CSE 201: Data Structures and Algorithms

Lecture 5: Queues Dr. Vidhya Balasubramanian

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Queues

- It is a first-in-first-out abstract data type
- Applications in Real World
 - Transportation
 - Operations Research
 - Acts as buffer in many applications



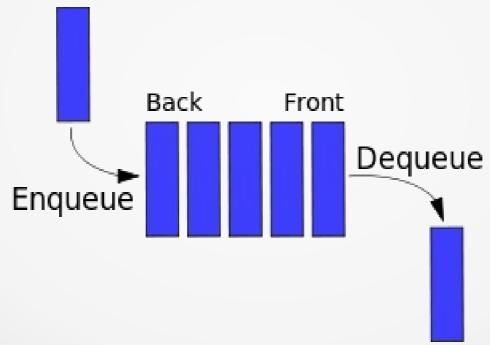




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Queues: An Overview

- Element that is inserted first is removed first
 - Insertions at the rear of the queue and deletions at the front of the queue



http://upload.wikimedia.org/wikipedia/commons/thumb/5/52/Data_Queue.svg/300px-

Data_Queue.svg.png 19CSE 212: Data Structures and Algorithms

Queue ADT: Main Operations

- enqueue(o)
 - Inserts an object o at the end of the queue
 - Input: object; Output: None
- dequeue()
 - Removes and returns the first element in the queue
 - Input: none; Output: object
 - Error occurs if queue is empty

Other Queue Operations

- size()
 - Returns the number of objects in the queue
- isEmpty()
 - Returns a Boolean indicating if the queue is empty
- front()
 - Return first element of the queue without removing it. Error occurs if queue is empty
 - Input: None; Output: Object

Queue Exceptions

- Some operations may cause an error causing an exceptions
- Exceptions in the Queue ADT
 - QueueEmptyException
 - dequeu() and front() cannot be performed if the queue is empty
 - QueueFullException
 - Occurs when the queue has a maximum size limit ie implemented with an array
 - enqueue(o) cannot occur when the queue is full

Queue Example

Operation	Output	Queue Contents
enqueue(5)	-	(5)
enqueue(3)	-	(5,3)
enqueue(7)	-	(5,3,7)
dequeue()	5	(3,7)
size()	2	(3,7)
enqueue(4)	-	(3,7,4)
dequeue()	3	(7,4)
dequeue()	7	(4)
size()	1	(4)
dequeue()	4	0
dequeue()	"error"	0

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Queue Interface (C++)

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```
template <typename Object>
class Queue {
public:
   int size() const: //returns number of objects in the queue
   bool is Empty() //returns true if queue is empty, false otherwise
   Object& front() throw(QueueEmptyException)
      //returns object in the front of the queue, throws exception if
      queue empty
   void enqueue(const Object& obj): //inserts object at rear of
   queue
   Object dequeue() throw(QueueEmptyException)
```

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Queue Interface (Java)

```
public interface Queue<E>
   int size(): //returns number of objects in the queue
   boolean isEmpty() //returns true if queue is empty, false
   otherwise
   E front();
      //returns front object in queue, throws exception if queue
      empty
   void enqueue(E element): //inserts object at rear of queue
   E dequeue();
      //throws(Queue EmptyException)
```

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Queue Interface (Python)

class MyQueue():

def size(self): //returns number of objects in the queue def isEmpty(self) //returns true if queue is empty, false otherwise

def front(self);//returns front object in queue, throws exception if queue empty

def enqueue(self,element): //inserts object at rear of queue def dequeue(self);

//throws(Queue EmptyException)

Exercise

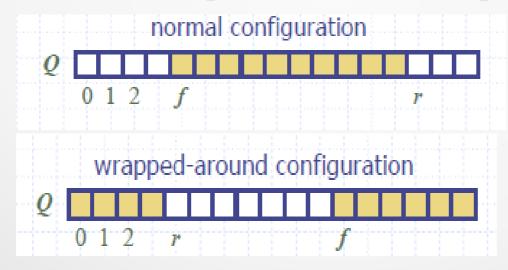
- Describe the output of the following series of queue operations
 - enqueue(5),enqueue(3), dequeue(), enqueue(2), enqueue(8), dequeue(), dequeue(), isEmpty(), enqueue(9), enqueue(1), size(), dequeue(), enqueue(7), enqueue(6), front(), dequeue(), dequeue(), dequeue()
- Show how to implement a queue using two stacks. Analyze the running time of the queue operations.

Array based implementation of a Queue

- A Queue may be implemented by using a simple array
 - An N-element array
 - Queue is limited by the size of the array
 - Two variable to keep track of front and rear
 - Integer f denotes the index of the front element
 - Integer r denotes the position immediately past the rear element
- Strategy
 - Elements are added left to right

Circular Array Implementation

- After repeated enqueue and dequeue operations the rear part may reach end of queue
 - There may be place at the beginning of array
- Circular Queue
 - Allow f and r to wrap around to end of queue



src: Goodrich notes

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Queue ADT Functions

Algorithm size()

return (*N-f+r*) mod *N #may use a variable* __len_ to keep track of size

Algorithm isEmpty()

return (size() == 0) # return (f=r) and (|r-f| = N-1) indicates queue is full

Algorithm front()

if isEmpty() then

throw a QueueEmptyException

return Q[f]

Queue ADT Functions

Algorithm enqueu(o)

$$Q[r] \leftarrow o$$
$$r \leftarrow (r+1) \bmod N$$

Algorithm dequeu()

if isEmpty() then

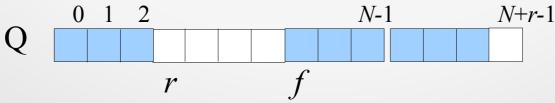
throw a QueueEmptyException

$$o \leftarrow Q[f]$$
$$f \leftarrow (f+1) \bmod N$$

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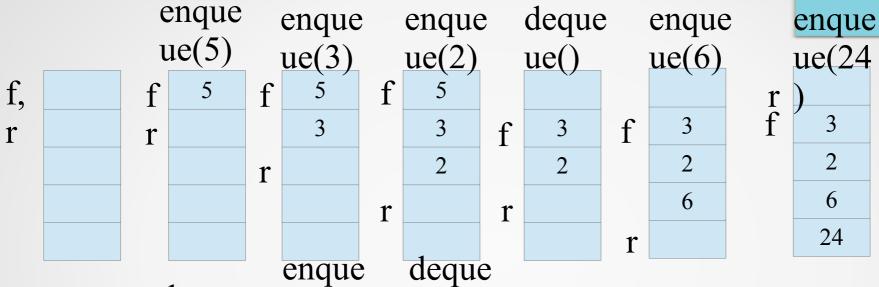
Circular Array

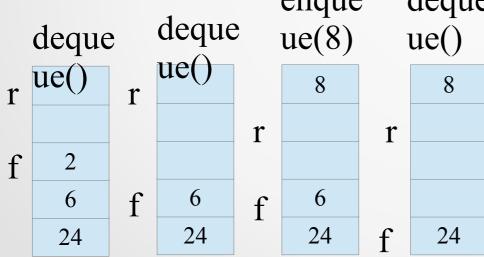
- Size Function
 - size(): return the number $(N f + r) \mod N$
 - If $r \square f$, then $r f \square 0$
 - $N + (r f) \square N$
 - $(N f + r) \mod N = -f + r = r f$
 - If r < f, then f r > 0
 - N f + r = N (f r) < N
 - $(N f + r) \mod N = N f + r$



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Circular Queue: Example





- enqueu(24)
 - $r \leftarrow (r+1) \mod N$
 - $= (4+1) \mod 5 = 0$
- dequeu() (fig 11)
 - $f \leftarrow (f+1) \mod N$
 - $= (4+1) \mod 5 = 0$

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Complexity Analysis

- Time Complexity
 - size O(1)
 - isEmpty O(1)
 - front O(1)
 - enqueue O(1)
 - dequeue O(1)
- Space Complexity
 - -O(N)

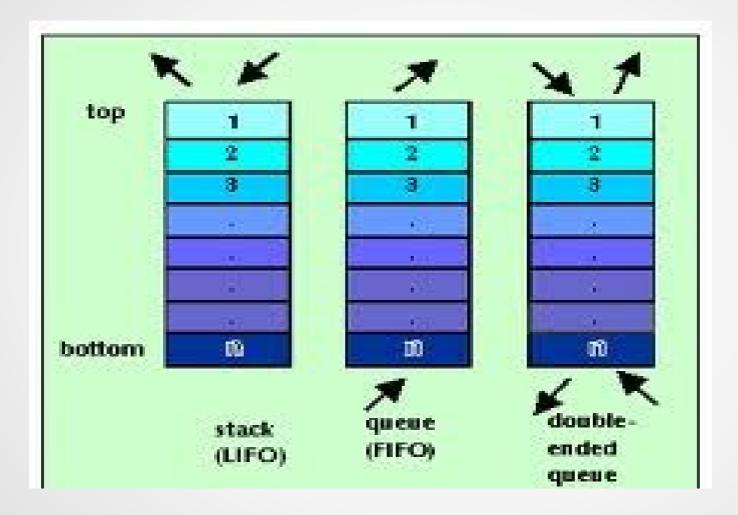
Growable Array-based Queue

- In an enqueue operation, when the array is full, instead of throwing an exception, we can replace the array with a larger one
- Similar to what we did for an array-based stack
- The enqueue operation has amortized running time
 - O(n) with the incremental strategy
 - O(1) with the doubling strategy

Exercises

- Reverse the order of elements in a stack S using one additional queue
- Using additional non-array variables, order all elements on a queue using
 - Two additional queues
 - One additional queue
- Is it possible to keep 2 stacks in a single array, if one grows from position one of the array, and the other grows from the last position. Write a procedure PUSH(x,s) that pushes element x onto stack S, where S is one or the other of these two stacks. Include all necessary error checks.

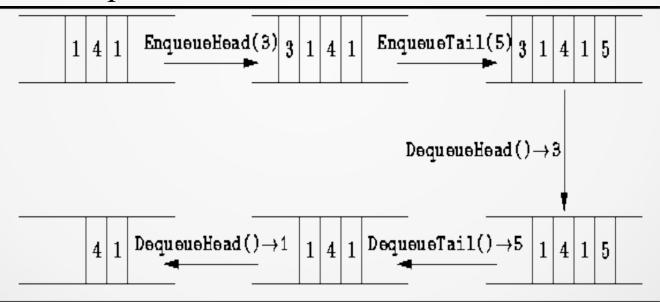
Double-Ended Queue



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Double-Ended Queues

- It is a queue like data structure that supports insertion and deletion at both ends
 - Front and rear of the queue
- Also known as deque



http://www.brpreiss.com/books/opus4/html/img751.gif

Deque Abstract Data Type

- insertFirst(o)
 - Insert a new object o at the beginning of D
 - Input: Object; Output: None
- insertLast(o)
 - Insert a new object o at the end of D
 - Input: Object; Output: None
- RemoveFirst()
 - Remove the first object of D. Error occurs if D is empty
 - Input: None; Output: None
- RemoveLast()
 - Remove the last object of D. Error occurs if D is empty
 - Input: None; Output: None 19CSE 212: Data Structures and Algorithms

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Additional Deque functions

- first()
 - Return first object of D; error occurs if D is empty
 - Input: None; Output: Object
- last()
 - Return last object of D; error occurs if D is empty
 - Input: None; Output: Object
- size()
 - Returns the number of objects in D
- isEmpty()
 - Returns a Boolean indicating if D is empty

Implementation

- Can use a dynamic array
 - uses a variant of a dynamic array that can grow from both ends,
 sometimes called array deques
 - Can also use circular arrays
- Dynamic Arrays
 - Works like regular arrays
 - No limit on size
 - array is discarded and replaced by a bigger array whenever necessary
 - Can use either linear or doubling strategy