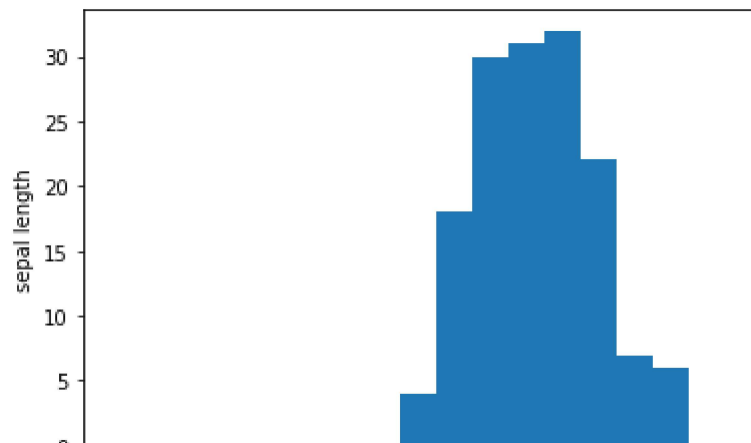




Session 6

▼ Introduction to statistics 1

```
1 import pandas as pd
2 import numpy as np
3 from scipy import stats
4 import matplotlib.pyplot as plt
5 import seaborn as sns
6 %matplotlib inline
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```



```
1 x = df['sepal.length'].values
2 x.dtype

dtype('float64')
```

Sample Mean:

$$\bar{x} = \frac{1}{n} \sum_{i=1}^n x_i$$

```
1 print("Sample-Mean=",sum(i for i in x) / len(x))
2 x_mean = np.mean(x)
3 x_mean
4 print("Sample-Mean=",x_mean)

Sample-Mean= 5.843333333333335
Sample-Mean= 5.843333333333334
```

Sample Variance:

$$Var_x = \frac{1}{n-1} \sum_{i=1}^n (x_i - \bar{x})^2$$

Bessel's correction to correct the bias of the population variance estimate Note the *unit* of the variable is now *unit*²

```
1 print("Sample Variance=",sum([(i - x_mean)**2 for i in x]) / (len(x) - 1))
2 print("Sample Variance=",np.var(x, ddof=1))
```

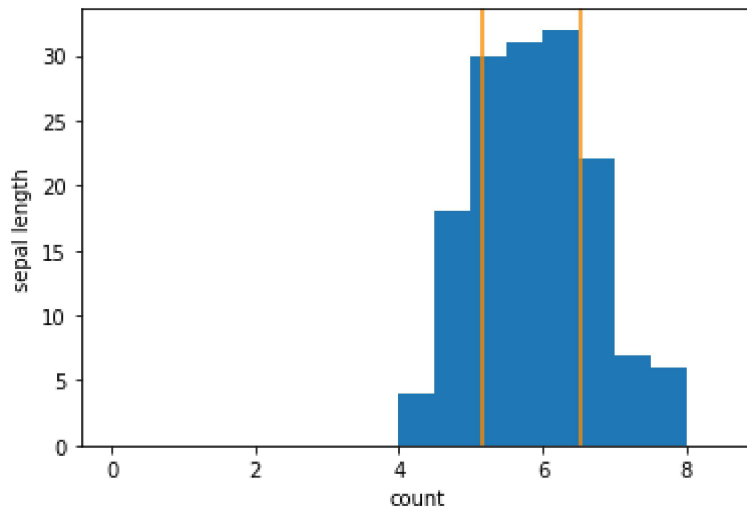
Sample Variance= 0.6856935123042504

Sample Variance= 0.6856935123042507

```
1 var=df['sepal.length'].var()
2 print("Sample Variance= ",df['sepal.length'].var(),) # note that Bessel's correction is the default
```

Sample Variance= 0.6856935123042505

```
1 histo()
2 plt.axvline(x_mean + var, color='darkorange')
3 plt.axvline(x_mean - var, color='darkorange')
4 plt.show()
```



Sample Standard Deviation:

$$Std_x = \sqrt{\frac{1}{n-1} \sum_{i=1}^n (x_i - \bar{x})^2}$$

```
1 print("Standard Deviation=", (sum([(i - x_mean)**2 for i in x]) / (len(x) - 1))**0.5)
2 print("Standard Deviation=", np.sqrt(np.var(x, ddof=1)))
```

```
Standard Deviation= 0.8280661279778628
Standard Deviation= 0.828066127977863
```

```
1 std = np.std(x, ddof=1)
2 std
3 print("Standard Deviation=", std)
4
5 df['sepal.length'].std() # note that Bessel's correction is the default
```

```
Standard Deviation= 0.828066127977863
0.8280661279778629
```

Min/Max:

```
1 #Min/Max:
2 print("Minimum=", np.min(x))
3 print("Maximum=", np.max(x))
```

```
Minimum= 4.3
Maximum= 7.9
```

Mode

```
1 lst = list(x)
2 mode = max(set(lst), key=lst.count)
3 mode
```

```
5.0
```

Count

```
1 lst.count(mode)
```

```
10
```

Mode

```
1 stats.mode(x)
```

```
2
```

```
ModeResult(mode=array([5.]), count=array([10]))
```

25th and 75th Percentile:

```
1 y = np.sort(x)
```

```
2 percentile_25th = y[round(0.25 * y.shape[0]) + 1]
```

```
3 percentile_25th
```

```
5.1
```

```
1 percentile_75th = y[round(0.75 * y.shape[0]) - 1]
```

```
2 percentile_75th
```

```
6.4
```

Using np array 25th and 75th Percentile:

```
1 np.percentile(x, q=[25, 75], interpolation='lower')
```

```
array([5.1, 6.4])
```

```
1 print(df['sepal.length'].quantile(0.25, interpolation='lower'))
```

```
2 print(df['sepal.length'].quantile(0.75, interpolation='lower'))
```

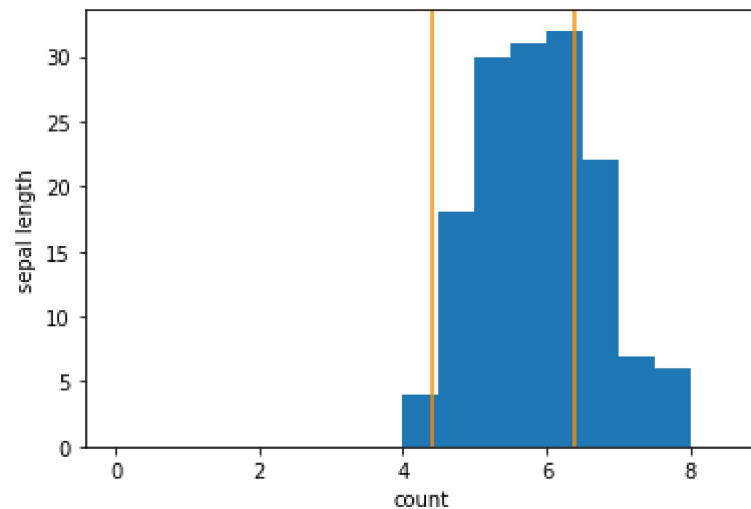
```
5.1
```

6.4

```

1 histo()
2 plt.axvline(percentile_75th, color='darkorange')
3 plt.axvline(percentile_25th - var, color='darkorange')
4 plt.show()
5

```



Median (50th Percentile):

```

1 x = np.sort(x)
2
3 tmp = round(0.5 * x.shape[0])
4
5 if x.shape[0] % 2:
6     median = x[tmp - 1]
7 else:
8     median = x[tmp - 1] + (x[tmp] - x[tmp - 1]) / 2.
9
10 median

```

5.8

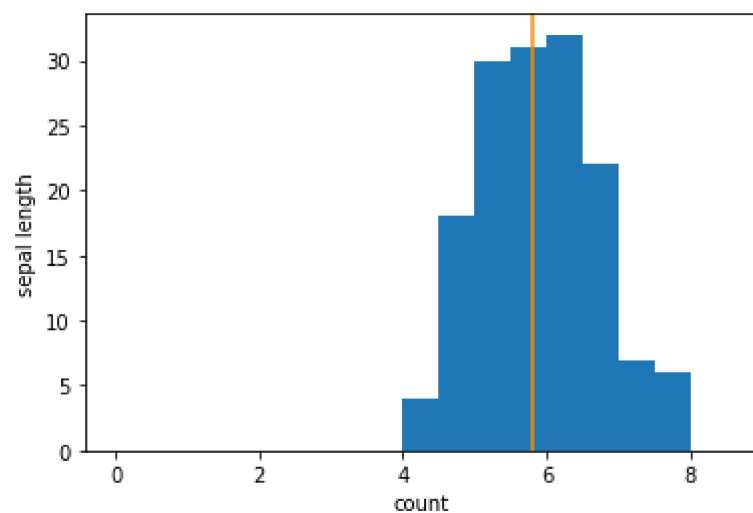
using np

```
1 np.median(x)
```

```
1 histo()
```

```
2 plt.axvline(median, color='darkorange')
```

```
3 plt.show()
```



▼ Box Plot

```
1 # Import libraries
```

```
2 import matplotlib.pyplot as plt
```

```
3 import numpy as np
```

```
4
```

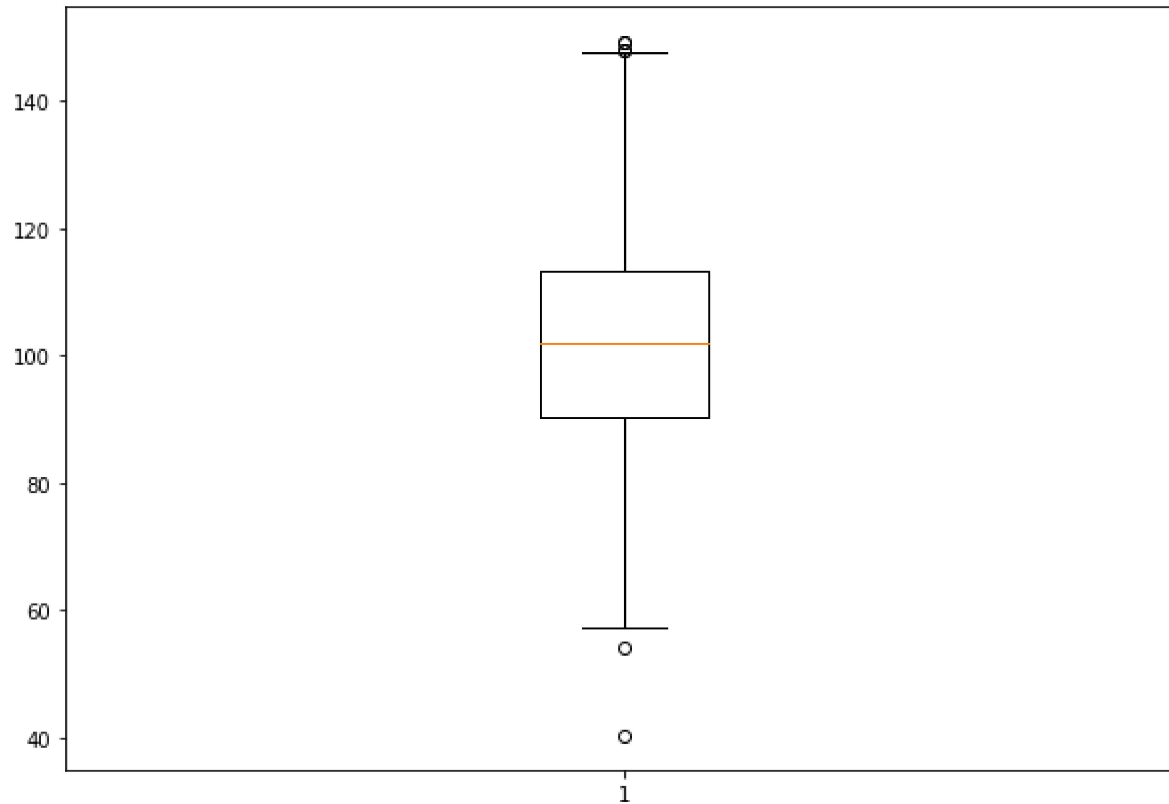
```
5
```

```
6 # Creating dataset
```

```
7 np.random.seed(10)
```

```
8 data = np.random.normal(100, 20, 200)
```

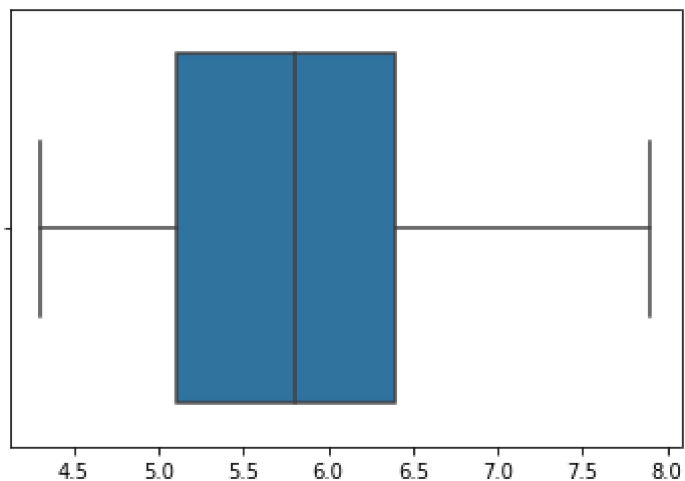
```
9
10 fig = plt.figure(figsize =(10, 7))
11
12 # Creating plot
13 plt.boxplot(data)
14
15 # show plot
16 plt.show()
17
```



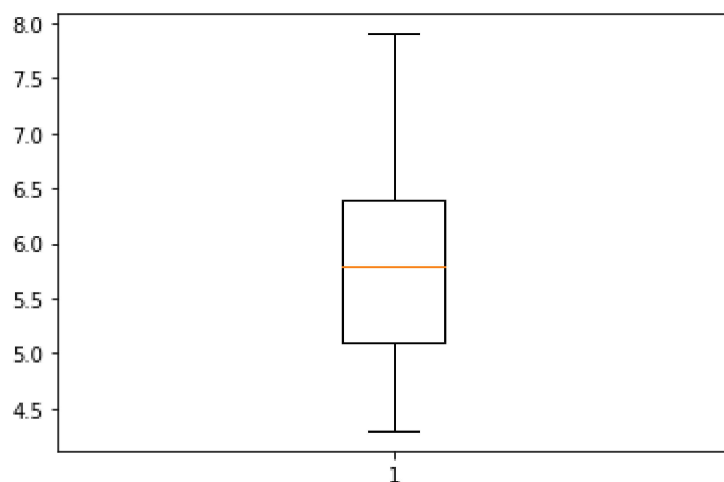
```
1 # Creating plot using seaborn
2
3 sns.boxplot(x)
```



```
/usr/local/lib/python3.7/dist-packages/seaborn/_decorators.py:43: FutureWarning: Pass the following variable as a keyword
FutureWarning
<matplotlib.axes._subplots.AxesSubplot at 0x7fbc622162d0>
```



```
1 # Creating plot using matplotlib
2 plt.boxplot(x)
3
4 # show plot
5 plt.show()
```



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