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In [898... import math
import pandas as pd
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In [899... #constants
c = math.pi/180 #conversion factor
g = 9.81 #gravity

#initial conditions

#joint acceleration of ankle throughout entire movement
x_1 = 0
y_1 = 0

#angular velocity segment 1 during 1st interval
w_1 = 0
w_2 = 0
w_3 = 0
w_lb1 = 0
w_a = 0

#segment dimensions
L_1 = 0.48
L_2 = 0.44
L_3 = 0.55
L_lb1 = 0.12
L_a = 0.69

#masses
M = 180 #total
M_b = 300 #bar

M_1 = M*0.043
M_2 = M*0.11
M_3 = M*0.53
M_3 += M*0.07 #adding head to the torso "simplification"
M_b1 = 0
M_a = M*0.049

#proximal distances for each segment
P_1 = 0.4459
P_2 = 0.4095
P_3 = 0.4486
P_lb1 = 0.5
P_a = 0.5280

#moment of inertia for each segment
I_1 = 1/12*M_1*L_1**2
I_2 = 1/12*M_2*L_2**2
I_3 = 1/12*M_3*L_3**2
I_lb1 = 1/12*M_b1*L_lb1**2
I_a = 1/12*M_a*L_a**2
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In [900... #to find angular accelerations and velocities for each segment
class angular_acceleration_velocity:

    #angular acceleration
    def a_i(O__i, O_i, t_i, w_i):
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        return(2*(O__i-O_i)/(t_i**2)-w_i*t_i)

#angular velocity
def w_i(O__i, O_i, a_i):
    return(2*a_i*(O__i-O_i))

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In [901... #to find linear accelerations of joints and segments
class accelerations:

    #general (joint)
    def x__i(x_i, L_i, a_i, w_i, theta): #x__i = x_(i+1)
        return(x_i-L_i*((a_i)*math.sin(theta)+w_i**2*math.cos(theta)))

    def y__i(y_i, L_i, a_i, w_i, theta):
        return(y_i+L_i*((a_i)*math.cos(theta)-w_i**2*math.sin(theta)))

    #general (center of mass)
    def x_c(x_i, P_i, L_i, a_i, w_i, theta):
        return(x_i-(1-P_i)*L_i*((a_i)*math.sin(theta)+w_i**2*math.cos(theta)))

    def y_c(y_i, P_i, L_i, a_i, w_i, theta):
        return(y_i+(1-P_i)*L_i*((a_i)*math.cos(theta)-w_i**2*math.sin(theta)))

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In [902... #to find forces experienced by each segment
class forces:

    def Fx_12(Fx__i,M_i,x_c):
        return(Fx__i - M_i*x_c)

    def Fy_12(Fy__i,M_i,y_c):
        return(Fy__i + M_i*(y_c+g))

    def Fx_3(Fx_lb1,M_3,x_c): #torso+head
        return(Fx_lb1 - M_3*x_c)

    def Fy_3(Fy_lb1,M_3,y_c):
        return(Fy_lb1 + M_3*(y_c+g))

    def Fx_lb1(Fx_a):
        return(Fx_a)

    def Fy_lb1(Fy_a):
        return(Fy_a)

    def Fx_a(Fx_b, M_5, x_c):
        return(Fx_b - M_5*x_c)

    def Fy_a(Fy_b, M_5, y_c):
        return(Fy_b + M_5*(y_c+g))

    def Fx_b(M_b, x_b):
        return(-M_b*x_b)

    def Fy_b(M_b, y_b):
        return(M_b*(y_b+g))

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In [903... #to find moments experienced by each segment
class moments:

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def m_i(m_i, a_i, Fx_i, Fy_i, Fx_i, Fy_i, theta):
    return(m_i-I_a*a_i-Fx_i*P_a*L_a*math.sin(theta)-Fy_i*P_a*L_a*math.cos(theta))

def m_lb1(m_a, I_lb1, a_lb1, Fy_4, P_lb1, L_lb1, theta):
    return(-I_lb1*a_lb1+m_a-Fy_4*(1-P_lb1)*L_lb1*math.cos(theta))

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In [904... *#to find shear and compression forces for the spine*

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class shear_compression:

    def shear(Fx_i, Fy_i, M_i, x_i, y_i, theta):
        shear = abs(Fx_i*math.sin(theta)+Fy_i*math.cos(theta)-M_i*g*math.cos(theta)-(M
        return shear

    def compression(Fx_i, Fy_i, M_i, x_i, y_i, theta):
        compression = abs(Fx_i*math.cos(theta)-Fy_i*math.sin(theta)+M_i*g*math.sin(the
        return compression

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In [905... *#interval 12*

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#inputs
#angle
O_1 = 80*c
O_2 = 209*c
O_3 = 40*c
O_4 = 180*c

#angle'
O__1=88*c
O__2=180*c
O__3=43*c
O__4=180*c

#time
t_i = 0.5

#accelerations (angular and linear)
#segment 1 & joint 2
a_1 = angular_acceleration_velocity.a_i(O__1, O_1, t_i, w_1)
w_1 = angular_acceleration_velocity.w_i(O__1, O_1, a_1)
x_1c = accelerations.x_c(x_1, P_1, L_1, a_1, w_1, O__1)
y_1c = accelerations.y_c(y_1, P_1, L_1, a_1, w_1, O__1)
x_2 = accelerations.x_i(x_1, L_1, a_1, w_1, O__1)
y_2 = accelerations.y_i(y_1, L_1, a_1, w_1, O__1)

#segment 2 & joint 3
a_2 = angular_acceleration_velocity.a_i(O__2, O_2, t_i, w_2)
w_2 = angular_acceleration_velocity.w_i(O__2, O_2, a_2)
x_2c = accelerations.x_c(x_2, P_2, L_2, a_2, w_2, O__2)
y_2c = accelerations.y_c(y_2, P_2, L_2, a_2, w_2, O__2)
x_3 = accelerations.x_i(x_2, L_2, a_2, w_2, O__2)
y_3 = accelerations.y_i(y_2, L_2, a_2, w_2, O__2)

#segment 3 & joint 4
a_3 = angular_acceleration_velocity.a_i(O__3, O_3, t_i, w_3)
w_3 = angular_acceleration_velocity.w_i(O__3, O_3, a_3)
x_3c = accelerations.x_c(x_3, P_3, L_3, a_3, w_3, O__3)
y_3c = accelerations.y_c(y_3, P_3, L_3, a_3, w_3, O__3)
x_lb1 = accelerations.x_i(x_3, L_3, a_3, w_3, O__3)

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y_lb1 = accelerations.y__i(y_3, L_3, a_3, w_3, 0__3)

#segment 4 & joint 5
a_lb1 = 0
w_lb1 = 0

#segment 5 & joint 6
a_4 = angular_acceleration_velocity.a_i(0__4, 0_4, t_i, w_a)
w_a = angular_acceleration_velocity.w_i(0__4, 0_4, a_4)
x_lb1c = accelerations.x_c(x_lb1, P_lb1, L_lb1, a_4, w_a, 0__4)
y_lb1c = accelerations.y_c(y_lb1, P_lb1, L_lb1, a_4, w_a, 0__4)
x_a = accelerations.x__i(x_lb1, L_lb1, a_4, w_a, 0__4)
y_a = accelerations.y__i(y_lb1, L_lb1, a_4, w_a, 0__4)

#the bar
x_b = x_a
y_b = y_a

#forces
Fy_b = forces.Fy_b(M_b, y_b)
Fx_b = forces.Fx_b(M_b, x_b)

Fy_a = forces.Fy_a(Fy_b, M_a, y_a)
Fx_a = forces.Fx_a(Fx_b, M_a, x_a)

Fx_lb1 = Fx_a
Fy_lb1 = Fy_a

Fy_3 = forces.Fy_3(Fy_lb1, M_3, y_3c)
Fx_3 = forces.Fx_3(Fx_lb1, M_3, x_3c)

Fy_2 = forces.Fy_12(Fy_3, M_2, y_2c)
Fx_2 = forces.Fx_12(Fx_3, M_2, x_2c)

Fy_1 = forces.Fy_12(Fy_2, M_1, y_1c)
Fx_1 = forces.Fx_12(Fx_2, M_1, x_1c)

#moments
m_a = moments.m__i(0, a_4, Fx_b, Fy_b, Fx_a, Fy_a, 0__4)

m_lb1 = moments.m_lb1(m_a, I_lb1, a_lb1, Fy_a, P_lb1, L_lb1, 180)

m_3 = moments.m__i(m_lb1, a_3, Fx_3, Fy_3, Fx_lb1, Fy_lb1, 0__3)

m_2 = moments.m__i(m_3, a_2, Fx_3, Fy_3, Fx_2, Fy_2, 0__2)

m_1 = moments.m__i(m_2, a_1, Fx_2, Fy_2, Fx_1, Fy_1, 0__1)

#output
d = {'x_acc':[x_1, x_2, x_3, x_lb1, x_a, x_b], 'y_acc':[y_1, y_2, y_3, y_lb1, y_a, y_b]}

i = ['shank', 'thigh', 'torso', 'shoulder', 'arm', 'bar']

int_12 = pd.DataFrame(d, i)

#compression & shear output for interval 12
spine_c12 = shear_compression.compression(Fx_3, Fy_3, M_3, x_3, y_3, 0__3)

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spine_s12 = shear_compression.shear(Fx_3, Fy_3, M_3, x_3, y_3, O__3)
```

In [906... int_12

Out[906]:

	x_acc	y_acc	x_force	y_force	moment
shank	0.000000	0.000000	-2872.655878	5172.094558	6880.757263
thigh	-0.537468	-0.027963	-2874.960937	5096.285085	5022.967308
torso	6.855079	1.753669	-2799.169891	4881.770094	1583.265763
shoulder	6.697184	1.921439	-2068.224235	3622.902953	2592.196142
arm	6.697184	1.921439	-2068.224235	3622.902953	2462.106377
bar	6.697184	1.921439	-2009.155075	3519.431662	0.000000

In [907...

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#interval 23
#inputs
#angle
O_1 = 88*c
O_2 = 180*c
O_3 = 43*c
O_4 = 180*c

#angle'
O__1=88*c
O__2=173*c
O__3=47*c
O__4=180*c

#time
t_i = 0.4

#accelerations (angular and linear)
#segment 1 & joint 2
a_1 = angular_acceleration_velocity.a_i(O__1, O_1, t_i, w_1)
w_1 = angular_acceleration_velocity.w_i(O__1, O_1, a_1)
x_1c = accelerations.x_c(x_1, P_1, L_1, a_1, w_1, O__1)
y_1c = accelerations.y_c(y_1, P_1, L_1, a_1, w_1, O__1)
x_2 = accelerations.x__i(x_1, L_1, a_1, w_1, O__1)
y_2 = accelerations.y__i(y_1, L_1, a_1, w_1, O__1)

#segment 2 & joint 3
a_2 = angular_acceleration_velocity.a_i(O__2, O_2, t_i, w_2)
w_2 = angular_acceleration_velocity.w_i(O__2, O_2, a_2)
x_2c = accelerations.x_c(x_2, P_2, L_2, a_2, w_2, O__2)
y_2c = accelerations.y_c(y_2, P_2, L_2, a_2, w_2, O__2)
x_3 = accelerations.x__i(x_2, L_2, a_2, w_2, O__2)
y_3 = accelerations.y__i(y_2, L_2, a_2, w_2, O__2)

#segment 3 & joint 4
a_3 = angular_acceleration_velocity.a_i(O__3, O_3, t_i, w_3)
w_3 = angular_acceleration_velocity.w_i(O__3, O_3, a_3)
x_3c = accelerations.x_c(x_3, P_3, L_3, a_3, w_3, O__3)
y_3c = accelerations.y_c(y_3, P_3, L_3, a_3, w_3, O__3)
x_lb1 = accelerations.x__i(x_3, L_3, a_3, w_3, O__3)
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y_lb1 = accelerations.y__i(y_3, L_3, a_3, w_3, 0__3)

#segment 4 & joint 5
a_lb1 = 0
w_lb1 = 0

#segment 5 & joint 6
a_4 = angular_acceleration_velocity.a_i(0__4, 0_4, t_i, w_a)
w_a = angular_acceleration_velocity.w_i(0__4, 0_4, a_4)
x_lb1c = accelerations.x_c(x_lb1, P_lb1, L_lb1, a_4, w_a, 0__4)
y_lb1c = accelerations.y_c(y_lb1, P_lb1, L_lb1, a_4, w_a, 0__4)
x_a = accelerations.x__i(x_lb1, L_lb1, a_4, w_a, 0__4)
y_a = accelerations.y__i(y_lb1, L_lb1, a_4, w_a, 0__4)

#the bar
x_b = x_a
y_b = y_a

#forces
Fy_b = forces.Fy_b(M_b, y_b)
Fx_b = forces.Fx_b(M_b, x_b)

Fy_a = forces.Fy_a(Fy_b, M_a, y_a)
Fx_a = forces.Fx_a(Fx_b, M_a, x_a)

Fx_lb1 = Fx_a
Fy_lb1 = Fy_a

Fy_3 = forces.Fy_3(Fy_lb1, M_3, y_3c)
Fx_3 = forces.Fx_3(Fx_lb1, M_3, x_3c)

Fy_2 = forces.Fy_12(Fy_3, M_2, y_2c)
Fx_2 = forces.Fx_12(Fx_3, M_2, x_2c)

Fy_1 = forces.Fy_12(Fy_2, M_1, y_1c)
Fx_1 = forces.Fx_12(Fx_2, M_1, x_1c)

#moments
m_a = moments.m__i(0, a_4, Fx_b, Fy_b, Fx_a, Fy_a, 0__4)

m_lb1 = moments.m_lb1(m_a, I_lb1, a_lb1, Fy_a, P_lb1, L_lb1, 180)

m_3 = moments.m__i(m_lb1, a_3, Fx_3, Fy_3, Fx_lb1, Fy_lb1, 0__3)

m_2 = moments.m__i(m_3, a_2, Fx_3, Fy_3, Fx_2, Fy_2, 0__2)

m_1 = moments.m__i(m_2, a_1, Fx_2, Fy_2, Fx_1, Fy_1, 0__1)

#output
d = {'x_acc':[x_1, x_2, x_3, x_lb1, x_a, x_b], 'y_acc':[y_1, y_2, y_3, y_lb1, y_a, y_b]}

i = ['shank', 'thigh', 'torso', 'shoulder', 'arm', 'bar']

int_23 = pd.DataFrame(d, i)

#compression & shear output for interval 23
spine_c23 = shear_compression.compression(Fx_3, Fy_3, M_3, x_3, y_3, 0__3)

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spine_s23 = shear_compression.shear(Fx_3, Fy_3, M_3, x_3, y_3, O__3)
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In [908... int_23

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Out[908]:
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	x_acc	y_acc	x_force	y_force	moment
shank	0.000000	0.000000	-82.524812	5053.159143	3870.793841
thigh	0.059854	-0.002090	-82.268115	4977.238707	3934.654283
torso	0.491142	1.348782	-76.040435	4767.247829	594.142361
shoulder	0.141828	1.663802	-43.799204	3543.339548	2535.268326
arm	0.141828	1.663802	-43.799204	3543.339548	2408.035492
bar	0.141828	1.663802	-42.548284	3442.140614	0.000000

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In [909... #interval 34
#inputs
#angle
O_1 = 88*c
O_2 = 173*c
O_3 = 47*c
O_4 = 180*c

#angle'
O__1=88*c
O__2=163*c
O__3=57*c
O__4=180*c

#time
t_i = 1.4

#accelerations (angular and linear)
#segment 1 & joint 2
a_1 = angular_acceleration_velocity.a_i(O__1, O_1, t_i, w_1)
w_1 = angular_acceleration_velocity.w_i(O__1, O_1, a_1)
x_1c = accelerations.x_c(x_1, P_1, L_1, a_1, w_1, O__1)
y_1c = accelerations.y_c(y_1, P_1, L_1, a_1, w_1, O__1)
x_2 = accelerations.x__i(x_1, L_1, a_1, w_1, O__1)
y_2 = accelerations.y__i(y_1, L_1, a_1, w_1, O__1)

#segment 2 & joint 3
a_2 = angular_acceleration_velocity.a_i(O__2, O_2, t_i, w_2)
w_2 = angular_acceleration_velocity.w_i(O__2, O_2, a_2)
x_2c = accelerations.x_c(x_2, P_2, L_2, a_2, w_2, O__2)
y_2c = accelerations.y_c(y_2, P_2, L_2, a_2, w_2, O__2)
x_3 = accelerations.x__i(x_2, L_2, a_2, w_2, O__2)
y_3 = accelerations.y__i(y_2, L_2, a_2, w_2, O__2)

#segment 3 & joint 4
a_3 = angular_acceleration_velocity.a_i(O__3, O_3, t_i, w_3)
w_3 = angular_acceleration_velocity.w_i(O__3, O_3, a_3)
x_3c = accelerations.x_c(x_3, P_3, L_3, a_3, w_3, O__3)
y_3c = accelerations.y_c(y_3, P_3, L_3, a_3, w_3, O__3)
x_lb1 = accelerations.x__i(x_3, L_3, a_3, w_3, O__3)
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y_lb1 = accelerations.y__i(y_3, L_3, a_3, w_3, 0__3)

#segment 4 & joint 5
a_lb1 = 0
w_lb1 = 0

#segment 5 & joint 6
a_4 = angular_acceleration_velocity.a_i(0__4, 0_4, t_i, w_a)
w_a = angular_acceleration_velocity.w_i(0__4, 0_4, a_4)
x_lb1c = accelerations.x_c(x_lb1, P_lb1, L_lb1, a_4, w_a, 0__4)
y_lb1c = accelerations.y_c(y_lb1, P_lb1, L_lb1, a_4, w_a, 0__4)
x_a = accelerations.x__i(x_lb1, L_lb1, a_4, w_a, 0__4)
y_a = accelerations.y__i(y_lb1, L_lb1, a_4, w_a, 0__4)

#the bar
x_b = x_a
y_b = y_a

#forces
Fy_b = forces.Fy_b(M_b, y_b)
Fx_b = forces.Fx_b(M_b, x_b)

Fy_a = forces.Fy_a(Fy_b, M_a, y_a)
Fx_a = forces.Fx_a(Fx_b, M_a, x_a)

Fx_lb1 = Fx_a
Fy_lb1 = Fy_a

Fy_3 = forces.Fy_3(Fy_lb1, M_3, y_3c)
Fx_3 = forces.Fx_3(Fx_lb1, M_3, x_3c)

Fy_2 = forces.Fy_12(Fy_3, M_2, y_2c)
Fx_2 = forces.Fx_12(Fx_3, M_2, x_2c)

Fy_1 = forces.Fy_12(Fy_2, M_1, y_1c)
Fx_1 = forces.Fx_12(Fx_2, M_1, x_1c)

#moments
m_a = moments.m__i(0, a_4, Fx_b, Fy_b, Fx_a, Fy_a, 0__4)

m_lb1 = moments.m_lb1(m_a, I_lb1, a_lb1, Fy_a, P_lb1, L_lb1, 180)

m_3 = moments.m__i(m_lb1, a_3, Fx_3, Fy_3, Fx_lb1, Fy_lb1, 0__3)

m_2 = moments.m__i(m_3, a_2, Fx_3, Fy_3, Fx_2, Fy_2, 0__2)

m_1 = moments.m__i(m_2, a_1, Fx_2, Fy_2, Fx_1, Fy_1, 0__1)

#output
d = {'x_acc':[x_1, x_2, x_3, x_lb1, x_a, x_b], 'y_acc':[y_1, y_2, y_3, y_lb1, y_a, y_b]}

i = ['shank', 'thigh', 'torso', 'shoulder', 'arm', 'bar']

int_34 = pd.DataFrame(d, i)

#compression & shear output for interval 34
spine_c34 = shear_compression.compression(Fx_3, Fy_3, M_3, x_3, y_3, 0__3)

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spine_s34 = shear_compression.shear(Fx_3, Fy_3, M_3, x_3, y_3, O__3)
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In [910]: int_34
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Out[910]:
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	x_acc	y_acc	x_force	y_force	moment
shank	0.000000	0.000000	-102.630039	4577.125430	3794.804307
thigh	0.000000	0.000000	-102.630039	4501.196030	3833.287476
torso	0.243845	0.505818	-99.779030	4301.044051	912.063204
shoulder	0.238795	0.509089	-73.744543	3186.740919	2280.121114
arm	0.238795	0.509089	-73.744543	3186.740919	2165.692882
bar	0.238795	0.509089	-71.638374	3095.726558	0.000000

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In [911]: #interval 45
#inputs
#angle
O_1 = 88*c
O_2 = 163*c
O_3 = 57*c
O_4 = 180*c

#angle'
O__1=88*c
O__2=140*c
O__3=79*c
O__4=180*c

#time
t_i = 0.4

#accelerations (angular and linear)
#segment 1 & joint 2
a_1 = angular_acceleration_velocity.a_i(O__1, O_1, t_i, w_1)
w_1 = angular_acceleration_velocity.w_i(O__1, O_1, a_1)
x_1c = accelerations.x_c(x_1, P_1, L_1, a_1, w_1, O__1)
y_1c = accelerations.y_c(y_1, P_1, L_1, a_1, w_1, O__1)
x_2 = accelerations.x__i(x_1, L_1, a_1, w_1, O__1)
y_2 = accelerations.y__i(y_1, L_1, a_1, w_1, O__1)

#segment 2 & joint 3
a_2 = angular_acceleration_velocity.a_i(O__2, O_2, t_i, w_2)
w_2 = angular_acceleration_velocity.w_i(O__2, O_2, a_2)
x_2c = accelerations.x_c(x_2, P_2, L_2, a_2, w_2, O__2)
y_2c = accelerations.y_c(y_2, P_2, L_2, a_2, w_2, O__2)
x_3 = accelerations.x__i(x_2, L_2, a_2, w_2, O__2)
y_3 = accelerations.y__i(y_2, L_2, a_2, w_2, O__2)

#segment 3 & joint 4
a_3 = angular_acceleration_velocity.a_i(O__3, O_3, t_i, w_3)
w_3 = angular_acceleration_velocity.w_i(O__3, O_3, a_3)
x_3c = accelerations.x_c(x_3, P_3, L_3, a_3, w_3, O__3)
y_3c = accelerations.y_c(y_3, P_3, L_3, a_3, w_3, O__3)
x_lb1 = accelerations.x__i(x_3, L_3, a_3, w_3, O__3)
```

```

y_lb1 = accelerations.y__i(y_3, L_3, a_3, w_3, 0__3)

#segment 4 & joint 5
a_lb1 = 0
w_lb1 = 0

#segment 5 & joint 6
a_4 = angular_acceleration_velocity.a_i(0__4, 0_4, t_i, w_a)
w_a = angular_acceleration_velocity.w_i(0__4, 0_4, a_4)
x_lb1c = accelerations.x_c(x_lb1, P_lb1, L_lb1, a_4, w_a, 0__4)
y_lb1c = accelerations.y_c(y_lb1, P_lb1, L_lb1, a_4, w_a, 0__4)
x_a = accelerations.x__i(x_lb1, L_lb1, a_4, w_a, 0__4)
y_a = accelerations.y__i(y_lb1, L_lb1, a_4, w_a, 0__4)

#the bar
x_b = x_a
y_b = y_a

#forces
Fy_b = forces.Fy_b(M_b, y_b)
Fx_b = forces.Fx_b(M_b, x_b)

Fy_a = forces.Fy_a(Fy_b, M_a, y_a)
Fx_a = forces.Fx_a(Fx_b, M_a, x_a)

Fx_lb1 = Fx_a
Fy_lb1 = Fy_a

Fy_3 = forces.Fy_3(Fy_lb1, M_3, y_3c)
Fx_3 = forces.Fx_3(Fx_lb1, M_3, x_3c)

Fy_2 = forces.Fy_12(Fy_3, M_2, y_2c)
Fx_2 = forces.Fx_12(Fx_3, M_2, x_2c)

Fy_1 = forces.Fy_12(Fy_2, M_1, y_1c)
Fx_1 = forces.Fx_12(Fx_2, M_1, x_1c)

#moments
m_a = moments.m__i(0, a_4, Fx_b, Fy_b, Fx_a, Fy_a, 0__4)

m_lb1 = moments.m_lb1(m_a, I_lb1, a_lb1, Fy_a, P_lb1, L_lb1, 180)

m_3 = moments.m__i(m_lb1, a_3, Fx_3, Fy_3, Fx_lb1, Fy_lb1, 0__3)

m_2 = moments.m__i(m_3, a_2, Fx_3, Fy_3, Fx_2, Fy_2, 0__2)

m_1 = moments.m__i(m_2, a_1, Fx_2, Fy_2, Fx_1, Fy_1, 0__1)

#output
d = {'x_acc':[x_1, x_2, x_3, x_lb1, x_a, x_b], 'y_acc':[y_1, y_2, y_3, y_lb1, y_a, y_b]}

i = ['shank', 'thigh', 'torso', 'shoulder', 'arm', 'bar']

int_45= pd.DataFrame(d, i)

#compression & shear output for interval 45
spine_c45 = shear_compression.compression(Fx_3, Fy_3, M_3, x_3, y_3, 0__3)

```

```
spine_s45 = shear_compression.shear(Fx_3, Fy_3, M_3, x_3, y_3, O__3)
```

In [912... int_45

Out[912]:

	x_acc	y_acc	x_force	y_force	moment
shank	0.000000	0.000000	-1661.856217	487.220934	2862.035566
thigh	0.000000	0.000000	-1661.856217	411.291534	1726.820490
torso	7.329984	-3.167293	-1576.154777	254.085210	834.477683
shoulder	3.314662	-9.993907	-1023.633775	-56.794091	-40.636314
arm	3.314662	-9.993907	-1023.633775	-56.794091	-38.596975
bar	3.314662	-9.993907	-994.398460	-55.172033	0.000000

In [913...

```
#interval 56
#inputs
#angle
O_1 = 88*c
O_2 = 140*c
O_3 = 79*c
O_4 = 180*c

#angle'
O__1=88*c
O__2=125*c
O__3=84*c
O__4=180*c

#time
t_i = 0.4

#accelerations (angular and linear)
#segment 1 & joint 2
a_1 = angular_acceleration_velocity.a_i(O__1, O_1, t_i, w_1)
w_1 = angular_acceleration_velocity.w_i(O__1, O_1, a_1)
x_1c = accelerations.x_c(x_1, P_1, L_1, a_1, w_1, O__1)
y_1c = accelerations.y_c(y_1, P_1, L_1, a_1, w_1, O__1)
x_2 = accelerations.x__i(x_1, L_1, a_1, w_1, O__1)
y_2 = accelerations.y__i(y_1, L_1, a_1, w_1, O__1)

#segment 2 & joint 3
a_2 = angular_acceleration_velocity.a_i(O__2, O_2, t_i, w_2)
w_2 = angular_acceleration_velocity.w_i(O__2, O_2, a_2)
x_2c = accelerations.x_c(x_2, P_2, L_2, a_2, w_2, O__2)
y_2c = accelerations.y_c(y_2, P_2, L_2, a_2, w_2, O__2)
x_3 = accelerations.x__i(x_2, L_2, a_2, w_2, O__2)
y_3 = accelerations.y__i(y_2, L_2, a_2, w_2, O__2)

#segment 3 & joint 4
a_3 = angular_acceleration_velocity.a_i(O__3, O_3, t_i, w_3)
w_3 = angular_acceleration_velocity.w_i(O__3, O_3, a_3)
x_3c = accelerations.x_c(x_3, P_3, L_3, a_3, w_3, O__3)
y_3c = accelerations.y_c(y_3, P_3, L_3, a_3, w_3, O__3)
x_lb1 = accelerations.x__i(x_3, L_3, a_3, w_3, O__3)
```

```

y_lb1 = accelerations.y__i(y_3, L_3, a_3, w_3, 0__3)

#segment 4 & joint 5
a_lb1 = 0
w_lb1 = 0

#segment 5 & joint 6
a_a = angular_acceleration_velocity.a_i(0__4, 0_4, t_i, w_a)
w_a = angular_acceleration_velocity.w_i(0__4, 0_4, a_a)
x_lb1c = accelerations.x_c(x_lb1, P_lb1, L_lb1, a_4, w_a, 0__4)
y_lb1c = accelerations.y_c(y_lb1, P_lb1, L_lb1, a_4, w_a, 0__4)
x_a = accelerations.x__i(x_lb1, L_lb1, a_4, w_a, 0__4)
y_a = accelerations.y__i(y_lb1, L_lb1, a_4, w_a, 0__4)

#the bar
x_b = x_a
y_b = y_a

#forces
Fy_b = forces.Fy_b(M_b, y_b)
Fx_b = forces.Fx_b(M_b, x_b)

Fy_a = forces.Fy_a(Fy_b, M_a, y_a)
Fx_a = forces.Fx_a(Fx_b, M_a, x_a)

Fx_lb1 = Fx_a
Fy_lb1 = Fy_a

Fy_3 = forces.Fy_3(Fy_lb1, M_3, y_3c)
Fx_3 = forces.Fx_3(Fx_lb1, M_3, x_3c)

Fy_2 = forces.Fy_12(Fy_3, M_2, y_2c)
Fx_2 = forces.Fx_12(Fx_3, M_2, x_2c)

Fy_1 = forces.Fy_12(Fy_2, M_1, y_1c)
Fx_1 = forces.Fx_12(Fx_2, M_1, x_1c)

#moments
m_a = moments.m__i(0, a_4, Fx_b, Fy_b, Fx_a, Fy_a, 0__4)

m_lb1 = moments.m_lb1(m_a, I_lb1, a_lb1, Fy_a, P_lb1, L_lb1, 180)

m_3 = moments.m__i(m_lb1, a_3, Fx_3, Fy_3, Fx_lb1, Fy_lb1, 0__3)

m_2 = moments.m__i(m_3, a_2, Fx_3, Fy_3, Fx_2, Fy_2, 0__2)

m_1 = moments.m__i(m_2, a_1, Fx_2, Fy_2, Fx_1, Fy_1, 0__1)

#output
d = {'x_acc':[x_1, x_2, x_3, x_lb1, x_a, x_b], 'y_acc':[y_1, y_2, y_3, y_lb1, y_a, y_b]}

i = ['shank', 'thigh', 'torso', 'shoulder', 'arm', 'bar']

int_56= pd.DataFrame(d, i)

#compression & shear output for interval 56
spine_c56 = shear_compression.compression(Fx_3, Fy_3, M_3, x_3, y_3, 0__3)

```

```
spine_s56 = shear_compression.shear(Fx_3, Fy_3, M_3, x_3, y_3, O__3)
```

In [914... int_56

Out[914]:

	x_acc	y_acc	x_force	y_force	moment
shank	0.000000	0.000000	-1563.803225	3850.935771	5913.692528
thigh	0.000000	0.000000	-1563.803225	3775.006371	4927.093251
torso	3.469486	-1.165016	-1523.238348	3594.389618	2597.302331
shoulder	3.678751	-1.189482	-1136.071898	2662.188320	1904.802414
arm	3.678751	-1.189482	-1136.071898	2662.188320	1809.209610
bar	3.678751	-1.189482	-1103.625314	2586.155353	0.000000

In [915...

```
#interval 67
#inputs
#angle
O_1 = 88*c
O_2 = 125*c
O_3 = 84*c
O_4 = 180*c

#angle'
O__1=90*c
O__2=90*c
O__3=90*c
O__4=180*c

#time
t_i = 0.6

#accelerations (angular and linear)
#segment 1 & joint 2
a_1 = angular_acceleration_velocity.a_i(O__1, O_1, t_i, w_1)
w_1 = angular_acceleration_velocity.w_i(O__1, O_1, a_1)
x_1c = accelerations.x_c(x_1, P_1, L_1, a_1, w_1, O__1)
y_1c = accelerations.y_c(y_1, P_1, L_1, a_1, w_1, O__1)
x_2 = accelerations.x_i(x_1, L_1, a_1, w_1, O__1)
y_2 = accelerations.y_i(y_1, L_1, a_1, w_1, O__1)

#segment 2 & joint 3
a_2 = angular_acceleration_velocity.a_i(O__2, O_2, t_i, w_2)
w_2 = angular_acceleration_velocity.w_i(O__2, O_2, a_2)
x_2c = accelerations.x_c(x_2, P_2, L_2, a_2, w_2, O__2)
y_2c = accelerations.y_c(y_2, P_2, L_2, a_2, w_2, O__2)
x_3 = accelerations.x_i(x_2, L_2, a_2, w_2, O__2)
y_3 = accelerations.y_i(y_2, L_2, a_2, w_2, O__2)

#segment 3 & joint 4
a_3 = angular_acceleration_velocity.a_i(O__3, O_3, t_i, w_3)
w_3 = angular_acceleration_velocity.w_i(O__3, O_3, a_3)
x_3c = accelerations.x_c(x_3, P_3, L_3, a_3, w_3, O__3)
y_3c = accelerations.y_c(y_3, P_3, L_3, a_3, w_3, O__3)
x_lb1 = accelerations.x_i(x_3, L_3, a_3, w_3, O__3)
```

```

y_lb1 = accelerations.y__i(y_3, L_3, a_3, w_3, 0__3)

#segment 4 & joint 5
a_lb1 = 0
w_lb1 = 0

#segment 5 & joint 6
a_a = angular_acceleration_velocity.a_i(0__4, 0_4, t_i, w_a)
w_a = angular_acceleration_velocity.w_i(0__4, 0_4, a_a)
x_lb1c = accelerations.x_c(x_lb1, P_lb1, L_lb1, a_4, w_a, 0__4)
y_lb1c = accelerations.y_c(y_lb1, P_lb1, L_lb1, a_4, w_a, 0__4)
x_a = accelerations.x__i(x_lb1, L_lb1, a_4, w_a, 0__4)
y_a = accelerations.y__i(y_lb1, L_lb1, a_4, w_a, 0__4)

#the bar
x_b = x_a
y_b = y_a

#forces
Fy_b = forces.Fy_b(M_b, y_b)
Fx_b = forces.Fx_b(M_b, x_b)

Fy_a = forces.Fy_a(Fy_b, M_a, y_a)
Fx_a = forces.Fx_a(Fx_b, M_a, x_a)

Fx_lb1 = Fx_a
Fy_lb1 = Fy_a

Fy_3 = forces.Fy_3(Fy_lb1, M_3, y_3c)
Fx_3 = forces.Fx_3(Fx_lb1, M_3, x_3c)

Fy_2 = forces.Fy_12(Fy_3, M_2, y_2c)
Fx_2 = forces.Fx_12(Fx_3, M_2, x_2c)

Fy_1 = forces.Fy_12(Fy_2, M_1, y_1c)
Fx_1 = forces.Fx_12(Fx_2, M_1, x_1c)

#moments
m_a = moments.m__i(0, a_4, Fx_b, Fy_b, Fx_a, Fy_a, 0__4)

m_lb1 = moments.m_lb1(m_a, I_lb1, a_lb1, Fy_a, P_lb1, L_lb1, 180)

m_3 = moments.m__i(m_lb1, a_3, Fx_3, Fy_3, Fx_lb1, Fy_lb1, 0__3)

m_2 = moments.m__i(m_3, a_2, Fx_3, Fy_3, Fx_2, Fy_2, 0__2)

m_1 = moments.m__i(m_2, a_1, Fx_2, Fy_2, Fx_1, Fy_1, 0__1)

#output
d = {'x_acc':[x_1, x_2, x_3, x_lb1, x_a, x_b], 'y_acc':[y_1, y_2, y_3, y_lb1, y_a, y_b]}

i = ['shank', 'thigh', 'torso', 'shoulder', 'arm', 'bar']

int_67= pd.DataFrame(d, i)

#compression & shear output for interval 56
spine_c67 = shear_compression.compression(Fx_3, Fy_3, M_3, x_3, y_3, 0__3)

```

```
spine_s67 = shear_compression.shear(Fx_3, Fy_3, M_3, x_3, y_3, 0__3)
```

In [916... int_67

Out[916]:

	x_acc	y_acc	x_force	y_force	moment
shank	0.000000	0.000000	-765.466715	-2528.262644	110.989419
thigh	-0.093084	-0.000088	-765.865929	-2604.191667	-417.260195
torso	2.083065	-16.064889	-742.265681	-2610.599879	-938.840342
shoulder	1.741026	-16.074219	-537.663533	-1934.516236	-1384.151215
arm	1.741026	-16.074219	-537.663533	-1934.516236	-1314.687372
bar	1.741026	-16.074219	-522.307687	-1879.265821	0.000000

```
In [917... #spine shear and compression output
d = {'Interval 12':[spine_s12, spine_c12], 'Interval 23':[spine_s23, spine_c23], 'Interval 34':[spine_s34, spine_c34], 'Interval 45':[spine_s45, spine_c45], 'Interval 56':[spine_s56, spine_c56], 'Interval 67':[spine_s67, spine_c67]}
i = ['Shear', 'Compression']

shear_compression= pd.DataFrame(d, i)
```

In [918... shear_compression

Out[918]:

	Interval 12	Interval 23	Interval 34	Interval 45	Interval 56	Interval 67
Shear	327.523320	2367.352015	1648.770991	1865.423049	1291.240137	742.265681
Compression	4132.802297	2650.170734	2722.086811	1336.389805	2287.145069	5419.612588