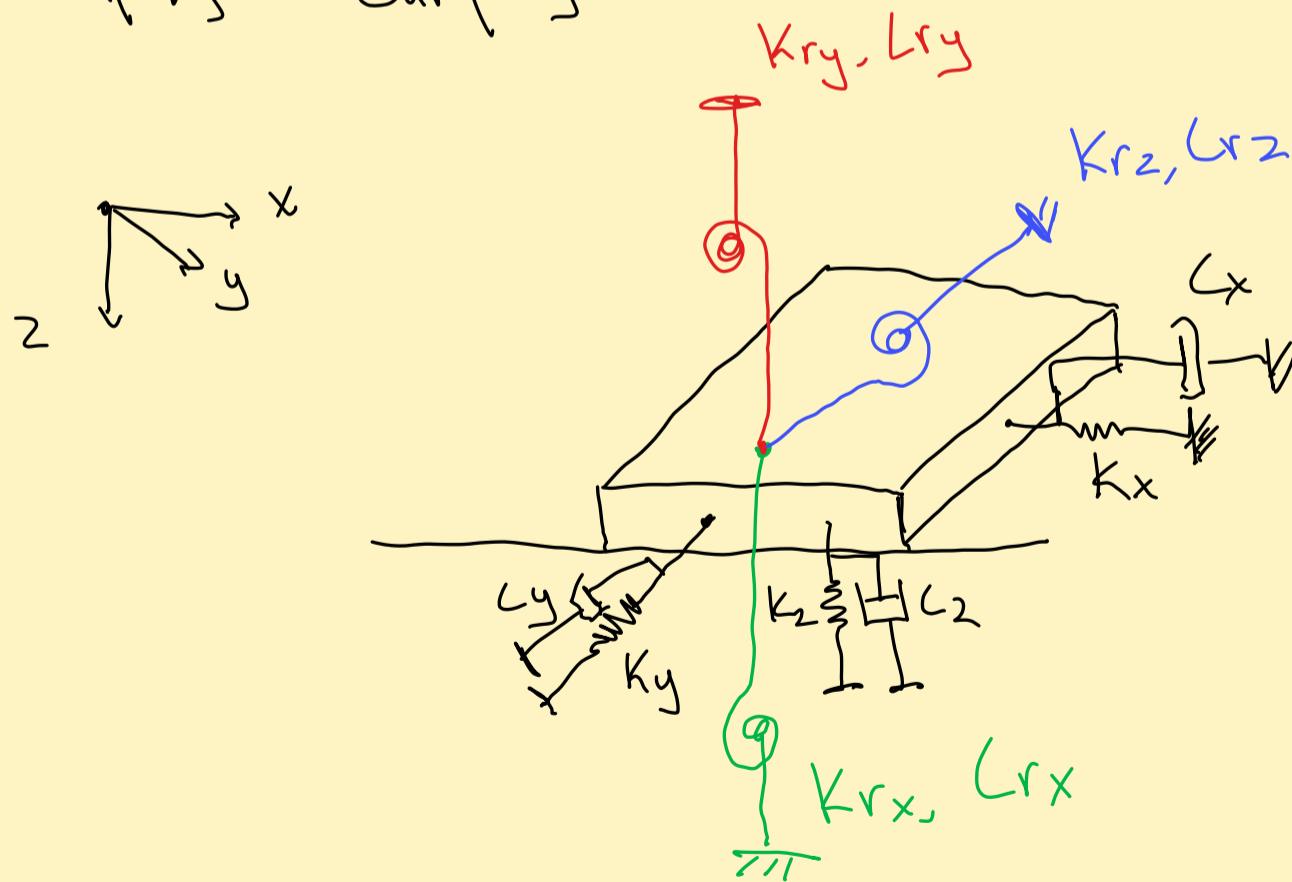


$$K = K_{\text{stat}} + K_{\text{dyn}}(\omega) \quad \begin{matrix} \text{frequency} \\ \text{of vibration} \end{matrix}$$

$$C = C_{\text{rad}} + C_{\text{hyst}} \quad \begin{matrix} \downarrow \\ \text{radiation damping} \end{matrix} \quad \begin{matrix} \downarrow \\ \text{hysteric damping} \end{matrix}$$

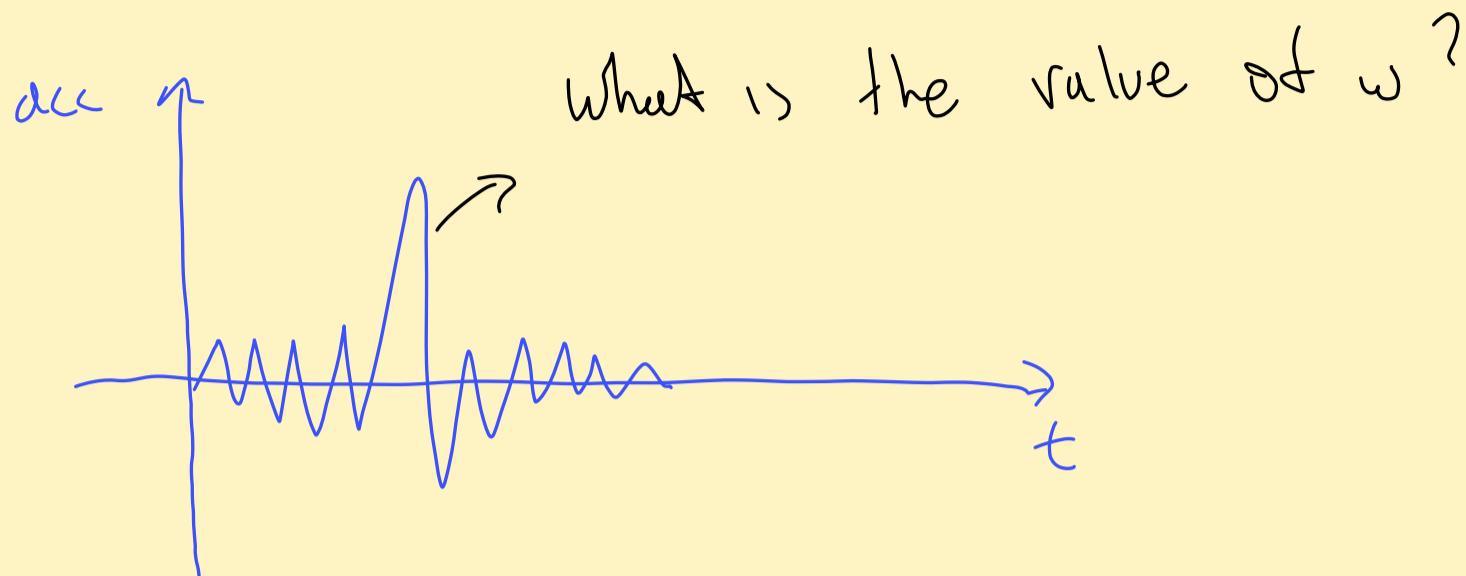
$$\omega = \frac{2\pi}{T}$$

smash
→ distributed
→ spring
capital



$$C_{\text{hyst}} = \frac{2K}{\omega} \cdot \beta_{\text{hyst}}$$

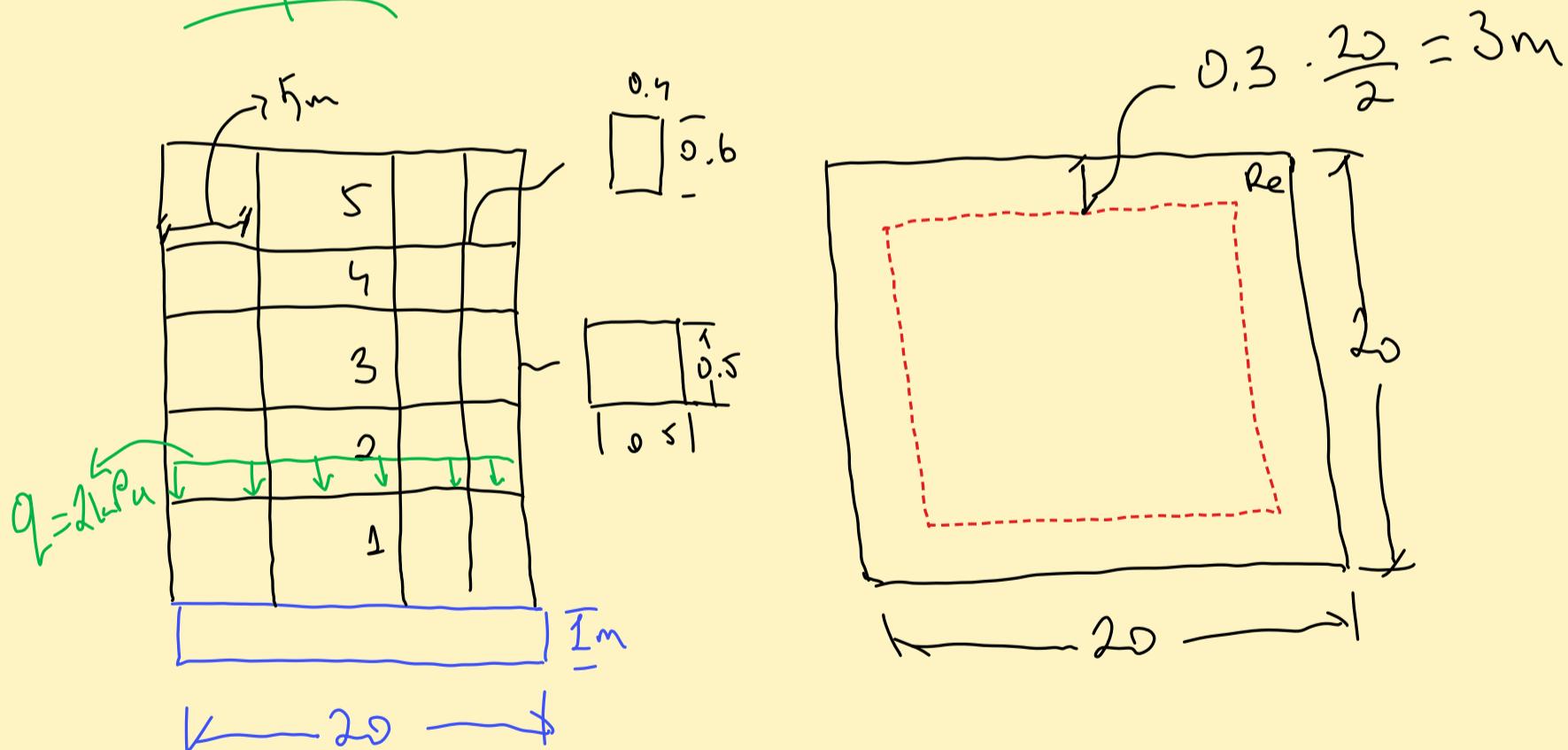
$$\omega_0 = \frac{w \cdot B \rightarrow \beta / 2}{\sqrt{s}}$$



$$\omega_1 = \frac{2\pi}{T_1} \quad T_1 \rightarrow \text{fundamental period of the structure}$$

Example 3 (IAP 2000)

Plan View



$$\left. \begin{array}{l} S_u = 200 \text{ kPa} \\ \rho = 2 \text{ ton/m}^3 \end{array} \right\} \text{Soil category}$$

$\hookrightarrow C$

$\therefore \text{Limbosol} \rightarrow a = 0.25y$

$$G + 0.3Q + F$$

Thickness of slabs = 0.2 m

\hookrightarrow Shell-thin

$r = 0.5$ (for clay)

$\zeta \rightarrow$ dead

for soil category $C \Rightarrow S=1,15$

$\alpha \rightarrow$ live

$$\alpha \cdot S = 0,25g \cdot 1,15$$

$F \rightarrow$ Quake

$$\alpha \cdot S = 0,29g$$

$$S_{0,1} \} = 0,10$$

$$V_s / V_{smax} = 0,6$$

$$G / G_{max} = 0,36$$

FL8 §423 Table 41

$$G_{max} = 1000 \text{ su}$$

$$G_{max} = 100000 \text{ kPa} \Rightarrow G = 0,36 \cdot 100000$$

$$G = 36000 \text{ kPa}$$

Vertical

$$k_s = \frac{G}{(1-v)B} (0,73 + 1,54 \left(\frac{B}{L}\right)^{0,75}) k_{dyn,2}$$

Guzzetta 1990
Slides Kipu
UTTO SST

$$= \frac{36000}{(1-0,5) 20} (0,73 + 1,54 \cdot 1) k_{dyn,2}$$

↳ 2,27

$$a_0 = \frac{\omega B^*}{v_s}$$

$$V_s = \sqrt{\frac{G}{\rho}} = \sqrt{\frac{36000}{2}} \Rightarrow V_s = 134 \text{ m/s}$$

$$\omega_L = \frac{2\pi}{T_1} \quad T_1 = 0.43 \text{ s} \quad (\text{from SAP 2000})$$

$$\omega_L = \frac{2\pi}{0.43} \Rightarrow \omega_L = 14.6 \text{ rad/sec}$$

$$a_0 = \frac{\omega B^*}{v_s} \Rightarrow a_0 = 1.1 \quad B^* = B/2$$

Gazetas
 $B = B^* - B/2$

Gazetas Tables (Page 21)

→ Using a_0 and B/L
 $\rightarrow k_{dyn,2} = 0,9$ → graph (a) Gazetas

Table 15.1

Vertical (z)

$$k_z = \frac{G}{(1-v)B} (0.73 + 1.54 \cdot 1) \quad 0,9$$

$$k_z = 7355 \text{ kPa/m}$$

$$k_y = \frac{G}{(2-v)} \left[2 + 2.5 \left(\frac{B}{B} \right)^{0.85} \right] k_{dyn,y} \rightarrow \text{slide Kano into SSJ}$$

Gazetas Table (15.1)

$$k_{dyn,y} = 0.95$$

$$\rightarrow k_y = 5130 \text{ kPa/m}$$

$$k_x = k_y \Rightarrow k_x = 5130 \text{ kPa/m}$$

NIST Approach (Calculation of R_k , R_c)

Using Gazetas (Torsional)

$$K_{ry} = \frac{3.66 B^3}{1-\nu}$$

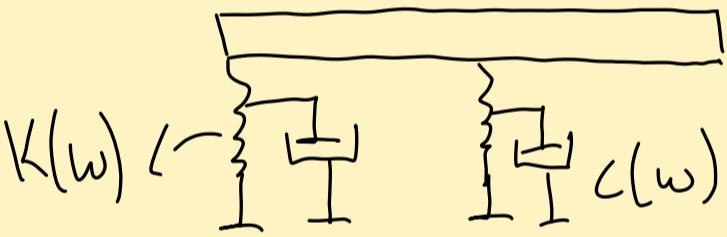
$$K_{ry} = \frac{36 \cdot 36000 \left(\frac{20}{2}\right)^3}{1-0.5} \Rightarrow kPa \rightarrow \frac{kN}{m^2} \rightarrow kNm$$

$$R_k = \frac{\left(\frac{K_{ry}}{k_s (BL^3/12)} \right) - (1-R_e)^3}{1-(1-R_e)^3}$$

$$R_k = 3.5$$

$$k_s = 7355 \text{ kPa/m}$$

5/10/23 example 3 mit Gazeta



$$Ab = 20^2 = 400 \text{ m}^2$$

Lateral velocity

$$VL_a = \frac{3.4}{\pi(1-\nu)} V \rightarrow VL_a = 290 \text{ m/s}$$

$$\bar{c}_2 = 0.95 \cdot 1.01 \Rightarrow \bar{c}_2 = 0.95$$

\hookrightarrow Add graph Gazeta (ν)

Formulas according to Gazetas (1990) for shallow foundation on soil layer of large thickness (no influence of bedrock)

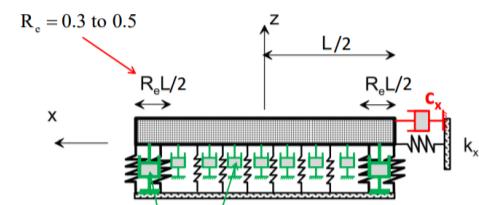
$$k_s = \frac{K_s}{BL} = \frac{G}{(1-\nu)B} \left(0.73 + 1.54 \left(\frac{B}{L} \right)^{0.75} \right) k_{dyn,z} \quad c_z = \rho \frac{3.4}{\pi(1-\nu)} V_s \tilde{c}_z$$

$$K_{rx} = \frac{G}{(1-\nu)} \left(\frac{LB^3}{12} \right)^{0.75} \left(\frac{L}{B} \right)^{0.25} \left(2.4 + 0.5 \frac{B}{L} \right) k_{dyn,rx} \quad C_{rx} = \rho \frac{3.4}{\pi(1-\nu)} V_s \frac{LB^3}{12} \tilde{c}_{rx}$$

$$k_y = \frac{K_y}{BL} = \frac{G}{(2-\nu)B} \left(2 + 2.5 \left(\frac{B}{L} \right)^{0.85} \right) k_{dyn,y} \quad c_x = \rho V_s \tilde{c}_x$$

$$k_x = k_y - \frac{0.1G}{(0.75-\nu)B} \left(1 - \frac{B}{L} \right) \quad c_y = \rho V_s \tilde{c}_y$$

NIST approach (2012)



Spring stiffness: $R_k \times k_s \times dA$, $R_c \times c_z \times dA$, $k_s \times dA$, $R_k \times k_s \times dA$ (dA =tributary area for individual spring)

$$R_k = \frac{\left(\frac{K_{ry}}{k_s (BL^3/12)} \right) - (1-R_e)^3}{1-(1-R_e)^3}$$

$$R_c = \frac{\left(\frac{C_{rx}}{c_z (BL^3/12)} \right)}{R_k (1-(1-R_e)^3) + (1-R_e)^3}$$

$$R_k = \frac{\left(\frac{K_{rx}}{k_s (LB^3/12)} \right) - (1-R_e)^3}{1-(1-R_e)^3}$$

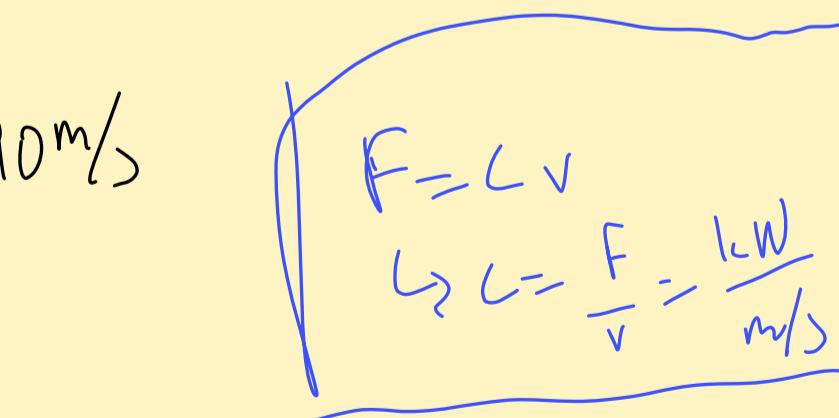
$$R_c = \frac{\left(\frac{C_{rx}}{c_z (LB^3/12)} \right)}{R_k (1-(1-R_e)^3) + (1-R_e)^3}$$

$$kN/m/s \rightarrow kN/m$$

$$c_2 = (\rho \sqrt{L_a A_b}) \bar{c}_2$$

$$d_0 = \frac{\omega B}{\sqrt{s}} \xrightarrow{*} \frac{B}{L} = 1.1 \text{ m/s}^2$$

$$V_s = 134 \text{ m/s}$$



Graph L $kN/m/s$
tangential

$$\frac{\bar{c}_2 (\nu=0.5)}{\bar{c}_2 (\nu=0.4)}$$

$$(c_2 = (2 \cdot 290 \cdot 400) \cdot 0,95$$

$$c_2 = 220400 \frac{\text{kN s}}{\text{m}}$$

graph ↗

$$(c_x = c_y = p \sqrt{s} A_b 0,95$$

$$= 2 \cdot 134 \cdot 400 \cdot 0,95$$

$$(c_x = c_y = 101840 \frac{\text{kN s}}{\text{m}}$$

Small c

- $\rightarrow \mu_{1140}$ damping ratio (%)
- \rightarrow higher Karlsruhe effects
- \rightarrow higher displacement surfaces

$$c_2 = \frac{c_2}{A_b} = \frac{220400}{400} \Rightarrow c_2 = 551 \frac{\text{kN s}}{\text{m}^3}$$

$$c_x = c_y = \frac{c_x}{A_b} = \frac{c_y}{A_b} = \frac{101840}{400} \Rightarrow c_x = c_y = 255 \frac{\text{kN s}}{\text{m}^3}$$

$$c_{ry} = p \frac{34}{\pi(1-v)} \text{ vs } \frac{LB^3}{12} \quad (\text{rysides})$$

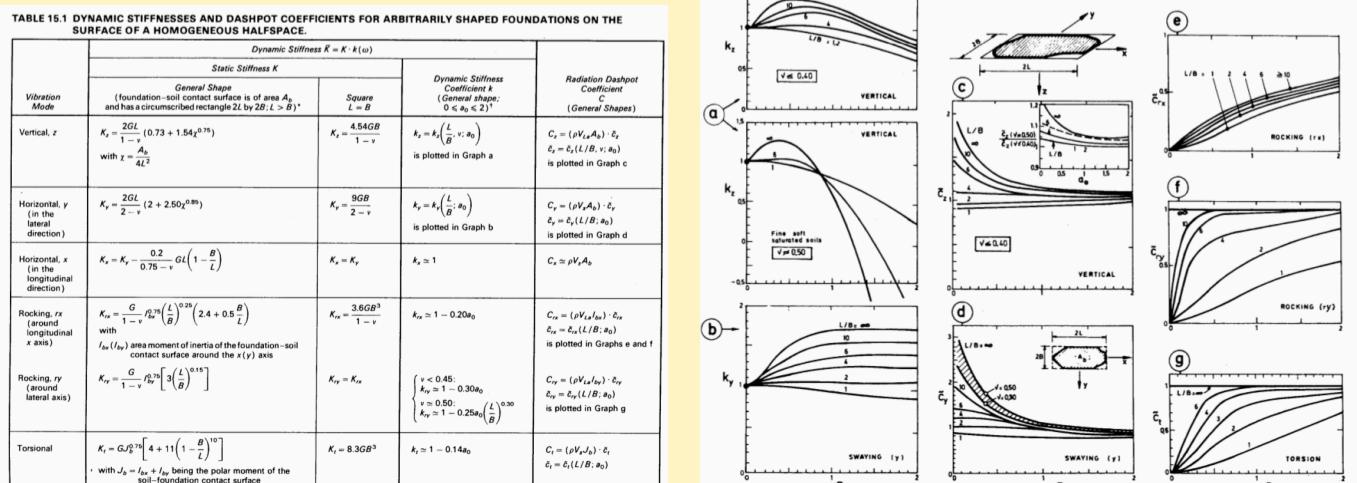
$\bar{c}_{ry} = 0,4 \rightarrow$ (squares) graph f

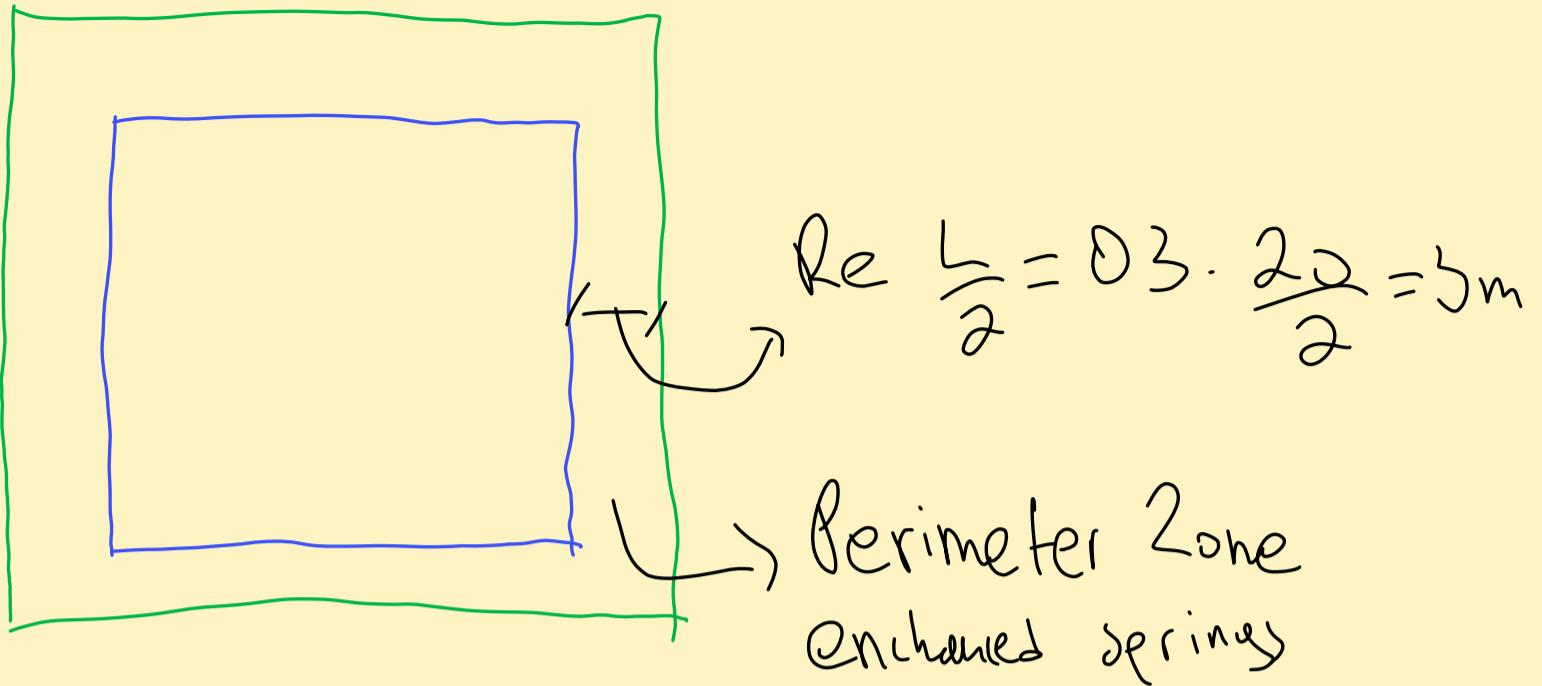
$$(c_{ry} = 2 \cdot \frac{34}{0,5\pi} \cdot 134 \cdot \frac{20^4}{12} \cdot 0,4 \Rightarrow c_{ry} = 30519125 \frac{\text{kNm}}{\text{s}})$$

$$R_L = \left(\frac{c_{ry}}{c_2 (BL^3/12)} \right)^3 = \frac{30519125}{35 (1 - (1 - R_e)^3) + (1 - R_e)^3}$$

$$R_L = 1,57$$

Vibration Mode	Dynamic Stiffness $K = k \cdot k(\omega)$		
	Static Stiffness K General Shape (foundation-soil contact surface is of area A_b and has a circumscribed rectangle 2L by 2B; $L > B$) with $\gamma = \frac{A_b}{2L^2}$	Square $L = B$	Dynamic Stiffness Coefficient k (General shape; $0 \leq a_0 \leq 2$) $k_p = k \left(\frac{L}{B} ; a_0 \right)$ is plotted in Graph a
Vertical, z	$K_p = \frac{2G}{1-v} \left(0.73 + 1.54 \gamma^{0.78} \right)$ with $\gamma = \frac{A_b}{2L^2}$	$K_p = \frac{4.54GB}{1-v}$	$k_p = k \left(\frac{L}{B} ; a_0 \right)$ is plotted in Graph a
Horizontal, y (in the lateral direction)	$K_p = \frac{2G}{2-v} \left(2 + 2.50 \gamma^{0.88} \right)$	$K_p = \frac{9GB}{2-v}$	$C_p = (\rho V_s A_b) \cdot \xi_p$ $\xi_p = \xi_p(L/B; a_0)$ is plotted in Graph d
Horizontal, x (in the longitudinal direction)	$K_x = K_p - \frac{0.2}{0.75-v} G L \left(1 - \frac{B}{L} \right)$	$K_x = K_p$	$C_x = \rho V_s A_b$
Rocking, rx (around x longitudinal axis)	$K_{rx} = \frac{G}{1-v} f_{rx}^{0.75} \left(\frac{L}{B} \right)^{0.25} \left(2.4 + 0.5 \frac{B}{L} \right)$ with $f_{rx} = I_{rx}/I_{xy}$ area moment of inertia of the foundation-soil contact surface around the x(y) axis	$K_{rx} = \frac{3.6GB^3}{1-v}$	$C_{rx} = (\rho V_s A_b) \cdot \xi_{rx}$ $\xi_{rx} = \xi_{rx}(L/B; a_0)$ is plotted in Graph e and f
Rocking, ry (around lateral axis)	$K_{ry} = \frac{G}{1-v} f_{ry}^{0.75} \left[3 \left(\frac{L}{B} \right)^{0.15} \right]$ with $f_{ry} = I_{ry}/I_{xy}$ being the polar moment of the soil-foundation contact surface	$K_{ry} = K_{rx}$ $\begin{cases} v < 0.45: \\ K_{ry} = 1 - 0.30a_0 \\ v = 0.50: \\ K_{ry} = 1 - 0.25a_0 \\ v > 0.50: \\ K_{ry} = \left(\frac{L}{B} \right)^{0.30} \end{cases}$	$C_{ry} = (\rho V_s A_b) \cdot \xi_{ry}$ $\xi_{ry} = \xi_{ry}(L/B; a_0)$ is plotted in Graph g
Torsional	$K_t = G J_0^{0.75} \left[4 + 11 \left(1 - \frac{B}{L} \right)^{10} \right]$ with $J_0 = I_{xy} - I_{rx}$ being the polar moment of the soil-foundation contact surface	$K_t = 8.3GB^3$	$C_t = (\rho V_s A_b) \cdot \xi_t$ $\xi_t = \xi_t(L/B; a_0)$





For dashpots \rightarrow Bow Links (SAE 2000)

Bow links $k_x, k_y, k_z \propto c_x, c_y, c_z$

for the central zone

$$k_x = 7355 \text{ kPa/m}$$

$$c_2 = 551 \text{ kPas/m}$$

$$c_x^* = c_x$$

$$c_y^* = c_y$$

$$k_x^* = k_x$$

$$k_y^* = k_y$$

$* \rightarrow$ Perimeter
Zone

for the perimeter zone

$$k_z^* = R_L k_z$$

$$= 3.5 \cdot 7355$$

$$k_z^* = 25743 \text{ kPa/m}$$

$$c_z^* = R_L R_k c_2$$

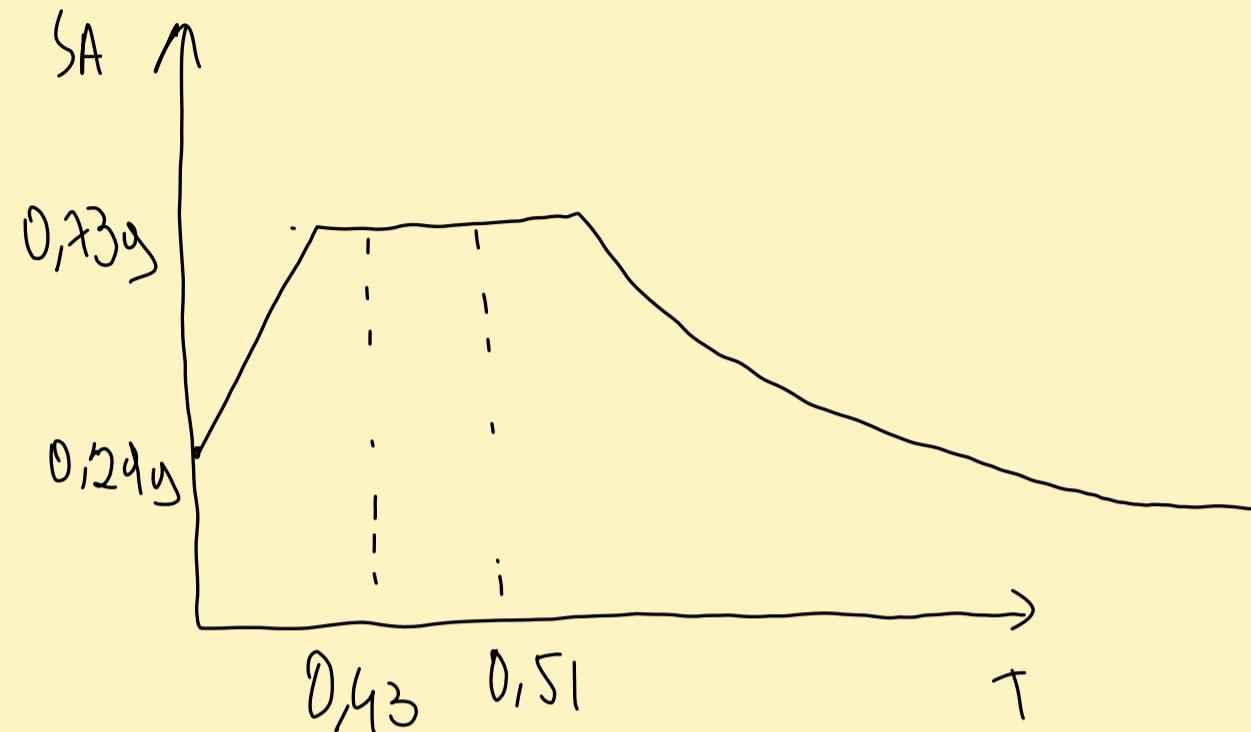
$$= 1.57 \cdot 3.57 \cdot 551$$

$$c_z^* = 3028 \text{ kN/m}^3$$

$$\downarrow$$

$$\text{kPas/m}$$

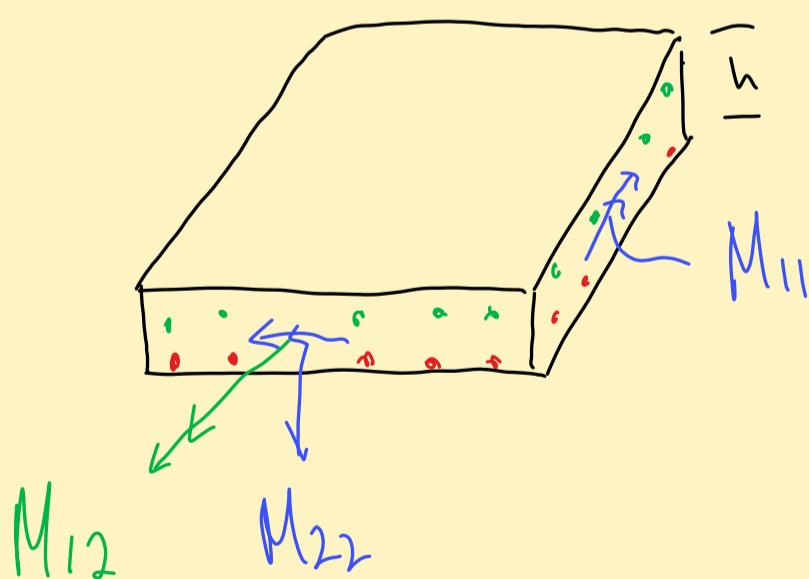
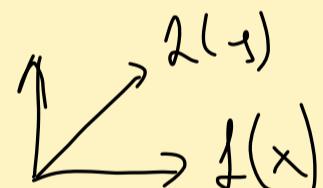
Mε ανθεκτισμένων τούφους τόντα εξω ληφθείστη Τ_s
 $SSI \Rightarrow T_s = 0,51 \text{ sec}$



Σεισμική Ενεργειακή:

$$\hookrightarrow G + 0,3 L + E$$

12/10/23 / SAP 2000 Example 3

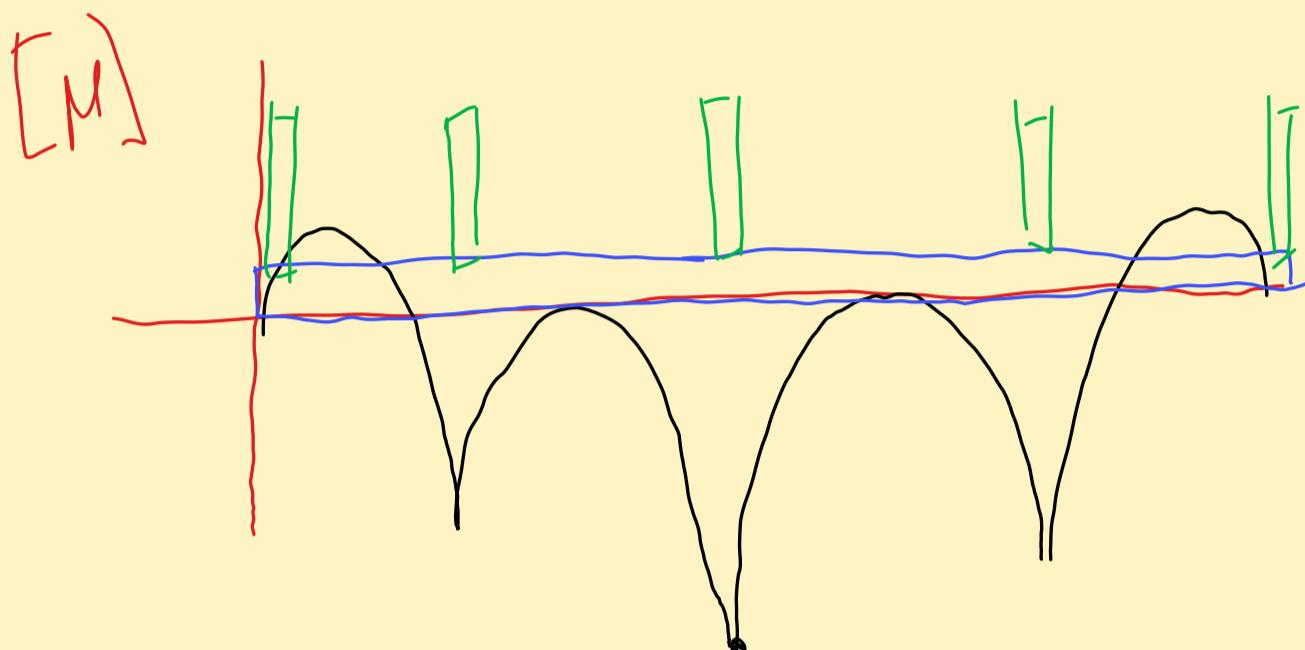


$$M_x = M_{11} + |M_{12}| \quad \left. \right\} \Rightarrow \text{Οπαδός κάτω (bottom reinforcement)}$$

$$M_y = M_{22} + |M_{12}|$$

$$\left. \begin{array}{l} m_x = M_{11} - |M_{12}| \\ m_y = M_{22} - |M_{12}| \end{array} \right\} \Rightarrow \text{Optimalisierung Flansch (top reinforcement)}$$

Comb1 $(s + 0.3L + E)$



$$\downarrow$$

$$M_{11} = 2200 \text{ kNm/m}$$

$$M_{22} = 130 \text{ kNm/m}$$

$$m_x = 2200 + 130$$

$$m_x = 2330 \text{ kNm/m}$$

$$k = \frac{M}{b \cdot d^2 \cdot f_{ck}} = \frac{2330 \text{ kNm/m}}{1 \text{ m} \cdot 0.95^2 \cdot 30 \text{ } 1000 \text{ kPa}}$$

$(b=1 \text{ m})$

Cover = 5 cm

$d = h - \text{cover}$

$$\hookrightarrow k = 0,086$$

$$2 = \frac{d}{2} \left[1 + \sqrt{1 - 3.53k} \right] \leq 0.95 \rightarrow$$

$$2 = \frac{0.95}{2} \left[1 + \sqrt{1 - 3.53 \cdot 0.086} \right] \Rightarrow 2 = 0.871$$

$$A_s = \frac{M}{f_y d^2} = \frac{2330 \text{ kNm/m}}{\frac{500}{1.15} \cdot 0.95} \Rightarrow A_s = 0.0062 \text{ m}^2$$

$$A_{s\min} = 0.00015 \text{ } A_L^{1 \times 1}$$

$$\hookrightarrow A_{s\min} = 0.00015 < 0.0062 \text{ m}^2$$

$$\rho = \frac{A_{s\min}}{b \cdot d} \quad (b=1, d=h-\text{cover}, d=0.95)$$

$$A_{s\max} = 0.04 A_s$$

$$= 0.04 > 0.0062 \text{ m}^2$$

$\phi 16$

$$D = 16 \text{ mm} \quad A_b = \pi \frac{0.0016^2}{4} \Rightarrow A_b = 0.0002 \text{ m}^2$$

$$N = \frac{A_s}{A_b} = \frac{0.0062}{0.0002} \Rightarrow N = 31$$

$$\text{Spacing} = \frac{1 \text{ m}}{31} = 0.0032 \rightarrow 32 \text{ cm}$$

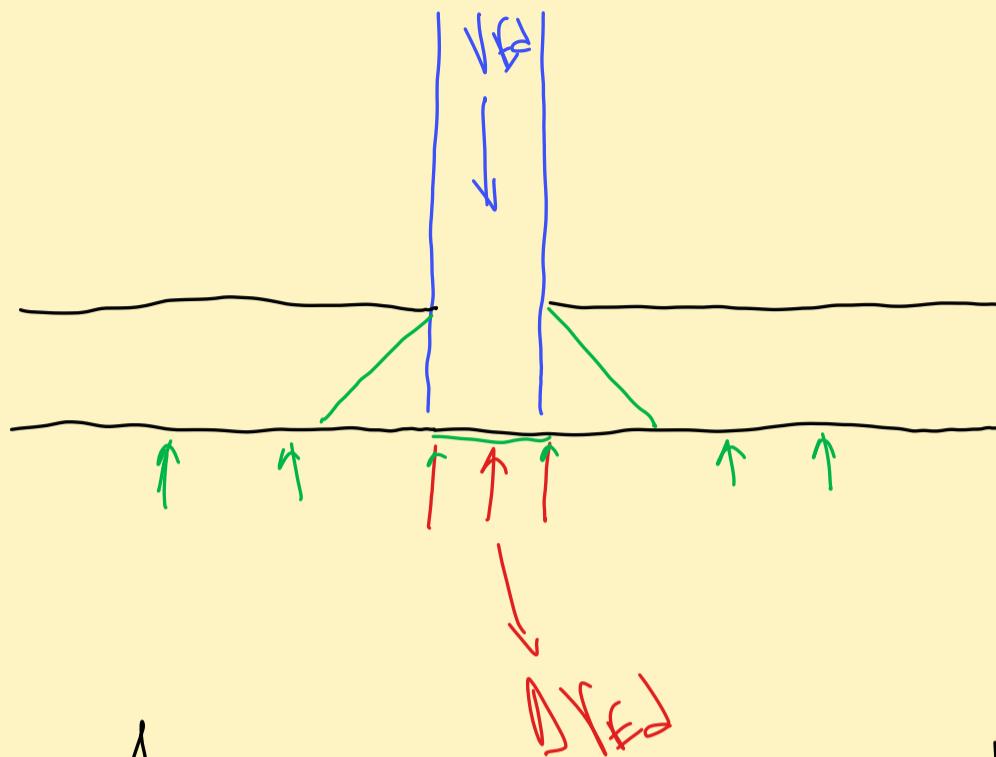
$\phi 30$

$$D = 30 \text{ mm} \quad A_b = \frac{0.03^2}{4} \pi \Rightarrow A_b = 0.0007 \text{ m}^2$$

$$N = \frac{0.0062}{0.0007} \Rightarrow N = 9 \quad \text{Spacing} = \frac{1 \text{ m}}{9} = 11 \text{ cm}$$

$\hookrightarrow \phi 30/10$

Diaphragm Punching Calculations



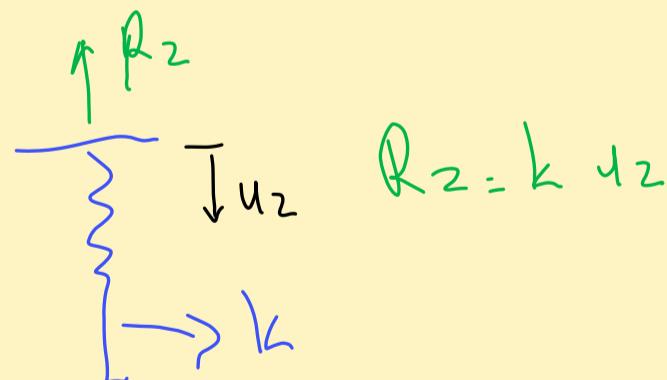
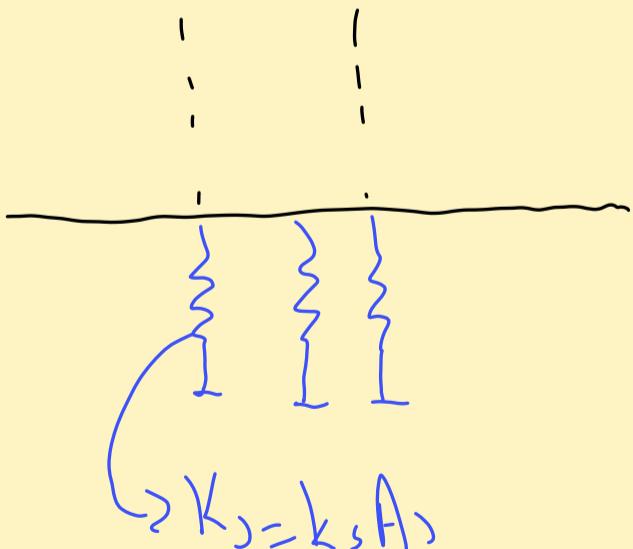
$$V_{Ed} = 3743 \text{ kN}$$

$$V_{Ed\max} = \frac{\delta (V_{Ed} - \Delta V_{Ed})}{u_0 \cdot d_{eff}}$$

Reinforcement
U'BUT

$$d_{eff} = h - (\text{cover} + \delta)$$

$$d_{eff} = 0.97 \text{ m}$$



$$\Delta V_{Ed} = \sum Q_2 = \sum k_s A u_2$$

$$\Delta V_{Ed} = u_2 k_s \sum A \rightarrow 0.5^2$$

$$\begin{array}{c} 10.5 \\ \hline 0.5 \end{array} \rightarrow u_0 = 4.05$$

$$u_0 = 2 \text{ m}$$

\rightarrow capacity and the
deformation characteristics

Figure 7
 $B=1$ (then $M=0$)

$$k_s = 7355 \frac{\text{kPa}}{\text{m}}$$

$$u_2 = 0,025 \text{ m}$$

$$\Delta V_{Ed} = 0,025 \text{ m} \cdot 7355 \cdot 0,5^2$$

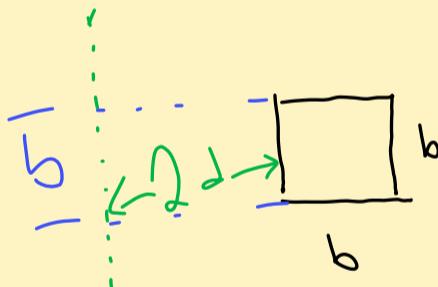
$$\Delta V_{Ed} = 46 \text{ kN}$$

$$V_{Ed,\max} = \frac{(3743 - 46)}{0,025 \cdot 0,92} \Rightarrow V_{Ed,\max} = 2009 \text{ kPa} \\ = 2 \text{ MPa}$$

$$V_{Rd,\max} = 5,28 \text{ MPa} > V_{Ed,\max}$$

table 7

$$V_{Ed} < V_{Rd} \quad (\text{Περικέπτεται ριν 2d})$$



$$d = \text{depth}$$

$$2d = 2 \cdot 0,92$$

$$2d = 1,84 \text{ m}$$

$$r = 2d$$

$$u_1 = u_1 \cdot 0,5 + \frac{2+r}{4} \cdot 4$$

$$u_1 = 13,60 \text{ m}$$

$$V_{Ed} = \frac{V_{Ed} - \Delta V_{Ed}}{u_1 \text{ def}}$$



$$\Delta V_E = U_2 K_s A$$

$$= 0,024 \cdot 7335 \cdot 14,60$$

$$A = 0,5^2 + 4(0,5 \cdot 1,84) + 4\pi r^L$$

$$A = 0,5^2 + 4(0,5 \cdot 1,84) + \pi 1,84^L$$

$$A = 14,60 \text{ m}^2$$

$$V_E = \frac{3743 - 2570}{13,60 + 0,92} \Rightarrow V_E = 93,75 \text{ kPa}$$

$$V_E = 0,094 \text{ MPa}$$

Table 6 ϕ_{30}

$$\rho_L = 9 \frac{\pi 0,03^2}{4} \Rightarrow \rho_L = 0,63\%$$

According to table 6 $\rightarrow V_{R,L} = 0,45 \text{ MPa} > V_E = 0,094 \text{ MPa}$

For safety reasons the required V_R is $\geq (V_E = ?)$

$$\rightarrow V_R = 2V_E \quad (V_R = \frac{2}{3} V_E)$$

19/10/23) Homework hardcopy on 2/11
Midterm 9/11

Homework 1

Answers

$$k_{\text{soil}} = \frac{100 \text{ MN}}{5 \text{ cm}}$$

Answers 2

Qualification Aviation

Gazetteer Tables

NIST Approach

$\gamma_{\text{soil}} = 19 \text{ kN/m}^3$

$\Delta_{\text{soil}} = 3 \text{ m}$

Erläuterung

→ Holzstruktur

NIST

Kontrollen Kriterien → Qualifikation Aviation

→ low Passagiers

ΤΙΑΣΣΑΝΟΙ

Settlements of Pile Foundations

Πλευρική σύρεψη

$$Q_{S,L} = q_{S,L} A_{S,L}$$

$A_{S,L} \rightarrow$ έπιβασης πλευρικής επιφάνειας
 $q_{S,L} \rightarrow$ αντίσταση (kPa)

$Q_{b,ult} \rightarrow$ οριακή αντίσταση εγκίνης ($\sigma_0 = 0.1 B$)

$Q_{S,L} \rightarrow$ οριακή αντίσταση πλευρικής ΤΠΙΒης

$G \rightarrow$ μετόπο σιτημάνιας

$r_m \rightarrow$ ακτινή επιπρόπορης παρούσας (radius of influence)

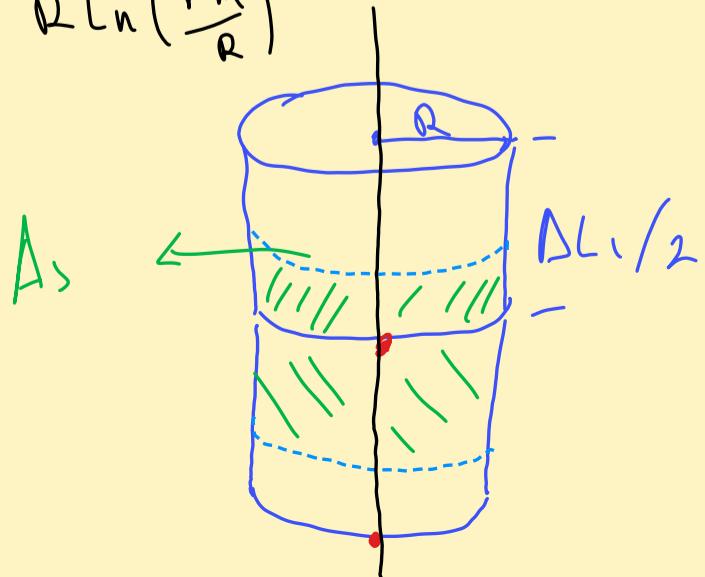
$$r_m = \left[0.25 + (2.5(1-v) \frac{G_{base}}{G_L} - 0.25) \frac{G_L}{G_{Base}} \right] L$$

$A_v \rightarrow$ πλευρικής ομοιομορφώς εδαφούς $G_{base} = G_L = G_{Base}$
 \hookrightarrow ομοιομορφής αρρεδούς ($v=0.5$)

$$r_m = \left[0.25 + (2.5(1-0.5) 1 - 0.25) 1 \right] L$$

$$r_m = 1.25 L$$

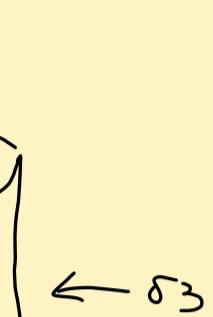
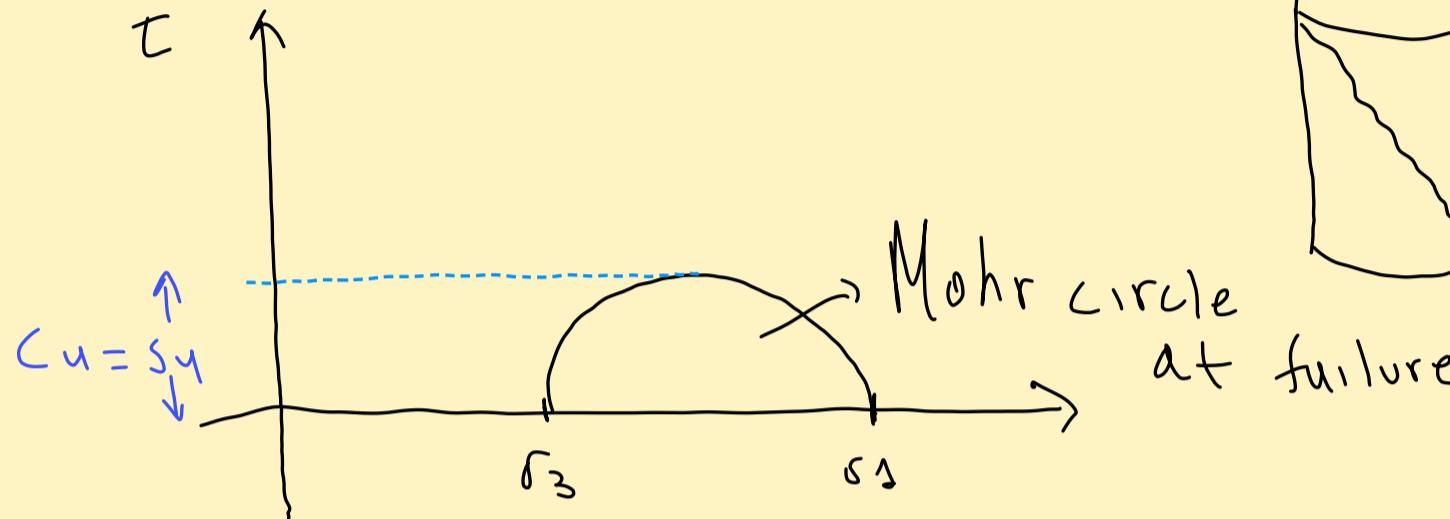
$$k_s = \frac{G}{R \ln\left(\frac{r_m}{R}\right)} \quad K_s = k_s A_s$$



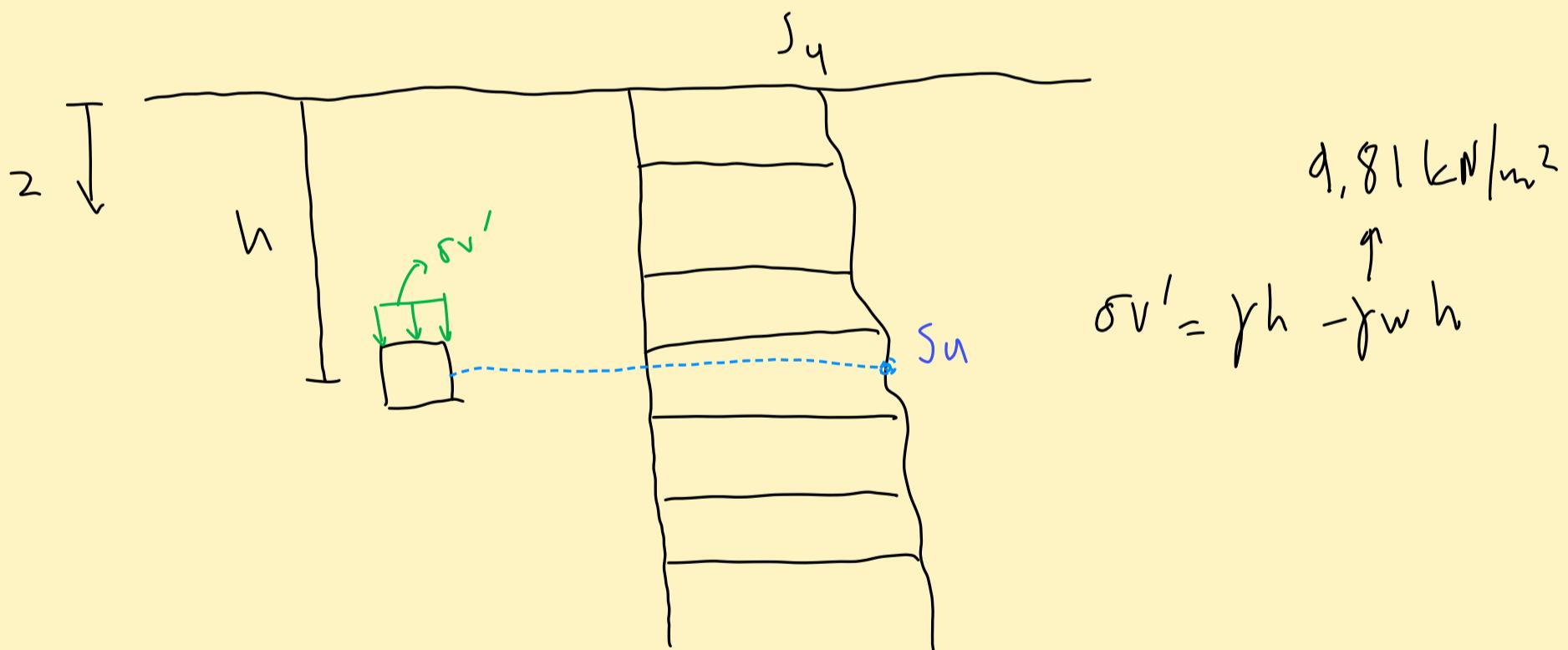
$$A_s = 2 \pi R \frac{\Delta L}{2}$$

$$K_s = \frac{G}{R \ln\left(\frac{r_m}{R}\right)} \quad 2\pi R \frac{\Delta L_1}{2} \Rightarrow K_s = \frac{2\pi}{\ln\left(\frac{r_m}{R}\right)} G \quad 0 < \Delta L_1$$

Undrained shear strength (s_u n c_u)



Driven piles $q_{SL} = a s_u$ $q_{BL} = q s_u$



$$a = \left(\frac{s_u}{\sigma_v'} \right)^{0.5} N_C \left(\frac{s_u}{\sigma_v'} \right)^{-0.5} r_{1u} \frac{s_u}{\sigma_v'} \leq 1$$

$$a = \left(\frac{s_u}{\sigma_v'} \right)^{0.5} N_C \left(\frac{s_u}{\sigma_v'} \right)^{-0.25} r_{1u} \frac{s_u}{\sigma_v'} > 1$$

$$\left(\frac{S_u}{\sigma_{v'}}\right)_{NL} = 0.11 + 0.0037 PI \quad PI = LL - PL$$

If the clay is Currently NC

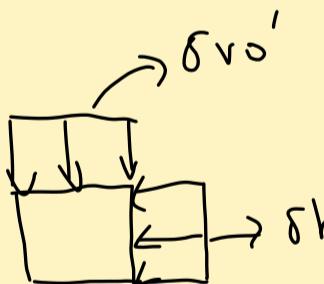
$$a = \left(\frac{S_u}{\sigma_{v'}}\right)_{NC}^{0.5} \left(\frac{S_u}{\sigma_{v'}}\right)_{NL}^{-0.5} \Rightarrow a=1$$

DR \rightarrow σκετική πυκνότητα (Relative density)

$$DR = \frac{\epsilon_{max} - \epsilon}{\epsilon_{max} - \epsilon_{min}} \quad \epsilon \rightarrow \text{στικτική πίεση}$$

From SPT $N_{SPT} \rightarrow N_{60}$

$$DR (\%) = \left\{ \frac{N_{60}}{365 + 27 \frac{\sigma_{v0'}}{PA}} \right\} \quad PA = 100 \text{ kPa}$$



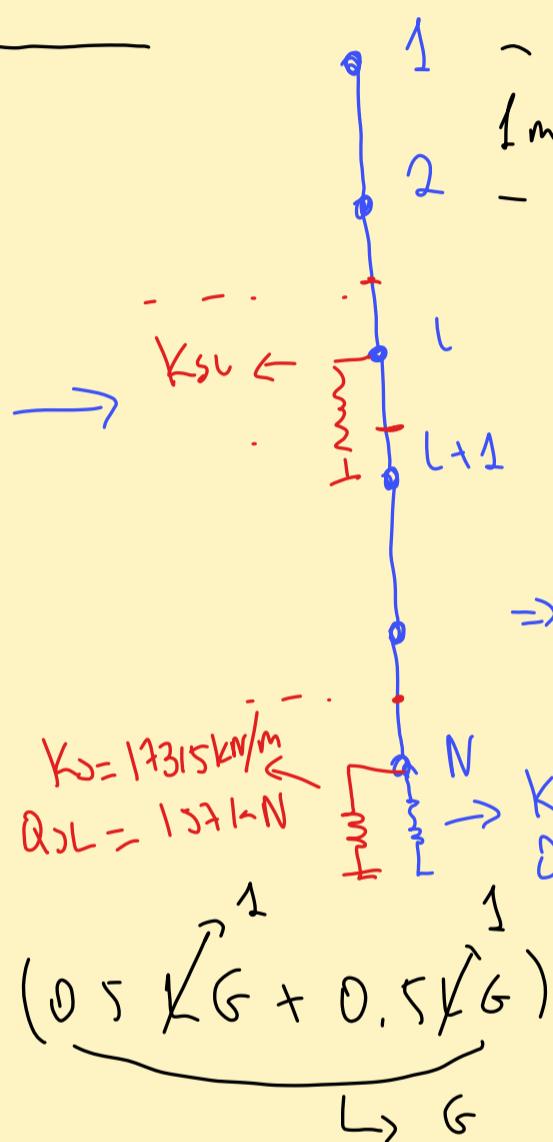
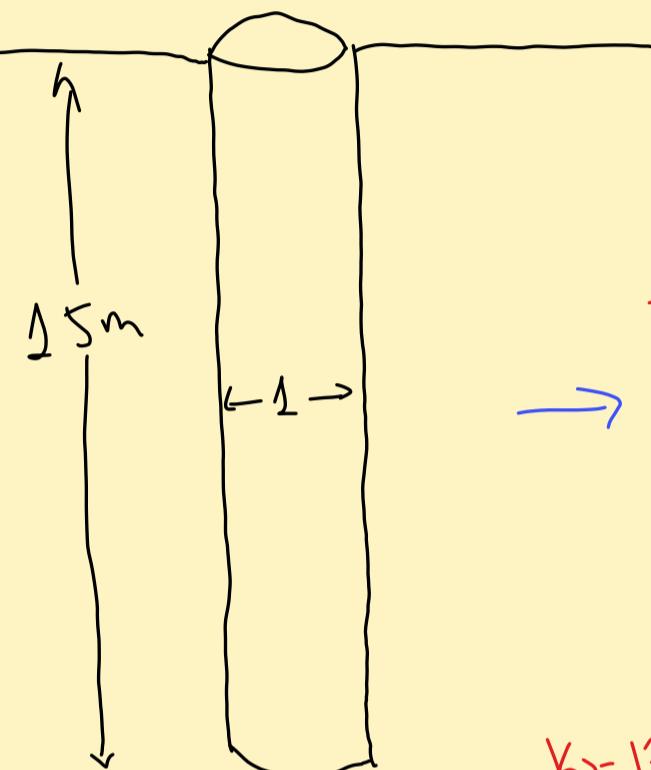
$$K_0 = \frac{\sigma_{h0'}}{\sigma_{v0'}} = 1 - \sin \phi$$

26/10/23

- ΣΤΟΥ > πλαστικός γεωπλοκώνιμος thick formulation
- Non Linear analysis > σΤΟ SAP 2000 (rla σχέδιο)

SAP 2000 Example 4

Drilllet shaft (30/37)



$$K_{sL} = \frac{2\pi}{\ln\left(\frac{r_m}{R}\right)} (0.5 K_G + 0.5 f_G)$$

$$f = 100 s_u$$

$$= 100 \cdot 200 \text{ kPa}$$

$$f = 20000 \text{ kPa}$$

$$1 \quad 15 \quad \hookrightarrow f = f_L = G \cdot B \cdot A \cdot f_E$$

$$r_m = \left[0.25 + (2.5(1-v) \frac{G \cdot f_E}{f_L} - 0.25) \frac{G \cdot f_E}{G \cdot B \cdot A \cdot f_E} \right] f$$

$$r_m = 1.25 \cdot 15 \Rightarrow r_m = 18.8 \text{ m}$$

$$K_{sL} = \frac{2\pi}{\ln\left(\frac{18.8}{0.5}\right)} 20000 \Rightarrow K_{sL} = 341722 \text{ kN/m} \rightarrow \text{inner nodes}$$

$$K_{Sf} = K_{SN} = \frac{2\pi}{\ln\left(\frac{r_m}{R}\right)} (0.5 L G)$$

$$K_{Sf} = K_{SN} = \frac{34729}{2} \Rightarrow \begin{cases} K_{Sf} = 17315 \text{ kN/m} \\ K_{SN} = 17315 \text{ kN/m} \end{cases} \text{ outer nodes}$$

Yard of soil $\rightarrow Q_{SL,i} \rightarrow$ Arrangement of supports

$$q_{SL} = a S_u$$

$$\frac{S_u}{P_A} = \frac{200}{100} = 2$$

$$q_{SL} = 0 \dots 200 \text{ kPa}$$

$$\hookrightarrow a = 0.55 - 0.1 \left(\frac{S_u}{P_A} - 1.5 \right) \xrightarrow{2}$$

$$a = 0.5$$

\downarrow Support

$$Q_{SLi} = 2\pi R (0.5 L q_{SL} + 0.5 L q_{SL})$$

$$Q_{SLi} = 2\pi 0.5 (0.5 \cdot 100 + 0.5 \cdot 100)$$

$$Q_{SLi} = 314 \text{ kN} \rightarrow \text{inner nodes}$$

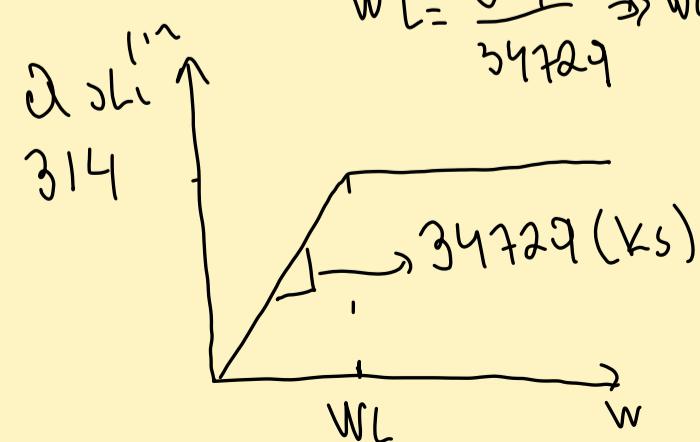
$$Q_{SLi}^{(out)} = \frac{314}{2}$$

$$Q_{SLi}^{(out)} = 157 \text{ kN} \rightarrow \text{outer nodes}$$

Inner

$$W_L = \frac{314}{34729} \Rightarrow W_L = 0.009 \text{ m}$$

$$\frac{W_L}{D} = 0.9\%$$



Υπολογισμός K_b και Q_{BL} (σημ βήμα που παραχθεί στον N node)

$$K_b = \frac{4RG}{1-v} (1,27 - 0,12 \ln v)$$

$$K_b = \frac{4 \cdot 0,5 \cdot 25000}{1-0,5} (1,27 - 0,12 \ln 0,5) \Rightarrow K_b = 108254 \text{ kN/m}$$

$$q_{BL} = q_{SU} \\ = q \cdot 200 \text{ kPa} \Rightarrow q_{BL} = 1800 \text{ kPa}$$

$$Q_{BL} = q_{BL} A_b \\ = 1800 \pi 0,5^2 \Rightarrow Q_{BL} = 1413 \text{ kN}$$

Υπολογισμός R (horizontal Non-linear model)

↳ Διάτρηση Lateral response of pile foundations

Υπολογισμός R στο excel

$$E_p = 210000000 \text{ kPa}$$

$$I_p = \frac{\pi r^4}{4} = \frac{\pi 0,5^4}{4} \Rightarrow I_p = 0,0491 \text{ m}^4$$

second moment area (κωνικής σιρόφυτης)

$$E_{Safous} = G_2(f+r)$$

$$= 20000 \text{ kPa } 2(f+0,5)$$

$$E_{Safous} = 60000 \text{ kPa}$$

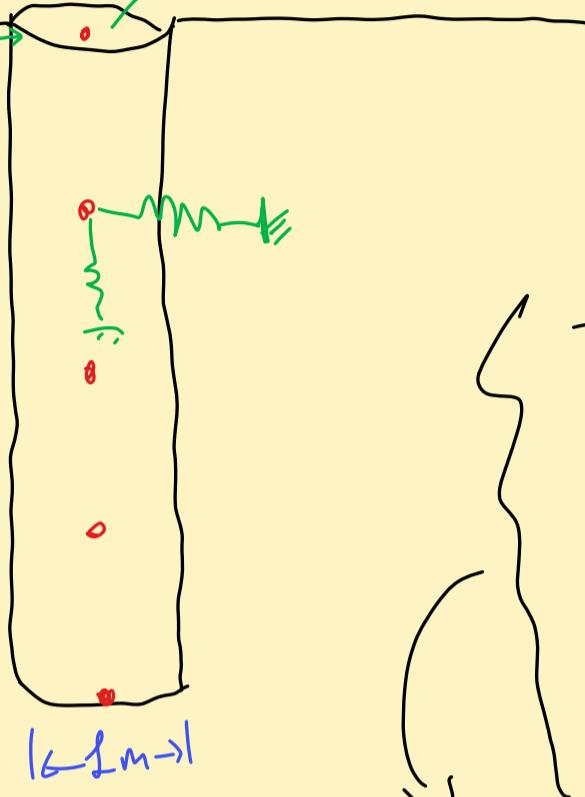
$$\left. \begin{aligned} & \left. \begin{aligned} & E_p = 210000000 \text{ kPa} \\ & I_p = 0,0491 \text{ m}^4 \\ & \text{second moment area (κωνικής σιρόφυτης)} \end{aligned} \right\} \\ & K_{rel} = \frac{E_p I_p}{E_{Safous} L^4} \quad L=15 \\ & = \frac{210000000 \cdot 0,0491}{60000 \cdot 15^4} \\ & K_{rel} = 0,0034 \end{aligned} \right.$$

2/11/23

Συρτεξια Τοπαστικη μετωπος

2000 kN
1000 kN

3000 kN

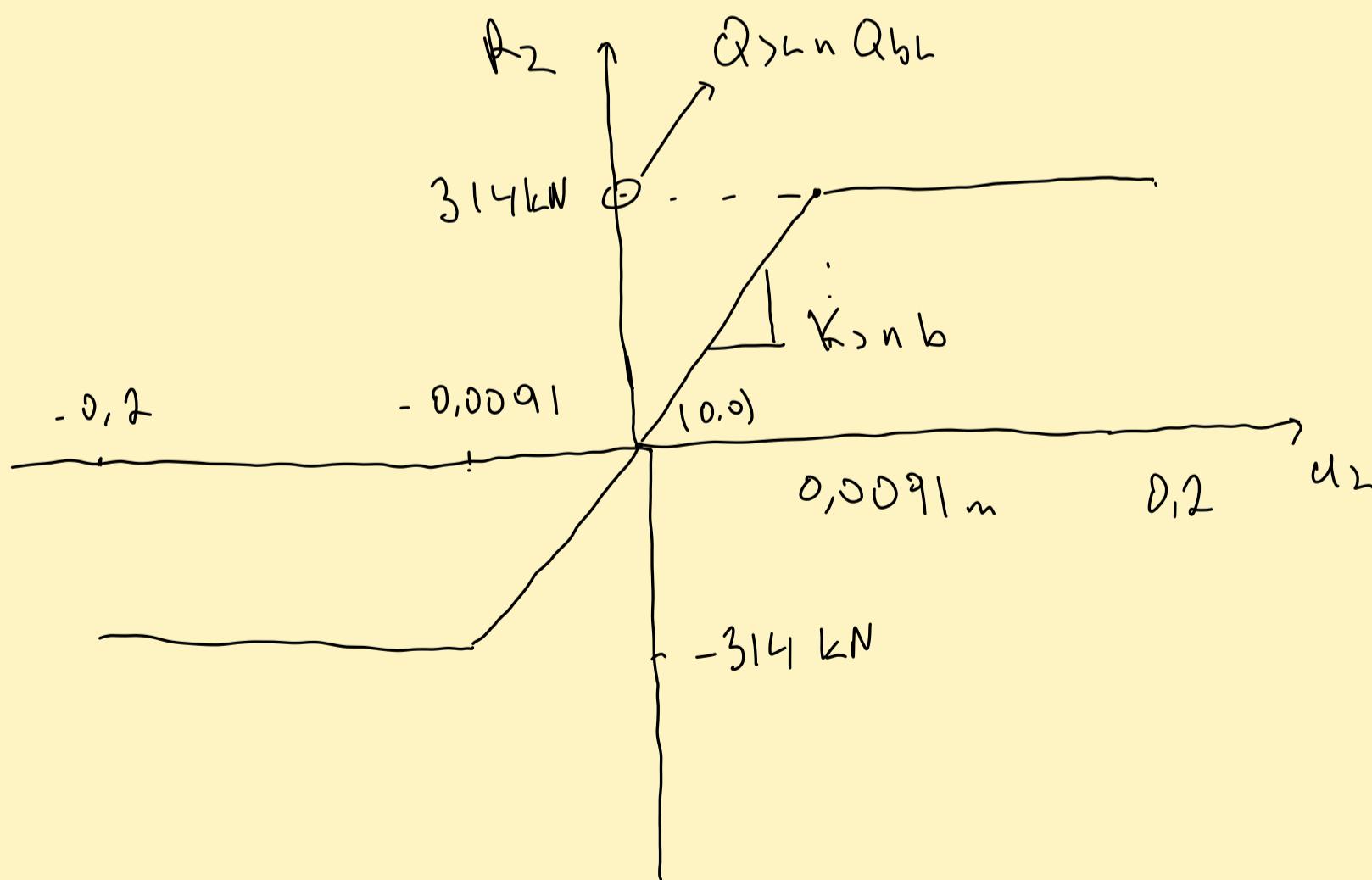


- Midterm
 - ↳ Ελω οι προσωδοι
 - ↳ σημαντικος κριτης
 - ↳ multiple choice
 - ↳ review EC8

Clay (OC)

Katakorufa \leftrightarrow utipie

σιρθητικος



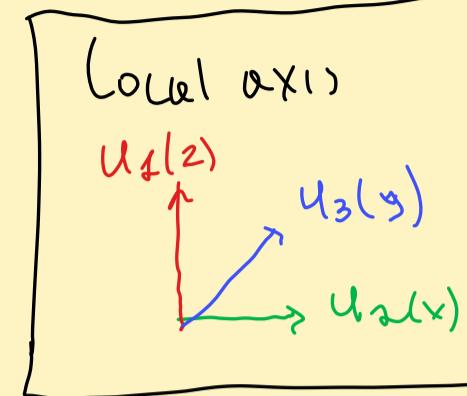
SAP 2000

↳ Der Biuw ausspars meiget, Biuw link support properties

Link support properties

↳ multilinear Plastic

- U₁
 - U₂
 - U₃
- } Non linear



modify ria us (karakopfo Local axes)

Kinematic

Disp	Force
-0.2	-157
-0.0091	-157
0	0
0.0091	157
0.2	157

Karakopfo
εστιπο

157 ria to καρκοφο ση
καρκοφο του πασσιδου
και των καρκοφο ση
βαμ του πασσιδου

314 ria του ερδιάκεδου

ria της Biuw το Link

draw joint Link και διαδημ το joint

→ U₂ και U₃ Biuw τοις αριθμούς του Excel

η μήν Disp → u (συν excel)

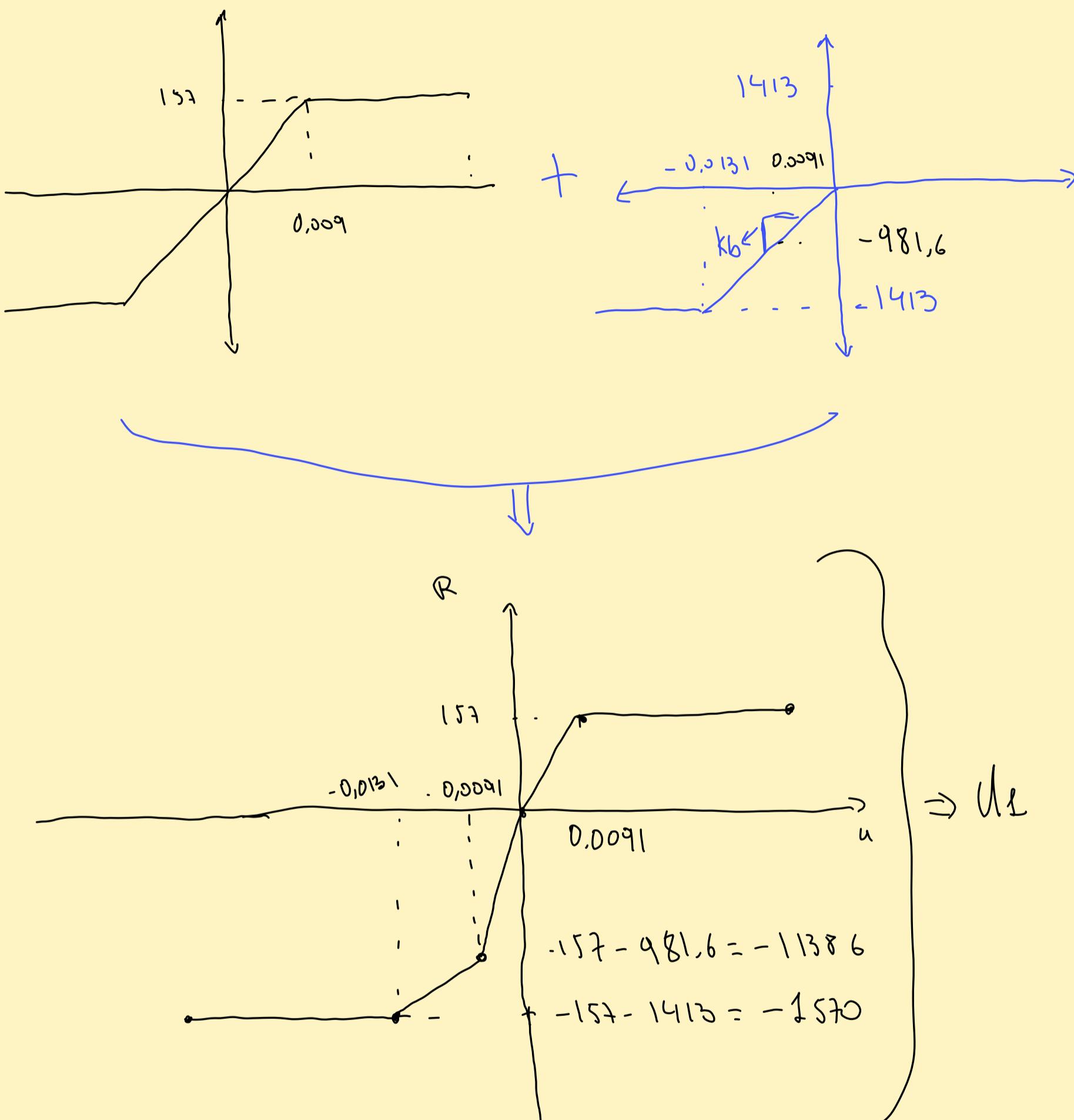
στις force → 2(1 n₂ n₃)) Auto excel

Επαναλήψη της διαδικασίας ria στους καρκοφους

Auto Biuw > G - 14 της Link

Fix node 15

↳ Update the load case to eliminate bus 15



Mn reaktivn aradwsh

↳ new case pattern → Static Nonlinear

↳ Add φspur

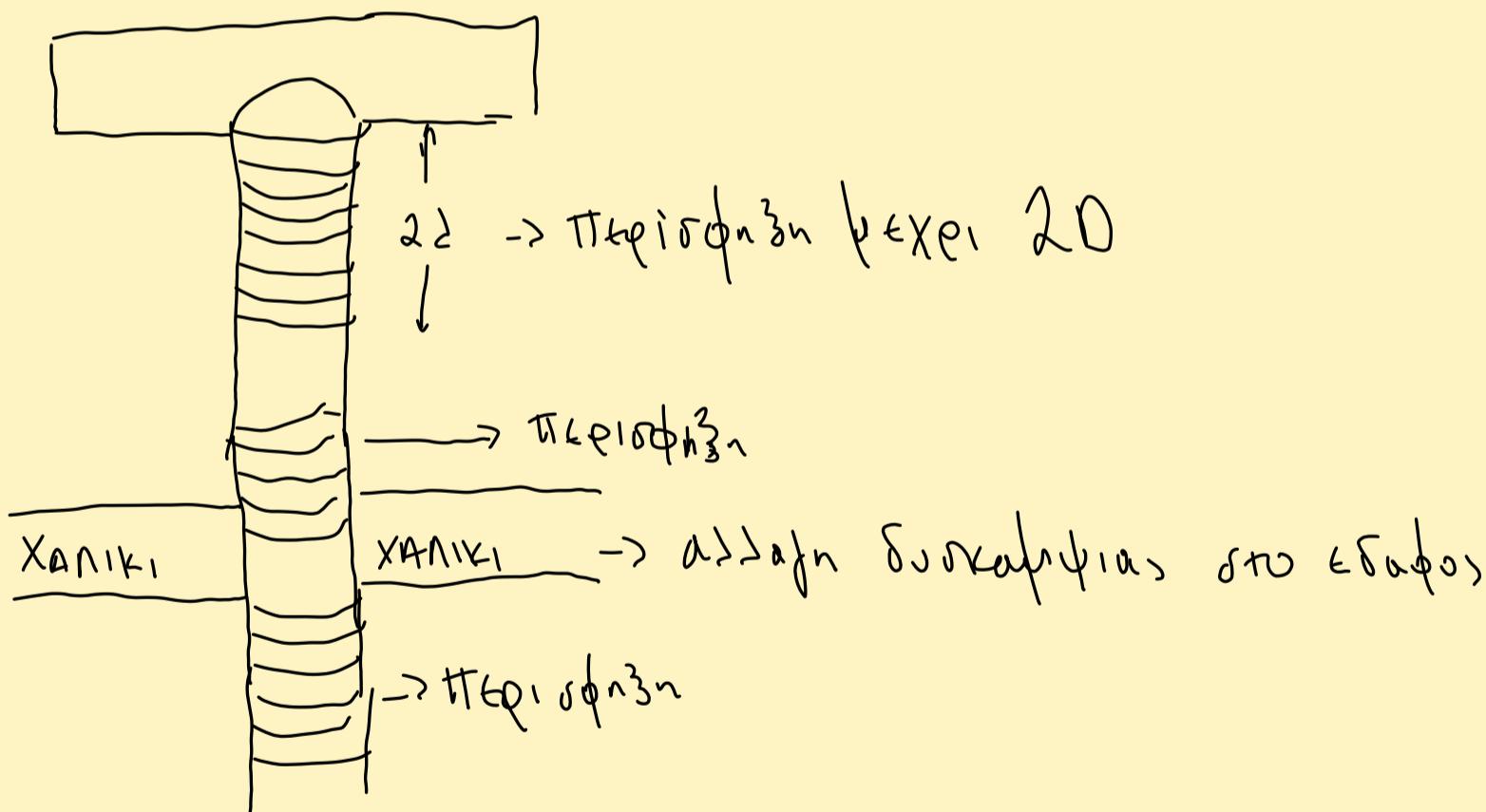
Set analyse options

R₂ → πρετει ρα ειραι \rightarrow tuθtρού

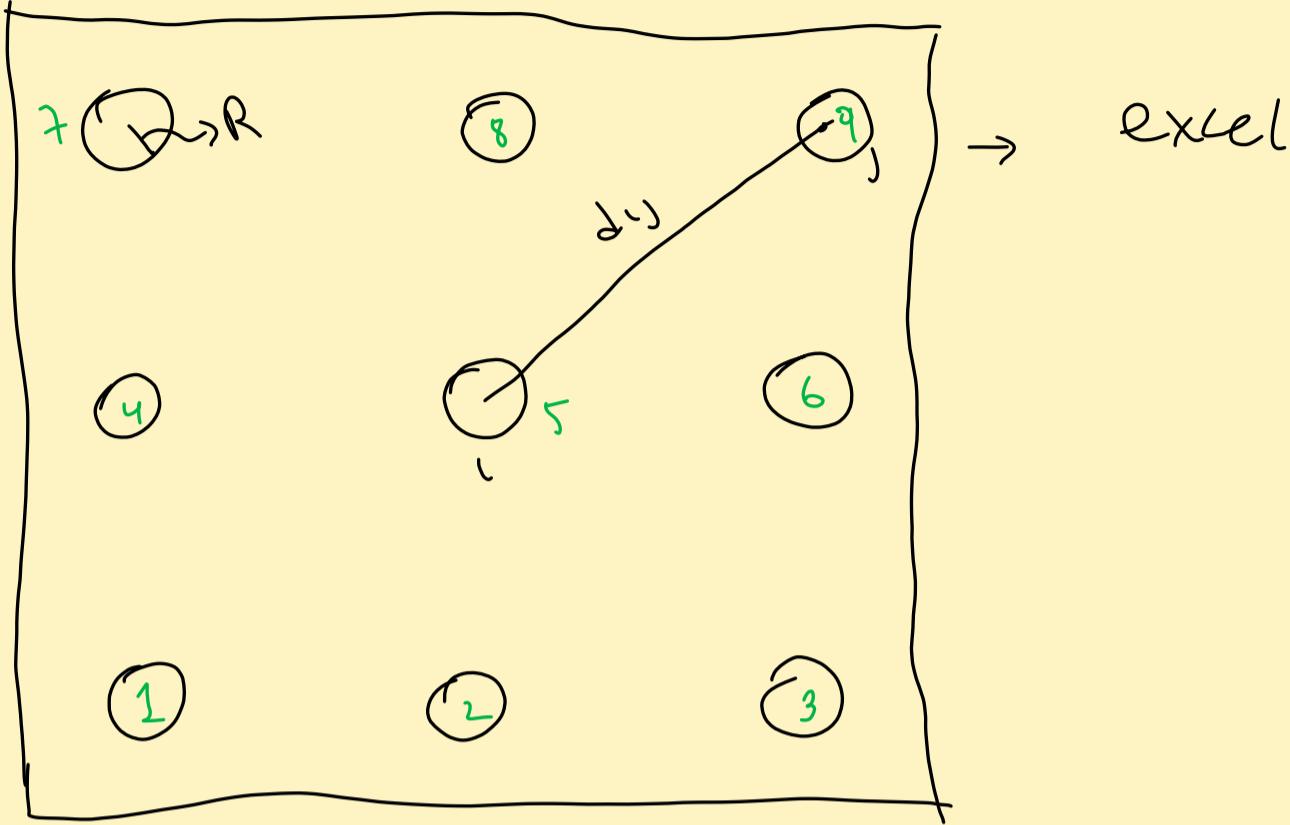
Run koro των A CASE 1 (in fun-graphikn)

Design of Pile

Cyprus → DCM n DCH

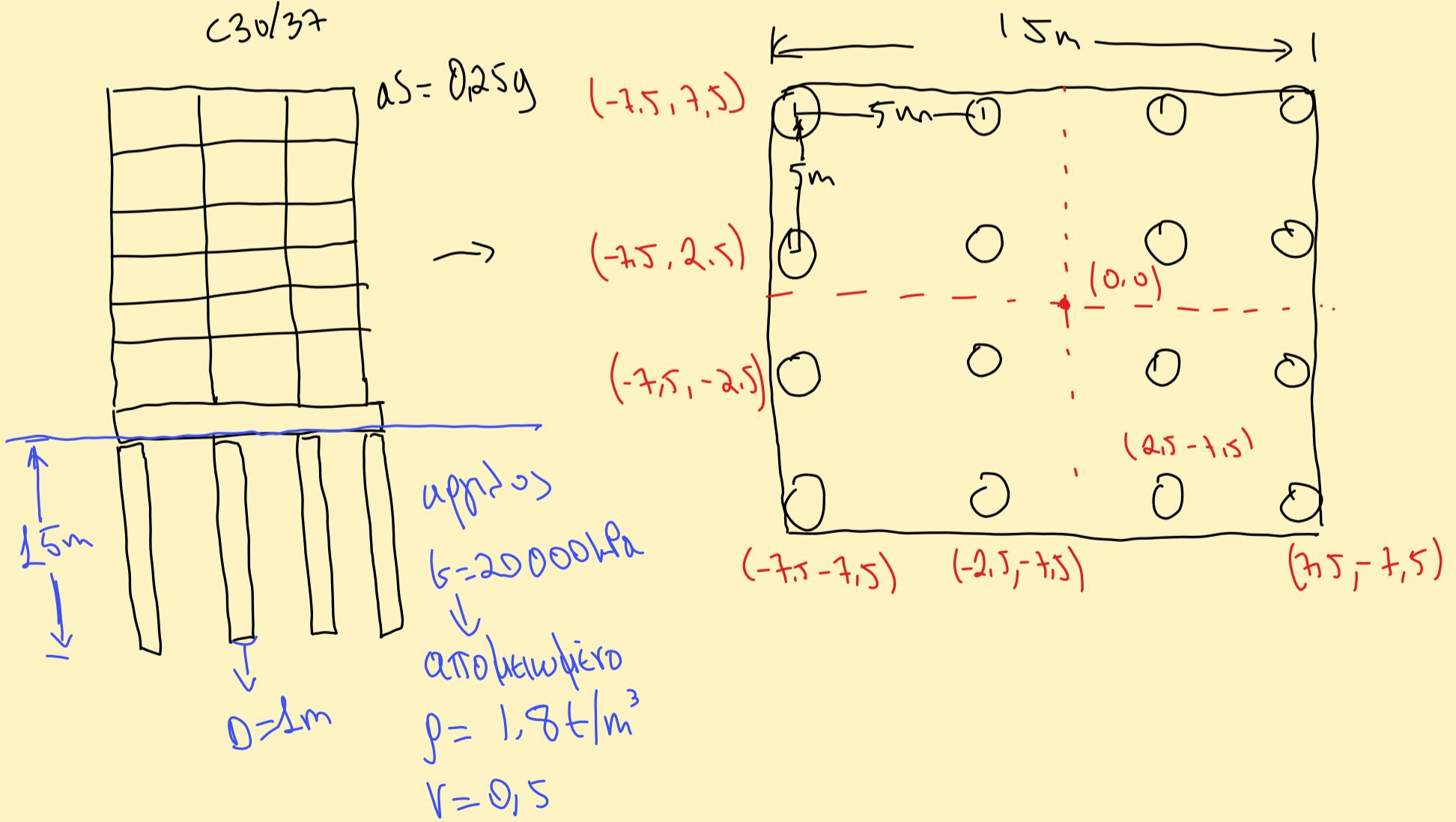


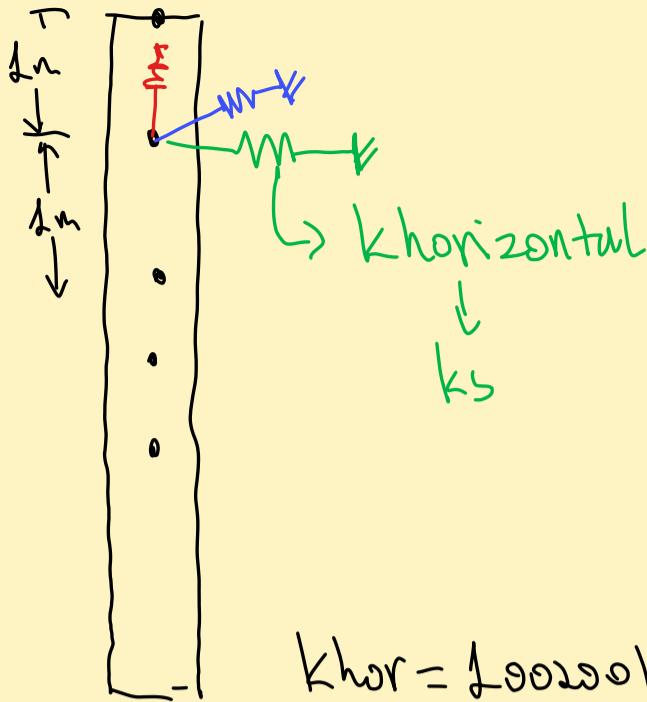
Settlement of Pile (groups)



9/11/23 Example - file - graph - class (SAP FILE)

c30/37





$$k_s = \frac{1.67 E}{D}$$

$$E = 2 G(1+\nu)$$

$$E = 20000 \cdot 2(1+0.15)$$

$$E = 60000 \text{ kPa}$$

$$k_s = \frac{1.67 \cdot 60000}{1m} \Rightarrow k_s = 100200 \text{ kPa/m}$$

$$k_{hor} = 100200 \text{ kN/m} \Rightarrow (0.5 \cdot 100200 + 0.5 \cdot 100200) \\ \hookrightarrow_{inner}$$

$$k_{hor}(\text{out}) = 50100 \text{ kN/m}$$

$$c_s = 2\rho V_s$$

$$V_s = \sqrt{\frac{G}{\rho}} = \sqrt{\frac{20000}{18}} \Rightarrow V_s = 105 \text{ m/s}$$

$$c_s = 2 \cdot 1.8 \cdot 105 \Rightarrow c_s = 378 \text{ kPa s/m}$$

$$C_{hor} = \pi c_s$$

$$C_{hor,rad} = 3.14 \cdot 378 \Rightarrow C_{hor} = 1187 \text{ kN s/m}$$

$$C_{hor,tot} = C_{hor,rad} + \frac{2K_{hor}}{\omega} \cdot 3$$

$$3 = 8\%$$

$$\omega = \frac{2\pi}{T} \Rightarrow \omega = \frac{2\pi}{0.7} \Rightarrow \omega = 9 \text{ rad/sec}$$

$$C_{hor,tot} = 1187 + 2 \cdot \frac{100200}{9} \cdot 0.08 \Rightarrow C_{hor,tot} = 2968 \text{ kN s/m} \\ \hookrightarrow_{inner}$$

$$C_{hor,tot} = 2968 / 2 = 1484 \text{ kN s/m} \\ \hookrightarrow_{outer}$$

Karukopufo Etatipio (settlements of pile foundations)

$$R = D/2 = 0.5 \text{ m}$$

$$r_m = \left[0.25 + (2.5(1-0.5) \frac{6}{6} - 0.25) \frac{6}{6} \right] L$$

Vertical
↑
 $r_m = 1.25 L = 1.25 \cdot 15$

$$r_m = 18.8 \text{ m}$$

$$K_{sv} = \frac{2\pi}{\ln\left(\frac{18.8}{0.5}\right)} (0.5 \cdot 1 \cdot 20000 + 0.5 \cdot 1 \cdot 20000)$$

$$K_s = 34600 \text{ kN/m} \quad K_s = 17300 \text{ kN/m}$$

↳ inner ↳ outer

$$K_b = \frac{4 R b}{1-r} (1.27 - 0.12 \ln 0.5)$$

$$= \frac{4 \cdot 0.5 \cdot 20000}{1-0.5} (1.27 - 0.12 \ln 0.5) \Rightarrow K_b = 108240 \text{ kN/m}$$

↳ base

$$c_s = \rho v_s = 1.8 \cdot 105 \Rightarrow c_s = 189 \text{ kPa} \frac{s}{m}$$

$$c_{s,inner} = \pi \cdot 189 \Rightarrow c_{s,inner} = 593 \text{ kN} \frac{s}{m}$$

$$c_{s,outter} = 593/2 \Rightarrow c_{s,outter} = 297 \text{ kN} \frac{s}{m}$$

$$c_{s,tot,inner} = 593 + \frac{2 \cdot 34600}{9} \cdot 0.08 \Rightarrow c_{s,tot,inner} = 1208 \text{ kN} \frac{s}{m}$$

$c_{s,tot,outter} = 604 \text{ kN} \frac{s}{m}$

$$c_b = \frac{3.4 R^2}{1-r} \sqrt{g b} = \frac{3.4 \cdot 0.5^2}{1-0.5} \sqrt{1.8 \cdot 20000}$$

$$c_b = 323 \text{ kN} \frac{s}{m}$$

Vertical \rightarrow eq = 0.43

3rd	2nd	1st	L	L	1st	2nd	3rd
0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0

$$F_L = 0,64 + 0,06 \frac{5}{1} \leq 1 \Rightarrow F_L = 0,94$$

$$F_{T1} = 0,34 + 0,11 \frac{5}{1} \leq 1 \Rightarrow F_{T1} = 0,89$$

$$F_{T2} = 0,16 + 0,14 \frac{5}{1} \leq 1 \Rightarrow F_{T2} = 0,86$$

$$F_{T3} = 0,04 + 0,16 \frac{5}{1} \leq 1 \Rightarrow F_{T3} = 0,84$$

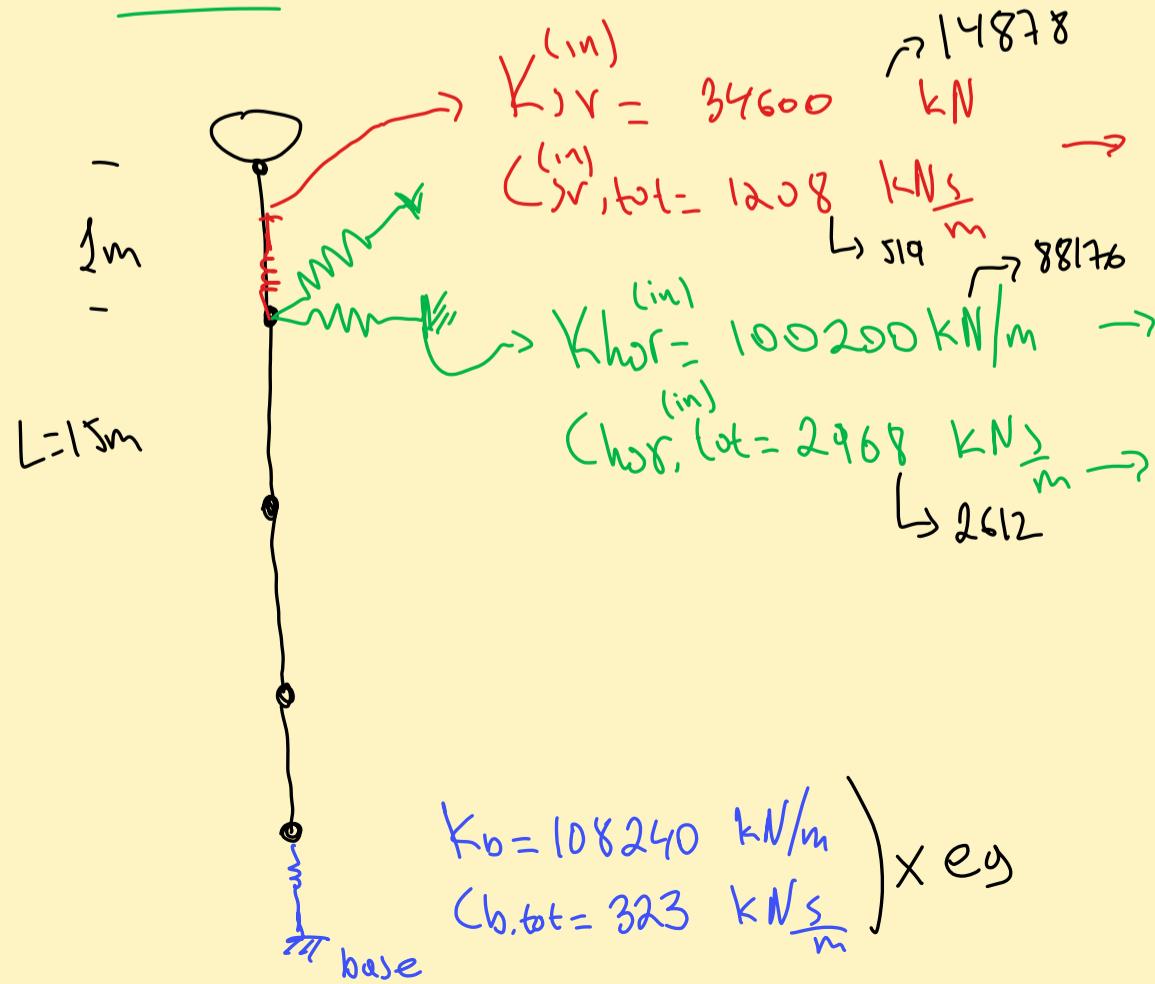
$$\left. \begin{aligned} f_{green} &= \frac{0,89 + 0,86}{2} \Rightarrow f_{green} = 0,875 \\ f_{red} &= \frac{0,94 + 0,84}{2} \Rightarrow f_{red} = 0,88 \end{aligned} \right\} \Rightarrow f = 0,88$$

16/11/23

$$eg = 0,43$$

$$f = 0,88$$

(eg, f → additivitätspunkt nach unten)



SAP file → example_pile_group-class

Here: $k_b = 108240 \cdot 0,43 + 7343 = 53982 \text{ kN/m}$

$C_b,\text{tot} = 323 \cdot 0,73 + 302 = 441 \text{ kN/m}$

↳ appears that it's about piles and U1

Draw 1 joint link

Nlosiu

$$ayR = 0.205$$

$$\frac{\sigma}{\sigma_{max}} = 0,43$$

$$\sigma = 20000 \text{ kPa}$$

$$\sigma_{max} = \frac{20000}{0,43} \Rightarrow \sigma_{max}: 46512 \text{ kPa}$$

$$V_{s,max} = \sqrt{\frac{\sigma_{max}}{\phi}} = \sqrt{\frac{46512}{1.8}} \Rightarrow V_{s,max} = 161 \text{ m/s}$$

↳ D ground type

$$S = 1,35$$

infusion → D + 0,5L + E

Define Mass Source

Define Elevation Law (50%)

↳ Load case for seismic

Define Bindpattern

FINAL

13/12/23

600 - 9.00 green Park

23/11/23

Wind Loads

- Net Load pattern
- Load Case

30/11/23

Final

- ↳ multiple choice
- ↳ question for exa SAP

Kinematic Interaction \Rightarrow more Optimal

- ↳ true or false